



Higgs CP measurement with EFT model in lepton collider

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Introduction

Properties of Higgs in Standard Model: $m_H = 125.10\text{GeV}$, $J^{PC} = 0^{++}$

Related experiments in LHC:

- The hypothesis of spin-1 or spin-2 Higgs has been excluded by ATLAS and CMS at >99% CL in $\sqrt{s} = 7\&8$ TeV, 25fb-1 data.
- SM+BSM Higgs CP mixing model is still under testing.

Higgs-gauge vector boson interaction lacks precise measurement in all inclusive Higgs production mode(i.e. ggF dominant).

[Eur. Phys. J. C75 \(2015\) 476](#)

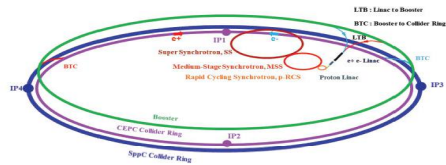
Any observation of CPV in Higgs would be New Physics!

What we want to study is the Higgs CP mixing model aiming to find the CP-odd Higgs.

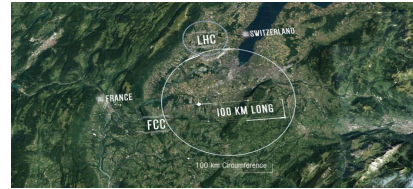
Introduction

Future e^+e^- collider experiment as Higgs factory :

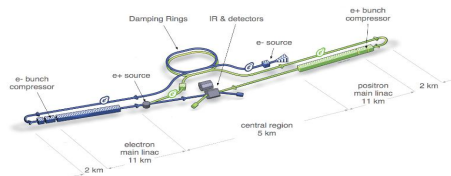
- At a center of mass energy of $\sqrt{s} \sim 240 \text{ GeV}$ which maximizes the Higgs boson production cross section through $e^+e^- \rightarrow ZH$ process.
- Cleaner environment and more events produced than (HL)-LHC.
- More precise Higgs-gauge boson coupling study.



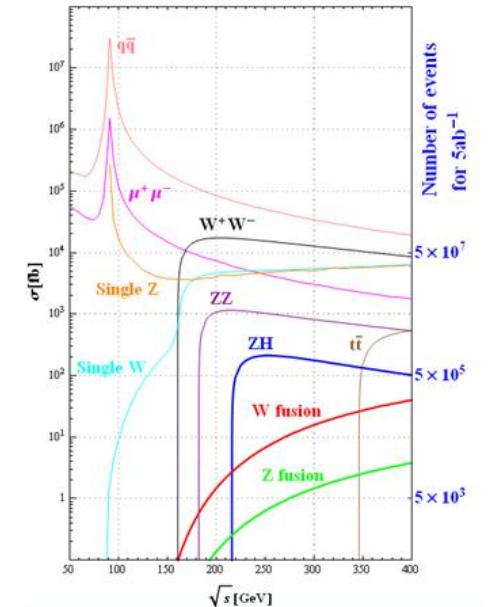
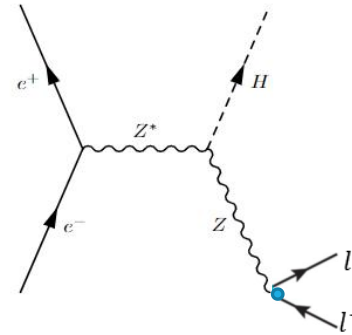
CEPC, 5.6 ab^{-1} @ 240 GeV



FCC-ee, 5 ab^{-1} @ 240 GeV



ILC, 2 ab^{-1} @ 250 GeV



Theory model

[JHEP 03\(2016\) 050](#)

[JHEP 11\(2014\) 028](#)

Consider a 6-dimension EFT model: $\mathcal{L}_{eff} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda^2} \sum_{k=1}^{59} \alpha_k \mathcal{O}_k (\mathcal{L}_{BSM})$

- In this base, the experimental observables G_F, m_Z, α_{em} could be presented:

$$m_Z = m_{Z0}(1 + \delta_Z), \quad G_F = G_{F0}(1 + \delta_{G_F}), \quad \alpha_{em} = \alpha_{em0}(1 + \delta_A)$$

$$\text{where: } \delta_Z = \hat{\alpha}_{ZZ} + \frac{1}{4}\hat{\alpha}_{\Phi D}, \quad \delta_{G_F} = -\hat{\alpha}_{4l} + 2\hat{\alpha}_{\Phi l}^{(3)}, \quad \delta_A = 2\hat{\alpha}_{AA}.$$

Theory model

[JHEP 03\(2016\) 050](#)

[JHEP 11\(2014\) 028](#)

The $H \rightarrow Zll$ matrix element:

$$\mathcal{M}_{HZ\ell\ell}^{\mu} = \frac{1}{m_H} \bar{u}(p_3, s_3) \left[\gamma^{\mu} (H_{1,V} + H_{1,A} \gamma_5) + \frac{q^{\mu} \not{p}}{m_H^2} (H_{2,V} + H_{2,A} \gamma_5) + \frac{\epsilon^{\mu\nu\sigma\rho} p_{\nu} q_{\sigma}}{m_H^2} \gamma_{\rho} (H_{3,V} + H_{3,A} \gamma_5) \right] v(p_4, s_4)$$

- Where $\epsilon_{0123} = +1$ and $q = p_3 + p_4$.

And the parameters in the function are following:

$$H_{1,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2}r}{r-s}g_V \left(1 + \hat{\alpha}_1^{\text{eff}} - \frac{\kappa}{r}\hat{\alpha}_{ZZ} - \frac{\kappa}{2r}\frac{Q_{\ell}g_{em}(r-s)}{sg_V}\hat{\alpha}_{AZ} \right)$$

$$H_{1,A} = \frac{2m_H(\sqrt{2}G_F)^{1/2}r}{r-s}g_A \left(1 + \hat{\alpha}_2^{\text{eff}} - \frac{\kappa}{r}\hat{\alpha}_{ZZ} \right),$$

$$H_{2,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2}}{r-s}g_V \left[2\hat{\alpha}_{ZZ} + \frac{Q_{\ell}g_{em}(r-s)}{sg_V}\hat{\alpha}_{AZ} \right]$$

$$H_{2,A} = \frac{4m_H(\sqrt{2}G_F)^{1/2}}{r-s}g_A\hat{\alpha}_{ZZ}$$

$$H_{3,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2}}{r-s}g_V \left[2\hat{\alpha}_{ZZ} + \frac{Q_{\ell}g_{em}(r-s)}{sg_V}\hat{\alpha}_{AZ} \right]$$

$$H_{3,A} = \frac{4m_H(\sqrt{2}G_F)^{1/2}}{r-s}g_A\hat{\alpha}_{ZZ}$$

$$\hat{\alpha}_1^{\text{eff}} \equiv \hat{\alpha}_{ZZ}^{(1)} - \frac{m_H(\sqrt{2}G_F)^{1/2}(r-s)}{2\sqrt{r}}\frac{\hat{\alpha}_{\Phi l}^V}{g_V}$$

$$\hat{\alpha}_2^{\text{eff}} \equiv \hat{\alpha}_{ZZ}^{(1)} + \frac{m_H(\sqrt{2}G_F)^{1/2}(r-s)}{2\sqrt{r}}\frac{\hat{\alpha}_{\Phi l}^A}{g_A}$$

 : SM term
Others : EFT contribution

Theory model

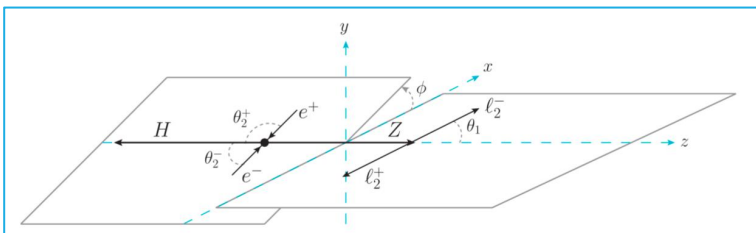
[JHEP 03\(2016\) 050](#)

[JHEP 11\(2014\) 028](#)

Differential cross section for $ee \rightarrow ZH \rightarrow llH$:

$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = \frac{\mathcal{N}_\sigma(q^2)}{m_H^2} \mathcal{J}(q^2, \theta_1, \theta_2, \phi),$$

$$\mathcal{N}_\sigma(q^2) = \frac{1}{2^{10}(2\pi)^3} \cdot \frac{1}{\sqrt{r}\gamma_Z} \cdot \frac{\sqrt{\lambda(1,s,r)}}{s^2}$$



$$\begin{aligned} \mathcal{J}(q^2, \theta_1, \theta_2, \phi) = & J_1(1 + \cos^2 \theta_1 \cos^2 \theta_2 + \cos^2 \theta_1 + \cos^2 \theta_2) \\ & + J_2 \sin^2 \theta_1 \sin^2 \theta_2 + J_3 \cos \theta_1 \cos \theta_2 \\ & + (J_4 \sin \theta_1 \sin \theta_2 + J_5 \sin 2\theta_1 \sin 2\theta_2) \sin \phi \\ & + (J_6 \sin \theta_1 \sin \theta_2 + J_7 \sin 2\theta_1 \sin 2\theta_2) \cos \phi \\ & + J_8 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\phi + J_9 \sin^2 \theta_1 \sin^2 \theta_2 \cos 2\phi. \end{aligned}$$

Variables for studying distribution: θ_1, θ_2, ϕ

Theory model

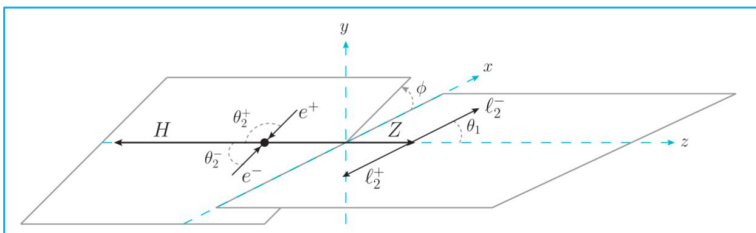
JHEP 03(2016) 050

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$$\begin{aligned} \mathcal{J}(q^2, \theta_1, \theta_2, \phi) = & J_1(1 + \cos^2 \theta_1 \cos^2 \theta_2 + \cos^2 \theta_1 + \cos^2 \theta_2) \\ & + J_2 \sin^2 \theta_1 \sin^2 \theta_2 + J_3 \cos \theta_1 \cos \theta_2 \\ & + (J_4 \sin \theta_1 \sin \theta_2 + J_5 \sin 2\theta_1 \sin 2\theta_2) \sin \phi \\ & + (J_6 \sin \theta_1 \sin \theta_2 + J_7 \sin 2\theta_1 \sin 2\theta_2) \cos \phi \\ & + J_8 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\phi + J_9 \sin^2 \theta_1 \sin^2 \theta_2 \cos 2\phi. \end{aligned}$$

Variables for studying distribution: θ_1, θ_2, ϕ

Assumption for simplification:

- $\delta_{GF} = \hat{\alpha}_{\phi l}^V = \hat{\alpha}_{\phi l}^A = \hat{\alpha}_{A\tilde{Z}} = \hat{\alpha}_{Z\tilde{Z}} = 10^{-3}$, others are set to 0, so $H_{2,V/A} = 0$.

$$J_1 = 2rs (g_A^2 + g_V^2) (|H_{1,V}|^2 + |H_{1,A}|^2),$$

$$J_2 = \kappa (g_A^2 + g_V^2) [\kappa (|H_{1,V}|^2 + |H_{1,A}|^2) + \lambda \text{Re}(H_{1,V} H_{2,V}^* + H_{1,A} H_{2,A}^*)],$$

$$J_3 = 32rs g_A g_V \text{Re}(H_{1,V} H_{1,A}^*),$$

$$J_4 = 4\kappa \sqrt{rs} \lambda g_A g_V \text{Re}(H_{1,V} H_{3,A}^* + H_{1,A} H_{3,V}^*),$$

$$J_5 = \frac{1}{2} \kappa \sqrt{rs} \lambda (g_A^2 + g_V^2) \text{Re}(H_{1,V} H_{3,V}^* + H_{1,A} H_{3,A}^*),$$

$$J_6 = 4\sqrt{rs} g_A g_V [4\kappa \text{Re}(H_{1,V} H_{1,A}^*) + \lambda \text{Re}(H_{1,V} H_{2,A}^* + H_{1,A} H_{2,V}^*)],$$

$$J_7 = \frac{1}{2} \sqrt{rs} (g_A^2 + g_V^2) [2\kappa (|H_{1,V}|^2 + |H_{1,A}|^2) + \lambda \text{Re}(H_{1,V} H_{2,V}^* + H_{1,A} H_{2,A}^*)],$$

$$J_8 = 2rs \sqrt{\lambda} (g_A^2 + g_V^2) \text{Re}(H_{1,V} H_{3,V}^* + H_{1,A} H_{3,A}^*),$$

$$J_9 = 2rs (g_A^2 + g_V^2) (|H_{1,V}|^2 + |H_{1,A}|^2).$$

6 of these 9 functions are independent

—	0 in assumption
 	EFT CP-odd term
Others	CP-even contribution

Optimal variable approach

Differential cross section could be represent as:

[PLB 306 \(1993\) 411-417](#)

$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = N \times (J_{CP-even}(\theta_1, \theta_2, \phi) + p \times J_{CP-odd}(\theta_1, \theta_2, \phi)).$$

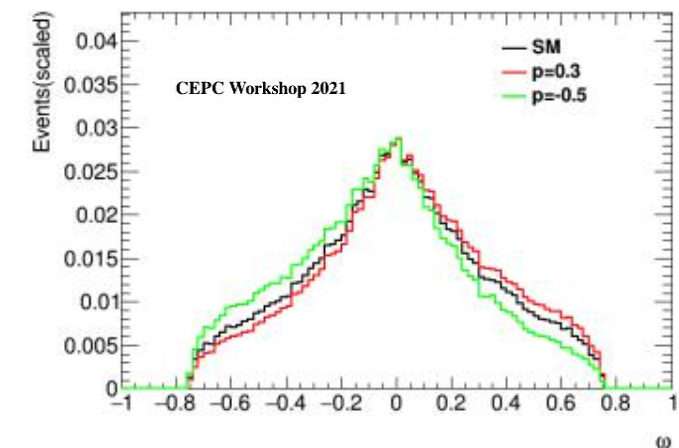
where p is an additional global CP-mixing parameter.

In this formation, we could define an **Optimal Variable** ω which combines the information from $\{\theta_1, \theta_2, \phi\}$:

$$\omega = \frac{J_{CP-odd}(\theta_1, \theta_2, \phi)}{J_{CP-even}(\theta_1, \theta_2, \phi)} \text{ to measure } p$$

Benefits:

- Combine the information from 3-dimension phase space
- Easier to study



Previous review

Previous Result : 95% CL $p \in [-5.70 \times 10^{-3}, 6.33 \times 10^{-3}]$, corresponding to $\delta G_F, \hat{\alpha}_{\phi l}^V, \hat{\alpha}_{\phi l}^A, \hat{\alpha}_{A\tilde{Z}}, \hat{\alpha}_{Z\tilde{Z}} < 10^{-6}$. [Higgs CP measurement analyses](#)

Previous comment: not consider the decay modes of Higgs & study on truth level.

Update: consider simulation and Higgs decay to $b\bar{b}/c\bar{c}/gg$.

MC: Whizard 1.95 in CEPC, $ee \rightarrow ZH \rightarrow \mu\mu H$.

Two samples:

- Simulation: fast simulation based on CEPC-v4 detector design
- Truth level: simulate the physical process of $ee \rightarrow ZH$ directly in dynamics

Higgs CP-mixing measurement

Event selection: (using Monte Carlo simulation sample)

- $\sqrt{s} = 240\text{GeV}$, $\int Ldt = 5.6\text{ab}^{-1}$
- **Signal**: $ee \rightarrow ZH \rightarrow \mu\mu H (\rightarrow b\bar{b}/c\bar{c}/gg)$ channel
- **Background**: Irreducible background which contains the same final states as that in signal.

- Muon pair selection:

$$|\cos\theta_{\mu^+\mu^-}| < 0.81; \quad \text{Mass}_{\mu\mu} \in (77.5\text{GeV}, 104.5\text{GeV}); \quad M_{recoil_{\mu\mu}} \in (124\text{GeV}, 140\text{GeV}).$$

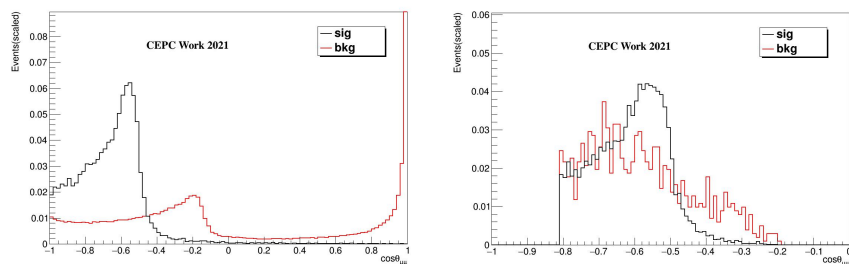
Where $M_{recoil_{\mu\mu}}^2 = (\sqrt{s} - E_{\mu\mu})^2 - p_{\mu\mu}^2 = s - 2E_{\mu\mu}\sqrt{s} + m_{\mu\mu}^2$

- Jets pair selection:

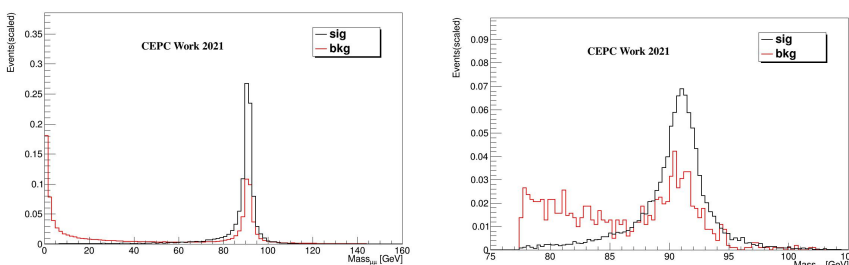
$$|\cos\theta_{jet}| < 0.96; \quad \text{Mass}_{jj} \in (100\text{GeV}, 150\text{GeV}).$$

Higgs CP-mixing measurement

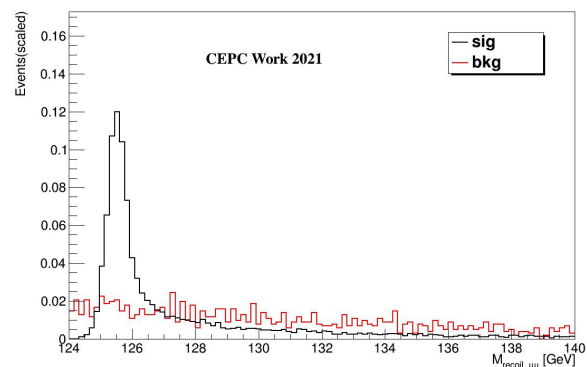
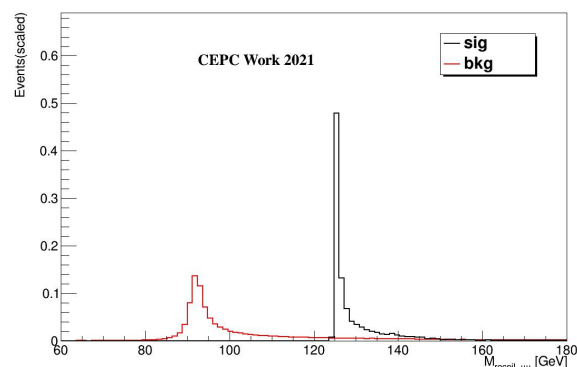
$$|\cos\theta_{\mu\mu}| < 0.81$$



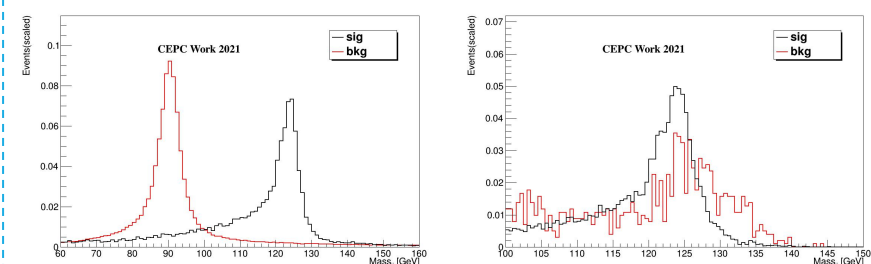
$$\text{Mass}_{\mu\mu} \in (77.5\text{GeV}, 104.5\text{GeV})$$



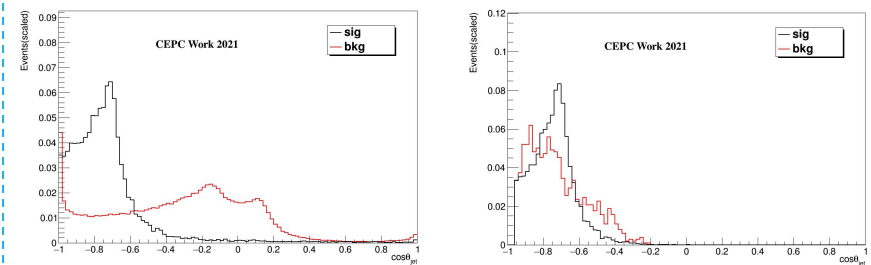
$$M_{\text{recoil}_{\mu\mu}} \in (124\text{GeV}, 140\text{GeV})$$



$$\text{Mass}_{jj} \in (100\text{GeV}, 150\text{GeV})$$



$$|\cos\theta_{\text{jet}}| < 0.96$$



Higgs CP-mixing measurement

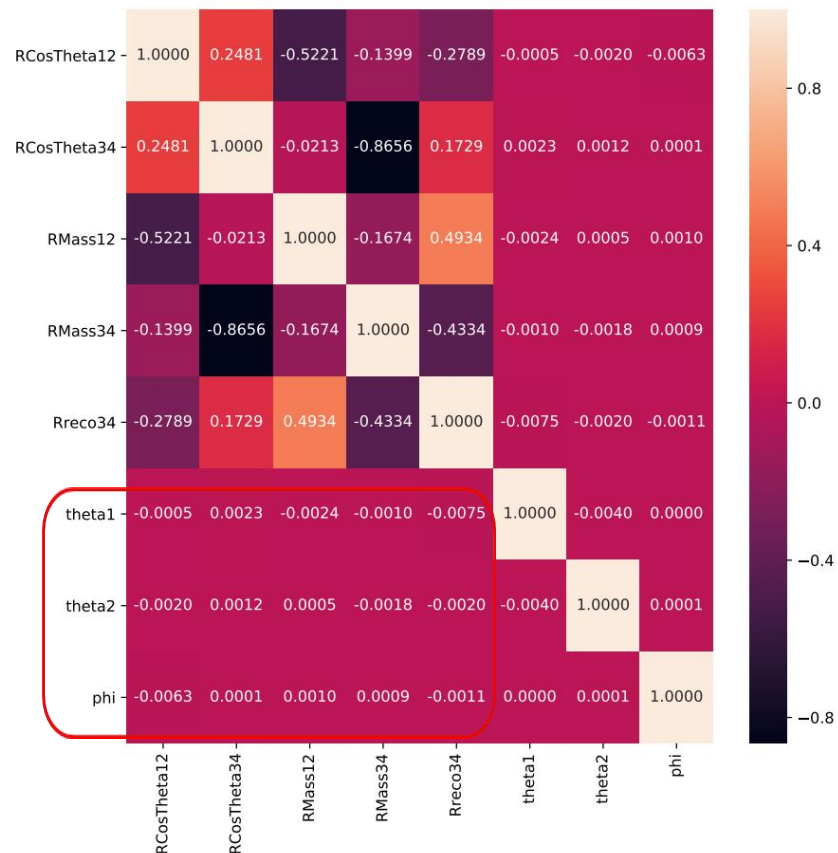
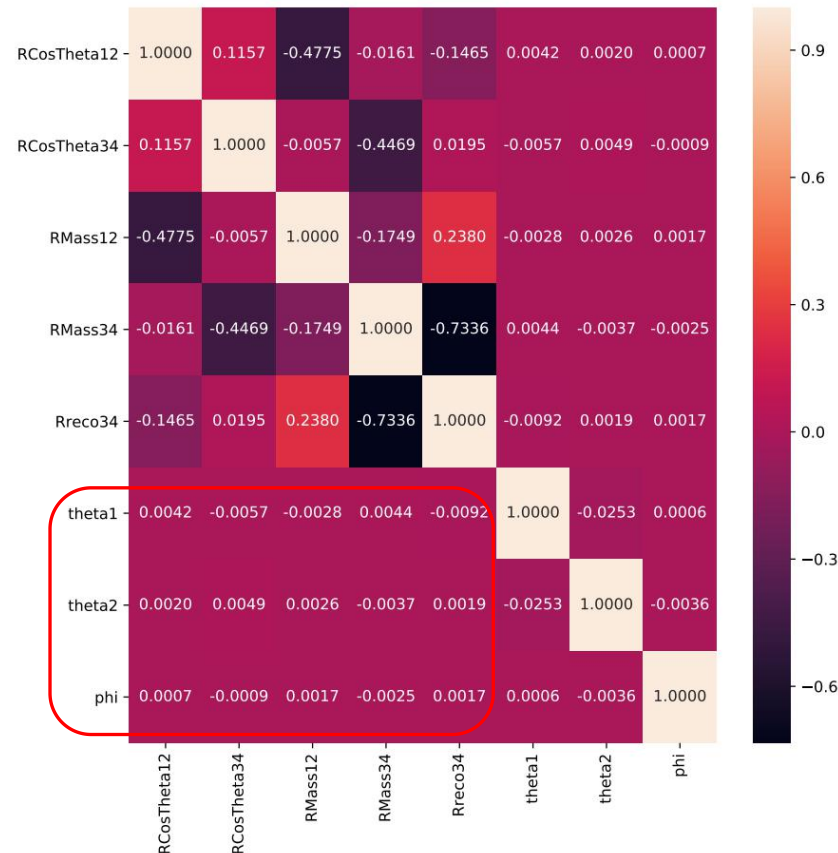
Cut Flow:

$ZH \rightarrow \mu^+ \mu^- + b\bar{b}/c\bar{c}/\tau\tau/gg$ channel		
	Signal	Irreducible Background
Original	28627	1251768
Muon pair selection	18420(efficiency:64.82%)	11370(efficiency:0.91%)
All selection	13312(efficiency:46.83%)	3610(efficiency:0.29%)

Higgs CP-mixing measurement

Correlation:

- We can see that θ_1 , θ_2 , ϕ have little correlation with $\cos\theta_{\mu^+\mu^-}$, $\text{Mass}_{\mu\mu}$, $M_{recoil_{\mu\mu}}$, $\cos\theta_{jet}$, Mass_{jj} .

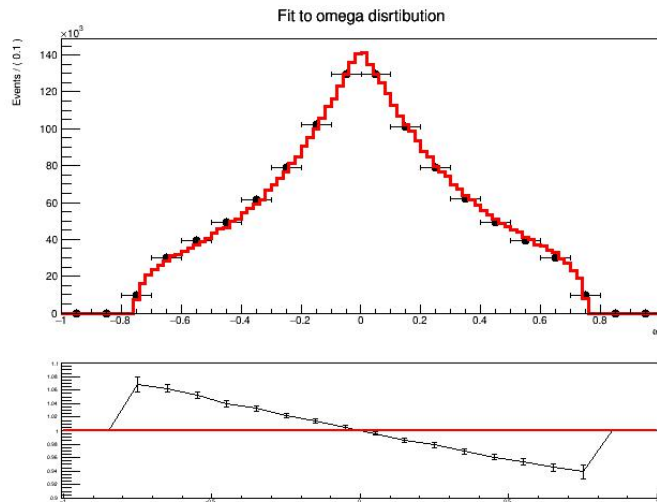


- So we can ignore the impact of event selections to θ_1 , θ_2 , and ϕ .

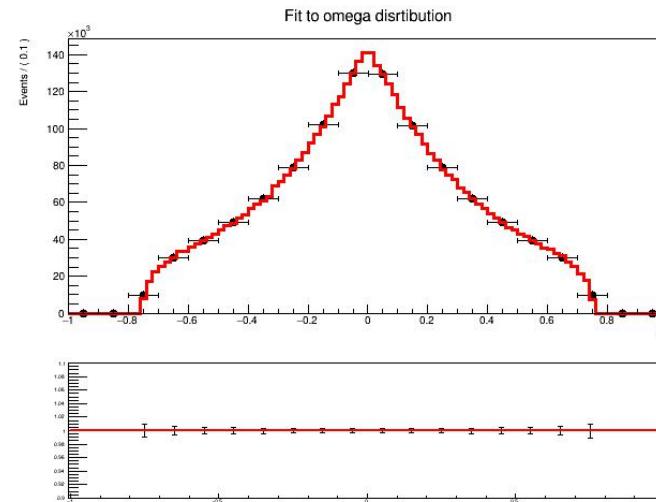
Higgs CP-mixing measurement

Fit strategy: Maximum-likelihood fit

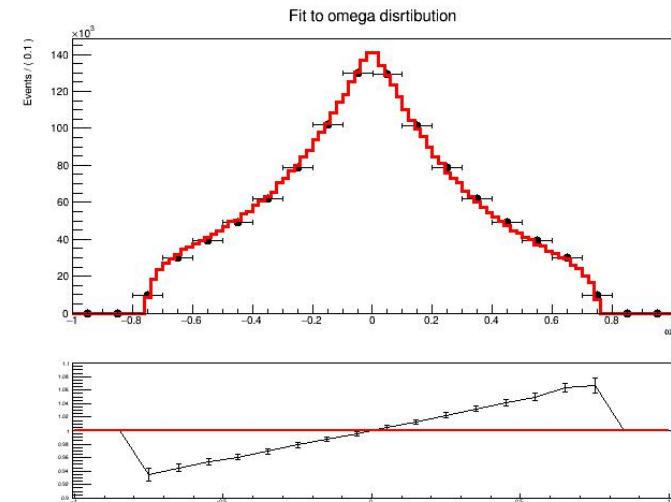
- $f^p(\omega) = N_{sig} * f_{sig}^p(\omega) + N_{bkg} * f_{bkg}^p(\omega)$
- **Fit ω to get $f_{sig}^p(\omega)$ and $f_{bkg}^p(\omega)$**
- **Fit $M_{recoil_{\mu\mu}}$ to get N_{sig} and N_{bkg}**
- Evaluate likelihood function for each p value hypothesis, and construct a ΔNLL as a function of p.



P= 0.09 compare p= 0



P= 0 compare p= 0



P= -0.09 compare p= 0

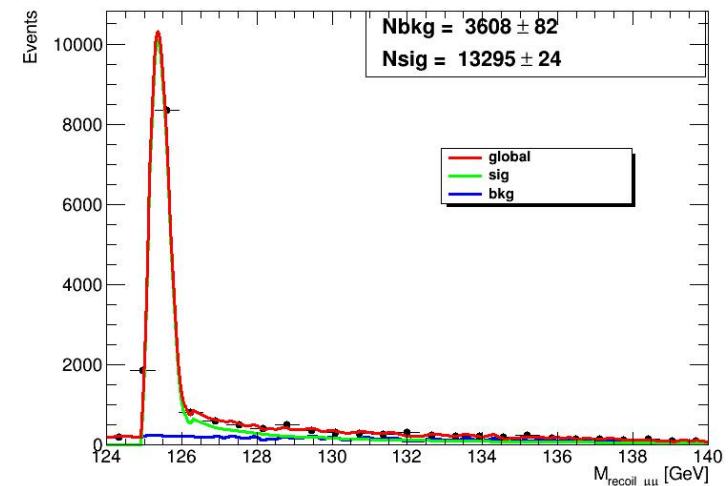
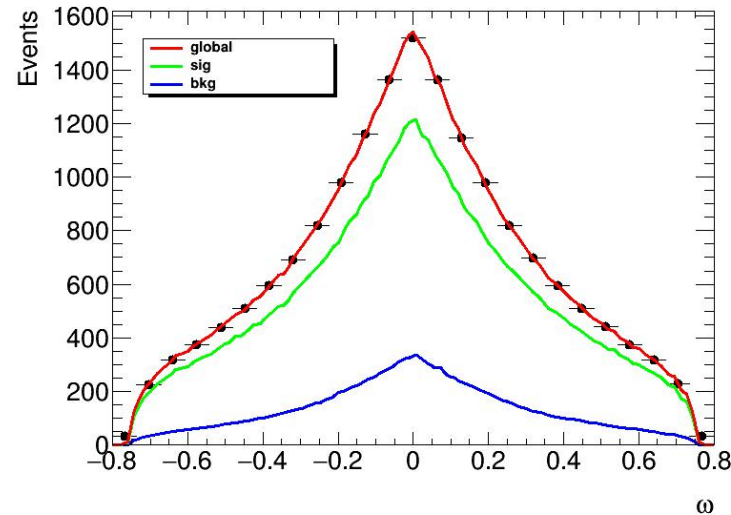
Higgs CP-mixing measurement

Fit ω :

- Use histogram pdf to fit **MC signal and background sample**.
- The red curve is global fit, the green curve is signal events, the blue curve is background events.

Fit $M_{recoil_{\mu\mu}}$:

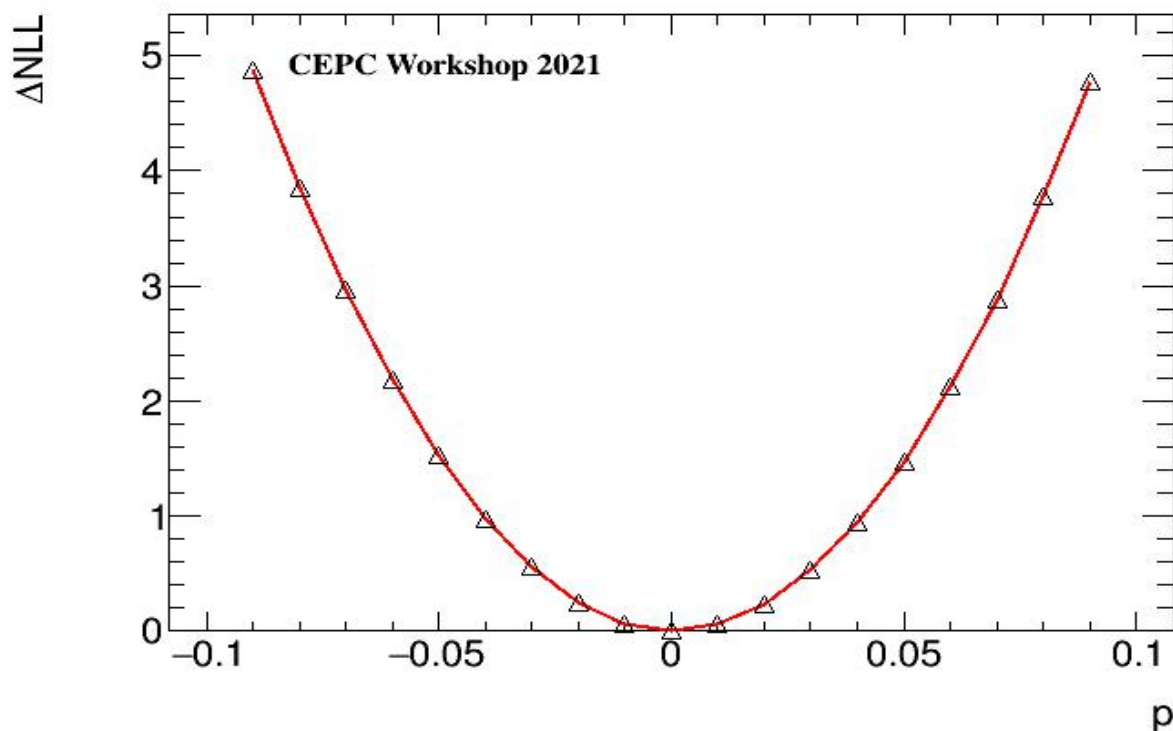
- Use histogram pdf to fit the $M_{recoil_{\mu\mu}}$ of signal (the signal is **on truth level** after **doing the smear to simulate detector error** and **considering the ISR** to simulate the small exponential tail).
- The $M_{recoil_{\mu\mu}}$ distribution of the combinatorial background (dominated by the $e^+e^- \rightarrow ZZ \rightarrow llq\bar{q}$) is modeled by a second order polynomial.



Higgs CP-mixing measurement

Extract maximum-likelihood fit p-value and interval

- Fit ΔNLL curve with a quadratic function $\Delta NLL(p) = a \cdot (p - p_0)^2$
- 68%(95%) CL interval corresponds to $\Delta NLL=0.5(1.96)$.



$$\Delta NLL(p|\omega) = 595.4(p - 4.2 \times 10^{-4})^2$$

For ω :

68% CL: $[-2.9 \times 10^{-2}, 2.9 \times 10^{-2}]$

95% CL: $[-5.7 \times 10^{-2}, 5.7 \times 10^{-2}]$

Summary

An EFT based Higgs CP-mixing test is performed.

- Set up some basic assumptions to have a simplest CP-mixing model.
- Introduced optimal variable with better performance.
- Used ML-fit in ω distribution to extract p .
- Result: 95% CL $p \in [- 5.7 \times 10^{-2}, 5.7 \times 10^{-2}]$, corresponding to $\delta G_F, \hat{\alpha}_{\phi l}^V, \hat{\alpha}_{\phi l}^A, \hat{\alpha}_{A\tilde{Z}}, \hat{\alpha}_{Z\tilde{Z}} < 10^{-5}$.

Backup

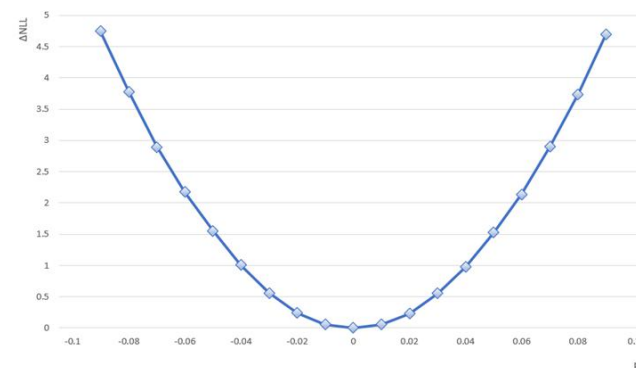
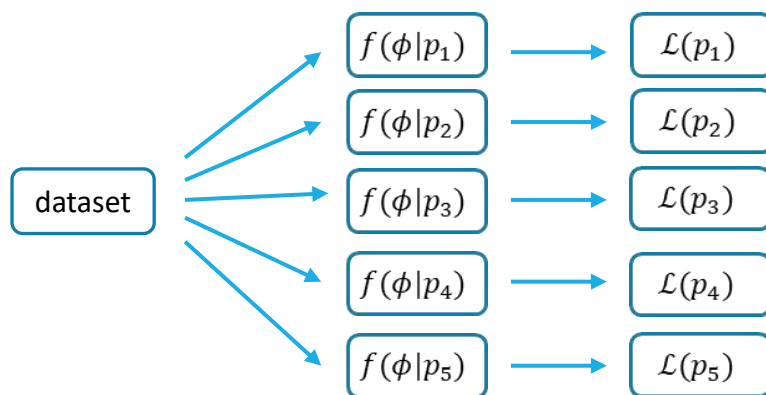
Maximum likelihood fit

Construct a likelihood function

- $\mathcal{L}(\vec{x}|p, \vec{\theta}) = \prod_{data} f(x_i | p, \vec{\theta})$

$\vec{\theta}$: nuisance parameter. p : POI, CP-mixing parameter. x_i : dataset (ω).

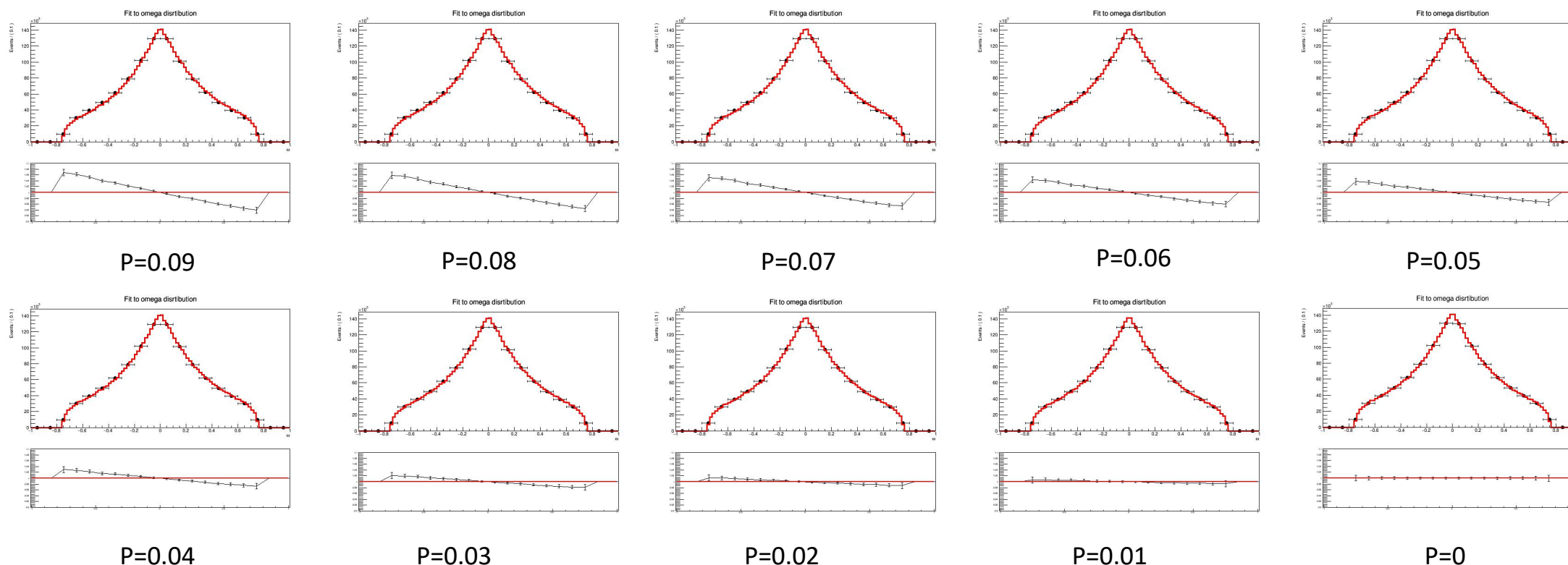
- When statistics is large enough, we suppose $\mathcal{L}(\vec{x}|p, \vec{\theta}) \sim \text{Gaus}(\hat{p}, \sigma_p^2)$, so $\ln \mathcal{L}(p) = \ln \mathcal{L}_{max} - \frac{1}{2} \left(\frac{p - \hat{p}}{\sigma_p} \right)^2$
- From $\Delta NLL = NLL - NLL_{min}$ (negative log likelihood) we can extract maximum likelihood estimate $\hat{p}$ and its CL interval.



Maximum likelihood fit

Sample modelling

- ω modelling: Histogram pdf. Highly depends on the sample statistics used to build histogram and HistPdf.



Maximum likelihood fit

Sample modelling

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