



LABORATÓRIO DE INSTRUMENTAÇÃO  
E FÍSICA EXPERIMENTAL DE PARTÍCULAS  
*partículas e tecnologia*



UNIVERSIDAD  
DE GRANADA

# Running in the ALPs

Based on 2012.09017

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# Motivation: EFT approach

Expansion into higher dimensional operators:

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{\mathcal{L}_5}{\Lambda} + \frac{\mathcal{L}_6}{\Lambda^2} + \frac{\mathcal{L}_7}{\Lambda^3} + \frac{\mathcal{L}_8}{\Lambda^4} + \dots$$

$$\mathcal{L}_d = c_i \mathcal{O}_i \quad [\mathcal{O}_i] = d$$

**If new states exist below electroweak scale, the SMEFT must be extended**

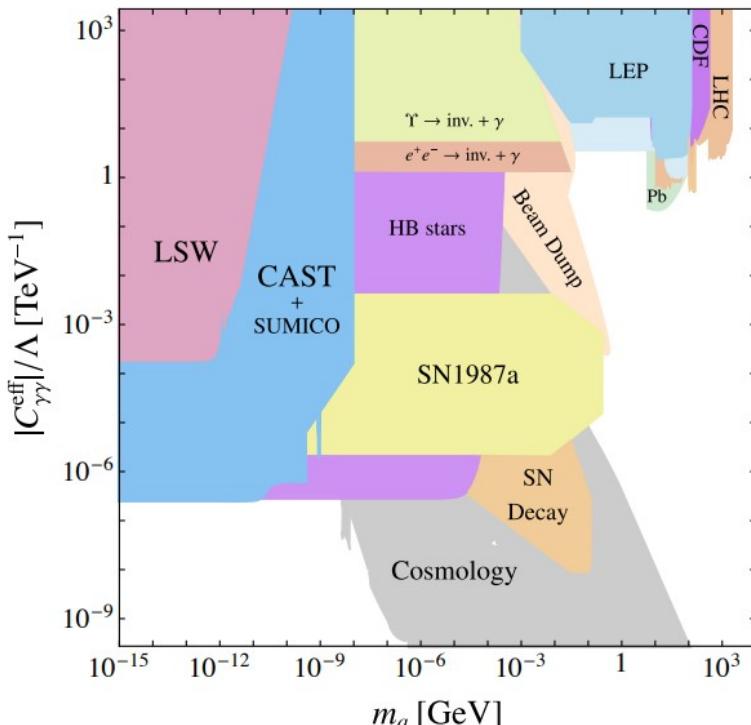
# Motivation: ALPs

**Axion-like particles = CP-odd singlet scalars**

**Theoretically well motivated:**

- Strong CP-problem Peccei, Quinn [PRL38 \(1977\) 1440](#)
- Composite Higgs Models Brando Bellazzini, Csaba Csáki and Javi Serra, [1401.2457](#)
- Dark Matter M. J. Dolan, F. Kahlhoefer, C. McCabe and K. Schmidt-Hoberg, [1412.5174](#)
- Anomalies Manuel A. Buen-Abad, Jiji Fan, Matthew Reece and Chen Sun [2104.03267](#)

# Motivation: ALPs



- Experiments span a huge range of energies
- Wilson coefficients **run**, and **mix**, following the corresponding RGEs

M. Bauer, M. Neubert,  
A. Thamm, 1708.00443

## SMEFT+ALP

$$\begin{aligned}\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2}\partial_\mu s\partial^\mu s - \frac{1}{2}m^2 s^2 - \frac{\lambda_s}{4!}s^4 - \lambda_{s\phi}s^2|\phi|^2 \\ + \sum_i \frac{1}{\Lambda}\alpha_i \mathcal{O}_i^{(5)}\end{aligned}$$

$\mathcal{O}_i^{(5)}$  invariant under SM gauge groups

**Assume only new physics is CP-even**

# SMEFT+ALP

Non-redundant basis

$$\mathcal{O}_{su\phi}^{\alpha\beta} = is(\overline{q_L^\alpha}\tilde{\phi}u_R^\beta - \overline{u_R^\beta}\tilde{\phi}^\dagger q_L^\alpha)$$

$$\mathcal{O}_{sd\phi}^{\alpha\beta} = is(\overline{q_L^\alpha}\phi d_R^\beta - \overline{d_R^\beta}\phi^\dagger q_L^\alpha)$$

$$\mathcal{O}_{se\phi}^{\alpha\beta} = is(\overline{l_L^\alpha}\phi e_R^\beta - \overline{e_R^\beta}\phi^\dagger l_L^\alpha)$$

$$\mathcal{O}_{s\tilde{G}} = sG_{\mu\nu}^A \tilde{G}_A^{\mu\nu}$$

$$\mathcal{O}_{s\tilde{W}} = sW_{\mu\nu}^A \tilde{W}_A^{\mu\nu}$$

$$\mathcal{O}_{s\tilde{B}} = sB_{\mu\nu} \tilde{B}^{\mu\nu}$$

EOM

Redundant ops

$$\mathcal{R}_{s\phi\square} = is(\phi^\dagger D^2\phi - (D^2\phi)^\dagger \phi)$$

$$\mathcal{R}_{sq}^{\alpha\beta} = s(\overline{q_L^\alpha}\not{D}q_L^\beta + \overline{q_L^\beta}\not{D}q_L^\alpha)$$

$$\mathcal{R}_{sl}^{\alpha\beta} = s(\overline{l_L^\alpha}\not{D}l_L^\beta + \overline{l_L^\beta}\not{D}l_L^\alpha)$$

$$\mathcal{R}_{su}^{\alpha\beta} = s(\overline{u_R^\alpha}\not{D}u_R^\beta + \overline{u_R^\beta}\not{D}u_R^\alpha)$$

$$\mathcal{R}_{sd}^{\alpha\beta} = s(\overline{d_R^\alpha}\not{D}d_R^\beta + \overline{d_R^\beta}\not{D}d_R^\alpha)$$

$$\mathcal{R}_{se}^{\alpha\beta} = s(\overline{e_R^\alpha}\not{D}e_R^\beta + \overline{e_R^\beta}\not{D}e_R^\alpha)$$

Complete Green basis of operators

# SMEFT+ALP

**Approximate shift symmetry:**  $s \rightarrow s + \sigma$

$$\mathcal{L}^{(5)} = \sum_{\Psi} (\partial_\mu s) \bar{\Psi} C_\Psi \gamma^\mu \Psi + C_X s X_{\mu\nu} \tilde{X}^{\mu\nu}$$

# SMEFT+ALP

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**Lepton sector:**

9 + 9 independent parameters:  $C_\ell + C_e$

9 + 9 independent parameters:  $a_{se\phi} + a_{\widetilde{se\phi}}$

$\mathcal{O}_{se\phi}$  CP-even       $\mathcal{O}_{\widetilde{se\phi}}$  CP-odd

# SMEFT+ALP

**Approximate shift symmetry:**  $s \rightarrow s + \sigma$

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**Lepton sector:**

9 + 9 independent parameters:

$$C_\ell + C_e$$

Only shift symmetric

9 + 9 independent parameters:

$$a_{se\phi} + a_{\widetilde{se\phi}}$$

$\mathcal{O}_{se\phi}$  CP-even       $\mathcal{O}_{\widetilde{se\phi}}$  CP-odd

# SMEFT+ALP

Performing the appropriate chiral rotations, the necessary conditions to ensure shift-symmetry are:

$$a_{se\phi} = \text{Re}(H_\ell y^e + y^e H_e)$$

$$\widetilde{a_{se\phi}} = -\text{Im}(H_\ell y^e + y^e H_e)$$

**Limit of 1 lepton family:**  $a_{se\phi}$  **vs**  $C_e + C_\ell$  **parameters**

# SMEFT+ALP

- Computation of divergences generated by 1PI diagrams at one-loop
- Up to  $\mathcal{O}(1/\Lambda)$  divergences are absorbed by operators of off-shell basis

**Computation:** FeynRules + FeynArts + FormCalc

T. Hahn,  
[hep-ph/0012260](#)

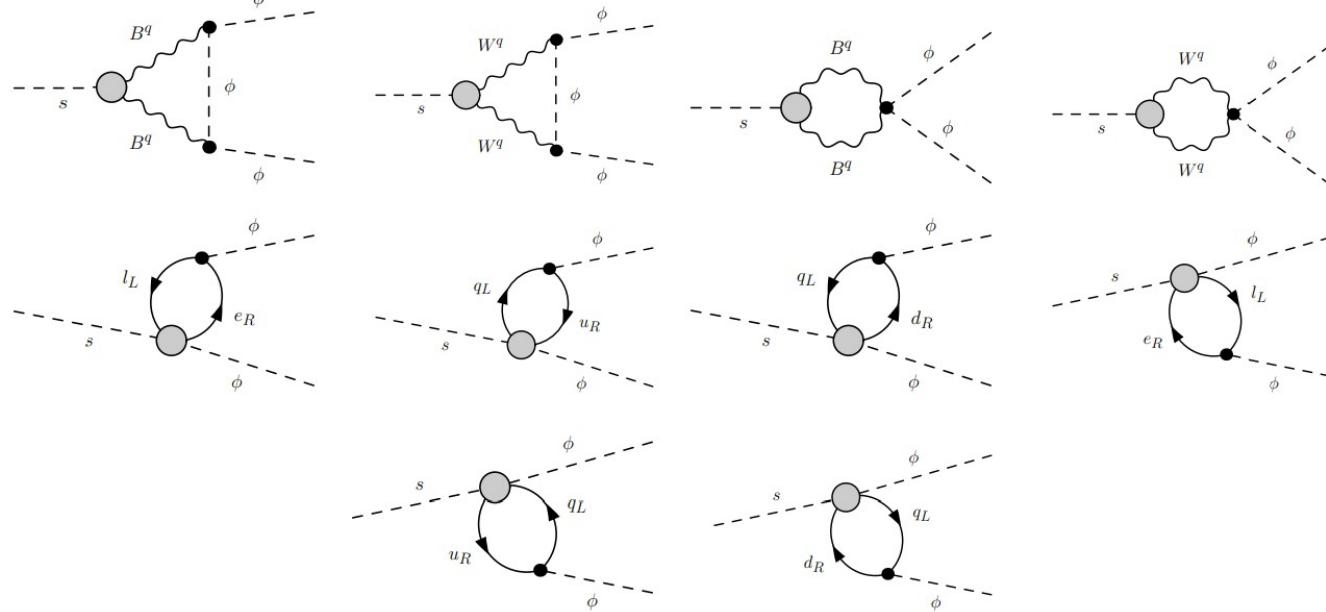
T. Hahn and M. Perez-Victoria  
[hep-ph/9807565](#)

**Manual check:** FeynRules + QGRAF

A. Alloul, N. D. Christensen,  
C. Degrande,  
C. Duhr, B. Fuks, [1310.1921](#) P. Nogueira, JCP  
105 (1993) 279

# SMEFT+ALP: removing redundancies

$$s \rightarrow \phi \phi^\dagger$$



# SMEFT+ALP: removing redundancies

$$i\mathcal{M}_{\text{loop}} = \left\{ \frac{1}{16\pi^2\epsilon} \text{Tr}[y^e a_{se\phi}^T] + 3\text{Tr}[y^d a_{sd\phi}^T - a_{su\phi} y^{u\dagger}] \right\} (\underline{p_2^2 - p_3^2})$$

$$i\mathcal{M}_{EFT} = r_{s\phi\square} (\underline{p_2^2 - p_3^2})$$

$$\boxed{\mathcal{R}_{s\phi\square} \stackrel{\leftrightarrow}{=} i s\phi^\dagger D^2 \phi}$$

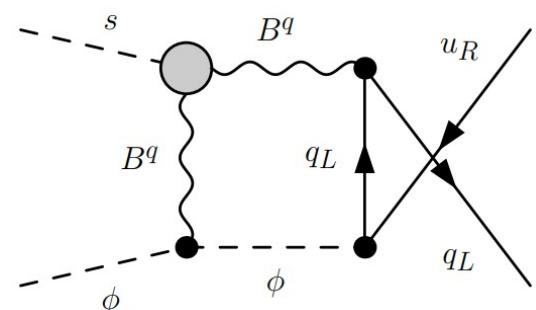
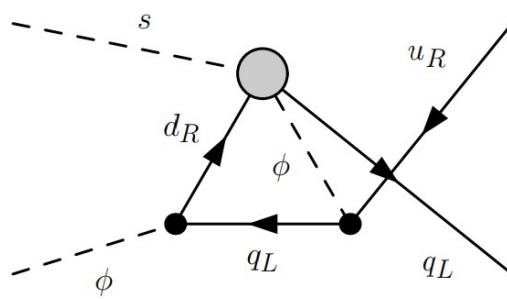
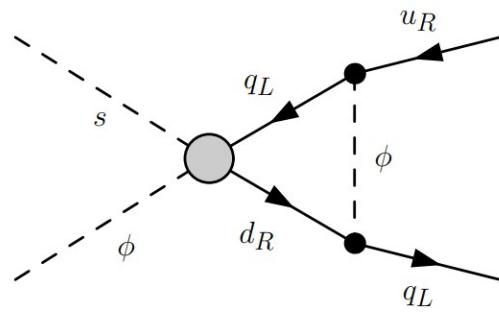


$$r_{s\phi\square} \mathcal{R}_{s\phi\square} = r_{s\phi\square} (\text{Re}(y^u) \mathcal{O}_{su\phi} + \text{Re}(y^d) \mathcal{O}_{sd\phi} + \text{Re}(y^e) \mathcal{O}_{se\phi})$$

# SMEFT+ALP: mixing

$$s\phi^\dagger \rightarrow q_L \bar{u}_R$$

$$\mathcal{O}_{su\phi} = i s \bar{q}_L \tilde{\phi} u_R + h.c.$$



## SMEFT+ALP: RGEs

$$\mathcal{L}_{div} = \mathcal{O}_n a'_n \equiv \mathcal{O}_n \frac{C_{nm}}{32\pi^2\epsilon} a_m$$

dim-4 couplings

$$\beta_{a_n} = 16\pi^2 \mu \frac{da_n}{d\mu} = \gamma_{nm} a_m$$

anomalous dimension matrix (AD matrix)

$$\gamma_{nm} = -(\mathcal{C}_{nm} + K_n^F \delta_{nm})$$

$$Z_n^F = 1 + \frac{K_n^F}{32\pi^2\epsilon}$$

Wave function renormalization

# SMEFT+ALP: AD matrix

$$\begin{pmatrix}
 \beta_{a_{su\phi}^\alpha} \\
 \beta_{a_{sd\phi}^\alpha} \\
 \beta_{a_{se\phi}^\alpha} \\
 \beta_{a_{s\tilde{G}}} \\
 \beta_{a_{s\tilde{W}}} \\
 \beta_{a_{s\tilde{B}}}
 \end{pmatrix} = \begin{pmatrix}
 \gamma_{11} + 6y_u^\alpha y_u^\rho & y_d^\alpha y_u^\alpha - 6y_u^\alpha y_d^\rho & -2y_u^\alpha y_e^\rho & -32g_3^2 y_u^\alpha & -9g_2^2 y_u^\alpha & -\frac{17}{3}g_1^2 y_u^\alpha \\
 y_u^\alpha y_d^\alpha - 6y_d^\alpha y_u^\rho & \gamma_{22} + 6y_d^\alpha y_d^\rho & 2y_d^\alpha y_e^\rho & -32g_3^2 y_d^\alpha & -9g_2^2 y_d^\alpha & -\frac{5}{3}g_1^2 y_d^\alpha \\
 -6y_e^\alpha y_u^\rho & 6y_e^\alpha y_d^\rho & \gamma_{33} + 2y_e^\alpha y_e^\rho & 0 & -9g_2^2 y_e^\alpha & -15g_1^2 y_e^\alpha \\
 0 & 0 & 0 & -14g_3^2 & 0 & 0 \\
 0 & 0 & 0 & 0 & -\frac{19}{3}g_2^2 & 0 \\
 0 & 0 & 0 & 0 & 0 & \frac{41}{3}g_1^2
 \end{pmatrix} \begin{pmatrix}
 a_{su\phi}^\rho \\
 a_{sd\phi}^\rho \\
 a_{se\phi}^\rho \\
 a_{s\tilde{G}} \\
 a_{s\tilde{W}} \\
 a_{s\tilde{B}}
 \end{pmatrix}$$

The matrix equation shows the relationship between the parameters  $\beta_{a_{su\phi}^\alpha}$ ,  $\beta_{a_{sd\phi}^\alpha}$ ,  $\beta_{a_{se\phi}^\alpha}$ ,  $\beta_{a_{s\tilde{G}}}$ ,  $\beta_{a_{s\tilde{W}}}$ , and  $\beta_{a_{s\tilde{B}}}$  on the left and the coefficients  $a_{su\phi}^\rho$ ,  $a_{sd\phi}^\rho$ ,  $a_{se\phi}^\rho$ ,  $a_{s\tilde{G}}$ ,  $a_{s\tilde{W}}$ , and  $a_{s\tilde{B}}$  on the right. A red dashed horizontal line separates the first three rows from the last three rows of the matrix.

# SMEFT+ALP: AD matrix

$$\begin{pmatrix}
 \beta_{a_{su\phi}^\alpha} \\
 \beta_{a_{sd\phi}^\alpha} \\
 \beta_{a_{se\phi}^\alpha} \\
 \beta_{a_{s\tilde{G}}} \\
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 -6y_e^\alpha y_u^\rho & 6y_e^\alpha y_d^\rho & \gamma_{33} + 2y_e^\alpha y_e^\rho & 0 & -9g_2^2 y_e^\alpha & -15g_1^2 y_e^\alpha \\
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 a_{s\tilde{G}} \\
 a_{s\tilde{W}} \\
 a_{s\tilde{B}}
 \end{pmatrix}$$

**Nonrenormalization theorems**

C. Cheung and C.-H. Shen, 1505.01844

# SMEFT+ALP: AD matrix

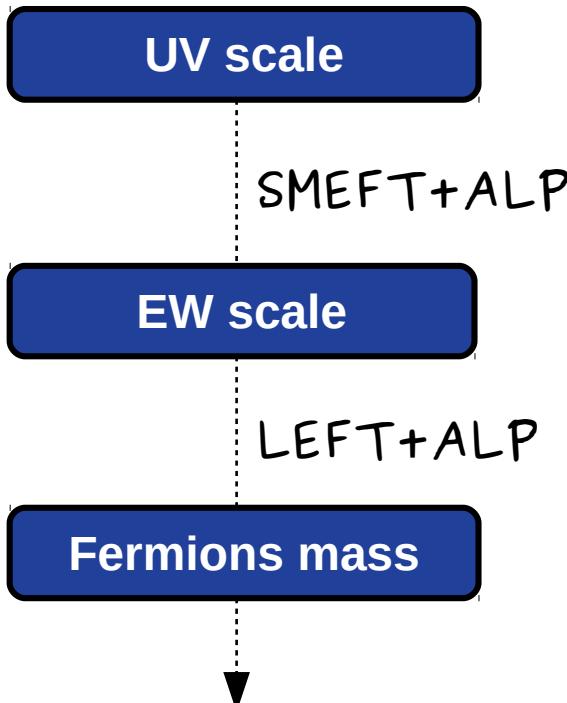
$$\begin{pmatrix}
 \beta_{a_{su\phi}^\alpha} \\
 \beta_{a_{sd\phi}^\alpha} \\
 \beta_{a_{se\phi}^\alpha} \\
 \beta_{a_{s\tilde{G}}} \\
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 a_{s\tilde{B}}
 \end{pmatrix}$$

**Nonrenormalization theorems**

C. Cheung and C.-H. Shen, 1505.01844

$g_3^2 C_{G\tilde{G}} \mathcal{O}_{sG\tilde{G}}$

# LEFT - below EW scale



## Below the electroweak scale:

- Write most general LEFT+ALP (without W, Z, H and top quark)
- Match to SMEFT+ALP

See also M. Bauer, M. Neubert, S. Renner, M. Schnubel, A. Thamm, 2012.12.272

- Integrate out fermions as mass thresholds are passed

# LEFT: independent basis

$$\begin{aligned}
\mathcal{L}_{\text{LEFT}} = & \frac{1}{2}(\partial_\mu s)(\partial^\mu s) - \frac{1}{2}\tilde{m}^2 s^2 - \frac{\tilde{\lambda}_s}{4!}s^4 - \frac{1}{4}A_{\mu\nu}A^{\mu\nu} - \frac{1}{4}G_{\mu\nu}^A G^{A\mu\nu} \\
& + \sum_{\psi=u,d,e} \left\{ \overline{\psi^\alpha} i \not{D} \psi^\alpha - \left[ (\tilde{m}_\psi)_{\alpha\beta} \overline{\psi_L^\alpha} \psi_R^\beta - s i (\tilde{c}_\psi)_{\alpha\beta} \overline{\psi_L^\alpha} \psi_R^\beta + \text{h.c.} \right] \right\} \\
& + \underbrace{\tilde{a}_{s\tilde{G}} s G_{\mu\nu}^A \tilde{G}^{A\mu\nu} + \tilde{a}_{s\tilde{A}} s A_{\mu\nu} \tilde{A}^{\mu\nu}}_{\text{dim-5 purely SMEFT}} \\
& + \sum_{\psi=u,d,e} \left\{ (\tilde{a}_{\psi A})_{\alpha\beta} \overline{\psi_L^\alpha} \sigma^{\mu\nu} \psi_R^\beta A_{\mu\nu} + (\tilde{a}_{\psi G})_{\alpha\beta} \overline{\psi_L^\alpha} \sigma^{\mu\nu} T_A \psi_R^\beta G_{\mu\nu}^A + s^2 (\tilde{a}_\psi)_{\alpha\beta} \overline{\psi_L^\alpha} \psi_R^\beta + \text{h.c.} \right\}
\end{aligned}$$

c: dim-4

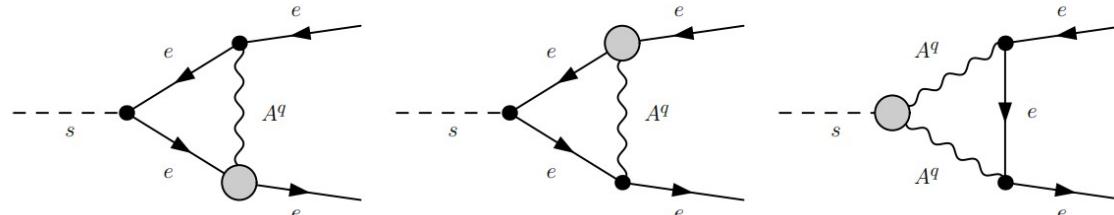
a: dim-5

# LEFT: masses

Effective operators can renormalize **lower** dimension operators:

$$\begin{aligned}
 \beta_{\tilde{c}_e} = & -6\tilde{e}^2\tilde{c}_e + 3\tilde{c}_e\tilde{c}_e^\dagger\tilde{c}_e + 2\left[\text{Tr}(\tilde{c}_e\tilde{c}_e^\dagger) + 6\text{Tr}(\tilde{c}_d\tilde{c}_d^\dagger) + 6\text{Tr}(\tilde{c}_u\tilde{c}_u^\dagger)\right]\tilde{c}_e \\
 & -8\left[3\tilde{e}^2\tilde{a}_{s\tilde{A}}\right]\tilde{m}_e + 2\left[\tilde{a}_e\left(\tilde{c}_e^\dagger\tilde{m}_e - 2\tilde{m}_e^\dagger\tilde{c}_e\right) + \left(\tilde{m}_e\tilde{c}_e^\dagger - 2\tilde{c}_e\tilde{m}_e^\dagger\right)\tilde{a}_e\right] \\
 & -12\tilde{e}\left[\tilde{m}_e\tilde{c}_e^\dagger\tilde{a}_{eA} + \tilde{a}_{eA}\tilde{c}_e^\dagger\tilde{m}_e - \tilde{c}_e\tilde{m}_e^\dagger\tilde{a}_{eA} - \tilde{a}_{eA}\tilde{m}_e^\dagger\tilde{c}_e\right];
 \end{aligned}$$

dim-4 contributions  
 dim-5 contributions



$$\tilde{a}_{s\tilde{A}} s A_{\mu\nu} \tilde{A}^{\mu\nu}$$

$$\tilde{a}_\psi \bar{\psi} \sigma^{\mu\nu} \psi A_{\mu\nu}$$

# LEFT: ALP-gauge couplings

$$\tilde{a}_{s\tilde{A}} s A_{\mu\nu} \tilde{A}^{\mu\nu}$$

$$\tilde{a}_{\psi A} \bar{\psi} \sigma^{\mu\nu} \psi A_{\mu\nu}$$

$$\begin{aligned} \beta_{\tilde{a}_{s\tilde{A}}} &= 4\tilde{e}\text{Tr} \left[ \left( \tilde{c}_e \underline{\tilde{a}_{eA}^\dagger} + \tilde{c}_e^\dagger \underline{\tilde{a}_{eA}} \right) + \left( \tilde{c}_d \underline{\tilde{a}_{dA}^\dagger} + \tilde{c}_d^\dagger \underline{\tilde{a}_{dA}} \right) - 2 \left( \tilde{c}_u \underline{\tilde{a}_{uA}^\dagger} + \tilde{c}_u^\dagger \underline{\tilde{a}_{uA}} \right) \right] \\ &+ 2\text{Tr} \left[ \tilde{c}_e \tilde{c}_e^\dagger + 3 \left( \tilde{c}_d \tilde{c}_d^\dagger + \tilde{c}_u \tilde{c}_u^\dagger \right) \right] \tilde{a}_{s\tilde{A}} + \frac{8}{3} \tilde{e}^2 \left[ n_\ell + \frac{1}{3} n_d + \frac{4}{3} n_u \right] \tilde{a}_{s\tilde{A}}, \end{aligned}$$

**NEW pheno: ALP-gauge boson couplings no longer run only proportional to itself.** They can be generated by dipole operator

# LEFT: ALP-gauge couplings

$$\beta_{\tilde{a}_{s\tilde{A}}} = 4\tilde{e}\text{Tr} \left[ \left( \tilde{c}_e \underline{\tilde{a}_{eA}^\dagger} + \tilde{c}_e^\dagger \underline{\tilde{a}_{eA}} \right) + \left( \tilde{c}_d \underline{\tilde{a}_{dA}^\dagger} + \tilde{c}_d^\dagger \underline{\tilde{a}_{dA}} \right) - 2 \left( \tilde{c}_u \underline{\tilde{a}_{uA}^\dagger} + \tilde{c}_u^\dagger \underline{\tilde{a}_{uA}} \right) \right]$$

$$+ 2\text{Tr} \left[ \tilde{c}_e \tilde{c}_e^\dagger + 3 \left( \tilde{c}_d \tilde{c}_d^\dagger + \tilde{c}_u \tilde{c}_u^\dagger \right) \right] \tilde{a}_{s\tilde{A}} + \frac{8}{3} \tilde{e}^2 \left[ n_\ell + \frac{1}{3} n_d + \frac{4}{3} n_u \right] \tilde{a}_{s\tilde{A}},$$

Result of integrating out fermions

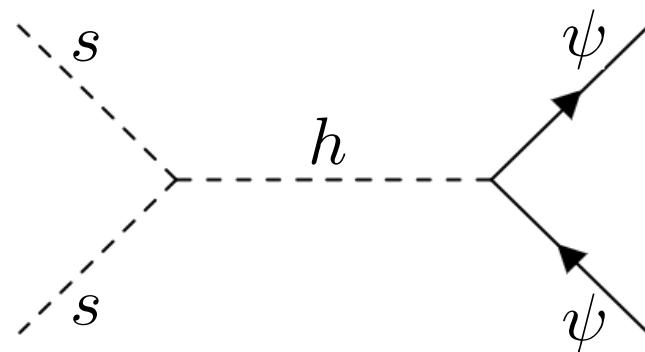
**NEW pheno: ALP-gauge boson couplings no longer run only proportional to itself.** They can be generated by dipole operator

$$\tilde{a}_{s\tilde{A}} s A_{\mu\nu} \tilde{A}^{\mu\nu}$$

$$\tilde{a}_{\psi A} \bar{\psi} \sigma^{\mu\nu} \psi A_{\mu\nu}$$

# LEFT: matching to SMEFT+ALP

The SMEFT+ALP alone does not generate all couplings, for example:



$$\sim \lambda_{s\phi} \frac{y^\psi}{v} \sim \lambda_{s\phi} \frac{m_\psi}{v^2}$$

higher order in the low energy  
power counting

Different completions above EW could generate them

# Phenomenological applications

## Photophobic ALP:

N. Craig, A. Hook and S. Kasko, 1805.06538

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2} \partial_\mu s \partial^\mu s + \frac{1}{2} \tilde{m}^2 s^2 + \frac{a_{s\tilde{Z}}}{c_\omega^2 - s_\omega^2} s \left( c_\omega^2 W_{\mu\nu} \widetilde{W}^{\mu\nu} - s_\omega^2 B_{\mu\nu} \widetilde{B}^{\mu\nu} \right)$$

### Direct constraints from mono-Z:

$$a_{s\tilde{Z}} < 0.2 \text{ TeV}^{-1}$$

@LHC Run II

$$a_{s\tilde{Z}} < 0.04 \text{ TeV}^{-1}$$

@LHC-HL

I. Brivio, M. Gavela,  
L. Merlo, K. Mimasu,  
J. No, R. del Rey  
and V. Sanz,  
1701.05379

# Phenomenological applications

The ALP-Z coupling generates the electron coupling through running:

$$\begin{aligned}\beta_{a_{se\phi}} = & 2 \left[ a_{se\phi} \left( \lambda_{s\phi} - \frac{15g_1^2}{8} - \frac{9g_2^2}{8} + \frac{1}{2}\gamma_\phi^{(Y)} \right) + \frac{5}{4}y^e y^{e\dagger} a_{se\phi} + a_{se\phi} y^{e\dagger} y^e \right. \\ & \left. - \left( \frac{15g_1^2}{2} a_{s\tilde{B}} + \frac{9g_2^2}{2} a_{s\tilde{W}} - \text{Tr} [y^e a_{se\phi}^\top + 3y^d a_{sd\phi}^\top - 3a_{su\phi} y^{u\dagger})] \right) y^e \right]\end{aligned}$$

**Strong constraints on the ALP-electron coupling through Red Giant cooling @KeV**

# Phenomenological applications

**Translate** the **ALP-ee** bound into an **ALP-ZZ** bound:

- Run LEFT coupling to electron up to EW scale  
(plus, match at fermion masses)
- Match at electroweak scale to get bound on  $a_{se\phi}$
- Compute ALP-Z coupling at high energy whose running generates the bound on  $a_{se\phi}$

$$a_{s\tilde{Z}} < 4.8 \times 10^{-6} \text{ TeV}^{-1} \quad \text{vs} \quad a_{s\tilde{Z}} < 0.04 \text{ TeV}^{-1}$$

# Phenomenological applications

**Top-philic ALP:**

$$\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{1}{2}\partial_\mu s \partial^\mu s + \frac{1}{2}\tilde{m}^2 s^2 + a_t s [i\bar{q}_L \tilde{\phi} t_R + \text{h.c.}]$$

J. Ebadi, S. Khatibi and M. M. Najafabadi, 1901.03061

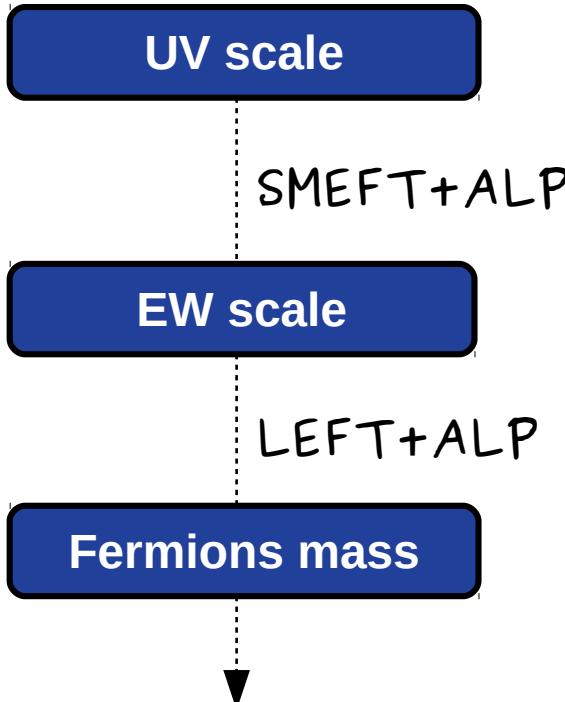
$$a_t \lesssim \text{TeV}^{-1}$$

indirect bound

$$a_t < 4.3 \times 10^{-6} \text{ TeV}^{-1}$$

vs  
RGE constraint

# Conclusions



- Important to use RGEs to correctly interpret experimental bounds
- Mixing effects can have significant contributions
- LEFT running can lead to interesting new pheno results

# Thanks

gguedes@lip.pt

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FCT, COMPETE2020-Portugal2020, FEDER, POCI-01-0145-FEDER-007334

# Back-up slides

# Periodic Axion

**Starting from a periodic axion:**

$$\mathcal{L} \supset \partial_\mu(s) (\bar{\ell}_L k_L \gamma^\mu \ell_L + \bar{\ell}_R k_R \gamma^\mu \ell_R) + \sum_{n \in Z} (M_n \bar{\ell}_R e^{(ina/f_a)} \ell_L + \text{h.c.})$$

$$+ c_{gg} \frac{\alpha_s}{8\pi} a G_{\mu\nu}^a \tilde{G}^{a\mu\nu} + c_{\gamma\gamma} \frac{\alpha}{4\pi} a A_{\mu\nu} \tilde{A}^{\mu\nu}$$

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