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Exotic behaviors of $\Omega_c(1P)$ under the unquenched model

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Outline

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3. The masses of $\Omega_c(1P)$ with the coupled-channel effect
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1. Background

The conventional quenched quark model has achieved great successes in hadron physics. But it is difficult to interpret the masses of D_{s0}^* (2317), D'_{s1} (2460), $X(3872)$, $\Lambda_c(2940)$, et al.

	D_{s0}^* (2317)	D'_{s1} (2460)	$X(3872)$	$\Lambda_c(2940)$
PDG [1] (MeV)	2317.8 ± 0.5	2459.5 ± 0.6	3871.69 ± 0.17	$2939.6^{+1.3}_{-1.5}$
potential model [2-4] (MeV)	2484	2556	3950	3035

The experimental measurements are about 100 MeV less than the potential model calculations .

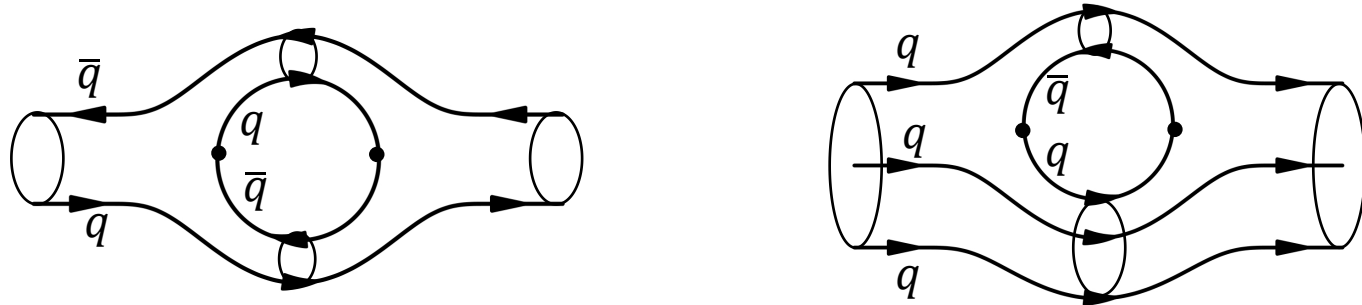
[1] PTEP 2020, 083C01 (2020)

[3] Phys. Rev. D 93, 034035 (2016)

[2] Phys. Rev. D 32, 189 (1985)

[4] Phys. Rev. D 34, 2809 (1986)

In order to understand the masses of D_{s0}^* (2317), D'_{s1} (2460), X (3872), Λ_c (2940), et al., the coupled-channel effect was introduced in hadron physics.



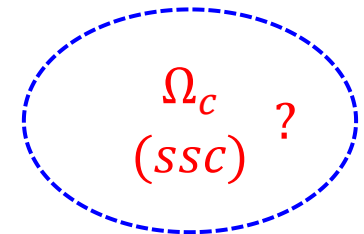
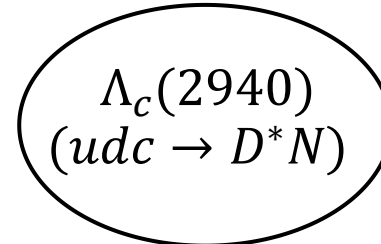
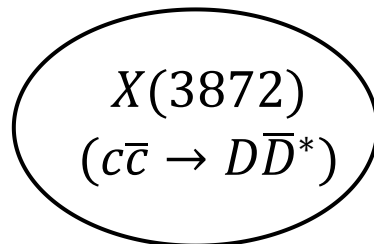
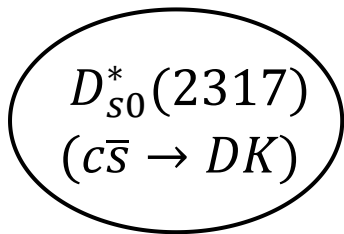
Coupled-channel effects of hadrons.

The hadron loops could affect the masses of hadrons.

$$m = m_0 + \delta m$$

Charmed-strange meson

Charmed-strange baryon



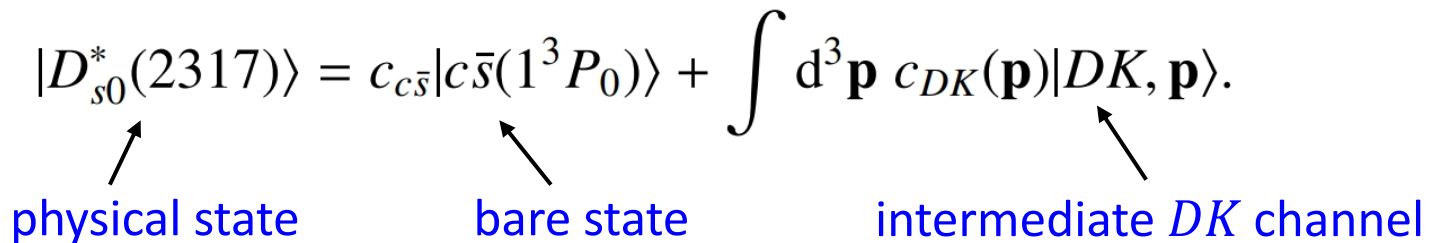
$$\bar{s} \longrightarrow ss$$

2. The interpretation of the $D_{s0}^*(2317)$ under the unquenched model

- (1) Making the calculations for Ω_c more reliable;
- (2) Determining the parameters in the model.

In the unquenched model, the physical state of $D_{s0}^*(2317)$ could be denoted as

$$|D_{s0}^*(2317)\rangle = c_{c\bar{s}}|c\bar{s}(1^3P_0)\rangle + \int d^3\mathbf{p} c_{DK}(\mathbf{p})|DK, \mathbf{p}\rangle.$$



physical state bare state intermediate DK channel

The full Hamiltonian of the physical $D_{s0}^*(2317)$ state could be written as

$$\hat{H} = \begin{pmatrix} \hat{H}_0 & \hat{H}_I \\ \hat{H}_I & \hat{H}_{DK} \end{pmatrix}.$$

The \hat{H}_0 is the Hamiltonian of the bare state with

$$\hat{H}_0 |c\bar{s}(1^3P_0)\rangle = M_0 |c\bar{s}(1^3P_0)\rangle.$$

↑
bare mass

The \hat{H}_I is the Hamiltonian of $c\bar{s}(1^3P_0) \rightarrow DK$ with

$$\mathcal{M}_{c\bar{s}(1^3P_0) \rightarrow DK}(p) = \langle DK, \mathbf{p} | \hat{H}_I | c\bar{s}(1^3P_0) \rangle.$$

↑
amplitude

Without including the interaction of D and K , the Hamiltonian of the intermediate DK channel could be obtained by

$$\hat{H}_{DK} |DK, \mathbf{p}\rangle = \left(\sqrt{m_D^2 + p^2} + \sqrt{m_K^2 + p^2} \right) |DK, \mathbf{p}\rangle.$$

Then, one could obtain the coupled-channel equation

$$M - M_0 - \Delta M(M) = 0.$$

The $\Delta M(M)$ is the mass shift with definition

$$\Delta M(M) = \text{Re} \int_0^\infty p^2 dp \frac{|\mathcal{M}_{c\bar{s}(1^3P_0) \rightarrow DK}(p)|^2}{M - \sqrt{M_D^2 + p^2} - \sqrt{M_K^2 + p^2}}.$$

(1) M_0 : nonrelativistic potential model

(2) $\mathcal{M}_{c\bar{s}(1^3P_0) \rightarrow DK}(p)$: QPC model

Nonrelativistic potential model:

$$\hat{H}_0 = \sum_{i=1} \left(m_i + \frac{p_i^2}{2m_i} \right) + \sum_{i < j} V_{ij}$$

$$V_{ij} = H_{ij}^{\text{conf}} + H_{ij}^{\text{hyp}} + H_{ij}^{\text{so(cm)}} + H_{ij}^{\text{so(tp)}}$$

spin-independent terms:

$$H_{ij}^{\text{conf}} = -\frac{4}{3} \frac{\alpha_s}{r_{ij}} + br_{ij} + C$$

spin-dependent terms:

$$H_{ij}^{\text{hyp}} = \frac{4\alpha_s}{3m_i m_j} \left(\frac{8\pi}{3} \mathbf{s}_i \cdot \mathbf{s}_j \tilde{\delta}(r) + \frac{1}{r_{ij}^3} S(\mathbf{r}_{ij}, \mathbf{s}_i, \mathbf{s}_j) \right)$$

$$\tilde{\delta}(r) = \frac{\sigma^3}{\pi^{3/2}} e^{-\sigma^2 r^2} \quad S(\mathbf{r}_{ij}, \mathbf{s}_i, \mathbf{s}_j) = \frac{3\mathbf{s}_i \cdot \mathbf{r}_{ij} \mathbf{s}_j \cdot \mathbf{r}_{ij}}{r_{ij}^2} - \mathbf{s}_i \cdot \mathbf{s}_j$$

$$H_{ij}^{\text{so(cm)}} = \frac{4\alpha_s}{3r_{ij}^3} \left(\frac{1}{m_i} + \frac{1}{m_j} \right) \left(\frac{\mathbf{s}_i}{m_i} + \frac{\mathbf{s}_j}{m_j} \right) \cdot \mathbf{L}$$

$$H_{ij}^{\text{so(tp)}} = -\frac{1}{2r_{ij}} \frac{\partial H_{ij}^{\text{conf}}}{\partial r_{ij}} \left(\frac{\mathbf{s}_i}{m_i^2} + \frac{\mathbf{s}_j}{m_j^2} \right) \cdot \mathbf{L}$$

QPC model:

$$\hat{H}_I = -3\gamma \sum_m \langle 1, m; 1, -m | 0, 0 \rangle \int d^3 \mathbf{p}_i d^3 \mathbf{p}_j \delta(\mathbf{p}_i + \mathbf{p}_j) \\ \times \mathcal{Y}_1^m \left(\frac{\mathbf{p}_i - \mathbf{p}_j}{2} \right) \omega_0^{(i,j)} \phi_0^{(i,j)} \chi_{1,-m}^{(i,j)} b_i^\dagger(\mathbf{p}_i) d_j^\dagger(\mathbf{p}_j)$$

Parameters:

The parameters in potential model are fixed by the low-lying well established π , K , D , and D_s mesons. The γ value is determined by the width of $D_{s2}^*(2573)$.

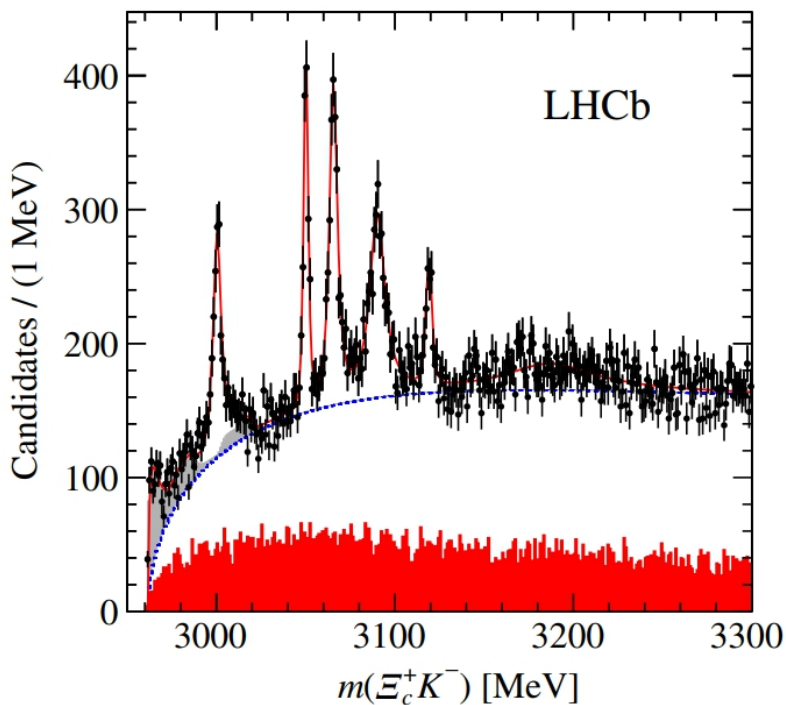
potential model:		QPC model:
$m_{u/d} = 0.370$ GeV	$\alpha_s = 0.578$	$\gamma = 4.1$
$m_s = 0.600$ GeV	$b = 0.144$ GeV ²	
$m_c = 1.880$ GeV	$\sigma = 1.028$ GeV	
	$C = -0.685$ GeV	

Numerical result:

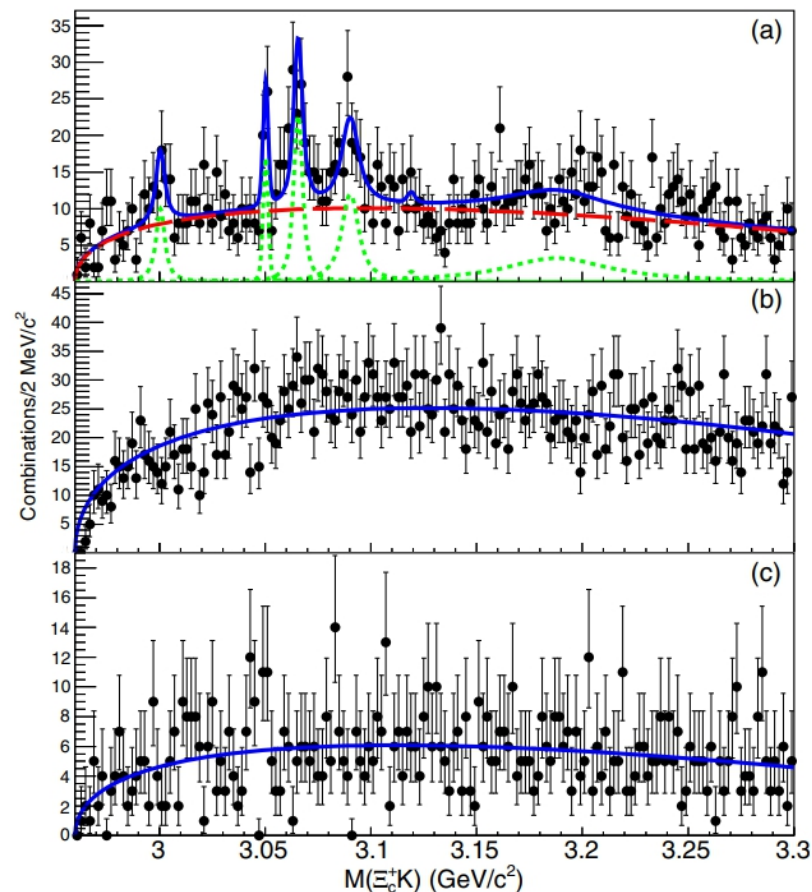
$$\begin{array}{c} M_0 = 2441 \text{ MeV} \\ \hline \downarrow 77 \text{ MeV} \\ \hline M_{\text{phy}} = 2364 \text{ MeV} \end{array}$$

The coupled channel effect plays an important role for $D_{s0}^*(2317)$!

3. The masses of $\Omega_c(1P)$ with the coupled-channel effect

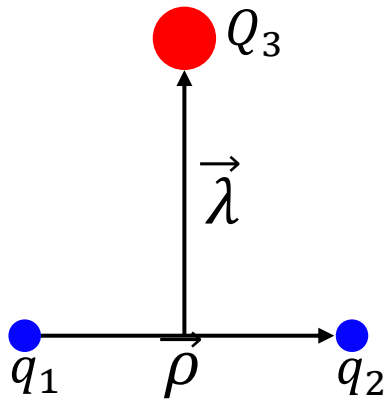


[LHCb] Phys. Rev. Lett. 118, 182001 (2017)



[Belle] Phys. Rev. D 97, 051102 (2018)

It is a good chance for us to study excited Ω_c .



The Jacobi coordinates of a singly heavy flavor baryon.

$$\vec{\rho} = \vec{r}_2 - \vec{r}_1$$

$$\vec{\lambda} = \vec{r}_3 - \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2}{m_1 + m_2}$$

Basis in heavy quark symmetry:

$$|s_\ell, L, j_\ell, J\rangle = |[[s_\ell \otimes L]_{j_\ell} \otimes s_Q]_J\rangle$$

s_ℓ : spin of the light degree of freedom

L : orbital angular momentum of the light degree of freedom

j_ℓ : angular momentum of the light degree of freedom

s_Q : spin of the heavy quark

$$j_\ell(\Xi_c(1S)) = 0$$

$$j_\ell(\Xi'_c(1S)) = 1$$

$$j_\ell(\Xi_c^*(1S)) = 1$$

$$j_\ell(\Omega_c(1S)) = 1$$

$$j_\ell(\Omega_c^*(1S)) = 1$$

$$\lambda\text{-mode excite } \Omega_c(1P) \left\{ \begin{array}{l} J^P = 1/2^- \left\{ \begin{array}{l} j_\ell = 0: \Omega_{c0}(1P, 1/2^-) \\ j_\ell = 1: \Omega_{c1}(1P, 1/2^-) \end{array} \right. \\ J^P = 3/2^- \left\{ \begin{array}{l} j_\ell = 1: \Omega_{c1}(1P, 3/2^-) \\ j_\ell = 2: \Omega_{c2}(1P, 3/2^-) \end{array} \right. \\ J^P = 5/2^-: \quad j_\ell = 2: \Omega_{c2}(1P, 5/2^-) \end{array} \right.$$

Application: strong decays

$$\begin{array}{ccc} \text{singly heavy} & \text{singly heavy} & \text{light flavor} \\ \text{flavor baryon} & \text{flavor baryon} & \text{pseudoscalar meson} \\ A(j_\ell, J, J_z) & \rightarrow & B(j'_\ell, J', J'_z) + C(l, l_z) \\ & & \uparrow \\ & & \text{orbital angular momentum of } BC \end{array}$$

Typical decay channels:

$$\Sigma_c \rightarrow \Lambda_c \pi$$

$$\Xi_c^* \rightarrow \Xi_c \pi$$

$$\Xi_c(2965) \rightarrow \Lambda_c K$$

In heavy quark symmetry, the angular momentum of the light degree of freedom is a conserved quantity in the strong decay process, i.e., $|j'_\ell - l| \leq j_\ell \leq |j'_\ell + l|$.

$$H_{ij}^{\text{conf}} = -\frac{2}{3} \frac{\alpha_s}{r_{ij}} + \frac{b}{2} r_{ij} + C$$

$$H_{ij}^{\text{hyp}} = \frac{2\alpha_s}{3m_i m_j} \left(\frac{8\pi}{3} \mathbf{s}_i \cdot \mathbf{s}_j \tilde{\delta}(r) + \frac{1}{r_{ij}^3} S(\mathbf{r}_{ij}, \mathbf{s}_i, \mathbf{s}_j) \right)$$

$$H_{ij}^{\text{so(cm)}} = \frac{2\alpha_s}{3r_{ij}^3} \left(\frac{\mathbf{r}_{ij} \times \mathbf{p}_i \cdot \mathbf{s}_i}{m_i^2} - \frac{\mathbf{r}_{ij} \times \mathbf{p}_j \cdot \mathbf{s}_j}{m_j^2} - \frac{\mathbf{r}_{ij} \times \mathbf{p}_j \cdot \mathbf{s}_i - \mathbf{r}_{ij} \times \mathbf{p}_i \cdot \mathbf{s}_j}{m_i m_j} \right)$$

$$H_{ij}^{\text{so(tp)}} = -\frac{1}{2r_{ij}} \frac{\partial H_{ij}^{\text{conf}}}{\partial r_{ij}} \left(\frac{\mathbf{r}_{ij} \times \mathbf{p}_i \cdot \mathbf{s}_i}{m_i^2} - \frac{\mathbf{r}_{ij} \times \mathbf{p}_j \cdot \mathbf{s}_j}{m_j^2} \right)$$

$$m_{u/d} = 0.370 \text{ GeV}$$

$$m_s = 0.600 \text{ GeV}$$

$$m_c = 1.880 \text{ GeV}$$

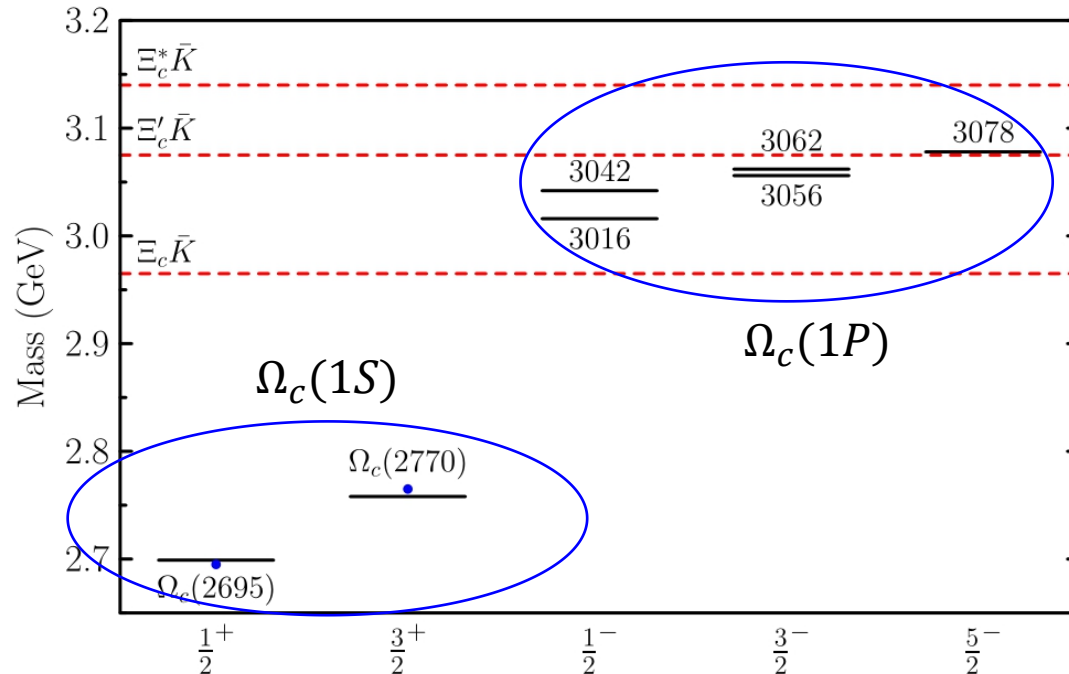
$$\alpha_s = 0.578$$

$$b = 0.144 \text{ GeV}^2$$

$$\sigma = 1.028 \text{ GeV}$$

$$C = -0.685 \text{ GeV}$$

$$\gamma = 8.66$$



The mass spectrum of Ω_c .

The two $J^P = 1/2^-$ of $\Omega_c(1P)$ states could be expanded by $|j_\ell = 0, 1/2^-\rangle$ and $|j_\ell = 1, 1/2^-\rangle$ with the relation

$$\begin{pmatrix} |\frac{1}{2}^-\rangle_1 \\ |\frac{1}{2}^-\rangle_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |j_\ell = 0, \frac{1}{2}^-\rangle \\ |j_\ell = 1, \frac{1}{2}^-\rangle \end{pmatrix},$$

where the θ is the mixing angle.

heavy quark symmetry

$$\begin{aligned} j_\ell(\Xi_c) &= 0 \\ j_\ell(\Xi'_c) &= 1 \end{aligned}$$

$$\left\{ \begin{array}{ll} \Omega_{c0}(1P, 1/2^-) \rightarrow \Xi_c \bar{K} & \text{s-wave} \\ \Omega_{c0}(1P, 1/2^-) \rightarrow \Xi'_c \bar{K} & \text{forbidden} \\ \Omega_{c1}(1P, 1/2^-) \rightarrow \Xi_c \bar{K} & \text{forbidden} \\ \Omega_{c1}(1P, 1/2^-) \rightarrow \Xi'_c \bar{K} & \text{s-wave} \end{array} \right.$$

Then, the coupled-channel Schrödinger equation could be written as

$$\begin{pmatrix} M^{j\ell=0} & \tilde{V}^{\text{spin}} & \int p^2 dp \langle \Omega_{c0} | \hat{H}_I | \Xi_c \bar{K} \rangle & 0 \\ \tilde{V}^{\text{spin}} & M^{j\ell=1} & 0 & \int p^2 dp \langle \Omega_{c1} | \hat{H}_I | \Xi'_c \bar{K} \rangle \\ \langle \Xi_c \bar{K} | \hat{H}_I | \Omega_{c0} \rangle & 0 & H_{\Xi_c \bar{K}} & 0 \\ 0 & \langle \Xi'_c \bar{K} | \hat{H}_I | \Omega_{c1} \rangle & 0 & H_{\Xi'_c \bar{K}} \end{pmatrix} \begin{pmatrix} c_0 \\ c_1 \\ c_{\Xi_c \bar{K}} \\ c_{\Xi'_c \bar{K}} \end{pmatrix} = M \begin{pmatrix} c_0 \\ c_1 \\ c_{\Xi_c \bar{K}} \\ c_{\Xi'_c \bar{K}} \end{pmatrix}.$$



$$\begin{pmatrix} M^{j\ell=0} + \Delta M^0(M) & \tilde{V}^{\text{spin}} \\ \tilde{V}^{\text{spin}} & M^{j\ell=1} + \Delta M^1(M) \end{pmatrix} \begin{pmatrix} c_0 \\ c_1 \end{pmatrix} = M \begin{pmatrix} c_0 \\ c_1 \end{pmatrix}$$

$$\Delta M^0(M) = \text{Re} \int_0^\infty p^2 dp \frac{|\mathcal{M}_{\Omega_{c0} \rightarrow \Xi_c \bar{K}}(p)|^2}{M - \sqrt{M_{\Xi_c}^2 + p^2} - \sqrt{M_K^2 + p^2}}$$

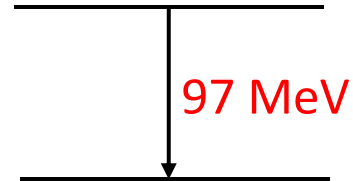
$$\Delta M^1(M) = \text{Re} \int_0^\infty p^2 dp \frac{|\mathcal{M}_{\Omega_{c1} \rightarrow \Xi'_c \bar{K}}(p)|^2}{M - \sqrt{M_{\Xi'_c}^2 + p^2} - \sqrt{M_K^2 + p^2}}$$

Numerical results:

(1) $\Omega_{c0}^d(1P, 1/2^-)$:

(The $j_\ell = 0$ component is dominate.)

$$M_0 = 3042 \text{ MeV}$$



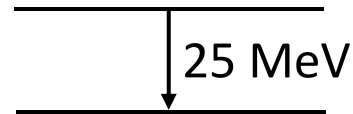
$$M_{\text{phy}} = 2945 \text{ MeV}$$

The coupled-channel effect plays an important role for this state.

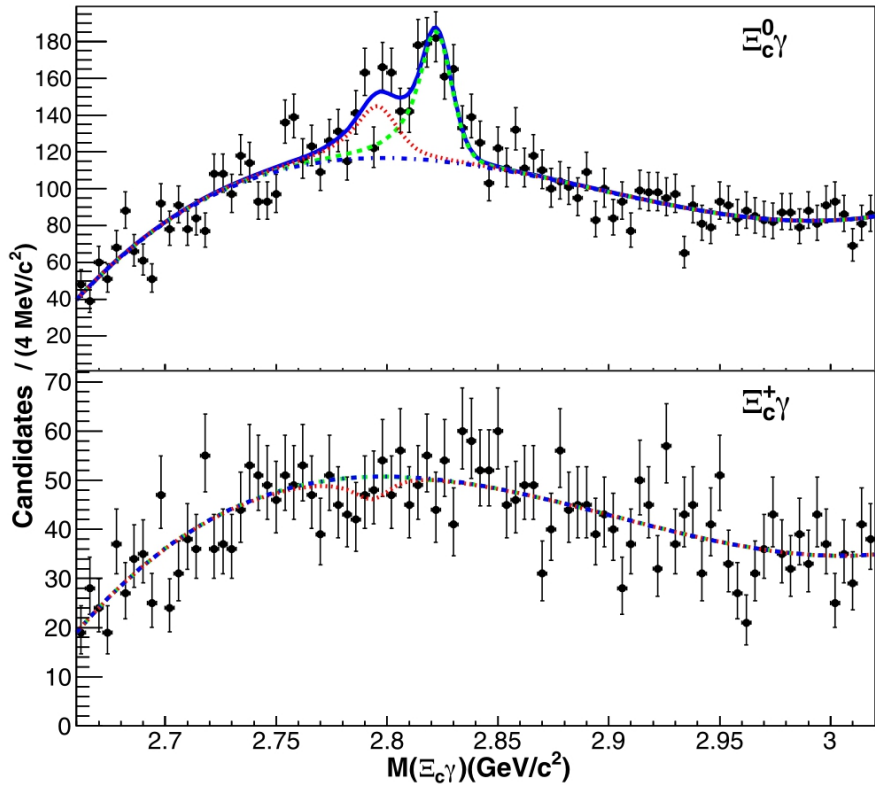
(2) $\Omega_{c1}^d(1P, 1/2^-)$:

(The $j_\ell = 1$ component is dominate.)

$$M_0 = 3016 \text{ MeV}$$



$$M_{\text{phy}} = 2991 \text{ MeV}$$



[Belle] Phys. Rev. D 102, 071103 (2020)

The Belle Collaboration observed *P*-wave excited states $\Xi_c(2790)^0$ and $\Xi_c(2815)^0$ via the radiative decay $\Xi_c^0 \gamma$.

We suggest searching for more possible excited Ω_c states in $\Omega_c^{(*)} \gamma$.

The two $J^P = 3/2^-$ of $\Omega_c(1P)$ states could be expanded by $|j_\ell = 1, 3/2^-\rangle$ and $|j_\ell = 2, 3/2^-\rangle$ with the relation

$$\begin{pmatrix} |\frac{3}{2}^-\rangle_1 \\ |\frac{3}{2}^-\rangle_2 \end{pmatrix} = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} |j_\ell = 1, \frac{3}{2}^-\rangle \\ |j_\ell = 2, \frac{3}{2}^-\rangle \end{pmatrix}.$$

Numerical results:

$$(1) \quad \Omega_{c1}^d(1P, 3/2^-): \quad M_0 = 3062 \text{ MeV}, \quad M_{\text{phy}} = 3029 \text{ MeV}$$

$$(2) \quad \Omega_{c2}^d(1P, 3/2^-): \quad M_0 = 3056 \text{ MeV}, \quad M_{\text{phy}} = 3058 \text{ MeV}$$

4. Summary

1. The mass of $D_{s0}^*(2317)$ could be interpreted by the coupled-channel effect.
2. The mass of $J^P = 1/2^- \Omega_c(1P)$ with predominate $j_\ell = 0$ is obviously affected by the coupled-channel effect.
3. We suggest searching for more possible excited Ω_c states in $\Omega_c^{(*)}\gamma$.

Thank you for attention.