

Jet Charge at CEPC

崔 瀚 化
2021 01 29

上期回顾

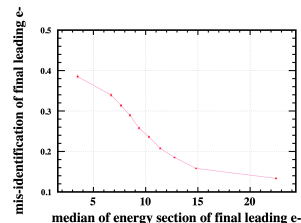
For each event,
Find a Final Leading Particle

Misjudgment rate ω vs energy section

$$\omega_{\text{leading particle}} = \sum (\omega_i * \text{Probability}^{N(\text{statistics})}_i * \text{Probability}^{E(\text{energy})}_i)$$

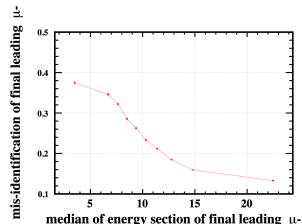
$$\omega_{e^-} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.212$$

All statistics of final leading $e^- = 408068$



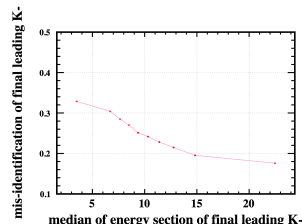
$$\omega_{\mu^-} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.213$$

All statistics of final leading $\mu^- = 408724$



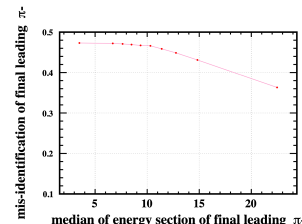
$$\omega_{K^-} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.252$$

All statistics of final leading $K^- = 908428$



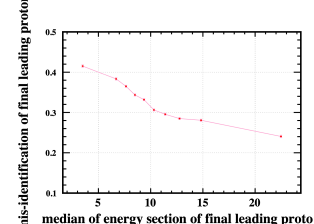
$$\omega_{\pi^-} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.456$$

All statistics of final leading $\pi^- = 2093538$



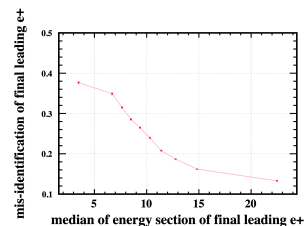
$$\omega_{\text{proton}} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.328$$

All statistics of final leading proton = 286430



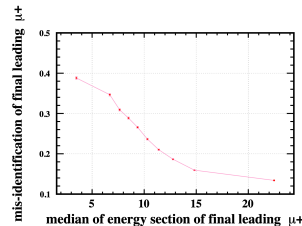
$$\omega_{e^+} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.214$$

All statistics of final leading $e^+ = 407433$



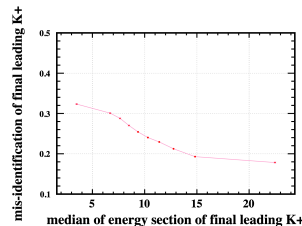
$$\omega_{\mu^+} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.214$$

All statistics of final leading $\mu^+ = 409297$



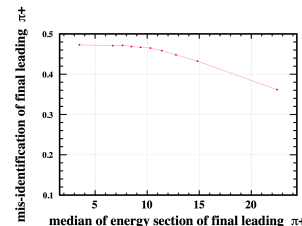
$$\omega_{K^+} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.252$$

All statistics of final leading $K^+ = 90871$



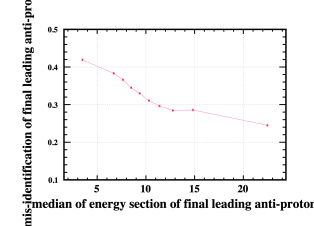
$$\omega_{\pi^+} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.456$$

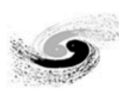
All statistics of final leading $\pi^+ = 2093683$



$$\omega_{\text{antiproton}} = \sum (\omega_i * P_{N_i} * P_{E_i}) = 0.330$$

All statistics of final leading anti-proton = 287031

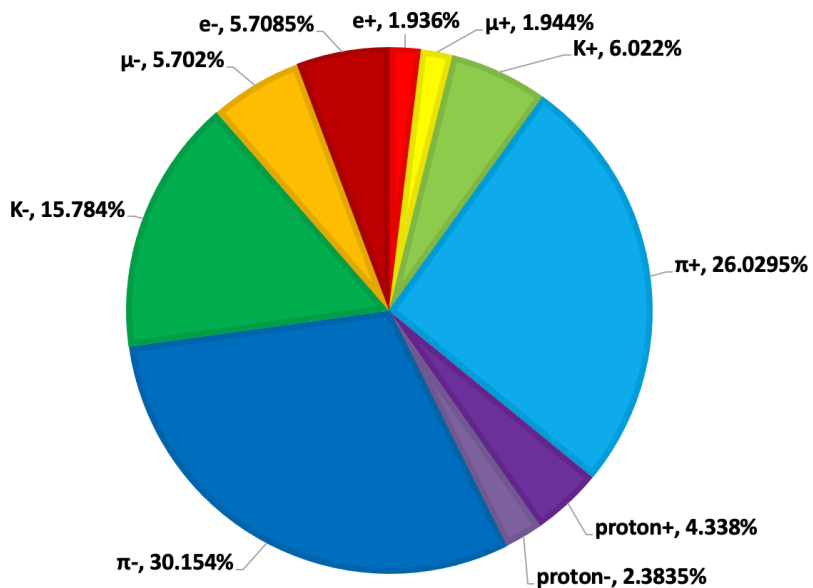




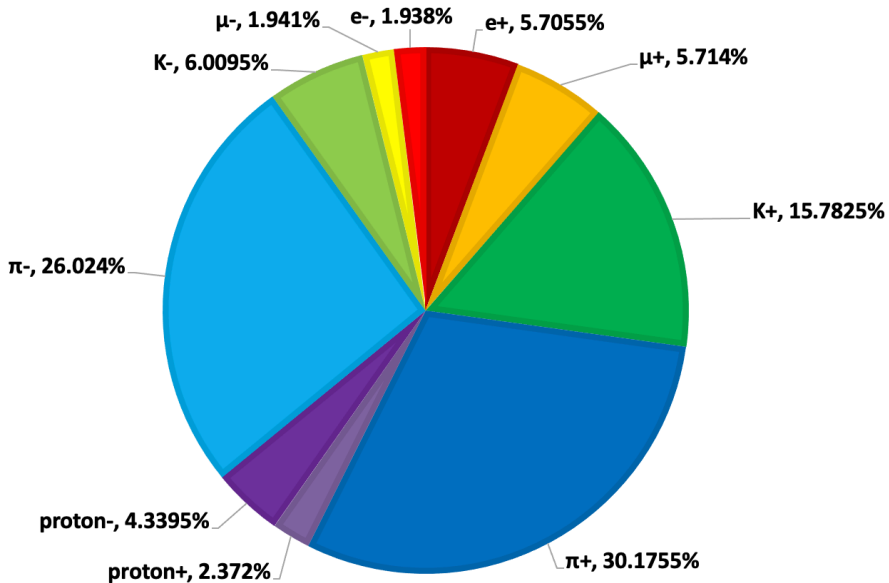
Now,

For each jet,
Find a Final Leading Particle

Percent of final charged leading particles of b jet and bbar jet



b jet



bbar jet

b jet & bbar jet leading particle distribution

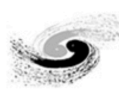
bbar→ b↓	e+	e-	μ+	μ-	K+	K-	π+	π-	p+	p-	total
e+	0.109%	0.037%	0.109%	0.037%	0.304%	0.117%	0.583%	0.507%	0.047%	0.086%	1.936%
e-	0.328%	0.110%	0.327%	0.111%	0.899%	0.341%	1.721%	1.488%	0.1345%	0.249%	5.7085%
μ+	0.1105%	0.037%	0.112%	0.038%	0.307%	0.117%	0.587%	0.506%	0.046%	0.0835%	1.944%
μ-	0.323%	0.110%	0.328%	0.110%	0.900%	0.342%	1.725%	1.480%	0.135%	0.249%	5.702%
K+	0.3435%	0.116%	0.342%	0.119%	0.949%	0.3645%	1.818%	1.564%	0.143%	0.263%	6.022%
K-	0.905%	0.307%	0.901%	0.307%	2.488%	0.944%	4.768%	4.112%	0.373%	0.679%	15.784%
π+	1.483%	0.506%	1.492%	0.503%	4.1045%	1.567%	7.861%	6.768%	0.617%	1.128%	26.0295%
π-	1.7205%	0.584%	1.721%	0.583%	4.775%	1.811%	9.090%	7.853%	0.7145%	1.302%	30.154%
p+	0.248%	0.084%	0.246%	0.086%	0.683%	0.261%	1.306%	1.125%	0.104%	0.195%	4.338%
p-	0.135%	0.047%	0.136%	0.047%	0.373%	0.145%	0.7165%	0.621%	0.058%	0.105%	2.3835%
total	5.7055%	1.938%	5.714%	1.941%	15.7825%	6.0095%	30.1755%	26.024%	2.372%	4.3395%	100.00%

b jet & bbar jet leading particle distribution

等待做成colorful的图。。。。

b jet & bbar jet leading particle distribution 先分四种情况研究

bbar jet→ b jet↓	$e\mu K$	$\pi\rho$
$e\mu K$	case 1	case 2
$\pi\rho$	case 3	case 4



~~1~~

For
b jet is $\{e, \mu, K\}$
bbar jet is $\{e, \mu, K\}$

For {b jet = e, μ , K}{bbar jet = e, μ , K}, no energy cut

$$N_{\text{all}} = 16396350$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\}} = 2254715$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_verse}\}}} = 1374412$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_nn}\}}} = 439801$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_np}\}}} = 1213180 = N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_verse}\}\{\text{charge_correct}\}}$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_pn}\}}} = 161232$$

$$N_{\text{b jet = e, } \mu, \text{ K}\{\text{bbar jet = e, } \mu, \text{ K}\{\text{charge_pp}\}}} = 440502$$

For {b jet = e, μ , K}{bbar jet = e, μ , K}, no energy cut

$$\text{Percent of } \{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\} = \frac{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\}}}{N_{\{\text{all}\}}} = \frac{2254715}{16396350} = 0.1375$$

$$\text{Percent of } \{\text{charge_verse}\} = \frac{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\} \{\text{charge_verse}\}}}{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\}}} = \frac{1374412}{2254715} = 0.6096$$

$$\text{Percent of } \{\text{charge_correct}\} = \frac{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\} \{\text{charge_verse}\} \{\text{charge_correct}\}}}{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\} \{\text{charge_verse}\}}} = \frac{1213180}{1374412} = 0.8827$$

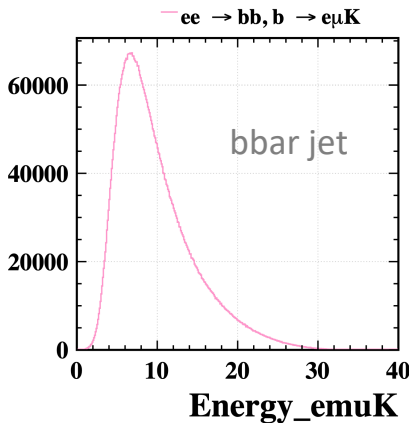
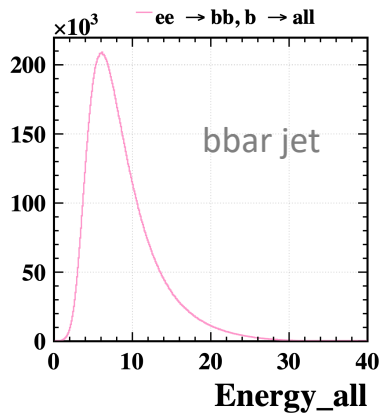
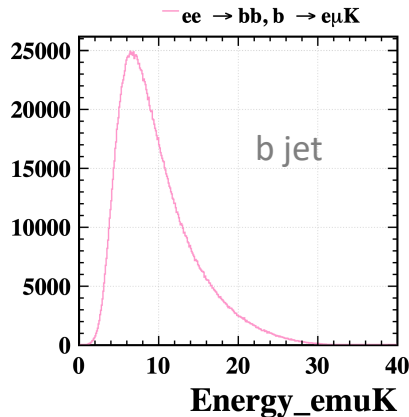
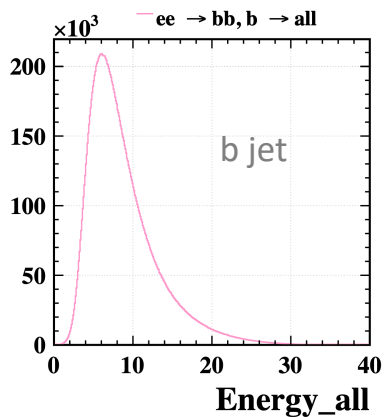
$$\text{Efficiency} = \frac{N_{\{b \text{ jet} = e, \mu, K\} \{b\text{bar jet} = e, \mu, K\} \{\text{charge_verse}\} \{\text{charge_correct}\}}}{N_{\{\text{all}\}}} = \frac{1213180}{16396350} = 0.07399$$

$$\omega = 1 - \text{Percent of } \{\text{charge_correct}\} = 0.1173$$

$$(1 - 2 * \omega)^2 = 0.5858$$

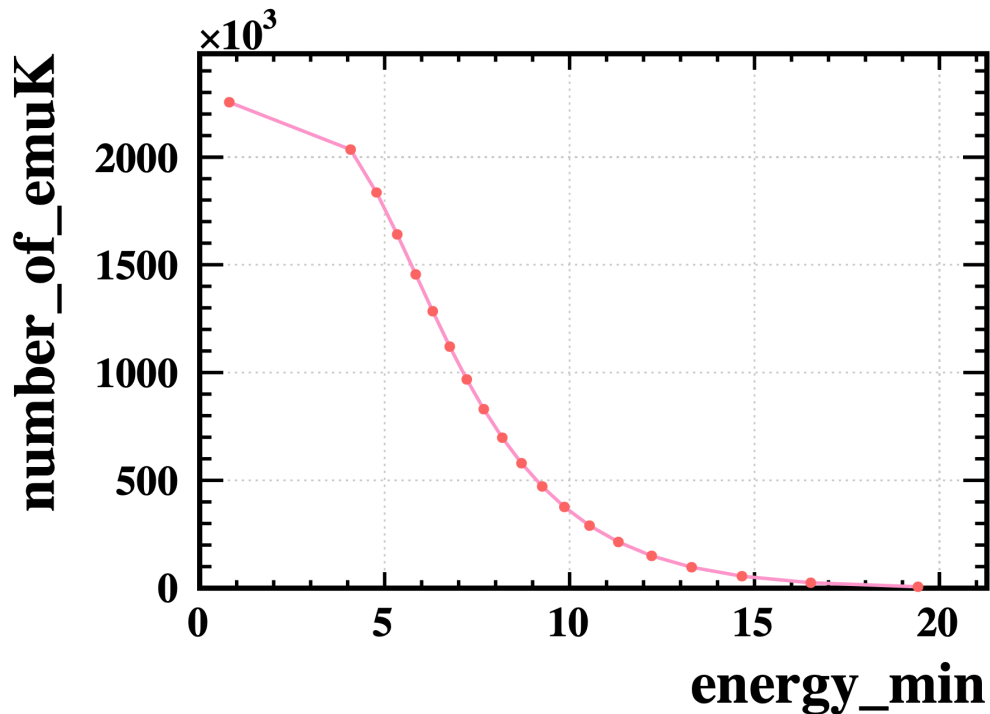
$$\text{Effective tagging power} = \text{Efficiency} * (1 - 2 * \omega)^2 = 0.04334$$

Energy spectrum of {b jet = e, μ, K}{bbar jet = e, μ, K}



$$\begin{aligned} & \text{Percent of } \{b \text{ jet} = e, \mu, K\} \{b\bar{b} \text{ jet} = e, \mu, K\} \\ &= \frac{N_{\{b \text{ jet} = e, \mu, K\}} \{b\bar{b} \text{ jet} = e, \mu, K\}}{N_{\{\text{all}\}}} = \frac{2254715}{16396350} = 0.1375 \end{aligned}$$

解决一个疑惑：Number of {b jet = e, μ , K}{bbar jet = e, μ , K}



说明左图的点纵轴的差值不应该等值:

设总事例数为 N , 每个 bin 内事例数为 n_i .

设第 i 次对两边 jet LP 做 energy cut, 还剩事例数为 n_i .

$\left\{ \begin{array}{l} \text{每一边还剩下的事例数占比为 } \frac{n_i}{N} \\ \text{两边还剩下的事例数占比为 } \left(\frac{n_i}{N}\right)^2 \end{array} \right.$

那么,

第 $(i+1)$ 次对两边 jet LP 做 energy cut,

比上次少了 $\left(\frac{n_i}{N}\right)^2 - \left(\frac{n_{i+1}}{N}\right)^2$

$$= \left(\frac{n_i}{N}\right)^2 - \left(\frac{n_i - n_0}{N}\right)^2$$

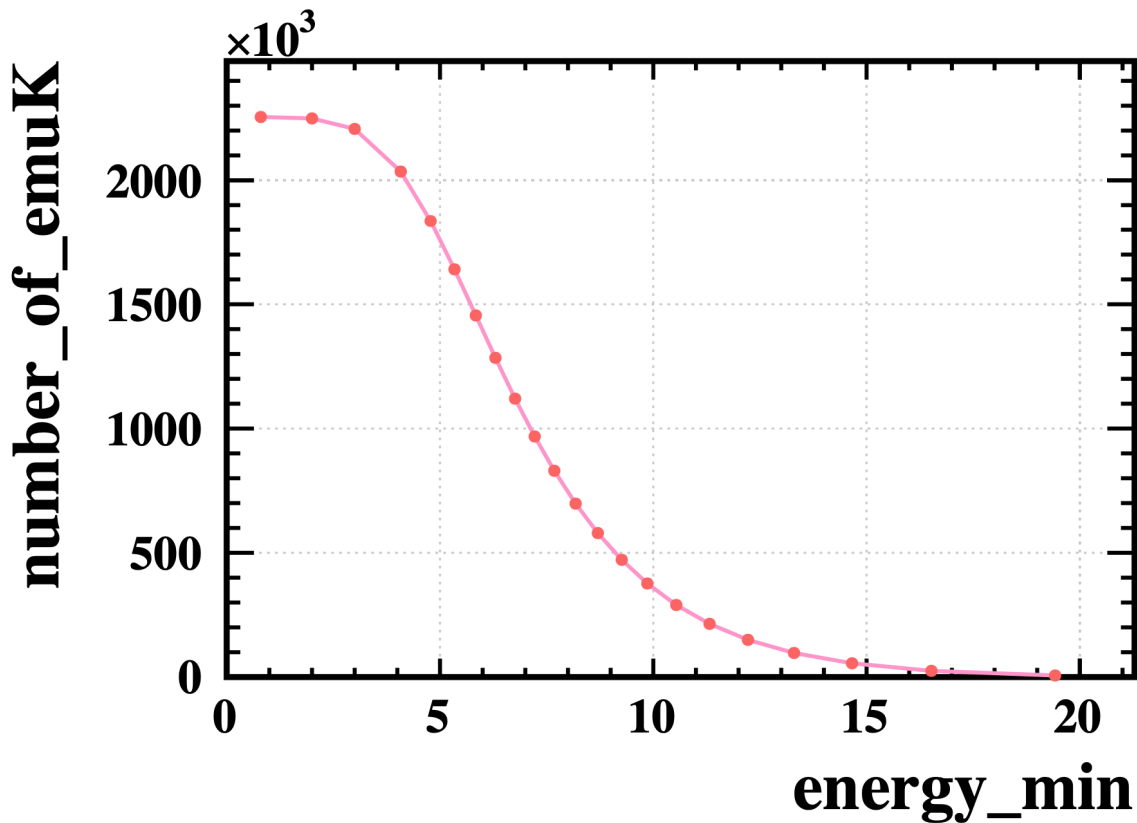
$$= \frac{2n_0}{N^2} \cdot n_i - \frac{n_0^2}{N^2}$$

是 n_i 的一次函数.

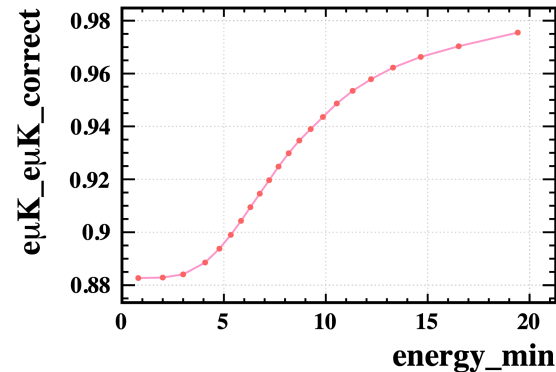
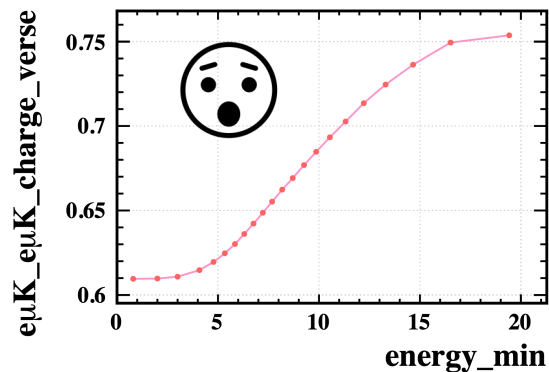
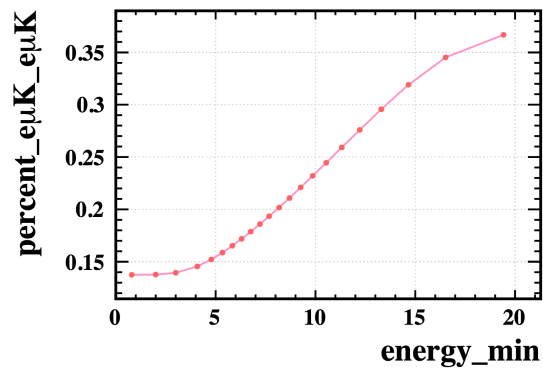
n_i 逐渐减小.

因此左图每两点的纵坐标差值逐渐减小.

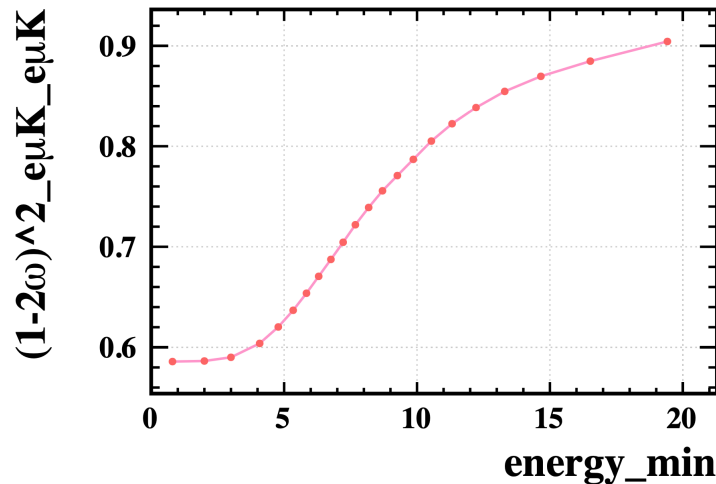
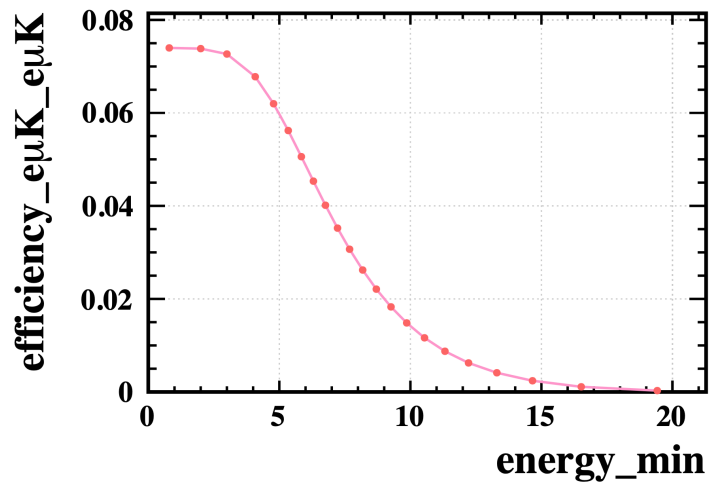
前面加上两个点之后。。 Number of {b jet = e, μ , K}{bbar jet = e, μ , K}



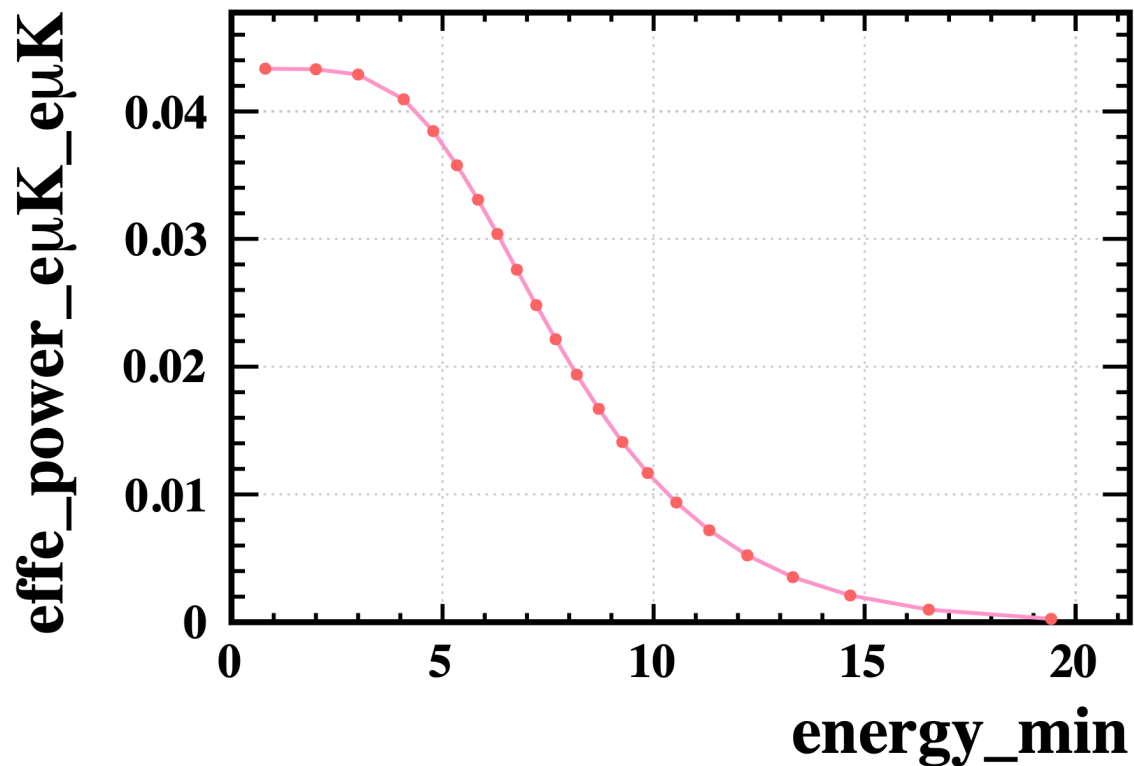
Steps for Efficiency of {b jet = e, μ , K}{bbar jet = e, μ , K}

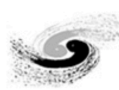


Efficiency & $(1-2\omega)^2$ of {b jet = e, μ , K} {bbar jet = e, μ , K}



Effective tagging power of {b jet = e, μ , K}{bbar jet = e, μ , K}





2

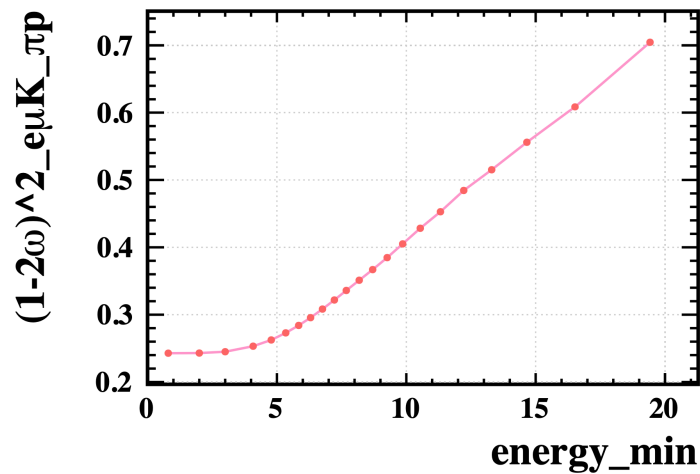
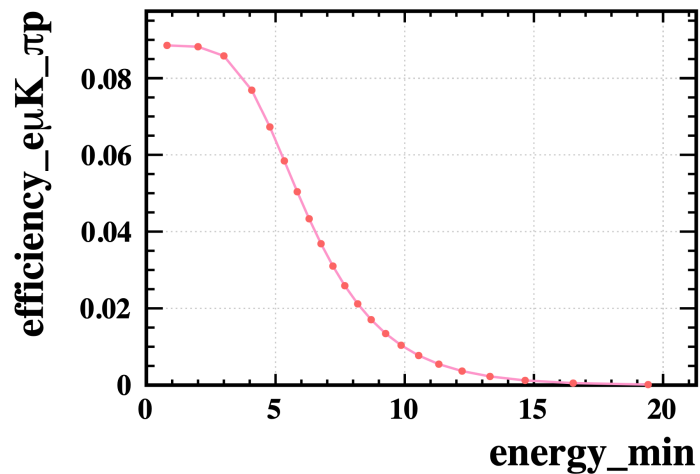
For
b jet is {e, μ , K}
bbar jet is { π , proton}

For $\{\pi, \text{proton}\}$

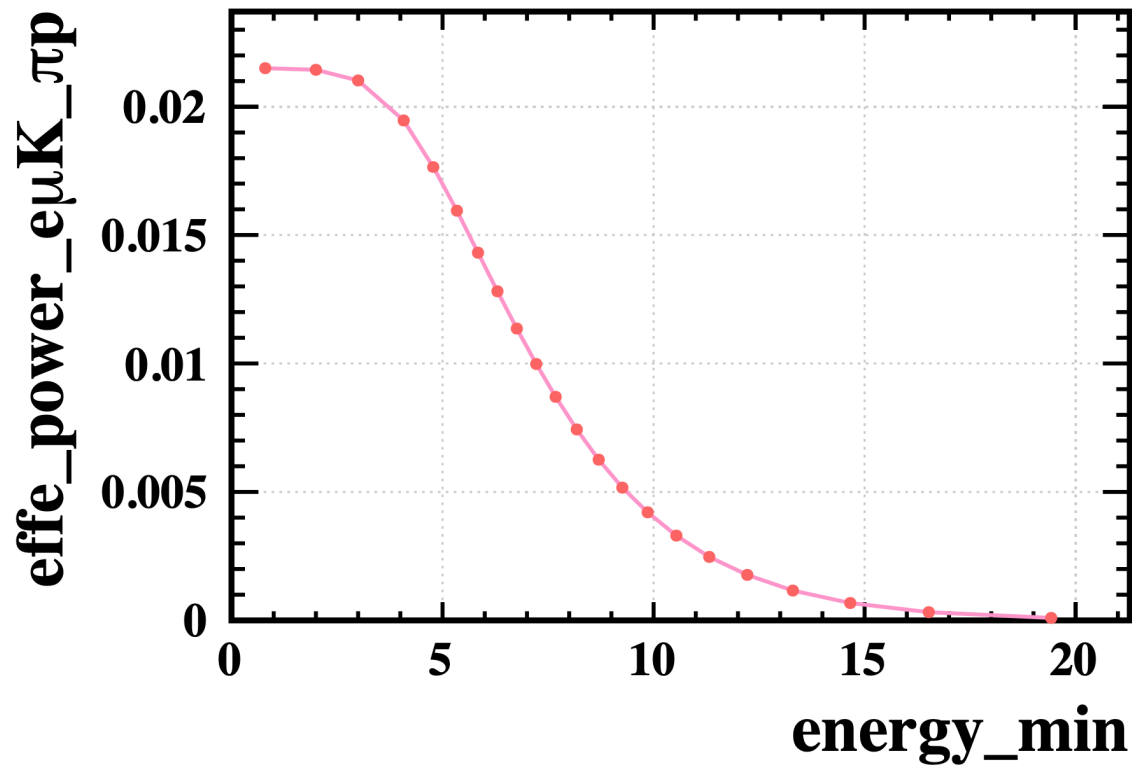
I need to check the **proton**...

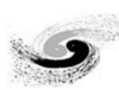
But even so, let's move on...

Efficiency & $(1-2\omega)^2$ of {b jet = e, μ , K}{bbar jet = π , proton}



Effective tagging power of {b jet = e, μ , K}{bbar jet = π , proton}

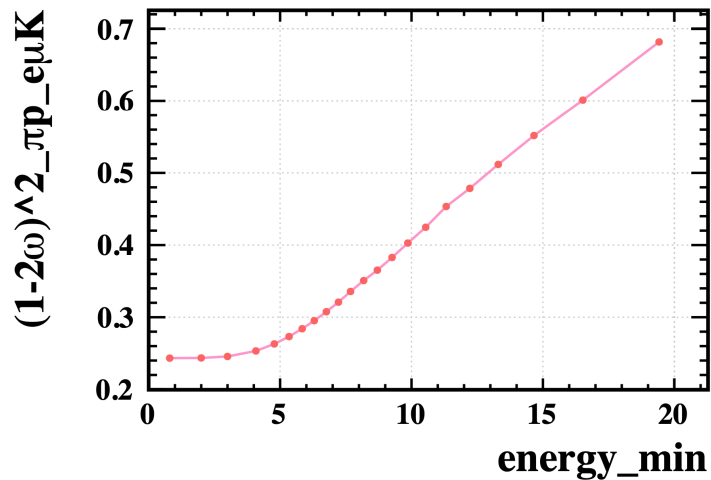
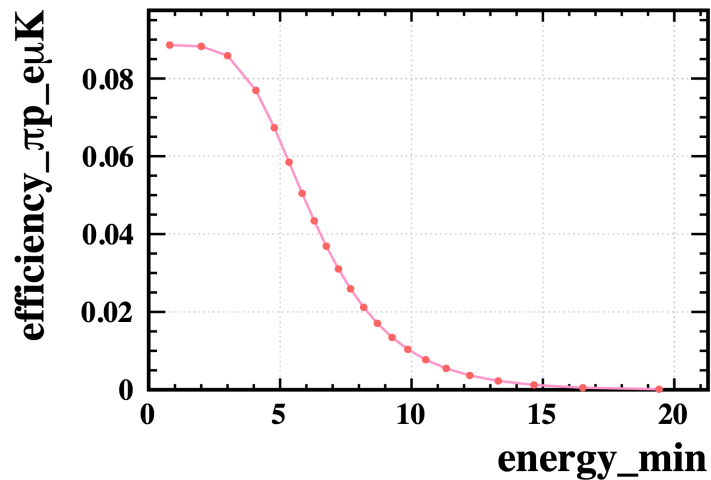




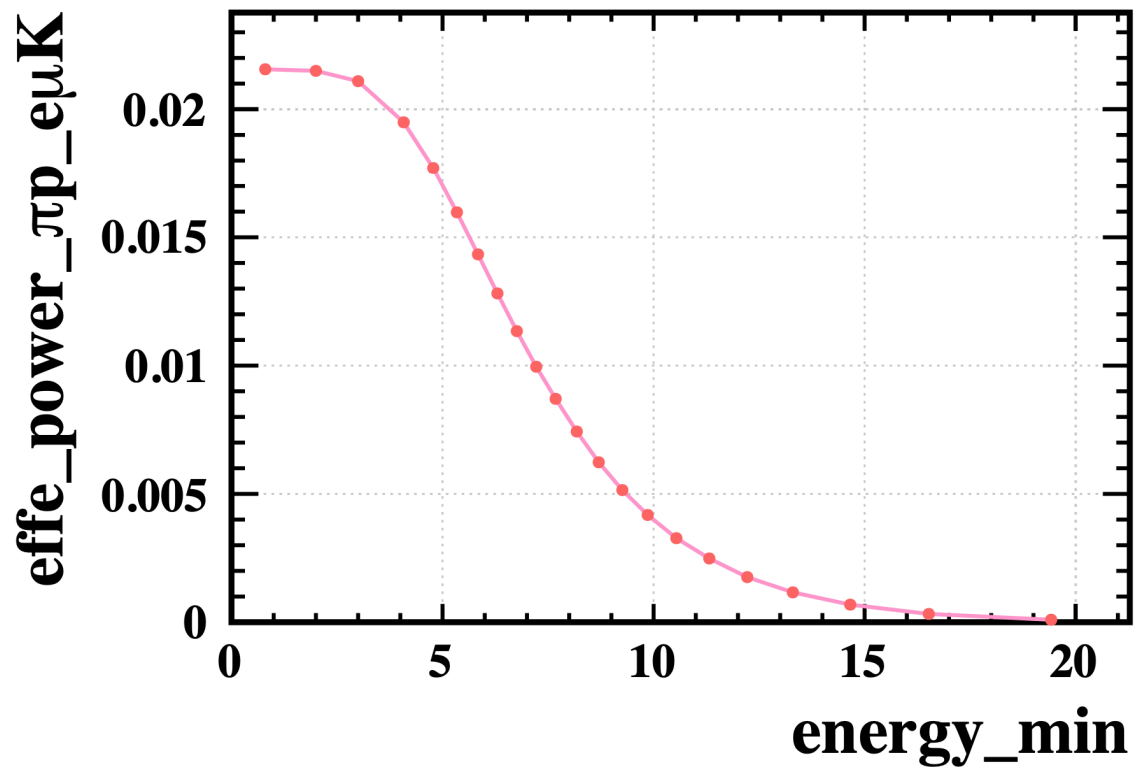
~~3~~

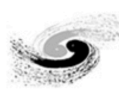
For
b jet is $\{\pi, \text{proton}\}$
bbar jet is $\{e, \mu, K\}$

Efficiency & $(1-2*\omega)^2$ of {b jet = π , proton}{bbar jet = e, μ , K}



Effective tagging power of {b jet = π , proton}{bbar jet = e, μ , K}

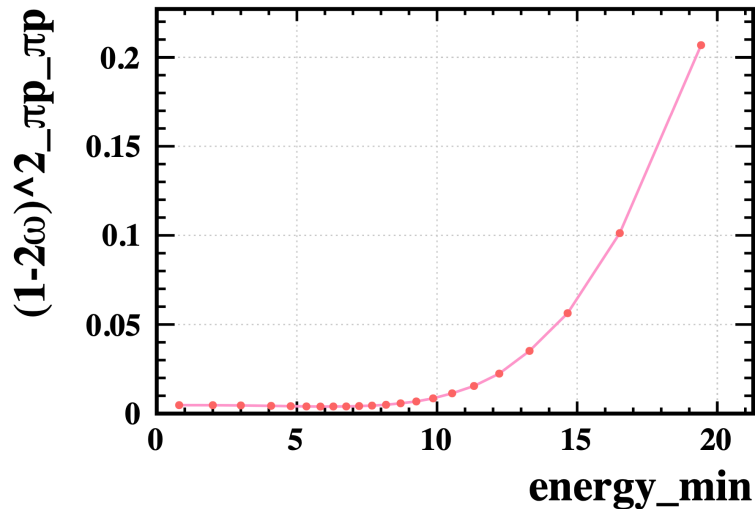
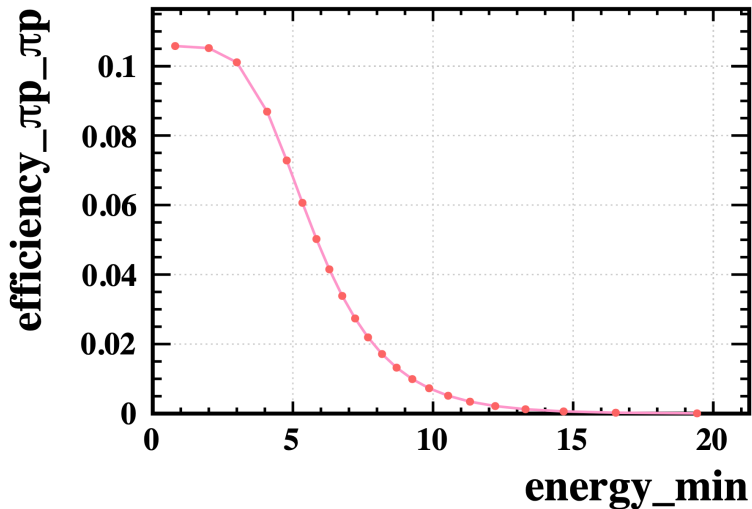




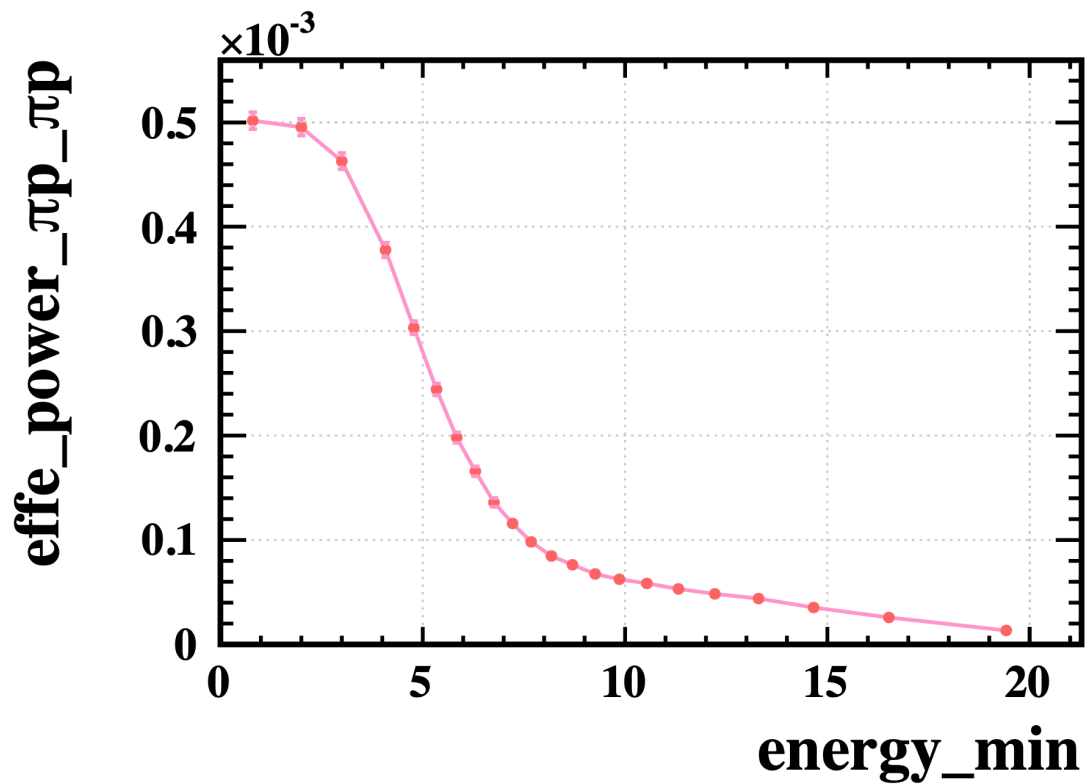
4

For
b jet is $\{\pi, \text{proton}\}$
bbar jet is $\{\pi, \text{proton}\}$

Efficiency & $(1-2\omega)^2$ of {b jet = π , proton}{bbar jet = π , proton}



Effective tagging power of {b jet = π ,proton}{bbar jet = π ,proton}



未完待续。。

Efficiency & omega之间隐含的关联关系，是啥？

为什么effective tagging power总是单调的？

Questions above ...

Same charge of two jets' leading particle

...