

# Recent CP violation results at the LHCb experiment

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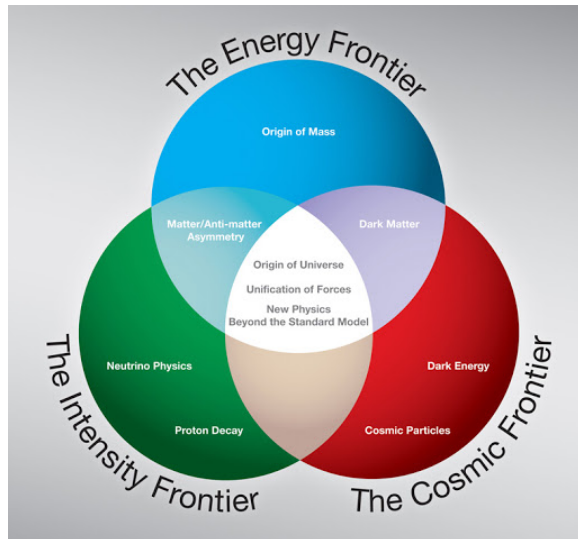
# Outline

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- **Introduction**
- **Recent highlights on CKM angle  $\gamma$  measurements**
- **Recent highlights on charmless b decays**
- **A new tool for amplitude analysis**
- **Conclusion**

# New Physics search

- All SM particles, including Higgs, have been found;
- However **new mechanism needed** for DM, matter-antimatter asymmetry, hierarchy problems etc.;
- Two ways to search for New Physics: **direct** search and **indirect** search through **precision** measurements;
- Examples in history: many beyond “current” model New Physics first found through indirect search

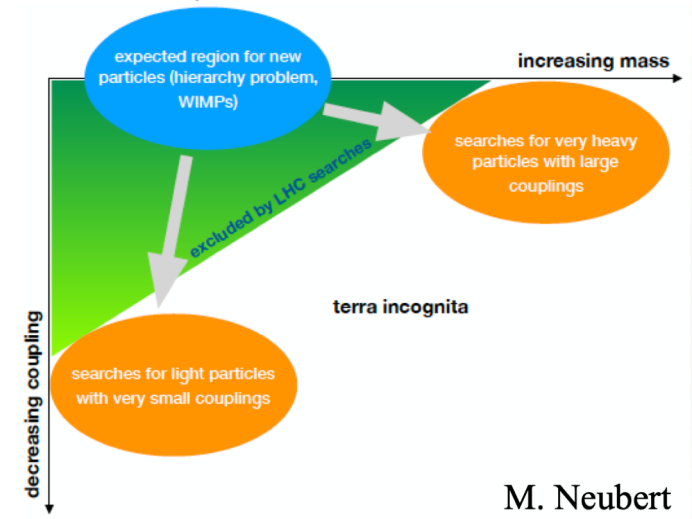
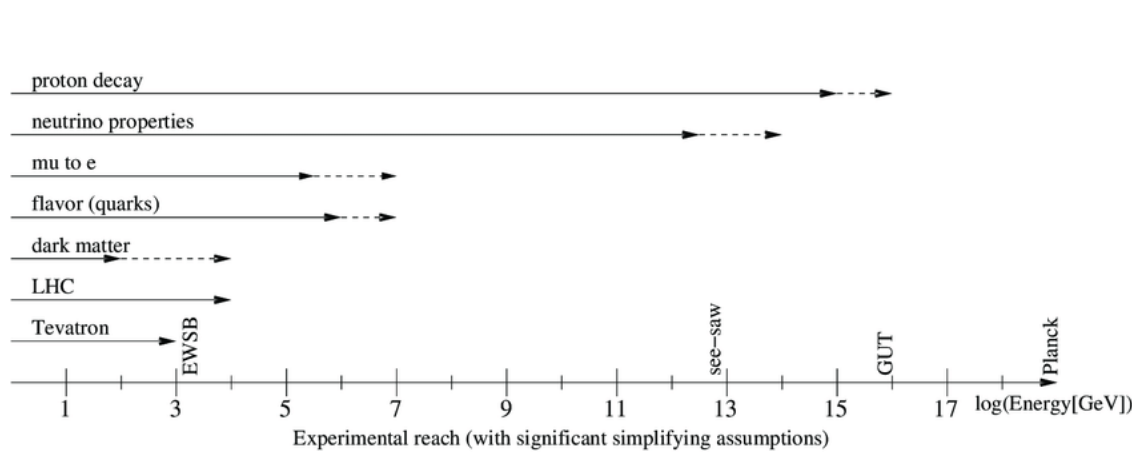


# New Physics search at flavor sector

- Sensitive to New Physics scale much **higher** than direct search: 1-10<sup>4</sup> TeV

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum \frac{c_i^{(d)}}{\Lambda^{(d-4)}} O_i^{(d)} (\text{SM fields}).$$

← Couplings  $\mathcal{O}(1)$  to avoid fine tuning



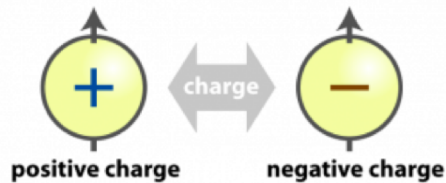
M. Neubert

- Also “tasteful”, not only can tell there is New Physics, but also tell properties of New Physics based on flavor it couples to
- Statistics or precision** is key for flavor program: New Physics scale, i.e. Dim = 6, proportional to  $\sqrt[4]{\text{statistics}}$  or  $1/\sqrt{\text{Uncertainty}}$ ,

# Fundamental questions

- If there are **new CPV mechanism** needed to explain the large matter-antimatter asymmetry observed in Universe; and what are they?

C:物质—反物质变换



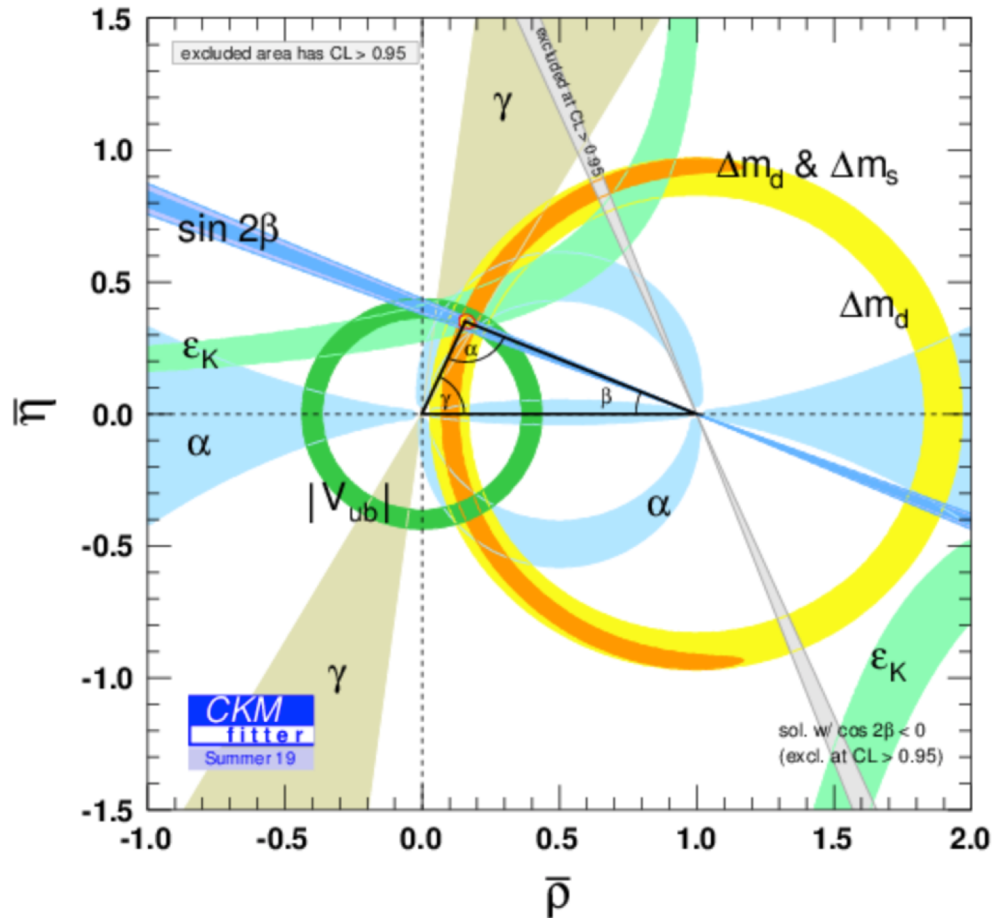
CP: 电荷共轭和宇称变换



- If there are **New Physics coupling to flavor sector**? Their energy scale and properties?

# CKM Physics

- SM CPV offered by CKM mechanism; however, **orders of magnitude smaller** than matter-antimatter asymmetry observed in Universe

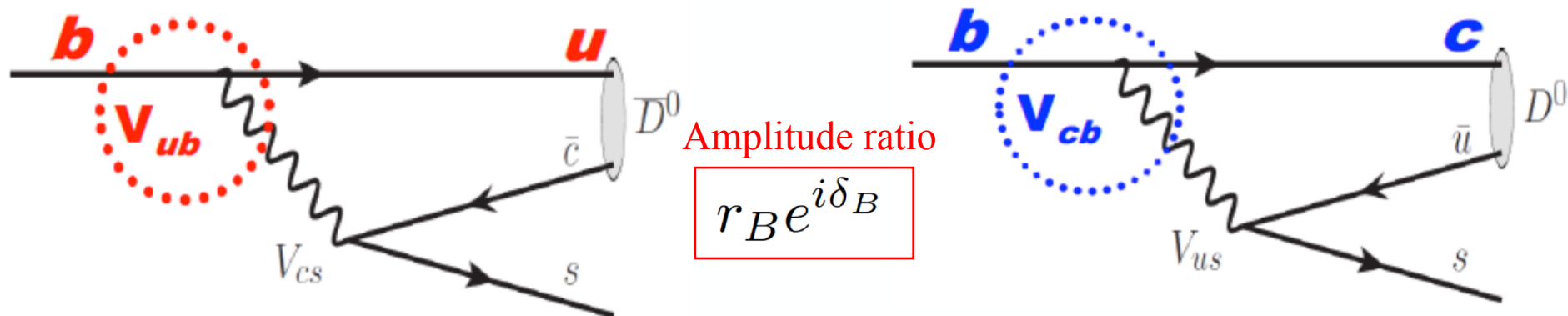


- CKM mechanism can explain what has been observed in current experiments, though still **~20%** space for New Physics; More precision needed
- Strategy:
  - SM candle:** tree level measurements such as  $\gamma$ ,  $|V_{ub}|$ ,  $|V_{cb}|$  etc.
  - New Physics search:** finding deviations in loop level processes w.r.t SM predictions

# Key parameter: angle $\gamma$

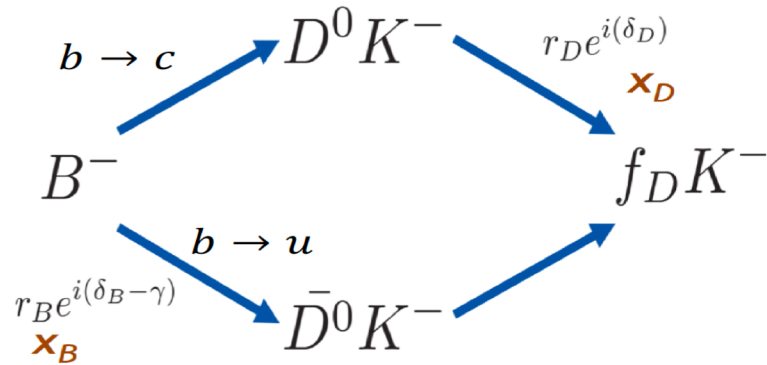
$$V_{CKM} = \begin{pmatrix} |V_{ud}| & |V_{us}| & |V_{ub}| e^{-i\gamma} \\ -|V_{cd}| & |V_{cs}| & |V_{cb}| \\ |V_{td}| e^{-i\beta} & -|V_{ts}| e^{i\beta_s} & |V_{tb}| \end{pmatrix}$$

- Angle  $\gamma$  is **the phase** response for CPV in SM, directly related to the triangle of b quarks
- Measured through  $b \rightarrow u$  and  $b \rightarrow c$  **interference** with  $B \rightarrow D^{(*)} K^{(*)}$  etc., theoretically clean



- Indirect measurements give:  $\gamma = (65.7^{+1.0}_{-2.5})^\circ$  [CKMFitter19]
- Before LHCb, precision from B-factories around  $14^\circ$

# Probe $\gamma$ in different methods



$D^0$  and  $\bar{D}^0$  decay to same final states to interference

GLW:  $D =$  CP eigenstates, e.g.  $KK, \pi\pi$

PLB 253 (1991) 483  
PLB 265 (1991) 172

ADS:  $D =$  quasi-flavour-specific states e.g.  $K\pi$

PRL 78 (1997) 3257

GGSZ:  $D =$  self-conjugate multi(3)-body states e.g.  $K_s\pi\pi$

PRD 68 (2003) 054018

GLS: ADS variant with singly Cabibbo-suppressed decay  $D \rightarrow K_s K\pi$

PRD 67 (2003) 071301

time-dependent  $B_s \rightarrow D_s K, B^0 \rightarrow D\pi$  etc

Nucl. phys. B 672 (2003) 459

Dalitz (GW) method:  $B^0 \rightarrow DK\pi$

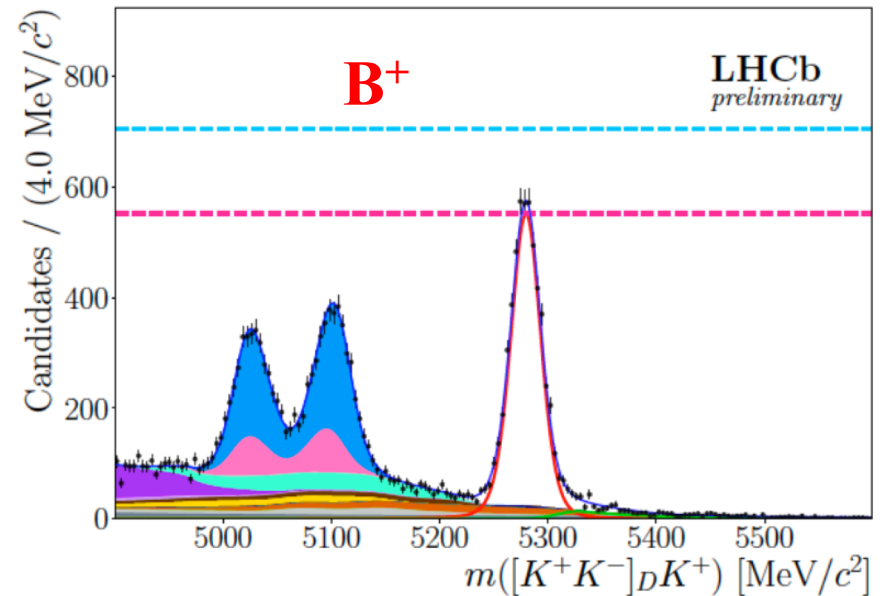
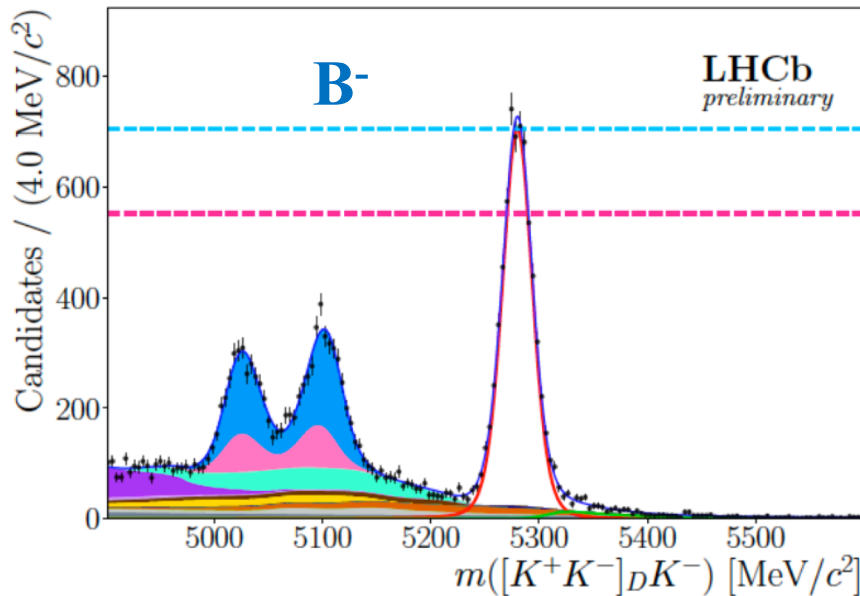
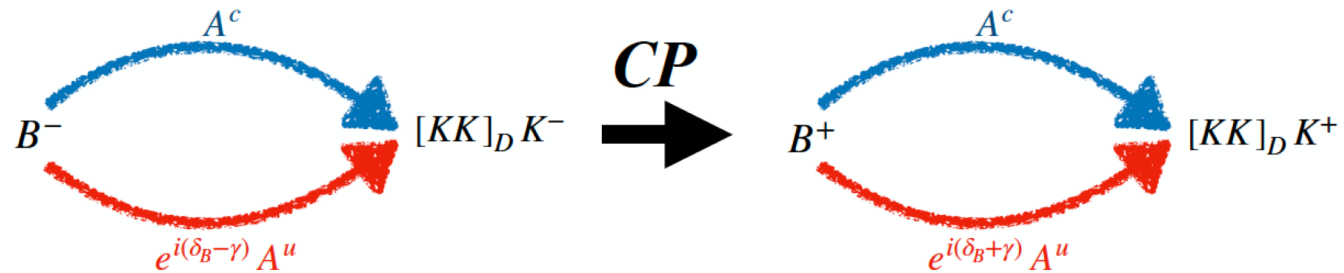
PRD 79 (2009) 051301

**Sensitivities of  $\gamma$  from many channels, important to measure as many as possible**



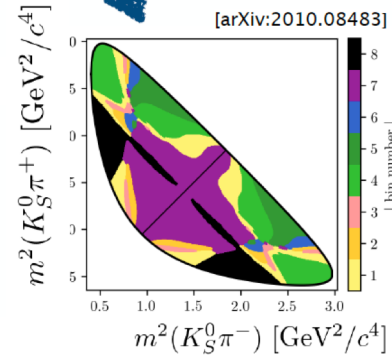
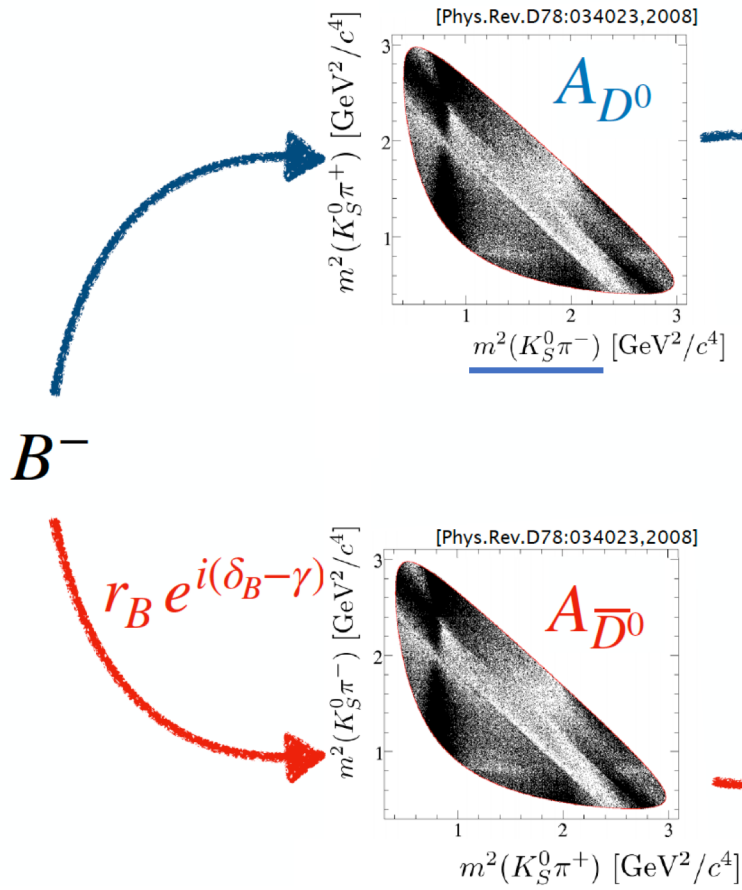
# Two-body D decays

- GLW/ADS measurements now performed with full Run1+Run2 data, for  $B \rightarrow DK, D\pi$  and partially reconstructed  $B \rightarrow D^*K, D^*\pi$



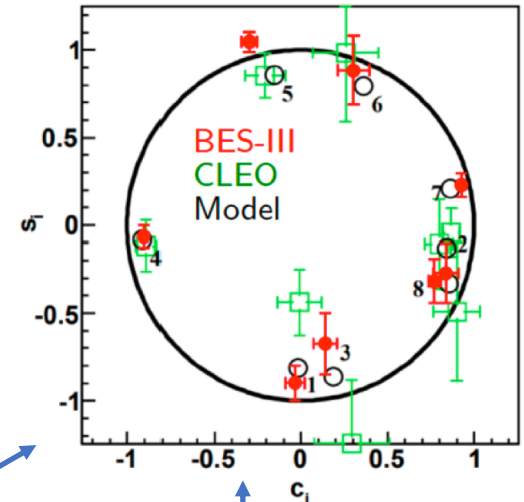
# Three-body D decays

- BPGGSZ (GLW/ADS over Dalitz plot) measurements now performed with full Run1+Run2 data, for  $B \rightarrow DK, D \rightarrow K_S\pi\pi, K_S KK$



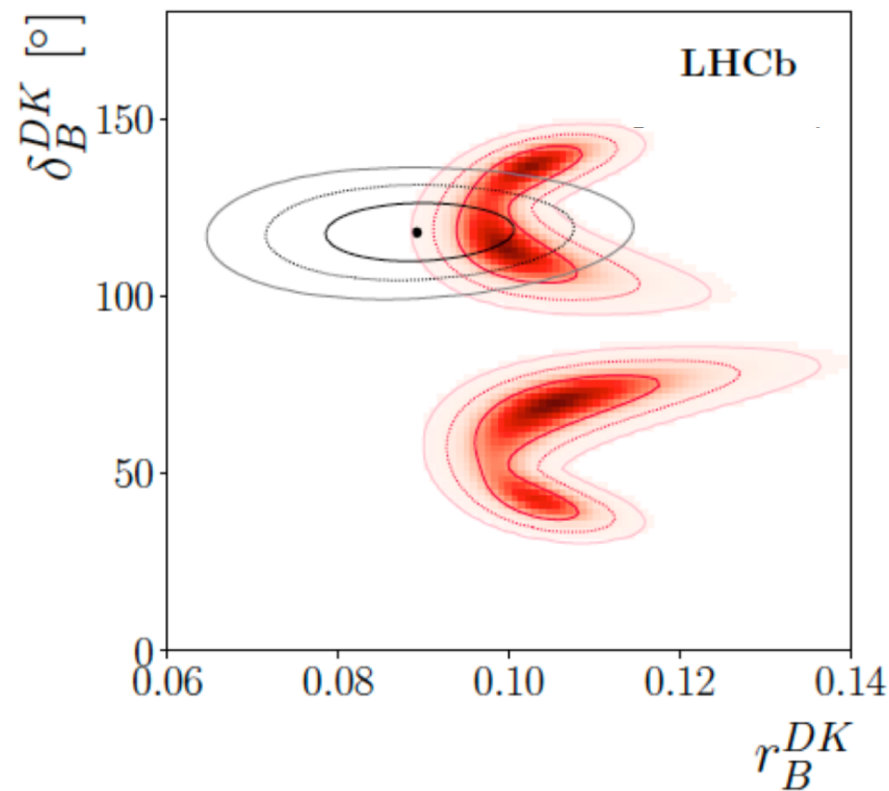
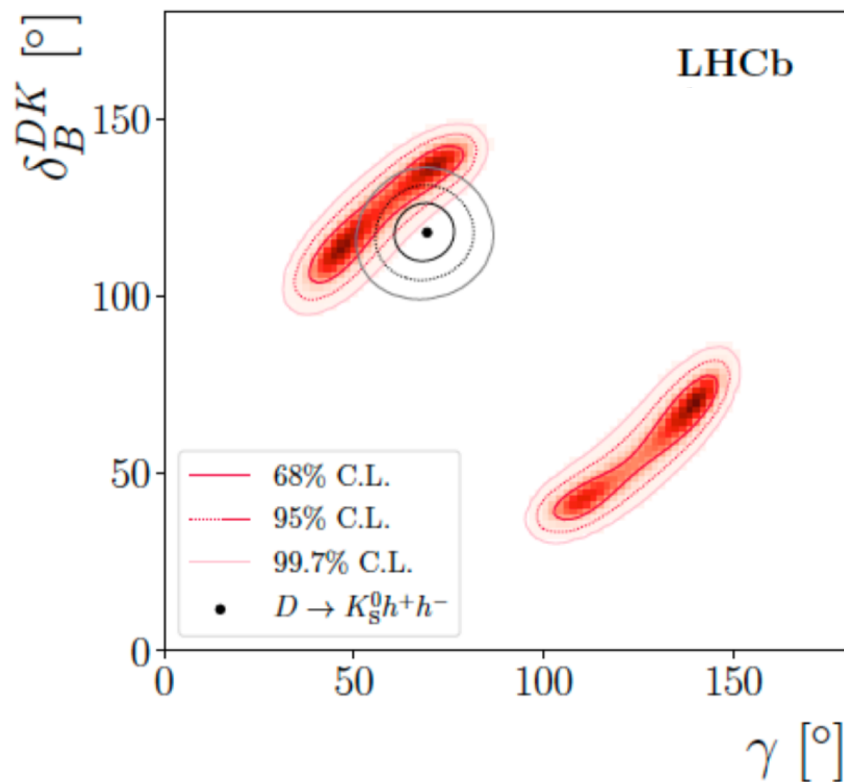
New charm input from BES-III (4 \* CLEO-c stat)

[PRD101, 112002(2020)]



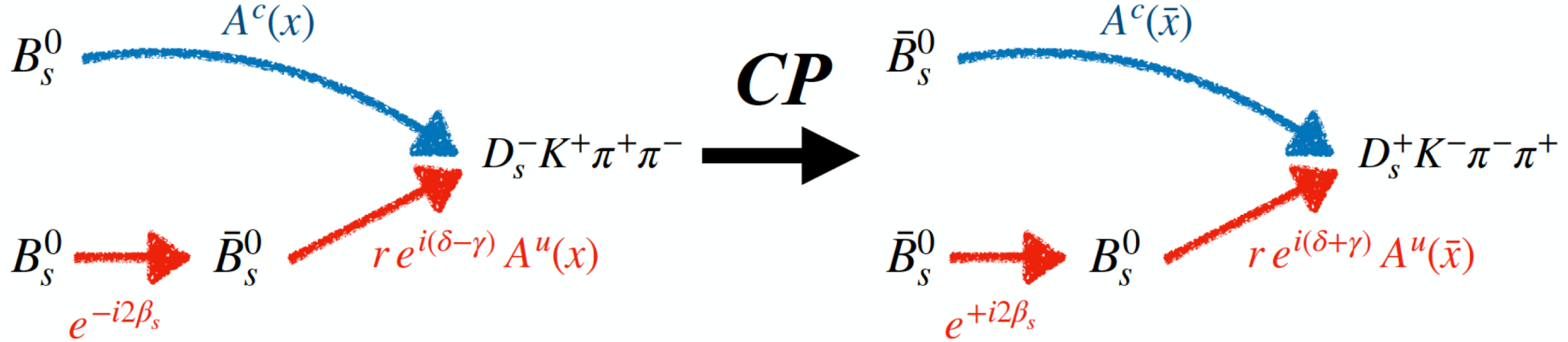
$$A_{B^\mp}(m_{K_S^0 \pi^+}^2, m_{K_S^0 \pi^-}^2) = A_{D^0}(m_{K_S^0 \pi^+}^2, m_{K_S^0 \pi^-}^2) + r_B e^{i(\delta_{B^\mp} \mp \gamma)} A_{\bar{D}^0}(m_{K_S^0 \pi^-}^2, m_{K_S^0 \pi^+}^2)$$

# Combination between the two

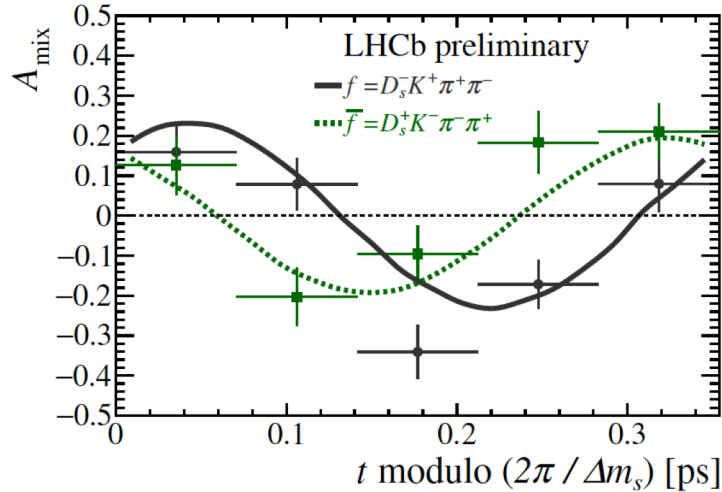


- Good agreement between the two modes (expected)
- **Much better** sensitivity **when combined** → key feature for  $\gamma$  measurements
- Important to add **more channels** and compare between them

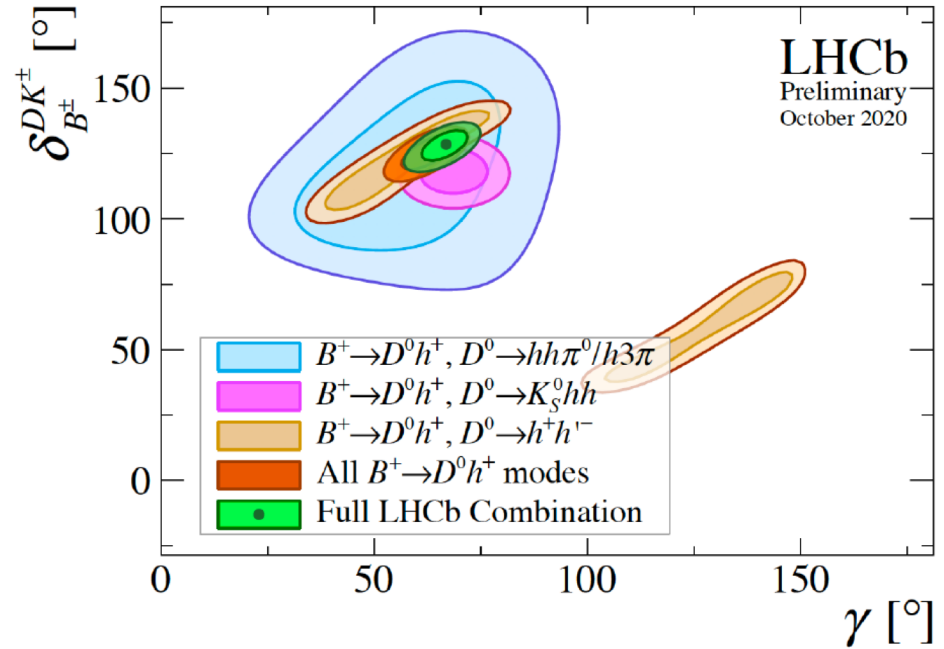
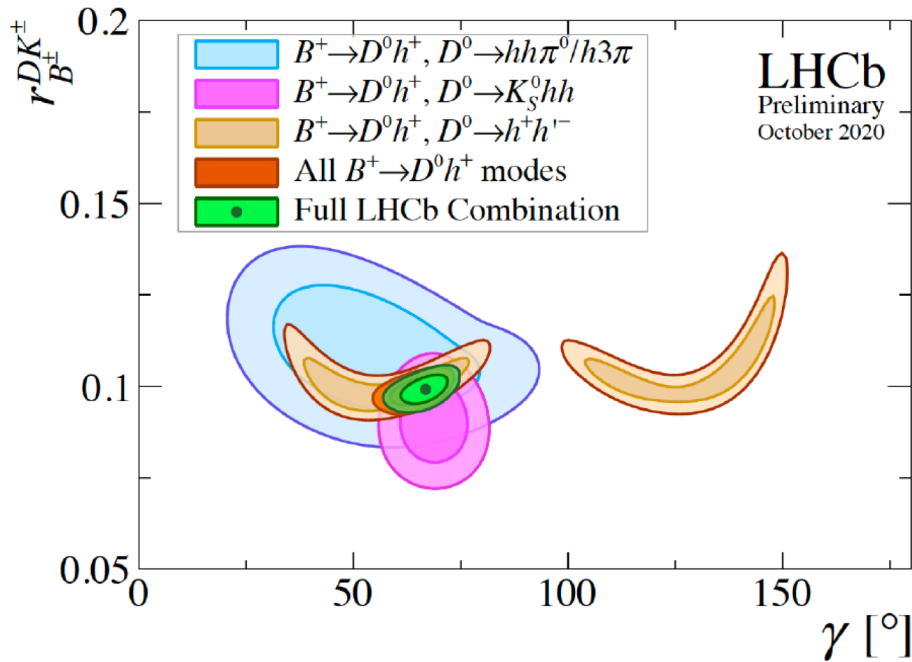
# New story from $B_s$ decays



- $b \rightarrow u$  and  $b \rightarrow c$  interference can also come with  $B_s$  mixing

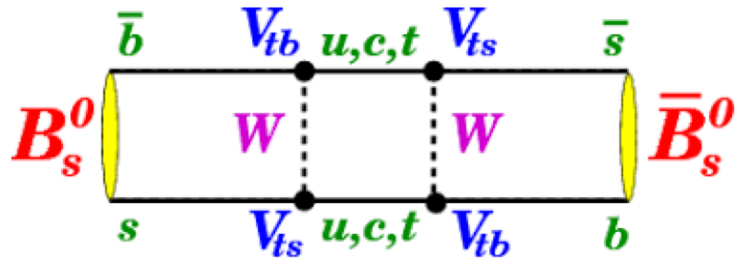


$r$	$0.56 \pm 0.05 \pm 0.04 \pm 0.07$
$\kappa$	$0.72 \pm 0.04 \pm 0.06 \pm 0.04$
$\delta [^\circ]$	$-14 \pm 10 \pm 4 \pm 5$
$\gamma - 2\beta_s [^\circ]$	$42 \pm \underbrace{10}_{\text{stat}} \pm \underbrace{4}_{\text{sys}} \pm \underbrace{5}_{\text{model}}$



- Now precision **mainly from  $B^+$  decays**, large potential from other b hadrons
- New average on  $\gamma$  from LHCb:  $\gamma = (67 \pm 4)^\circ$ , compared to  $14^\circ$  in B-factories
- Also now much closer to indirect determination:  $\gamma = (65.7_{-2.5}^{+1.0})^\circ$

# Mixing parameters



$$i \frac{d}{dt} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \begin{pmatrix} M - i\frac{\Gamma}{2} & M_{12} - i\frac{\Gamma_{12}}{2} \\ M_{12}^* - i\frac{\Gamma_{12}^*}{2} & M - i\frac{\Gamma}{2} \end{pmatrix} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

Mass eigenstates  
Heavy & Light

$$|B_H\rangle = p|B_s^0\rangle - q|\bar{B}_s^0\rangle$$

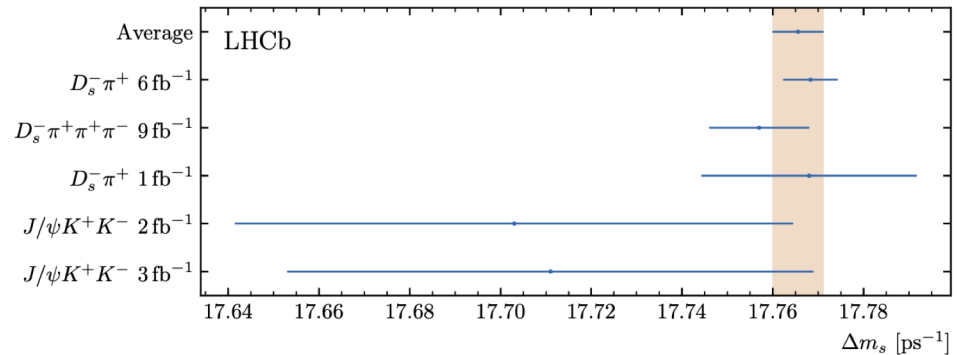
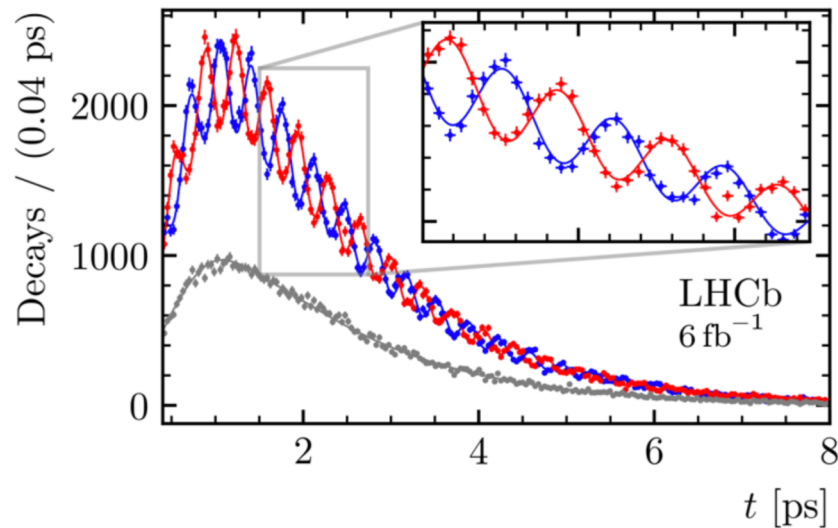
$$|B_L\rangle = p|B_s^0\rangle + q|\bar{B}_s^0\rangle$$

With  $|p|^2 + |q|^2 = 1$

Phase  $\phi_2^{SM} - \arg(-\frac{M_{12}}{\Gamma_{12}}) \approx 0.04 \text{ rad}$

- Mass eigenstates different from flavor eigenstates

—  $B_s^0 \rightarrow D_s^- \pi^+$  —  $\bar{B}_s^0 \rightarrow D_s^- \pi^+$  — Untagged



$$17.7656 \pm 0.0057 \text{ ps}^{-1}$$

- Textbook measurements, most precise to date; call for better precision on lattice parameters

# Textbook story continues

LHCb-PAPER-2020-029

2001

Beauty particles: Time-dependent  $CP$  violation in  $B^0$  meson decays  
BaBar and Belle collaborations

2004

Beauty particles: Time-integrated  $CP$  violation in  $B^0$  meson decays  
BaBar and Belle collaborations

2013

Beauty-strange particles: Time-integrated  $CP$  violation in  $B_s^0$  meson decays  
LHCb collaboration

2020

Beauty-strange particles: Time-dependent  $CP$  violation in  $B_s^0$  meson decays  
LHCb collaboration

1964

Strange particles:  $CP$  violation in  $K$  meson decays  
J. W. Cronin, V. L. Fitch *et al.*

1999, 2001

Strange particles:  $CP$  violation in decay  
KTeV and NA48 collaborations

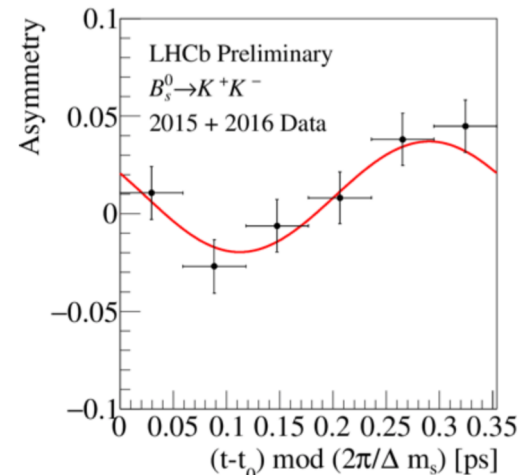
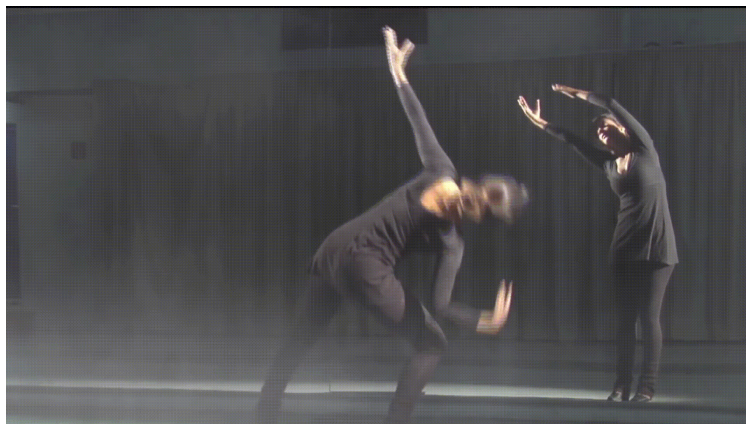
2012

Beauty particles:  $CP$  violation in  $B^+$  meson decays  
LHCb collaboration

2019

Charm particles:  $CP$  violation in  $D^0$  meson decays  
LHCb collaboration

**TODAY**

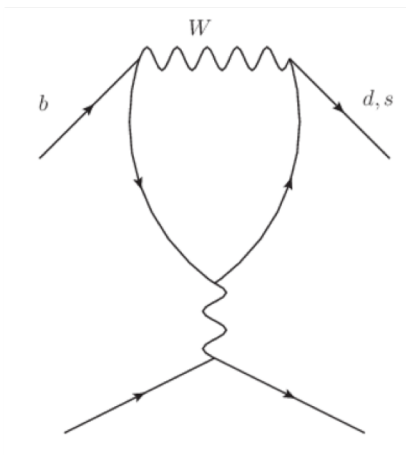


**A first discovery of time-dependent  $CP$  violation in  $B_s^0$  decays**

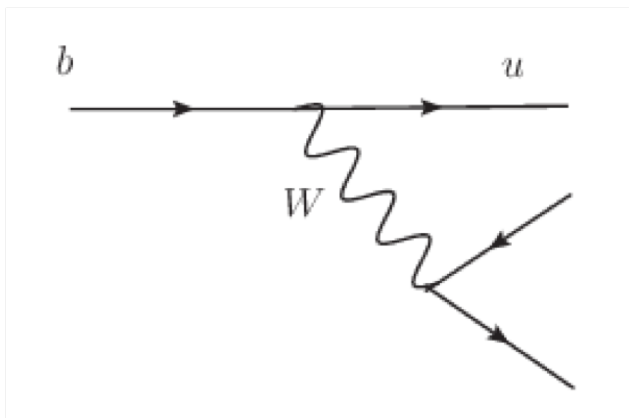
# Looking for new physics in penguins

- Not only from global fit, but also from new physics sensitive channels
- New sources of CP violation easy to enter in penguins: smoking gun for NP search
- Competitive contributions from tree and penguin diagrams:

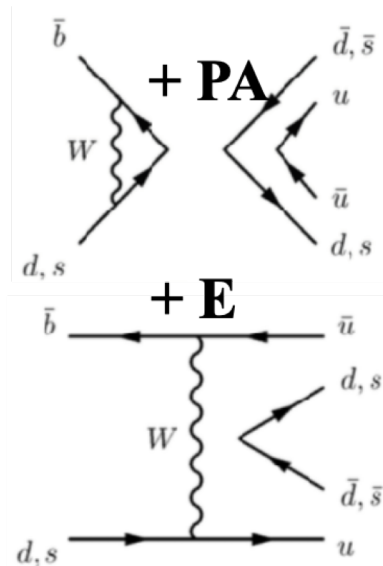
large CPV



$$|V_{td}|e^{i\beta} \quad \text{or} \quad -|V_{ts}|e^{-i\beta_s}$$



$$|V_{ub}|e^{-i\gamma}$$



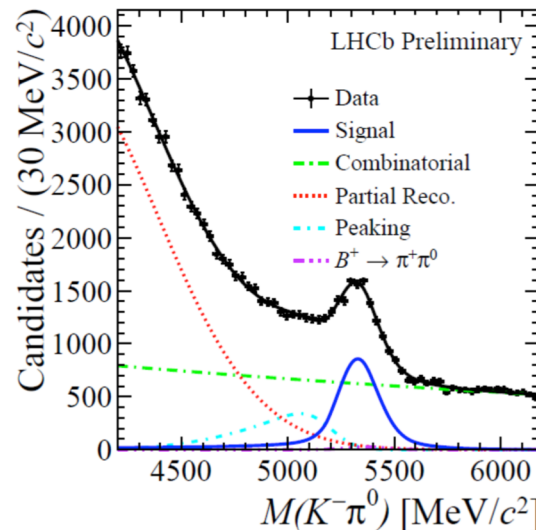
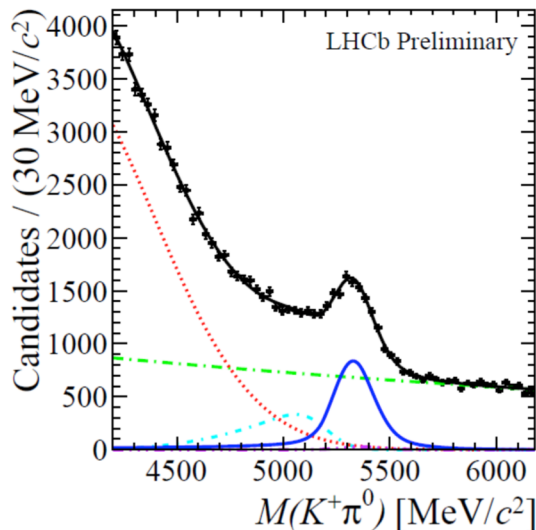
**+ New Physics**



# $K\pi$ puzzle

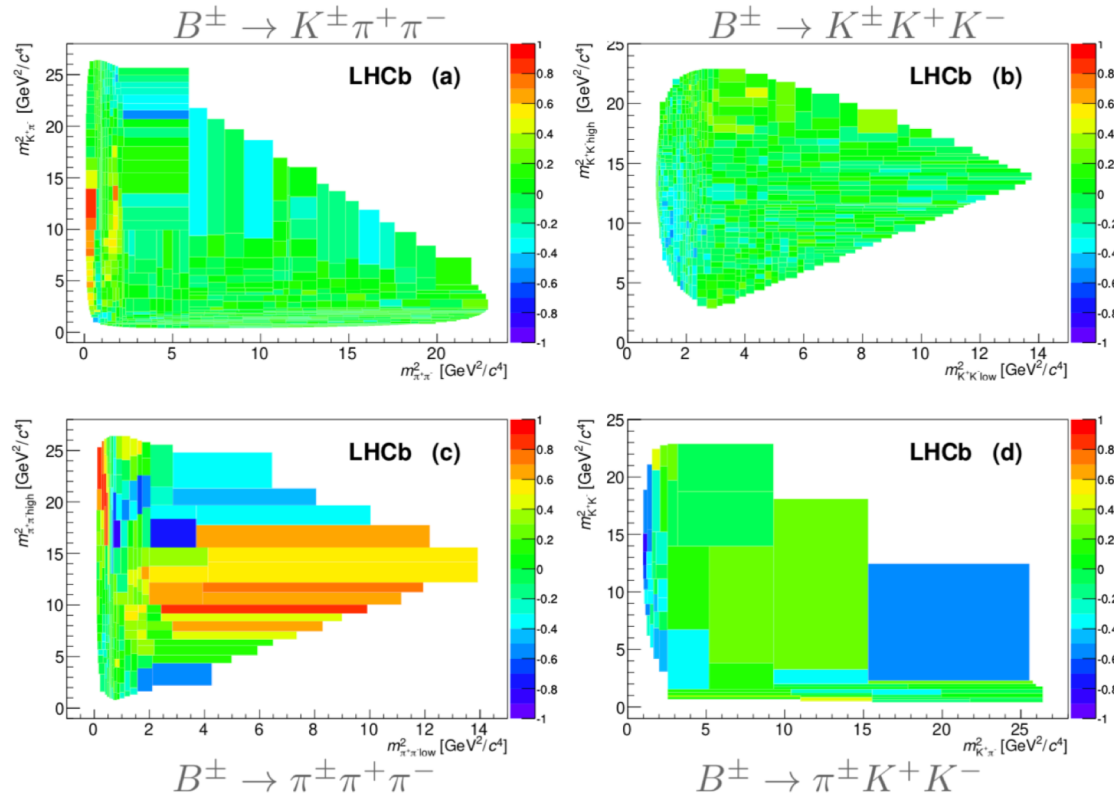
- CPV from interference between suppressed tree-level process and QCD/EW penguin is sensitive for New Physics,  $K\pi$  puzzle as an example [LHCb-PAPER-2020-040]
- Simple version of  $K\pi$  puzzle: Isospin violated as  $A_{CP}(B^+ \rightarrow K^+\pi^0) - A_{CP}(B^0 \rightarrow K^+\pi^-) = 0.122 \pm 0.022$  (HFLAV); More complicated version involves full analysis of  $K\pi$  system and tension also found inside.

$$A_{CP}(K^+\pi^-) + A_{CP}(K^0\pi^+) \frac{B(K^0\pi^+) \tau_0}{B(K^+\pi^-) \tau_+} = A_{CP}(K^+\pi^0) \frac{2B(K^+\pi^0) \tau_0}{B(K^+\pi^-) \tau_+} + A_{CP}(K^0\pi^0) \frac{2B(K^0\pi^0)}{B(K^+\pi^-)}$$



- Very difficult measurements in hadron colliders
- $$A_{CP}(B^+ \rightarrow K^+\pi^0) = 0.025 \pm 0.015(\text{stat.}) \pm 0.006(\text{syst.}) \pm 0.003(\text{ext.})$$
- Strengthen the  $K\pi$  puzzling and motivate further investigation in  $B^0 \rightarrow K^0\pi^0$

- Interesting CPV pattern seen on Dalitz plot of  $B^+ \rightarrow h^+ h^- h'^+, h^{(\prime)} = K, \pi$
- Dalitz plot analysis needed to shed more light on understanding nature of these CPV



- Now, amplitude analyses of  $B^+ \rightarrow \pi^+ \pi^- \pi^+$  and  $B^+ \rightarrow K^+ K^- \pi^+$ , with much larger statistics than previous B-factory analyses, has been performed

# Dalitz plot analyses with CP violation

- Amplitude with CPV is modelled as

$$A(\Phi_3) = \sum_i A_i(\Phi_3) = \sum_i c_i F_i(\Phi_3) \quad \text{Strong dynamics}$$
$$\bar{A}(\bar{\Phi}_3) = \sum_i \bar{c}_i F_i(\Phi_3) \quad \text{Strong + weak}$$

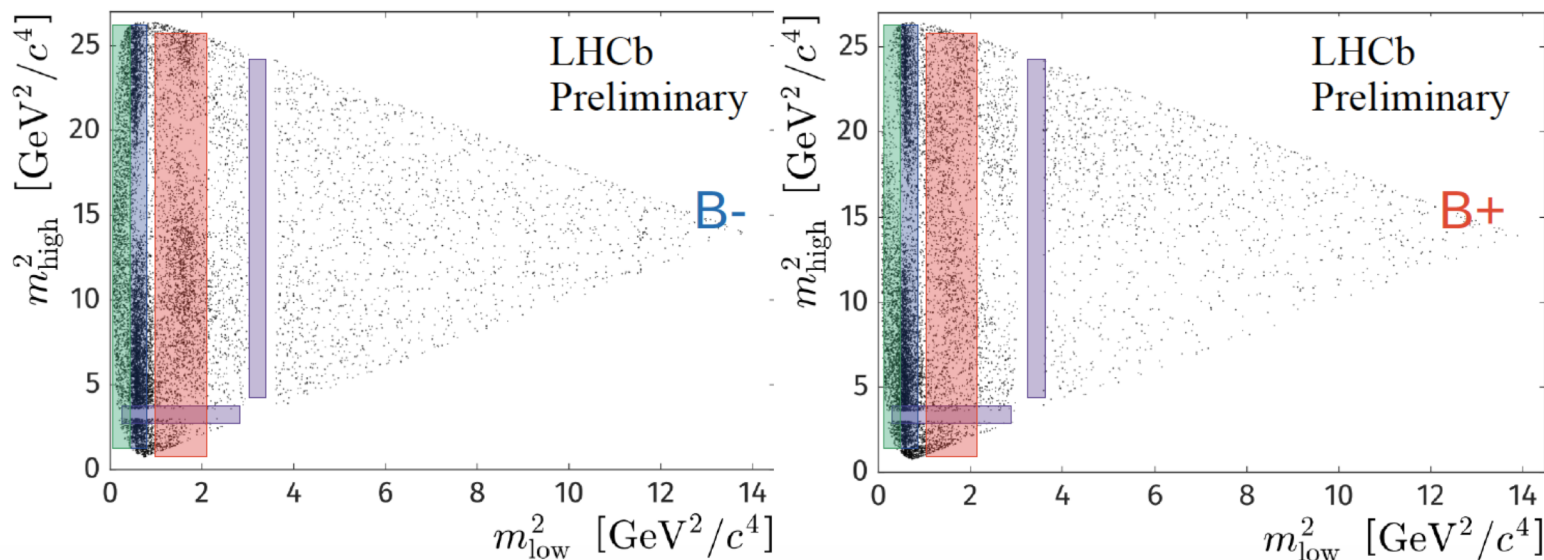
- CPV then described as

$$c_i = (x_i + \Delta x_i) + i(y_i + \Delta y_i)$$
$$\bar{c}_i = (x_i - \Delta x_i) + i(y_i - \Delta y_i)$$

- Observables:

$$\mathcal{F}_i \equiv \frac{\int d\Phi_3 |A_i(\Phi_3)|^2 + \int d\Phi_3 |\bar{A}_i(\Phi_3)|^2}{\int d\Phi_3 |A(\Phi_3)|^2 + \int d\Phi_3 |\bar{A}(\Phi_3)|^2} \quad \mathcal{A}_{CP}^i \equiv \frac{\int d\Phi_3 |\bar{A}_i(\Phi_3)|^2 - \int d\Phi_3 |A_i(\Phi_3)|^2}{\int d\Phi_3 |\bar{A}_i(\Phi_3)|^2 + \int d\Phi_3 |A_i(\Phi_3)|^2}$$

- Dalitz plot analysis with  $20594 \pm 1569$  events (3 fb<sup>-1</sup> data)



- Resonant contributions:

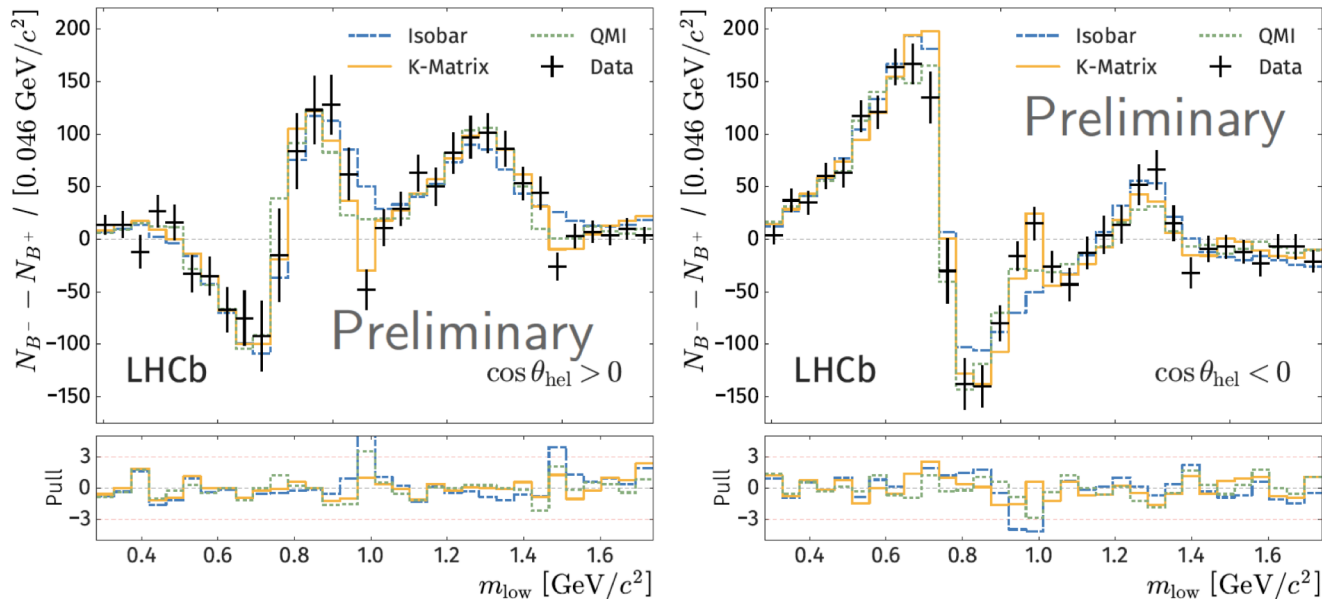
$\rho - \omega, f_0(500), f_0(980)$ , region: S-P wave interference

$f_2(1270)$  region: D-S, P wave interference

High mass:  $KK - \pi\pi$  rescattering

- Three different methods to describe S-wave: Isobar model, K-Matrix approach, quasi model independent approach

- CP violation around  $\rho(770)$  pole well described by the three S-wave models



- Over  $25\sigma$  significance for CPV due to S-P interference, first observation
- CP violation sign flips around  $\rho(770)$  pole and over helicity angle

# Sign of CP violation

- CPV comes from interference of two processes:

$$A = a_1 e^{i(\delta_1 + \phi_1)} + a_2 e^{i(\delta_2 + \phi_2)} \quad \bar{A} = a_1 e^{i(\delta_1 - \phi_1)} + a_2 e^{i(\delta_2 - \phi_2)}$$

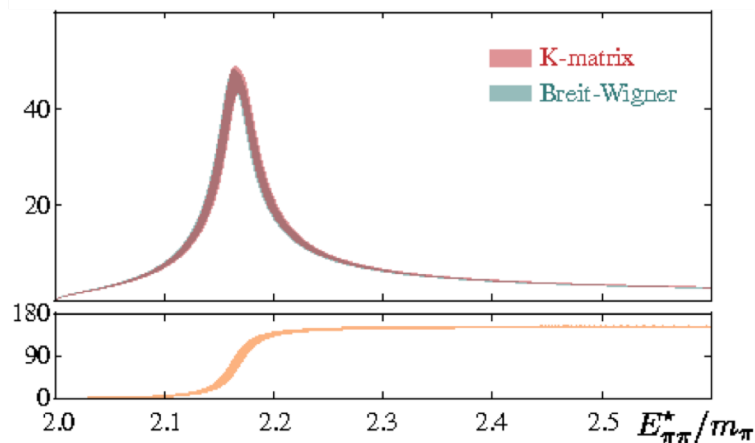
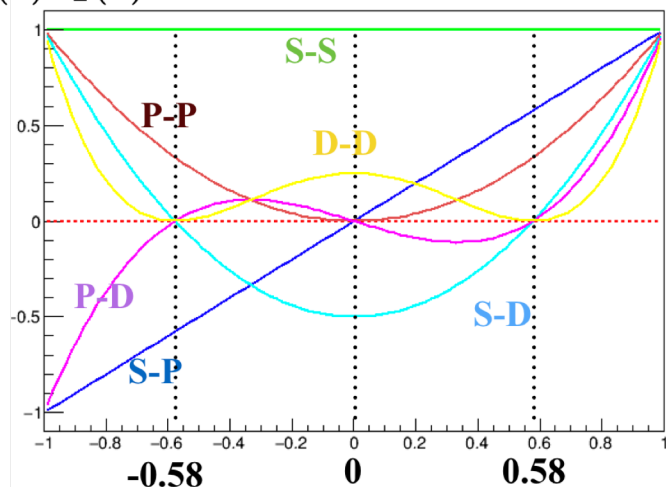
$$A_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} \propto \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

- Weak phases change sign under CP operation while strong phases don't

$$A_{CP} = \frac{|A|^2 - |\bar{A}|^2}{|A|^2 + |\bar{A}|^2} = \frac{2a_1 a_2 h_1(\theta) h_2(\theta) \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)}{a_1^2 h_1^2(\theta) + a_2^2 h_2^2(\theta) + 2a_1 a_2 h_1(\theta) h_2(\theta) \cos(\delta_1 - \delta_2) \cos(\phi_1 - \phi_2)}$$

$\theta$  : helicity angle       $h(\theta)$  : angular distribution of resonance

$h_1(\theta)h_2(\theta)$



## A **general** and **user-friendly** partial wave analysis framework

Hao Cai<sup>1</sup>, Chen Chen<sup>5</sup>, **Yi Jiang<sup>2</sup>**, Pei-Rong Li<sup>3</sup>, **Yin-Rui Liu<sup>2</sup>**, Xiao-Rui Lyu<sup>2</sup>,  
Rong-Gang Ping<sup>4</sup>, Wenbin Qian<sup>2</sup>, Mengzhen Wang<sup>5</sup>, Zi-Yi Wang<sup>2</sup>,  
Liming Zhang<sup>5</sup>, Yang-Heng Zheng<sup>2</sup>

<sup>1</sup>WHU, <sup>2</sup>UCAS, <sup>3</sup>LZU, <sup>4</sup>IHEP, <sup>5</sup>THU

- **Several independent fitters developed previously for dedicated analyses: e.g.  $Z(4430)^+$  and pentaquark search,  $B^0 \rightarrow \bar{D}^0 \pi^+ \pi^-$  analysis etc.**
- **Joint efforts + experience on previous analyses + very good students**

# Features

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- Based on Tensor-Flow v2

- Fast

- GPU based
- Vectorized calculation
- Automatic differentiation

- **General**

- Custom model available

- Easy to use

- Simple configuration file
- Automatics process
- All necessary functions implemented

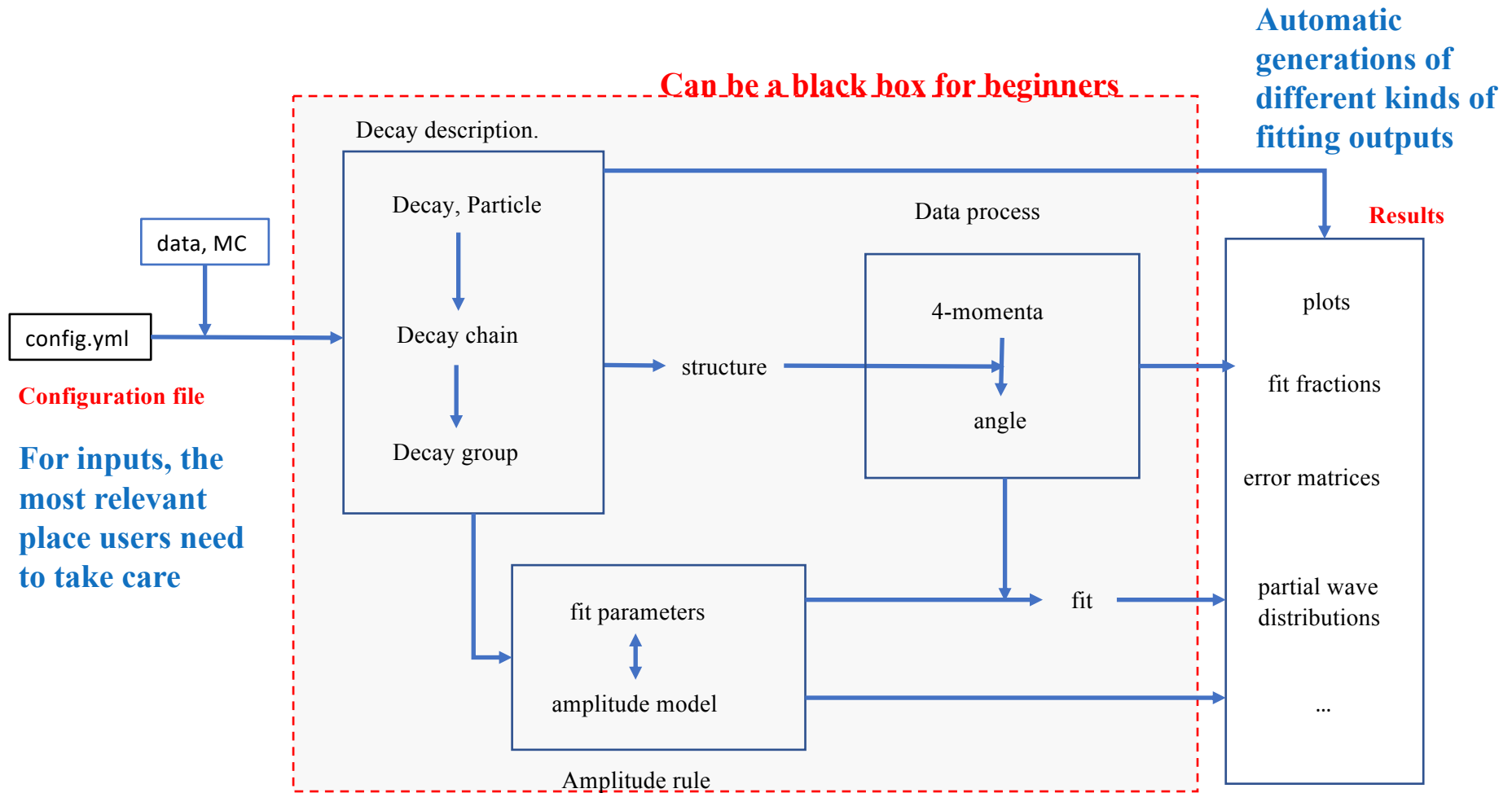
- **Open access and well supported**

<https://gitlab.com/jiangyi15/tf-pwa>

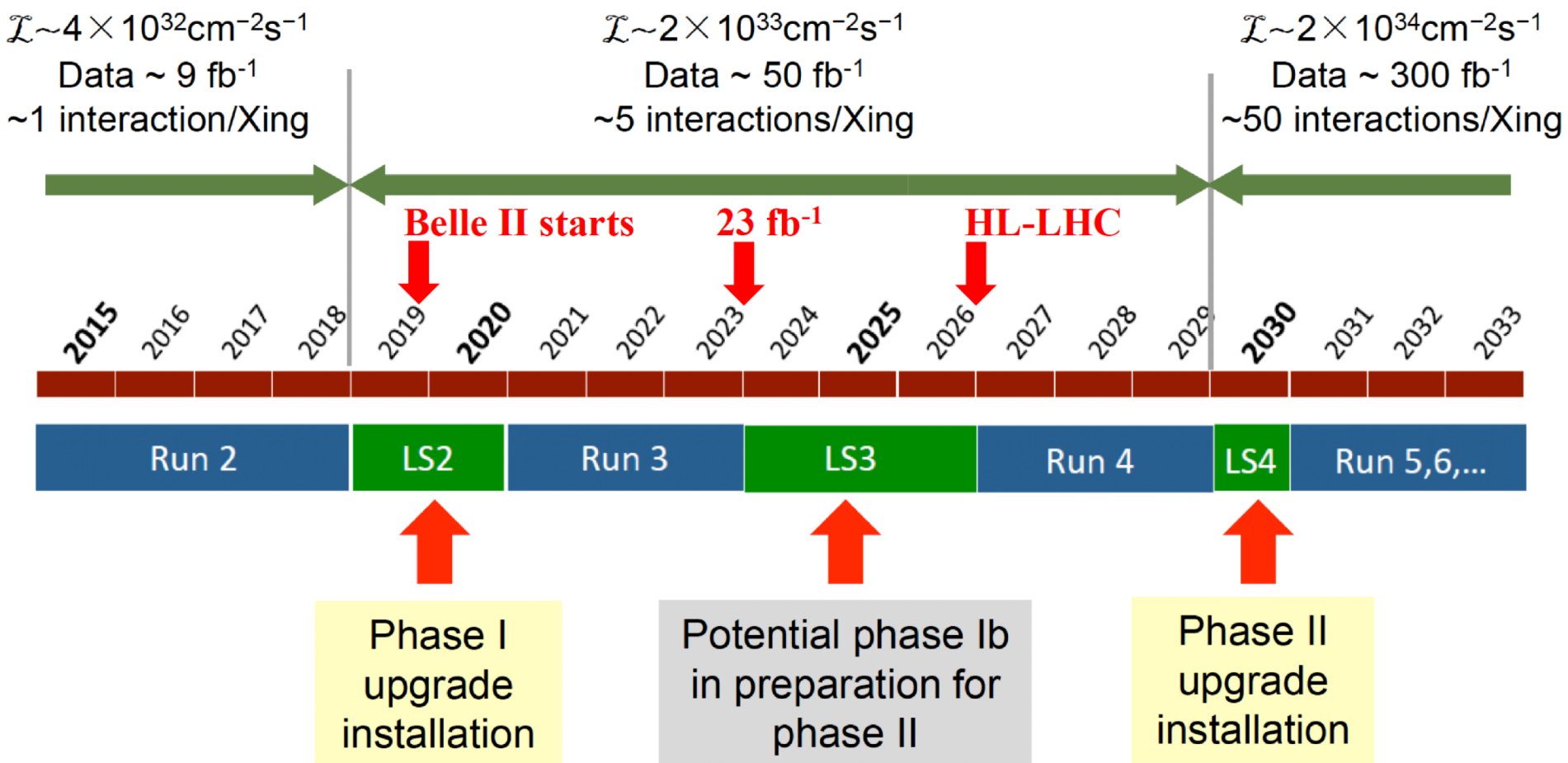




# Framework



# The LHCb upgrade plans

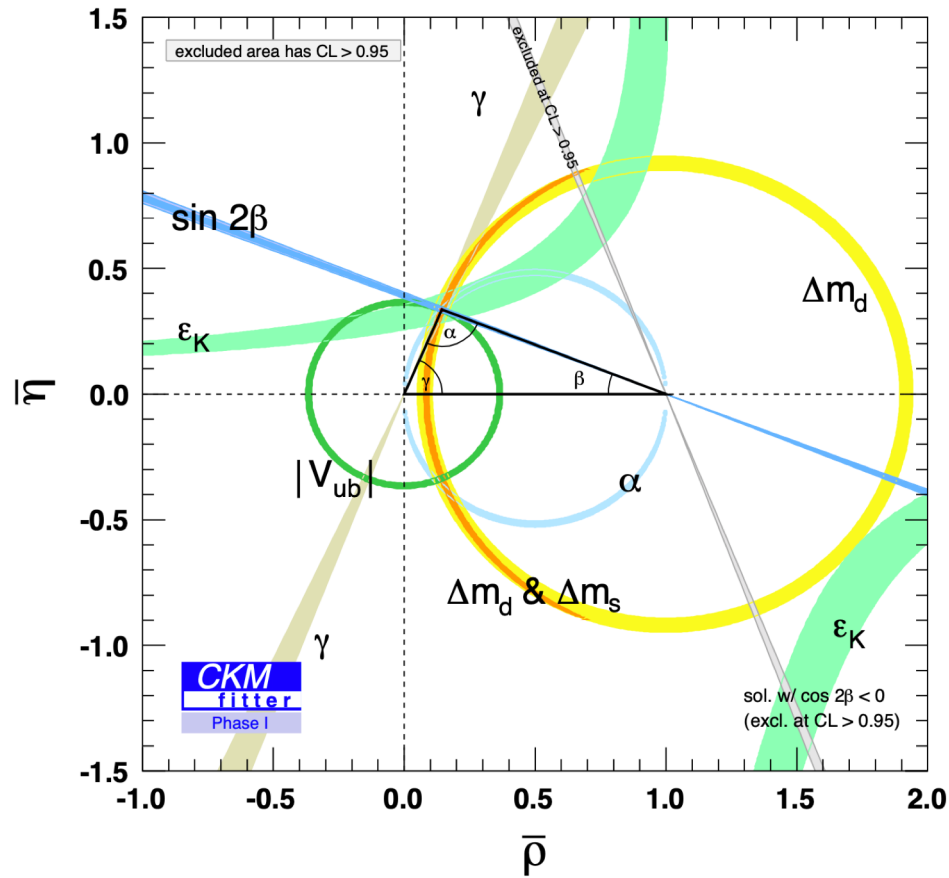


# Physics potential for LHCb upgrade

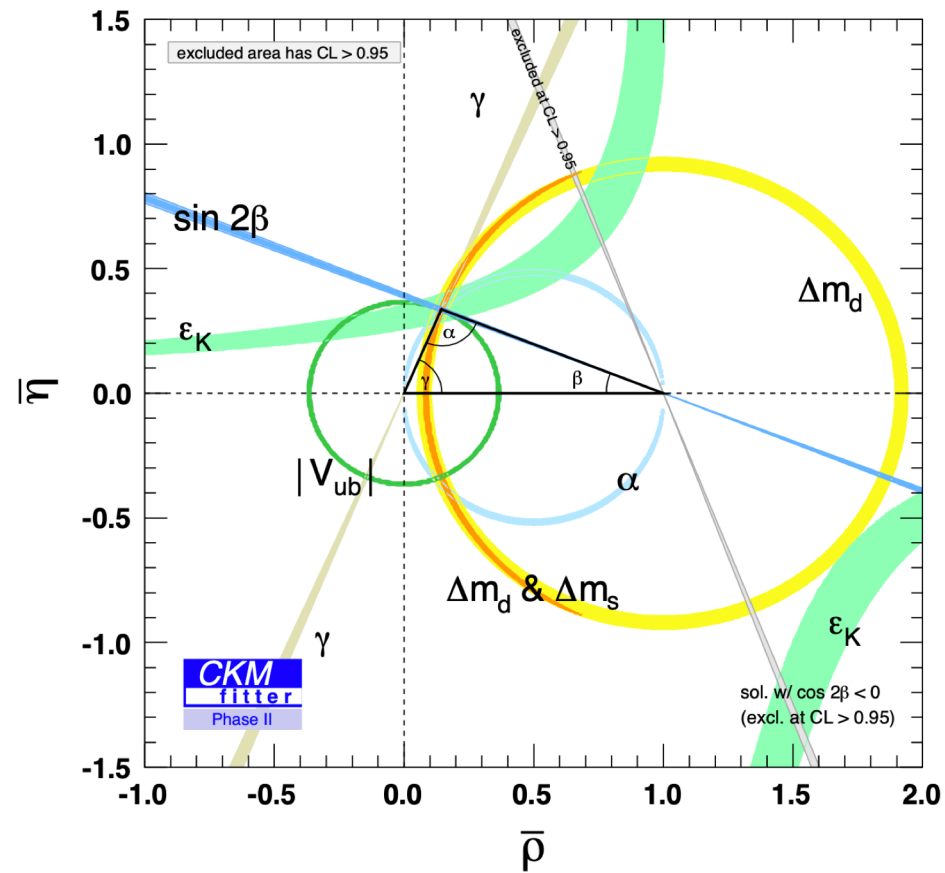
Observable	Current LHCb	LHCb 2025	Belle II	Upgrade II	ATLAS & CMS
<b>EW Penguins</b>					
$R_K (1 < q^2 < 6 \text{ GeV}^2 c^4)$	0.1 [274]	0.025	0.036	0.007	–
$R_{K^*} (1 < q^2 < 6 \text{ GeV}^2 c^4)$	0.1 [275]	0.031	0.032	0.008	–
$R_\phi, R_{pK}, R_\pi$	–	0.08, 0.06, 0.18	–	0.02, 0.02, 0.05	–
<b>CKM tests</b>					
$\gamma$ , with $B_s^0 \rightarrow D_s^+ K^-$	$(_{-22}^{+17})^\circ$ [136]	$4^\circ$	–	$1^\circ$	–
$\gamma$ , all modes	$(_{-5.8}^{+5.0})^\circ$ [167]	$1.5^\circ$	$1.5^\circ$	$0.35^\circ$	–
$\sin 2\beta$ , with $B^0 \rightarrow J/\psi K_S^0$	0.04 [609]	0.011	0.005	0.003	–
$\phi_s$ , with $B_s^0 \rightarrow J/\psi \phi$	49 mrad [44]	14 mrad	–	4 mrad	22 mrad [610]
$\phi_s$ , with $B_s^0 \rightarrow D_s^+ D_s^-$	170 mrad [49]	35 mrad	–	9 mrad	–
$\phi_s^{s\bar{s}}$ , with $B_s^0 \rightarrow \phi \phi$	154 mrad [94]	39 mrad	–	11 mrad	Under study [611]
$a_{sl}^s$	$33 \times 10^{-4}$ [211]	$10 \times 10^{-4}$	–	$3 \times 10^{-4}$	–
$ V_{ub} / V_{cb} $	6% [201]	3%	1%	1%	–
<b><math>B_s^0, B^0 \rightarrow \mu^+ \mu^-</math></b>					
$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	90% [264]	34%	–	10%	21% [612]
$\tau_{B_s^0 \rightarrow \mu^+ \mu^-}$	22% [264]	8%	–	2%	–
$S_{\mu\mu}$	–	–	–	0.2	–
<b><math>b \rightarrow c \ell^- \bar{\nu}_\ell</math> LUV studies</b>					
$R(D^*)$	0.026 [215, 217]	0.0072	0.005	0.002	–
$R(J/\psi)$	0.24 [220]	0.071	–	0.02	–
<b>Charm</b>					
$\Delta A_{CP}(KK - \pi\pi)$	$8.5 \times 10^{-4}$ [613]	$1.7 \times 10^{-4}$	$5.4 \times 10^{-4}$	$3.0 \times 10^{-5}$	–
$A_\Gamma (\approx x \sin \phi)$	$2.8 \times 10^{-4}$ [240]	$4.3 \times 10^{-5}$	$3.5 \times 10^{-4}$	$1.0 \times 10^{-5}$	–
$x \sin \phi$ from $D^0 \rightarrow K^+ \pi^-$	$13 \times 10^{-4}$ [228]	$3.2 \times 10^{-4}$	$4.6 \times 10^{-4}$	$8.0 \times 10^{-5}$	–
$x \sin \phi$ from multibody decays	–	( $K3\pi$ ) $4.0 \times 10^{-5}$	( $K_S^0 \pi\pi$ ) $1.2 \times 10^{-4}$	( $K3\pi$ ) $8.0 \times 10^{-6}$	–

# CKM triangles in two decades

**Phase I**



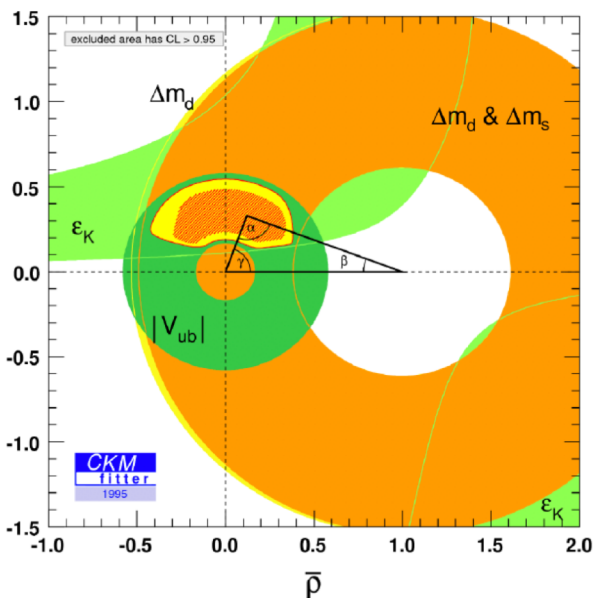
**Phase II**



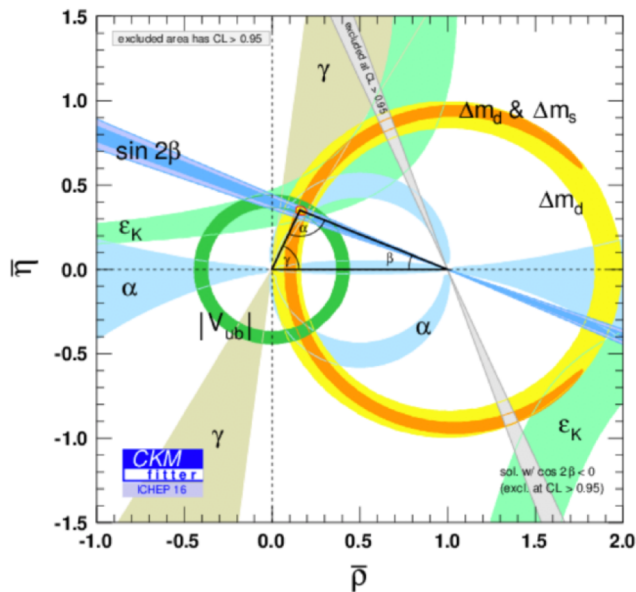
- With assumptions on improvements on lattice plus measurements from Belle II
- Central values at current fit values

# Conclusion

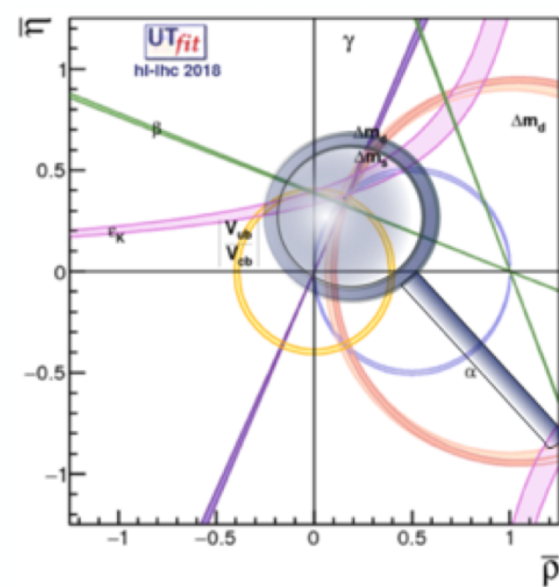
1995



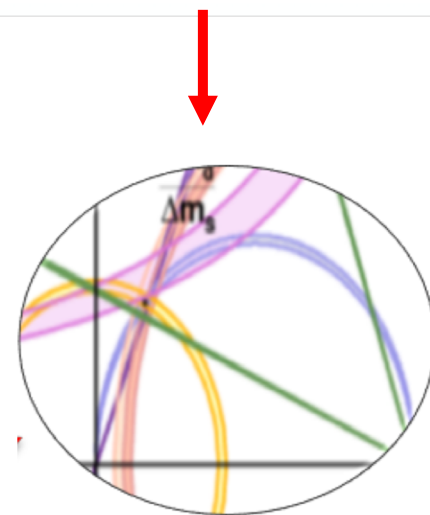
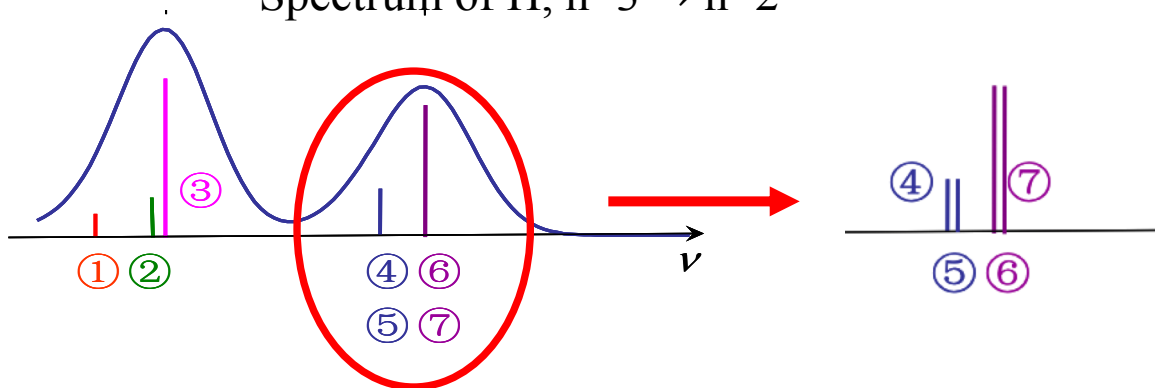
2016

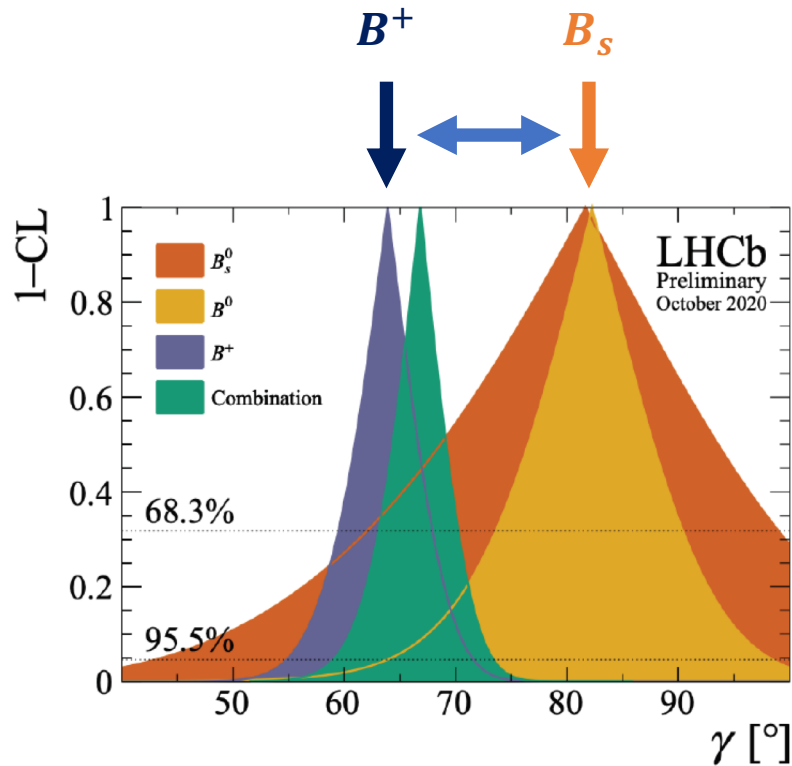


future



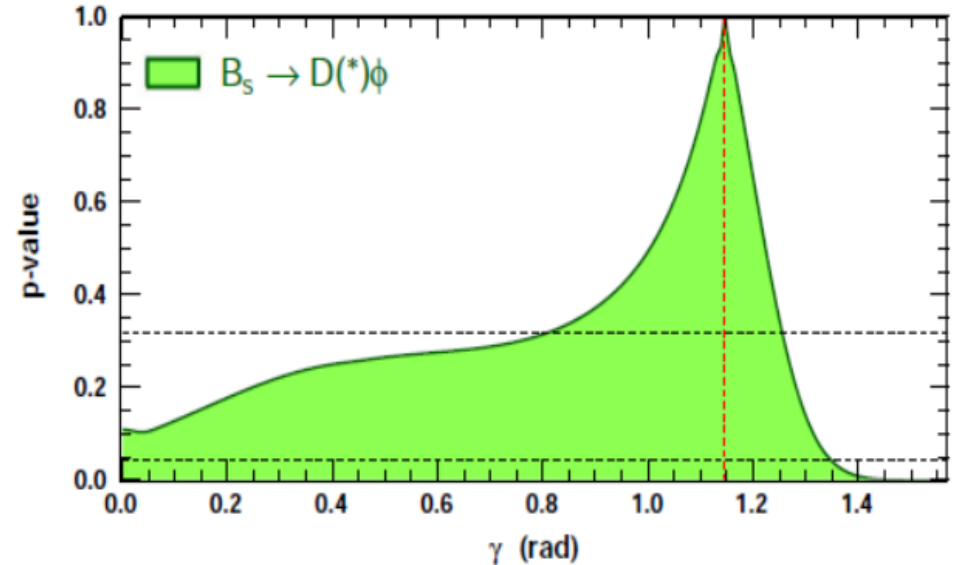
Spectrum of H,  $n=3 \rightarrow n=2$





- $B_s^0 \rightarrow \overline{D}^0 K^+ K^-$  and  $B_s^0 \rightarrow \overline{D}^{*0} \phi$ : golden channels for measuring  $\gamma$  in  $B_s$  decays
- Sensitivity studies performed:  $10\text{-}15^\circ$  with LHCb Run 1+2 data

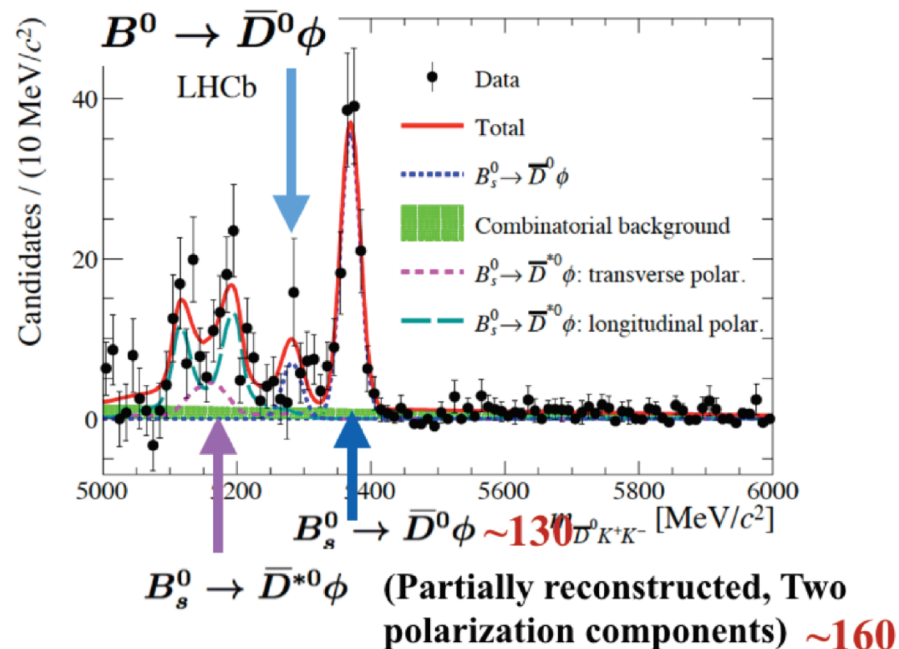
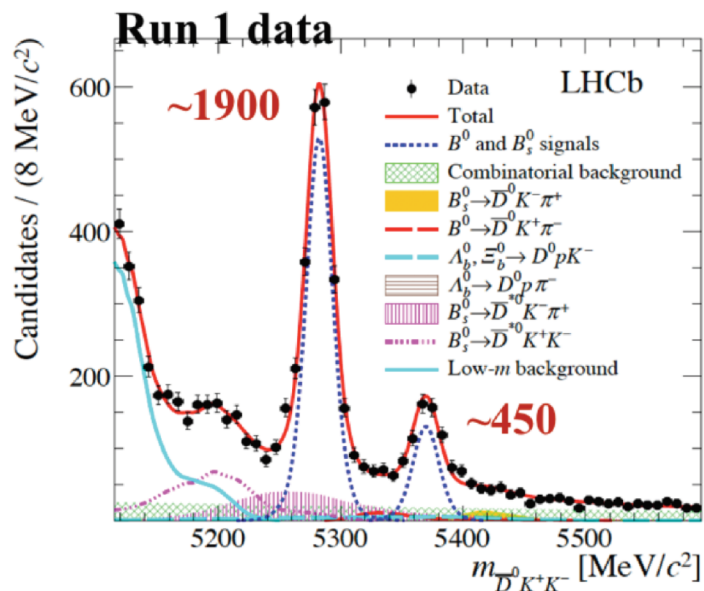
- Uncertainties of  $\gamma$  in  $B_s$  decays still large, potential improvements
- Important to understand discrepancies of  $\gamma$  measured from  $B^0$  and  $B_s$  decays



# Finding these decays in LHCb

Phys. Rev. D98 (2018) 072006  
Phys. Rev. D98 (2018) 071103(R)

- $B^0 \rightarrow D^0 \bar{K} K$  and  $B_s \rightarrow D^0 \bar{K} K$  decays
  - Time-Dependent Dalitz analyses to access CKM angle  $\gamma$  and  $\beta_{(s)}$
  - Not only probe  $\sin 2\beta_{(s)}$ , but also  $\cos 2\beta_{(s)}$
  - Dalitz structures interesting for charm spectroscopy studies
- $B_s \rightarrow D^{(*)} \phi$  decays: special cases where final states are in CP eigenstates



- Not only on  $B_s$  decays, efforts also ongoing to use new methods to measure old golden channels (EPJC78 (2018) 121)

- Fit fractions:

Component	Isobar				K-matrix				QMI			
$\rho(770)^0$	55.5	$\pm 0.6$	$\pm 0.7$	$\pm 2.5$	56.5	$\pm 0.7$	$\pm 1.5$	$\pm 3.1$	54.8	$\pm 1.0$	$\pm 1.9$	$\pm 1.0$
$\omega(782)$	0.50	$\pm 0.03$	$\pm 0.03$	$\pm 0.04$	0.47	$\pm 0.04$	$\pm 0.01$	$\pm 0.03$	0.57	$\pm 0.10$	$\pm 0.12$	$\pm 0.12$
$f_2(1270)$	9.0	$\pm 0.3$	$\pm 0.8$	$\pm 1.4$	9.3	$\pm 0.4$	$\pm 0.6$	$\pm 2.4$	9.6	$\pm 0.4$	$\pm 0.7$	$\pm 3.9$
$\rho(1450)^0$	5.2	$\pm 0.3$	$\pm 0.4$	$\pm 1.9$	10.5	$\pm 0.7$	$\pm 0.8$	$\pm 4.5$	7.4	$\pm 0.5$	$\pm 3.9$	$\pm 1.1$
$\rho_3(1690)^0$	0.5	$\pm 0.1$	$\pm 0.1$	$\pm 0.4$	1.5	$\pm 0.1$	$\pm 0.1$	$\pm 0.4$	1.0	$\pm 0.1$	$\pm 0.5$	$\pm 0.1$
S-wave	25.4	$\pm 0.5$	$\pm 0.7$	$\pm 3.6$	25.7	$\pm 0.6$	$\pm 2.6$	$\pm 1.4$	26.8	$\pm 0.7$	$\pm 2.0$	$\pm 1.0$

- Dominant contributions from S-wave and  $\rho(770)$
- CP asymmetries:

Component	Isobar				K-matrix				QMI			
$\rho(770)^0$	+0.7	$\pm 1.1$	$\pm 1.2$	$\pm 1.5$	+4.2	$\pm 1.5$	$\pm 2.6$	$\pm 5.8$	+4.4	$\pm 1.7$	$\pm 2.3$	$\pm 1.6$
$\omega(782)$	-4.8	$\pm 6.5$	$\pm 6.6$	$\pm 3.5$	-6.2	$\pm 8.4$	$\pm 5.6$	$\pm 8.1$	-7.9	$\pm 16.5$	$\pm 14.2$	$\pm 7.0$
$f_2(1270)$	+46.8	$\pm 6.1$	$\pm 3.6$	$\pm 4.4$	+42.8	$\pm 4.1$	$\pm 2.1$	$\pm 8.9$	+37.6	$\pm 4.4$	$\pm 6.0$	$\pm 5.2$
$\rho(1450)^0$	-12.9	$\pm 3.3$	$\pm 7.0$	$\pm 35.7$	+9.0	$\pm 6.0$	$\pm 10.8$	$\pm 45.7$	-15.5	$\pm 7.3$	$\pm 14.3$	$\pm 32.2$
$\rho_3(1690)^0$	-80.1	$\pm 11.4$	$\pm 13.5$	$\pm 24.1$	-35.7	$\pm 10.8$	$\pm 8.5$	$\pm 35.9$	-93.2	$\pm 6.8$	$\pm 8.0$	$\pm 38.1$
S-wave	+14.4	$\pm 1.8$	$\pm 2.1$	$\pm 1.9$	+15.8	$\pm 2.6$	$\pm 2.1$	$\pm 6.9$	+15.0	$\pm 2.7$	$\pm 4.2$	$\pm 7.0$

- Large CPV from S-wave and  $f_2(1270)$  (first observation)