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Measurement of $B^0/B_s \rightarrow \pi^0\pi^0$ at CEPC

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2021.01.13

CEPC Physics and Detector Plenary meeting

Outline

- **Brief introduction of B^0 & $B_s \rightarrow \pi^0\pi^0$**
- **Reconstruction of π^0**
- **Separation of B^0 and B_s**
- **Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$**
- **Mixed measurement of $B^0/B_s \rightarrow \pi^0\pi^0$**
- **Summary**

Brief introduction of B^0 & $B_s \rightarrow \pi^0\pi^0$

$B^0 \rightarrow \pi^0\pi^0$

$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ in PDG 2018					Γ_{388}/Γ
VALUE (units 10^{-6})	CL%	DOCUMENT ID	TECN	COMMENT	
1.59 ± 0.26	OUR AVERAGE	Error includes scale factor of 1.4.			
$1.31 \pm 0.19 \pm 0.19$		¹ JULIUS	17	BELL	$e^+e^- \rightarrow \Upsilon(4S)$
$1.83 \pm 0.21 \pm 0.13$		¹ LEES	13D	BABR	$e^+e^- \rightarrow \Upsilon(4S)$

(2017) <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.96.032007>

$B_s \rightarrow \pi^0\pi^0$

Experimental upper limit

$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ in PDG 2018					Γ_{87}/Γ
VALUE	CL%	DOCUMENT ID	TECN	COMMENT	
$<2.1 \times 10^{-4}$	90	¹ ACCIARRI	95H	L3	$e^+e^- \rightarrow Z$
¹ ACCIARRI 95H assumes $f_{B^0} = 39.5 \pm 4.0$ and $f_{B_s} = 12.0 \pm 3.0\%$.					

(1995) <https://www.sciencedirect.com/science/article/pii/0370269395010420>

Theoretical estimation

$\bar{B}_s^0 \rightarrow \pi^+\pi^-$	ann	$0.024^{+0.003+0.025+0.000+0.163}_{-0.003-0.012-0.000-0.021}$	...	$0.57^{+0.16+0.09+0.01}_{-0.13-0.10-0.00}$	<1.36
$\bar{B}_s^0 \rightarrow \pi^0\pi^0$	ann	$0.012^{+0.001+0.013+0.000+0.082}_{-0.001-0.006-0.000-0.011}$	...	$0.28^{+0.08+0.04+0.01}_{-0.07-0.05-0.00}$	<210

(2007) <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.76.074018>

$\sim 3 \times 10^{-7}$

Why choose $B^0/B_s \rightarrow \pi^0\pi^0$?

- Clear dependence on detector and reconstruction performance
 - $\pi^0 \rightarrow \gamma\gamma$, EM object, ECAL performance
 - B_s , b-tagging, background rejection
- CEPC can achieve Tera-Z ($\sim 10^{10}$ Bs) $\gg$ LEP
 - promising to observe this rare decay



ELSEVIER

16 November 1995

Physics Letters B 363 (1995) 127–136

PHYSICS LETTERS B

Search for neutral charmless B decays at LEP

L3 Collaboration

Since no candidate event has been found in data for any of the eight final configurations, upper limits at 90% confidence level have been set using the following numerical values: $N_{\text{had}} = 3\,088\,053$ as the number of Z bosons decaying to hadrons, $\Gamma_b/\Gamma_{\text{had}} = 0.222 \pm 0.003(\text{stat.}) \pm 0.007(\text{syst.})$ as the partial width of Z decays into b quark with respect to the hadronic decays [20], $f(b \rightarrow B_d^0) = 39.5 \pm 4.0\%$ and $f(b \rightarrow B_s^0) = 12.0 \pm 3.0\%$ as the fractions of $B_{d(s)}^0$ produced in the fragmentation of b quarks at LEP, in agreement with the available measurements [21], $\text{Br}(\eta \rightarrow \gamma\gamma) = 38.8\%$ and $\text{Br}(\pi^0 \rightarrow \gamma\gamma) = 98.8\%$ [22]. The errors on

The following results are all based on fast simulation...

Reconstruction of π^0

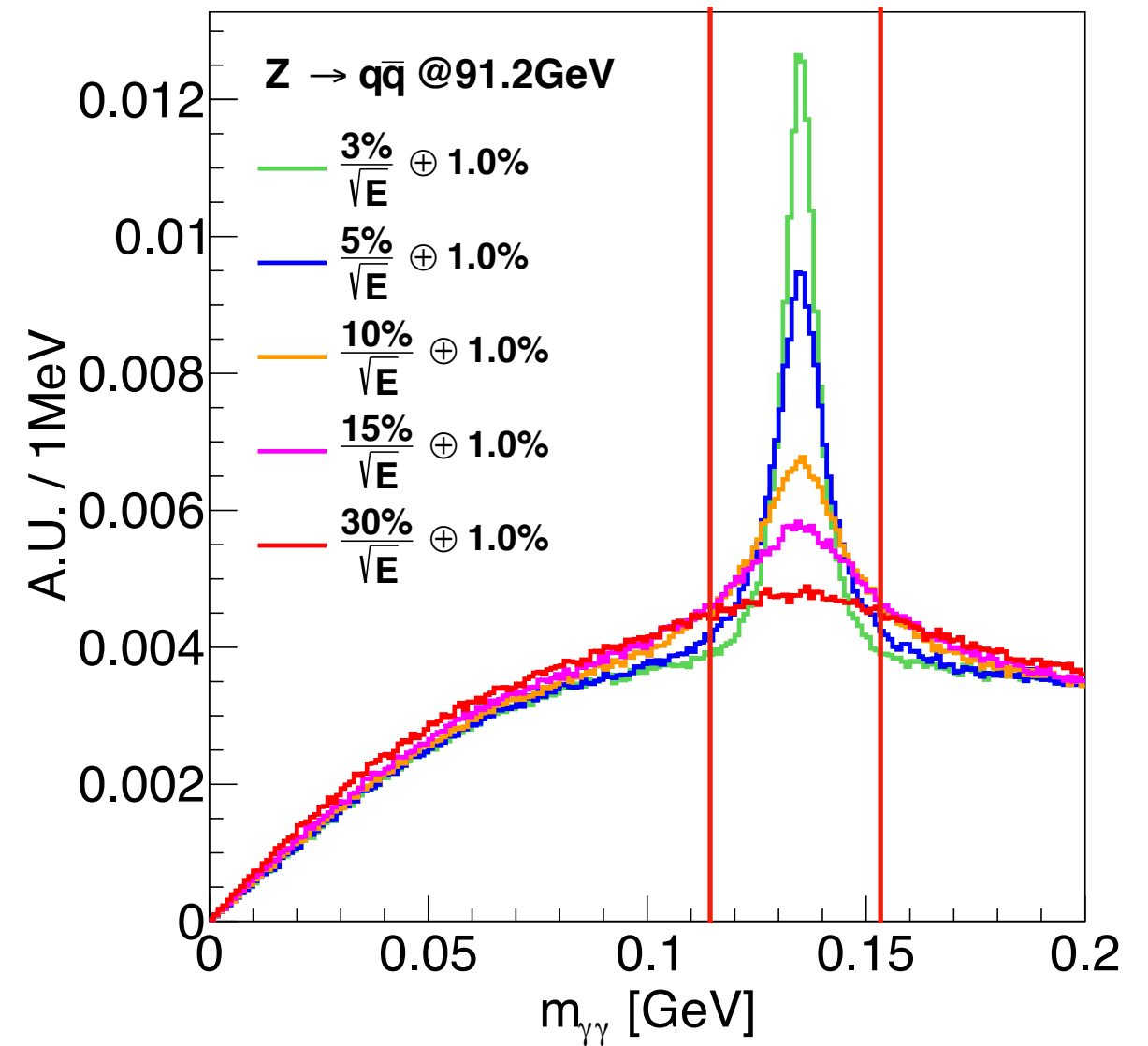
Decay channel: $\pi^0 \rightarrow \gamma\gamma$

Pair up photons and select π^0 candidates according to the invariant mass

Optimize the mass window to get **maximal efficiency $\times$ purity**

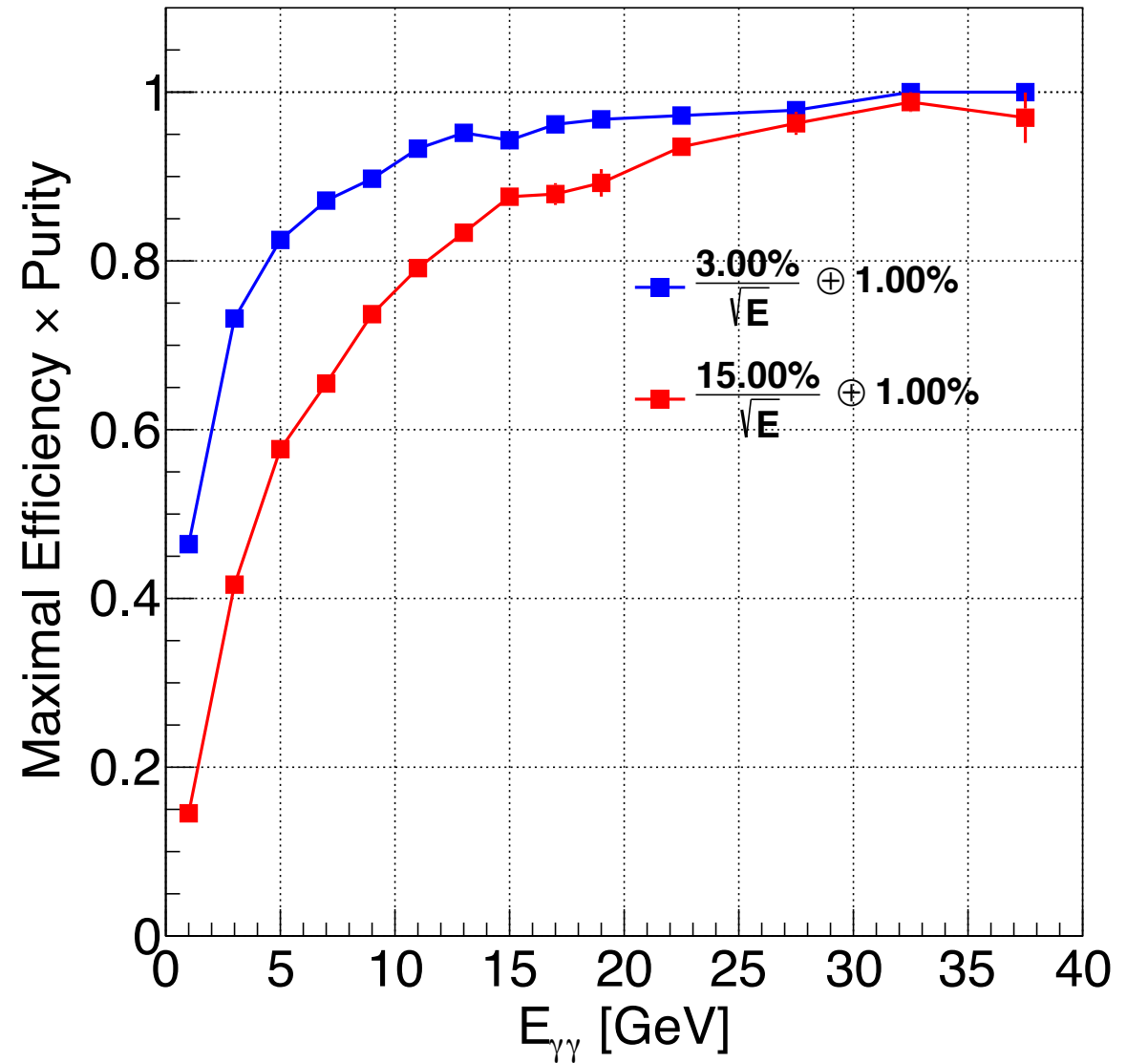
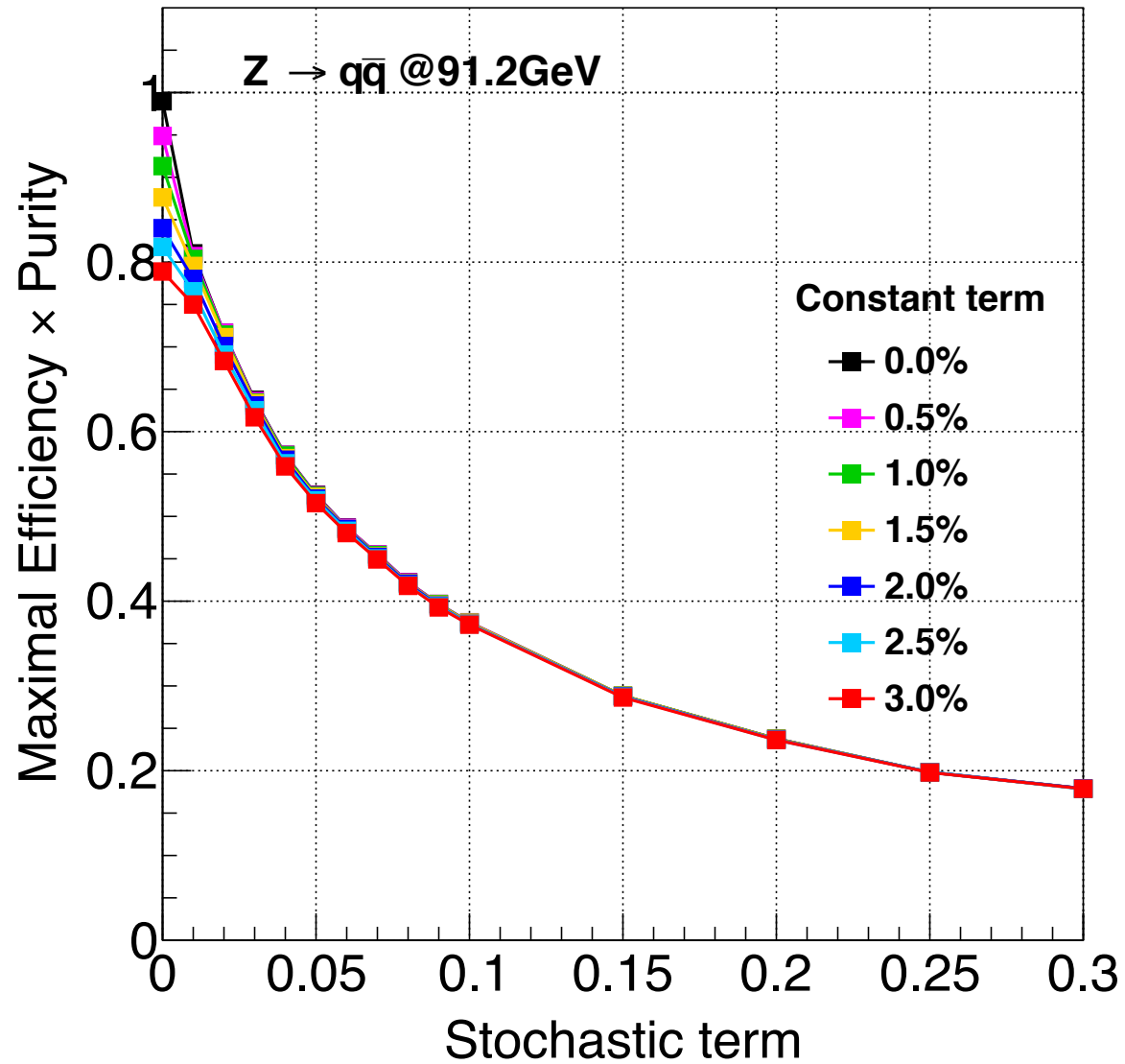
$$\epsilon = \frac{\text{Number of selected } \pi^0 \text{ s that are true } \pi^0 \text{ s in Monte Carlo}}{\text{Number of all generated } \pi^0 \text{ s}}$$

$$p = \frac{\text{Number of selected } \pi^0 \text{ s that are true } \pi^0 \text{ s in Monte Carlo}}{\text{Number of all selected } \pi^0 \text{ s}}$$



Reconstruction of π^0

Maximal efficiency $\times$ purity

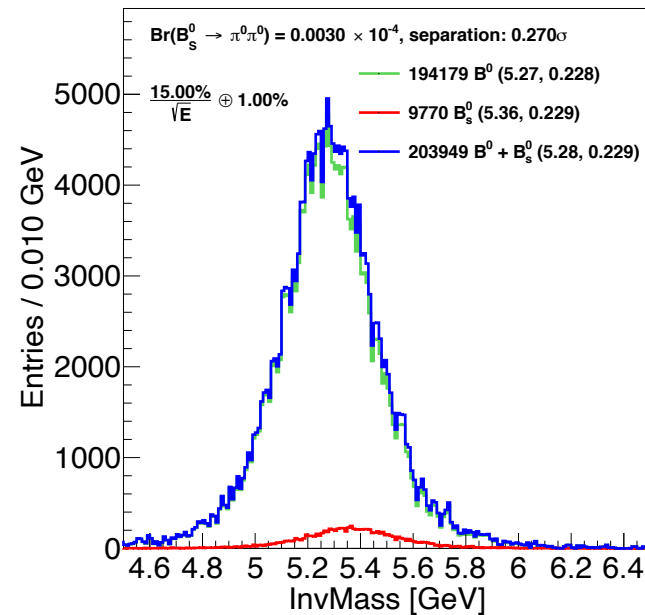
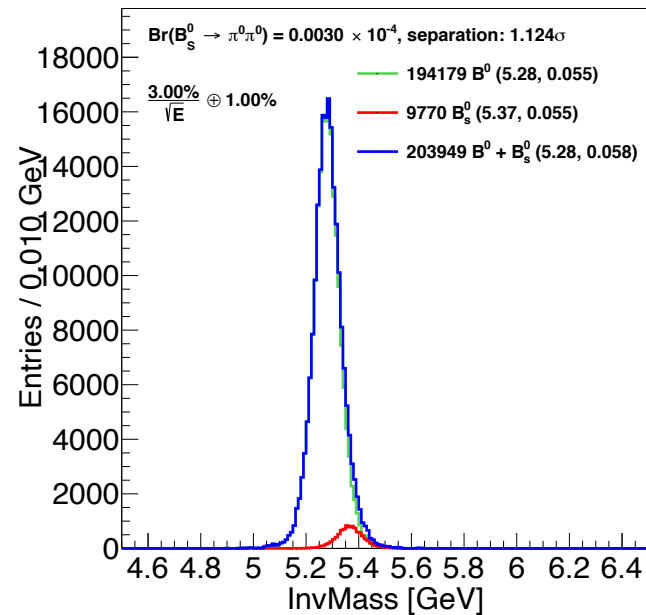
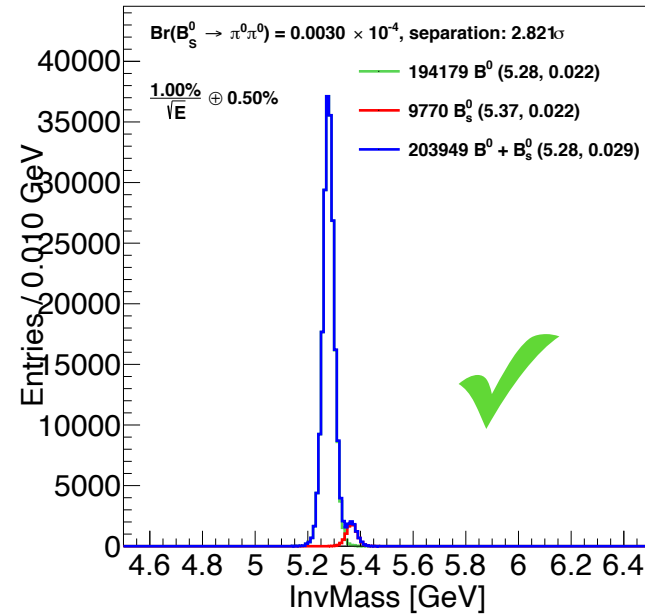
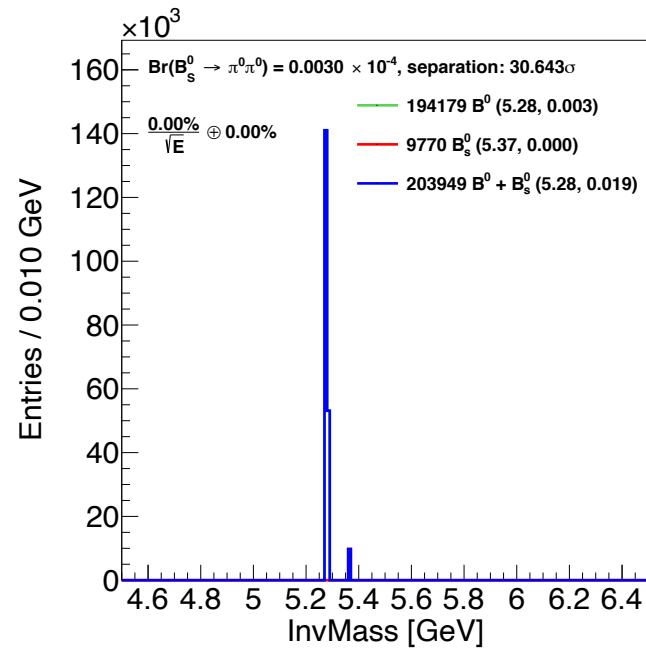


More details in CEPC Note: <http://cepcdoc.ihep.ac.cn/DocDB/0002/000249/002/Pi0FastSimuReco.pdf>

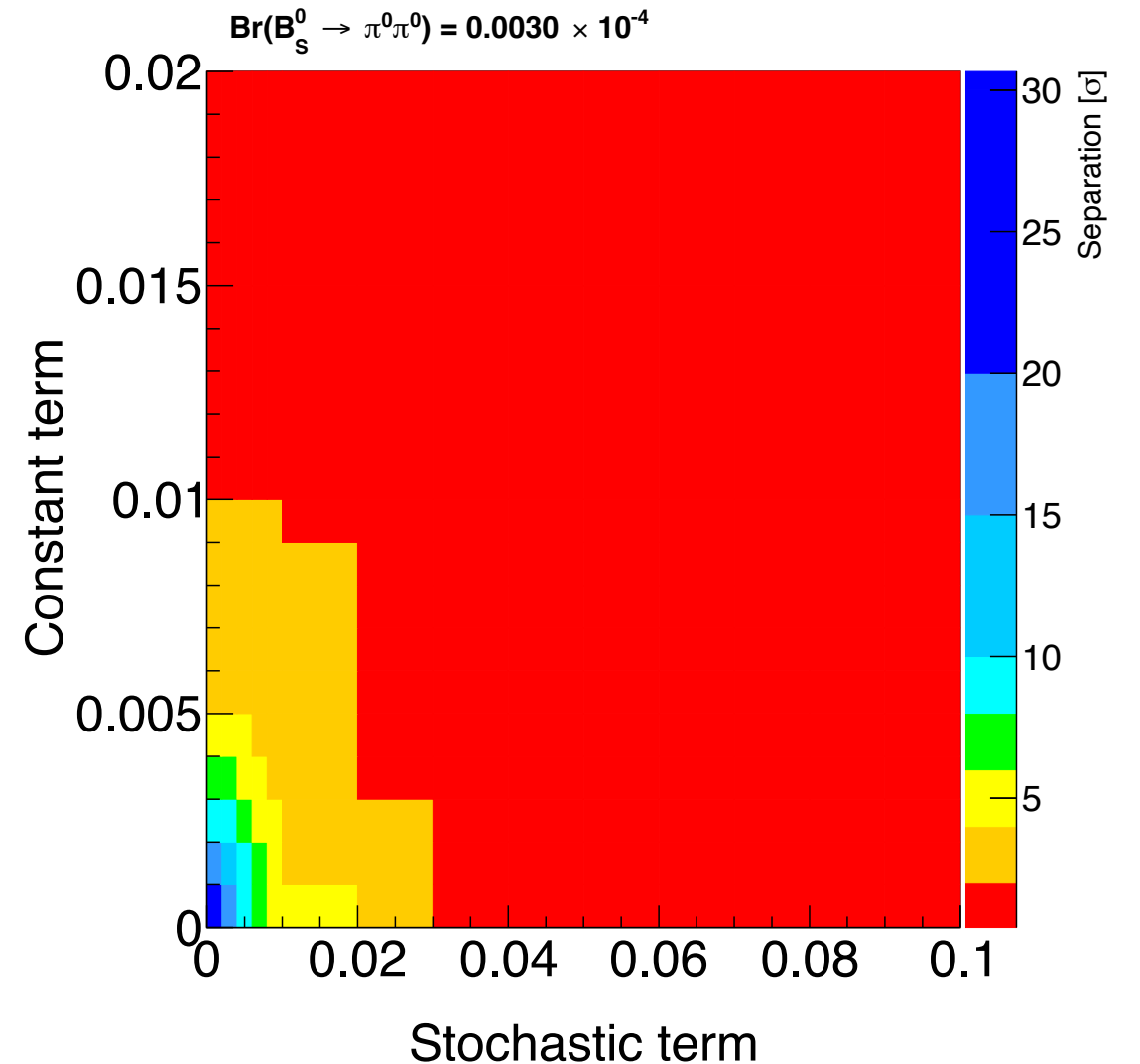
Separation of B^0 and B_s

$$\text{Mass } m_{B^0} = 5279.63 \pm 0.15 \text{ MeV}$$

$$\text{Mass } m_{B_s^0} = 5366.89 \pm 0.19 \text{ MeV}$$

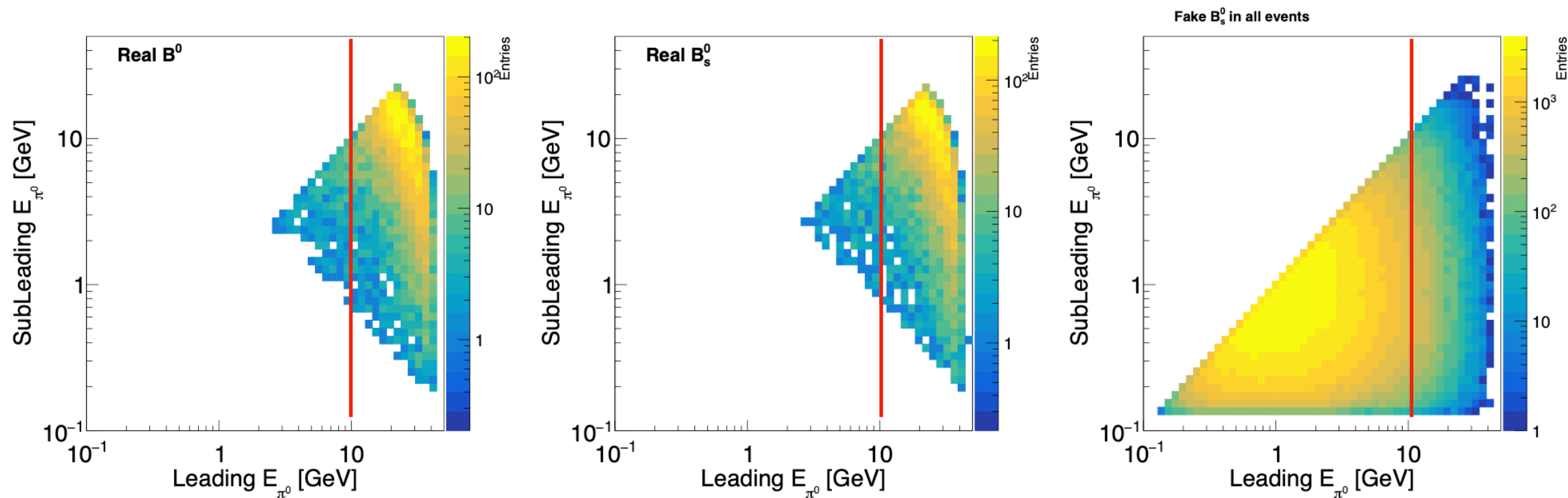


$$\text{separation power} = \frac{|\bar{m}_{B^0} - \bar{m}_{B_s^0}|}{\sqrt{\sigma_{m_{B^0}}^2 + \sigma_{m_{B_s^0}}^2}}$$

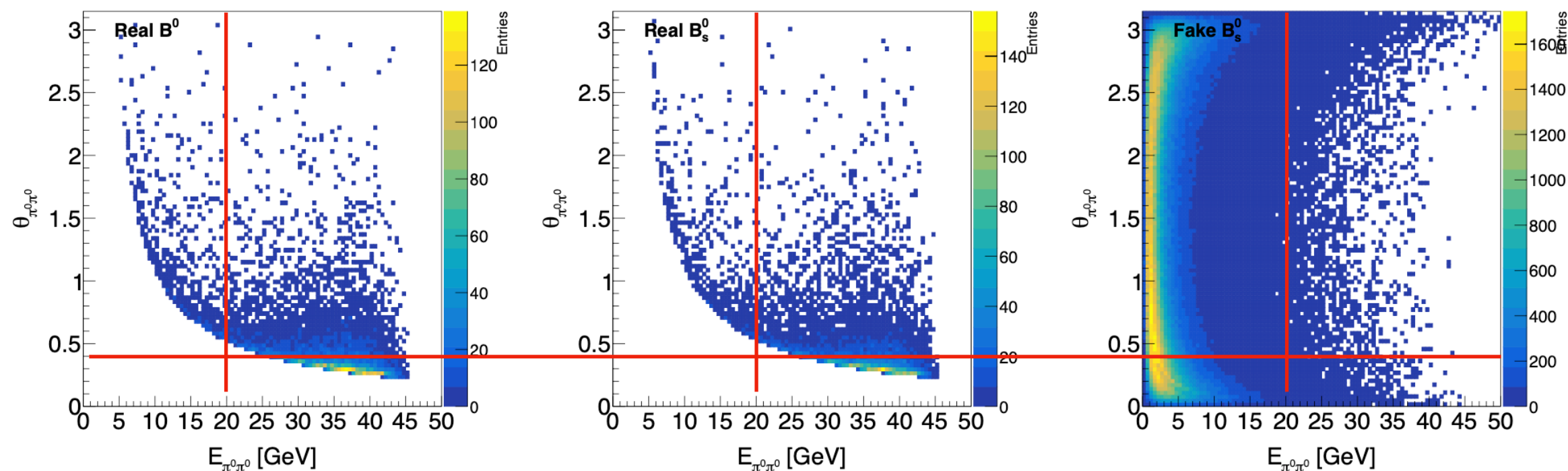


ECAL energy resolution better than $1\%/\sqrt{E} \oplus 0.5\%$ is required.

MCTruth Distribution of $B^0/B_s \rightarrow \pi^0\pi^0$



(a) Energy spectrum of π^0 pairs in $B^0 \rightarrow \pi^0\pi^0$ (left), $B_s^0 \rightarrow \pi^0\pi^0$ (middle), and $Z \rightarrow q\bar{q}$ (right) events.



(b) $\theta_{\pi^0\pi^0}$ vs $E_{\pi^0\pi^0}$ in $B^0 \rightarrow \pi^0\pi^0$ (left), $B_s^0 \rightarrow \pi^0\pi^0$ (middle), and $Z \rightarrow q\bar{q}$ (right) events.

Cut chain

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Table I

Final cuts for all the B_d^0 and B_s^0 decay modes. The (I) and (II) modes refer to the search for a four photon final state, or one with a photon pair for one η and a single cluster for the other one, respectively. “Kinematics” refers to global kinematic variables of the $B_{d(s)}^0$ candidate, “Photons”, “Cluster” and “2nd cluster” to the cuts on purity of photons, single cluster or most energetic π^0 single cluster, if any.

	Cut	$B_{d(s)}^0 \rightarrow \eta\eta$ (I)	$B_{d(s)}^0 \rightarrow \eta\eta$ (II)	$B_{d(s)}^0 \rightarrow \eta\pi^0$	$B_{d(s)}^0 \rightarrow \pi^0\pi^0$
Kinematics	$M_{\gamma\gamma}$ (GeV)	0.51–0.58	0.530–0.564	0.530–0.564	–
	$\cos\theta^*$	0.7	0.775	0.75	0.6
	θ_{mesons}	28°	25°	26°	23°
	Total energy	17.0	27.5	25.0	22.0
Photons	Energy (GeV)	0.3	0.5	1.0	–
	χ_{em}^2	10.0	8.0	8.0	–
	θ_{3D} (mrad)	30.0	50.0	50.0	–
Cluster	Energy (GeV)	–	10.0	13.0	6.0
	χ_{em}^2	–	–	8.0	30.0
	θ_{3D} (mrad)	–	50.0	50.0	40.0
2 nd cluster	Energy (GeV)	–	–	–	14.0
	χ_{em}^2	–	–	–	5.0
	θ_{3D} (mrad)	–	–	–	40.0

As a starting point, just use the values in L3 paper:

π^0 $E_{\text{min}} > 6\text{GeV}$ & $E_{\text{max}} > 14\text{GeV}$ & Total $E > 22\text{GeV}$ & angle $< 23^\circ$

Measure $B^0/B_s \rightarrow \pi^0\pi^0$ individually

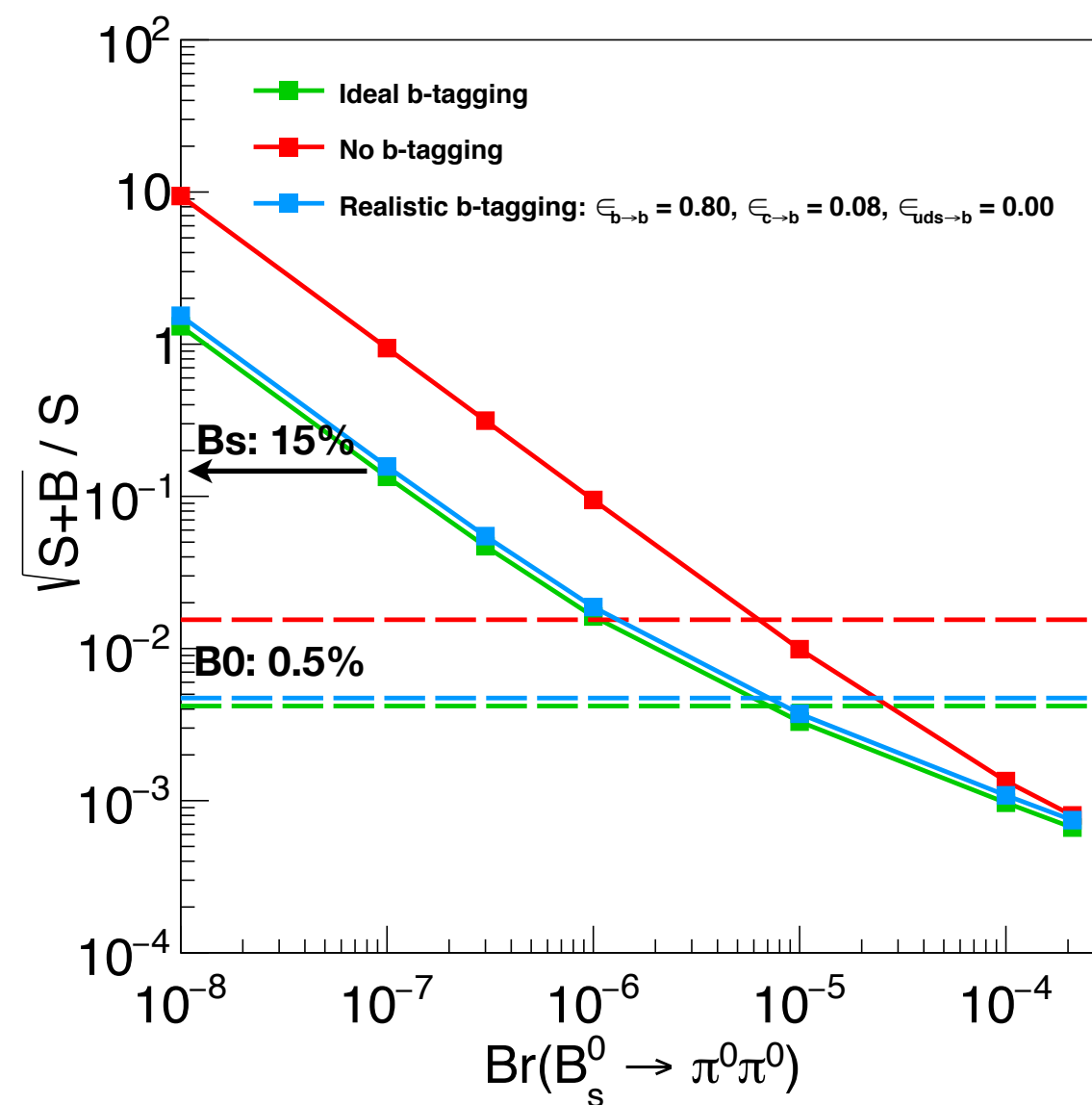
at $1\%/\sqrt{E} \oplus 0.5\%$ ECAL resolution

An artificial sample contains **1e4 $B^0/B_s \rightarrow \pi^0\pi^0$ signal** and **2.4e8 $Z \rightarrow qq$ background**

Cut chain

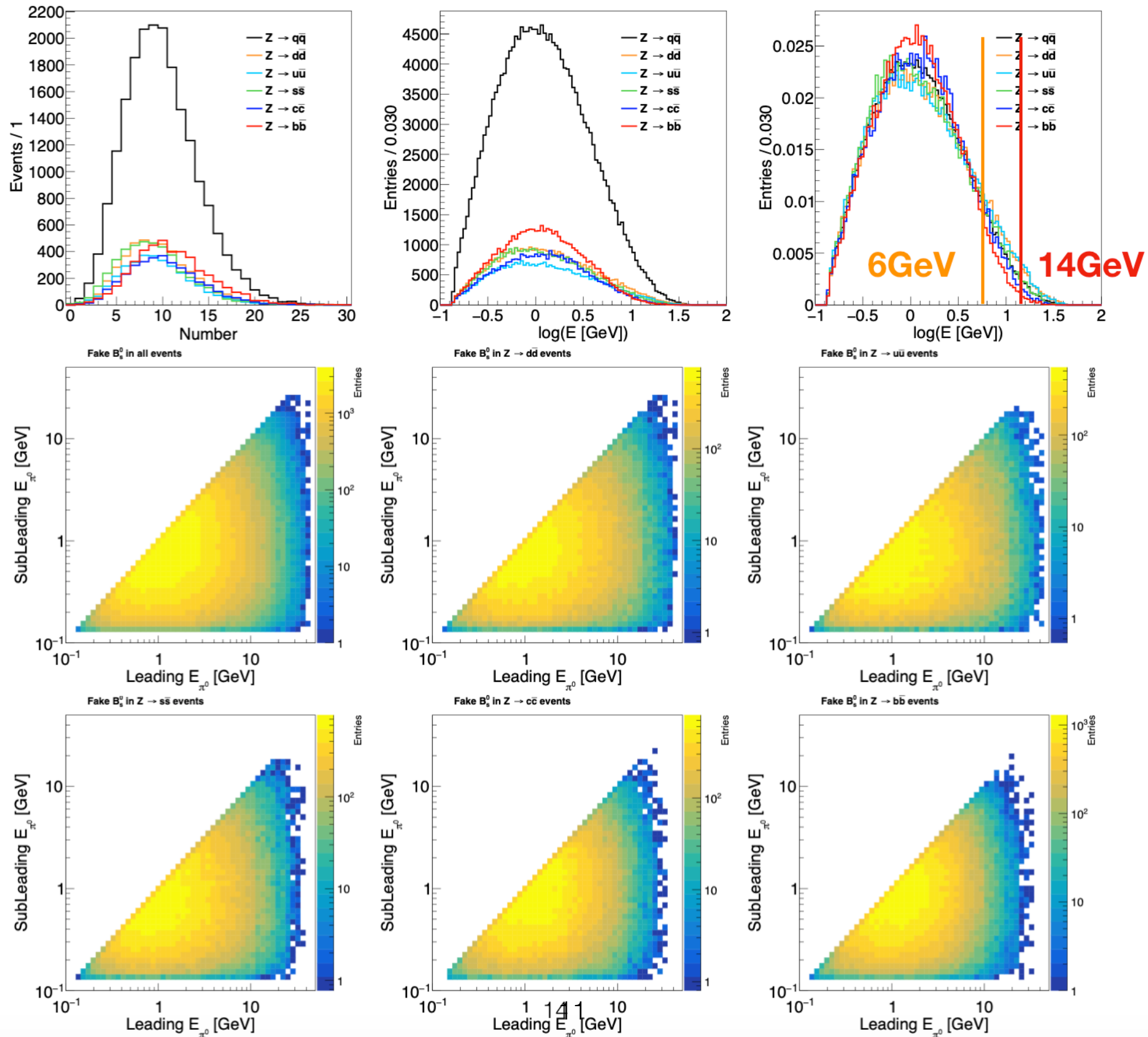
B0 mass window (5.20, 5.36) GeV					
	Sig	Bkg_All	Bkg_uds	Bkg_c	Bkg_b
No cut	9551	46145880	25644234	8524421	11977225
Emin > 6GeV	5917	15633	12608	1765	1260
Emax > 14GeV	5590	1744	1584	104	56
ESum > 22GeV	5574	1424	1308	70	46
Angle < 23°	4987	274	266	4	4
Bs mass window (5.29, 5.45) GeV					
	Sig	Bkg_All	Bkg_uds	Bkg_c	Bkg_b
No cut	9549	44494734	24781183	8215742	11497809
Emin > 6GeV	6005	15254	12195	1775	1284
Emax > 14GeV	5666	1787	1625	101	61
ESum > 22GeV	5645	1457	1329	78	50
Angle < 23°	4975	259	249	5	5

Just raw data, need to be scaled to Tera-Z



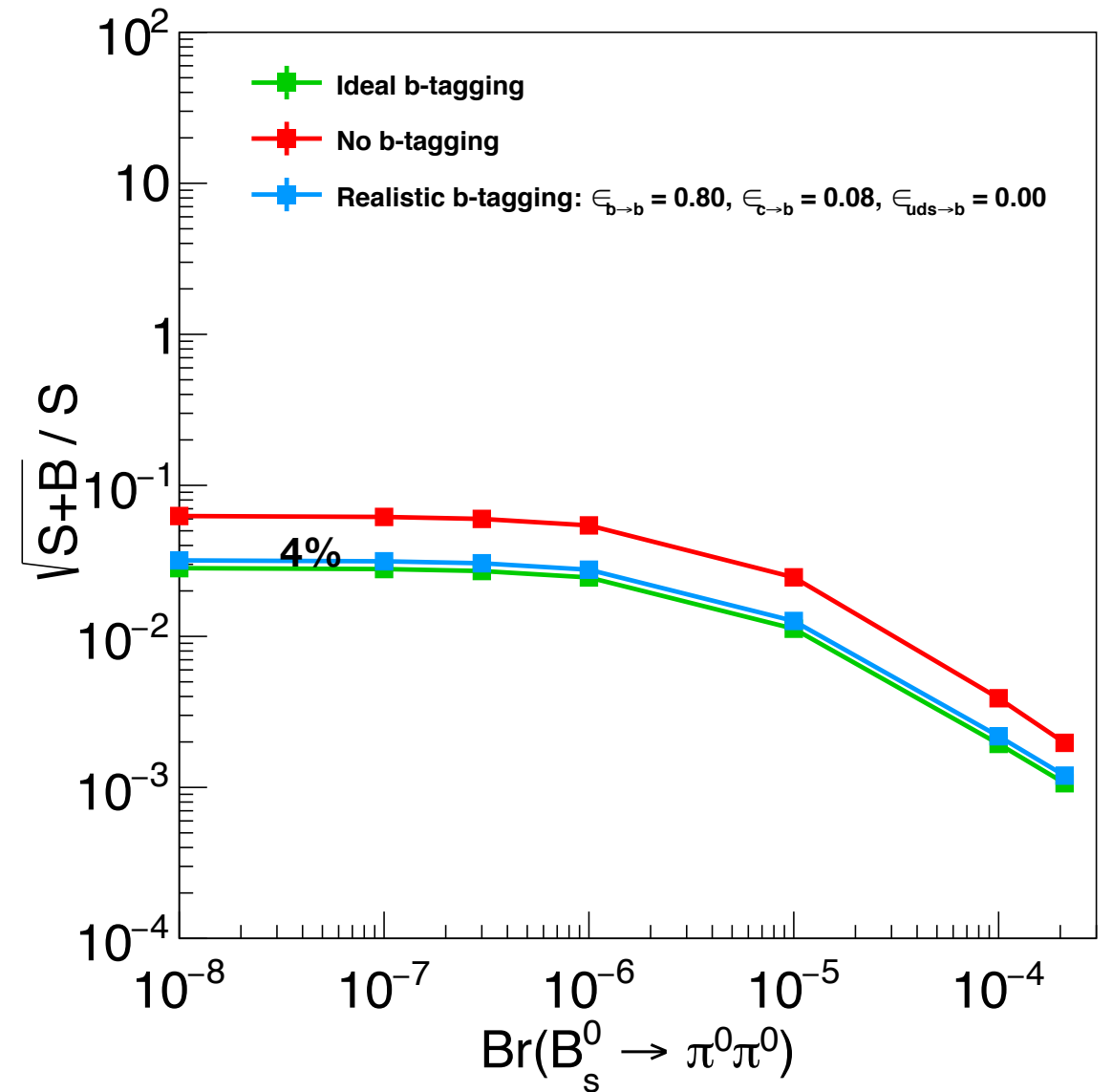
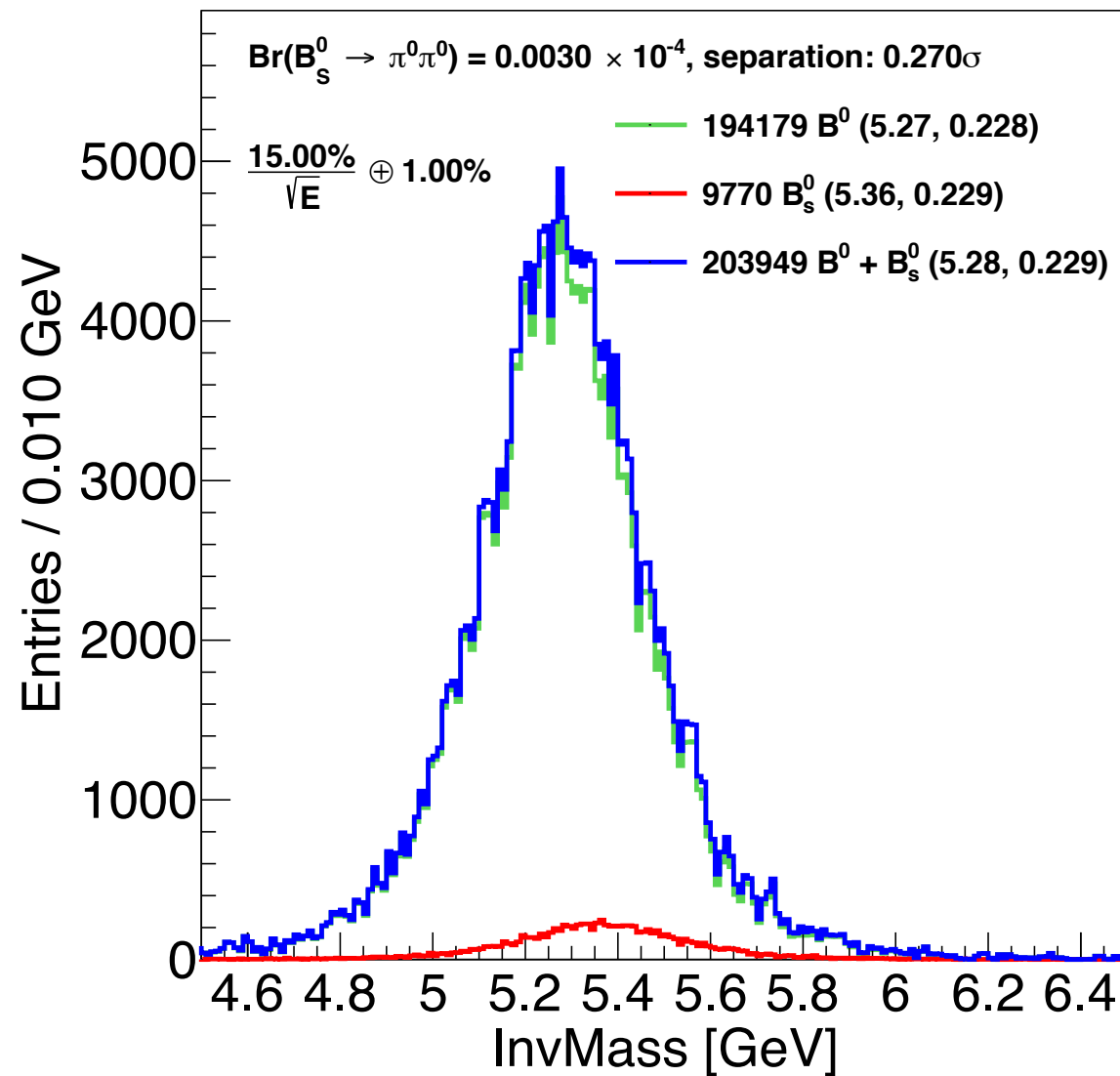
Further understanding on the effect of b-tagging

π^0 energy spectrum differs in different quark flavor events



Mixed measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $15\%/\sqrt{E} \oplus 1\%$ ECAL resolution



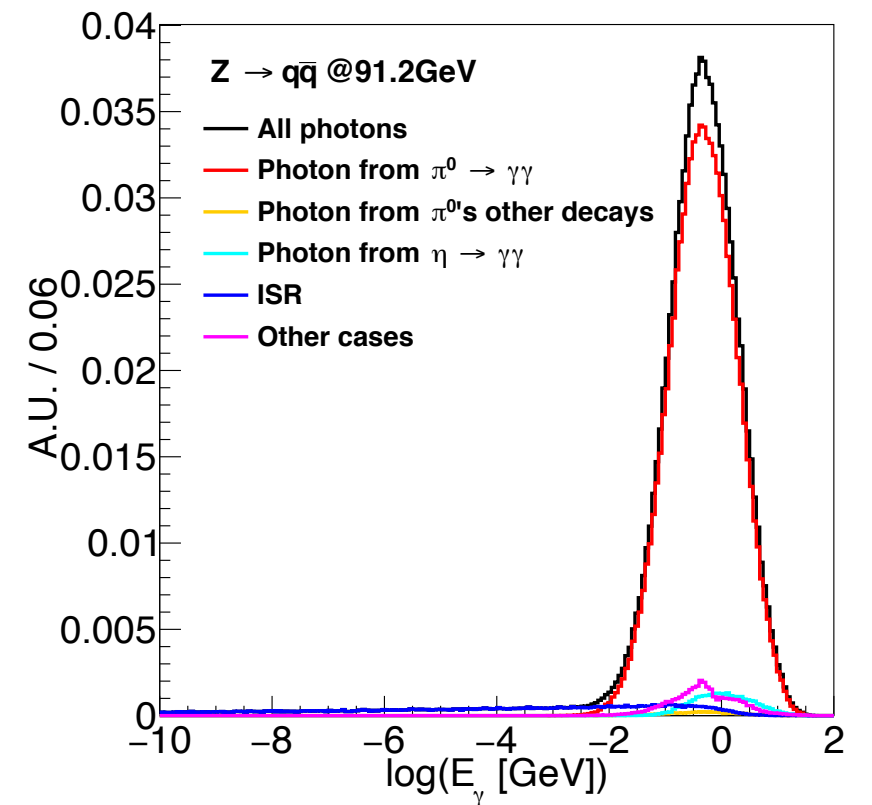
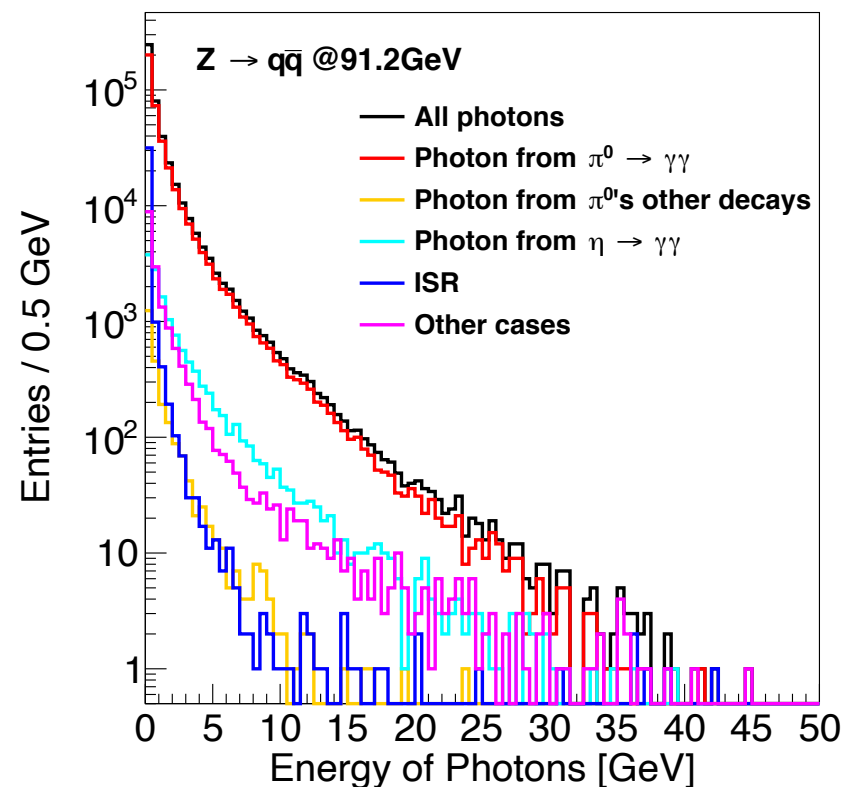
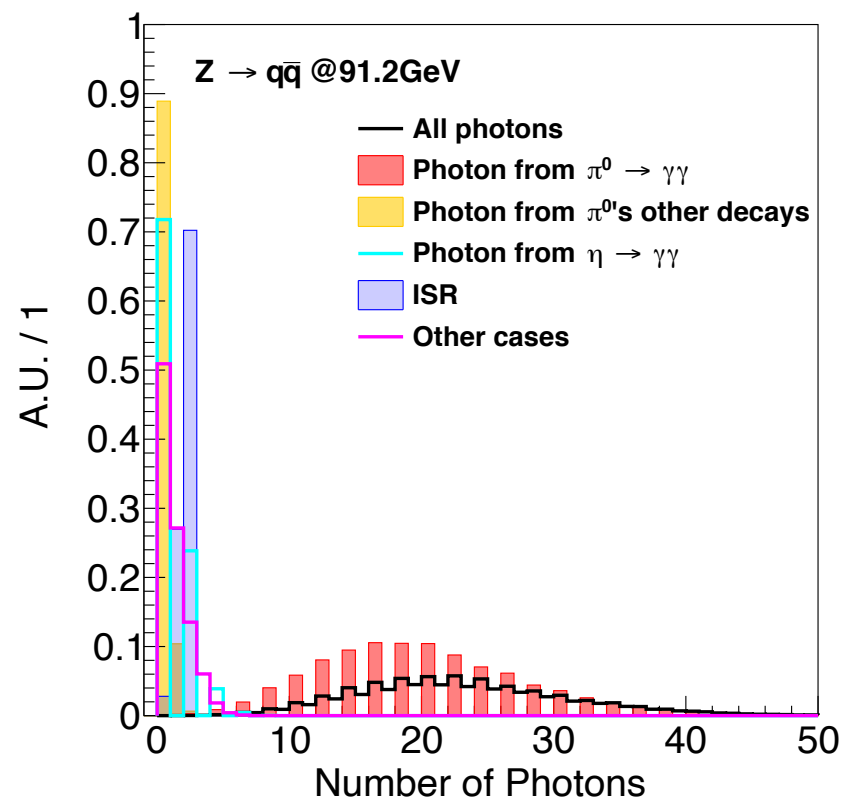
$BR(B_s \rightarrow \pi^0\pi^0)$ can also be estimated by using the $BR(B^0 \rightarrow \pi^0\pi^0)$ measured in other experiments...

Next step...

Further evaluation of the impact of some realistic physics effects:

- **Energy threshold**
- **Acceptance**
- **Separation of nearby photons**
- **Fake photons**
- ...

Reconstruction of $\eta \rightarrow \gamma\gamma$



Summary

Fast simulation study

Reconstruction of π^0

dependence on ECAL resolution and π^0 energy (sample dependent)

Separation of B^0 & B_s

strong limitation on ECAL resolution

stochastic term better than 1%

constant term better than 0.5%

Individual measurement of B^0 & $B_s \rightarrow \pi^0\pi^0$

Mixed measurement of B^0 & $B_s \rightarrow \pi^0\pi^0$

B-tagging is necessary

Future works

Further evaluate the impact of some realistic physics effects

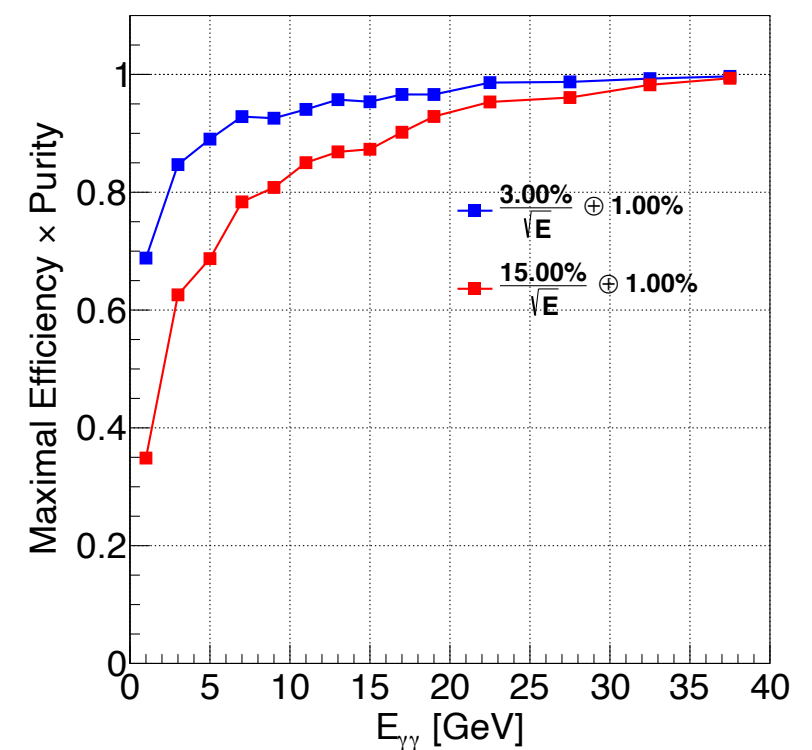
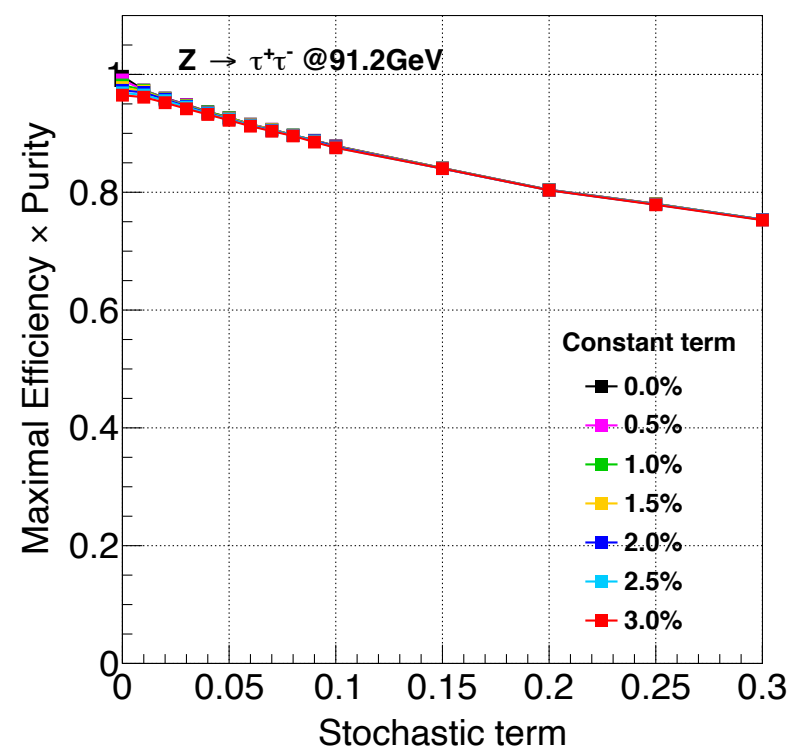
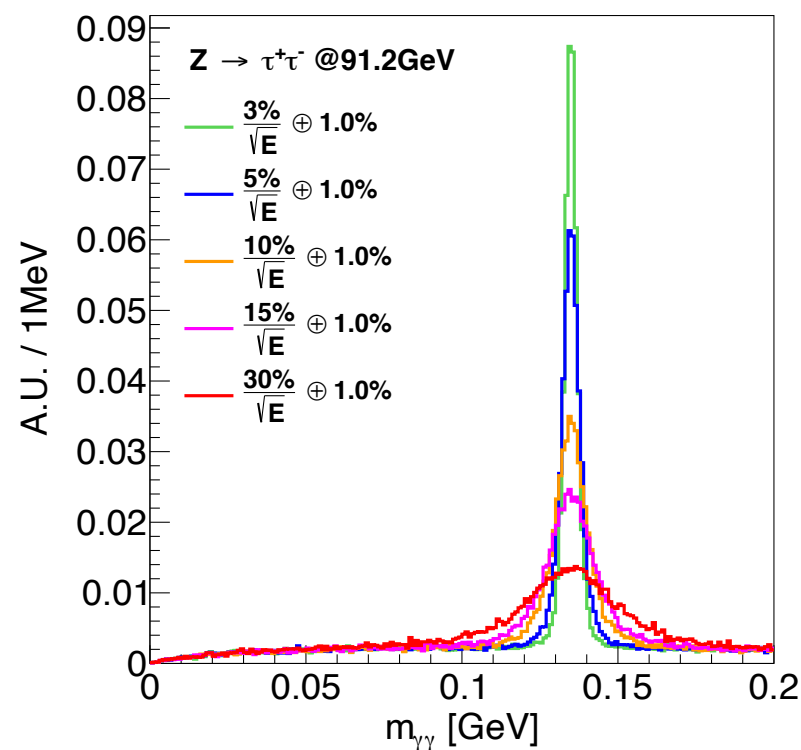
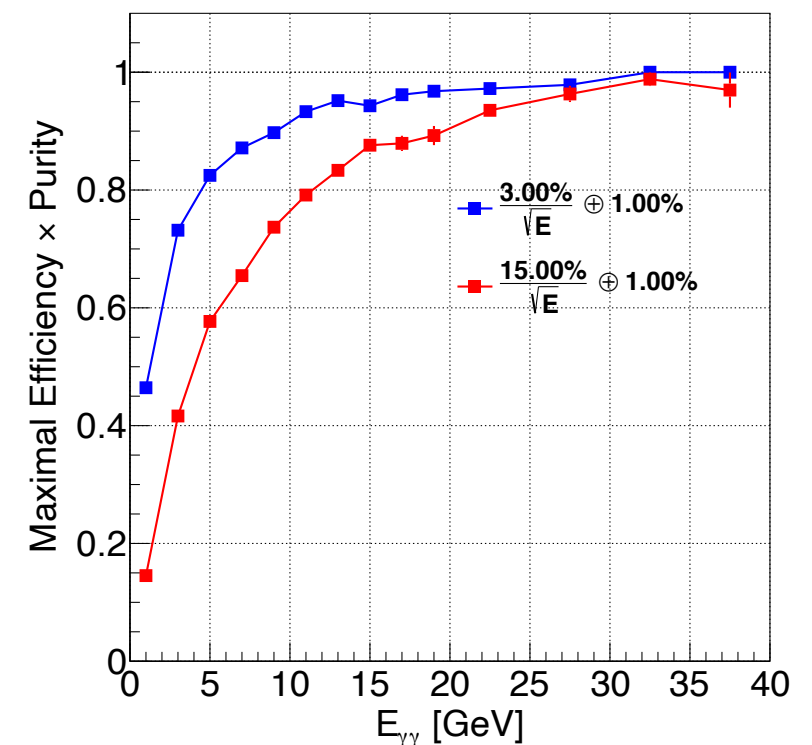
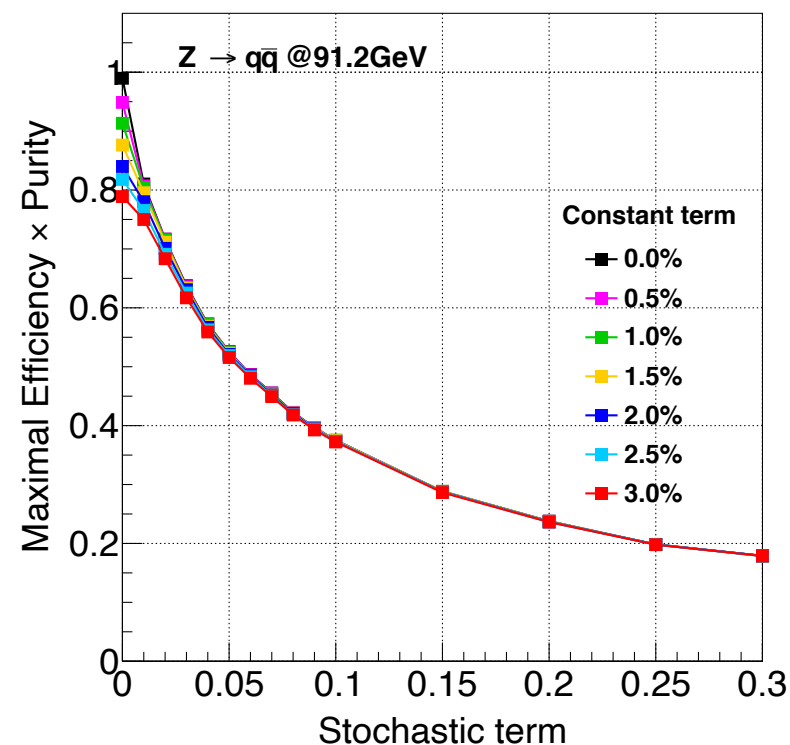
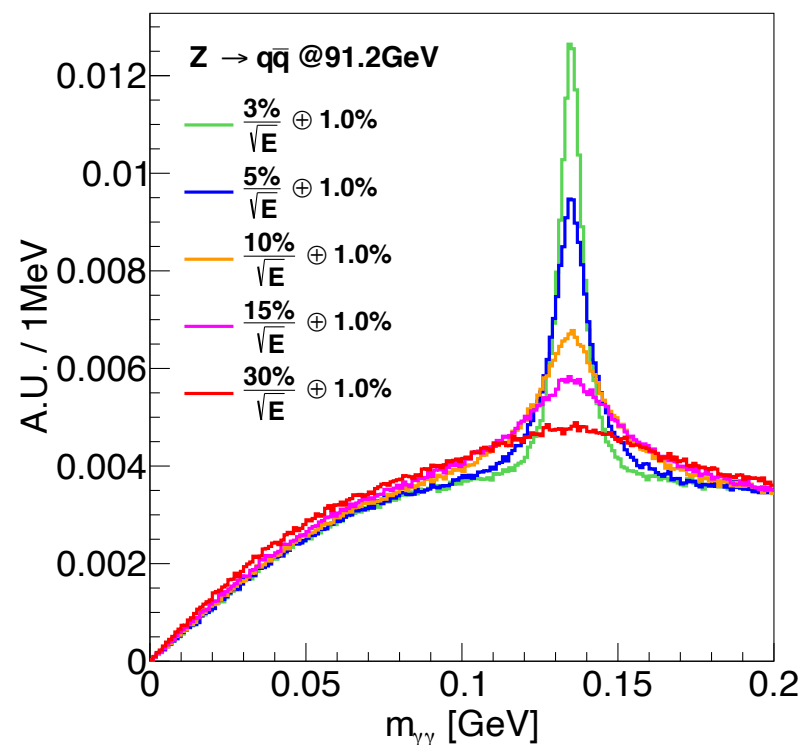
Reconstruction of $\eta \rightarrow \gamma\gamma$

Thanks!

Backup

π^0 reconstruction performance

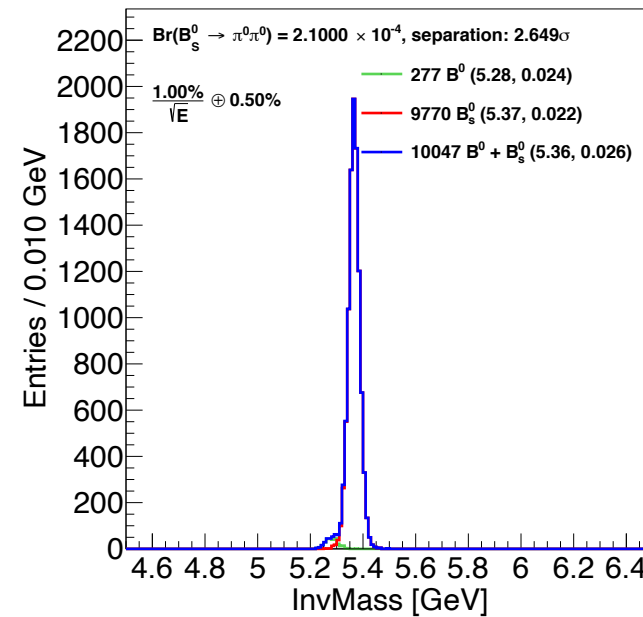
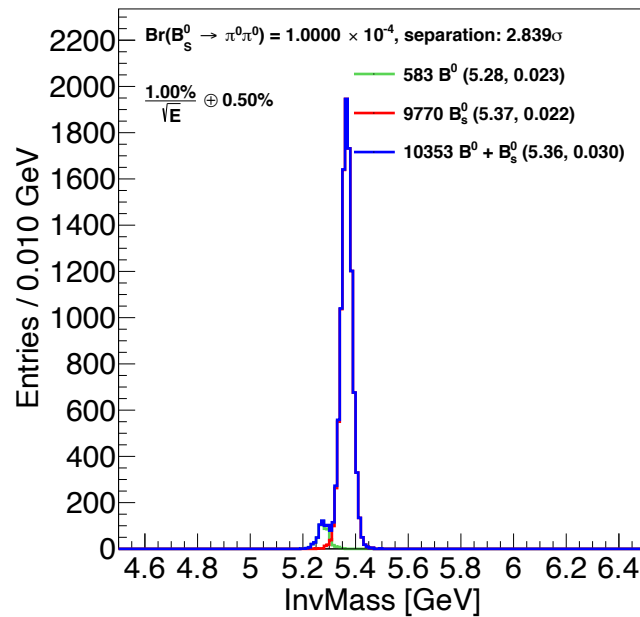
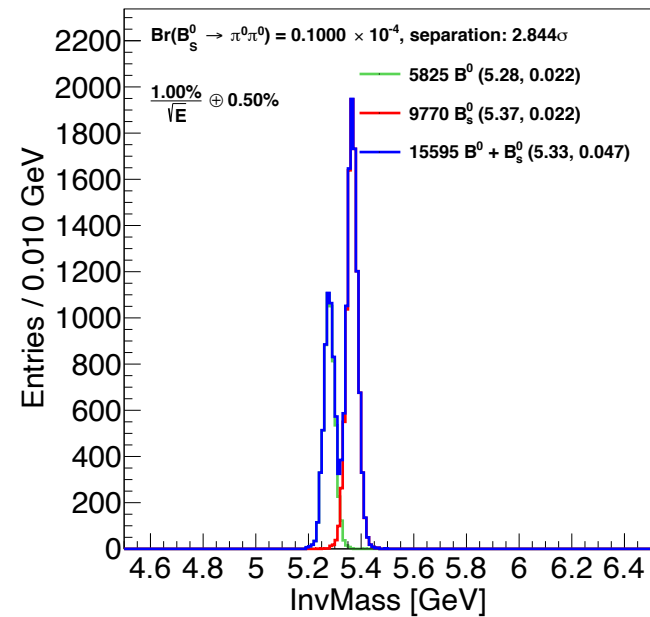
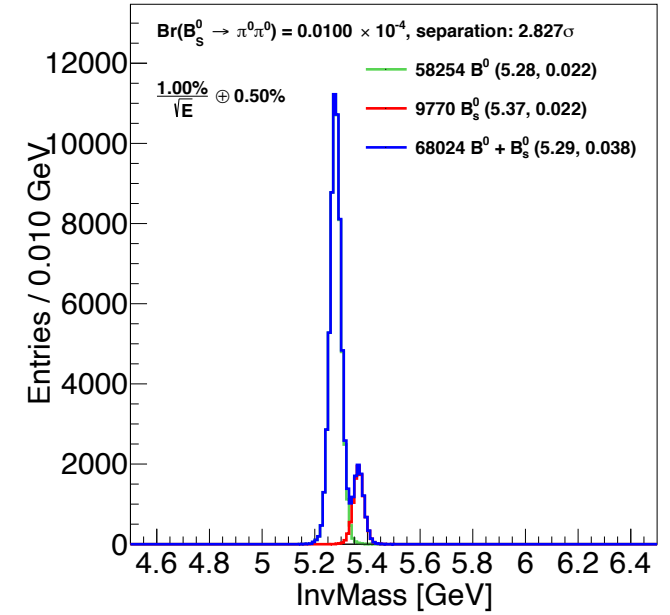
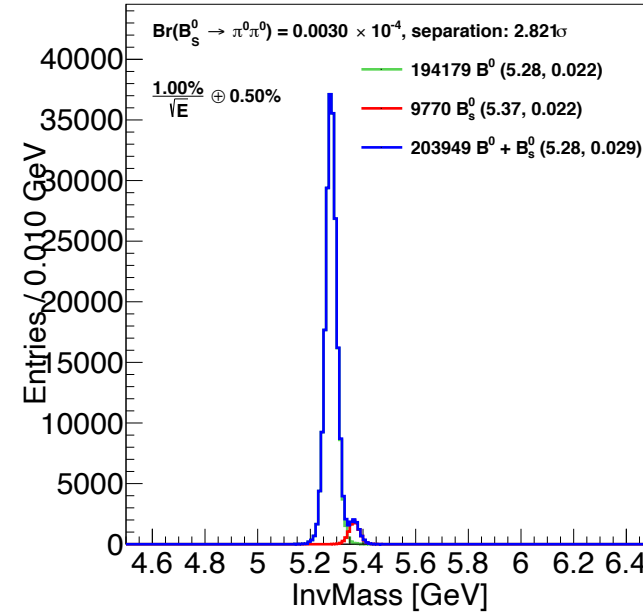
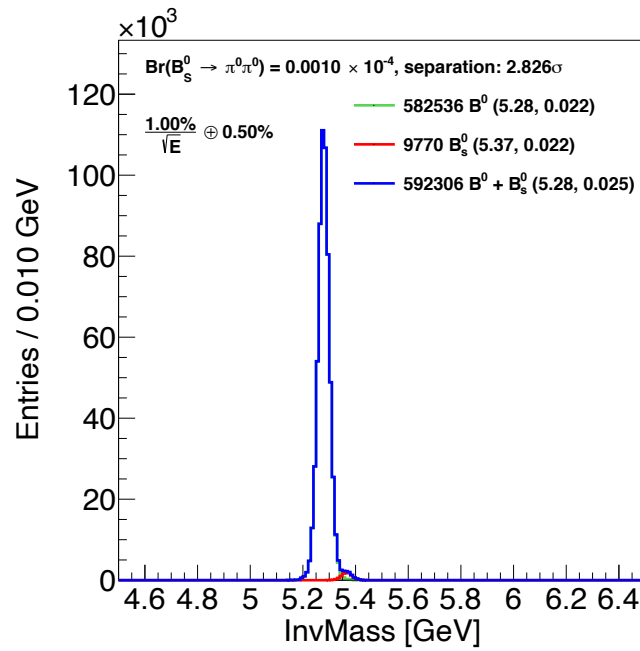
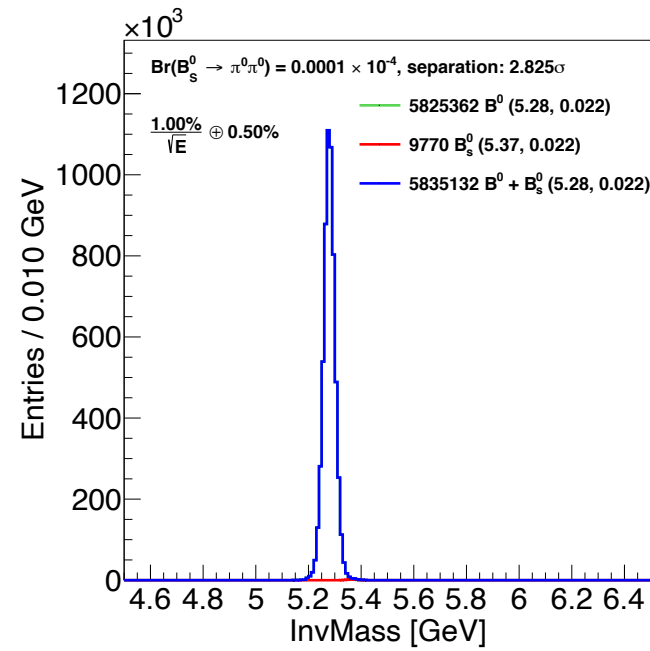
Fast simulation analysis



✓ The first draft of CEPC Note has finished.

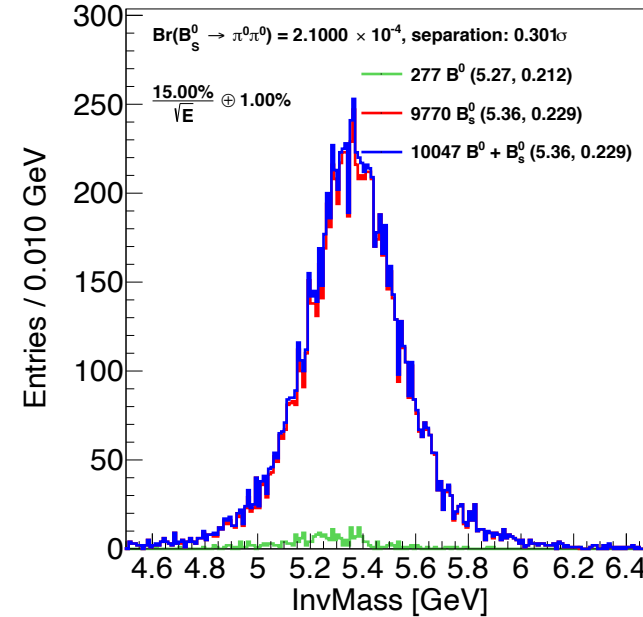
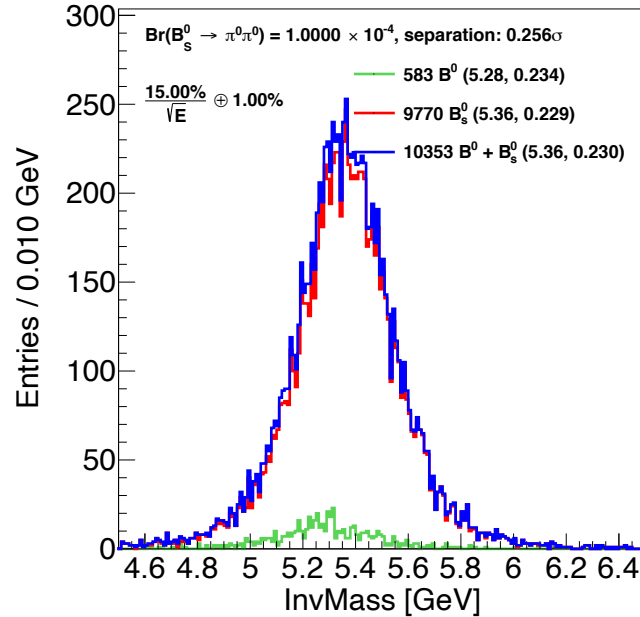
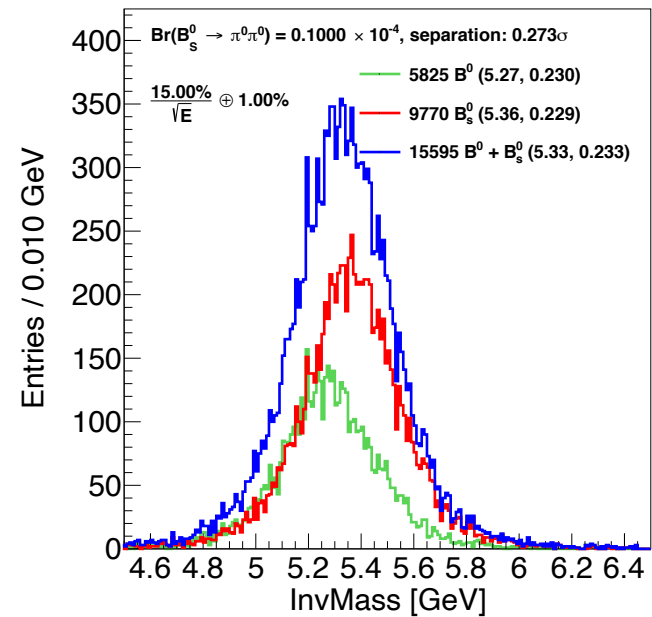
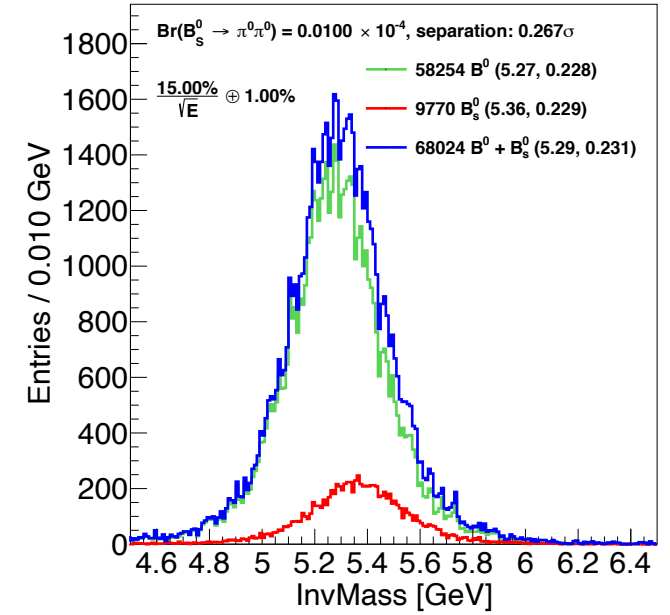
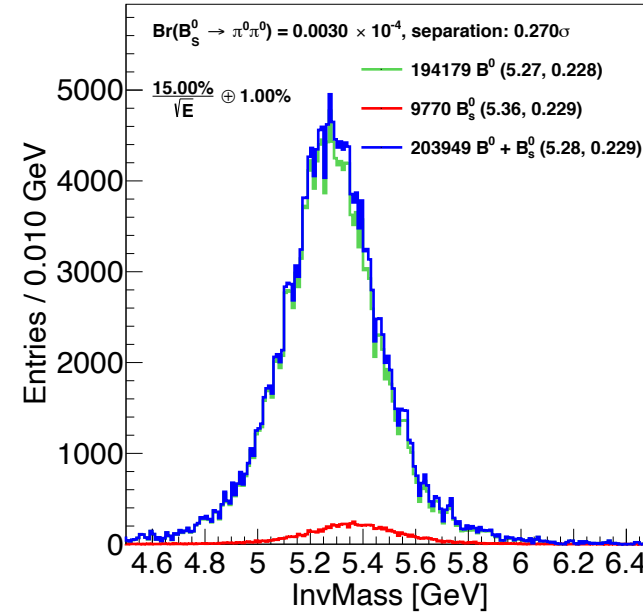
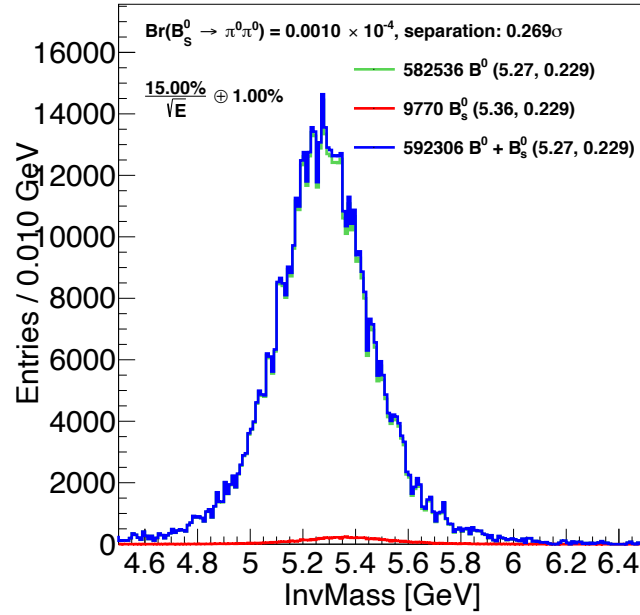
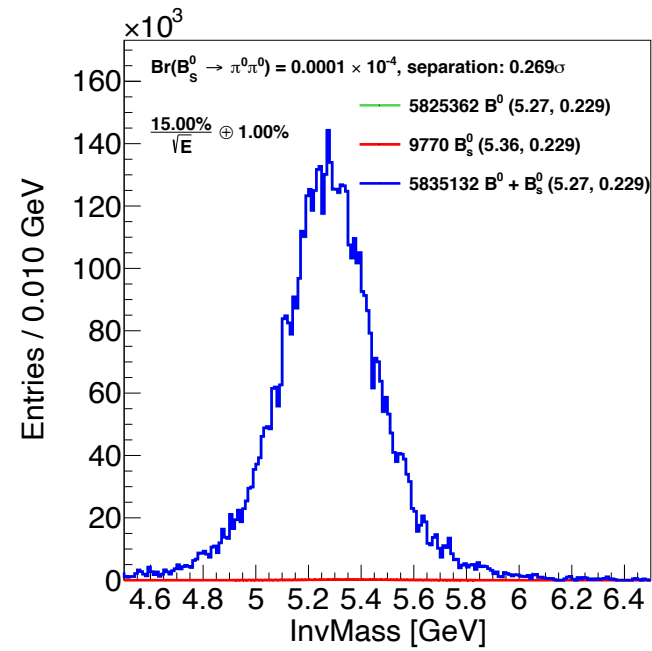
Separation of B^0 and B_s

at $1\%/\sqrt{E} \oplus 0.5\%$ ECAL resolution
varying $BR(B_s \rightarrow \pi^0\pi^0)$ from 10^{-8} to 2.1×10^{-4}

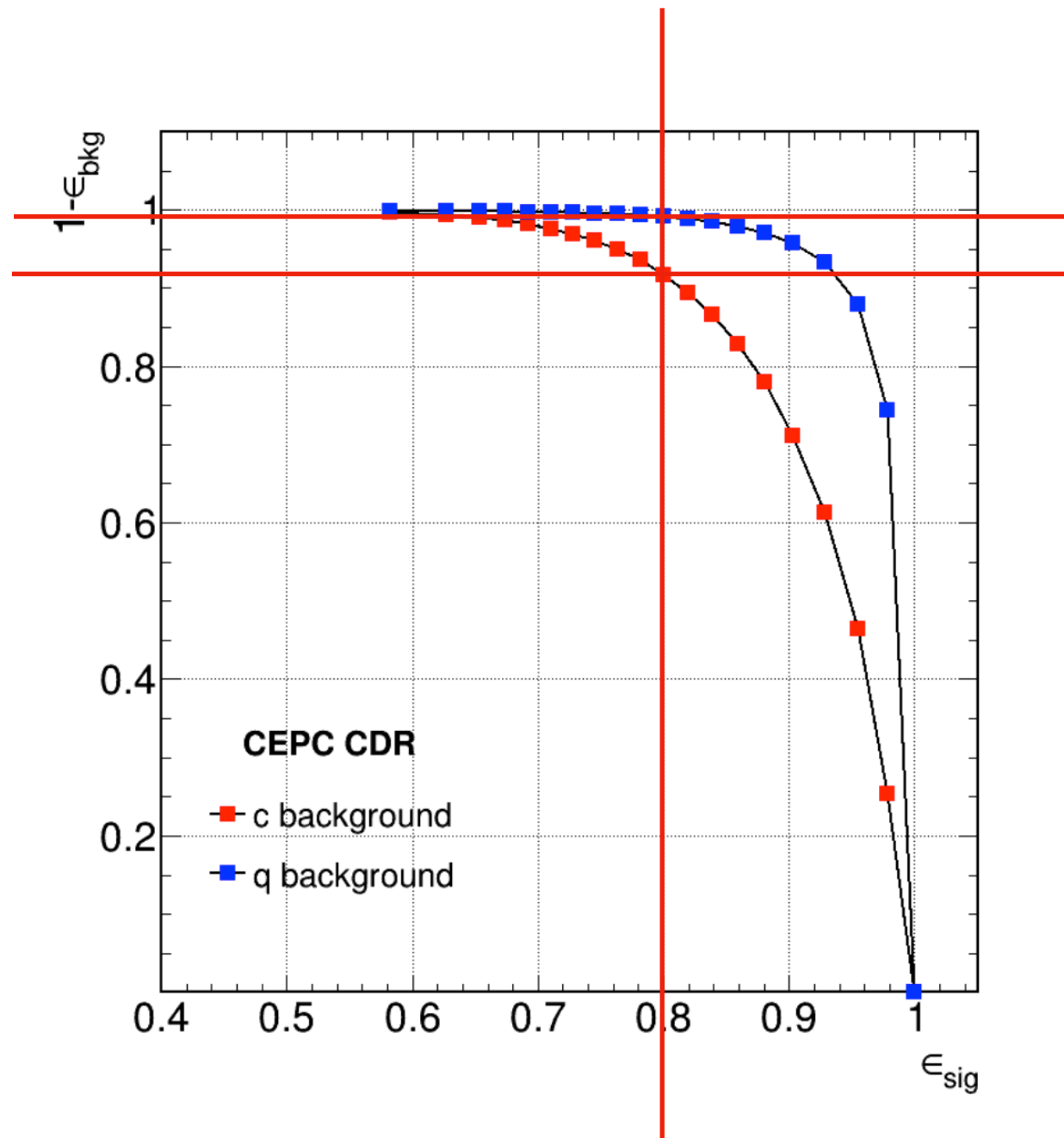


Separation of B^0 and B_s

at $15\%/\sqrt{E} \oplus 1\%$ ECAL resolution
varying $BR(B_s \rightarrow \pi^0\pi^0)$ from 10^{-8} to 2.1×10^{-4}



b-tagging efficiency



eff_bb	eff_cb	eff_qb	Purity	eff*pur
1	1	1	0.216	0.216
0.98	0.75	0.25	0.4287798	0.4202042
0.96	0.54	0.13	0.5459716	0.5241327
0.93	0.39	0.06	0.6593147	0.6131627
0.9	0.3	0.05	0.70282	0.632538
0.88	0.22	0.03	0.7718045	0.6791879
0.86	0.17	0.02	0.8174617	0.7030171
0.84	0.14	0.01	0.8573049	0.7201361
0.82	0.1	0.005	0.8973554	0.7358314
0.8	0.08	0	0.9262436	0.7409949
0.78	0.06	0	0.9422819	0.7349799
0.76	0.05	0	0.95022	0.7221672
0.74	0.04	0	0.9587332	0.7094626
0.72	0.03	0	0.9678865	0.6968783
0.69	0.01	0	0.9885911	0.6821279
0.58	0	0	1	0.58

Introduction of $B^0 \rightarrow \pi^0\pi^0$

$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ in PDG 2018				Γ_{388}/Γ	
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$1.83 \pm 0.21 \pm 0.13$		¹ LEES	13D	BABR	$e^+e^- \rightarrow \Upsilon(4S)$

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Measurement of the branching fraction and CP asymmetry in $B^0 \rightarrow \pi^0\pi^0$ decays, and an improved constraint on ϕ_2

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We measure the branching fraction and CP violation asymmetry in the decay $B^0 \rightarrow \pi^0\pi^0$, using a data sample of 752×10^6 $B\bar{B}$ pairs collected at the $\Upsilon(4S)$ resonance with the Belle detector at the KEKB e^+e^- collider. The obtained branching fraction and direct CP asymmetry are $\mathcal{B}(B \rightarrow \pi^0\pi^0) = [1.31 \pm 0.19(\text{stat}) \pm 0.19(\text{syst})] \times 10^{-6}$ and $A_{CP} = +0.14 \pm 0.36(\text{stat}) \pm 0.10(\text{syst})$, respectively. The signal significance, including the systematic uncertainty, is **6.4 standard deviations**. We combine these results with Belle's earlier measurements of $B^0 \rightarrow \pi^+\pi^-$ and $B^\pm \rightarrow \pi^\pm\pi^0$ to exclude the CP -violating parameter ϕ_2 from the range $15.5^\circ < \phi_2 < 75.0^\circ$ at 95% confidence level.

(Belle Collaboration)

<https://journals.aps.org/prd/abstract/10.1103/PhysRevD.96.032007>

Introduction of $B_s \rightarrow \pi^0 \pi^0$

Experimental upper limit

$\Gamma(\pi^0 \pi^0)/\Gamma_{\text{total}}$ in PDG 2018

Γ_{87}/Γ

VALUE	CL%	DOCUMENT ID	TECN	COMMENT
$<2.1 \times 10^{-4}$	90	¹ ACCIARRI 95H	L3	$e^+ e^- \rightarrow Z$
¹ ACCIARRI 95H assumes $f_{B^0} = 39.5 \pm 4.0$ and $f_{B_s} = 12.0 \pm 3.0\%$.				



ELSEVIER

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Physics Letters B 363 (1995) 127–136

Search for neutral charmless B decays at LEP

L3 Collaboration

<https://www.sciencedirect.com/science/article/pii/0370269395010420>

Table 2

Resolutions (σ of a Gaussian fit to the signal Monte Carlo invariant mass distribution), efficiencies and experimental limits for B_d^0 and B_s^0 branching ratios. The (I) and (II) modes refer respectively to the search for a four photon final state or one with a photon pair for one η and a single cluster for the other one. The first error on the efficiencies is statistical, the second systematic.

Process	Resolution (MeV)	Efficiency (%)	Upper limit 90% C.L.
$B_d^0 \rightarrow \eta\eta$ (I)	107 ± 10	$2.5 \pm 0.2^{+0.2}_{-0.2}$	
$B_d^0 \rightarrow \eta\eta$ (II)	146 ± 11	$4.6 \pm 0.3^{+0.02}_{-0.2}$	
$B_d^0 \rightarrow \eta\eta$			$< 4.1 \times 10^{-4}$
$B_d^0 \rightarrow \eta\pi^0$	79 ± 5	$4.5 \pm 0.3^{+0.05}_{-0.03}$	$< 2.5 \times 10^{-4}$
$B_d^0 \rightarrow \pi^0\pi^0$	97 ± 4	$7.6 \pm 0.4^{+0.2}_{-0.5}$	$< 6.0 \times 10^{-5}$
$B_s^0 \rightarrow \eta\eta$ (I)	101 ± 10	$2.4 \pm 0.2^{+0.2}_{-0.2}$	
$B_s^0 \rightarrow \eta\eta$ (II)	129 ± 8	$4.8 \pm 0.3^{+0.2}_{-0.3}$	
$B_s^0 \rightarrow \eta\eta$			$< 1.5 \times 10^{-3}$
$B_s^0 \rightarrow \eta\pi^0$	81 ± 1	$4.3 \pm 0.3^{+0.02}_{-0.1}$	$< 1.0 \times 10^{-3}$
$B_s^0 \rightarrow \pi^0\pi^0$	99 ± 4	$8.3 \pm 0.4^{+0.4}_{-0.7}$	$< 2.1 \times 10^{-4}$

Introduction of $B_s \rightarrow \pi^0 \pi^0$

Theoretical estimation

ALI, KRAMER, LI, LÜ, SHEN, WANG, AND WANG

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TABLE III. The CP -averaged branching ratios ($\times 10^{-6}$) of $B_s \rightarrow PP$ decays obtained in the pQCD approach (This work); the errors for these entries correspond to the uncertainties in the input hadronic quantities, from the scale dependence, and the CKM matrix elements, respectively. We have also listed the current experimental measurements and upper limits (90% C.L.) wherever available [13]. For comparison, we also cite the theoretical estimates of the branching ratios in the QCD factorization framework [16] and in SCET [20], quoting two estimates in the latter case for some decays.

Modes	Class	QCDF	SCET	This work	Experiment
$\bar{B}_s^0 \rightarrow K^+ \pi^-$	T	$10.2^{+4.5+3.8+0.7+0.8}_{-3.9-3.2-1.2-0.7}$	$4.9 \pm 1.2 \pm 1.3 \pm 0.3$	$7.6^{+3.2+0.7+0.5}_{-2.3-0.7-0.5}$	$5.0 \pm 0.75 \pm 1.0$
$\bar{B}_s^0 \rightarrow K^0 \pi^0$	C	$0.49^{+0.28+0.22+0.40+0.33}_{-0.24-0.14-0.14-0.17}$	$0.76 \pm 0.26 \pm 0.27 \pm 0.17$	$0.16^{+0.05+0.10+0.02}_{-0.04-0.05-0.01}$	
$\bar{B}_s^0 \rightarrow K^+ K^-$	P	$22.7^{+3.5+12.7+2.0+24.1}_{-3.2-8.4-2.0-9.1}$	$18.2 \pm 6.7 \pm 1.1 \pm 0.5$	$13.6^{+4.2+7.5+0.7}_{-3.2-4.1-0.2}$	$24.4 \pm 1.4 \pm 4.6$
$\bar{B}_s^0 \rightarrow K^0 \bar{K}^0$	P	$24.7^{+2.5+13.7+2.6+25.6}_{-2.4-9.2-2.9-9.8}$	$17.7 \pm 6.6 \pm 0.5 \pm 0.6$	$15.6^{+5.0+8.3+0.0}_{-3.8-4.7-0.0}$	
$\bar{B}_s^0 \rightarrow \pi^0 \eta$	P_{EW}	$0.075^{+0.013+0.030+0.008+0.010}_{-0.012-0.025-0.010-0.007}$	$0.014 \pm 0.004 \pm 0.005 \pm 0.004$ $0.016 \pm 0.0007 \pm 0.005 \pm 0.006$	$0.05^{+0.02+0.01+0.00}_{-0.02-0.01-0.00}$	<1000
$\bar{B}_s^0 \rightarrow \pi^0 \eta'$	P_{EW}	$0.11^{+0.02+0.04+0.01+0.01}_{-0.02-0.04-0.01-0.01}$	$0.006 \pm 0.003 \pm 0.002^{+0.064}_{-0.006}$ $0.038 \pm 0.013 \pm 0.016^{+0.260}_{-0.036}$	$0.11^{+0.05+0.02+0.00}_{-0.03-0.01-0.00}$	
$\bar{B}_s^0 \rightarrow K^0 \eta$	C	$0.34^{+0.19+0.64+0.21+0.16}_{-0.16-0.27-0.07-0.08}$	$0.80 \pm 0.48 \pm 0.29 \pm 0.18$ $0.59 \pm 0.34 \pm 0.24 \pm 0.15$	$0.11^{+0.05+0.06+0.01}_{-0.03-0.03-0.01}$	
$\bar{B}_s^0 \rightarrow K^0 \eta'$	C	$2.0^{+0.3+1.5+0.6+1.5}_{-0.3-1.1-0.3-0.6}$	$4.5 \pm 1.5 \pm 0.4 \pm 0.5$ $3.9 \pm 1.3 \pm 0.5 \pm 0.4$	$0.72^{+0.20+0.28+0.11}_{-0.16-0.17-0.05}$	
$\bar{B}_s^0 \rightarrow \eta \eta$	P	$15.6^{+1.6+9.9+2.2+13.5}_{-1.5-6.8-2.5-5.5}$	$7.1 \pm 6.4 \pm 0.2 \pm 0.8$ $6.4 \pm 6.3 \pm 0.1 \pm 0.7$	$8.0^{+2.6+4.7+0.0}_{-1.9-2.5-0.0}$	<1500
$\bar{B}_s^0 \rightarrow \eta \eta'$	P	$54.0^{+5.5+32.4+8.3+40.5}_{-5.2-22.4-6.4-16.7}$	$24.0 \pm 13.6 \pm 1.4 \pm 2.7$ $23.8 \pm 13.2 \pm 1.6 \pm 2.9$	$21.0^{+6.0+10.0+0.0}_{-4.6-5.6-0.0}$	
$\bar{B}_s^0 \rightarrow \eta' \eta'$	P	$41.7^{+4.2+26.3+15.2+36.6}_{-4.0-17.2-8.5-15.4}$	$44.3 \pm 19.7 \pm 2.3 \pm 17.1$ $49.4 \pm 20.6 \pm 8.4 \pm 16.2$	$14.0^{+3.2+6.2+0.0}_{-2.7-3.9-0.0}$	
$\bar{B}_s^0 \rightarrow \pi^+ \pi^-$	ann	$0.024^{+0.003+0.025+0.000+0.163}_{-0.003-0.012-0.000-0.021}$	...	$0.57^{+0.16+0.09+0.01}_{-0.13-0.10-0.00}$	<1.36
$\bar{B}_s^0 \rightarrow \pi^0 \pi^0$	ann	$0.012^{+0.001+0.013+0.000+0.082}_{-0.001-0.006-0.000-0.011}$	...	$0.28^{+0.08+0.04+0.01}_{-0.07-0.05-0.00}$	<210

$\sim 3 \times 10^{-7}$

Unique Opportunities at Z pole

Giga- Z , Tera- Z and $10\times$ Tera- Z : a phase of future linear/circular lepton colliders. [Fujii et al.(2019), Dong et al.(2018), Abada et al.(2019)]

Z factories are also $b(c/\tau)$ factories:

Channel	Belle II	LHCb	Giga- Z	Tera- Z	$10\times$ Tera- Z
$B^0, \bar{B}^0$	5.3×10^{10}	$\sim 6 \times 10^{13}$	1.2×10^8	1.2×10^{11}	1.2×10^{12}
$B^\pm$	5.6×10^{10}	$\sim 6 \times 10^{13}$	1.2×10^8	1.2×10^{11}	1.2×10^{12}
$B_s, \bar{B}_s$	5.7×10^8	$\sim 2 \times 10^{13}$	3.2×10^7	3.2×10^{10}	3.2×10^{11}
$B_c^\pm$	-	$\sim 4 \times 10^{11}$	2.2×10^5	2.2×10^8	2.2×10^9
$\Lambda_b, \bar{\Lambda}_b$	-	$\sim 2 \times 10^{13}$	1.0×10^7	1.0×10^{10}	1.0×10^{11}