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π^0 reconstruction and physics measurement of $B^0/B_s \rightarrow \pi^0\pi^0$ at CEPC

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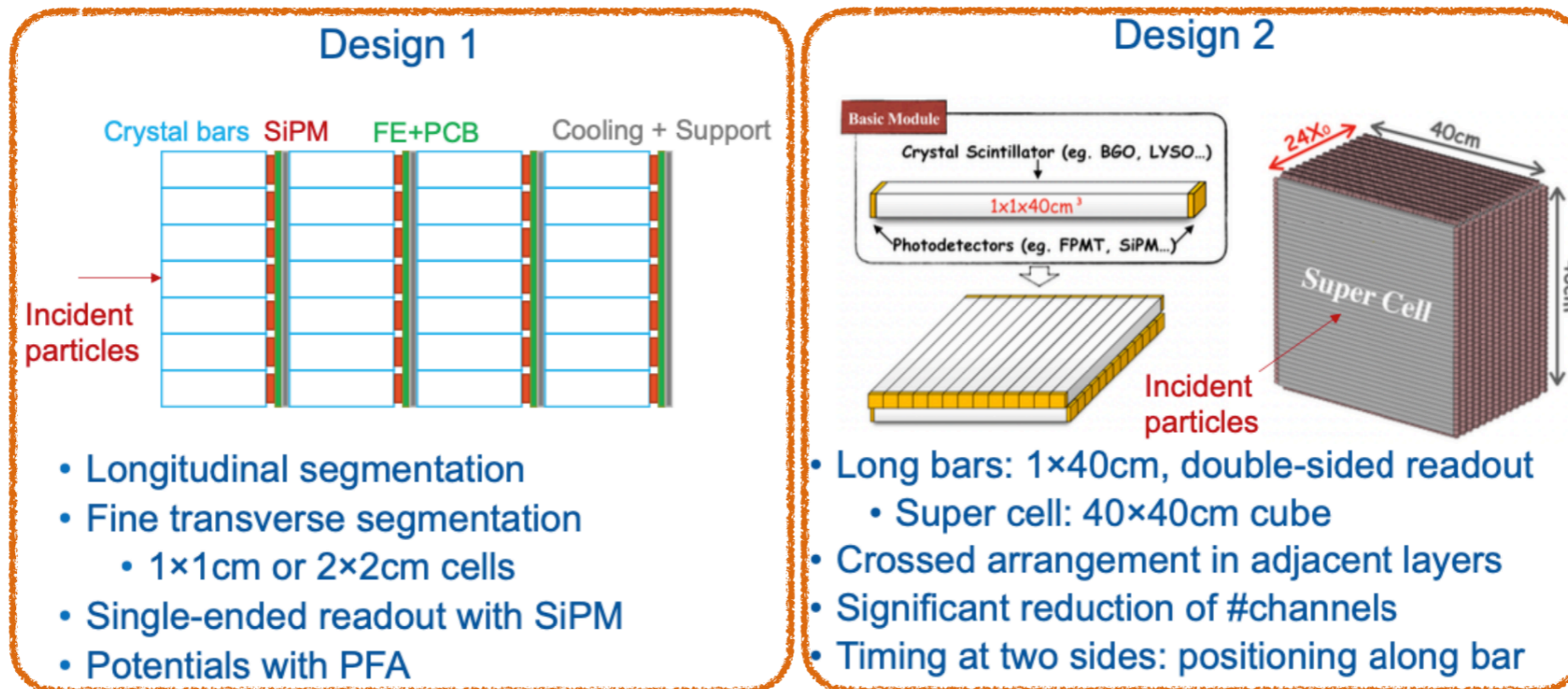
CEPC Workshop at Yangzhou, April 15, 2021

Outline

- 1. Motivation and introduction**
- 2. Reconstruction of π^0**
- 3. Separation of B^0 and B_s**
- 4. Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$**
- 5. Mixed measurement of $B^0&B_s \rightarrow \pi^0\pi^0$**
- 6. Summary**

Motivation

Physics requirements for the 4th Conceptual Detector with the Crystal ECAL Design



Homogeneous Crystal ECAL

Baseline sampling ECAL (in CEPC CDR)

EM resolution: $3\% / \sqrt{E} \oplus 1\%$

VS

$17\% / \sqrt{E} \oplus 1\%$

- $\pi^0 \rightarrow \gamma\gamma$, EM object, depends on ECAL performance
- **How much can we benefit from this EM resolution improvement in physics measurement?**

Brief introduction of B^0 & $B_s \rightarrow \pi^0\pi^0$

$B^0 \rightarrow \pi^0\pi^0$

$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ in PDG 2018					Γ_{388}/Γ	
VALUE (units 10^{-6})	CL%	DOCUMENT ID	TECN	COMMENT		
1.59 ± 0.26	OUR AVERAGE	Error includes scale factor of 1.4.				
$1.31 \pm 0.19 \pm 0.19$		¹ JULIUS	17	BELL	$e^+e^- \rightarrow \Upsilon(4S)$	
$1.83 \pm 0.21 \pm 0.13$		¹ LEES	13D	BABR	$e^+e^- \rightarrow \Upsilon(4S)$	

(2017) <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.96.032007>

$B_s \rightarrow \pi^0\pi^0$

Experimental upper limit

$\Gamma(\pi^0\pi^0)/\Gamma_{\text{total}}$ in PDG 2018					Γ_{87}/Γ	
VALUE	CL%	DOCUMENT ID	TECN	COMMENT		
$<2.1 \times 10^{-4}$	90	¹ ACCIARRI	95H	L3	$e^+e^- \rightarrow Z$	
¹ ACCIARRI 95H assumes $f_{B^0} = 39.5 \pm 4.0$ and $f_{B_s} = 12.0 \pm 3.0\%$.						

(1995) <https://www.sciencedirect.com/science/article/pii/0370269395010420>

Theoretical estimation

$\bar{B}_s^0 \rightarrow \pi^+\pi^-$	ann	$0.024^{+0.003+0.025+0.000+0.163}_{-0.003-0.012-0.000-0.021}$...	$0.57^{+0.16+0.09+0.01}_{-0.13-0.10-0.00}$	<1.36
$\bar{B}_s^0 \rightarrow \pi^0\pi^0$	ann	$0.012^{+0.001+0.013+0.000+0.082}_{-0.001-0.006-0.000-0.011}$...	$0.28^{+0.08+0.04+0.01}_{-0.07-0.05-0.00}$	<210

(2007) <https://journals.aps.org/prd/abstract/10.1103/PhysRevD.76.074018>

$\sim 3 \times 10^{-7}$

Reconstruction of π^0

Decay channel: $\pi^0 \rightarrow \gamma\gamma$ (BR~98.8%)

Pair up photons and select π^0 candidates according to the invariant mass

Preliminary Fast Simulation modeling:

Currently focus on the energy response

- *Smear E_γ with EM resolution*
- *Simply 10MeV E_γ threshold*

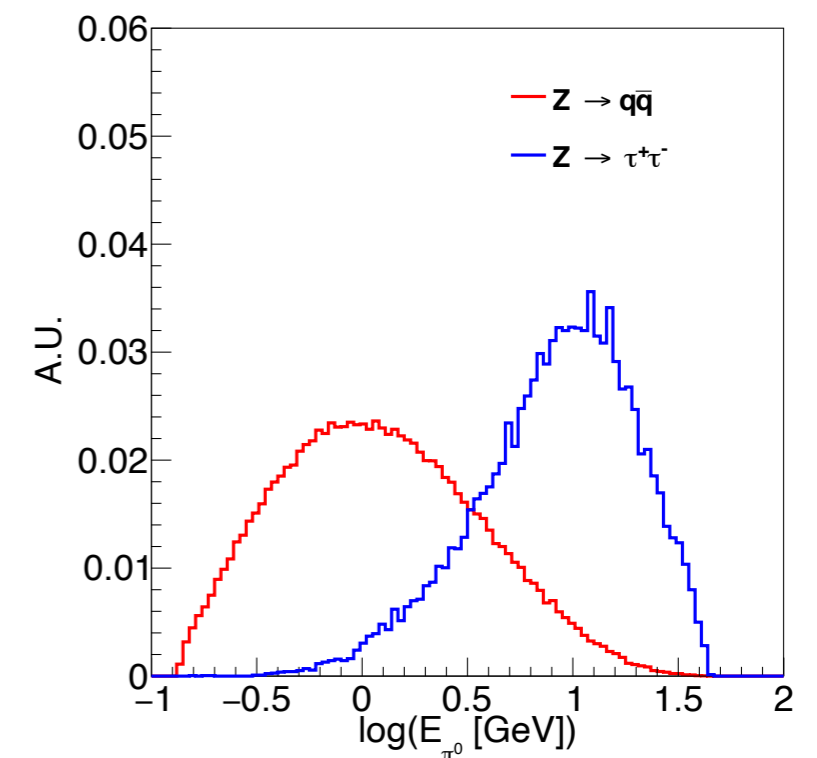
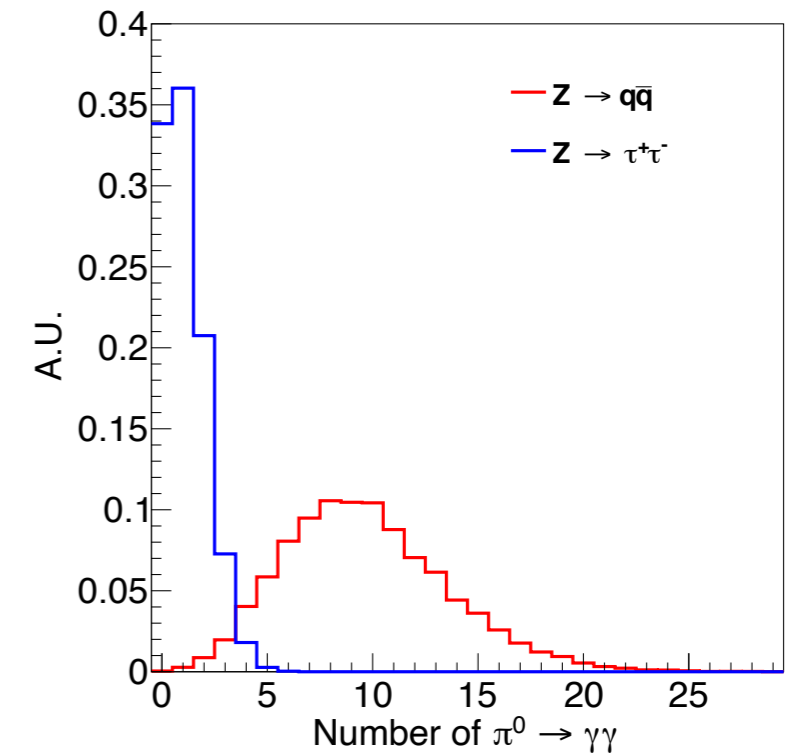
Some effects not included yet...

- *Photon angular resolution (~ 0.5 mrad, ~ 1 cm)*
- *Di-photon separation ($\pi^0 < 30$ GeV, > 9 mrad, > 1.6 cm)*
- *Detector acceptance ($|\cos\theta| < 0.99$)*

Values in parentheses are results of baseline detector as a reference

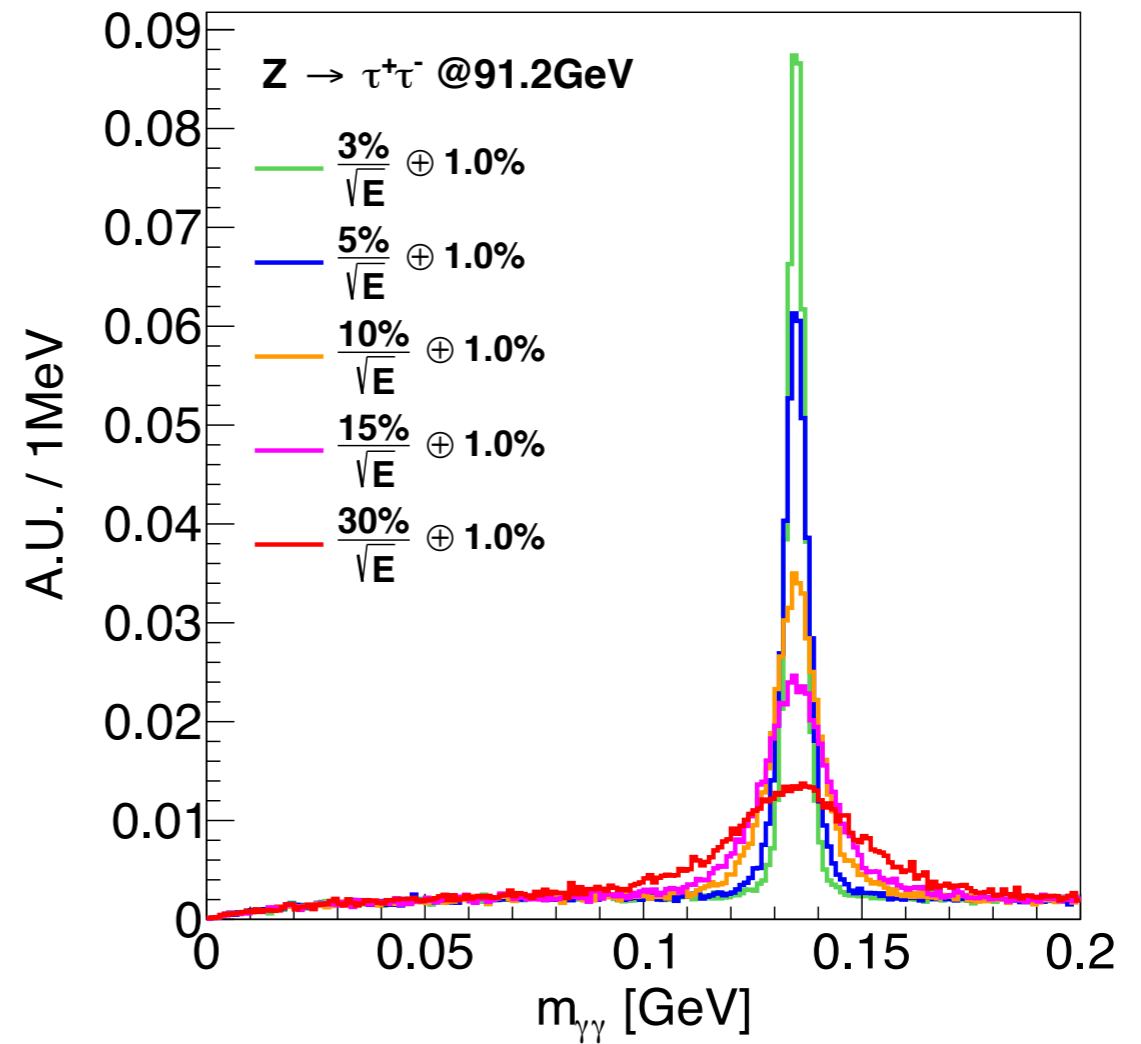
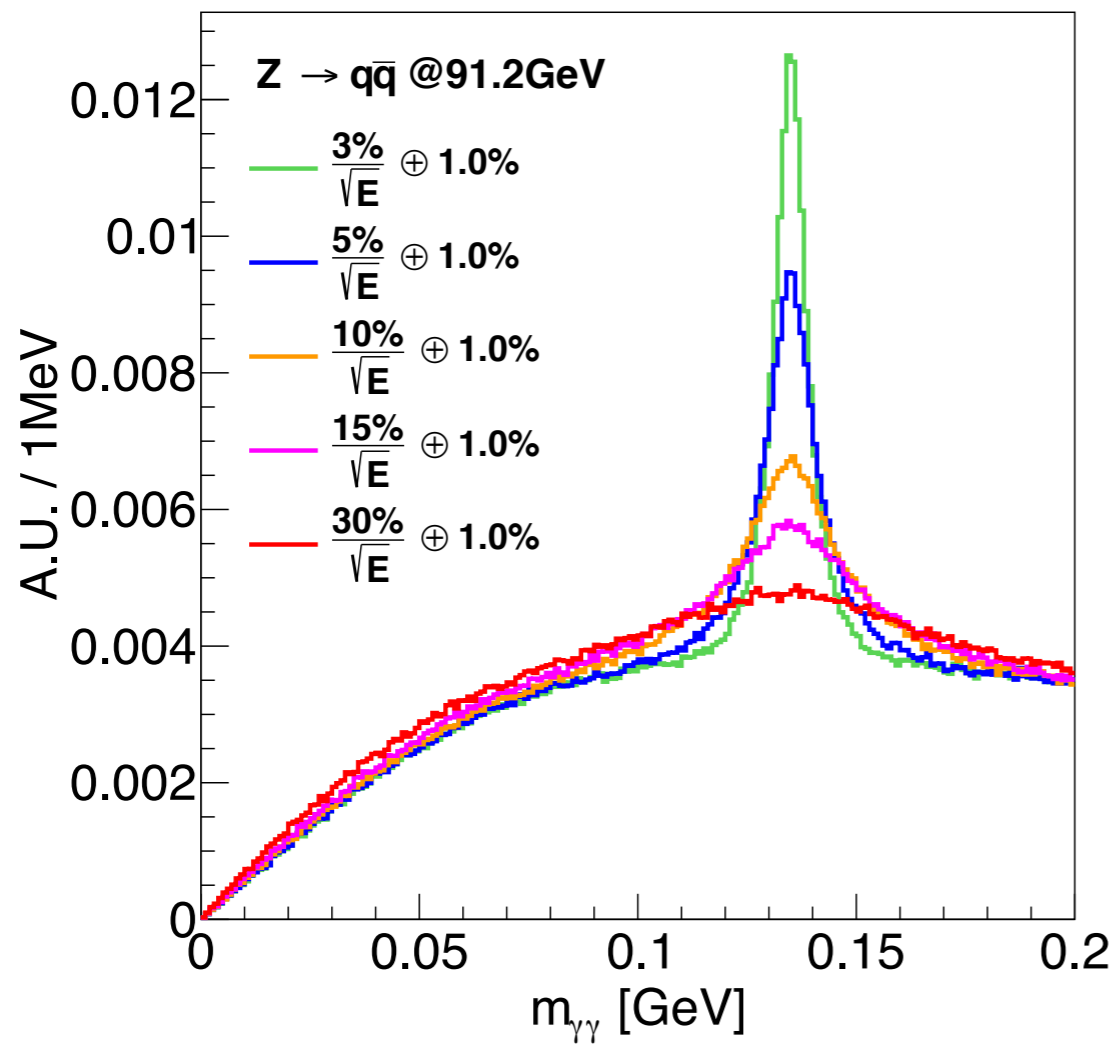
Two samples at Z pole operation (91.2GeV):

$Z \rightarrow qq$ & $Z \rightarrow \tau\tau$ (with different topologies)



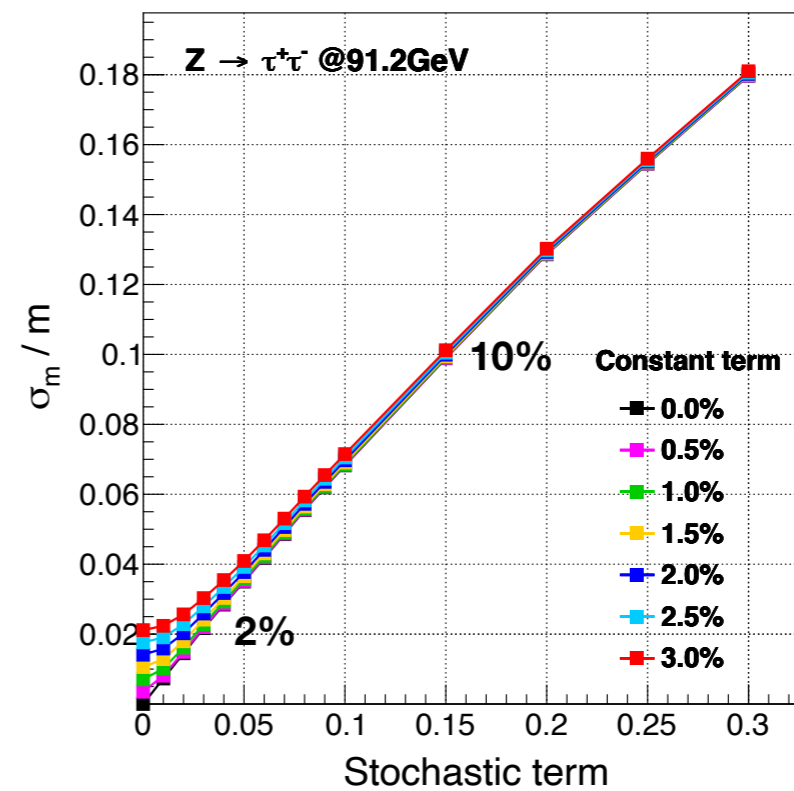
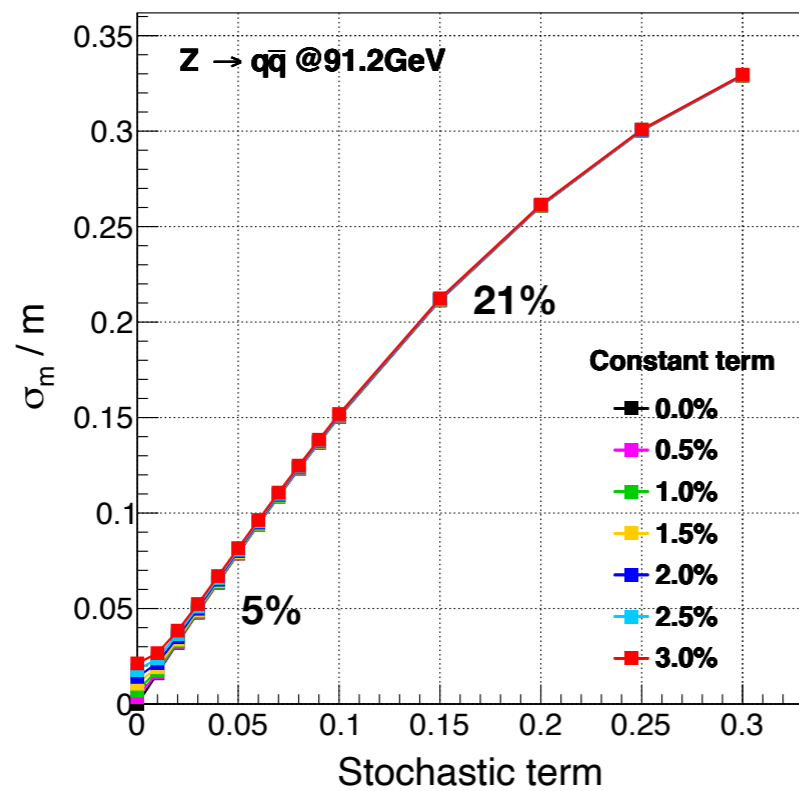
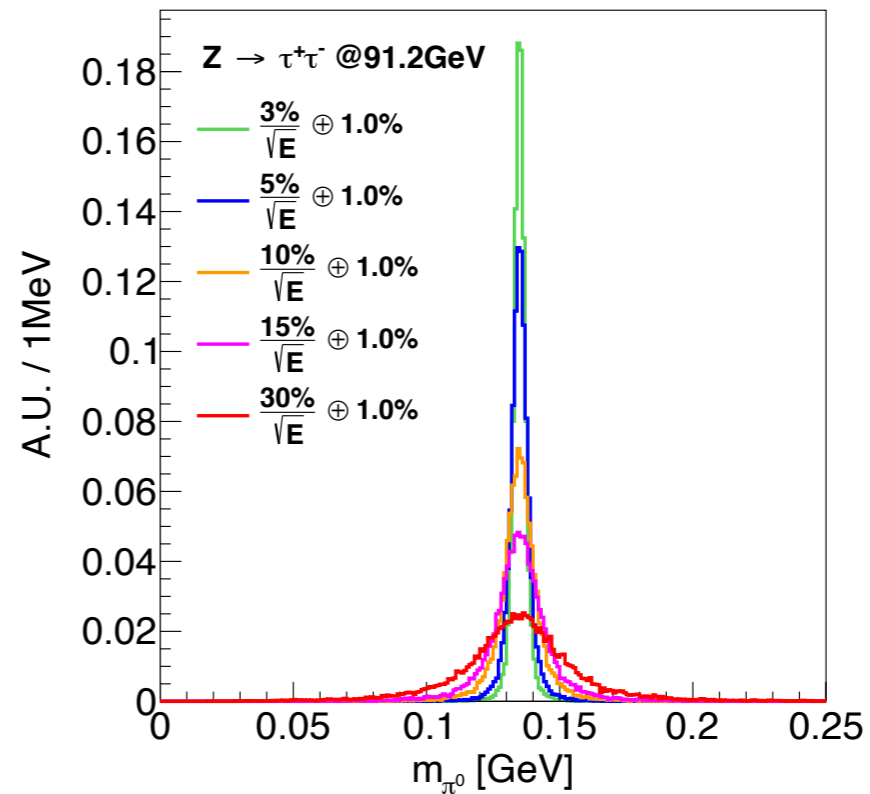
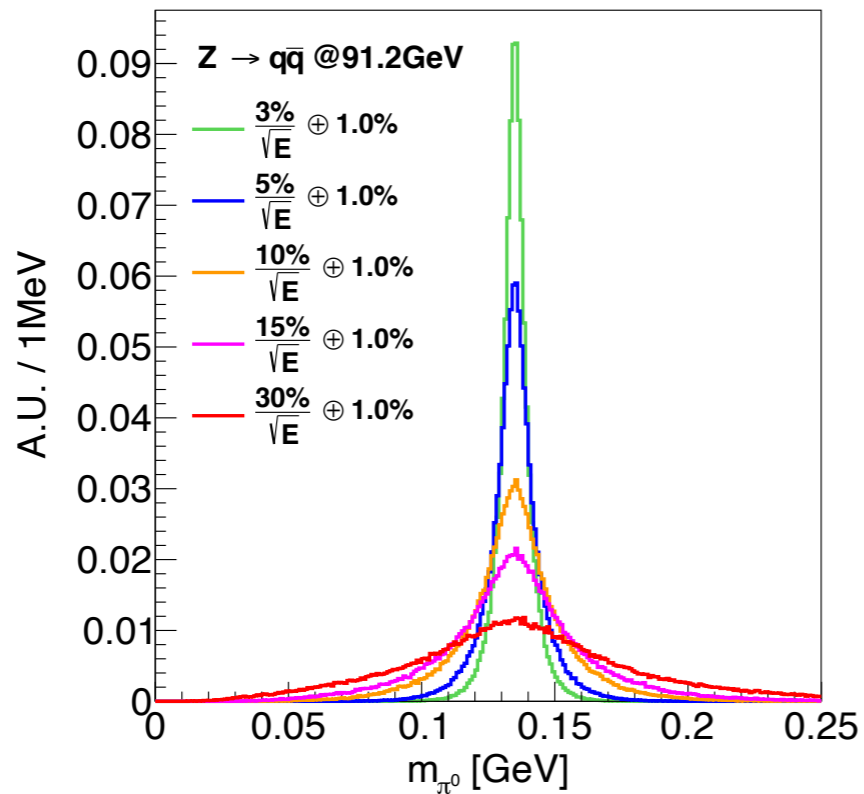
Reconstruction of π^0

Distribution of $m_{\gamma\gamma}$



Reconstruction of π^0

π^0 mass resolution

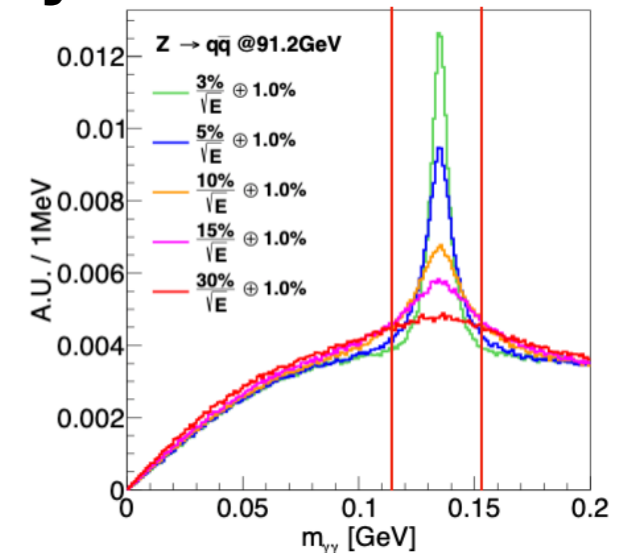


Reconstruction of π^0

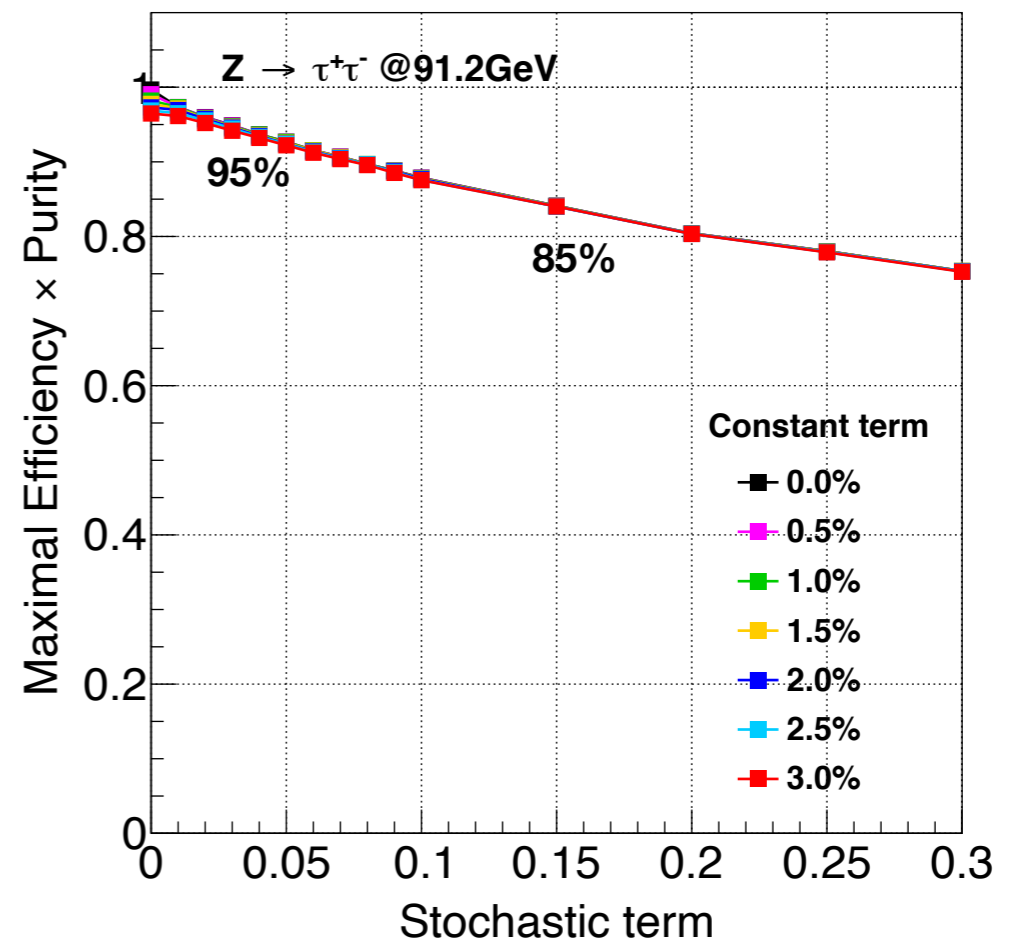
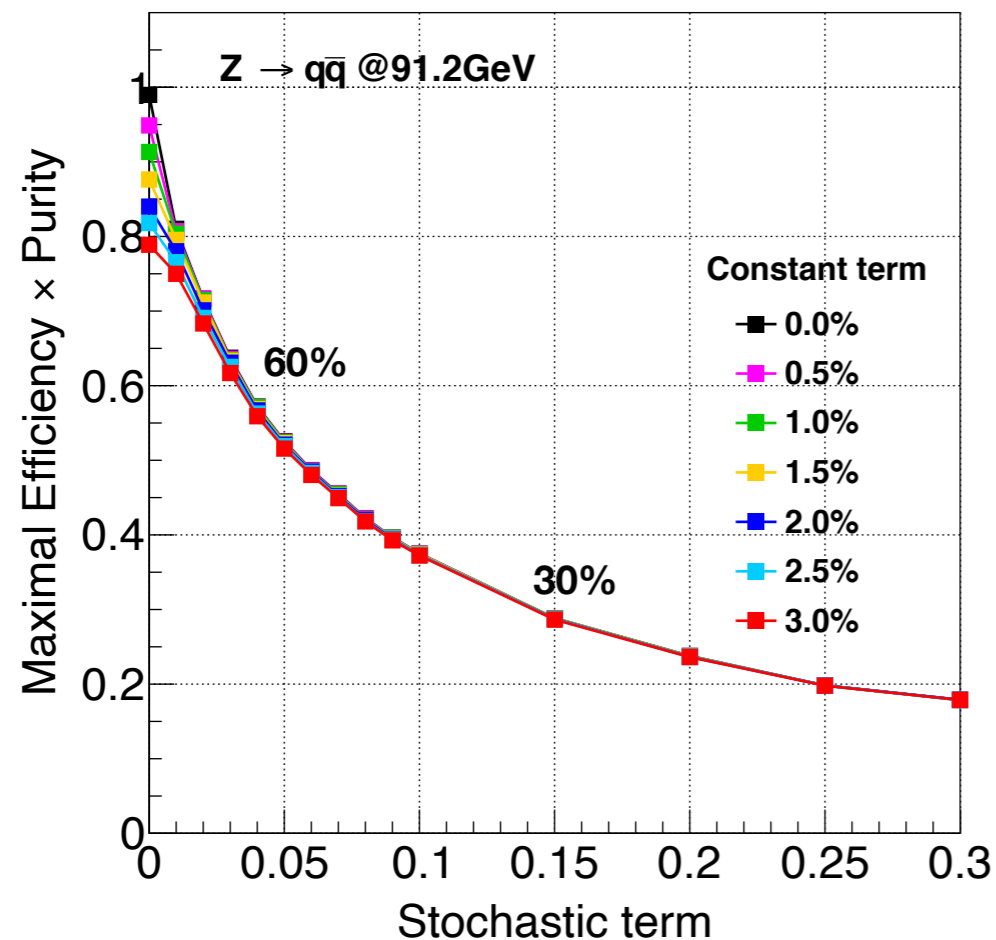
π^0 identification efficiency & purity

$$\epsilon = \frac{\text{Number of selected } \pi^0 \text{ s that are true } \pi^0 \text{ s in Monte Carlo}}{\text{Number of all generated } \pi^0 \text{ s}}$$

$$p = \frac{\text{Number of selected } \pi^0 \text{ s that are true } \pi^0 \text{ s in Monte Carlo}}{\text{Number of all selected } \pi^0 \text{ s}}$$



Simply **energy sorted strategy** to pair each photon at most once
 Optimize the **mass window** to get **maximal efficiency × purity**

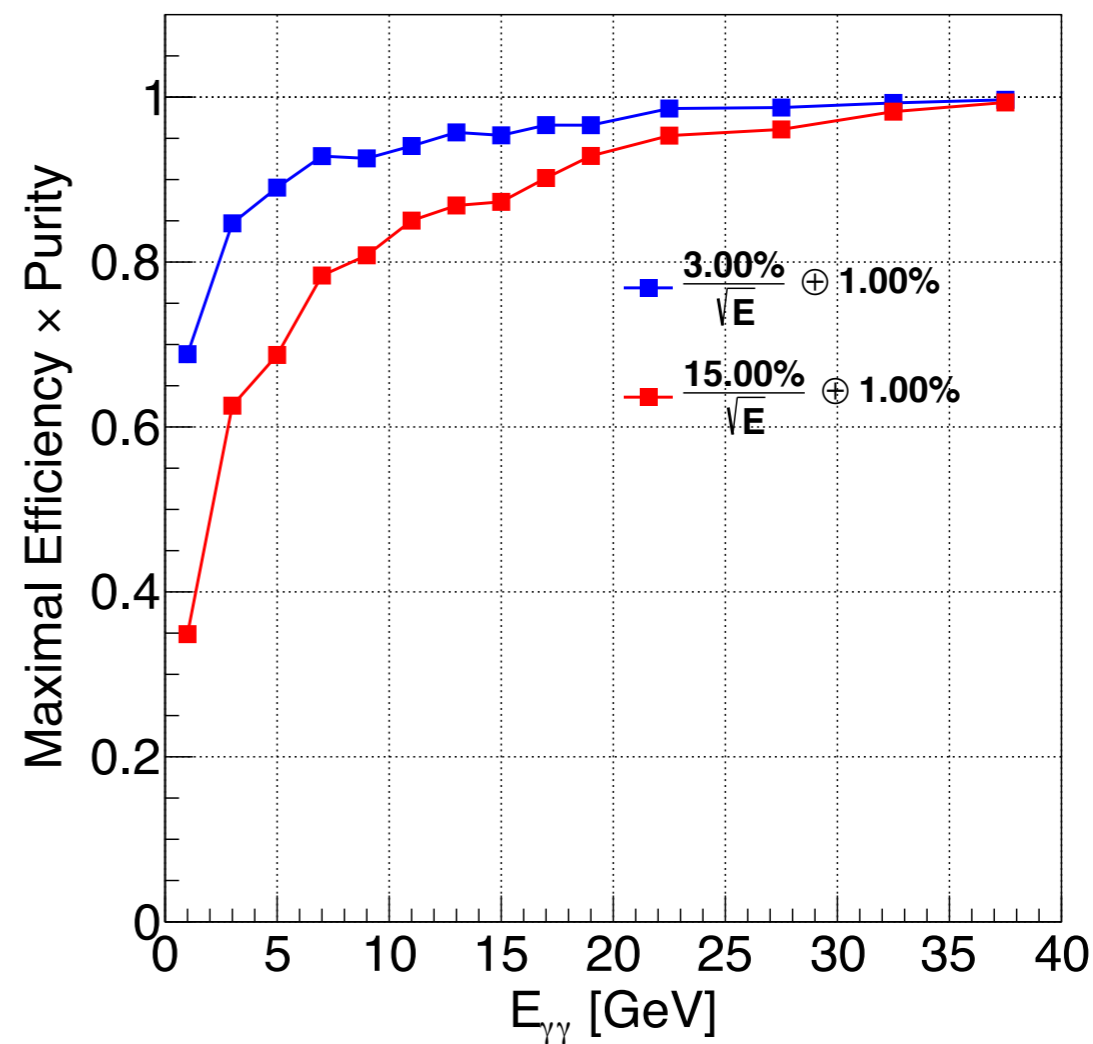
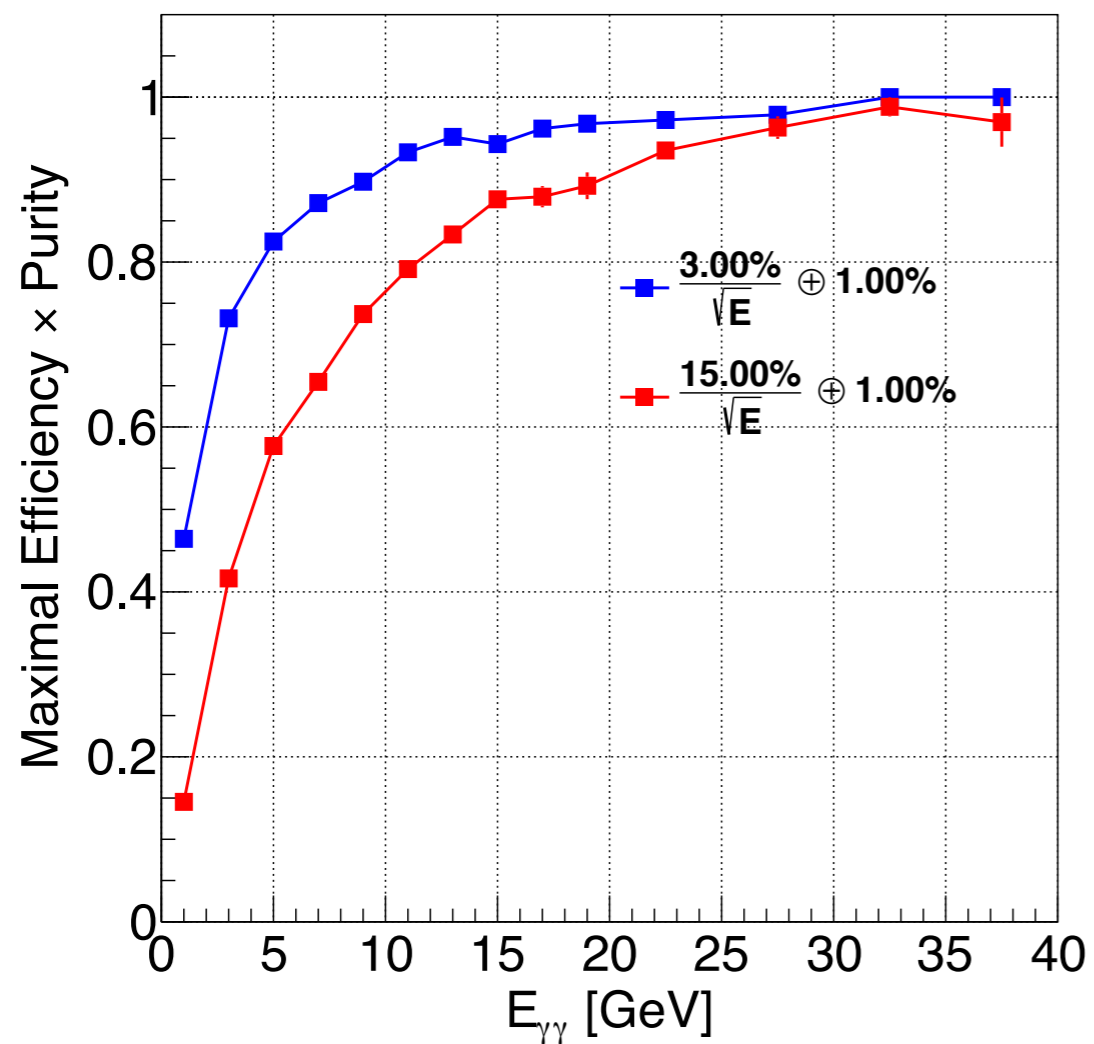


Reconstruction of π^0

Energy differential results

$Z \rightarrow qq$

$Z \rightarrow \tau\tau$

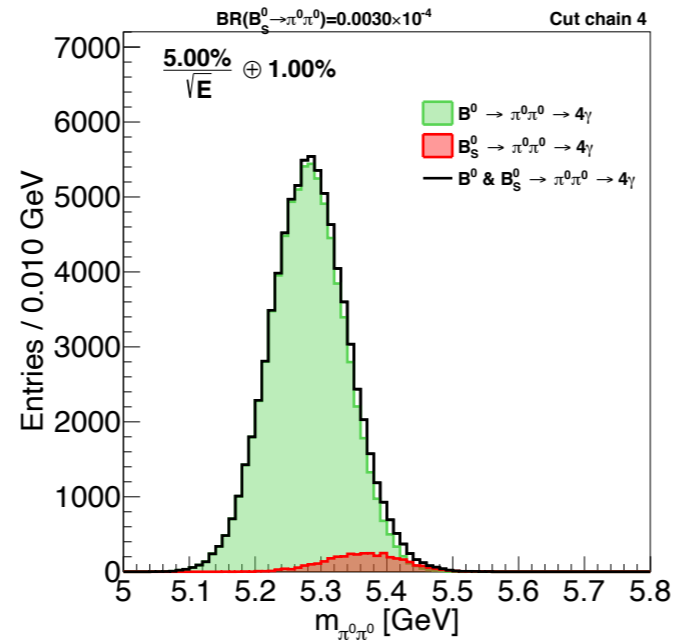
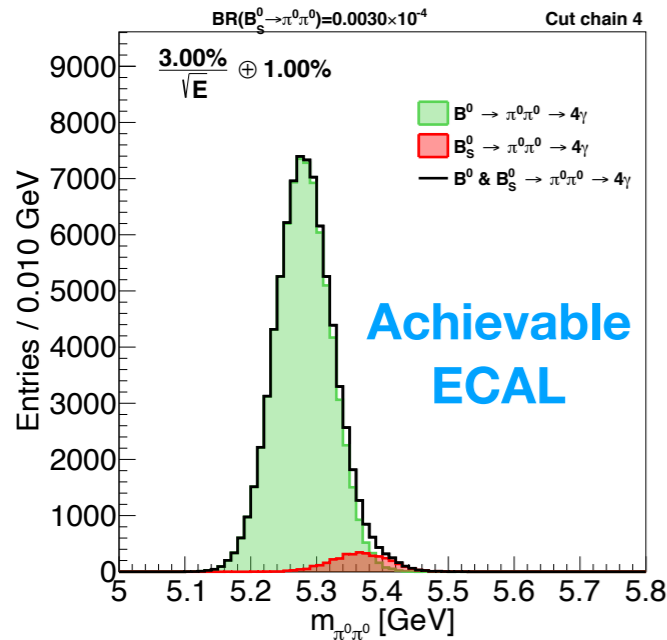
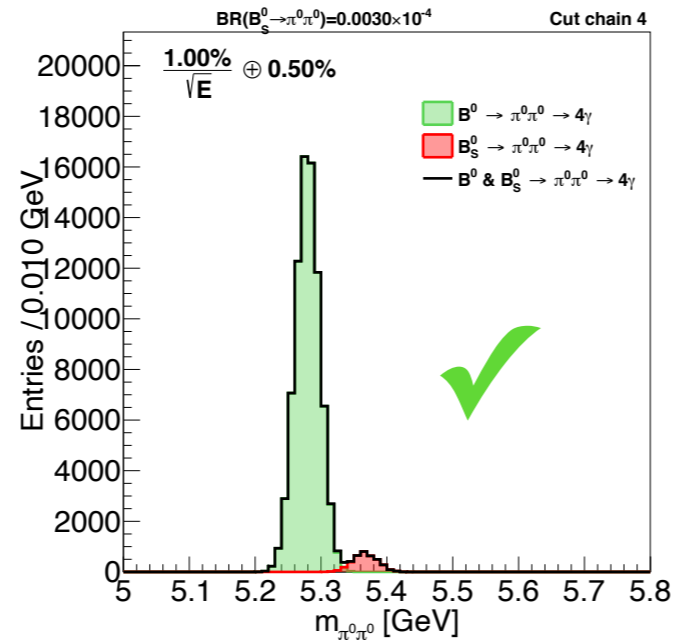
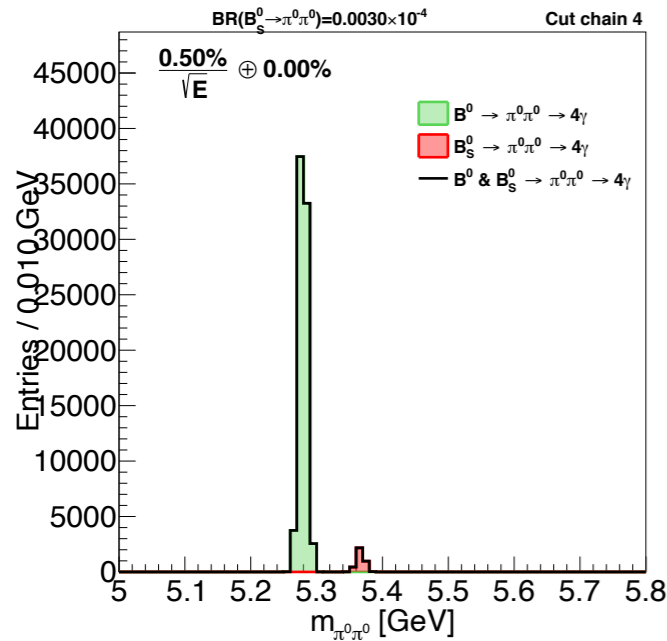


$\epsilon \times p > 90\%$ in energy range $> 20\text{GeV}$

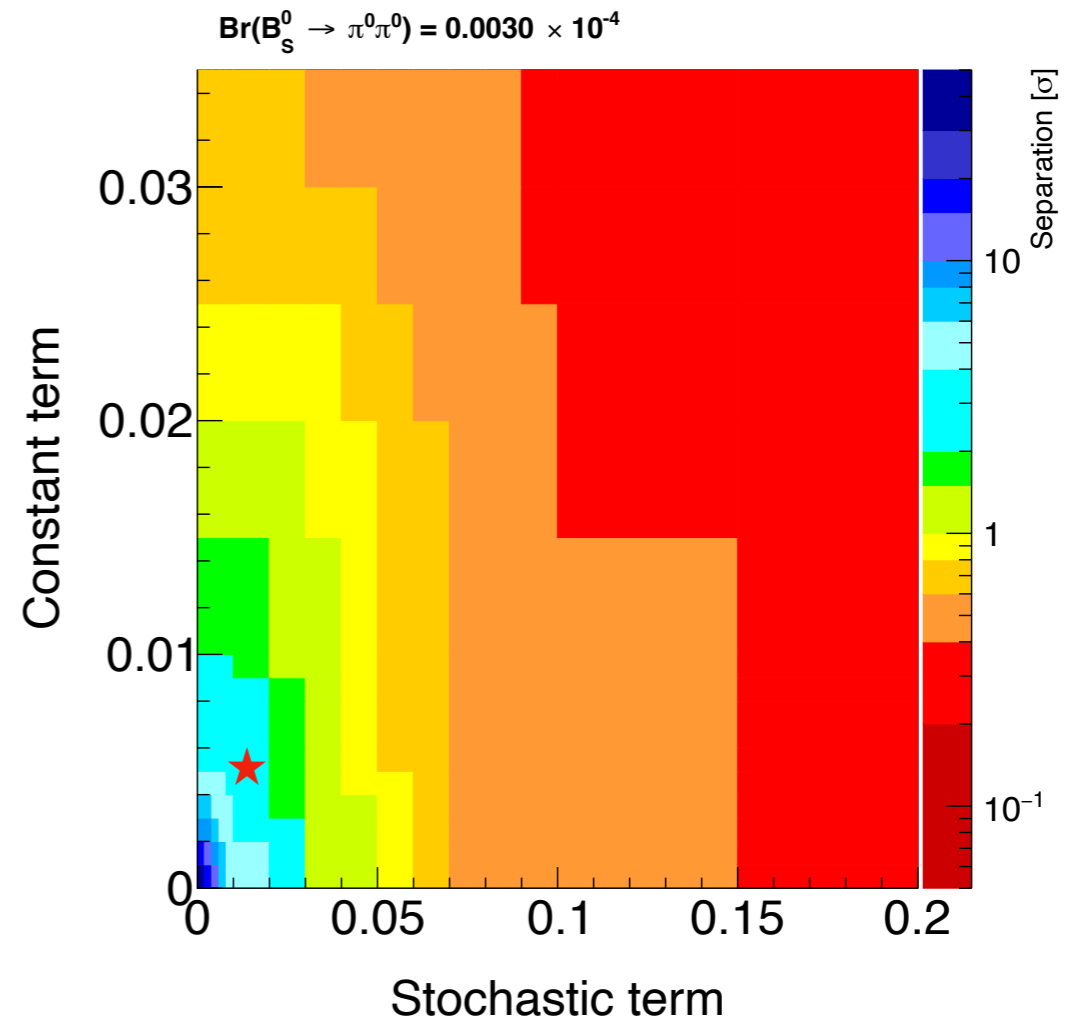
Separation of B^0 and B_s

$$m_{B^0} = 5279.63 \pm 0.15 \text{ MeV}$$

$$m_{B_s^0} = 5366.89 \pm 0.19 \text{ MeV}$$

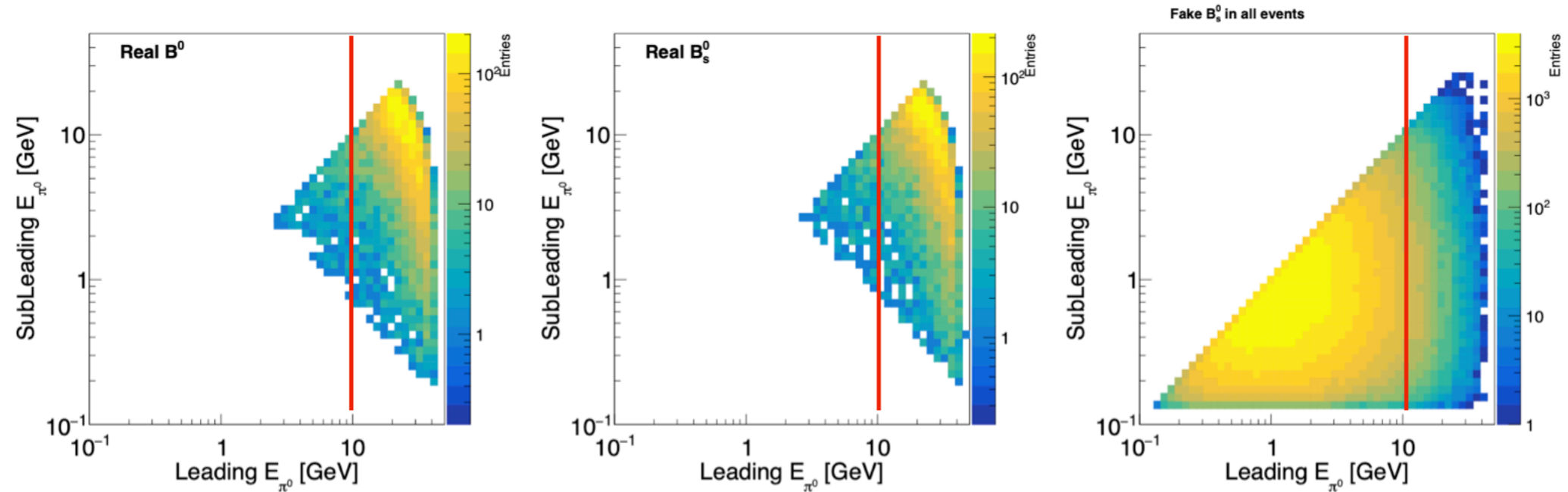


$$\text{separation power} = \frac{|\bar{m}_{B^0} - \bar{m}_{B_s^0}|}{\sqrt{\sigma_{m_{B^0}}^2 + \sigma_{m_{B_s^0}}^2}}$$

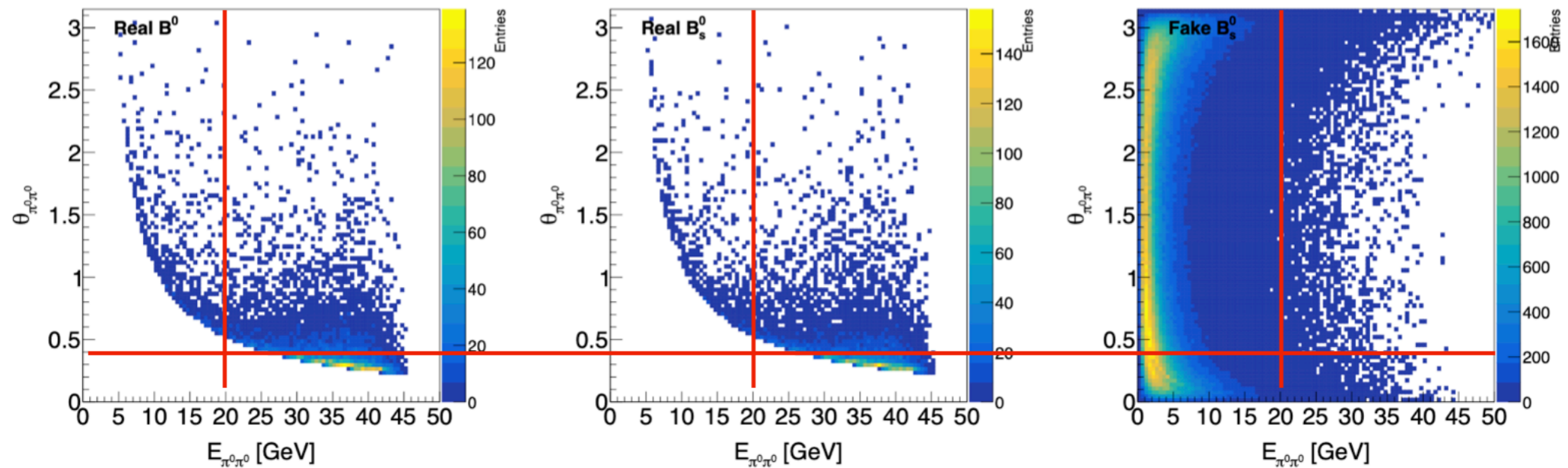


ECAL energy resolution $\text{better than } 1\%/\sqrt{E} \oplus 0.5\%$ is required.

MCTruth Distribution of $B^0/B_s \rightarrow \pi^0\pi^0$



(a) Energy spectrum of π^0 pairs in $B^0 \rightarrow \pi^0\pi^0$ (left), $B_s^0 \rightarrow \pi^0\pi^0$ (middle), and $Z \rightarrow q\bar{q}$ (right) events.

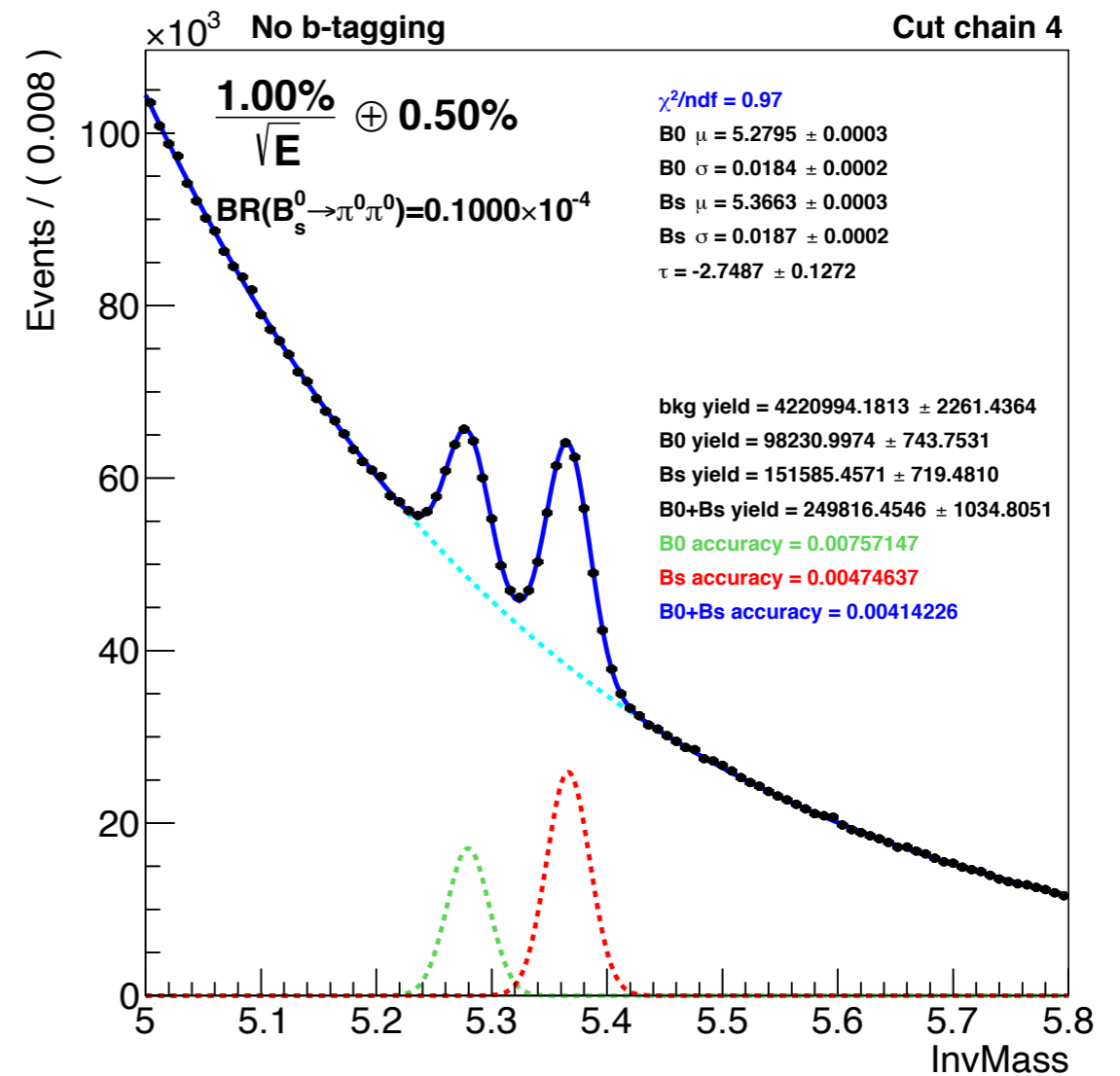
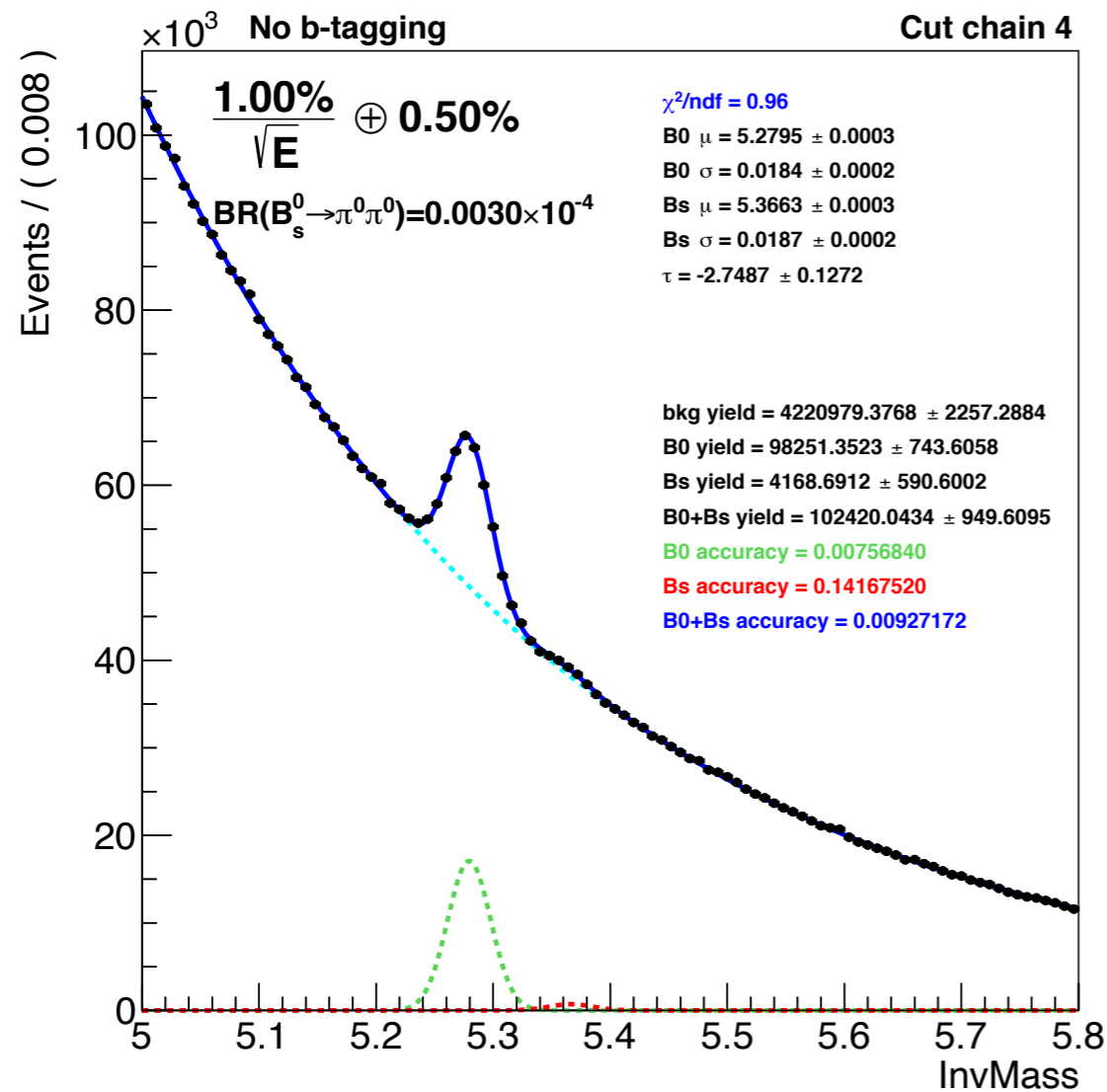


(b) $\theta_{\pi^0\pi^0}$ vs $E_{\pi^0\pi^0}$ in $B^0 \rightarrow \pi^0\pi^0$ (left), $B_s^0 \rightarrow \pi^0\pi^0$ (middle), and $Z \rightarrow q\bar{q}$ (right) events.

Energy and Angle cut on π^0
 $E_{\min} > 6\text{GeV}$ & $E_{\max} > 14\text{GeV}$ & Total $E > 22\text{GeV}$ & Angle $< 23^\circ$

Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $1\%/\sqrt{E} \oplus 0.5\%$ ECAL resolution



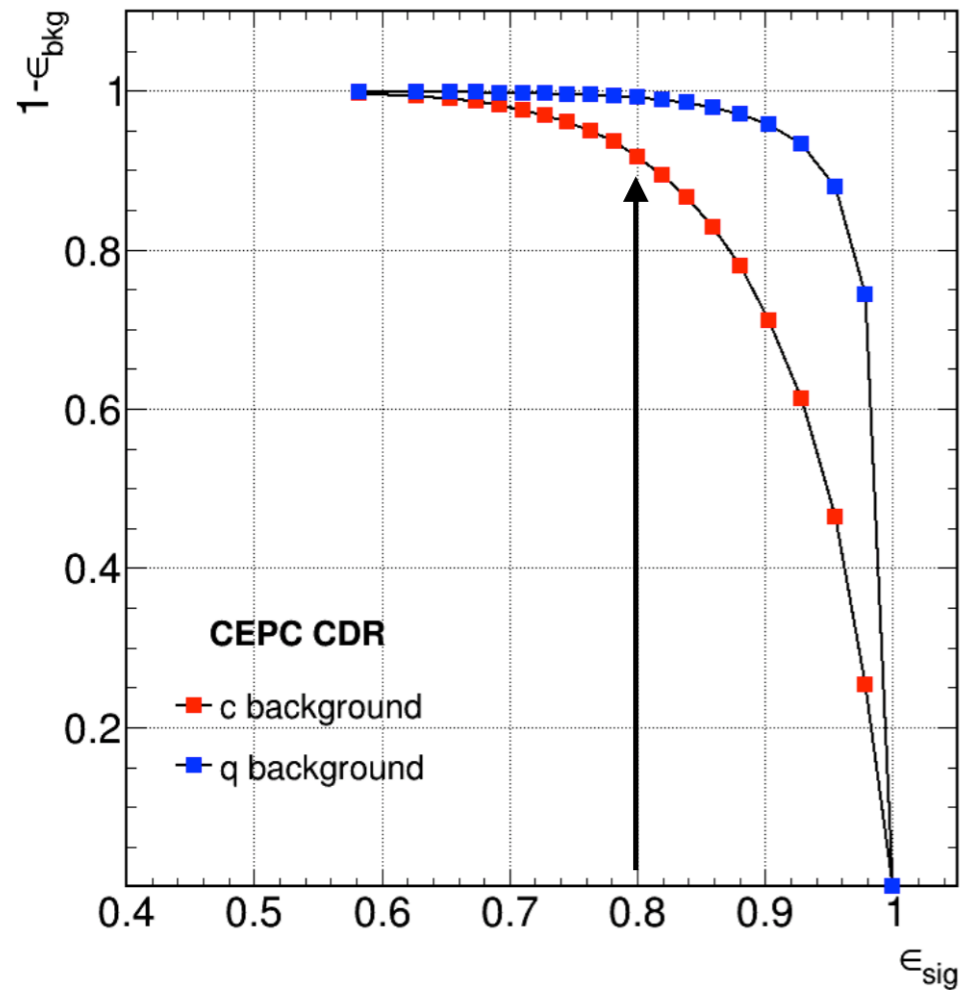
Gaussian signal + exponential background

Results without b-tagging

Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

Shape of background wo/wi b-tagging

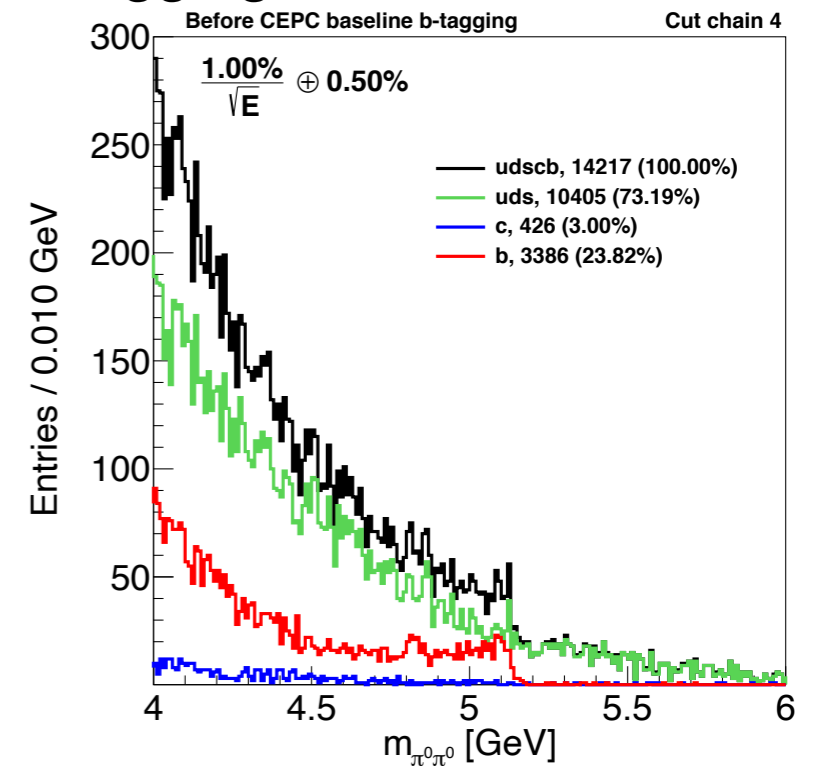
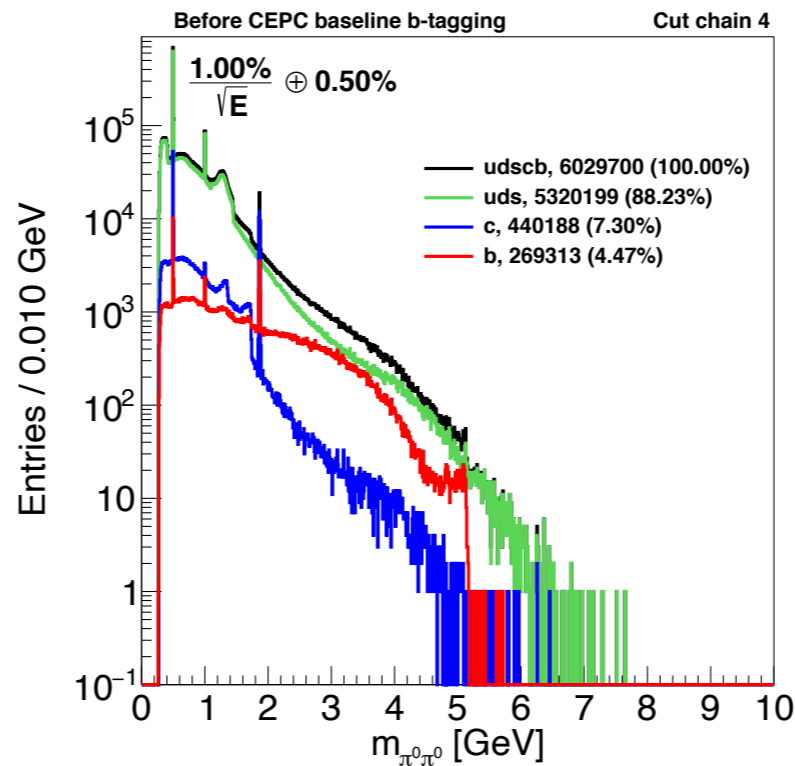
CEPC baseline b-tagging



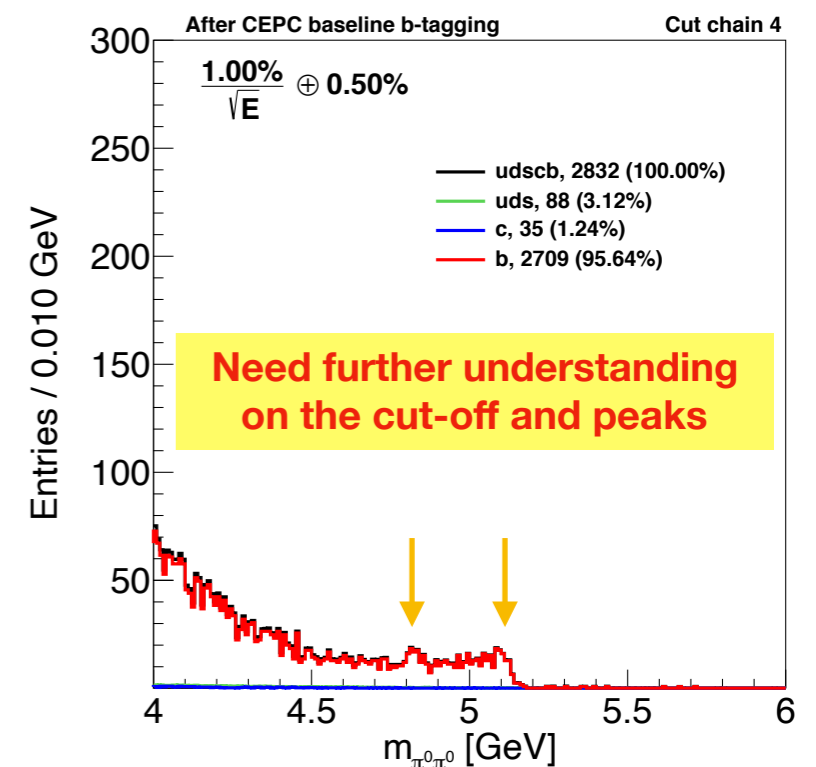
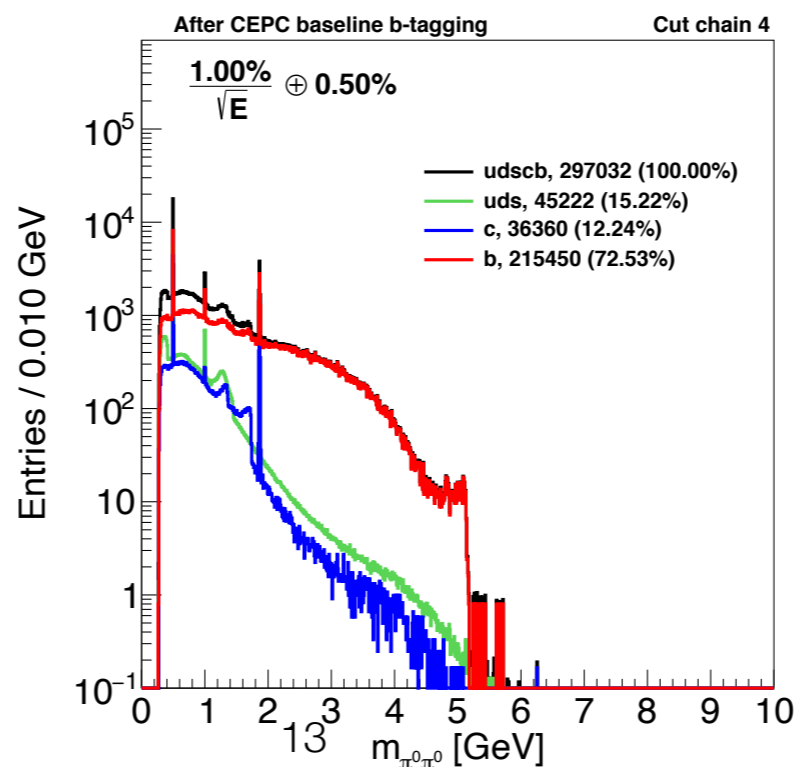
efficiency of 80%
purity of 90%

$$(\epsilon_{b \rightarrow b} = 80\%, \epsilon_{c \rightarrow b} = 8.26\%, \epsilon_{uds \rightarrow b} = 0.85\%)$$

Before b-tagging

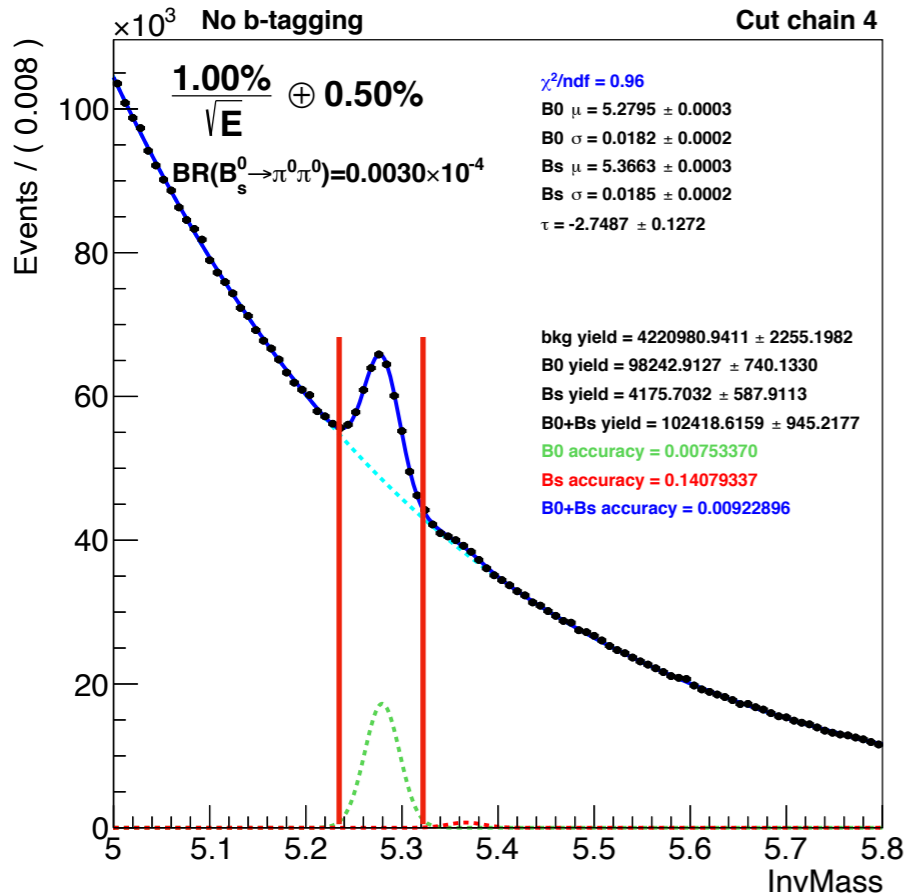


After b-tagging



Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $1\%/\sqrt{E} \oplus 0.5\%$ ECAL resolution



Mass window cut (counting) instead of **Fitting**
with results in the same order of magnitude

$$Accuracy = \sqrt{S + B/S}$$

	B^0	B_s^0
Fitting	0.75337%	14.079337%
Mass window cut	0.748274%	12.7002%

Cut chain	$B^0 \rightarrow \pi^0\pi^0 \rightarrow 4\gamma$	$B_s^0 \rightarrow \pi^0\pi^0 \rightarrow 4\gamma$	$q\bar{q}$	$u\bar{u}+d\bar{d}+s\bar{s}$	$c\bar{c}$	$b\bar{b}$	$\sqrt{S + B/S}$
Total generated	191113	8948	7e11 (100.00%)	4.285e11 (61.21%)	1.203e11 (17.19%)	1.512e11 (21.60%)	
$\gamma\gamma \rightarrow \pi^0$	187085	8760	28207036652152	15280186294352	5098265560853	7828584796947	
Lower $E_{\pi^0} > 6$ GeV	115684	5501	85022859011	64444435158	11390098533	9188325320	
Higher $E_{\pi^0} > 14$ GeV	109291	5190	19115874096	16695075894	1487448714	933349488	
$E_{\pi^0\pi^0} > 22$ GeV	108978	5171	17108689993	15097417243	1247342344	763930406	
$\theta_{\pi^0\pi^0} < 23^\circ$	97502	4557	17025770647	15022387179	1242937448	760446021	
$m_{\pi^0\pi^0} \in (5.2578, 5.3013)$ GeV ($1.2 \sigma_{m_{B^0}}$)	83268	1	304954	296483	2824	5647	0.748274%
$m_{\pi^0\pi^0} \in (5.3404, 5.3922)$ GeV ($1.4 \sigma_{m_{B^0}}$)	391	3981	251305	240010	5647	5647	12.700201%

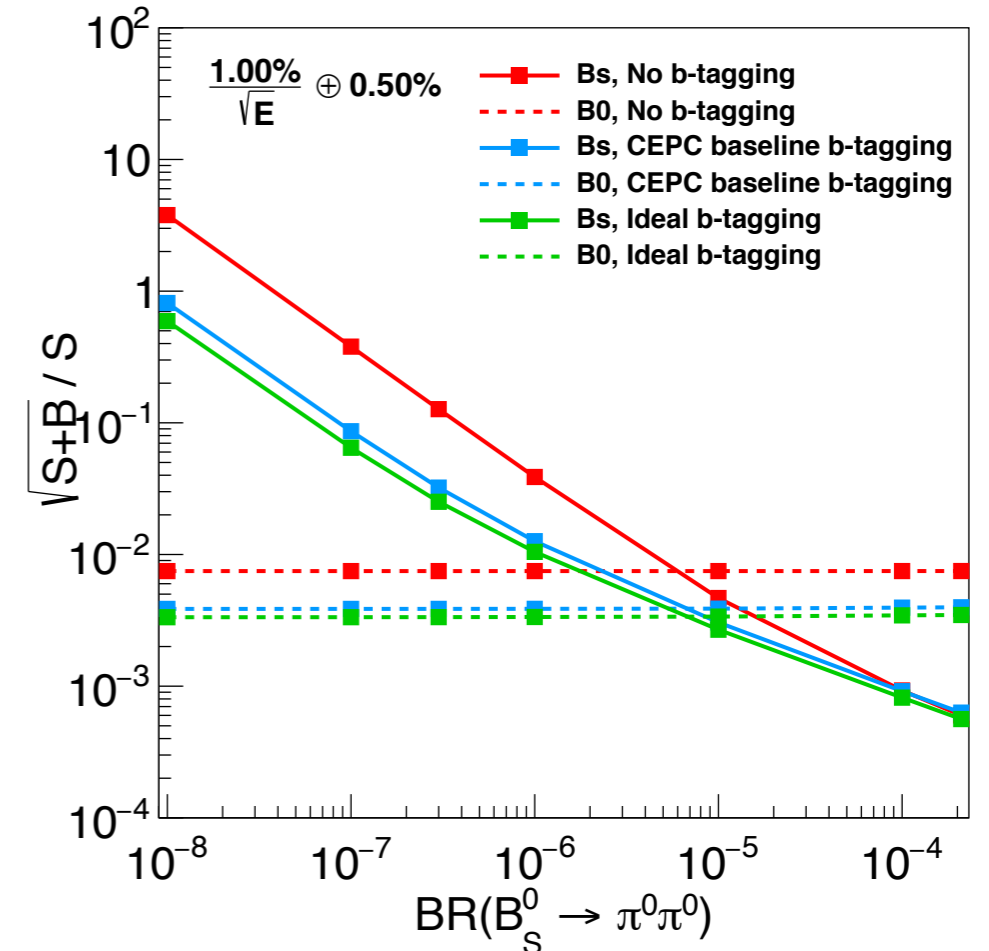
Table 2: Scaled (to Tera-Z) statistics in wide range mass window (0,10) GeV, no b-tagging, at $\frac{1\%}{\sqrt{E}} \oplus 0.5\%$

Individual measurement of $B^0/B_s \rightarrow \pi^0\pi^0$ at $1\%/\sqrt{E} \oplus 0.5\%$ ECAL resolution

Cut chain	$B^0 \rightarrow \pi^0\pi^0 \rightarrow 4\gamma$	$B_s^0 \rightarrow \pi^0\pi^0 \rightarrow 4\gamma$	$q\bar{q}$	$u\bar{u}+d\bar{d}+s\bar{s}$	$c\bar{c}$	$b\bar{b}$	$\sqrt{S+B}/S$
Total generated	191113	8948	7e11 (100.00%)	4.285e11 (61.21%)	1.203e11 (17.19%)	1.512e11 (21.60%)	
b-tagging ($\epsilon_{b \rightarrow b} = 80\%$, $\epsilon_{c \rightarrow b} = 8.26\%$, $\epsilon_{uds \rightarrow b} = 0.85\%$)	152890	7158	1.34539e11 (100.00%)	3.64225e9 (2.70%)	9.93678e9 (7.38%)	1.2096e11 (89.92%)	
$\gamma\gamma \rightarrow \pi^0$	149668	7008	6813866156386	129881583502	421116735326	7828584796947	
Lower $E_{\pi^0} > 6$ GeV	92547	4401	8839260094	547777699	940822139	7350660256	
Higher $E_{\pi^0} > 14$ GeV	87433	4152	1011451000	141908145	122863264	746679591	
$E_{\pi^0\pi^0} > 22$ GeV	87183	4137	842502849	128328047	103030478	611144325	
$\theta_{\pi^0\pi^0} < 23^\circ$	78001	3646	838713741	127690291	102666633	608356816	
$m_{\pi^0\pi^0} \in (5.2251, 5.3339)$ GeV ($3 \sigma_{m_{B^0}}$)	77673	88	12307	5064	466	6777	0.386382%
$m_{\pi^0\pi^0} \in (5.3404, 5.3922)$ GeV ($1.4 \sigma_{m_{B_s^0}}$)	313	3185	7024	2040	466	4518	3.220553%

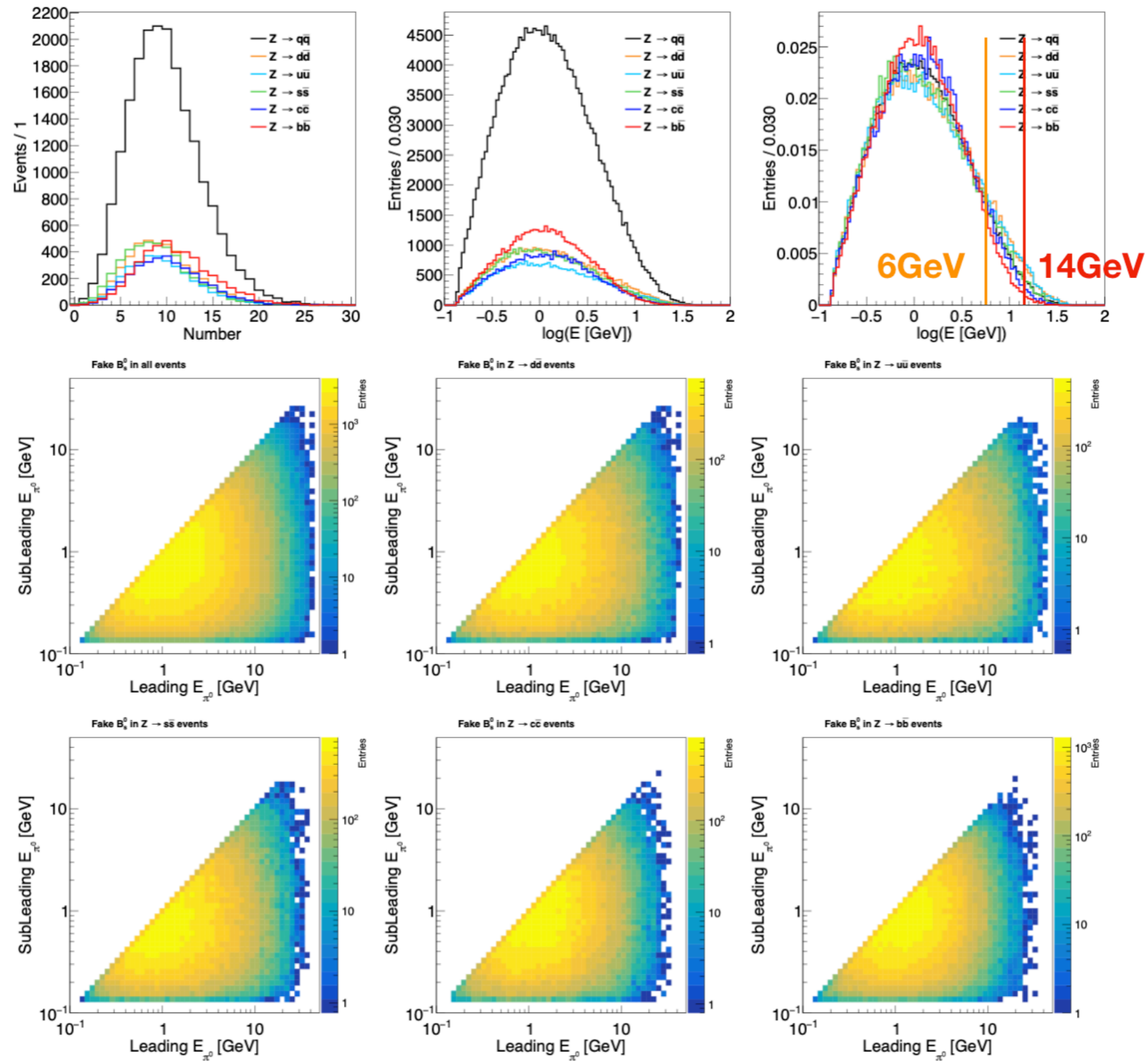
Table 4: Scaled (to Tera-Z) statistics in wide range mass window (0,10) GeV, CEPC baseline b-tagging, at $\frac{1\%}{\sqrt{E}} \oplus 0.5\%$

	B^0	B_s^0
No b-tagging	0.748274%	12.7002%
CEPC baseline b-tagging	0.386382%	3.220553%



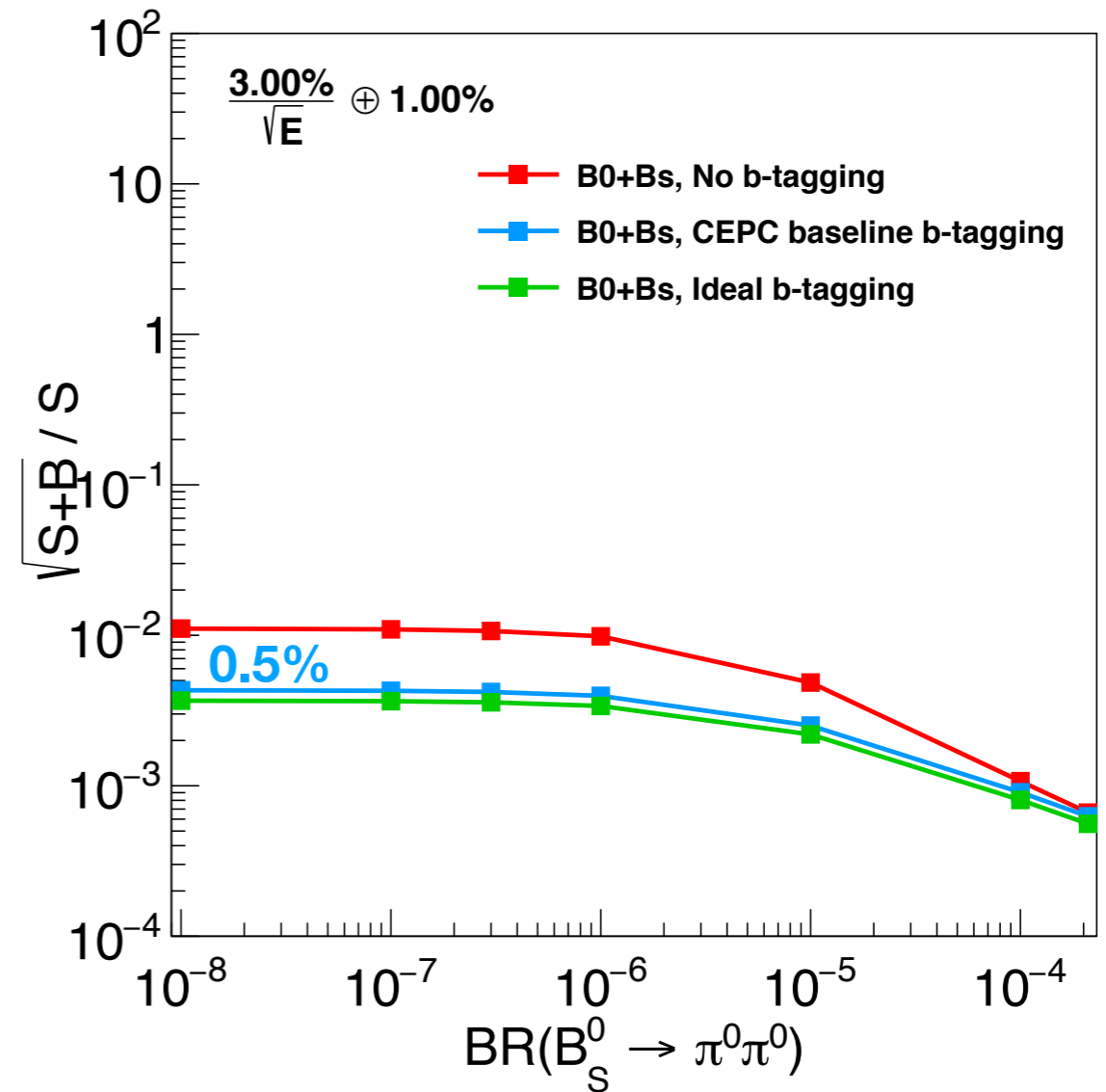
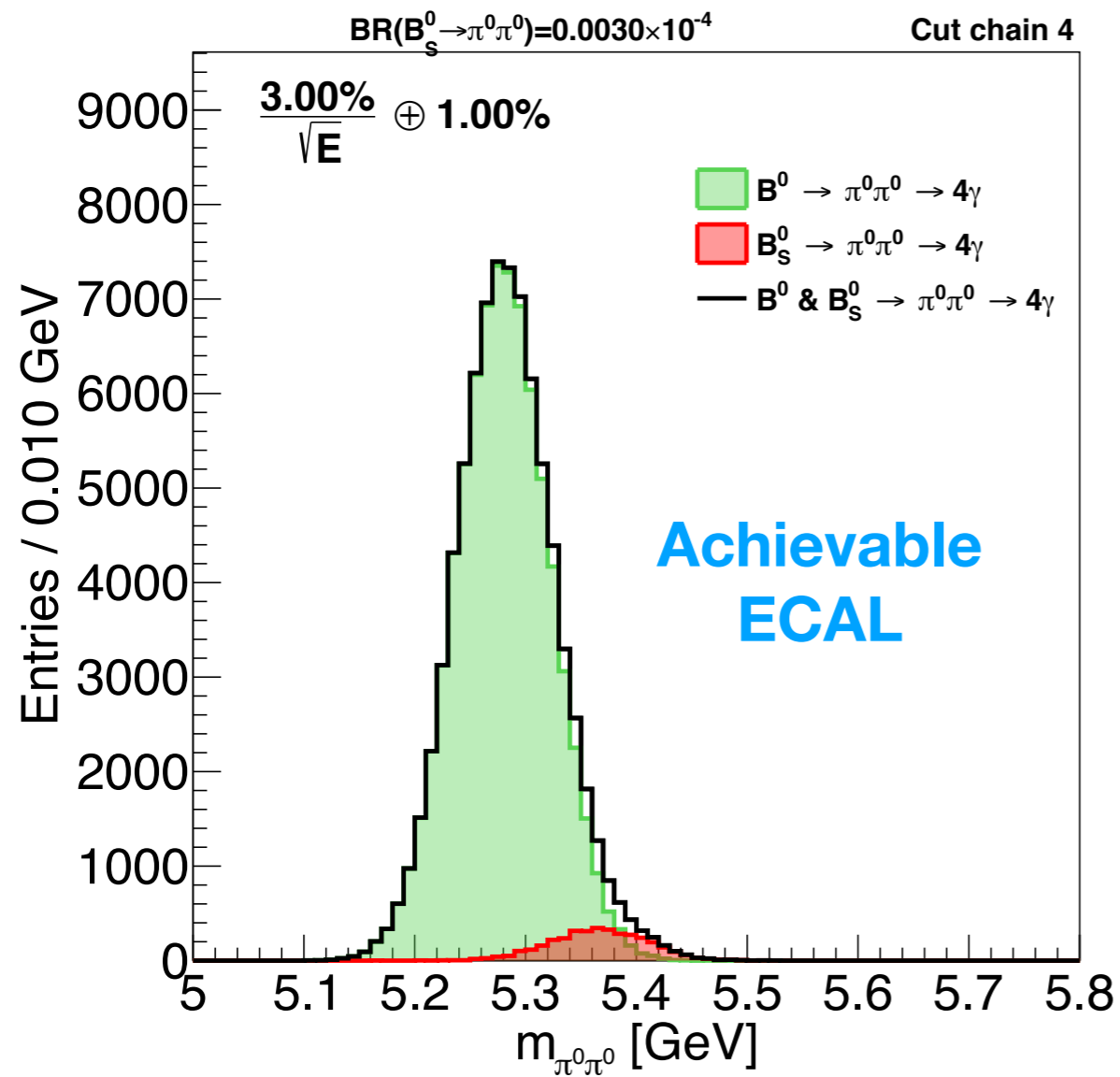
Further understanding on the effect of b-tagging

π^0 energy spectrum differs in different quark flavor events



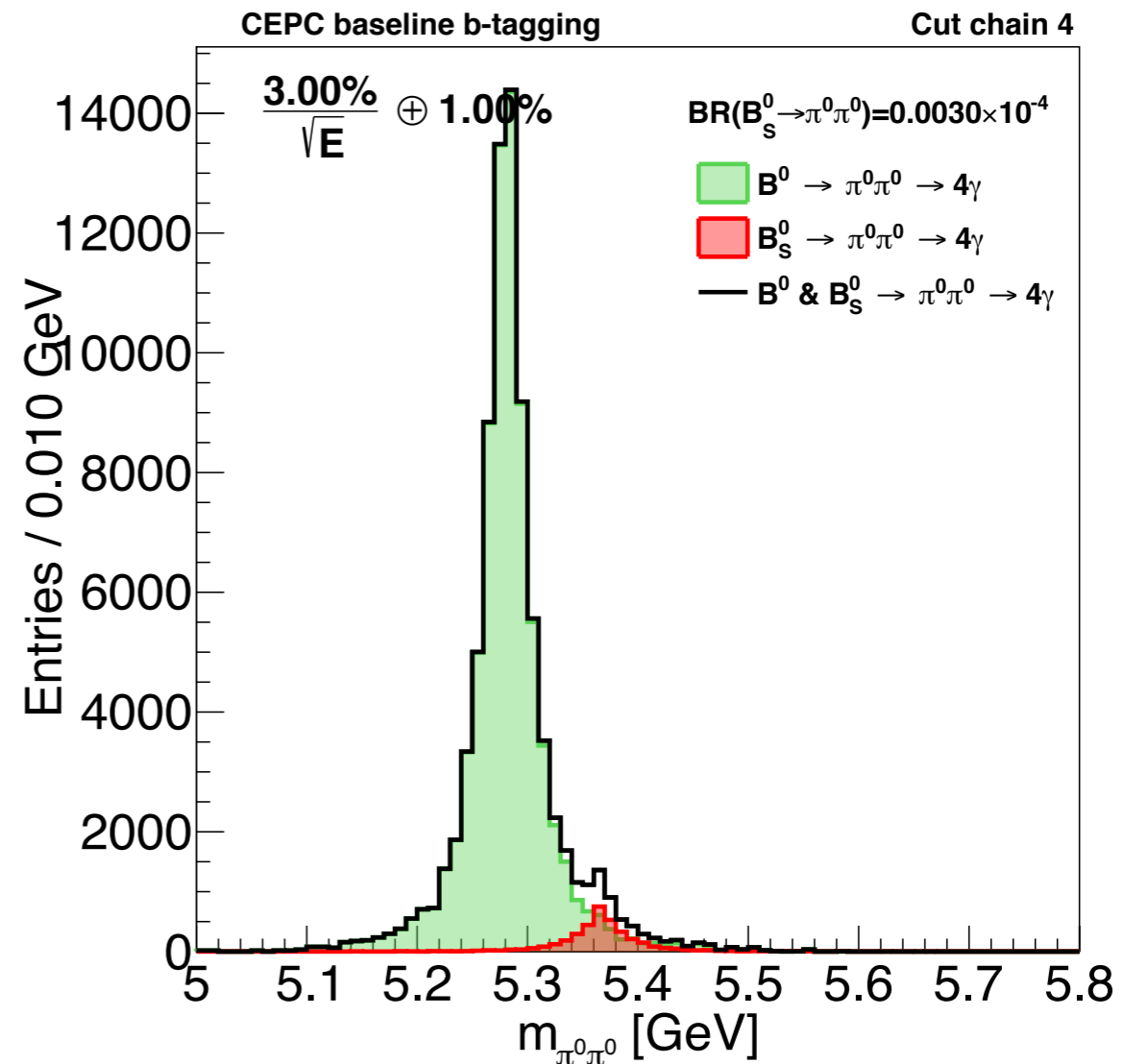
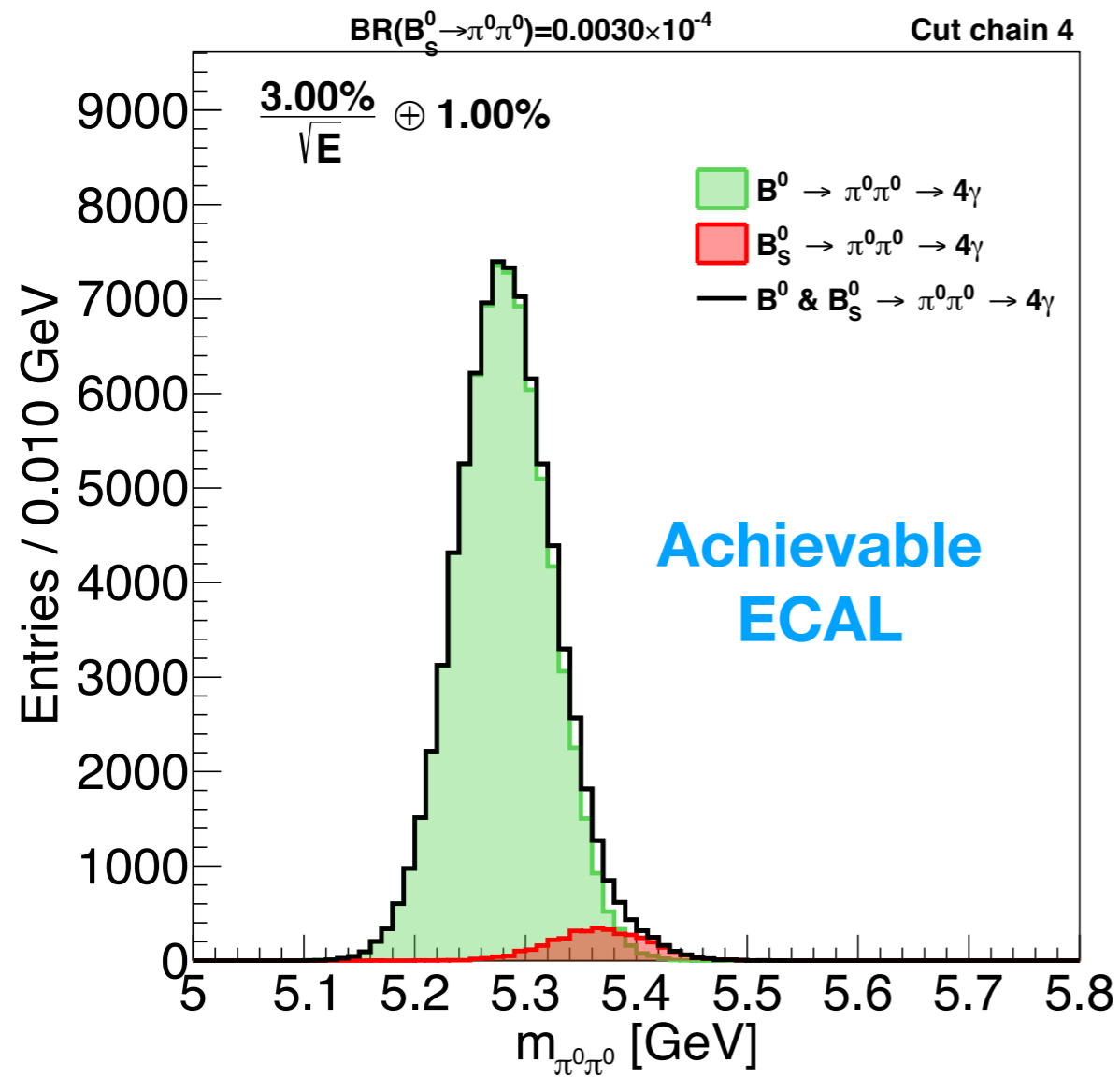
Mixed measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $3\%/\sqrt{E} \oplus 1\%$ ECAL resolution



Kinematic Fit

at $3\%/\sqrt{E} \oplus 1\%$ ECAL resolution



Signal peak gets sharpened after Kinematic Fit
Still on-going work to model the signal and background

Summary

Fast simulation study

Reconstruction of π^0

EM resolution: $15\%/\sqrt{E} \oplus 1\% \rightarrow 3\%/\sqrt{E} \oplus 1\%$

π^0 mass resolution: 4-5 times improvement

$\varepsilon \times p > 60\%$ especially for high energy ones

A neat separation of B^0 & B_s wo Kinematic fit requires ECAL resolution better than $1\%/\sqrt{E} \oplus 0.5\%$

B-tagging is necessary: improve the accuracy by 2-4 times

Future works

Further understanding on the shape of bb background

Kinematic fit

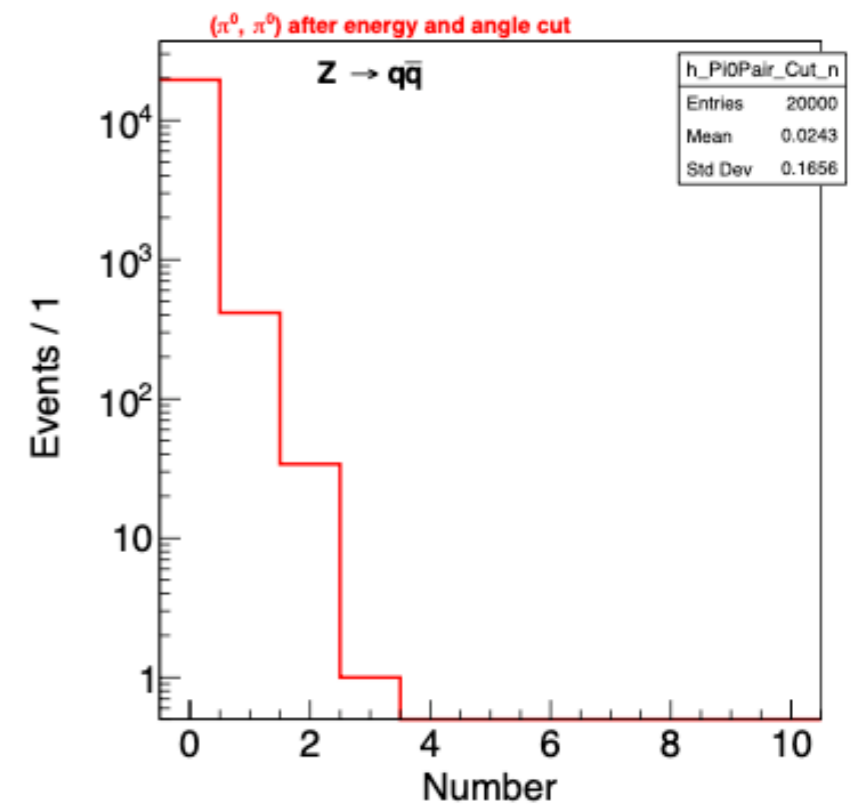
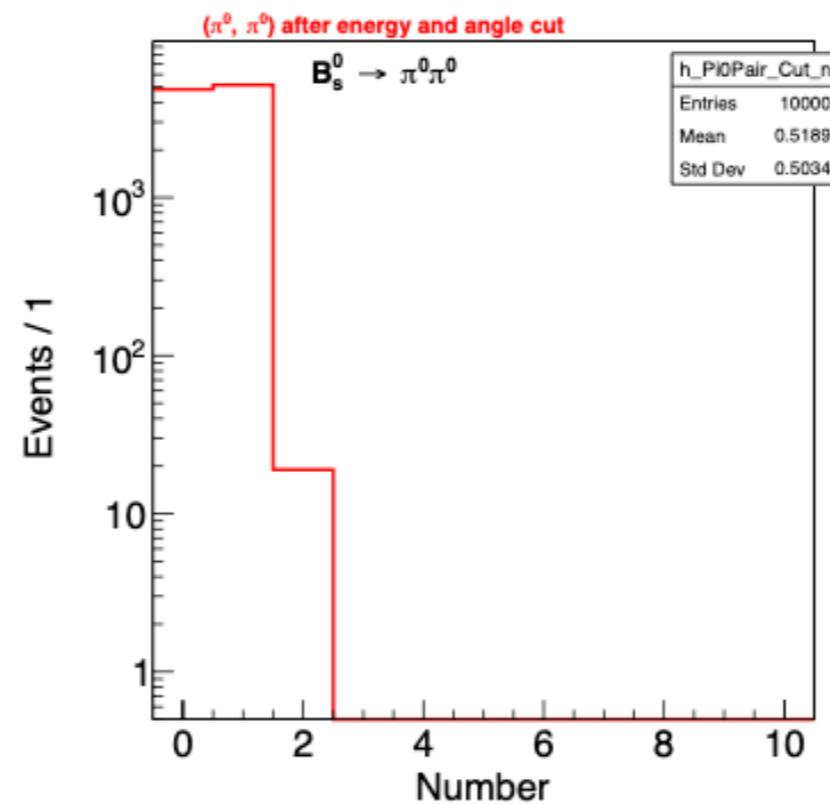
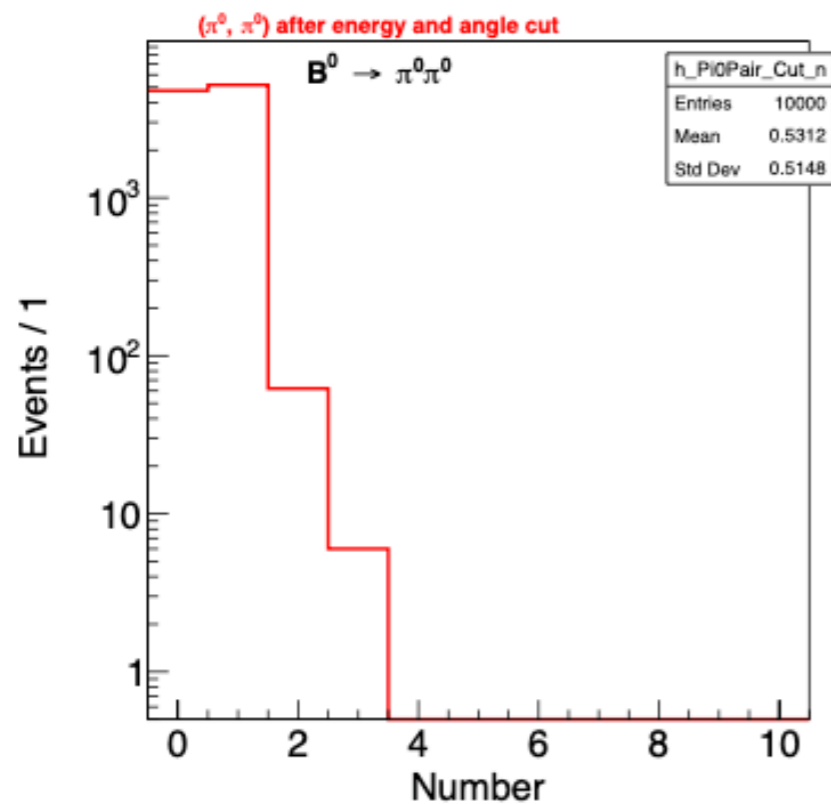
Thanks!

Backup

A Number of (π^0, π^0) after energy and angle cut

Information from MCTruth sample.

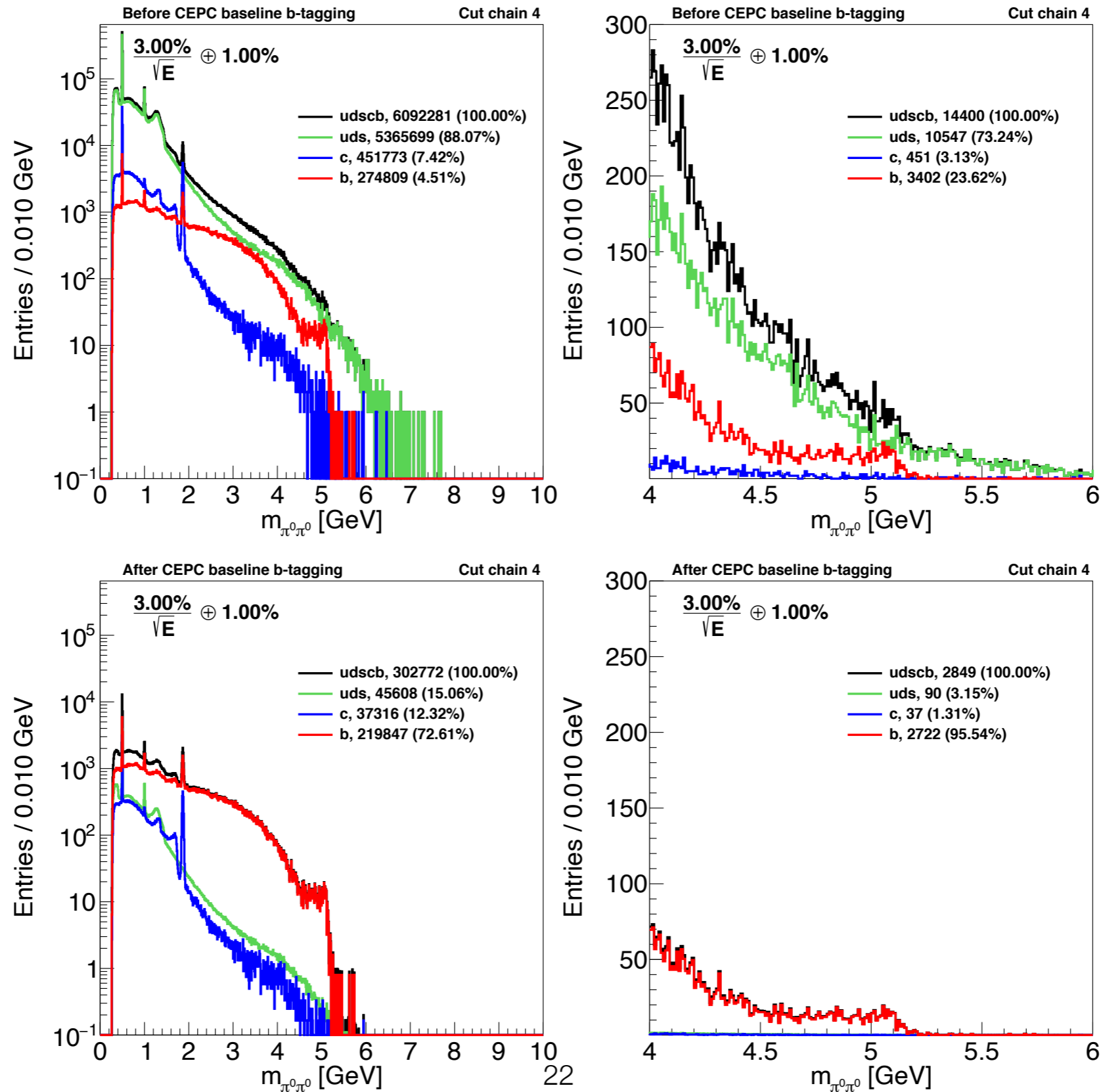
Cut: Lower $E_{\pi^0} > 6$ GeV & Higher $E_{\pi^0} > 14$ GeV & $E_{\pi^0\pi^0} > 22$ GeV & $\theta_{\pi^0\pi^0} < 23^\circ$



Fraction of events remaining more than 1 π^0 pair after energy and angle cut is small.

Mixed measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $3\%/\sqrt{E} \oplus 1\%$ ECAL resolution



Mixed measurement of $B^0/B_s \rightarrow \pi^0\pi^0$

at $3\%/\sqrt{E} \oplus 1\%$ ECAL resolution without b-tagging

