



含径向/轨道激发全重 四夸克态质量谱

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第七届XYZ粒子研讨会（青岛）



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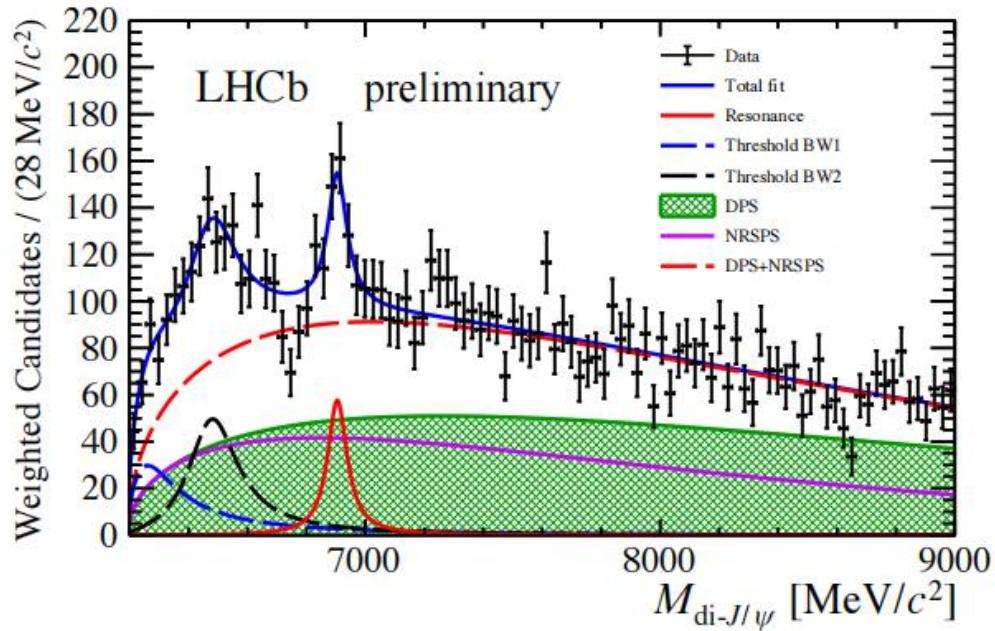


研究背景

第七届XYZ粒子研讨会（青岛）

研究背景

LHCb Collaboration, Science Bulletin 65 (2020) 1983–1993



工作：

M. S. Liu, F. X. Liu, X. H. Zhong, Q. Zhao, arXiv: 2006.11952

F. X. Liu, M. S. Liu, X. H. Zhong, Q. Zhao, Phys. Rev. D 103, 016016



夸克模型与波函数分类

第七届XYZ粒子研讨会（青岛）



夸克模型

哈密顿量: $H = T + \sum_{i < j} (V_{ij}^{Conf} + V_{ij}^{Coul}) + \sum_{i < j} (V_{ij}^{SS} + V_{ij}^{LS} + V_{ij}^{Ten})$

参数:

m_c (GeV)	1.483
m_b (GeV)	4.852
α_{cc}	0.5461
α_{bb}	0.4311
σ_{cc} (GeV)	1.1384
σ_{bb} (GeV)	2.3200
b (GeV ²)	0.1425

W. J. Deng, H. Liu, L. C. Gui and X. H. Zhong, Phys. Rev. D 95, 034026.

Q. Li, M. S. Liu, L. S. Lu, Q. F. L, L. C. Gui, and X. H. Zhong, Phys. Rev. D 99, 096020.



波函数分类：

味道空间：

对称 $\{\{qq\} \ \{\bar{q}\bar{q}\}\}$

颜色空间：

对称 $|6\bar{6}\rangle^c : \left\{ \{qq\}^6 \{\bar{q}\bar{q}\}^6 \right\}$

反对称 $|\bar{3}3\rangle^c : \left\{ \{qq\}^3 \{\bar{q}\bar{q}\}^3 \right\}$

自旋空间：(S-S耦合)

$qq (\bar{q}\bar{q})$ 对称 $s=1$, 反对称 $s=0$ 。

$\{\{qq\}_{s=0} \ \{\bar{q}\bar{q}\}_{s=0}\}_{S=0}$

$\{\{qq\}_{s=0} \ \{\bar{q}\bar{q}\}_{s=1}\}_{S=1}$

$\{\{qq\}_{s=1} \ \{\bar{q}\bar{q}\}_{s=0}\}_{S=1}$

$\{\{qq\}_{s=1} \ \{\bar{q}\bar{q}\}_{s=1}\}_{S=0,1,2}$

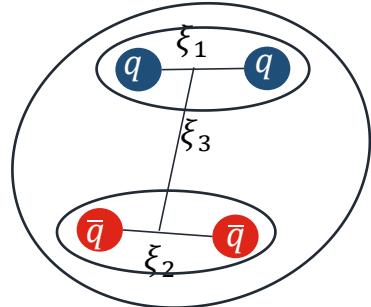
波函数分类：

自旋空间：

$$\begin{aligned}
 1 \quad \chi_{00}^{00} &= \frac{1}{2} (\downarrow\uparrow\downarrow\uparrow - \downarrow\uparrow\uparrow\downarrow - \uparrow\downarrow\downarrow\uparrow + \uparrow\downarrow\uparrow\downarrow) \\
 2 \quad \chi_{11}^{10} &= \frac{1}{\sqrt{2}} (-\uparrow\uparrow\downarrow\uparrow + \uparrow\uparrow\uparrow\downarrow) \\
 3 \quad \chi_{10}^{10} &= \frac{1}{2} (-\downarrow\uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow\downarrow - \uparrow\downarrow\downarrow\uparrow + \uparrow\downarrow\uparrow\downarrow) \\
 4 \quad \chi_{1-1}^{10} &= \frac{1}{\sqrt{2}} (\downarrow\downarrow\uparrow\downarrow - \downarrow\downarrow\downarrow\uparrow) \\
 5 \quad \chi_{11}^{01} &= \frac{1}{\sqrt{2}} (\uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \\
 6 \quad \chi_{10}^{01} &= \frac{1}{2} (\uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\downarrow\uparrow - \downarrow\uparrow\downarrow\uparrow) \\
 7 \quad \chi_{1-1}^{01} &= \frac{1}{\sqrt{2}} (\uparrow\downarrow\downarrow\downarrow - \downarrow\uparrow\downarrow\downarrow) \\
 8 \quad \chi_{00}^{11} &= \frac{1}{\sqrt{12}} (2\uparrow\uparrow\downarrow\downarrow - \uparrow\downarrow\uparrow\downarrow - \downarrow\uparrow\uparrow\downarrow - \uparrow\downarrow\downarrow\uparrow - \downarrow\uparrow\downarrow\uparrow + 2\downarrow\downarrow\uparrow\uparrow) \\
 9 \quad \chi_{11}^{11} &= \frac{1}{2} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow - \uparrow\downarrow\uparrow\uparrow - \downarrow\uparrow\uparrow\uparrow) \\
 10 \quad \chi_{10}^{11} &= \frac{1}{\sqrt{2}} (\uparrow\uparrow\downarrow\downarrow - \downarrow\downarrow\uparrow\uparrow) \\
 11 \quad \chi_{1-1}^{11} &= \frac{1}{2} (\uparrow\downarrow\downarrow\downarrow + \downarrow\uparrow\downarrow\downarrow - \downarrow\downarrow\uparrow\downarrow - \downarrow\downarrow\downarrow\uparrow) \\
 12 \quad \chi_{22}^{11} &= \uparrow\uparrow\uparrow\uparrow \\
 13 \quad \chi_{21}^{11} &= \frac{1}{2} (\uparrow\uparrow\uparrow\downarrow + \uparrow\uparrow\downarrow\uparrow + \uparrow\downarrow\uparrow\uparrow + \downarrow\uparrow\uparrow\uparrow) \\
 14 \quad \chi_{20}^{11} &= \frac{1}{\sqrt{6}} (\uparrow\uparrow\downarrow\downarrow + \uparrow\downarrow\uparrow\downarrow + \downarrow\uparrow\uparrow\downarrow + \uparrow\downarrow\downarrow\uparrow + \downarrow\uparrow\downarrow\uparrow + \downarrow\downarrow\uparrow\uparrow) \\
 15 \quad \chi_{2-1}^{11} &= \frac{1}{2} (\uparrow\downarrow\downarrow\downarrow + \downarrow\uparrow\downarrow\downarrow + \downarrow\downarrow\uparrow\downarrow + \downarrow\downarrow\downarrow\uparrow) \\
 16 \quad \chi_{2-2}^{11} &= \downarrow\downarrow\downarrow\downarrow
 \end{aligned}$$

波函数分类:

坐标空间: (L-L耦合)



		$ _{\xi_1}$	$ _{\xi_2}$	$ _{\xi_3}$	L
2S		0	0	0	0
1P	ξ_1	1	0	0	1
	ξ_2	0	1	0	1
	ξ_3	0	0	1	1
1D	ξ_1	2	0	0	2
	ξ_2	0	2	0	2
	ξ_3	0	0	2	2
	$\xi_1 \otimes \xi_3$	1	0	1	0,1,2
	$\xi_2 \otimes \xi_3$	0	1	1	0,1,2
	$\xi_1 \otimes \xi_2$	1	1	0	0,1,2

波函数分类：

依据置换对称性、 J^{PC} 量子数的要求构造总波函数。

4个1S态

0^{++}	J_{00}^{00}	:	$\psi_{000}^{1S} \chi_{00}^{00}$	$ 6\bar{6}\rangle^c$
	J_{00}^{00}	:	$\psi_{000}^{1S} \chi_{00}^{11}$	$ \bar{3}3\rangle^c$
1^{+-}	J_{11}^{01}	:	$\psi_{000}^{1S} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{02}	:	$\psi_{000}^{1S} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$

12个2S态

0^{+-}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} - \psi_{100}^{\xi_2})$	χ_{00}^{00}	$ 6\bar{6}\rangle^c$
0^{+-}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} - \psi_{100}^{\xi_2})$	χ_{00}^{11}	$ \bar{3}3\rangle^c$
0^{++}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} + \psi_{100}^{\xi_2})$	χ_{00}^{00}	$ 6\bar{6}\rangle^c$
0^{++}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} + \psi_{100}^{\xi_2})$	χ_{00}^{11}	$ \bar{3}3\rangle^c$
0^{++}	$\psi_{100}^{\xi_3}$	χ_{00}^{00}	$ 6\bar{6}\rangle^c$
0^{++}	$\psi_{100}^{\xi_3}$	χ_{00}^{11}	$ \bar{3}3\rangle^c$

1^{+-}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} - \psi_{100}^{\xi_2})$	χ_{11}^{11}	$ \bar{3}3\rangle^c$
1^{+-}	$\psi_{100}^{\xi_3}$	χ_{11}^{11}	$ \bar{3}3\rangle^c$
1^{++}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} + \psi_{100}^{\xi_2})$	χ_{11}^{11}	$ \bar{3}3\rangle^c$
2^{+-}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} - \psi_{100}^{\xi_2})$	χ_{22}^{11}	$ \bar{3}3\rangle^c$
2^{++}	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} + \psi_{100}^{\xi_2})$	χ_{22}^{11}	$ \bar{3}3\rangle^c$
2^{++}	$\psi_{100}^{\xi_3}$	χ_{22}^{11}	$ \bar{3}3\rangle^c$



波函数分类：

20个1P态

0^{--}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1} \chi_{1-1}^{10} - \psi_{010}^{\xi_1} \chi_{10}^{10} + \psi_{01-1}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{1-1}^{01} + \psi_{010}^{\xi_2} \chi_{10}^{01} - \psi_{01-1}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
0^{--}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1} \chi_{1-1}^{01} - \psi_{010}^{\xi_1} \chi_{10}^{01} + \psi_{01-1}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{1-1}^{10} + \psi_{010}^{\xi_2} \chi_{10}^{10} - \psi_{01-1}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
0^{-+}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1} \chi_{1-1}^{10} - \psi_{010}^{\xi_1} \chi_{10}^{10} + \psi_{01-1}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{1-1}^{01} - \psi_{010}^{\xi_2} \chi_{10}^{01} + \psi_{01-1}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
0^{-+}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1} \chi_{1-1}^{01} - \psi_{010}^{\xi_1} \chi_{10}^{01} + \psi_{01-1}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{1-1}^{10} - \psi_{010}^{\xi_2} \chi_{10}^{10} + \psi_{01-1}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
0^{-+}	J_{00}^{11}	$\sqrt{\frac{1}{3}} \left(\psi_{011}^{\xi_3} \chi_{1-1}^{11} - \psi_{010}^{\xi_3} \chi_{10}^{11} + \psi_{01-1}^{\xi_3} \chi_{11}^{11} \right)$	$ \bar{3}3\rangle^c$
1^{--}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1} \chi_{10}^{10} - \psi_{010}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{10}^{01} + \psi_{010}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
1^{--}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1} \chi_{10}^{01} - \psi_{010}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{10}^{10} + \psi_{010}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
1^{--}	J_{11}^{12}	$\sqrt{\frac{1}{10}} \psi_{011}^{\xi_3} \chi_{20}^{11} - \sqrt{\frac{3}{10}} \psi_{010}^{\xi_3} \chi_{21}^{11} + \sqrt{\frac{3}{5}} \psi_{01-1}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
1^{--}	J_{11}^{10}	$\psi_{011}^{\xi_3} \chi_{00}^{00}$	$ 6\bar{6}\rangle^c$
1^{--}	J_{11}^{10}	$\psi_{011}^{\xi_3} \chi_{00}^{11}$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1} \chi_{10}^{10} - \psi_{010}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{10}^{01} - \psi_{010}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1} \chi_{10}^{01} - \psi_{010}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{10}^{10} - \psi_{010}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{11}	$\sqrt{\frac{1}{2}} \left(\psi_{011}^{\xi_3} \chi_{10}^{11} - \psi_{010}^{\xi_3} \chi_{11}^{11} \right)$	$ \bar{3}3\rangle^c$
2^{--}	J_{22}^{11}	$\sqrt{\frac{1}{2}} \left(\psi_{011}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
2^{--}	J_{22}^{11}	$\sqrt{\frac{1}{2}} \left(\psi_{011}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
2^{--}	J_{22}^{12}	$\sqrt{\frac{1}{3}} \psi_{011}^{\xi_3} \chi_{21}^{11} - \sqrt{\frac{2}{3}} \psi_{010}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
2^{-+}	J_{22}^{11}	$\sqrt{\frac{1}{2}} \left(\psi_{011}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
2^{-+}	J_{22}^{11}	$\sqrt{\frac{1}{2}} \left(\psi_{011}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
2^{-+}	J_{22}^{11}	$\psi_{011}^{\xi_3} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
3^{--}	J_{33}^{12}	$\psi_{011}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$



波函数分类：

80个1D态

0^{+-}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{1-1}^{10} - \psi_{010}^{\xi_1 \xi_3} \chi_{10}^{10} + \psi_{01-1}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{011}^{\xi_2 \xi_3} \chi_{1-1}^{01} + \psi_{010}^{\xi_2 \xi_3} \chi_{10}^{01} - \psi_{01-1}^{\xi_2 \xi_3} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
0^{+-}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{1-1}^{01} - \psi_{010}^{\xi_1 \xi_3} \chi_{10}^{01} + \psi_{01-1}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{011}^{\xi_2 \xi_3} \chi_{1-1}^{10} + \psi_{010}^{\xi_2 \xi_3} \chi_{10}^{10} - \psi_{01-1}^{\xi_2 \xi_3} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
0^{+-}	J_{00}^{22}	$\sqrt{\frac{1}{10}} \left(\psi_{022}^{\xi_1} \chi_{2-2}^{11} - \psi_{021}^{\xi_1} \chi_{2-1}^{11} + \psi_{020}^{\xi_1} \chi_{20}^{11} - \psi_{02-1}^{\xi_1} \chi_{21}^{11} + \psi_{02-2}^{\xi_1} \chi_{22}^{11} - \psi_{022}^{\xi_2} \chi_{2-2}^{11} + \psi_{021}^{\xi_2} \chi_{2-1}^{11} - \psi_{020}^{\xi_2} \chi_{20}^{11} + \psi_{02-1}^{\xi_2} \chi_{21}^{11} - \psi_{02-2}^{\xi_2} \chi_{22}^{11} \right)$	$ \bar{3}3\rangle^c$
0^{++}	J_{00}^{00}	$\psi_{000}^{\xi_1 \xi_2} \chi_{00}^{00}$	$ \bar{3}3\rangle^c$
0^{++}	J_{00}^{00}	$\psi_{000}^{\xi_1 \xi_2} \chi_{00}^{11}$	$ 6\bar{6}\rangle^c$
0^{++}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{1-1}^{10} - \psi_{010}^{\xi_1 \xi_3} \chi_{10}^{10} + \psi_{01-1}^{\xi_1 \xi_3} \chi_{11}^{10} + \psi_{011}^{\xi_2 \xi_3} \chi_{1-1}^{01} - \psi_{010}^{\xi_2 \xi_3} \chi_{10}^{01} + \psi_{01-1}^{\xi_2 \xi_3} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
0^{++}	J_{00}^{11}	$\sqrt{\frac{1}{6}} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{1-1}^{01} - \psi_{010}^{\xi_1 \xi_3} \chi_{10}^{01} + \psi_{01-1}^{\xi_1 \xi_3} \chi_{11}^{01} + \psi_{011}^{\xi_2 \xi_3} \chi_{1-1}^{10} - \psi_{010}^{\xi_2 \xi_3} \chi_{10}^{10} + \psi_{01-1}^{\xi_2 \xi_3} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
0^{++}	J_{00}^{11}	$\sqrt{\frac{1}{3}} \left(\psi_{011}^{\xi_1 \xi_2} \chi_{1-1}^{11} - \psi_{010}^{\xi_1 \xi_2} \chi_{10}^{11} + \psi_{01-1}^{\xi_1 \xi_2} \chi_{11}^{11} \right)$	$ 6\bar{6}\rangle^c$
0^{++}	J_{00}^{22}	$\sqrt{\frac{1}{10}} \left(\psi_{022}^{\xi_1} \chi_{2-2}^{11} - \psi_{021}^{\xi_1} \chi_{2-1}^{11} + \psi_{020}^{\xi_1} \chi_{20}^{11} - \psi_{02-1}^{\xi_1} \chi_{21}^{11} + \psi_{02-2}^{\xi_1} \chi_{22}^{11} - \psi_{022}^{\xi_2} \chi_{2-2}^{11} + \psi_{021}^{\xi_2} \chi_{2-1}^{11} - \psi_{020}^{\xi_2} \chi_{20}^{11} + \psi_{02-1}^{\xi_2} \chi_{21}^{11} - \psi_{02-2}^{\xi_2} \chi_{22}^{11} \right)$	$ \bar{3}3\rangle^c$
0^{++}	J_{00}^{22}	$\sqrt{\frac{1}{5}} \left(\psi_{022}^{\xi_3} \chi_{2-2}^{11} - \psi_{021}^{\xi_3} \chi_{2-1}^{11} + \psi_{020}^{\xi_3} \chi_{20}^{11} - \psi_{02-1}^{\xi_3} \chi_{21}^{11} + \psi_{02-2}^{\xi_3} \chi_{22}^{11} \right)$	$ \bar{3}3\rangle^c$
0^{++}	J_{00}^{22}	$\sqrt{\frac{1}{5}} \left(\psi_{022}^{\xi_1 \xi_2} \chi_{2-2}^{11} - \psi_{021}^{\xi_1 \xi_2} \chi_{2-1}^{11} + \psi_{020}^{\xi_1 \xi_2} \chi_{20}^{11} - \psi_{02-1}^{\xi_1 \xi_2} \chi_{21}^{11} + \psi_{02-2}^{\xi_1 \xi_2} \chi_{22}^{11} \right)$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{01}	$\sqrt{\frac{1}{2}} \left(\psi_{000}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{000}^{\xi_2 \xi_3} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{01}	$\sqrt{\frac{1}{2}} \left(\psi_{000}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{000}^{\xi_2 \xi_3} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{01}	$\psi_{000}^{\xi_1 \xi_2} \chi_{11}^{11}$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{10}	$\psi_{011}^{\xi_1 \xi_2} \chi_{00}^{00}$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{10}	$\psi_{011}^{\xi_1 \xi_2} \chi_{00}^{11}$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{10} - \psi_{010}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{01} + \psi_{010}^{\xi_2 \xi_3} \chi_{11}^{01} \right)$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{11}	$\frac{1}{2} \left(\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{01} - \psi_{010}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{10} + \psi_{010}^{\xi_2 \xi_3} \chi_{11}^{10} \right)$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{12}	$\sqrt{\frac{1}{10}} \psi_{011}^{\xi_1 \xi_2} \chi_{20}^{11} - \sqrt{\frac{3}{10}} \psi_{010}^{\xi_1 \xi_2} \chi_{21}^{11} + \sqrt{\frac{3}{5}} \psi_{011}^{\xi_1 \xi_2} \chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1} \chi_{1-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1} \chi_{10}^{11} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1} \chi_{11}^{11} - \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2} \chi_{1-1}^{01} + \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2} \chi_{10}^{01} - \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2} \chi_{11}^{01}$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{21}	$\sqrt{\frac{3}{5}} \psi_{022}^{\xi_3} \chi_{1-1}^{11} - \sqrt{\frac{3}{10}} \psi_{021}^{\xi_3} \chi_{10}^{11} + \sqrt{\frac{1}{10}} \psi_{020}^{\xi_3} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1 \xi_3} \chi_{1-1}^{10} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1 \xi_3} \chi_{10}^{10} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1 \xi_3} \chi_{11}^{10} - \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2 \xi_3} \chi_{1-1}^{01} + \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2 \xi_3} \chi_{10}^{01} - \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2 \xi_3} \chi_{11}^{01}$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1 \xi_3} \chi_{1-1}^{01} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1 \xi_3} \chi_{10}^{01} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1 \xi_3} \chi_{11}^{01} - \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2 \xi_3} \chi_{1-1}^{10} + \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2 \xi_3} \chi_{10}^{10} - \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2 \xi_3} \chi_{11}^{10}$	$ \bar{3}3\rangle^c$
1^{-+}	J_{11}^{21}	$\sqrt{\frac{3}{5}} \psi_{022}^{\xi_1 \xi_2} \chi_{1-1}^{11} - \sqrt{\frac{3}{10}} \psi_{021}^{\xi_1 \xi_2} \chi_{10}^{11} + \sqrt{\frac{1}{10}} \psi_{020}^{\xi_1 \xi_2} \chi_{11}^{11}$	$ 6\bar{6}\rangle^c$
1^{-+}	J_{11}^{22}	$\sqrt{\frac{1}{10}} \psi_{022}^{\xi_1} \chi_{2-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1} \chi_{20}^{11} + \sqrt{\frac{3}{10}} \psi_{020}^{\xi_1} \chi_{21}^{11} - \sqrt{\frac{1}{10}} \psi_{022}^{\xi_2} \chi_{2-1}^{01} + \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2} \chi_{20}^{01} - \sqrt{\frac{1}{10}} \psi_{020}^{\xi_2} \chi_{21}^{01}$	$ \bar{3}3\rangle^c$



波函数分类：

1^{++}	J_{11}^{01}	$\sqrt{\frac{1}{2}} (\psi_{000}^{\xi_1 \xi_3} \chi_{11}^{10} + \psi_{000}^{\xi_2 \xi_3} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
1^{++}	J_{11}^{01}	$\sqrt{\frac{1}{2}} (\psi_{000}^{\xi_1 \xi_3} \chi_{11}^{01} + \psi_{000}^{\xi_2 \xi_3} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{11}	$\frac{1}{2} (\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{10} - \psi_{010}^{\xi_1 \xi_3} \chi_{11}^{10} + \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{01} - \psi_{010}^{\xi_2 \xi_3} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
1^{++}	J_{11}^{11}	$\frac{1}{2} (\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{01} - \psi_{010}^{\xi_1 \xi_3} \chi_{11}^{01} + \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{10} - \psi_{010}^{\xi_2 \xi_3} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{11}	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_2} \chi_{10}^{11} - \psi_{010}^{\xi_1 \xi_2} \chi_{11}^{11})$	$ 6\bar{6}\rangle^c$
1^{++}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1} \chi_{1-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1} \chi_{11}^{11} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1} \chi_{11}^{11} + \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2} \chi_{1-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2} \chi_{10}^{11} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1 \xi_3} \chi_{1-1}^{10} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1 \xi_3} \chi_{10}^{10} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1 \xi_3} \chi_{11}^{10} + \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2 \xi_3} \chi_{1-1}^{01} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2 \xi_3} \chi_{10}^{01} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2 \xi_3} \chi_{11}^{01}$	$ 6\bar{6}\rangle^c$
1^{++}	J_{11}^{21}	$\sqrt{\frac{3}{10}} \psi_{022}^{\xi_1 \xi_3} \chi_{1-1}^{01} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1 \xi_3} \chi_{10}^{01} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1 \xi_3} \chi_{11}^{01} + \sqrt{\frac{3}{10}} \psi_{022}^{\xi_2 \xi_3} \chi_{1-1}^{10} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_2 \xi_3} \chi_{10}^{10} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_2 \xi_3} \chi_{11}^{10}$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{22}	$\sqrt{\frac{1}{10}} \psi_{022}^{\xi_1} \chi_{2-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1} \chi_{20}^{11} + \sqrt{\frac{1}{20}} \psi_{020}^{\xi_1} \chi_{21}^{11} - \sqrt{\frac{1}{10}} \psi_{022}^{\xi_1} \chi_{2-1}^{11} + \sqrt{\frac{1}{20}} \psi_{021}^{\xi_2} \chi_{20}^{11} + \sqrt{\frac{3}{20}} \psi_{020}^{\xi_2} \chi_{21}^{11} - \sqrt{\frac{1}{10}} \psi_{02-1}^{\xi_2} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{22}	$\sqrt{\frac{1}{5}} \psi_{022}^{\xi_3} \chi_{2-1}^{11} - \sqrt{\frac{3}{10}} \psi_{021}^{\xi_3} \chi_{20}^{11} + \sqrt{\frac{3}{10}} \psi_{020}^{\xi_3} \chi_{21}^{11} - \sqrt{\frac{1}{5}} \psi_{02-1}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
1^{++}	J_{11}^{22}	$\sqrt{\frac{1}{10}} \psi_{022}^{\xi_1 \xi_2} \chi_{2-1}^{11} - \sqrt{\frac{3}{20}} \psi_{021}^{\xi_1 \xi_2} \chi_{20}^{11} + \sqrt{\frac{3}{10}} \psi_{020}^{\xi_1 \xi_2} \chi_{21}^{11} - \sqrt{\frac{1}{5}} \psi_{02-1}^{\xi_1 \xi_2} \chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{11}	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{11}	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
2^{+-}	J_{22}^{12}	$\sqrt{\frac{1}{3}} \psi_{011}^{\xi_1 \xi_2} \chi_{21}^{11} - \sqrt{\frac{2}{3}} \psi_{010}^{\xi_1 \xi_2} \chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{20}	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{00} - \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{00}$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{20}	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{11} - \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{11}$	$ \bar{3}3\rangle^c$
2^{+-}	J_{22}^{21}	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1} \chi_{10}^{11} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1} \chi_{11}^{11} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2} \chi_{10}^{11} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
2^{+-}	J_{22}^{21}	$\sqrt{\frac{2}{3}} \psi_{022}^{\xi_3} \chi_{10}^{11} - \sqrt{\frac{1}{3}} \psi_{021}^{\xi_3} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
2^{+-}	J_{22}^{21}	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{10} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{10} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{01} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{01}$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{21}	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{01} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{01} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{10} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{10}$	$ \bar{3}3\rangle^c$
2^{+-}	J_{22}^{21}	$\sqrt{\frac{2}{3}} \psi_{022}^{\xi_1 \xi_2} \chi_{10}^{11} - \sqrt{\frac{1}{3}} \psi_{021}^{\xi_1 \xi_2} \chi_{11}^{11}$	$ 6\bar{6}\rangle^c$
2^{+-}	J_{22}^{22}	$\sqrt{\frac{2}{14}} \psi_{022}^{\xi_1} \chi_{20}^{11} - \sqrt{\frac{3}{14}} \psi_{021}^{\xi_1} \chi_{21}^{11} + \sqrt{\frac{2}{14}} \psi_{020}^{\xi_1} \chi_{22}^{11} - \sqrt{\frac{2}{14}} \psi_{022}^{\xi_2} \chi_{20}^{11} + \sqrt{\frac{3}{14}} \psi_{021}^{\xi_2} \chi_{21}^{11} - \sqrt{\frac{2}{14}} \psi_{020}^{\xi_2} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{02}	$\psi_{000}^{\xi_1 \xi_2} \chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
2^{++}	J_{22}^{11}	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{10} + \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
2^{++}	J_{22}^{11}	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{01} + \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{11}	$\psi_{011}^{\xi_1 \xi_2} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{20}	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{00} + \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{00}$	$ 6\bar{6}\rangle^c$



波函数分类：

2^{++}	J_{22}^{20}	$\sqrt{\frac{1}{2}}\psi_{022}^{\xi_1}\chi_{00}^{11} + \sqrt{\frac{1}{2}}\psi_{022}^{\xi_2}\chi_{00}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{20}	$\psi_{022}^{\xi_3}\chi_{00}^{00}$	$ 6\bar{6}\rangle^c$
2^{++}	J_{22}^{20}	$\psi_{022}^{\xi_2}\chi_{00}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{20}	$\psi_{022}^{\xi_1\xi_2}\chi_{00}^{00}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{20}	$\psi_{022}^{\xi_1\xi_2}\chi_{00}^{11}$	$ 6\bar{6}\rangle^c$
2^{++}	J_{22}^{21}	$\sqrt{\frac{2}{6}}\psi_{022}^{\xi_1}\chi_{10}^{11} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_1}\chi_{11}^{11} + \sqrt{\frac{2}{6}}\psi_{022}^{\xi_2}\chi_{10}^{11} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_2}\chi_{11}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{21}	$\sqrt{\frac{2}{6}}\psi_{022}^{\xi_1\xi_3}\chi_{10}^{10} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_1\xi_3}\chi_{11}^{10} + \sqrt{\frac{2}{6}}\psi_{022}^{\xi_2\xi_3}\chi_{10}^{01} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_2\xi_3}\chi_{11}^{01}$	$ 6\bar{6}\rangle^c$
2^{++}	J_{22}^{21}	$\sqrt{\frac{2}{6}}\psi_{022}^{\xi_1\xi_3}\chi_{10}^{01} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_1\xi_3}\chi_{11}^{01} + \sqrt{\frac{2}{6}}\psi_{022}^{\xi_2\xi_3}\chi_{10}^{10} - \sqrt{\frac{1}{6}}\psi_{021}^{\xi_2\xi_3}\chi_{11}^{10}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{22}	$\sqrt{\frac{2}{14}}\psi_{022}^{\xi_1}\chi_{20}^{11} - \sqrt{\frac{3}{14}}\psi_{021}^{\xi_1}\chi_{21}^{11} + \sqrt{\frac{2}{14}}\psi_{022}^{\xi_1}\chi_{20}^{11} + \sqrt{\frac{2}{14}}\psi_{021}^{\xi_2}\chi_{21}^{11} - \sqrt{\frac{3}{14}}\psi_{020}^{\xi_2}\chi_{22}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{22}	$\sqrt{\frac{2}{7}}\psi_{022}^{\xi_3}\chi_{20}^{11} - \sqrt{\frac{3}{7}}\psi_{021}^{\xi_3}\chi_{21}^{11} + \sqrt{\frac{2}{7}}\psi_{020}^{\xi_3}\chi_{22}^{11}$	$ \bar{3}3\rangle^c$
2^{++}	J_{22}^{22}	$\sqrt{\frac{2}{7}}\psi_{022}^{\xi_1\xi_2}\chi_{20}^{11} - \sqrt{\frac{3}{7}}\psi_{021}^{\xi_1\xi_2}\chi_{21}^{11} + \sqrt{\frac{2}{7}}\psi_{020}^{\xi_1\xi_2}\chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
3^{+-}	J_{33}^{12}	$\psi_{011}^{\xi_1\xi_2}\chi_{22}^{11}$	$ 6\bar{6}\rangle^c$
3^{+-}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1}\chi_{11}^{11} - \psi_{022}^{\xi_2}\chi_{11}^{11})$	$ \bar{3}3\rangle^c$
3^{+-}	J_{33}^{21}	$\psi_{022}^{\xi_3}\chi_{11}^{11}$	$ \bar{3}3\rangle^c$
3^{+-}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1\xi_3}\chi_{11}^{10} - \psi_{022}^{\xi_2\xi_3}\chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
3^{+-}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1\xi_3}\chi_{11}^{01} - \psi_{022}^{\xi_2\xi_3}\chi_{11}^{10})$	$ \bar{3}3\rangle^c$
3^{+-}	J_{33}^{21}	$\psi_{022}^{\xi_1\xi_2}\chi_{11}^{11}$	$ 6\bar{6}\rangle^c$
3^{+-}	J_{33}^{22}	$\frac{1}{2}(\psi_{022}^{\xi_1}\chi_{21}^{11} - \psi_{021}^{\xi_1}\chi_{22}^{11} - \psi_{022}^{\xi_2}\chi_{21}^{11} + \psi_{021}^{\xi_2}\chi_{22}^{11})$	$ \bar{3}3\rangle^c$
3^{++}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1}\chi_{11}^{11} + \psi_{022}^{\xi_2}\chi_{11}^{11})$	$ \bar{3}3\rangle^c$
3^{++}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1\xi_3}\chi_{11}^{10} + \psi_{022}^{\xi_2\xi_3}\chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
3^{++}	J_{33}^{21}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1\xi_3}\chi_{11}^{01} + \psi_{022}^{\xi_2\xi_3}\chi_{11}^{10})$	$ \bar{3}3\rangle^c$
3^{++}	J_{33}^{22}	$\frac{1}{2}(\psi_{022}^{\xi_1}\chi_{21}^{11} - \psi_{021}^{\xi_1}\chi_{22}^{11} + \psi_{022}^{\xi_2}\chi_{21}^{11} - \psi_{021}^{\xi_2}\chi_{22}^{11})$	$ \bar{3}3\rangle^c$
3^{++}	J_{33}^{22}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1}\chi_{21}^{11} - \psi_{021}^{\xi_1}\chi_{22}^{11})$	$ \bar{3}3\rangle^c$
3^{++}	J_{33}^{22}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1\xi_2}\chi_{21}^{11} - \psi_{021}^{\xi_1\xi_2}\chi_{22}^{11})$	$ 6\bar{6}\rangle^c$
4^{+-}	J_{44}^{22}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1}\chi_{22}^{11} - \psi_{022}^{\xi_2}\chi_{22}^{11})$	$ \bar{3}3\rangle^c$
4^{++}	J_{44}^{22}	$\sqrt{\frac{1}{2}}(\psi_{022}^{\xi_1}\chi_{22}^{11} + \psi_{022}^{\xi_2}\chi_{22}^{11})$	$ \bar{3}3\rangle^c$
4^{++}	J_{44}^{22}	$\psi_{022}^{\xi_3}\chi_{22}^{11}$	$ \bar{3}3\rangle^c$
4^{++}	J_{44}^{22}	$\psi_{022}^{\xi_1\xi_2}\chi_{22}^{11}$	$ 6\bar{6}\rangle^c$



计算方法

第七届XYZ粒子研讨会（青岛）



计算方法

计算质量矩阵元

$$\langle \psi^n | H | \psi^m \rangle = E_m \langle \psi^n | \psi^m \rangle$$

$$\begin{aligned}
& \langle \bar{\psi}^n | H | \bar{\psi}^m \rangle \\
= & \left(\sum_{i=1}^4 m_i \right) \langle \varphi^{c_n} | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
+ & \langle \varphi^{c_n} | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \left(\sum_{i=1}^4 T_i \right) - T_G | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
- & \sum_{i < j} \frac{3}{16} \cdot b_{ij} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | r_{ij} | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
+ & \sum_{i < j} \frac{\alpha_{ij}^{Coul}}{4} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \frac{1}{r_{ij}} | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
- & \sum_{i < j} \frac{2\pi\alpha_{ij}^{SS}}{3m_i m_j} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \frac{\sigma_{ij}^3 e^{-\sigma_{ij}^2 r_{ij}^2}}{\pi^{\frac{3}{2}}} \cdot (\mathbf{s}_i \cdot \mathbf{s}_j) | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
- & \sum_{i < j} \frac{\alpha_{ij}^{ten}}{4m_i m_j} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \frac{1}{r_{ij}^3} \cdot \left[\frac{3(\mathbf{s}_i \cdot \mathbf{r}_{ij})(\mathbf{s}_j \cdot \mathbf{r}_{ij})}{r_{ij}^2} - (\mathbf{s}_i \cdot \mathbf{s}_j) \right] | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
- & \sum_{i < j} \frac{\alpha_{ij}^{SO}}{16} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \frac{1}{r_{ij}^3} \cdot \left[\left(\frac{1}{m_i^2} + \frac{1}{m_j^2} + 4\frac{1}{m_i m_j} \right) \cdot \mathbf{l}_{ij} \cdot (\mathbf{s}_i + \mathbf{s}_j) \right] | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle \\
- & \sum c_{ij} \langle \varphi^{c_n} | \boldsymbol{\lambda}_i \cdot \boldsymbol{\lambda}_j | \varphi^{c_m} \rangle \langle \psi^n \chi^n | \psi^m \chi^m \rangle \langle \phi^f | \phi^f \rangle
\end{aligned}$$



计算方法

试探波函数用一组高斯基展开：

$$\begin{aligned} \prod_{i=1}^3 R_{n_{\xi_i} l_{\xi_i}}(\xi_i) &= \sum_{\ell}^n \sum_{\ell'}^n \sum_{\ell''}^n C_{\xi_1 \ell} C_{\xi_2 \ell'} C_{\xi_3 \ell''} \phi_{n_{\xi_1} l_{\xi_1}}(\omega_{\xi_1 \ell}, \xi_1) \phi_{n_{\xi_2} l_{\xi_2}}(\omega_{\xi_2 \ell'}, \xi_2) \phi_{n_{\xi_3} l_{\xi_3}}(\omega_{\xi_3 \ell''}, \xi_3) \delta_{\ell \ell'} \delta_{\ell' \ell''} \\ &= \sum_{\ell}^n C_{\ell} \phi_{n_{\xi_1} l_{\xi_1}}(\omega_{\ell}, \xi_1) \phi_{n_{\xi_2} l_{\xi_2}}(\omega_{\ell}, \xi_2) \phi_{n_{\xi_3} l_{\xi_3}}(\omega_{\ell}, \xi_3). \end{aligned}$$

$$\phi_{n_{\xi} l_{\xi}}(d_{\xi \ell}, \xi) = \left(\frac{1}{d_{\xi \ell}} \right)^{\frac{3}{2}} \left[\frac{2^{l_{\xi}+2-n_{\xi}} (2l_{\xi} + 2n_{\xi} + 1)!!}{\sqrt{\pi} n_{\xi}! [(2l_{\xi} + 1)!!]^2} \right]^{\frac{1}{2}} \left(\frac{\xi}{d_{\xi \ell}} \right)^{l_{\xi}} \times e^{-\frac{1}{2} \left(\frac{\xi}{d_{\xi \ell}} \right)^2} F \left(-n_{\xi}, l_{\xi} + \frac{3}{2}, \left(\frac{\xi}{d_{\xi \ell}} \right)^2 \right)$$

参数 $d_{\xi l}$ 与谐振子频率 $\omega_{\xi l}$ 的关系： $\frac{1}{d_{\xi l}^2} = M_{\xi} \omega_{\xi l}$

d_l 设为： $d_l = d_1 a^{l-1}$ ($l = 1, \dots, n$)

n 是谐振子函数的个数
 a 是等比系数

计算方法

2S试探波函数展开：

$$\psi_{NLM}(\xi_1, \xi_2, \xi_3)$$

$$= \psi_{nlm}(\xi_1) \psi_{nlm}(\xi_2) \psi_{nlm}(\xi_3)$$

$$= \left[\sum_{l1=1}^n C_l^{(1)} \psi_{nlm}(\omega_l^{(1)} \xi_1) \right] \left[\psi_{nlm}(\omega_l^{(2)} \xi_2) \psi_{nlm}(\omega_l^{(2)} \xi_3) \right]$$

激发态：多高斯展开

基态：单高斯



计算方法

一、求解广义本征值问题-确定质量和波函数

$$\sum_{l'=1}^l (H_{ll'} - EN_{ll'}) C_{l'} = 0$$

二、对角化相同 J^{PC} 量子数质量矩阵获得物理态

eg.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{++}	$1^1S_{0^{++}(6\bar{6})_c}$	$\begin{pmatrix} 6518 & 45 \\ 45 & 6487 \end{pmatrix}$	$\begin{pmatrix} 6455 \\ 6550 \end{pmatrix}$	$\begin{pmatrix} (0.58 & -0.81) \\ (-0.81 & -0.58) \end{pmatrix}$
	$1^1S_{0^{++}(\bar{3}\bar{3})_c}$			

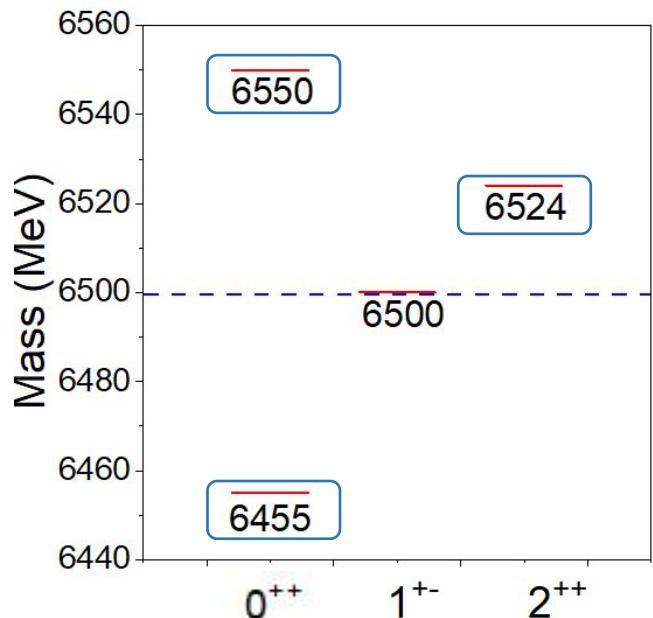


计算结果

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1S质量谱：

$J^P(C)$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{++}	$1^1S_{0^{++}}(6\bar{6})_c$	(6518 45)	(6455)	((0.58 -0.81))
	$1^1S_{0^{++}}(\bar{3}3)_c$	(45 6487)	(6550)	((-0.81 -0.58))
1^{+-}	$1^3S_{1^{+-}}(\bar{3}3)_c$	{ 6500 }	6500	1
2^{++}	$1^5S_{2^{++}}(\bar{3}3)_c$	{ 6524 }	6524	1



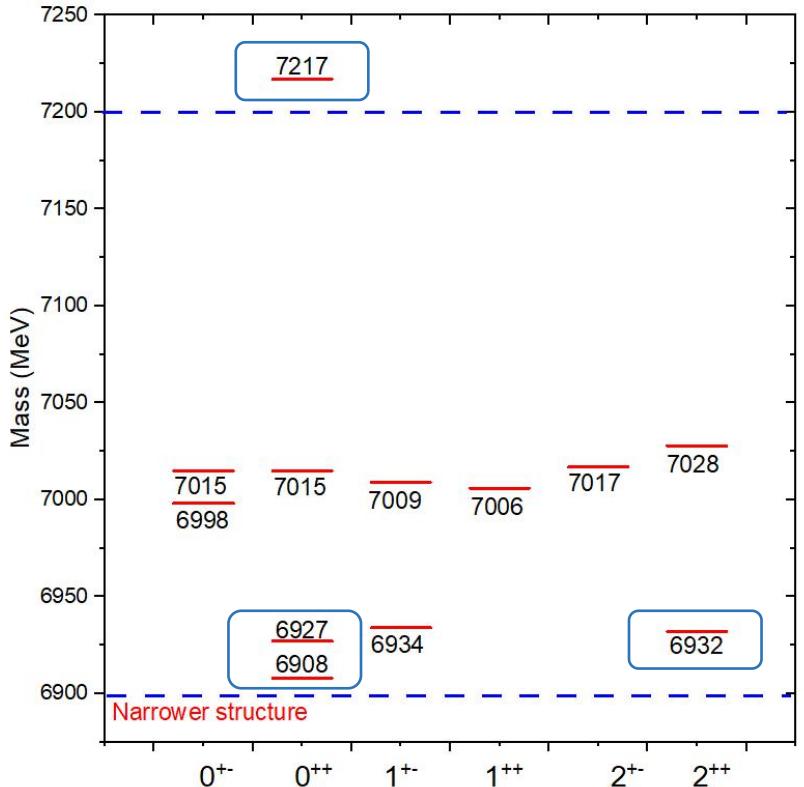
- 1S态的质量分布在6.4GeV~6.6GeV范围内。

- $T_{0^{++}}(6455)$ 、 $T_{0^{++}}(6550)$ 、 $T_{2^{++}}(6524)$ 对(6200-6800)有重要贡献，是X(6500)可能的候选者。

2S激发态质量谱：

$J^P(C)$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{+-}	$2^1S_{0^{+-}(\bar{6}\bar{6})_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 7008 & -8 \\ -8 & 7005 \end{pmatrix}$	$\begin{pmatrix} 6998 \\ 7015 \end{pmatrix}$	$\begin{pmatrix} (-0.63 & -0.78) \\ (-0.78 & 0.63) \end{pmatrix}$
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$			
	$2^1S_{0^{++}(\bar{6}\bar{6})_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 6954 & -19 & 93 & -8 \\ -19 & 7000 & -4 & -33 \end{pmatrix}$	$\begin{pmatrix} 6908 \\ 6927 \end{pmatrix}$	$\begin{pmatrix} (-0.62 & 0.69 & 0.13 & -0.34) \\ (-0.36 & -0.13 & -0.92 & 0.04) \end{pmatrix}$
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 93 & -4 & 7183 & -12 \\ -8 & -33 & -12 & 6930 \end{pmatrix}$	$\begin{pmatrix} 7015 \\ 7217 \end{pmatrix}$	$\begin{pmatrix} (0.18 & -0.28 & -0.07 & -0.94) \\ (-0.67 & -0.65 & 0.35 & 0.04) \end{pmatrix}$
0^{++}	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 7009 & 0 \\ 0 & 6934 \end{pmatrix}$	$\begin{pmatrix} 7009 \\ 6934 \end{pmatrix}$	$\begin{pmatrix} (1 & 0) \\ (0 & 1) \end{pmatrix}$
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$			
1^{+-}	$2^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 7006 \end{pmatrix}$	7006	1
2^{+-}	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 7017 \end{pmatrix}$	7017	1
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\begin{pmatrix} 7018 & -29 \\ -29 & 6942 \end{pmatrix}$	$\begin{pmatrix} 7028 \\ 6932 \end{pmatrix}$	$\begin{pmatrix} (-0.95 & 0.32) \\ (0.32 & -0.95) \end{pmatrix}$
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$			

2S激发态的计算结果



- 2S态的质量分布在6.9GeV~7.3GeV范围内。

- $T_{0^{++}}(6908)$ 、 $T_{0^{++}}(6927)$ 、 $T_{2^{++}}(6932)$ 是X(6900)可能的候选者。

- $T_{0^{++}}(7217)$ 是X(7200)可能的候选者。

2S激发态的计算结果

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$
0^{+-}	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	7008	706	899	-540	10
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7005	776	924	-629	3
	$2^1S_{0^{++}(6\bar{6})_c(\xi_1,\xi_2)}$	6954	725	883	-598	11
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7000	774	919	-622	-4
0^{++}	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	7183	757	1010	-522	7
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	6930	761	876	-642	3
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7009	773	925	-628	7
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	6934	745	885	-634	6
1^{++}	$3^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7006	774	920	-622	2
2^{+-}	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7017	762	932	-624	15
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7018	753	932	-613	14
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	6942	741	888	-633	14

- $\langle T \rangle$ 、 $\langle V^{Lin} \rangle$ 、 $\langle V^{Coul} \rangle$ 对2S态有重要贡献。
- S-S相互作用的贡献很小，但对混合矩阵元有关键影响。

2S激发态的计算结果比较

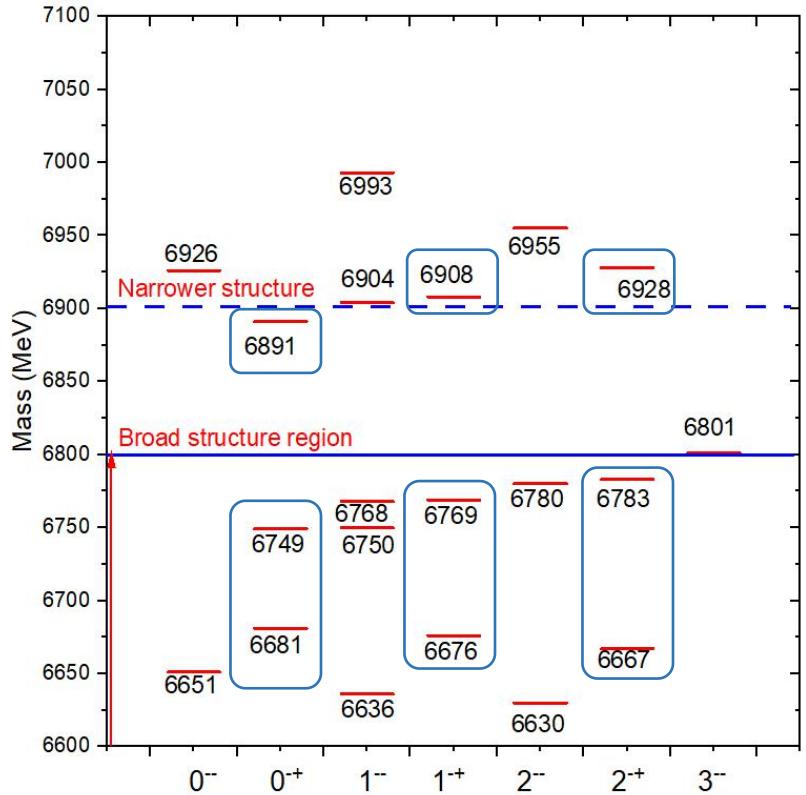
$J^{P(C)}$	Configuration	Mass (MeV)	
		Ours	Q. F. L
0^{+-}	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	(6998)	
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(7015)	
0^{++}	$2^1S_{0^{++}(6\bar{6})_c(\xi_1,\xi_2)}$	(6908)	(6849)
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(6927)	(6940)
1^{+-}	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	(7015)	
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	(7217)	
1^{+-}	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(6934)	(6928)
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	(7009)	
1^{++}	$2^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7006	
2^{+-}	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7017	
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(6932)	(6947)
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	(7028)	

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1P激发态的计算结果

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0 ⁻	$^3P_{0--}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6751 & -132 \\ -132 & 6827 \end{pmatrix}$	$\begin{pmatrix} 6651 \\ 6926 \end{pmatrix}$	$\begin{pmatrix} (-0.80 & -0.60) \\ (-0.6 & 0.80) \end{pmatrix}$
	$^3P_{0--}(\bar{3}3)_c(\xi_1, \xi_2)$			
	$^3P_{0-+}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6746 & 88 & 37 \\ 88 & 6825 & 18 \\ 37 & 18 & 6750 \end{pmatrix}$	$\begin{pmatrix} 6681 \\ 6749 \\ 6891 \end{pmatrix}$	$\begin{pmatrix} (0.82 & -0.47 & -0.32) \\ (-0.14 & 0.38 & 0.91) \\ (0.55 & 0.80 & 0.25) \end{pmatrix}$
0 ⁺	$^3P_{0-+}(\bar{3}3)_c(\xi_1, \xi_2)$			
	$^3P_{1--}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6733 & 132 & -29 & -16 & 31 \\ 132 & 6827 & -14 & -7 & 26 \end{pmatrix}$	$\begin{pmatrix} 6636 \\ 6750 \end{pmatrix}$	$\begin{pmatrix} (0.82 & -0.55 & 0.12 & 0.06 & -0.03) \\ (0.02 & -0.24 & -0.96 & -0.16 & 0.06) \end{pmatrix}$
	$^5P_{1--}(\bar{3}3)_c(\xi_3)$	$\begin{pmatrix} -29 & -14 & 6754 & -3 & 10 \\ -16 & -7 & -3 & 6770 & -19 \end{pmatrix}$	$\begin{pmatrix} 6768 \\ 6904 \\ 6993 \end{pmatrix}$	$\begin{pmatrix} (-0.01 & 0.05 & -0.17 & 0.98 & 0.10) \\ (-0.48 & -0.69 & 0.19 & 0.02 & 0.50) \\ (0.31 & 0.39 & -0.02 & -0.11 & 0.86) \end{pmatrix}$
1 ⁻	$^1P_{1--}(\bar{3}3)_c(\xi_3)$			
	$^1P_{1--}(6\bar{6})_c(\xi_3)$			
	$^3P_{1-+}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6751 & -108 & 9 \\ -108 & 6834 & -4 \\ 9 & -4 & 6769 \end{pmatrix}$	$\begin{pmatrix} 6676 \\ 6769 \\ 6908 \end{pmatrix}$	$\begin{pmatrix} (0.82 & 0.56 & -0.05) \\ (-0.01 & -0.08 & -1.00) \\ (-0.57 & 0.82 & -0.06) \end{pmatrix}$
1 ⁺	$^3P_{1-+}(\bar{3}3)_c(\xi_1, \xi_2)$			
	$^3P_{1-+}(\bar{3}3)_c(\xi_3)$			
	$^3P_{2--}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6746 & -155 & -18 \\ -155 & 6837 & 9 \\ -18 & 9 & 6781 \end{pmatrix}$	$\begin{pmatrix} 6630 \\ 6780 \\ 6955 \end{pmatrix}$	$\begin{pmatrix} (0.80 & 0.59 & 0.06) \\ (-0.01 & 0.12 & -1.00) \\ (-0.60 & 0.80 & 0.10) \end{pmatrix}$
2 ⁻	$^5P_{2--}(\bar{3}3)_c(\xi_3)$			
	$^3P_{2-+}(6\bar{6})_c(\xi_1, \xi_2)$			
	$^3P_{2-+}(\bar{3}3)_c(\xi_3)$			
2 ⁺	$^3P_{2-+}(6\bar{6})_c(\xi_1, \xi_2)$	$\begin{pmatrix} 6754 & 123 & 12 \\ 123 & 6841 & 6 \\ 12 & 6 & 6783 \end{pmatrix}$	$\begin{pmatrix} 6667 \\ 6783 \\ 6928 \end{pmatrix}$	$\begin{pmatrix} (0.82 & -0.57 & -0.06) \\ (0.00 & 0.10 & -1.00) \\ (0.58 & 0.81 & 0.08) \end{pmatrix}$
	$^3P_{2-+}(\bar{3}3)_c(\xi_3)$			
3 ⁻	$^5P_{3--}(\bar{3}3)_c(\xi_3)$	(6801)	6801	1

1P激发态的计算结果



- 1P态的质量分布在6.6GeV~7.0GeV范围内。

- $T_{0-+}(6681)$ 、 $T_{0-+}(6749)$ 、 $T_{1-+}(6676)$ 、 $T_{1-+}(6769)$ 、 $T_{1-+}(6667)$ 、 $T_{1-+}(6783)$ 是X(6500)可能的候选者。

- $T_{0-+}(6891)$ 、 $T_{1-+}(6908)$ 、 $T_{2-+}(6928)$ 是X(6900)可能的候选者。

1P激发态的计算结果

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Conf} \rangle$	$\langle V_{coul}^{OGE} \rangle$	$\langle V_{SS}^{OGE} \rangle$	$\langle V_{tensor}^{OGE} \rangle$	$\langle V_{LS}^{OGE} \rangle$
0--	$^3P_{0--}(6\bar{6})_c(\xi_1,\xi_2)$	6751	717	778	-686	1.62	12.92	-4.31
	$^3P_{0--}(\bar{3}3)_c(\xi_1,\xi_2)$	6827	741	810	-651	0.62	3.04	-9.11
	$^3P_{0-+}(6\bar{6})_c(\xi_1,\xi_2)$	6746	727	773	-691	11.59	-1.48	-4.43
0 ⁺	$^3P_{0-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6825	745	808	-653	4.70	-3.07	-9.21
	$^3P_{0-+}(\bar{3}3)_c(\xi_3)$	6750	765	769	-694	4.22	-6.45	-19.35
	$^3P_{1--}(6\bar{6})_c(\xi_1,\xi_2)$	6733	743	765	-699	1.73	-6.89	-2.30
1 ⁻⁻	$^3P_{1--}(\bar{3}3)_c(\xi_1,\xi_2)$	6827	741	810	-651	0.62	-1.52	-4.55
	$^5P_{1--}(\bar{3}3)_c(\xi_3)$	6754	761	771	-692	15.62	-4.47	-28.76
	$^1P_{1--}(\bar{3}3)_c(\xi_3)$	6770	734	784	-679	-1.38	0	0
1 ⁻⁺	$^1P_{1--}(6\bar{6})_c(\xi_3)$	6968	714	885	-578	13.51	0	0
	$^3P_{1-+}(6\bar{6})_c(\xi_1,\xi_2)$	6751	720	776	-688	11.45	0.73	-2.18
	$^3P_{1-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6834	732	815	-647	4.63	1.49	-4.46
1 ⁺	$^3P_{1-+}(\bar{3}3)_c(\xi_3)$	6769	736	783	-680	4.03	3.01	-9.03
	$^3P_{2--}(6\bar{6})_c(\xi_1,\xi_2)$	6746	724	774	-690	1.65	1.32	2.19
	$^3P_{2--}(\bar{3}3)_c(\xi_1,\xi_2)$	6837	725	819	-644	0.64	0.29	4.38
2 ⁻⁻	$^5P_{2--}(\bar{3}3)_c(\xi_3)$	6781	720	791	-672	14.38	4.05	-8.69
	$^3P_{2-+}(6\bar{6})_c(\xi_1,\xi_2)$	6754	715	779	-685	11.35	-0.14	2.15
	$^3P_{2-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6841	722	821	-642	4.57	-0.29	4.35
2 ⁺	$^3P_{2-+}(\bar{3}3)_c(\xi_3)$	6783	715	794	-670	3.89	-0.57	8.59
	$^5P_{3--}(\bar{3}3)_c(\xi_3)$	6801	692	807	-658	13.55	-1.08	16.20

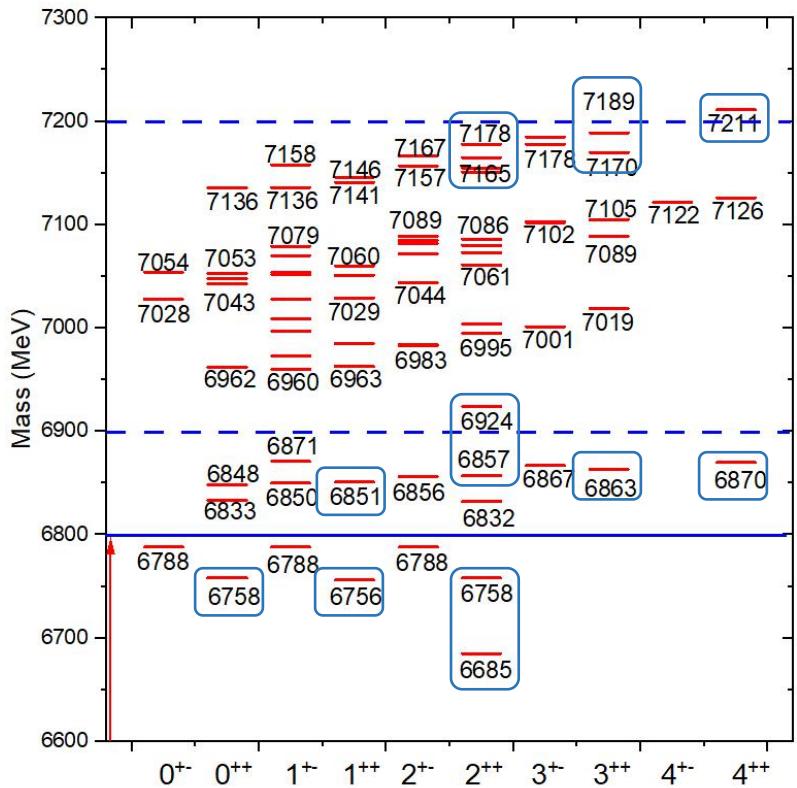


主要贡献来自于
 $\langle T \rangle$ 、 $\langle V^{Lin} \rangle$ 、 $\langle V^{Coul} \rangle$ 。

1D激发态的计算结果

$J^P(C)$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{+-}	$1^3P_{0^{+-}}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\begin{pmatrix} 6868 & -113 \\ -113 & 6948 \end{pmatrix}$	$\begin{pmatrix} 6788 \\ 7028 \end{pmatrix}$	$\begin{pmatrix} (-0.82 & -0.58) \\ (-0.58 & 0.82) \end{pmatrix}$
	$1^3P_{0^{+-}}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\begin{pmatrix} 7054 \end{pmatrix}$	7054	1
	$1^5D_{0^{+-}}(\bar{3}3)_c(\xi_1 \otimes \xi_2)$			
0^{++}	$1^1S_{0^{++}}(\bar{3}3)_c(\xi_1 \otimes \xi_2)$	$\begin{pmatrix} 6838 & -24 \\ -24 & 6957 \end{pmatrix}$	$\begin{pmatrix} 6833 \\ 6962 \end{pmatrix}$	$\begin{pmatrix} (-0.98 & -0.19) \\ (-0.19 & 0.98) \end{pmatrix}$
	$1^1S_{0^{++}}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	$\begin{pmatrix} 7053 \end{pmatrix}$	7053	1
	$1^3P_{0^{++}}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	$\begin{pmatrix} 6857 & 136 \\ 136 & 6944 \end{pmatrix}$	$\begin{pmatrix} 6758 \\ 7043 \end{pmatrix}$	$\begin{pmatrix} (-0.81 & 0.59) \\ (0.59 & 0.81) \end{pmatrix}$
	$1^3P_{0^{++}}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$			
	$1^5D_{0^{++}}(\bar{3}3)_c(\xi_1 \otimes \xi_2)$	$\begin{pmatrix} 7051 & 61 & 6 \\ 61 & 6968 & -128 \\ 6 & -128 & 7013 \end{pmatrix}$	$\begin{pmatrix} 7048 \\ 6848 \\ 7136 \end{pmatrix}$	$\begin{pmatrix} (0.88 & -0.09 & 0.47) \\ (-0.25 & 0.76 & 0.6) \\ (0.41 & 0.64 & -0.65) \end{pmatrix}$
	$1^5D_{0^{++}}(\bar{3}3)_c(\xi_3)$			

1D激发态的计算结果



- 1D态的质量分布在 $6.6\text{GeV}\sim7.3\text{GeV}$ 范围内。

- $T_{0^{++}}(6758)$ 、 $T_{1^{++}}(6756)$ 、 $T_{2^{++}}(6685)$ 、 $T_{2^{++}}(6758)$ 是 $X(6500)$ 可能的候选者。

- $T_{1^{++}}(6851)$ 、 $T_{2^{++}}(6857)$ 、 $T_{2^{++}}(6924)$ 、 $T_{3^{++}}(6863)$ 、 $T_{4^{++}}(6870)$ 是 $X(6900)$ 可能的候选者。

- $T_{2^{++}}(7165)$ 、 $T_{2^{++}}(7178)$ 、 $T_{3^{++}}(7170)$ 、 $T_{3^{++}}(7189)$ 、 $T_{4^{++}}(7211)$ 是 $X(7200)$ 可能的候选者。

1D激发态的计算结果

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0 ⁺⁻	$1^3P_{0+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6868	732	837	-636	6.18	0	-2.28
	$1^3P_{0+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6948	749	876	-601	-2.66	0	-4.73
	$1^5D_{0+-}(\bar{3}3)_c(\xi_1, \xi_2)$	7054	809	924	-572	9.25	-5.91	-43.52
0 ⁺⁺	$1^1S_{0++}(\bar{3}3)_c(\xi_1 \otimes \xi_2)$	6838	769	818	-657	-24.14	0	0
	$1^1S_{0++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	6957	788	877	-603	-37.55	0	0
	$1^3P_{0++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6857	745	830	-642	-2.02	-2.35	-2.35
	$1^3P_{0++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6944	754	873	-603	-6.08	-0.96	-4.79
	$1^3P_{0++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7053	775	925	-553	-15.43	2.49	-12.47
	$1^5D_{0++}(\bar{3}3)_c(\xi_1, \xi_2)$	7051	798	927	-577	9.84	-4.46	-35.39
	$1^5D_{0++}(\bar{3}3)_c(\xi_3)$	6968	783	883	-603	10.84	-4.59	-32.12
	$1^5D_{0++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7013	802	902	-585	9.78	-5.96	-41.73

混合矩阵元：

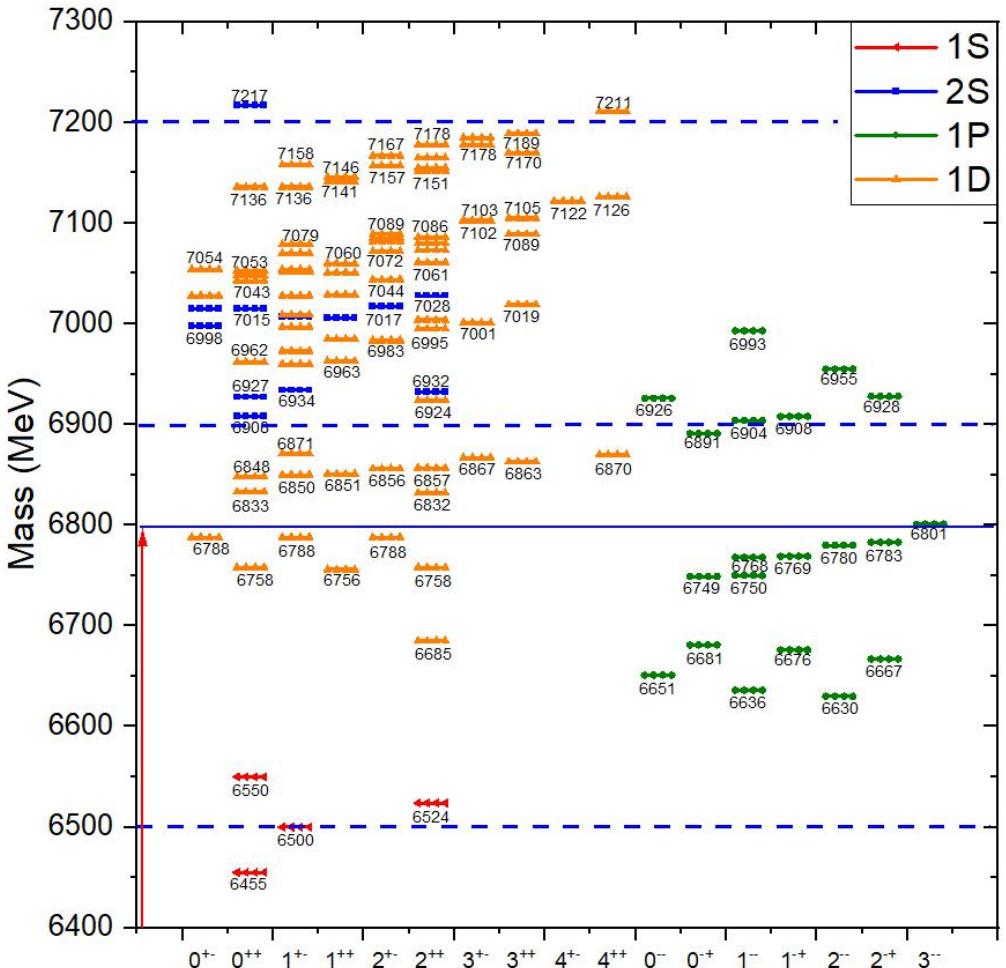
$$\begin{array}{c}
 \begin{array}{l}
 {}^3P_{1--(6\bar{6})_c(\xi_1,\xi_2)} \\
 {}^3P_{1--(\bar{3}3)_c(\xi_1,\xi_2)} \\
 1^{--} \quad {}^5P_{1--(\bar{3}3)_c(\xi_3)} \\
 {}^1P_{1--(\bar{3}3)_c(\xi_3)} \\
 {}^1P_{1--(6\bar{6})_c(\xi_3)}
 \end{array}
 \left\{
 \begin{array}{cccccc}
 6733 & 132 & -29 & -16 & 31 & \\
 132 & 6827 & -14 & -7 & 26 & \\
 -29 & -14 & 6754 & -3 & 10 & \\
 -16 & -7 & -3 & 6770 & -19 & \\
 31 & 26 & 10 & -19 & 6968 &
 \end{array}
 \right\}
 \begin{array}{l}
 \frac{1}{2}\left(\psi_{011}^{\xi_1}\chi_{10}^{10}-\psi_{010}^{\xi_1}\chi_{11}^{10}-\psi_{011}^{\xi_2}\chi_{10}^{01}+\psi_{010}^{\xi_2}\chi_{11}^{01}\right) \\
 \frac{1}{2}\left(\psi_{011}^{\xi_1}\chi_{10}^{01}-\psi_{010}^{\xi_1}\chi_{11}^{01}-\psi_{011}^{\xi_2}\chi_{10}^{10}+\psi_{010}^{\xi_2}\chi_{11}^{10}\right) \\
 \sqrt{\frac{1}{10}}\psi_{011}^{\xi_3}\chi_{20}^{11}-\sqrt{\frac{3}{10}}\psi_{010}^{\xi_3}\chi_{21}^{11}+\sqrt{\frac{3}{5}}\psi_{01-1}^{\xi_3}\chi_{22}^{11} \\
 \psi_{011}^{\xi_3}\chi_{00}^{11} \\
 \psi_{011}^{\xi_3}\chi_{00}^{00}
 \end{array}
 \end{array}$$

Mass	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
------	---------------------------	----------------------------	--------------------------	-----------------------	--------------------------

132	64	66	16	-3	-10
-29	0	0	0	-11	-18
-19	0	0	-19	0	0

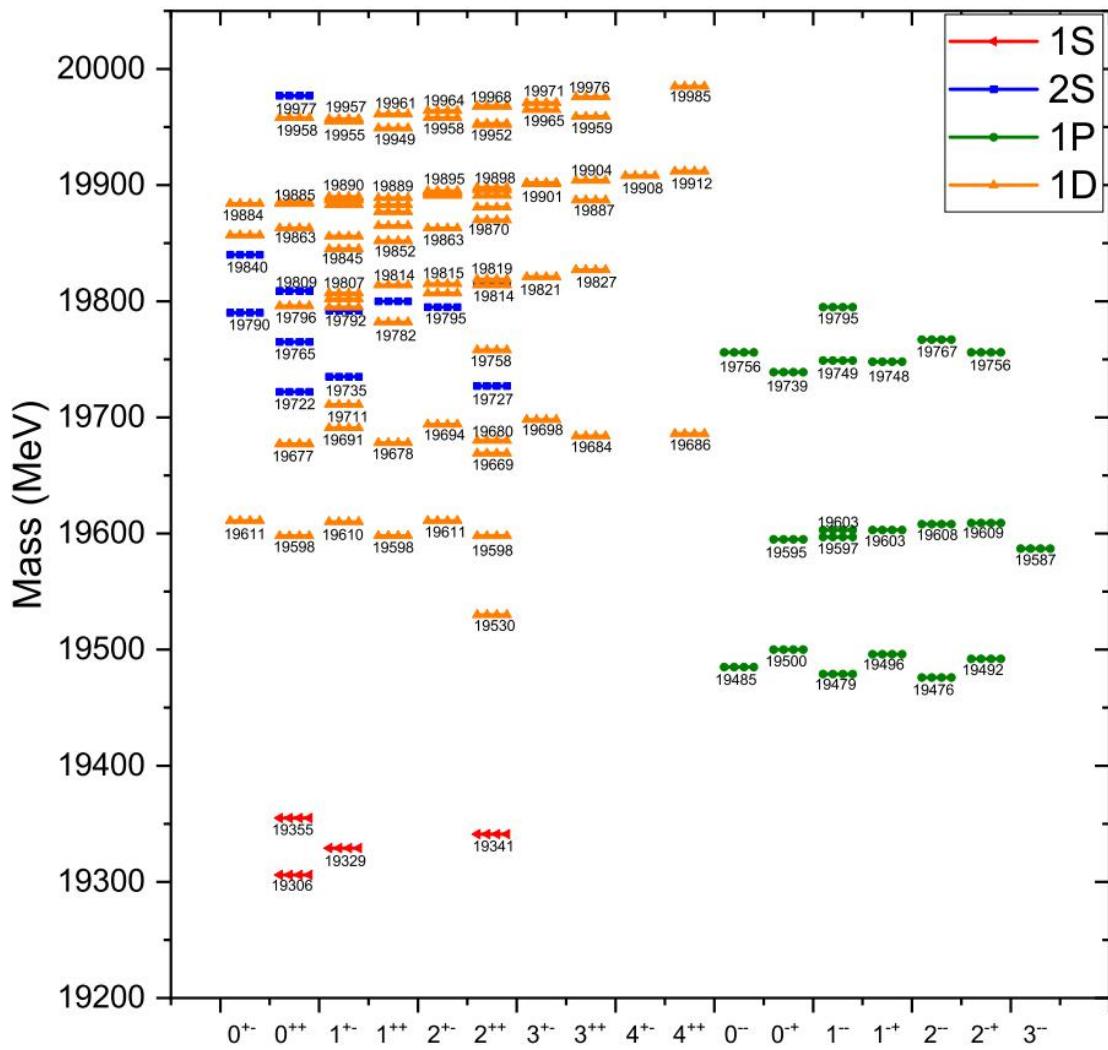
- 不同颜色结构也有混合。
- $\chi_{SS_m}^{S_{12}S_{34}}$ 相同时， V^{Lin} 、 V^{Coul} 和 V^{SS} 有较大的贡献。
- SS_m 相同时， V^{SS} 有贡献。

$CC\bar{C}\bar{C}$ 质量谱



- 1S态 $T_{0^{++}}(6455)$ 、 $T_{0^{++}}(6550)$ 、 $T_{2^{++}}(6524)$ 对 (6200-6800) 有重要贡献，
 1P态 $T_{0^{-+}}(6681)$ 、 $T_{0^{-+}}(6749)$ 、 $T_{1^{-+}}(6676)$ 、 $T_{1^{-+}}(6769)$ 、 $T_{1^{-+}}(6667)$ 、 $T_{1^{-+}}(6783)$ ，
 1D态 $T_{0^{++}}(6758)$ 、 $T_{1^{++}}(6756)$ 、
 $T_{2^{++}}(6685)$ 、 $T_{2^{++}}(6758)$ 都是 $X(6500)$ 可能的候选者。
- 2S态 $T_{0^{++}}(6908)$ 、 $T_{0^{++}}(6927)$ 、 $T_{2^{++}}(6932)$ ，
 1P态 $T_{0^{-+}}(6891)$ 、 $T_{1^{-+}}(6908)$ 、 $T_{2^{-+}}(6928)$ ，
 1D态 $T_{1^{++}}(6851)$ 、 $T_{2^{++}}(6857)$ 、
 $T_{2^{++}}(6924)$ 、 $T_{3^{++}}(6863)$ 、 $T_{4^{++}}(6870)$ 是 $X(6900)$ 可能的候选者。
- 2S态 $T_{0^{++}}(7217)$
 1D态 $T_{2^{++}}(7165)$ 、 $T_{2^{++}}(7178)$ 、
 $T_{3^{++}}(7170)$ 、 $T_{3^{++}}(7189)$ 、 $T_{4^{++}}(7211)$ 是 $X(7200)$ 可能的候选者。
- 需要进一步研究衰变性质。

$bbbb$ 质量谱





谢谢

TABLE I: Configurations for the tetraquark $qq\bar{q}\bar{q}$ system.

$J^{P(C)}$	Configuration	Wave Function
$J^{PC}=0^{++}$	$1^1S_{0^{++}(6\bar{6})_c}$	$\psi_{000}^{1S} \chi_{00}^{00}$
$J^{PC}=0^{++}$	$1^1S_{0^{++}(\bar{3}3)_c}$	$\psi_{000}^{1S} \chi_{11}^{00}$
$J^{PC}=1^{+-}$	$1^3S_{1^{+-}(\bar{3}3)_c}$	$\psi_{000}^{1S} \chi_{11}^{11}$
$J^{PC}=2^{++}$	$1^5S_{2^{++}(\bar{3}3)_c}$	$\psi_{000}^{1S} \chi_{22}^{00}$

TABLE II: Configurations for the tetraquark $qq\bar{q}\bar{q}$ system up to the $2S$ -wave states. ξ_1, ξ_2, ξ_3 are the Jacobi coordinates. (ξ_1, ξ_2) stands for a configuration containing both ξ_1 - and ξ_2 -mode orbital excitations.

$J^{P(C)}$	Configuration	Wave Function
$J^{PC}=0^{+-}$	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{00}^{00} - \psi_{100}^{\xi_2} \chi_{00}^{00})$
$J^{PC}=0^{+-}$	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{00}^{11} - \psi_{100}^{\xi_2} \chi_{00}^{11})$
$J^{PC}=0^{++}$	$2^1S_{0^{++}(6\bar{6})_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{00}^{00} + \psi_{100}^{\xi_2} \chi_{00}^{00})$
$J^{PC}=0^{++}$	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{00}^{11} + \psi_{100}^{\xi_2} \chi_{00}^{11})$
$J^{PC}=0^{++}$	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	$\psi_{100}^{\xi_3} \chi_{00}^{00}$
$J^{PC}=0^{++}$	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	$\psi_{100}^{\xi_3} \chi_{00}^{11}$
$J^{PC}=1^{+-}$	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{11}^{11} - \psi_{100}^{\xi_2} \chi_{11}^{11})$
$J^{PC}=1^{+-}$	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	$\psi_{100}^{\xi_3} \chi_{11}^{11}$
$J^{PC}=1^{++}$	$2^3S_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{11}^{11} + \psi_{100}^{\xi_2} \chi_{11}^{11})$
$J^{PC}=2^{+-}$	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{22}^{11} - \psi_{100}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=2^{++}$	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{100}^{\xi_1} \chi_{22}^{11} + \psi_{100}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=2^{++}$	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	$\psi_{100}^{\xi_3} \chi_{22}^{11}$

TABLE III: Configurations for the tetraquark $qq\bar{q}\bar{q}$ system up to the $1P$ -wave states. ξ_1, ξ_2, ξ_3 are the Jacobi coordinates. (ξ_1, ξ_2) stands for a configuration containing both ξ_1 - and ξ_2 -mode orbital excitations.

J^{PC}	Configuration	Wave Function	
$J^{PC}=0^{--}$	$1^3P_{0^{--}(66)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{6}} (\psi_{011}^{\xi_1} \chi_{1-1}^{10} - \psi_{010}^{\xi_1} \chi_{10}^{10} + \psi_{01-1}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{1-1}^{01} + \psi_{010}^{\xi_2} \chi_{10}^{01} - \psi_{01-1}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=0^{--}$	$1^3P_{0^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{6}} (\psi_{011}^{\xi_1} \chi_{1-1}^{01} - \psi_{010}^{\xi_1} \chi_{10}^{01} + \psi_{01-1}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{1-1}^{10} + \psi_{010}^{\xi_2} \chi_{10}^{10} - \psi_{01-1}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=0^{+-}$	$1^3P_{0^{+}(66)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{6}} (\psi_{011}^{\xi_1} \chi_{1-1}^{10} - \psi_{010}^{\xi_1} \chi_{10}^{10} + \psi_{01-1}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{1-1}^{01} - \psi_{010}^{\xi_2} \chi_{10}^{01} + \psi_{01-1}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=0^{+-}$	$1^3P_{0^{+}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{6}} (\psi_{011}^{\xi_1} \chi_{1-1}^{01} - \psi_{010}^{\xi_1} \chi_{10}^{01} + \psi_{01-1}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{1-1}^{10} - \psi_{010}^{\xi_2} \chi_{10}^{10} + \psi_{01-1}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=0^{+-}$	$1^3P_{0^{+}(\bar{3}3)_c(\xi_3)}$	$\sqrt{\frac{1}{3}} (\psi_{011}^{\xi_3} \chi_{1-1}^{11} - \psi_{010}^{\xi_3} \chi_{11}^{11} + \psi_{01-1}^{\xi_3} \chi_{11}^{11})$	$ \bar{3}3\rangle^c$
$J^{PC}=1^{--}$	$1^3P_{1^{--}(66)_c(\xi_1,\xi_2)}$	$\frac{1}{2} (\psi_{011}^{\xi_1} \chi_{10}^{10} - \psi_{010}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{10}^{01} + \psi_{010}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=1^{--}$	$1^3P_{1^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\frac{1}{2} (\psi_{011}^{\xi_1} \chi_{10}^{01} - \psi_{010}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{10}^{10} + \psi_{010}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=1^{--}$	$1^5P_{1^{--}(\bar{3}3)_c(\xi_3)}$	$\sqrt{\frac{1}{10}} \psi_{011}^{\xi_3} \chi_{20}^{11} - \sqrt{\frac{3}{10}} \psi_{010}^{\xi_3} \chi_{21}^{11} + \sqrt{\frac{3}{5}} \psi_{01-1}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
$J^{PC}=1^{--}$	$1^1P_{1^{--}(\bar{3}3)_c(\xi_3)}$	$\psi_{011}^{\xi_3} \chi_{00}^{11}$	$ \bar{3}3\rangle^c$
$J^{PC}=1^{--}$	$1^1P_{1^{--}(66)_c(\xi_3)}$	$\psi_{011}^{\xi_3} \chi_{00}^{00}$	$ 6\bar{6}\rangle^c$
$J^{PC}=1^{++}$	$1^3P_{1^{+}(66)_c(\xi_1,\xi_2)}$	$\frac{1}{2} (\psi_{011}^{\xi_1} \chi_{10}^{10} - \psi_{010}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{10}^{01} - \psi_{010}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=1^{++}$	$1^3P_{1^{+}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\frac{1}{2} (\psi_{011}^{\xi_1} \chi_{10}^{01} - \psi_{010}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{10}^{10} - \psi_{010}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=1^{++}$	$1^3P_{1^{+}(\bar{3}3)_c(\xi_3)}$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_3} \chi_{10}^{11} - \psi_{010}^{\xi_3} \chi_{11}^{11})$	$ \bar{3}3\rangle^c$
$J^{PC}=2^{--}$	$1^3P_{2^{--}(66)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1} \chi_{11}^{10} - \psi_{011}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=2^{--}$	$1^3P_{2^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1} \chi_{11}^{01} - \psi_{011}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=2^{--}$	$1^5P_{2^{--}(\bar{3}3)_c(\xi_3)}$	$\sqrt{\frac{1}{3}} \psi_{011}^{\xi_3} \chi_{21}^{11} - \sqrt{\frac{2}{3}} \psi_{010}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$
$J^{PC}=2^{+-}$	$1^3P_{2^{+}(66)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1} \chi_{11}^{10} + \psi_{011}^{\xi_2} \chi_{11}^{01})$	$ 6\bar{6}\rangle^c$
$J^{PC}=2^{+-}$	$1^3P_{2^{+}(\bar{3}3)_c(\xi_1,\xi_2)}$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1} \chi_{11}^{01} + \psi_{011}^{\xi_2} \chi_{11}^{10})$	$ \bar{3}3\rangle^c$
$J^{PC}=2^{+-}$	$1^3P_{2^{+}(\bar{3}3)_c(\xi_3)}$	$\psi_{011}^{\xi_3} \chi_{11}^{11}$	$ \bar{3}3\rangle^c$
$J^{PC}=3^{--}$	$1^5P_{3^{--}(\bar{3}3)_c(\xi_3)}$	$\psi_{011}^{\xi_3} \chi_{22}^{11}$	$ \bar{3}3\rangle^c$

TABLE IV: Configurations for the tetraquark $qq\bar{q}\bar{q}$ system up to the $1D$ -wave states. ξ_1, ξ_2, ξ_3 are the Jacobi coordinates. (ξ_1, ξ_2) stands for a configuration containing both ξ_1 - and ξ_2 -mode orbital excitations. $\xi_i \otimes \xi_j$ means two independent internal $\psi_{n_{\xi_i}, l_{\xi_i} m_{\xi_i}}(\xi_i)$ and $\psi_{n_{\xi_j}, l_{\xi_j} m_{\xi_j}}(\xi_j)$ wave functions excited.

TABLE V: Configurations for the tetraquark $qq\bar{q}\bar{q}$ system up to the 1D-wave states. ξ_1, ξ_2, ξ_3 are the Jacobi coordinates. (ξ_1, ξ_2) stands for a configuration containing both ξ_1 - and ξ_2 -mode orbital excitations. $\xi_i \otimes \xi_j$ means two independent internal $\psi_{n_{\xi_i}, l_{\xi_i} m_{\xi_i}}(\xi_i)$ and $\psi_{n_{\xi_j}, l_{\xi_j} m_{\xi_j}}(\xi_j)$ wave functions excited.

J^{PC}	Configuration	Wave Function
$J^{PC}=2^{+-}$	$1^3P_{2^{+-}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{01})$
$J^{PC}=2^{+-}$	$1^3P_{2^{+-}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{011}^{\xi_2 \xi_3} \chi_{11}^{10})$
$J^{PC}=2^{+-}$	$1^5P_{2^{+-}(66)_c}(\xi_1 \otimes \xi_2)$	$\sqrt{\frac{1}{3}} \psi_{011}^{\xi_1 \xi_2} \chi_{21}^{11} - \sqrt{\frac{2}{3}} \psi_{010}^{\xi_1 \xi_2} \chi_{22}^{11}$
$J^{PC}=2^{+-}$	$1^1D_{2^{+-}(66)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{00} - \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{00}$
$J^{PC}=2^{+-}$	$1^1D_{2^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{11} - \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{11}$
$J^{PC}=2^{+-}$	$1^3D_{2^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1} \chi_{10}^{11} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1} \chi_{11}^{11} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2} \chi_{10}^{11} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2} \chi_{11}^{11}$
$J^{PC}=2^{+-}$	$1^3D_{2^{+-}(\bar{3}3)_c}(\xi_3)$	$\sqrt{\frac{2}{3}} \psi_{022}^{\xi_3} \chi_{10}^{11} - \sqrt{\frac{1}{3}} \psi_{021}^{\xi_3} \chi_{11}^{11}$
$J^{PC}=2^{+-}$	$1^3D_{2^{+-}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{10} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{10} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{01} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{01}$
$J^{PC}=2^{+-}$	$1^3D_{2^{+-}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{01} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{01} - \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{10} + \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{10}$
$J^{PC}=2^{+-}$	$1^3D_{2^{+-}(\bar{3}3)_c}(\xi_1 \otimes \xi_2)$	$\sqrt{\frac{2}{3}} \psi_{022}^{\xi_1 \xi_2} \chi_{10}^{11} - \sqrt{\frac{1}{3}} \psi_{021}^{\xi_1 \xi_2} \chi_{11}^{11}$
$J^{PC}=2^{+-}$	$1^5D_{2^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{2}{14}} \psi_{022}^{\xi_1} \chi_{20}^{11} - \sqrt{\frac{3}{14}} \psi_{021}^{\xi_1} \chi_{21}^{11} + \sqrt{\frac{2}{14}} \psi_{020}^{\xi_1} \chi_{22}^{11} - \sqrt{\frac{2}{14}} \psi_{022}^{\xi_2} \chi_{20}^{11} + \sqrt{\frac{3}{14}} \psi_{021}^{\xi_2} \chi_{21}^{11} - \sqrt{\frac{2}{14}} \psi_{020}^{\xi_2} \chi_{22}^{11}$
$J^{PC}=2^{++}$	$1^5S_{2^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{000}^{\xi_1 \xi_2} \chi_{22}^{11}$
$J^{PC}=2^{++}$	$1^3P_{2^{++}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{10} + \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{01})$
$J^{PC}=2^{++}$	$1^3P_{2^{++}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{011}^{\xi_1 \xi_3} \chi_{10}^{01} + \psi_{011}^{\xi_2 \xi_3} \chi_{10}^{10})$
$J^{PC}=2^{++}$	$1^3P_{2^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{011}^{\xi_1 \xi_2} \chi_{11}^{11}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(66)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{00} + \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{00}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} \psi_{022}^{\xi_1} \chi_{00}^{11} + \sqrt{\frac{1}{2}} \psi_{022}^{\xi_2} \chi_{00}^{11}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(66)_c}(\xi_3)$	$\psi_{022}^{\xi_3} \chi_{00}^{00}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(\bar{3}3)_c}(\xi_3)$	$\psi_{022}^{\xi_3} \chi_{00}^{11}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(\bar{3}3)_c}(\xi_1 \otimes \xi_2)$	$\psi_{022}^{\xi_1 \xi_2} \chi_{00}^{00}$
$J^{PC}=2^{++}$	$1^1D_{2^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{022}^{\xi_1 \xi_2} \chi_{00}^{11}$
$J^{PC}=2^{++}$	$1^3D_{2^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1} \chi_{10}^{11} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1} \chi_{11}^{11} + \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2} \chi_{10}^{11} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2} \chi_{11}^{11}$
$J^{PC}=2^{++}$	$1^3D_{2^{++}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{10} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{10} + \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{01} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{01}$
$J^{PC}=2^{++}$	$1^3D_{2^{++}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{2}{6}} \psi_{022}^{\xi_1 \xi_3} \chi_{10}^{01} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_1 \xi_3} \chi_{11}^{01} + \sqrt{\frac{2}{6}} \psi_{022}^{\xi_2 \xi_3} \chi_{10}^{10} - \sqrt{\frac{1}{6}} \psi_{021}^{\xi_2 \xi_3} \chi_{11}^{10}$
$J^{PC}=2^{++}$	$1^5D_{2^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{2}{14}} \psi_{022}^{\xi_1} \chi_{20}^{11} - \sqrt{\frac{3}{14}} \psi_{021}^{\xi_1} \chi_{21}^{11} + \sqrt{\frac{2}{14}} \psi_{020}^{\xi_1} \chi_{22}^{11} - \sqrt{\frac{2}{14}} \psi_{022}^{\xi_2} \chi_{20}^{11} + \sqrt{\frac{3}{14}} \psi_{021}^{\xi_2} \chi_{21}^{11} - \sqrt{\frac{2}{14}} \psi_{020}^{\xi_2} \chi_{22}^{11}$
$J^{PC}=2^{++}$	$1^5D_{2^{++}(\bar{3}3)_c}(\xi_3)$	$\sqrt{\frac{2}{7}} \psi_{022}^{\xi_3} \chi_{20}^{11} - \sqrt{\frac{3}{7}} \psi_{021}^{\xi_3} \chi_{21}^{11} + \sqrt{\frac{2}{7}} \psi_{020}^{\xi_3} \chi_{22}^{11}$
$J^{PC}=2^{++}$	$1^5D_{2^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\sqrt{\frac{2}{7}} \psi_{022}^{\xi_1 \xi_2} \chi_{20}^{11} - \sqrt{\frac{3}{7}} \psi_{021}^{\xi_1 \xi_2} \chi_{21}^{11} + \sqrt{\frac{2}{7}} \psi_{020}^{\xi_1 \xi_2} \chi_{22}^{11}$
$J^{PC}=3^{+-}$	$1^5P_{3^{+-}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{011}^{\xi_1 \xi_2} \chi_{22}^{11}$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1} \chi_{11}^{11} - \psi_{022}^{\xi_2} \chi_{11}^{11})$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(\bar{3}3)_c}(\xi_3)$	$\psi_{022}^{\xi_3} \chi_{11}^{11}$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1 \xi_3} \chi_{11}^{10} - \psi_{022}^{\xi_2 \xi_3} \chi_{11}^{01})$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1 \xi_3} \chi_{11}^{01} - \psi_{022}^{\xi_2 \xi_3} \chi_{11}^{10})$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{022}^{\xi_1 \xi_2} \chi_{11}^{11}$
$J^{PC}=3^{+-}$	$1^3D_{3^{+-}(\bar{3}3)_c}(\xi_1 \otimes \xi_2)$	$\psi_{022}^{\xi_1 \xi_2} \chi_{11}^{11}$
$J^{PC}=3^{+-}$	$1^5D_{3^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\frac{1}{2} (\psi_{022}^{\xi_1} \chi_{21}^{11} - \psi_{021}^{\xi_1} \chi_{22}^{11} - \psi_{022}^{\xi_2} \chi_{21}^{11} + \psi_{021}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=3^{++}$	$1^3D_{3^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1} \chi_{21}^{11} + \psi_{022}^{\xi_2} \chi_{21}^{11})$
$J^{PC}=3^{++}$	$1^3D_{3^{++}(66)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1 \xi_3} \chi_{21}^{10} + \psi_{022}^{\xi_2 \xi_3} \chi_{21}^{01})$
$J^{PC}=3^{++}$	$1^3D_{3^{++}(\bar{3}3)_c}(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1 \xi_3} \chi_{21}^{01} + \psi_{022}^{\xi_2 \xi_3} \chi_{21}^{10})$
$J^{PC}=3^{++}$	$1^5D_{3^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\frac{1}{2} (\psi_{022}^{\xi_1} \chi_{21}^{11} - \psi_{021}^{\xi_1} \chi_{22}^{11} + \psi_{022}^{\xi_2} \chi_{21}^{11} - \psi_{021}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=3^{++}$	$1^5D_{3^{++}(\bar{3}3)_c}(\xi_3)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_3} \chi_{21}^{11} - \psi_{021}^{\xi_3} \chi_{22}^{11})$
$J^{PC}=3^{++}$	$1^5D_{3^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1 \xi_2} \chi_{21}^{11} - \psi_{021}^{\xi_1 \xi_2} \chi_{22}^{11})$
$J^{PC}=4^{+-}$	$1^5D_{4^{+-}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1} \chi_{22}^{11} - \psi_{022}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=4^{++}$	$1^5D_{4^{++}(\bar{3}3)_c}(\xi_1, \xi_2)$	$\sqrt{\frac{1}{2}} (\psi_{022}^{\xi_1} \chi_{22}^{11} + \psi_{022}^{\xi_2} \chi_{22}^{11})$
$J^{PC}=4^{++}$	$1^5D_{4^{++}(\bar{3}3)_c}(\xi_3)$	$\psi_{022}^{\xi_3} \chi_{22}^{11}$
$J^{PC}=4^{++}$	$1^5D_{4^{++}(66)_c}(\xi_1 \otimes \xi_2)$	$\psi_{022}^{\xi_1 \xi_2} \chi_{22}^{11}$

TABLE VI: Predicted mass spectra for the $cc\bar{c}\bar{c}$ systems up to the $1S$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0 ⁺⁺	$1^1S_{0^{++}(66)_c(\xi_1,\xi_2)}$	(6518 45)	(6455)	((0.58 -0.81))
	$1^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(45 6487)	(6550)	((-0.81 -0.58))
1 ⁺⁻	$1^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(6500)	6500	1
2 ⁺⁺	$1^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(6524)	6524	1

TABLE VII: Predicted mass spectra for the $cc\bar{c}\bar{c}$ systems up to the $2S$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0 ⁺⁻	$2^1S_{0^{+-}(66)_c(\xi_1,\xi_2)}$	(7008 -8)	(6998)	((-0.63 -0.78))
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(-8 7005)	(7015)	((-0.78 0.63))
0 ⁺⁺	$2^1S_{0^{++}(66)_c(\xi_1,\xi_2)}$	(6954 -19 93 -8)	(6908)	((-0.62 0.69 0.13 -0.34))
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(-19 7000 -4 -33)	(6927)	((-0.36 -0.13 -0.92 0.04))
	$2^1S_{0^{++}(66)_c(\xi_3)}$	(93 -4 7183 -12)	(7015)	((0.18 -0.28 -0.07 -0.94))
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	(-8 -33 -12 6930)	(7217)	((-0.67 -0.65 0.35 0.04))
1 ⁺⁻	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(7009 0)	(7009)	((1 0))
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	(0 6934)	(6934)	((0 1))
1 ⁺⁺	$2^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(7006)	7006	1
2 ⁺⁻	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(7017)	7017	1
2 ⁺⁺	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(7018 -29)	(7028)	((-0.95 0.32))
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	(-29 6942)	(6932)	((0.32 -0.95))

TABLE VIII: Predicted masses for the P -wave $cc\bar{c}\bar{c}$ states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0 ⁻⁻	$3P_{0^{--}(66)_c(\xi_1,\xi_2)}$	(6751 -132)	(6651)	((-0.7985 -0.6020))
	$3P_{0^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	(-132 6827)	(6926)	((-0.6020 0.7985))
0 ⁺⁻	$3P_{0^{+-}(66)_c(\xi_1,\xi_2)}$	(6746 88 37)	(6681)	((0.82 -0.47 -0.32))
	$3P_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(88 6825 18)	(6749)	((-0.14 0.38 0.91))
	$3P_{0^{+-}(\bar{3}3)_c(\xi_3)}$	(37 18 6750)	(6891)	((0.55 0.80 0.25))
1 ⁻⁻	$3P_{1^{--}(66)_c(\xi_1,\xi_2)}$	(6733 132 -29 -16 31)	(6636)	((0.82 -0.55 0.12 0.06 -0.03))
	$3P_{1^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	(132 6827 -14 -7 26)	(6750)	((0.02 -0.24 -0.96 -0.16 0.06))
	$5P_{1^{--}(\bar{3}3)_c(\xi_3)}$	(-29 -14 6754 -3 10)	(6768)	((-0.01 0.05 -0.17 0.98 0.10))
	$1P_{1^{--}(\bar{3}3)_c(\xi_3)}$	(-16 -7 -3 6770 -19)	(6904)	((-0.48 -0.69 0.19 0.02 0.50))
	$1P_{1^{--}(66)_c(\xi_3)}$	(31 26 10 -19 6968)	(6993)	((0.31 0.39 -0.02 -0.11 0.86))
1 ⁺	$3P_{1^{+}(66)_c(\xi_1,\xi_2)}$	(6751 -108 9)	(6676)	((0.82 0.56 -0.05))
	$3P_{1^{+}(\bar{3}3)_c(\xi_1,\xi_2)}$	(-108 6834 -4)	(6769)	((-0.01 -0.08 -1.00))
	$3P_{1^{+}(\bar{3}3)_c(\xi_3)}$	(9 -4 6769)	(6908)	((-0.57 0.82 -0.06))
2 ⁻⁻	$3P_{2^{--}(66)_c(\xi_1,\xi_2)}$	(6746 -155 -18)	(6630)	((0.80 0.59 0.06))
	$3P_{2^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	(-155 6837 9)	(6780)	((-0.01 0.12 -1.00))
	$5P_{2^{--}(\bar{3}3)_c(\xi_3)}$	(-18 9 6781)	(6955)	((-0.60 0.80 0.10))
2 ⁺⁻	$3P_{2^{+-}(66)_c(\xi_1,\xi_2)}$	(6754 123 12)	(6667)	((0.82 -0.57 -0.06))
	$3P_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(123 6841 6)	(6783)	((0.00 0.10 -1.00))
	$3P_{2^{+-}(\bar{3}3)_c(\xi_3)}$	(12 6 6783)	(6928)	((0.58 0.81 0.08))
3 ⁻⁻	$5P_{3^{--}(\bar{3}3)_c(\xi_3)}$	(6801)	6801	1

TABLE IX: Predicted mass spectra for the $cc\bar{c}\bar{c}$ systems up to the $1D$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{+-}	$\begin{pmatrix} 1^3P_{0^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{0^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6868 & -113 \\ -113 & 6948 \end{pmatrix}$	$\begin{pmatrix} 6788 \\ 7028 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ -0.58 & 0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^5D_{0^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7054 \end{pmatrix}$	7054	1
	$\begin{pmatrix} 1^1S_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_2)} \\ 1^1S_{0^{++}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 6838 \\ 6957 \end{pmatrix}$	6838 6957	1 1
0^{++}	$\begin{pmatrix} 1^3P_{0^{++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6857 & 136 \\ 136 & 6944 \end{pmatrix}$	$\begin{pmatrix} 6758 \\ 7043 \end{pmatrix}$	$\begin{pmatrix} -0.81 & 0.59 \\ 0.59 & 0.81 \end{pmatrix}$
	$\begin{pmatrix} 1^3P_{0^{++}(66)_c(\xi_1 \otimes \xi_2)} \\ 1^5D_{0^{++}(\bar{3}3)_c(\xi_1, \xi_2)} \\ 1^5D_{0^{++}(\bar{3}3)_c(\xi_3)} \\ 1^5D_{0^{++}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7053 \\ 7051 & 61 & 6 \\ 61 & 6968 & -128 \\ 6 & -128 & 7013 \end{pmatrix}$	$\begin{pmatrix} 7048 \\ 6848 \\ 7136 \end{pmatrix}$	$\begin{pmatrix} 0.88 & -0.09 & 0.47 \\ -0.25 & 0.76 & 0.6 \\ 0.41 & 0.64 & -0.65 \end{pmatrix}$
	$\begin{pmatrix} 1^3S_{1^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3S_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 7002 & -7 \\ -7 & 7007 \end{pmatrix}$	$\begin{pmatrix} 6997 \\ 7012 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ -0.58 & 0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^3S_{1^{+-}(66)_c(\xi_1 \otimes \xi_2)} \\ 1^1P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_2)} \\ 1^1P_{1^{+-}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 6973 \\ 6871 \\ 7052 \end{pmatrix}$	6973 6871 7052	1 1 1
1^{+-}	$\begin{pmatrix} 1^3P_{1^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6867 & -112 \\ -112 & 6946 \end{pmatrix}$	$\begin{pmatrix} 6788 \\ 7025 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ -0.58 & 0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^5P_{1^{+-}(66)_c(\xi_1 \otimes \xi_2)} \\ 1^3D_{1^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \\ 1^3D_{1^{+-}(\bar{3}3)_c(\xi_3)} \\ 1^3D_{1^{+-}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7069 \\ 7070 \\ 6978 & -142 \\ -142 & 7008 \end{pmatrix}$	$\begin{pmatrix} 7069 \\ 7070 \\ 6850 \\ 7136 \end{pmatrix}$	$\begin{pmatrix} 1 \\ 1 \\ -0.74 & -0.67 \\ -0.67 & 0.74 \end{pmatrix}$
	$\begin{pmatrix} 1^3D_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3D_{1^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 7092 & 93 \\ 93 & 7026 \end{pmatrix}$	$\begin{pmatrix} 7158 \\ 6960 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ 0.58 & -0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^5D_{1^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7064 \end{pmatrix}$	7064	1
	$\begin{pmatrix} 1^3S_{1^{++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3S_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6991 & 34 \\ 34 & 7003 \end{pmatrix}$	$\begin{pmatrix} 6962 \\ 7032 \end{pmatrix}$	$\begin{pmatrix} -0.77 & 0.64 \\ 0.64 & 0.77 \end{pmatrix}$
	$\begin{pmatrix} 1^3P_{1^{++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6861 & 140 \\ 140 & 6944 \end{pmatrix}$	$\begin{pmatrix} 6756 \\ 7049 \end{pmatrix}$	$\begin{pmatrix} -0.80 & 0.60 \\ 0.60 & 0.80 \end{pmatrix}$
1^{++}	$\begin{pmatrix} 1^3P_{1^{++}(66)_c(\xi_1 \otimes \xi_2)} \\ 1^3D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7051 \\ 7062 \end{pmatrix}$	7051 7062	1 1
	$\begin{pmatrix} 1^3D_{1^{++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3D_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 7096 & -69 \\ -69 & 7028 \end{pmatrix}$	$\begin{pmatrix} 7139 \\ 6985 \end{pmatrix}$	$\begin{pmatrix} -0.85 & 0.53 \\ -0.53 & -0.85 \end{pmatrix}$
	$\begin{pmatrix} 1^5D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)} \\ 1^5D_{1^{++}(\bar{3}3)_c(\xi_3)} \\ 1^5D_{1^{++}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7059 & 62 & 10 \\ 62 & 6976 & -132 \\ 10 & -132 & 7022 \end{pmatrix}$	$\begin{pmatrix} 7060 \\ 6851 \\ 7146 \end{pmatrix}$	$\begin{pmatrix} 0.89 & -0.06 & 0.46 \\ -0.25 & 0.76 & 0.6 \\ 0.38 & 0.65 & -0.66 \end{pmatrix}$
	$\begin{pmatrix} 1^3P_{2^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 6873 & -121 \\ -121 & 6959 \end{pmatrix}$	$\begin{pmatrix} 6788 \\ 7044 \end{pmatrix}$	$\begin{pmatrix} 0.82 & 0.58 \\ -0.58 & 0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^5P_{2^{+-}(66)_c(\xi_1 \otimes \xi_2)} \\ 1^1D_{2^{+-}(\bar{6}6)_c(\xi_1, \xi_2)} \\ 1^1D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7072 \\ 6985 \\ 7087 \end{pmatrix}$	7072 6985 7087	1 1 1
2^{+-}	$\begin{pmatrix} 1^3D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \\ 1^3D_{2^{+-}(\bar{3}3)_c(\xi_3)} \\ 1^3D_{2^{+-}(66)_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7085 \\ 6985 & -149 \\ -149 & 7028 \end{pmatrix}$	7085 7087 7085	1 1 1
	$\begin{pmatrix} 1^3D_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3D_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 7106 & 86 \\ 86 & 7045 \end{pmatrix}$	$\begin{pmatrix} 7167 \\ 6984 \end{pmatrix}$	$\begin{pmatrix} 0.82 & 0.58 \\ -0.58 & 0.82 \end{pmatrix}$
	$\begin{pmatrix} 1^5D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 7082 \end{pmatrix}$	7082	1

TABLE X: Predicted mass spectra for the $cc\bar{c}\bar{c}$ systems up to the $1D$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
	$(1^5S_{2++}(66)_c(\xi_1 \otimes \xi_2))$	(7004)	7004	1
	$(1^3P_{2++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(6864 145 145 6955)	(6758 7061)	(-0.81 0.59 0.59 0.81)
	$(1^3P_{2++}(66)_c(\xi_1 \otimes \xi_2))$	(7073)	7073	1
2^{++}	$(1^1D_{2++}(66)_c(\xi_1, \xi_2))$	(6955 -19 174 5 25 3)	(7151)	(-0.45 -0.17 -0.55 -0.45 0.21 0.46)
	$(1^1D_{2++}(33)_c(\xi_1, \xi_2))$	(-19 7073 5 72 1 28)	(7086)	(0.03 -0.9 -0.08 0.02 0.09 -0.42)
	$(1^1D_{2++}(66)_c(\xi_3))$	(174 5 6964 -21 -147 -6)	(6685)	(0.46 0.06 -0.62 -0.13 -0.6 -0.12)
	$(1^1D_{2++}(33)_c(\xi_3))$	(5 72 -21 6986 -2 -153)	(6832)	(-0.09 0.28 0.1 -0.72 0.13 -0.61)
	$(1^1D_{2++}(33)_c(\xi_1 \otimes \xi_2))$	(25 1 -147 -2 6859 -20)	(6924)	(-0.65 -0.08 0.21 0.01 -0.72 -0.07)
	$(1^1D_{2++}(66)_c(\xi_1 \otimes \xi_2))$	(3 28 -6 -153 -20 7018)	(7178)	(-0.38 0.28 -0.5 0.51 0.23 -0.46)
	$(1^3D_{2++}(33)_c(\xi_1, \xi_2))$	(7073)	7073	1
3^{+-}	$(1^3D_{2++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(7105 -74)	(7155)	(-0.83 0.56)
	$(1^3D_{2++}(33)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(-74 7045)	(6995)	(0.56 0.83)
	$(1^5D_{2++}(33)_c(\xi_1, \xi_2))$	(7073 65 17)	(7080)	(-0.90 0.02 -0.43)
	$(1^5D_{2++}(33)_c(\xi_3))$	(65 6989 -138)	(6857)	(-0.27 0.76 0.59)
	$(1^5D_{2++}(66)_c(\xi_1 \otimes \xi_2))$	(17 -138 7040)	(7165)	(-0.34 -0.65 0.68)
	$(1^5P_{3+-}(66)_c(\xi_1 \otimes \xi_2))$	(7102)	7102	1
	$(1^3D_{3++}(33)_c(\xi_1, \xi_2))$	(7103)	7103	1
3^{++}	$(1^3D_{3+-}(33)_c(\xi_3))$	(7002 -154)	(6867)	(0.75 0.66)
	$(1^3D_{3+-}(66)_c(\xi_1 \otimes \xi_2))$	(-154 7043)	(7178)	(-0.66 0.75)
	$(1^3D_{3+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(7124 87)	(7185)	(-0.82 -0.58)
	$(1^3D_{3+-}(33)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(87 7062)	(7001)	(0.58 -0.82)
	$(1^5D_{3++}(33)_c(\xi_1, \xi_2))$	(7103)	7103	1
	$(1^3D_{3++}(33)_c(\xi_1, \xi_2))$	(7089)	7089	1
	$(1^3D_{3++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(7126 -69)	(7170)	(0.84 -0.54)
4^{+-}	$(1^3D_{3++}(33)_c(\xi_1, \xi_2))$	(-69 7063)	(7019)	(0.54 0.84)
	$(1^5D_{3++}(33)_c(\xi_1, \xi_2))$	(7091 69 25)	(7105)	(0.91 0.03 0.41)
	$(1^5D_{3++}(33)_c(\xi_3))$	(69 7005 -146)	(6863)	(-0.29 0.75 0.59)
	$(1^5D_{3++}(66)_c(\xi_1 \otimes \xi_2))$	(25 -146 7060)	(7189)	(-0.29 -0.66 0.69)
	$(1^5D_{4+-}(33)_c(\xi_1, \xi_2))$	(7122)	7122	1
	$(1^5D_{4+-}(33)_c(\xi_1, \xi_2))$	(7108 72 31)	(7126)	(0.92 0.07 0.39)
	$(1^5D_{4+-}(33)_c(\xi_3))$	(72 7020 -153)	(6870)	(-0.3 0.75 0.59)
	$(1^5D_{4+-}(66)_c(\xi_1 \otimes \xi_2))$	(31 -153 7079)	(7211)	(0.25 0.66 -0.71)

TABLE XI: Predicted mass spectra for the $cc\bar{c}\bar{c}$ systems up to the $1S$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{++}	$1^1S_{0++}(66)_c$	(19338 -23)	(19306)	((0.58 -0.81))
	$1^1S_{0++}(33)_c$	(-23 19322)	(19355)	((-0.81 -0.58))
1^{+-}	$1^3S_{1+-}(33)_c$	(19329)	19329	1
2^{++}	$1^5S_{2++}(33)_c$	(19341)	19341	1

TABLE XII: Predicted mass spectra for the $bb\bar{b}\bar{b}$ systems up to the $2S$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{+-}	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19840 \quad 3 \quad 19790)$	$(19840 \quad 19790)$	$\begin{pmatrix} (-1.0000 & -0.0500) \\ (0.0500 & -1.0000) \end{pmatrix}$
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$			
0^{++}	$2^1S_{0^{++}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19770 \quad -7 \quad 32 \quad -3)$	(19765)	$\begin{pmatrix} (-0.97 & -0.07 & 0.15 & 0.15) \\ (0.12 & -0.93 & -0.02 & 0.35) \end{pmatrix}$
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(-7 \quad 19797 \quad -2 \quad -28)$	(19809)	
	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	$(32 \quad -2 \quad 19972 \quad -4)$	(19977)	$\begin{pmatrix} (-0.16 & 0.01 & -0.99 & 0.02) \\ (0.12 & 0.36 & 0 & 0.93) \end{pmatrix}$
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	$(-3 \quad -28 \quad -4 \quad 19733)$	(19722)	
1^{+-}	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(19792 \quad 0)$	(19792)	$\begin{pmatrix} (1 & 0) \\ (0 & 1) \end{pmatrix}$
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	$(0 \quad 19735)$	(19735)	
1^{++}	$2^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	(19800)	19800	1
	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	(19795)	19795	1
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(19804 \quad -28)$	(19815)	$\begin{pmatrix} (-0.94 & 0.35) \\ (0.35 & -0.94) \end{pmatrix}$
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	$(-28 \quad 19738)$	(19727)	

TABLE XIII: Predicted masses for the P -wave $cc\bar{c}\bar{c}$ states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{--}	$1^3P_{0^{--}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19579 \quad 129)$	(19485)	$\begin{pmatrix} (-0.81 & 0.59) \\ (0.59 & 0.81) \end{pmatrix}$
	$1^3P_{0^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(129 \quad 19662)$	(19756)	
0^{-+}	$1^3P_{0^{-+}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19577 \quad -110 \quad 15)$	(19500)	$\begin{pmatrix} (0.82 & 0.56 & -0.09) \\ (0.02 & 0.13 & 0.99) \\ (0.57 & -0.82 & 0.10) \end{pmatrix}$
	$1^3P_{0^{-+}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(-110 \quad 19662 \quad -7)$	(19595)	
	$1^3P_{0^{-+}(\bar{3}3)_c(\xi_3)}$	$(15 \quad -7 \quad 19596)$	(19739)	
1^{--}	$1^3P_{1^{--}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19571 \quad -129 \quad 12 \quad -12 \quad 7)$	(19479)	$\begin{pmatrix} (-0.82 & -0.57 & 0.06 & -0.01 & 0.03) \\ (0.00 & 0.10 & 0.98 & -0.02 & 0.18) \\ (0.00 & 0.03 & -0.18 & 0.04 & 0.98) \\ (0.53 & -0.76 & 0.08 & 0.36 & 0.02) \\ (0.22 & -0.28 & 0.00 & -0.93 & 0.05) \end{pmatrix}$
	$1^3P_{1^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(-129 \quad 19662 \quad -5 \quad 10 \quad -3)$	(19597)	
	$1^5P_{1^{--}(\bar{3}3)_c(\xi_3)}$	$(12 \quad -5 \quad 19598 \quad 4 \quad -1)$	(19603)	
	$1^1P_{1^{--}(\bar{3}3)_c(\xi_3)}$	$(-12 \quad 10 \quad 4 \quad 19789 \quad -8)$	(19749)	
	$1^1P_{1^{--}(6\bar{6})_c(\xi_3)}$	$(7 \quad -3 \quad -1 \quad -8 \quad 19604)$	(19795)	
1^{+-}	$1^3P_{1^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19579 \quad -118 \quad -4)$	(19496)	$\begin{pmatrix} (0.82 & 0.57 & 0.02) \\ (0.00 & 0.03 & -1.00) \\ (-0.57 & 0.82 & 0.02) \end{pmatrix}$
	$1^3P_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(-118 \quad 19665 \quad 2)$	(19603)	
	$1^3P_{1^{+-}(\bar{3}3)_c(\xi_3)}$	$(-4 \quad 2 \quad 19604)$	(19748)	
2^{--}	$1^3P_{2^{--}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19576 \quad 138 \quad 8)$	(19476)	$\begin{pmatrix} (0.81 & -0.59 & -0.03) \\ (0.00 & 0.06 & -1.00) \\ (0.59 & 0.81 & 0.05) \end{pmatrix}$
	$1^3P_{2^{--}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(138 \quad 19667 \quad 4)$	(19608)	
	$1^5P_{2^{--}(\bar{3}3)_c(\xi_3)}$	$(8 \quad 4 \quad 19609)$	(19767)	
2^{+-}	$1^3P_{2^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	$(19580 \quad -124 \quad 5)$	(19492)	$\begin{pmatrix} (0.82 & 0.58 & -0.02) \\ (0.00 & -0.04 & -1.00) \\ (-0.58 & 0.82 & -0.03) \end{pmatrix}$
	$1^3P_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	$(-124 \quad 19668 \quad -2)$	(19609)	
	$1^3P_{2^{+-}(\bar{3}3)_c(\xi_3)}$	$(5 \quad -2 \quad 19609)$	(19756)	
3^{--}	$1^5P_{3^{--}(\bar{3}3)_c(\xi_3)}$	(19587)	19587	1

TABLE XIV: Predicted mass spectra for the $b\bar{b}b\bar{b}$ systems up to the 1D-wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
0^{+-}	$\begin{pmatrix} 1^3P_{0^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{0^{+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19693 & -116 \\ -116 & 19775 \end{pmatrix}$	$\begin{pmatrix} 19611 \\ 19857 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ 0.58 & -0.82 \end{pmatrix}$
0^{+-}	$1^5D_{0^{+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19884)	19884	1
0^{++}	$1^1S_{0^{++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2)}$	(19677)	19677	1
0^{++}	$1^1S_{0^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19796)	19796	1
0^{++}	$\begin{pmatrix} 1^3P_{0^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{0^{++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19688 & 125 \\ 125 & 19773 \end{pmatrix}$	$\begin{pmatrix} 19598 \\ 19863 \end{pmatrix}$	$\begin{pmatrix} -0.81 & 0.58 \\ 0.58 & 0.81 \end{pmatrix}$
0^{++}	$1^3P_{0^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19884)	19884	1
0^{++}	$\begin{pmatrix} 1^5D_{0^{++}(\bar{3}\bar{3})_c(\xi_1, \xi_2)} \\ 1^5D_{0^{++}(\bar{3}\bar{3})_c(\xi_3)} \\ 1^5D_{0^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 19873 & 59 & 22 \\ 59 & 19800 & -126 \\ 22 & -126 & 19847 \end{pmatrix}$	$\begin{pmatrix} 19885 \\ 19677 \\ 19958 \end{pmatrix}$	$\begin{pmatrix} 0.91 & 0.04 & 0.4 \\ -0.29 & 0.75 & 0.59 \\ 0.28 & 0.66 & -0.7 \end{pmatrix}$
1^{-+}	$\begin{pmatrix} 1^3S_{1^{-+}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3S_{1^{-+}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19812 & -24 \\ -24 & 19828 \end{pmatrix}$	$\begin{pmatrix} 19795 \\ 19845 \end{pmatrix}$	$\begin{pmatrix} 0.81 & 0.58 \\ 0.58 & -0.81 \end{pmatrix}$
1^{-+}	$1^3S_{1^{-+}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19802)	19802	1
1^{-+}	$1^1P_{1^{-+}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2)}$	(19711)	19711	1
1^{-+}	$1^1P_{1^{-+}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2)}$	(19883)	19883	1
1^{-+}	$\begin{pmatrix} 1^3P_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{1^{+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19692 & -116 \\ -116 & 19774 \end{pmatrix}$	$\begin{pmatrix} 19610 \\ 19856 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ -0.58 & 0.82 \end{pmatrix}$
1^{-+}	$1^5P_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19890)	19890	1
1^{-+}	$1^3D_{1^{+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19889)	19889	1
1^{-+}	$1^3D_{1^{+-}(\bar{3}\bar{3})_c(\xi_3)}$	$\begin{pmatrix} 19803 & -131 \\ -131 & 19845 \end{pmatrix}$	$\begin{pmatrix} 19691 \\ 19957 \end{pmatrix}$	$\begin{pmatrix} -0.76 & -0.65 \\ -0.65 & 0.76 \end{pmatrix}$
1^{-+}	$1^3D_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	$\begin{pmatrix} 19906 & 70 \\ 70 & 19856 \end{pmatrix}$	$\begin{pmatrix} 19955 \\ 19807 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ 0.58 & -0.82 \end{pmatrix}$
1^{-+}	$1^5D_{1^{+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2)}$	(19887)	19887	1
1^{++}	$\begin{pmatrix} 1^3S_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3S_{1^{++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19807 & 34 \\ 34 & 19827 \end{pmatrix}$	$\begin{pmatrix} 19782 \\ 19852 \end{pmatrix}$	$\begin{pmatrix} -0.8 & 0.6 \\ 0.6 & 0.8 \end{pmatrix}$
1^{++}	$\begin{pmatrix} 1^3P_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{1^{++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19690 & 127 \\ 127 & 19773 \end{pmatrix}$	$\begin{pmatrix} 19598 \\ 19865 \end{pmatrix}$	$\begin{pmatrix} -0.81 & 0.59 \\ 0.59 & 0.81 \end{pmatrix}$
1^{++}	$1^3P_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19883)	19883	1
1^{++}	$1^3D_{1^{++}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19877)	19877	1
1^{++}	$\begin{pmatrix} 1^3D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3D_{1^{++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19907 & -62 \\ -62 & 19856 \end{pmatrix}$	$\begin{pmatrix} 19949 \\ 19814 \end{pmatrix}$	$\begin{pmatrix} -0.83 & 0.55 \\ 0.56 & 0.83 \end{pmatrix}$
1^{++}	$\begin{pmatrix} 1^5D_{1^{++}(\bar{3}\bar{3})_c(\xi_1, \xi_2)} \\ 1^5D_{1^{++}(\bar{3}\bar{3})_c(\xi_3)} \\ 1^5D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)} \end{pmatrix}$	$\begin{pmatrix} 19876 & 60 & 23 \\ 60 & 19802 & -127 \\ 23 & -127 & 19850 \end{pmatrix}$	$\begin{pmatrix} 19889 \\ 19678 \\ 19961 \end{pmatrix}$	$\begin{pmatrix} 0.91 & 0.04 & 0.4 \\ -0.3 & 0.75 & 0.59 \\ 0.28 & 0.66 & -0.7 \end{pmatrix}$
2^{+-}	$\begin{pmatrix} 1^3P_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \\ 1^3P_{2^{+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)} \end{pmatrix}$	$\begin{pmatrix} 19695 & -119 \\ -119 & 19779 \end{pmatrix}$	$\begin{pmatrix} 19611 \\ 19863 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ -0.58 & 0.82 \end{pmatrix}$
2^{+-}	$1^5P_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	(19891)	19891	1
2^{+-}	$1^1D_{2^{+-}(\bar{6}\bar{6})_c(\xi_1, \xi_2)}$	(19807)	19807	1
2^{+-}	$1^1D_{2^{+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19895)	19895	1
2^{+-}	$1^3D_{2^{+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19894)	19894	1
2^{+-}	$1^3D_{2^{+-}(\bar{3}\bar{3})_c(\xi_3)}$	$\begin{pmatrix} 19806 & -133 \\ -133 & 19852 \end{pmatrix}$	$\begin{pmatrix} 19694 \\ 19964 \end{pmatrix}$	$\begin{pmatrix} -0.76 & -0.64 \\ -0.64 & 0.76 \end{pmatrix}$
2^{+-}	$1^3D_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	$\begin{pmatrix} 19910 & 68 \\ 68 & 19863 \end{pmatrix}$	$\begin{pmatrix} 19958 \\ 19815 \end{pmatrix}$	$\begin{pmatrix} -0.81 & -0.58 \\ 0.58 & -0.81 \end{pmatrix}$
2^{+-}	$1^5D_{2^{+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2)}$	(19893)	19893	1

TABLE XV: Predicted mass spectra for the $bb\bar{b}\bar{b}$ systems up to the $1D$ -wave states.

$J^{P(C)}$	Configuration	$\langle H \rangle$ (MeV)	Mass (MeV)	Eigenvector
2^{++}	$(1^5S_{2++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2))$	(19814)	19814	1
2^{++}	$(1^3P_{2++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19691 & 129 \\ 129 & 19777 \end{pmatrix}$	$\begin{pmatrix} 19598 \\ 19870 \end{pmatrix}$	$\begin{pmatrix} -0.81 & 0.58 \\ 0.58 & 0.81 \end{pmatrix}$
2^{++}	$(1^3P_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	(19891)	19891	1
2^{++}	$(1^1D_{2++}(\bar{6}\bar{6})_c(\xi_1, \xi_2))$	$\begin{pmatrix} 19773 & 156 & 29 \\ 156 & 19770 & -133 \\ 29 & -133 & 19697 \end{pmatrix}$	$\begin{pmatrix} 19952 \\ 19758 \\ 19530 \end{pmatrix}$	$\begin{pmatrix} -0.59 & -0.74 & 0.32 \\ 0.64 & -0.2 & 0.74 \\ 0.48 & -0.64 & -0.59 \end{pmatrix}$
2^{++}	$(1^1D_{2++}(\bar{6}\bar{6})_c(\xi_3))$			
2^{++}	$(1^1D_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2))$			
2^{++}	$(1^1D_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2, \xi_3))$	$\begin{pmatrix} 19881 & 63 & 30 \\ 63 & 19806 & -135 \\ 30 & -135 & 19848 \end{pmatrix}$	$\begin{pmatrix} 19968 \\ 19669 \\ 19898 \end{pmatrix}$	$\begin{pmatrix} 0.25 & 0.67 & -0.7 \\ -0.3 & 0.74 & 0.61 \\ 0.92 & 0.06 & 0.39 \end{pmatrix}$
2^{++}	$(1^3D_{2++}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$	(19881)	19881	1
2^{++}	$(1^3D_{2++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19910 & -63 \\ -63 & 19862 \end{pmatrix}$	$\begin{pmatrix} 19953 \\ 19819 \end{pmatrix}$	$\begin{pmatrix} -0.82 & 0.57 \\ -0.57 & -0.82 \end{pmatrix}$
2^{++}	$(1^5D_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19881 & 61 & 26 \\ 61 & 19807 & -129 \\ 26 & -129 & 19856 \end{pmatrix}$	$\begin{pmatrix} 19896 \\ 19680 \\ 19968 \end{pmatrix}$	$\begin{pmatrix} 0.92 & 0.06 & 0.39 \\ -0.3 & 0.75 & 0.59 \\ 0.25 & 0.66 & -0.7 \end{pmatrix}$
3^{+-}	$(1^5P_{3+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2))$	(19902)	19902	1
3^{+-}	$(1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$	(19901)	19901	1
3^{+-}	$(1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_3))$			
3^{+-}	$(1^3D_{3+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2))$	$\begin{pmatrix} 19812 & -135 \\ -135 & 19857 \end{pmatrix}$	$\begin{pmatrix} 19698 \\ 19971 \end{pmatrix}$	$\begin{pmatrix} 0.76 & 0.65 \\ -0.65 & 0.76 \end{pmatrix}$
3^{+-}	$(1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19917 & 68 \\ 68 & 19869 \end{pmatrix}$	$\begin{pmatrix} 19965 \\ 19821 \end{pmatrix}$	$\begin{pmatrix} -0.82 & -0.58 \\ 0.58 & -0.82 \end{pmatrix}$
3^{+-}	$(1^5D_{3+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$	(19901)	19901	1
3^{++}	$(1^3D_{3++}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$	(19887)	19887	1
3^{++}	$(1^3D_{3++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19917 & -61 \\ -61 & 19869 \end{pmatrix}$	$\begin{pmatrix} 19959 \\ 19827 \end{pmatrix}$	$\begin{pmatrix} 0.83 & -0.56 \\ 0.56 & 0.83 \end{pmatrix}$
3^{++}	$(1^5D_{3++}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$			
3^{++}	$(1^5D_{3++}(\bar{3}\bar{3})_c(\xi_3))$			
3^{++}	$(1^5D_{3++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3))$	$\begin{pmatrix} 19887 & 62 & 28 \\ 62 & 19813 & -131 \\ 28 & -131 & 19864 \end{pmatrix}$	$\begin{pmatrix} 19904 \\ 19684 \\ 19976 \end{pmatrix}$	$\begin{pmatrix} 0.92 & 0.08 & 0.38 \\ -0.31 & 0.75 & 0.59 \\ -0.24 & -0.66 & 0.71 \end{pmatrix}$
4^{+-}	$(1^5D_{4+-}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$	(7122)	19908	1
4^{++}	$(1^3D_{4++}(\bar{3}\bar{3})_c(\xi_1, \xi_2))$			
4^{++}	$(1^5D_{4++}(\bar{3}\bar{3})_c(\xi_3))$			
4^{++}	$(1^5D_{4++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2))$	$\begin{pmatrix} 19894 & 63 & 30 \\ 63 & 19819 & -134 \\ 30 & -134 & 19871 \end{pmatrix}$	$\begin{pmatrix} 19912 \\ 19686 \\ 19985 \end{pmatrix}$	$\begin{pmatrix} 0.92 & 0.1 & 0.37 \\ -0.31 & 0.74 & 0.59 \\ -0.22 & -0.66 & 0.72 \end{pmatrix}$

TABLE XVI: The average contributions of each part of the Hamiltonian to the $c\bar{c}\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0^{+-}	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	7008	706	899	-540	10		
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7005	776	924	-629	3		
0^{++}	$2^1S_{0^{++}(6\bar{6})_c(\xi_1,\xi_2)}$	6954	725	883	-598	11		
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7000	774	919	-622	-4		
	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	7183	757	1010	-522	7		
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	6930	761	876	-642	3		
1^{+-}	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7009	773	925	-628	7		
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	6934	745	885	-634	6		
1^{++}	$^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7006	774	920	-622	2		
2^{+-}	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	7017	762	932	-624	15		
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	7018	753	932	-613	14		
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	6942	741	888	-633	14		

TABLE XVII: The average contributions of each part of the Hamiltonian to the $cc\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0 ⁻⁻	$1^3P_{0--}(66)_c(\xi_1,\xi_2)$	6751	716	778	-686	1.62	12.92	-4.31
	$1^3P_{0--}(\bar{3}3)_c(\xi_1,\xi_2)$	6827	741	811	-651	0.62	3.04	-9.11
0 ⁺	$1^3P_{0-+}(6\bar{6})_c(\xi_1,\xi_2)$	6746	727	773	-691	11.59	-1.48	-4.43
	$1^3P_{0-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6825	745	808	-653	4.7	-3.07	-9.22
	$1^3P_{0-+}(\bar{3}3)_c(\xi_3)$	6750	765	769	-694	4.22	-6.45	-19.36
1 ⁻⁻	$1^3P_{1--}(66)_c(\xi_1,\xi_2)$	6733	743	765	-699	1.73	-6.89	-2.3
	$1^3P_{1--}(\bar{3}3)_c(\xi_1,\xi_2)$	6827	741	811	-651	0.62	-1.52	-4.55
	$1^5P_{1--}(\bar{3}3)_c(\xi_3)$	6754	761	771	-692	15.62	-4.47	-28.76
	$1^1P_{1--}(\bar{3}3)_c(\xi_3)$	6968	714	886	-578	13.51	0	0
	$1^1P_{1--}(66)_c(\xi_3)$	6770	734	784	-679	-1.38	0	0
1 ⁻⁺	$1^3P_{1-+}(6\bar{6})_c(\xi_1,\xi_2)$	6751	720	776	-688	11.45	0.73	-2.18
	$1^3P_{1-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6834	732	815	-647	4.63	1.49	-4.46
	$1^3P_{1-+}(\bar{3}3)_c(\xi_3)$	6769	736	783	-680	4.03	3.01	-9.03
2 ⁻⁻	$1^3P_{2--}(66)_c(\xi_1,\xi_2)$	6751	720	776	-688	11.45	0.73	-2.18
	$1^3P_{2--}(\bar{3}3)_c(\xi_1,\xi_2)$	6834	732	815	-647	4.63	1.49	-4.46
	$1^5P_{2--}(\bar{3}3)_c(\xi_3)$	6769	736	783	-680	4.03	3.01	-9.03
2 ⁻⁺	$1^3P_{2-+}(6\bar{6})_c(\xi_1,\xi_2)$	6754	715	779	-685	11.35	-0.14	2.15
	$1^3P_{2-+}(\bar{3}3)_c(\xi_1,\xi_2)$	6841	721	821	-642	4.57	-0.29	4.35
	$1^3P_{2-+}(\bar{3}3)_c(\xi_3)$	6783	715	794	-670	3.89	-0.57	8.59
3 ⁻⁻	$1^5P_{3--}(\bar{3}3)_c(\xi_3)$	6795	693	803	-663	13.92	-1.12	16.87

TABLE XVIII: The average contributions of each part of the Hamiltonian to the $cc\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0^{+-}	$1^3P_{0^{+-}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6868	732	837	-636	6.18	0	-2.28
	$1^3P_{0^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6948	749	876	-601	-2.66	0	-4.73
	$1^5D_{0^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	7054	809	924	-572	9.25	-5.91	-43.52
0^{++}	$1^1S_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_2)}$	6838	769	818	-657	-24.14	0	0
	$1^1S_{0^{++}(66)_c(\xi_1 \otimes \xi_2)}$	6957	788	877	-603	-37.55	0	0
	$1^3P_{0^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6857	745	830	-642	-2.02	-2.35	-2.35
	$1^3P_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6944	754	873	-603	-6.08	-0.96	-4.79
	$1^3P_{0^{++}(66)_c(\xi_1 \otimes \xi_2)}$	7053	775	925	-553	-15.43	2.49	-12.47
	$1^5D_{0^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	7051	798	927	-577	9.84	-4.46	-35.39
	$1^5D_{0^{++}(\bar{3}3)_c(\xi_3)}$	6968	783	883	-603	10.84	-4.59	-32.12
	$1^5D_{0^{++}(66)_c(\xi_1 \otimes \xi_2)}$	7013	802	902	-585	9.78	-5.96	-41.73
1^{+-}	$1^3S_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7002	739	908	-584	7.19	0	0
	$1^3S_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7007	743	906	-571	-2.36	0	0
	$1^3S_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	6973	768	888	-595	-20.14	0	0
	$1^1P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_2)}$	6871	767	834	-637	-23.89	0	0
	$1^1P_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7052	776	924	-554	-26.86	0	0
	$1^3P_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6867	733	836	-637	6.2	-0.86	-2.58
	$1^3P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6946	753	874	-603	-2.68	-1.79	-5.37
	$1^5P_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7069	754	937	-545	7.04	0.6	-16.07
1^{++}	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	7070	783	939	-562	-0.47	-0.76	-20.53
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_3)}$	6978	767	891	-597	-1.51	1.23	-15.46
	$1^3D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7092	782	953	-555	1.73	-0.06	-19.86
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7026	786	912	-575	-4.9	-2.18	-21.88
	$1^3D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7008	804	901	-586	-18.28	-2.98	-20.89
	$1^5D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	7064	794	933	-566	8.98	-2.86	-35.06
	$1^3S_{1^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6991	747	903	-588	-3.32	0	0
	$1^3S_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7003	746	903	-572	-6.56	0	0
1^{++}	$1^3P_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6861	739	833	-640	-2	2.03	-2.61
	$1^3P_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6944	755	873	-603	-6.09	-0.6	-5.39
	$1^3P_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7051	779	923	-555	-15.54	-3.14	-9.43
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	7062	781	937	-570	-1.23	-0.13	-17.01
	$1^3D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7096	777	956	-554	2.85	1.81	-19.64
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7028	784	913	-574	-4.41	-1.4	-21.78
	$1^5D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	7059	786	934	-572	9.62	-2.17	-28.72
	$1^5D_{1^{++}(\bar{3}3)_c(\xi_3)}$	6976	772	889	-599	10.6	-2.24	-26.09
2^{+-}	$1^5D_{1^{++}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7022	787	911	-580	9.49	-2.88	-33.63
	$1^3P_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6873	725	841	-633	6.1	0.17	2.53
	$1^3P_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	6959	735	884	-595	-2.57	0.34	5.15
	$1^5P_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7072	751	939	-544	6.99	-4.13	-8.86
	$1^1D_{2^{+-}(\bar{6}\bar{6})_c(\xi_1, \xi_2)}$	6985	727	895	-575	5.62	0	0
	$1^1D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	7087	760	953	-553	-4.84	0	0
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	7085	762	952	-554	-0.44	0.72	-6.52
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_3)}$	6985	755	898	-592	-1.48	-1.2	-5.02
2^{++}	$1^3D_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7106	763	964	-549	1.67	0.06	-6.35
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	7045	760	927	-565	-4.63	2.05	-6.87
	$1^3D_{2^{+-}(\bar{6}\bar{6})_c(\xi_1 \otimes \xi_2)}$	7028	774	917	-575	-17.3	2.8	-6.53
	$1^5D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	7082	768	948	-556	8.53	1.16	-19.86

TABLE XIX: The average contributions of each part of the Hamiltonian to the $cc\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
	$1^5S_{2++}(66)_c(\xi_1 \otimes \xi_2)$	7004	731	911	-581	11.30	0	0
	$1^3P_{2++}(66)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6864	735	835	-638	-1.99	-0.4	2.58
	$1^3P_{2++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	6955	739	882	-597	-5.89	0.12	5.19
	$1^3P_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7073	748	941	-543	-14.59	0.59	8.79
	$1^1D_{2++}(6\bar{6})_c(\xi_1, \xi_2)$	6955	733	883	-598	5.68	0	0
	$1^1D_{2++}(\bar{3}3)_c(\xi_1, \xi_2)$	7073	764	947	-563	-6.38	0	0
	$1^1D_{2++}(6\bar{6})_c(\xi_3)$	6964	744	894	-613	6.43	0	0
	$1^1D_{2++}(\bar{3}3)_c(\xi_3)$	6986	754	899	-591	-7.33	0	0
2^{++}	$1^1D_{2++}(\bar{3}3)_c(\xi_1 \otimes \xi_2)$	6859	769	829	-647	-24.01	0	0
	$1^1D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7018	787	910	-579	-31.28	0	0
	$1^3D_{2++}(\bar{3}3)_c(\xi_1, \xi_2)$	7073	765	947	-564	-1.19	0.12	-5.47
	$1^3D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7105	764	963	-549	2.77	-1.76	-6.36
	$1^3D_{2++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7045	760	927	-565	-4.2	1.33	-6.87
	$1^5D_{2++}(\bar{3}3)_c(\xi_1, \xi_2)$	7073	766	946	-564	9.24	0.89	-16.46
	$1^5D_{2++}(\bar{3}3)_c(\xi_3)$	6989	752	900	-591	10.19	0.92	-14.97
	$1^5D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7040	761	925	-570	9.03	1.17	-19.07
	$1^5P_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7102	711	964	-529	6.38	1.08	16.13
	$1^3D_{3+-}(\bar{3}3)_c(\xi_1, \xi_2)$	7103	738	967	-545	-0.4	-0.2	12.34
	$1^3D_{3+-}(\bar{3}3)_c(\xi_3)$	7002	733	911	-583	-1.43	0.32	9.54
3^{+-}	$1^3D_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7124	739	979	-539	1.6	-0.02	12.01
	$1^3D_{3+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7062	736	942	-555	-4.4	-0.55	13
	$1^3D_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7043	752	930	-566	-16.57	-0.76	12.43
	$1^5D_{3+-}(\bar{3}3)_c(\xi_1, \xi_2)$	7103	740	965	-545	8.04	2.89	0
	$1^3D_{3++}(\bar{3}3)_c(\xi_1, \xi_2)$	7089	743	960	-555	-1.14	-0.03	10.41
	$1^3D_{3++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7126	736	981	-538	2.59	0.47	11.94
	$1^3D_{3++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	7063	735	942	-555	-3.99	-0.36	12.97
	$1^5D_{3++}(\bar{3}3)_c(\xi_1, \xi_2)$	7091	742	961	-555	8.81	2.24	0
3^{++}	$1^5D_{3++}(\bar{3}3)_c(\xi_3)$	7005	730	913	-582	9.74	2.32	0
	$1^5D_{3++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7060	734	942	-559	8.52	2.92	0
4^{+-}	$1^5D_{4+-}(\bar{3}3)_c(\xi_1, \xi_2)$	7122	715	982	-536	7.62	-1.36	23.36
4^{++}	$1^5D_{4++}(\bar{3}3)_c(\xi_1, \xi_2)$	7108	720	975	-546	8.42	-1.07	19.74
	$1^5D_{4++}(\bar{3}3)_c(\xi_3)$	7020	710	925	-573	9.34	-1.11	18.09
	$1^5D_{4++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	7079	710	957	-549	8.09	-1.38	22.5

TABLE XX: The average contributions of each part of the Hamiltonian to the $cc\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0^{+-}	$2^1S_{0^{+-}(6\bar{6})_c(\xi_1,\xi_2)}$	19840	627	529	-727	3.99		
	$2^1S_{0^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	19790	701	543	-864	2.28		
0^{++}	$2^1S_{0^{++}(6\bar{6})_c(\xi_1,\xi_2)}$	19770	653	515	-810	4.48		
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	19797	690	538	-837	-1.21		
	$2^1S_{0^{++}(6\bar{6})_c(\xi_3)}$	19972	646	604	-688	2.36		
	$2^1S_{0^{++}(\bar{3}3)_c(\xi_3)}$	19733	694	510	-881	1.58		
1^{+-}	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	19792	700	543	-863	3.81		
	$2^3S_{1^{+-}(\bar{3}3)_c(\xi_3)}$	19735	693	511	-880	3.09		
1^{++}	$^3S_{1^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	19800	690	538	-837	1.14		
2^{+-}	$2^5S_{2^{+-}(\bar{3}3)_c(\xi_1,\xi_2)}$	19795	692	546	-859	6.83		
2^{++}	$2^5S_{2^{++}(\bar{3}3)_c(\xi_1,\xi_2)}$	19804	671	545	-826	5.60		
	$2^5S_{2^{++}(\bar{3}3)_c(\xi_3)}$	19738	692	512	-880	6.11		

TABLE XXI: The average contributions of each part of the Hamiltonian to the $cc\bar{c}\bar{c}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0 ⁻⁻	$1^3P_{0--}(66)_c(\xi_1,\xi_2)$	19579	696	438	-968	0.69	5.58	-1.86
	$1^3P_{0--}(\bar{3}3)_c(\xi_1,\xi_2)$	19662	685	467	-896	0.41	1.21	-3.63
0 ⁺	$1^3P_{0-+}(6\bar{6})_c(\xi_1,\xi_2)$	19577	701	437	-972	5.25	-0.63	-1.89
	$1^3P_{0-+}(\bar{3}3)_c(\xi_1,\xi_2)$	19662	687	467	-898	2.19	-1.22	-3.65
	$1^3P_{0-+}(\bar{3}3)_c(\xi_3)$	19596	713	442	-959	1.86	-2.59	-7.77
1 ⁻⁻	$1^3P_{1--}(66)_c(\xi_1,\xi_2)$	19571	711	434	-978	0.72	-2.89	-0.96
	$1^3P_{1--}(\bar{3}3)_c(\xi_1,\xi_2)$	19662	685	467	-896	0.41	-0.61	-1.82
	$1^5P_{1--}(\bar{3}3)_c(\xi_3)$	19598	711	442	-957	6.58	-1.80	-11.58
	$1^1P_{1--}(\bar{3}3)_c(\xi_3)$	19789	644	517	-785	5.48	0.00	0.00
	$1^1P_{1--}(66)_c(\xi_3)$	19604	698	446	-948	-0.49	0.00	0.00
1 ⁺	$1^3P_{1-+}(6\bar{6})_c(\xi_1,\xi_2)$	19579	698	438	-969	5.21	0.31	-0.93
	$1^3P_{1-+}(\bar{3}3)_c(\xi_1,\xi_2)$	19665	681	469	-893	2.16	0.60	-1.79
	$1^3P_{1-+}(\bar{3}3)_c(\xi_3)$	19604	699	446	-948	1.81	1.25	-3.75
2 ⁻⁻	$1^3P_{2--}(66)_c(\xi_1,\xi_2)$	19576	701	437	-971	0.70	0.56	0.94
	$1^3P_{2--}(\bar{3}3)_c(\xi_1,\xi_2)$	19667	677	470	-891	0.41	0.12	1.78
	$1^5P_{2--}(\bar{3}3)_c(\xi_3)$	19609	690	449	-942	6.29	1.71	-3.67
2 ⁺	$1^3P_{2-+}(6\bar{6})_c(\xi_1,\xi_2)$	19580	695	438	-967	5.18	-0.06	0.93
	$1^3P_{2-+}(\bar{3}3)_c(\xi_1,\xi_2)$	19668	675	471	-890	2.15	-0.12	1.77
	$1^3P_{2-+}(\bar{3}3)_c(\xi_3)$	19609	688	449	-941	1.77	-0.24	3.64
3 ⁻⁻	$1^5P_{3--}(\bar{3}3)_c(\xi_3)$	19587	723	466	-1026	7.57	-0.61	9.19

TABLE XXII: The average contributions of each part of the Hamiltonian to the $bb\bar{b}\bar{b}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
0^{+-}	$1^3P_{0^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19693	677	482	-876	2.6	0	-0.91
	$1^3P_{0^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19775	667	514	-812	-0.98	0	-1.77
	$1^5D_{0^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19884	674	561	-746	3.24	-1.98	-14.56
0^{++}	$1^1S_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_2)}$	19677	697	475	-893	-9.68	0	0
	$1^1S_{0^{++}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19796	681	523	-801	-13.94	0	0
	$1^3P_{0^{++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19688	684	480	-881	-0.91	-0.92	-0.92
	$1^3P_{0^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19773	670	513	-813	-2.37	-0.36	-1.78
	$1^3P_{0^{++}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19884	655	557	-728	-5.53	0.86	-4.3
	$1^5D_{0^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	19873	674	559	-757	3.56	-1.53	-12.13
	$1^5D_{0^{++}(\bar{3}3)_c(\xi_3)}$	19800	678	525	-803	4.05	-1.64	-11.46
1^{-+}	$1^5D_{0^{++}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19847	676	544	-768	3.49	-2.04	-14.25
	$1^3S_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19812	662	535	-796	2.97	0	0
	$1^3S_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19828	653	536	-768	-0.73	0	0
	$1^3S_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19802	671	526	-796	-7.59	0	0
	$1^1P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_2)}$	19711	689	488	-864	-9.56	0	0
	$1^1P_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19883	656	557	-728	-9.59	0	0
	$1^3P_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19692	678	482	-877	2.61	-0.34	-1.02
1^{+-}	$1^3P_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19774	669	514	-813	-0.98	-0.67	-2
	$1^5P_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19890	646	561	-722	2.51	0.21	-5.67
	$1^3D_{1^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19889	664	565	-740	-0.13	-0.26	-7.1
	$1^3D_{1^{+-}(\bar{3}3)_c(\xi_3)}$	19803	672	528	-799	-0.63	0.45	-5.64
	$1^3D_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19906	662	573	-731	0.66	-0.02	-6.86
	$1^3D_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19856	668	548	-758	-1.73	-0.75	-7.58
	$1^3D_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19845	678	543	-769	-6.61	-1.02	-7.15
1^{++}	$1^5D_{1^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19887	668	563	-742	3.2	-0.97	-11.95
	$1^3S_{1^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19807	667	533	-799	-1.48	0	0
	$1^3S_{1^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19827	655	535	-770	-2.46	0	0
	$1^3P_{1^{++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19690	681	481	-879	-0.91	0.8	-1.03
	$1^3P_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19773	670	513	-813	-2.37	-0.22	-2.01
	$1^3P_{1^{++}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19883	657	556	-728	-5.55	-1.08	-3.24
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	19877	667	562	-753	-0.44	-0.04	-5.96
2^{+-}	$1^3D_{1^{++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19907	660	574	-730	0.97	0.63	-6.83
	$1^3D_{1^{++}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19856	667	548	-757	-1.6	-0.49	-7.57
	$1^5D_{1^{++}(\bar{3}3)_c(\xi_1, \xi_2)}$	19876	669	561	-754	3.52	-0.75	-9.98
	$1^5D_{1^{++}(\bar{3}3)_c(\xi_3)}$	19802	673	527	-800	4.01	-0.81	-9.44
	$1^5D_{1^{++}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19850	670	546	-765	3.44	-1	-11.69
	$1^3P_{2^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19695	674	483	-874	2.58	0.07	1.01
	$1^3P_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19779	660	517	-807	-0.96	0.13	1.96
2^{++}	$1^5P_{2^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19891	645	561	-721	2.5	-1.46	-3.14
	$1^1D_{2^{+-}(6\bar{6})_c(\xi_1, \xi_2)}$	19807	648	525	-777	2.21	0	0
	$1^1D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19895	654	569	-734	-1.73	0	0
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19894	655	568	-735	-0.12	0.26	-2.31
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_3)}$	19806	667	529	-796	-0.62	-0.44	-1.86
	$1^3D_{2^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19910	654	576	-727	0.65	0.02	-2.24
	$1^3D_{2^{+-}(\bar{3}3)_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)}$	19863	657	552	-751	-1.69	0.73	-2.46
2^{--}	$1^3D_{2^{+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)}$	19852	666	548	-763	-6.44	0.99	-2.31
	$1^5D_{2^{+-}(\bar{3}3)_c(\xi_1, \xi_2)}$	19893	657	567	-736	3.12	0.41	-6.98

TABLE XXIII: The average contributions of each part of the Hamiltonian to the $bb\bar{b}\bar{b}$ configurations. $\langle T \rangle$ stands for the contribution of the kinetic energy term. $\langle V^{Lin} \rangle$ and $\langle V^{Coul} \rangle$ stand for the contributions from the linear confinement potential and Coulomb type potential, respectively. $\langle V^{SS} \rangle$, $\langle V^T \rangle$, and $\langle V^{LS} \rangle$ stand for the contributions from the spin-spin interaction term, the tensor potential term, and the spin-orbit interaction term, respectively.

$J^{P(C)}$	Configuration	Mass	$\langle T \rangle$	$\langle V^{Lin} \rangle$	$\langle V^{Coul} \rangle$	$\langle V^{SS} \rangle$	$\langle V^T \rangle$	$\langle V^{LS} \rangle$
	$1^5S_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19814	653	534	-785	4.39	0	0
	$1^3P_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19691	679	481	-878	-0.9	-0.16	1.03
	$1^3P_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19777	662	516	-809	-2.33	0.04	1.97
	$1^3P_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19891	644	562	-721	-5.38	0.21	3.13
	$1^1D_{2++}(6\bar{6})_c(\xi_1 \cdot \xi_2)$	19773	661	515	-814	2.27	0	0
	$1^1D_{2++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19881	660	564	-749	-2.37	0	0
	$1^1D_{2++}(6\bar{6})_c(\xi_3)$	19770	674	521	-835	2.53	0	0
	$1^1D_{2++}(\bar{3}\bar{3})_c(\xi_3)$	19806	666	530	-796	-2.9	0	0
2^{++}	$1^1D_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_2)$	19697	695	484	-880	-9.67	0	0
	$1^1D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19848	672	546	-766	-11.5	0	0
	$1^3D_{2++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19881	660	564	-749	-0.43	0.04	-1.95
	$1^3D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19910	654	576	-727	0.96	-0.62	-2.24
	$1^3D_{2++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19862	657	552	-751	-1.56	0.47	-2.46
	$1^5D_{2++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19881	660	564	-749	3.45	0.32	-5.86
	$1^5D_{2++}(\bar{3}\bar{3})_c(\xi_3)$	19807	665	530	-795	3.93	0.34	-5.54
	$1^5D_{2++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19856	659	550	-759	3.36	0.42	-6.83
	$1^5P_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19902	627	569	-711	2.39	0.4	5.98
	$1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19901	644	573	-729	-0.12	-0.07	4.5
	$1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_3)$	19812	657	533	-789	-0.61	0.12	3.62
3^{+-}	$1^3D_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19917	643	581	-720	0.64	-0.01	4.36
	$1^3D_{3+-}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19869	647	557	-745	-1.64	-0.2	4.78
	$1^3D_{3+-}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19857	657	552	-757	-6.3	-0.28	4.52
	$1^5D_{3+-}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19901	645	573	-729	3.03	1.05	0
	$1^3D_{3++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19887	651	568	-744	-0.42	-0.01	3.81
	$1^3D_{3++}(6\bar{6})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19917	642	581	-720	0.93	0.17	4.35
	$1^3D_{3++}(\bar{3}\bar{3})_c(\xi_1 \otimes \xi_3, \xi_2 \otimes \xi_3)$	19869	646	557	-745	-1.52	-0.13	4.78
	$1^5D_{3++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19887	650	569	-743	3.37	0.82	0
3^{++}	$1^5D_{3++}(\bar{3}\bar{3})_c(\xi_3)$	19813	655	534	-788	3.83	0.88	0
	$1^5D_{3++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19864	647	555	-751	3.26	1.08	0
4^{+-}	$1^5D_{4+-}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19908	634	578	-722	2.94	-0.51	8.74
4^{++}	$1^5D_{4++}(\bar{3}\bar{3})_c(\xi_1 \cdot \xi_2)$	19894	640	573	-737	3.29	-0.4	7.41
	$1^5D_{4++}(\bar{3}\bar{3})_c(\xi_3)$	19819	645	538	-782	3.75	-0.43	7.02
	$1^5D_{4++}(6\bar{6})_c(\xi_1 \otimes \xi_2)$	19871	636	560	-744	3.17	-0.52	8.56