

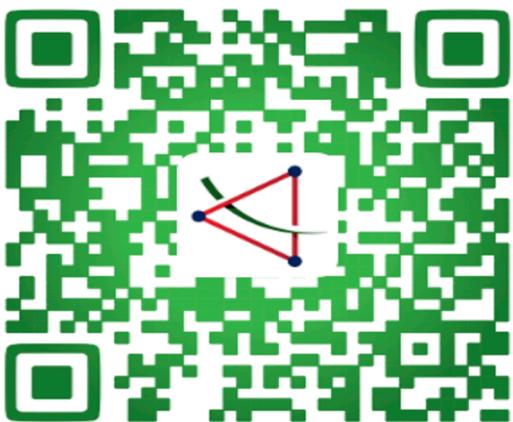


相变引力波

中山大学物理与天文学院天琴中心 黄发朋

中国高能物理非加速器战略研讨会
@ 高能所, 北京, 2021年5月15日

微信公众号



天琴中心大楼



激光测距台站





报告提纲



一、研究动机

二、相变引力波简介

三、四个重要的方向

四、总结和展望

理论动机

CEPC/LHC一圈
水平上的对撞机信号

内在关联、 \updownarrow 互补验证

Higgs物理（势函数的形状）、Z-pole物理、TeV新物理

天琴/LISA
相变引力波
（精确预言）

宇宙正反物质
不对称性的起源

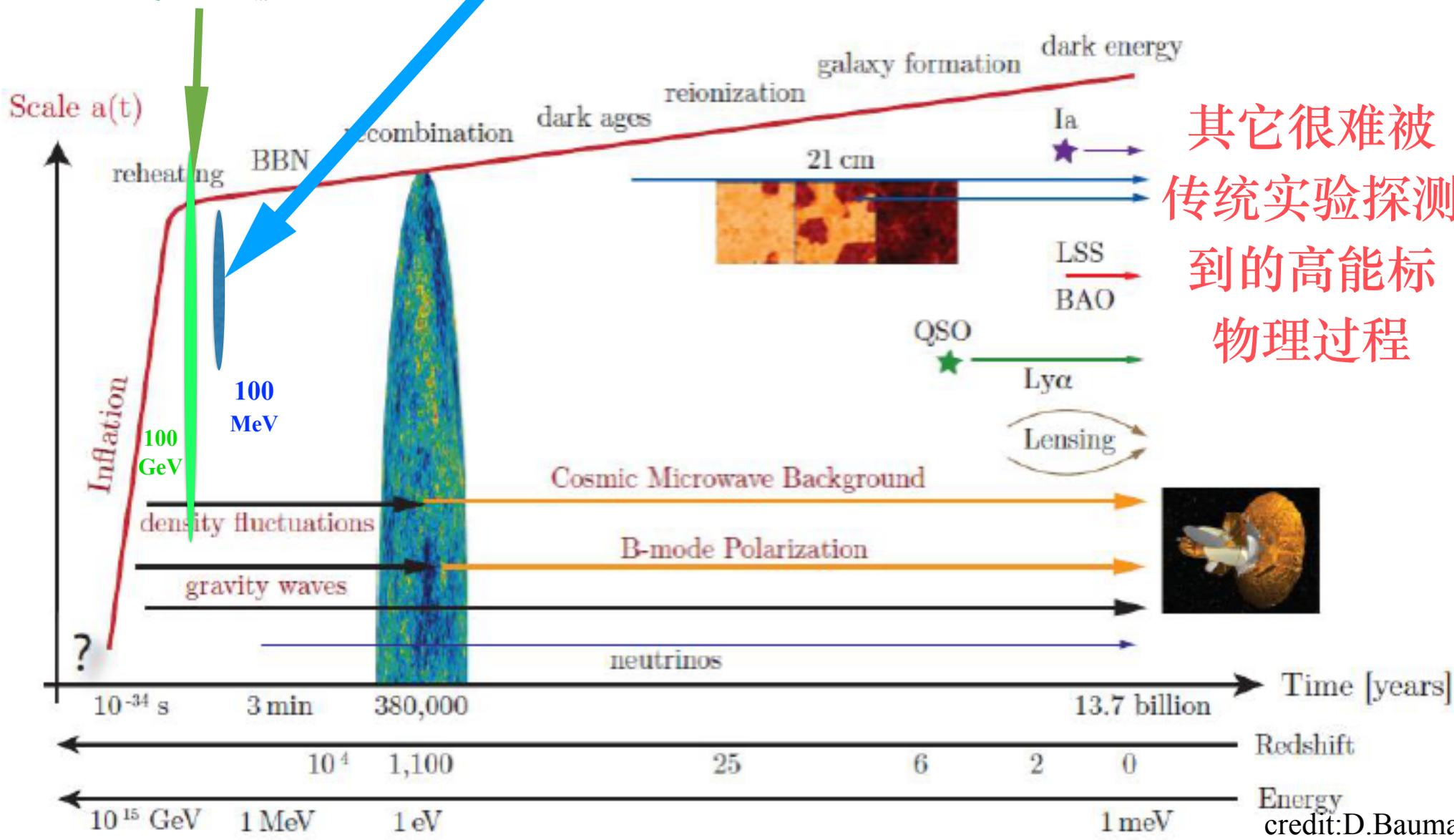
早期宇宙、原初磁场、
高能标物理(中微子)过
程、额外维等

新的暗物质探测方法;
新的暗物质产生机制

实验动机

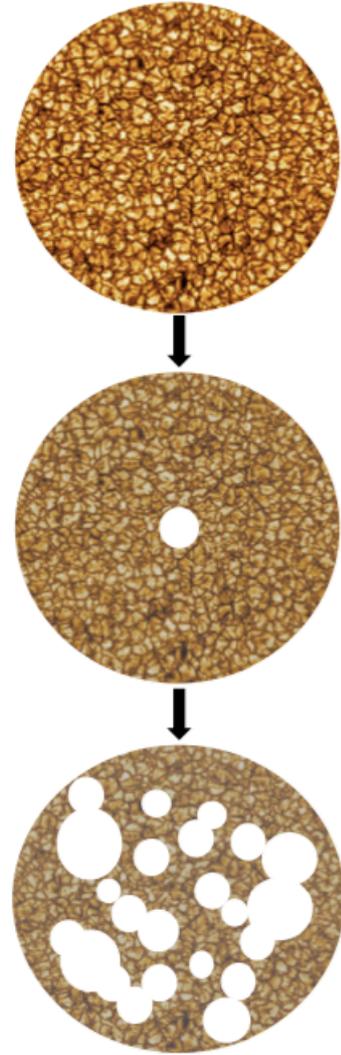
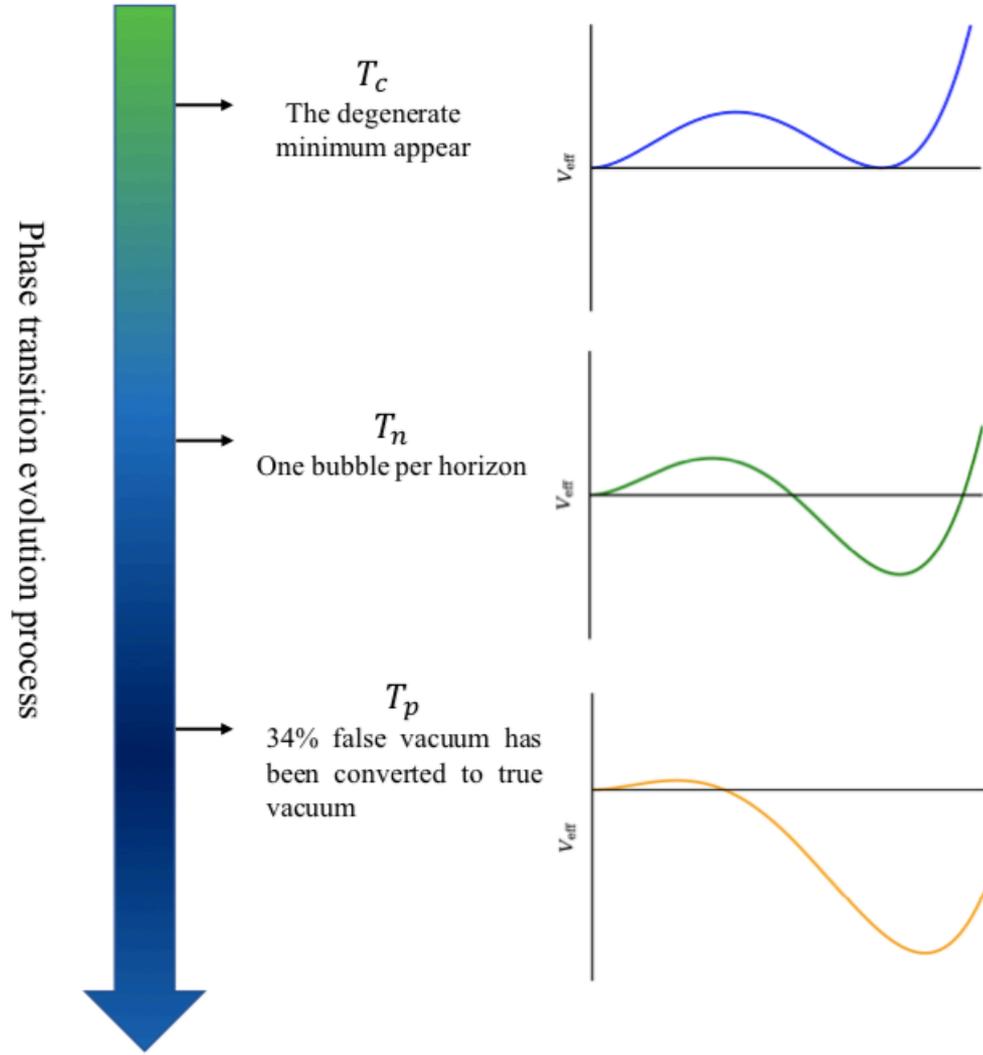
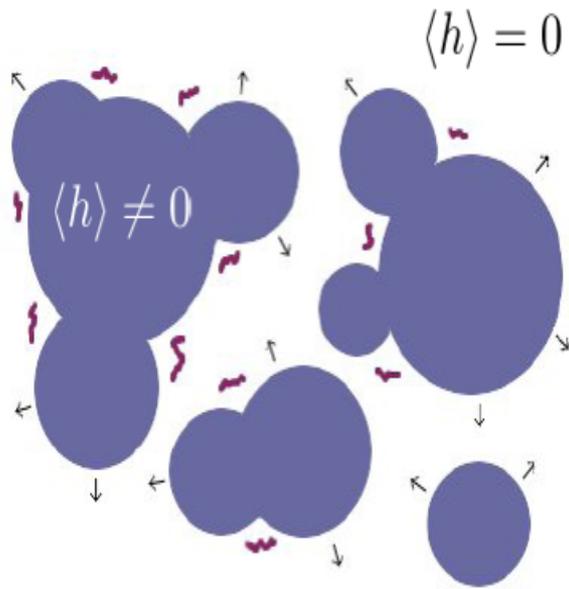
电弱相变、TeV相变
(宇宙正反物质不对称
性的起源、暗物质)：
天琴/太极/LISA

QCD 相变(暗物质)：SKA/FAST





相变引力波简介

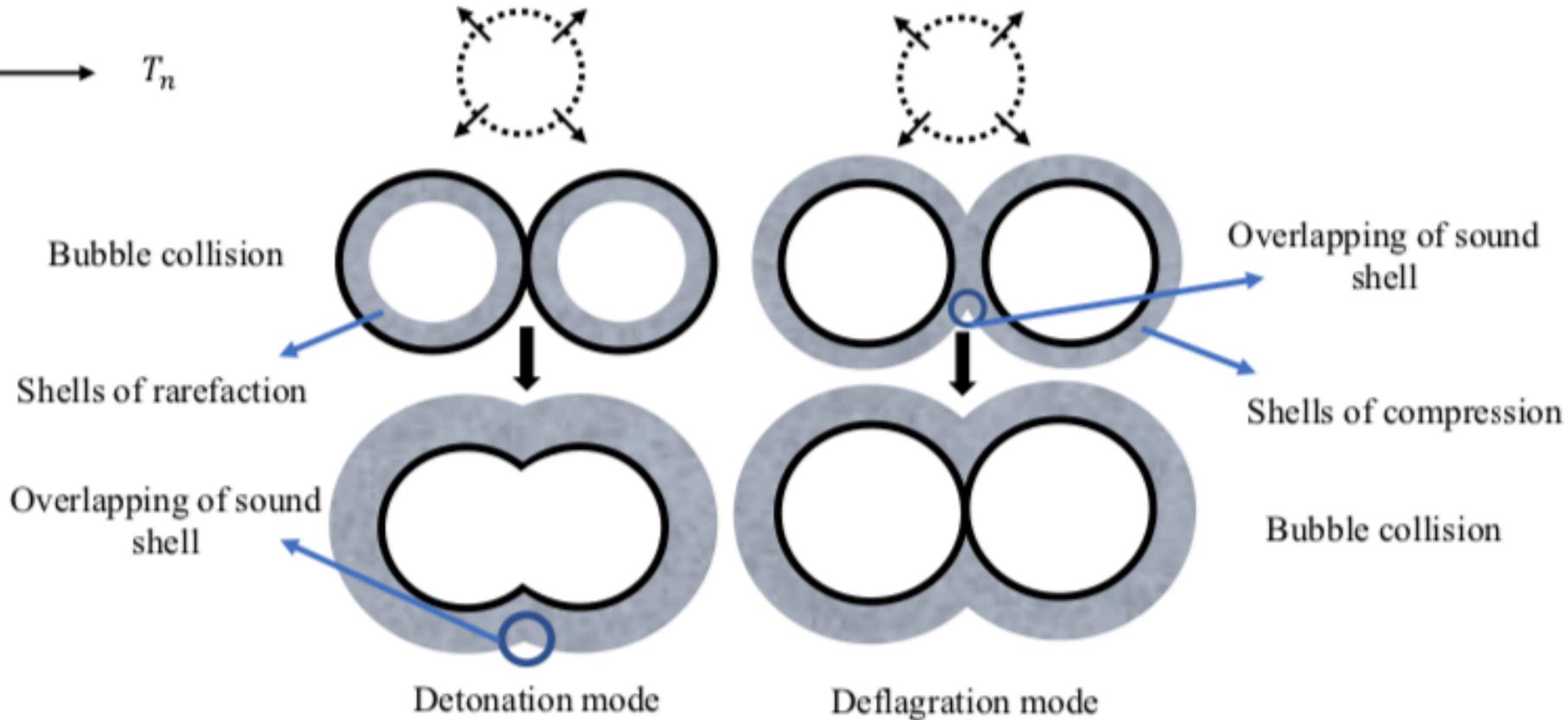


Xiao Wang, **FPH**, Xinmin Zhang, JCAP05(2020)045

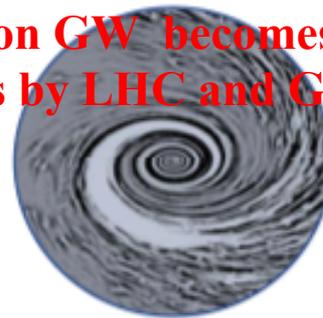
High temperature

Gravitational wave (GW) from a strong first-order phase transition (SFOPT)

Formation and expansion of bubbles



Electroweak phase transition GW becomes more interesting and realistic after the discovery of Higgs by LHC and GW by LIGO.



Turbulence

Low temperature

Xiao Wang, **FPH**, Xinmin Zhang, JCAP05(2020)045

GW signals from SFOPT

Bubble collisions

$$h^2 \Omega_{\text{co}}(f) \simeq 1.67 \times 10^{-5} \left(\frac{H_* R_*}{(8\pi)^{1/3}} \right)^2 \left(\frac{\kappa_\phi \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} \frac{0.11 v_b}{0.42 + v_b^2} \frac{3.8 (f/f_{\text{co}})^{2.8}}{1 + 2.8 (f/f_{\text{co}})^{3.8}}$$

Turbulence

$$h^2 \Omega_{\text{turb}}(f) \simeq 1.14 \times 10^{-4} H_* R_* \left(\frac{\kappa_{\text{turb}} \alpha}{1 + \alpha} \right)^{3/2} \left(\frac{100}{g_*} \right)^{1/3} \frac{(f/f_{\text{turb}})^3}{(1 + f/f_{\text{turb}})^{11/3} (1 + 8\pi f/H_*)}$$

Sound wave

$$h^2 \Omega_{\text{sw}}(f) \simeq 1.64 \times 10^{-6} (H_* \tau_{\text{sw}}) (H_* R_*) \left(\frac{\kappa_v \alpha}{1 + \alpha} \right)^2 \left(\frac{100}{g_*} \right)^{1/3} (f/f_{\text{sw}})^3 \left(\frac{7}{4 + 3(f/f_{\text{sw}})^2} \right)^{7/2}$$

E. Witten, Phys. Rev. D 30, 272 (1984)

C. J. Hogan, Phys. Lett. B 133, 172 (1983);

M. Kamionkowski, A. Kosowsky and M. S. Turner, Phys. Rev. D 49, 2837 (1994) Mark Hindmarsh, *et al.*, PRL 112, 041301 (2014); Lots of unlisted papers.



相变动力学、相变引力波精确预言



There are many difficult but interesting directions

1. **Daisy resummation problem:** Pawani scheme vs. Arnold scheme
2. **Gauge dependence problem:** see Michael J. Ramsey-Musolf's works
3. **No perturbative calculations:** lattice calculations and dim-reduction method: by D. Weir, Michael J. Ramsey-Musolf et.al
4. **Reliable calculations of bubble wall velocity**

Xiao Wang, **FPH**, Xinmin Zhang, arXiv:2011.12903,
S. H"oche, J. Kozaczuk, A. J. Long, J. Turner and Y. Wang, arXiv:2007.10343,
Avi Friedlander, Ian Banta, James M. Cline, David Tucker-Smith, arXiv:2009.14295v2

5. **GW spectra prediction for ultra-supercooling**

6. **energy budget during phase transition**

Xiao Wang, **FPH** and Xinmin Zhang, arXiv:2010.13770

F. Giese, T. Konstandin, K. Schmitz and J. van de Vis, arXiv:2010.09744



相变引力波实验迹象



Searching For Gravitational Waves From Cosmological Phase Transitions With The NANOGrav 12.5-year dataset (The NANOGrav Collaboration) arXiv:2104.13930 .

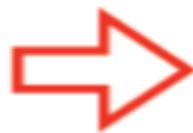
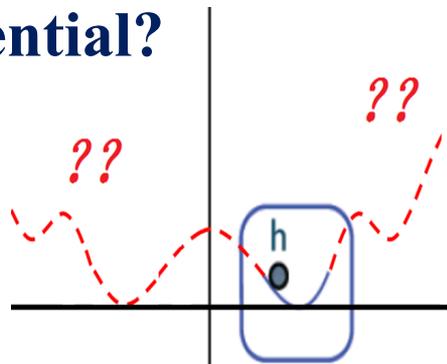
“We find that the data can be explained in terms of a strong first order phase transition taking place at temperatures below the electroweak scale.”



相变引力波与希格斯物理



What is the shape of Higgs potential?

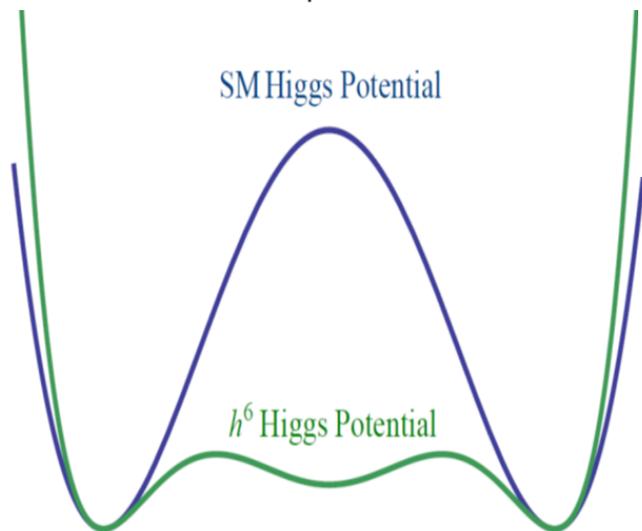


From current data, we know nothing but the quadratic oscillation around the VEV 246 GeV with 125 GeV mass.

$$V(h) = \frac{1}{2}\mu^2 h^2 + \frac{\lambda}{4}h^4$$



or
$$V(h) = \frac{1}{2}\mu^2 h^2 - \frac{\lambda}{4}h^4 + \frac{1}{\Lambda^2}h^6$$



Produce a SFOPT, large deviation of Higgs trilinear coupling and GW

Xinmin Zhang Phys.Rev. D47 (1993) 3065-3067

C. Grojean, G. Servant, J. Well PRD71(2005)036001

D.J.H. Chung, A. J. Long, Lian-tao Wang Phys.Rev. D87(2013) 023509

FPH, et.al, Phys.Rev.D94(2016)no.4,041702 ,

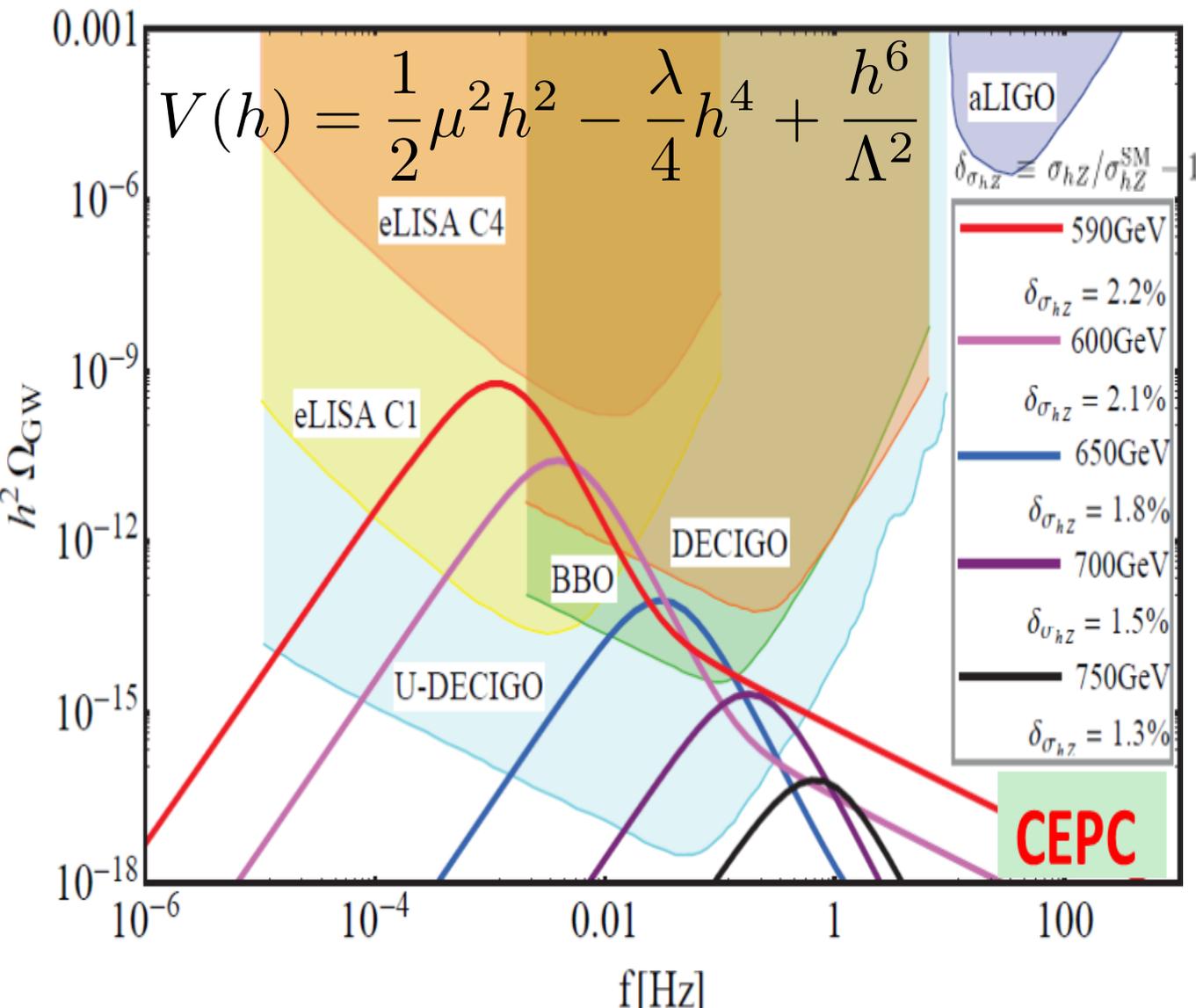
FPH, et.al, Phys.Rev.D93 (2016) no.10,103515

arXiv:1511.06495 Nima Arkani-Hamed et. al.;

PreCDR of CEPC;

arXiv: 1811.10545 CDR of CEPC

Correlate particle collider and GW signals: Double test on Higgs nature and baryogenesis from particle to wave



- For CEPC with 10 ab^{-1} at $\sqrt{s} = 240$ GeV, precision of σ_{zh} may be about 0.4% and can test the scenario.
- LISA, BBO, U-DECIGO are capable of detection
- The study on EW phase transition naturally bridges the particle physics at collider with GW survey and baryogenesis

FPH, et.al, Phys.Rev.D94(2016)no.4,041702

FPH, et.al, Phys.Rev.D93 (2016) no.10,103515

Consistent check in standard model effective field theory from EW observables to future lepton collider

$$\mathcal{L} \supset -\mu^2 |H|^2 - \lambda |H|^4 + c_6 |H|^6 \\ + c_T \mathcal{O}_T + c_{WW} \mathcal{O}_{WW} + \text{other dimension-six operators}$$



$$\delta_{\sigma(hZ)} \approx (0.26c_{WW} + 0.01c_{BB} + 0.04c_{WB} - 0.06c_H - 0.04c_T + 0.74c_L^{(3)\ell} \\ + 0.28c_{LL}^{(3)\ell} + 1.03c_L^\ell - 0.76c_R^e) \times 1 \text{ TeV}^2 + 0.016\delta_h,$$

SFOPT produces large modification of trilinear Higgs coupling

δ_h

c_6 dominates the hZ cross section deviation

Taking a general study of the scalar extended models and the composite Higgs model as examples, we can see that the Higgs sextic scenario still works well after considering all the dim-6 operators and the precise measurements.

Renormalizable realization of the from doublet model

$$\begin{aligned} \delta\mathcal{L} = & D_\mu\Phi^\dagger D^\mu\Phi - M_\Phi^2\Phi^\dagger\Phi - \frac{\lambda_\Phi}{4}(\Phi^\dagger\Phi)^2 - \lambda_1\Phi^\dagger\Phi H^\dagger H - \lambda_2|\Phi \cdot H|^2 \\ & - \lambda_3[(\Phi \cdot H)^2 + h.c.] + (\eta_H|H|^2 + \eta_\Phi|\Phi|^2)(\Phi \cdot H + h.c.), \end{aligned}$$

Using **Covariant Derivative Expansion method**, the matched dim-6 operators and their coefficients in the doublet scalar models are obtained:

Dimension-six operator	Wilson coefficient
$\mathcal{O}_{WW} = g^2 H ^2 W_{\mu\nu}^a W^{a,\mu\nu}$	$c_{WW} = \frac{1}{(4\pi)^2} \frac{1}{48} (2\lambda_1 + \lambda_2) \frac{1}{M_\Phi^2}$
$\mathcal{O}_{2W} = -\frac{1}{2}(D^\mu W_{\mu\nu}^a)^2$	$c_{2W} = \frac{1}{(4\pi)^2} \frac{g^2}{60} \frac{1}{M_\Phi^2}$
$\mathcal{O}_{3W} = \frac{1}{3!} g\epsilon^{abc} W_\rho^{a\mu} W_\mu^{b\nu} W_\nu^{c\rho}$	$c_{3W} = \frac{1}{(4\pi)^2} \frac{g^2}{60} \frac{1}{M_\Phi^2}$
$\mathcal{O}_{BB} = g'^2 H ^2 B_{\mu\nu} B^{\mu\nu}$	$c_{BB} = \frac{1}{(4\pi)^2} \frac{1}{48} (2\lambda_1 + \lambda_2) \frac{1}{M_\Phi^2}$
$\mathcal{O}_{WB} = gg' H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu}$	$c_{WB} = \frac{1}{(4\pi)^2} \frac{\lambda_2}{24} \frac{1}{M_\Phi^2}$
$\mathcal{O}_{2B} = -\frac{1}{2}(\partial^\mu B^{\mu\nu})^2$	$c_{2B} = \frac{1}{(4\pi)^2} \frac{g'^2}{60} \frac{1}{M_\Phi^2}$
$\mathcal{O}_H = \frac{1}{2}(\partial_\mu H ^2)^2$	$c_H = \frac{1}{(4\pi)^2} [6\eta_\Phi\eta_H + \frac{1}{12}(4\lambda_1^2 + 4\lambda_1\lambda_2 + \lambda_2^2 + 4\lambda_3^2)] \frac{1}{M_\Phi^2}$
$\mathcal{O}_T = \frac{1}{2}(H^\dagger \overleftrightarrow{D}_\mu H)^2$	$c_T = \frac{1}{(4\pi)^2} \frac{1}{12} (\lambda_2^2 - 4\lambda_3^2) \frac{1}{M_\Phi^2}$
$\mathcal{O}_r = H ^2 D_\mu H ^2$	$c_r = \frac{1}{(4\pi)^2} (6\eta_\Phi\eta_H + \frac{1}{6}(\lambda_2^2 + 4\lambda_3^2)) \frac{1}{M_\Phi^2}$
$\mathcal{O}_6 = H ^6$	$c_6 = \eta_H^2 + \frac{1}{(4\pi)^2} [\frac{3}{2}\lambda_\Phi\eta_H^2 + 6\eta_\Phi(\lambda_1 + \lambda_2) - \frac{1}{6}(2\lambda_1^3 + 3\lambda_1^2\lambda_2 + 3\lambda_1\lambda_2^2 + \lambda_2^3) - 2(\lambda_1 + \lambda_2)\lambda_3^2] \frac{1}{M_\Phi^2}$



相变引力波与宇宙正反物质不对称性的起源



A long standing problem in particle cosmology is the origin of baryon asymmetry of the universe (BAU).

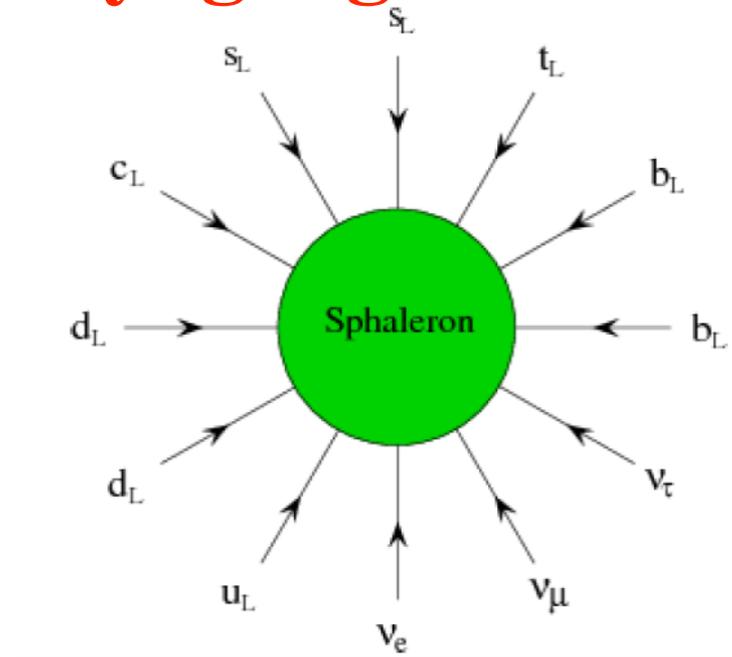
After the discovery of the Higgs boson by LHC and GW by aLIGO, electroweak (EW) baryogenesis becomes a timely and testable scenario for explaining the BAU.



$$\eta_B = n_B/n_\gamma = 5.8 - 6.6 \times 10^{-10} \quad (\text{CMB, BBN})$$

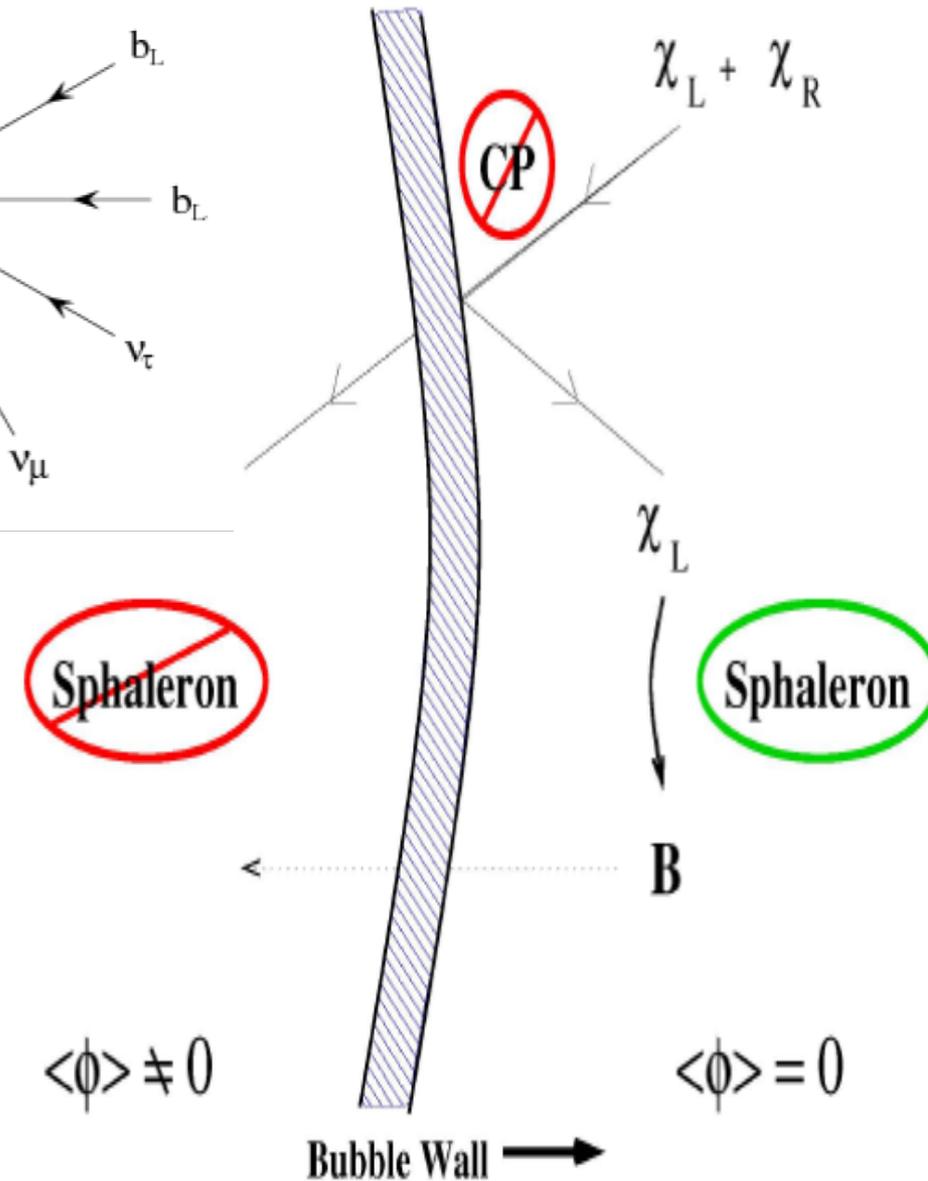
Electroweak baryogenesis

SM technically has all the three elements for baryogenesis, (**B**aryon violation, **C** and **CP** violation, **D**eparture from thermal equilibrium or **CPT** violation) but not enough.



- **B violation from anomaly in B+L current.**
- **CKM matrix, but too weak.**
- **SFOPT with expanding Higgs bubble wall**

D. E. Morrissey and M. J. Ramsey-Musolf,
New J. Phys. 14, 125003 (2012).



Dynamical CP violation for baryogenesis

Current electric dipole moment (EDM) experiments put severe constraints on many baryogenesis models. For example, the ACME Collaboration's new result, i.e. $|d_e| < 1.1 \times 10^{-29} \text{ cm} \cdot e$ at 90% C.L. (Nature vol.562,357,18th Oct.2018), has ruled out a large portion of the CP violation parameter space for many baryogenesis models.

Large enough
CP-violating source
for successful
EW baryogenesis

Strong tension in most cases



pretty small
CP-violation
to avoid strong EDM
constraints

How to alleviate this tension for successful baryogenesis?

Question: How to alleviate the tension for successful baryogenesis?

Answer: Dynamical CP-violating source

Large enough
CP-violating source
in the early universe
for successful
EW baryogenesis

Alleviate by assuming the
CP-violating source is time dependent



Dynamical/cosmological evolve

**Negligible
CP-violating source
at current time
to avoid strong EDM
constraints**

Effective field theory study: FPH, Zhuoni Qian, Mengchao Zhang, Phys. Rev. D 98 (2018) no.1, 015014

FPH, Chong Sheng Li, Phys. Rev. D 92, 075014 (2015)

Renormalizable model: Complex 2HDM: Xiao Wang, FPH, Xinmin Zhang, arXiv: 1909.02978 And work in progress with Eibun Senaha in an extended IDM model

Baldes, T. Konstandin and G. Servant, arXiv:1604.04526, I. Baldes, T. Konstandin and G. Servant, JHEP 1612, 073 (2016) S. Bruggisser, T.

Konstandin and G. Servant, JCAP 1711, no. 11, 034 (2017)

Taking the effective scenario as a representative example:

arXiv:1804.06813, Phys.Rev. D98 (2018) no.1, 015014

(**FPH**, Zhuoni Qian, Mengchao Zhang)

$$\mathcal{L}_{\text{SM}} = y_t \frac{\eta}{\Lambda} S \bar{Q}_L \tilde{\Phi} t_R + \text{H.c.} + \frac{1}{2} \partial_\mu S \partial^\mu S + \frac{1}{2} \mu^2 S^2 - \frac{1}{4} \lambda S^4 - \frac{1}{2} \kappa S^2 (\Phi^\dagger \Phi)$$

$\eta = a + ib$ The singlet and the dim-5 operator can come from many types composite Higgs model, arXiv:0902.1483 , arXiv:1703.10624 ,arXiv:1704.08911,

Firstly, a second-order phase transition happens, the scalar field S acquire a vacuum expectation value (VEV) and the dim-5 operator generates a sizable CP-violating Yukawa coupling for successful baryogenesis.

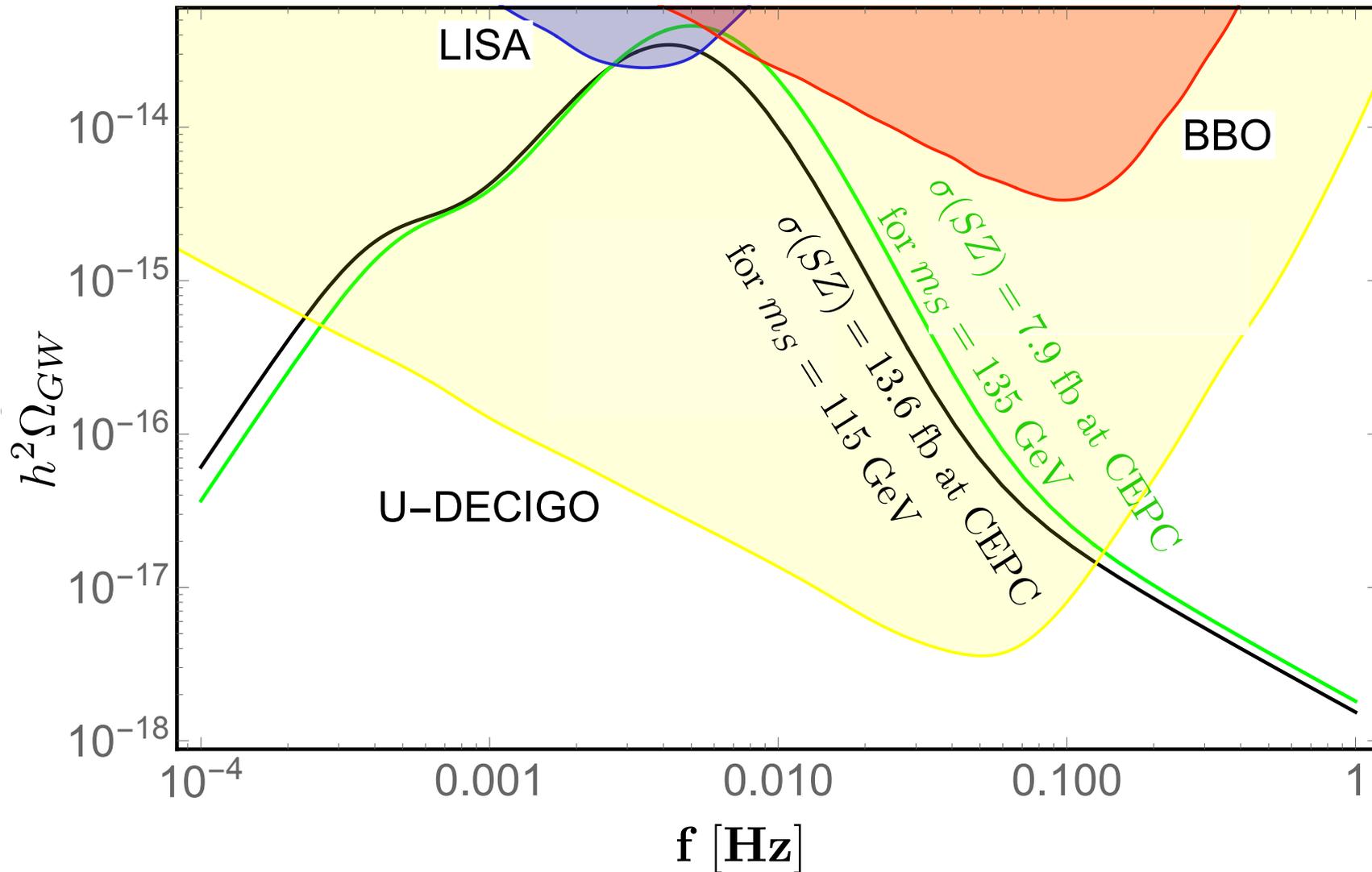
Secondly, SFOPT occurs when vacuum transits from $(0, \langle S \rangle)$ to $(\langle \Phi \rangle, 0)$.

- 1. During the SFOPT, detectable GW can be produced.**
- 2. After the SFOPT, the VEV of S vanishes at tree-level which avoids the strong EDM constraints, and produces abundant collider phenomenology**

J. R. Espinosa, B. Gripaios, T. Konstandin and F. Riva, JCAP **1201**, 012 (2012)

J. M. Cline and K. Kainulainen, JCAP **1301**, 012 (2013)

The correlation between the future GW and collider signals



For example taking benchmark set I, the GW spectrum is represented by the black line, which can be detected by LISA and U-DECIGO. The black line also corresponds to $0.9339\sigma_{\text{SM}}(\text{HZ})$ of the HZ cross section for $e^+e^- \rightarrow \text{HZ}$ process and 115 GeV recoil mass with 13.6 fb cross section for the $e^+e^- \rightarrow \text{SZ}$ process, which has a 5σ discovery potential with 5 ab^{-1} luminosity at CEPC.



相变引力波与新的暗物质产生机制



➤ **New dark matter (DM) production scenario filtered by the bubbles of the SFOPT in the early universe**

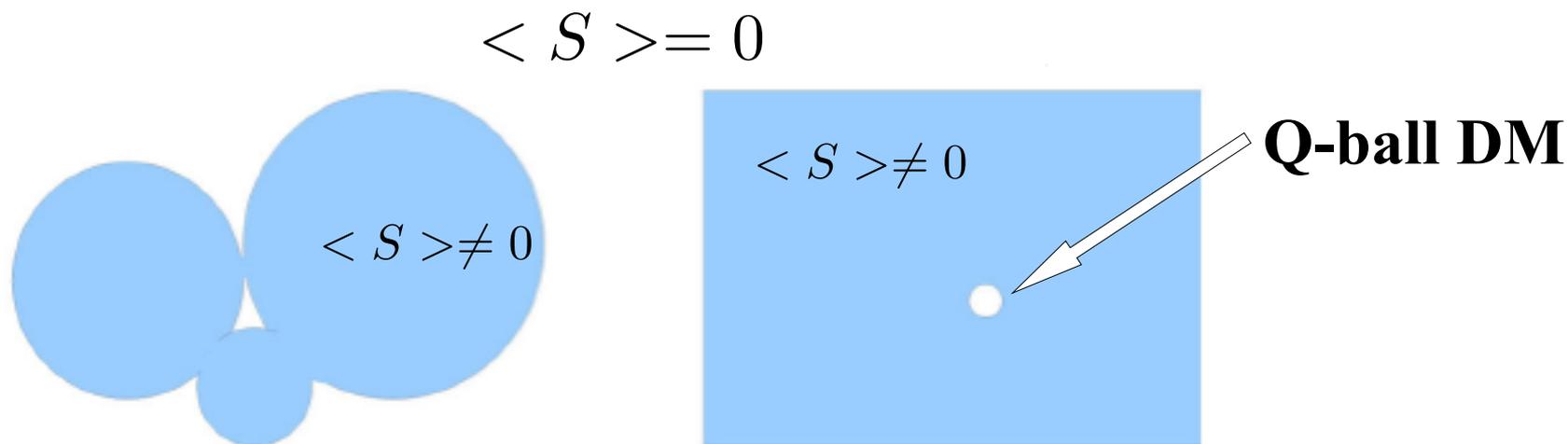
The cosmic phase transition with Q-balls production can explain baryogenesis and DM simultaneously, where constraints on DM mass and reverse dilution are significantly relaxed. We study how to probe this scenario by GW signals and collider signals at QCD NLO.

FPH, Chong Sheng Li, Phys.Rev. D96 (2017) no.9, 095028

Many mechanisms to simultaneously solve the baryogenesis and DM puzzles usually have two strong constraints.

B. Shuve, C. Tamarit, JHEP 1710 (2017) 122

SFOPT naturally correlates DM, baryogenesis, particle collider and GW signals.



And with the bubble expansion, the symmetric phase eventually shrinks to very small size objects and become the so-called Q-balls as DM candidates.

$$\begin{aligned}
 \mathcal{L} = & \frac{1}{2}(\partial_\mu S)^2 - U(S) + (\partial_\mu \chi)^*(\partial_\mu \chi) - k_1^2 S^2 \chi^* \chi \\
 & - \sum_i \frac{h_i^2}{2} S^2 \phi_i^2 + \sum_i \frac{1}{2}(\partial_\mu \phi_i)^2 \\
 & - \sum_{a=1,2} \frac{\lambda_a^{ijk}}{\Lambda^2} \bar{X}_a P_R D_i \bar{U}_j^C P_R D_k + \frac{\zeta_a}{\Lambda} \bar{X}_a Y^C \chi \chi^* \\
 & + \text{H.c.}
 \end{aligned}$$

Final conditions to produce the observed baryon asymmetry and DM density: **FPH, C.S. Li, Phys.Rev. D96 (2017) no.9, 09502**

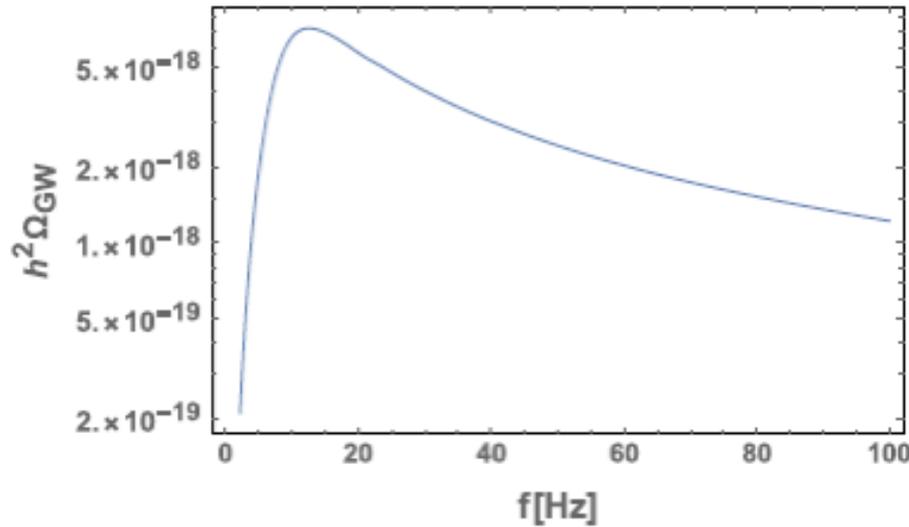
$$\rho_{\text{DM}}^4 v_b^{3/4} = 73.5 (2\eta_B s_0)^3 \lambda_S \sigma^4 \Gamma^{3/4}$$

TABLE I. The benchmark sets after considering the combined constraints for producing the observed DM density and BAU with $v_b = 0.3$.

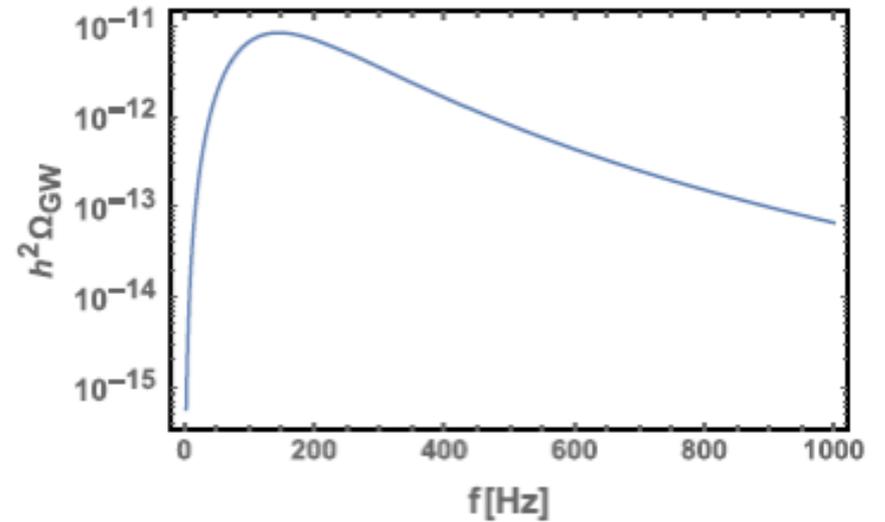
Benchmark sets	λ_S	e	c	T_c [TeV]	$\frac{\sigma}{T_c}$
I	0.008	0.754	1	15.9	5
II	0.0016	0.151	1	6.6	5

Extension work for the gauged Q-balls is working in progress with Prof. P. Ko

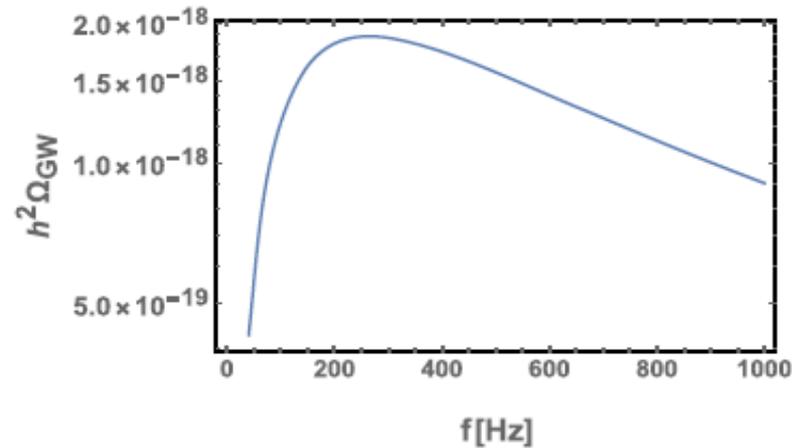
The predicted GW spectrum for benchmark points with $v_b = 0.3$. Figure(a), (b), (c) represents the GW spectrum from bubble collision, sound waves and turbulence, respectively, which may be detected by future LIGO-like experiments, Einstein telescope or cosmic explorer.



(a)



(b)



(c)

FPH, Chong Sheng Li, Phys.Rev. D96 (2017) no.9, 095028

In the recent two years, this dynamical DM formed by phase transition has become a new idea and attracted more and more attentions.

Namely, bubbles in SF OPT can be the “filters” to packet your needed heavy DM.

arXiv:1912.04238, Dongjin Chway, Tae Hyun Jung, Chang Sub Shin

arXiv:1912.02830, Michael J. Baker, Joachim Kopp, and Andrew J. Long

arXiv:2012.15113, Wei Chao, Xiu-Fei Li, Lei Wang

arXiv:2101.05721, Aleksandr Azatov, Miguel Vanvlasselaer, Wen Yin

arXiv:2103.09827, Pouya Asadi, Eric David Kramer, Eric Kuflik, Gregory W. Ridgway, Tracy R. Slatyer, Juri Smirnov

arXiv:2103.09822, Pouya Asadi, Eric David Kramer, Eric Kuflik, Gregory W. Ridgway, Tracy R. Slatyer, Juri Smirnov

arXiv:2008.04430 Jeong-Pyong Hong, Sunghoon Jung, Ke-pan Xie



相变引力波与暗物质探测



- **The observation of GW by LIGO has initiated a new era of exploring DM by GW.**
- **DM can trigger a SFOPT in the early universe, which can leads to detectable GW signals.**

Hearing the signal of dark sectors with gravitational wave detectors

J.Jaeckel, V. V. Khoze, M. Spannowsky, Phys.Rev. D94 (2016) no.10, 103519

Yan Wang, Chong Sheng Li, and **FPH**, arXiv:2012.03920

FPH, Eibun Senaha Phys.Rev. D100 (2019) no.3, 03501

FPH PoS ICHEP2018 (2019) 397

FPH, Chong Sheng Li Phys.Rev. D96 (2017) no.9, 095028

FPH, Jiang-Hao Yu Phys.Rev. D98 (2018) no.9, 095022

FPH, Xinmin Zhang, Phys.Lett. B788 (2019) 288-29

Inert Doublet Models

$$V_0 = M_D^2 D^\dagger D + \lambda_D (D^\dagger D)^2 + \lambda_3 \Phi^\dagger \Phi D^\dagger D \\ + \lambda_4 |\Phi^\dagger D|^2 + (\lambda_5/2)[(\Phi^\dagger D)^2 + h.c.],$$

mixed singlet-doublet model

$$V_0 = \frac{1}{2} M_S^2 S^2 + M_D^2 H_2^\dagger H_2 + \frac{1}{2} \lambda_S S^2 |\Phi|^2 + \lambda_3 \Phi^\dagger \Phi H_2^\dagger H_2 \\ + \lambda_4 |\Phi^\dagger H_2|^2 + \frac{\lambda_5}{2} [(\Phi^\dagger H_2)^2 + H.c.] + A[S\Phi H_2^\dagger + H.c.].$$

mixed singlet-triplet model

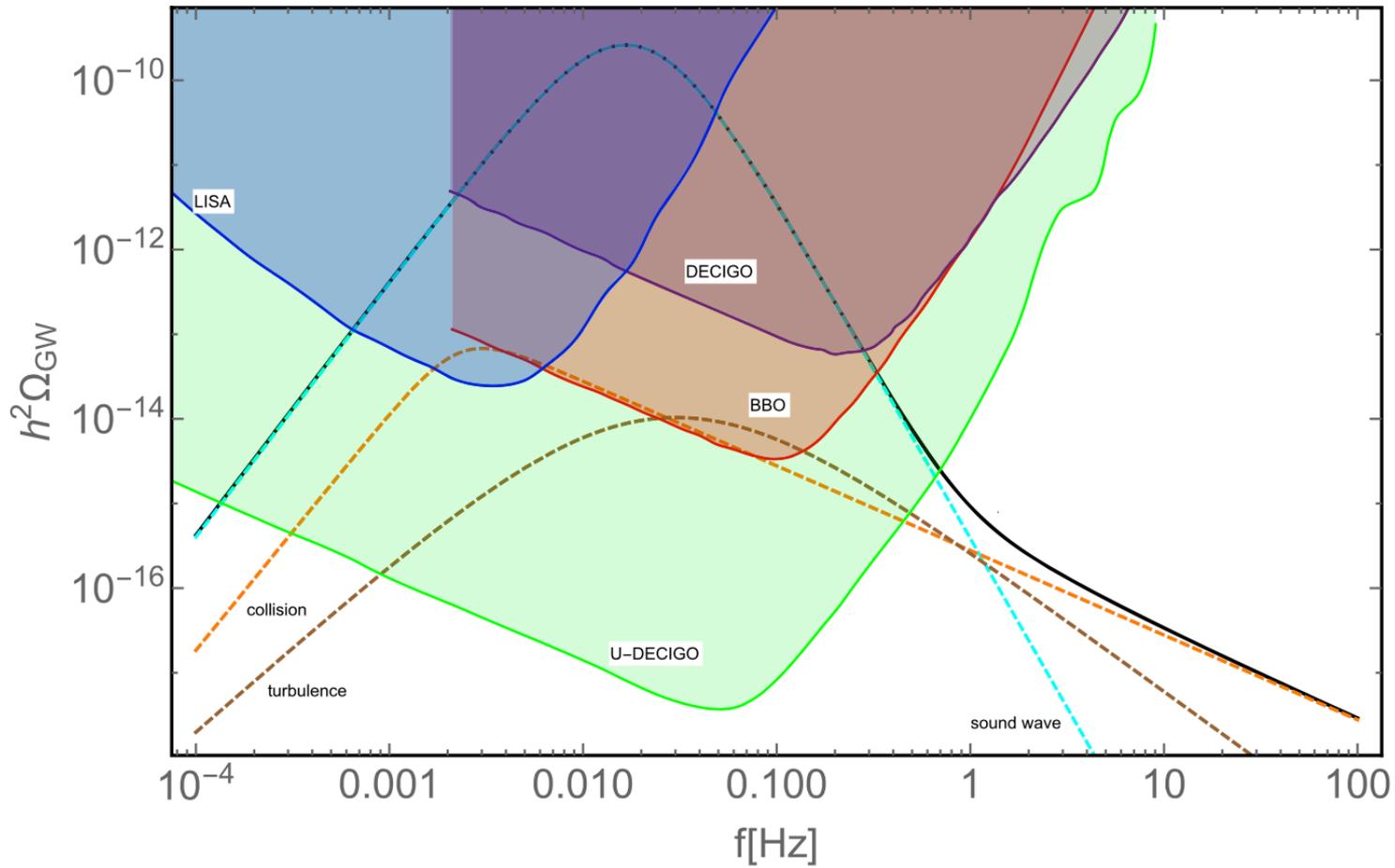
$$V_0 = \frac{1}{2} M_S^2 S^2 + M_\Sigma^2 \text{Tr}(H_3^2) + \kappa_\Sigma \Phi^\dagger \Phi \text{Tr}(H_3^2) \\ + \frac{\kappa}{2} |\Phi|^2 S^2 + \xi S \Phi^\dagger H_3 \Phi.$$

provide natural
DM candidate

produce SFOPT and phase transition
GW

FPH, Jiang-hao Yu, *Phy. Rev. D* **98**, 095022 (2018)

Yan Wang, Chong Sheng Li, **FPH**, arXiv: 2012.03920



GW in the mixed singlet-doublet model

FPH, Jiang-hao Yu, *Phy. Rev. D* 98, 095022 (2018)



相变引力波探测其它新物理和 早期宇宙过程

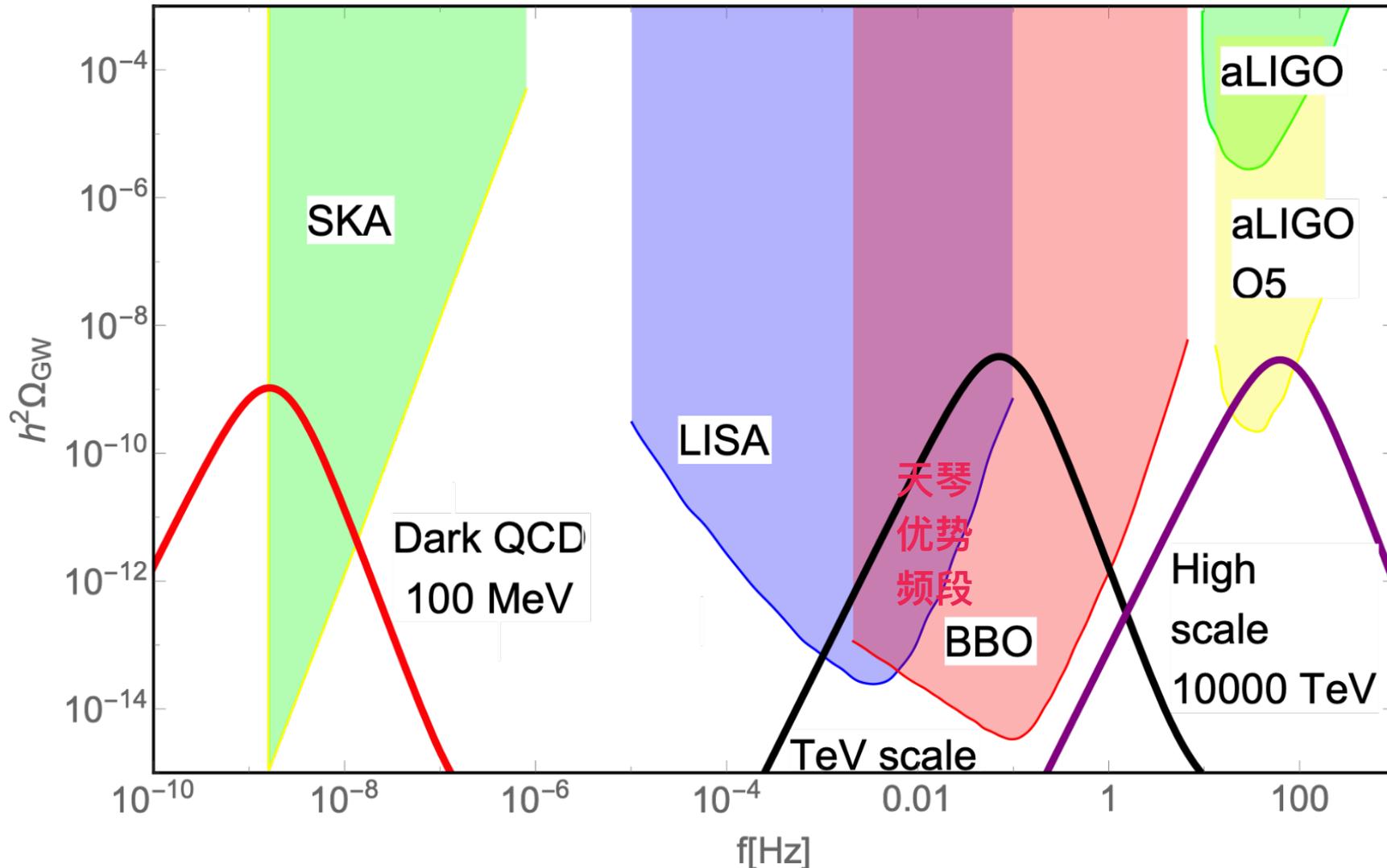


Phase transition GW can provide a unique way to probe many important physics processes: inflation, PQ-symmetry breaking, neutrino physics, axion physics, extra dimension, primordial magnetic field, cosmic defects...

Wei-Chih Huang, et. al, arXiv: 2012.11614
Mark Hindmarsh, et. al. arXiv: 2011.12878
Bhupal Dev, et. al. arXiv: 1905.00891
Yiyang Zhang, et. al. arXiv:1902.02751
Yang Bai, et. al. arXiv:1810.04360
Andrew Long, et. al. arXiv:1703.04902
Graciela Gelmini, et. al. arXiv:2009.01903
Stephen King, et.al. arXiv:2005.13549
Bhupal Dev, et.al. arXiv:1602.04203
Astrid Eichhorn et.al. arXiv:2010.00017

Yuefeng Di, et. al., arXiv: 2012.15625
Haipeng An, et.al. arXiv:2009.12381
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More general cases



Schematic phase transition GW spectra for SKA-like and LISA-like experiments to explore DM and baryogenesis

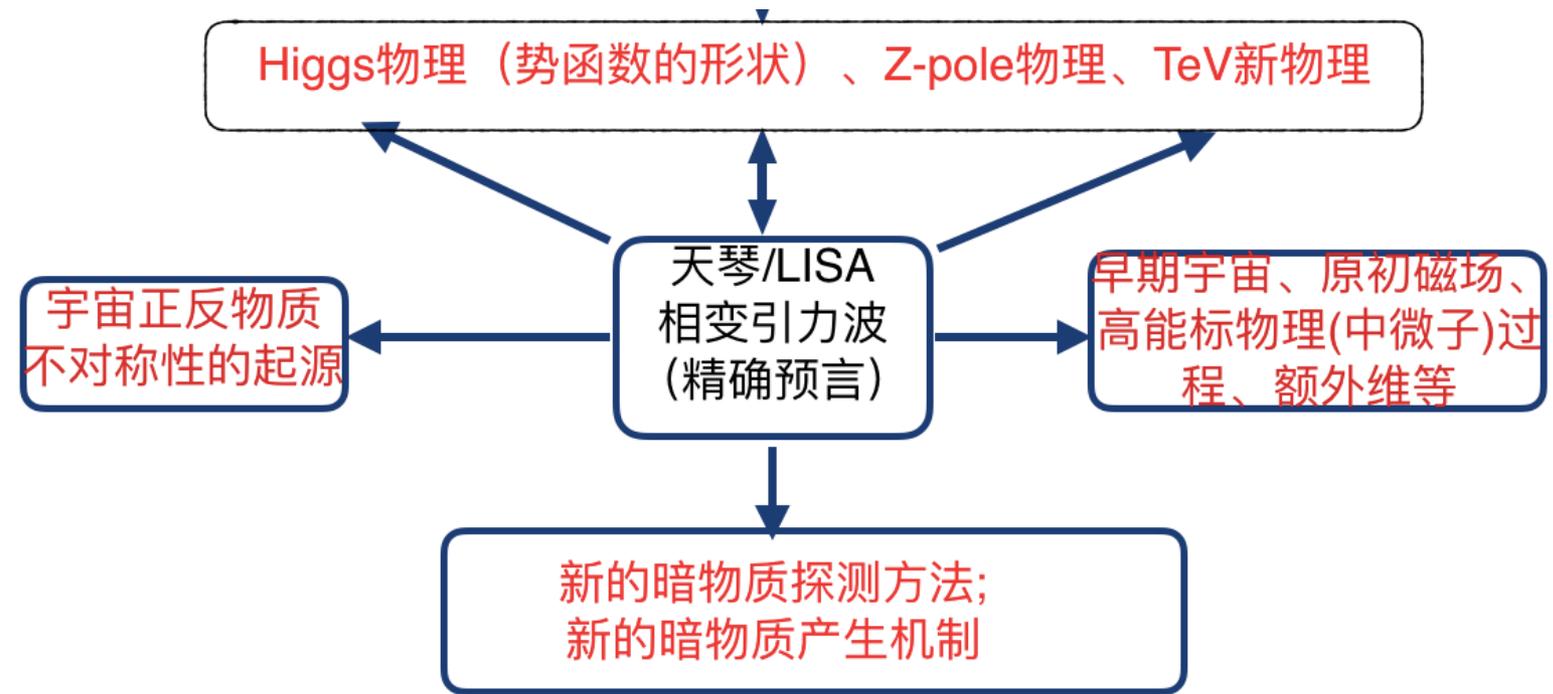
FPH, Xinmin Zhang, Physics Letters B 788 (2019) 288-294



总结与展望



- 从理论角度相变引力波能给提供探索Higgs、TeV新物理、暗物质、宇宙正反物质不对称性的起源等新的方法.
- 从实验角度国际国内空间引力波实验的快速推进，使这些研究有实验验证.



感谢您的参加!



地球
Earth

月球
Moon

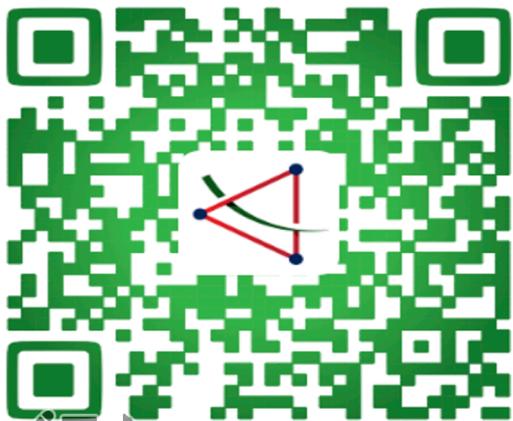
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太阳
Sun

水星
Mercury

金星

微信公众号

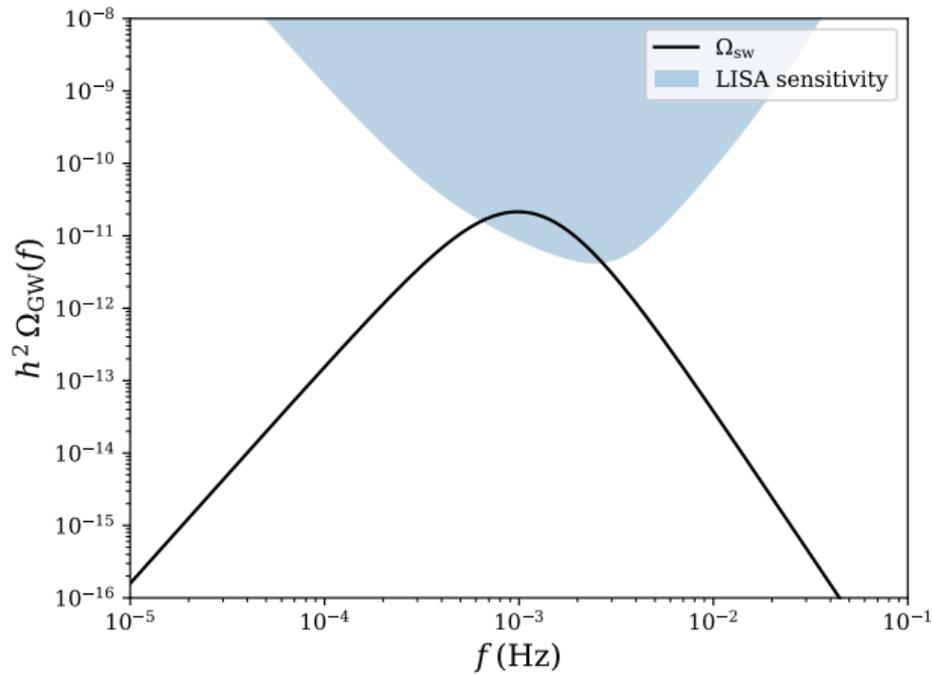


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激光测距台站





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LISA
CosWG-19-04

DESY 19-159

IPPP/19/27

HIP-2019-14/TH

MITP/19-066

IFT-UAM/CSIC-19-139

Detecting gravitational waves from cosmological phase transitions with LISA: an update

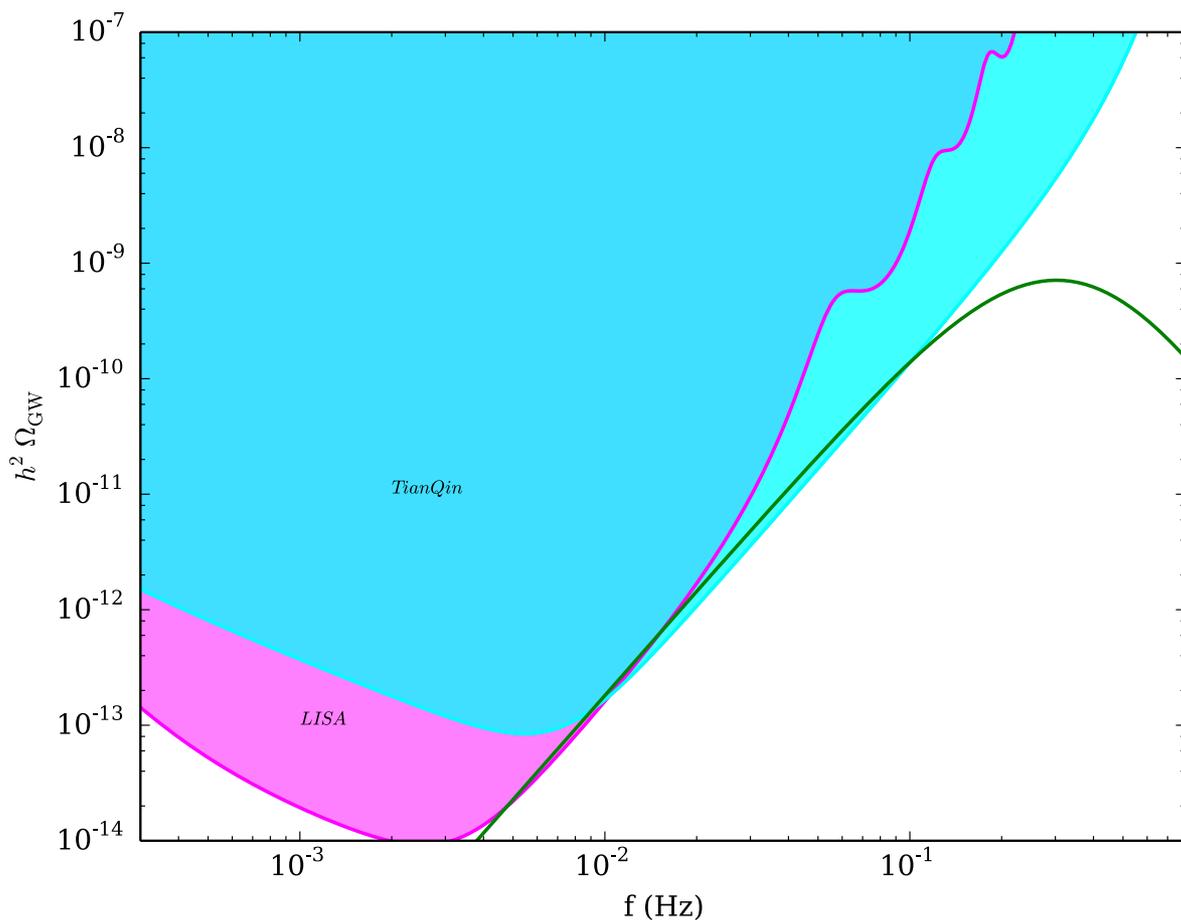
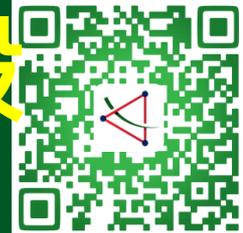
“Our results emphasize LISA’s importance for exploring the early Universe and BSM physics, as well as the Mission’s complementarity with other experimental efforts.”

For the LISA Cosmology Working Group

JCAP03(2020)024



天琴探测相变引力波的优势频段



FPH, Xinmin Zhang, Physics Letters B 788 (2019) 288-294