

# New physics at muon collider

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# Outline

- Why a muon collider?
- Production features and new physics at muon collider
- Summary

# Why a muon collider?

- The past and ongoing particle colliders (LEP,  $Spp\bar{p}S$ , PETRA, SPEAR, SLC, Tevatron, and LHC) made important measurements for the SM and BSM. They have so far seen no conclusive evidence of BSM phenomena.
- The quest for discovery in particle physics has always required higher energy experiments.



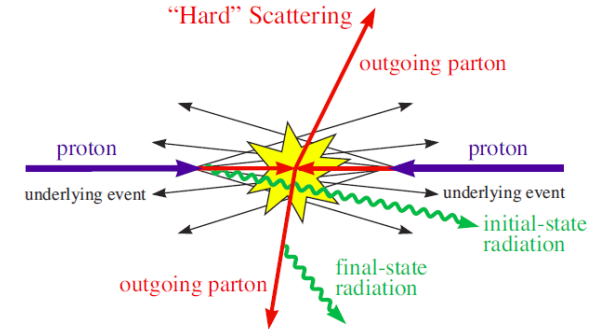
What kind of environment is ideal?

- The key factor to the collider energy: energy loss

$$\Delta E \propto \left(\frac{E}{m}\right)^4$$

- An accelerator is more efficient for a more massive beam particle.
- Large muon mass ( $m_\mu/m_e \approx 207$ ) suppresses the synchrotron radiation by a factor of  $10^9$ , compared with electron beams.
- Circular muon colliders with smaller ring size have the potential to reach tens of TeV c.m. energies.

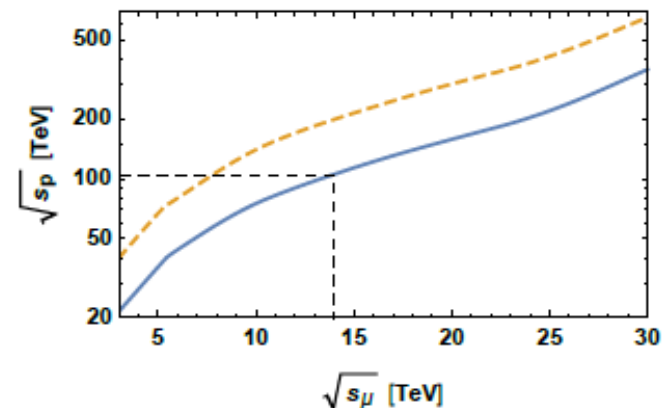
- In hadronic collisions, only a fraction of the total c.m. energy is carried by the partons.



- The muon collider c.m. energy can be fully converted into the physics threshold.

- A 14 TeV muon collider has potential similar to that of a 100 TeV pp collider.

- Lower background



- The idea of muon collider introduced in 1980's.

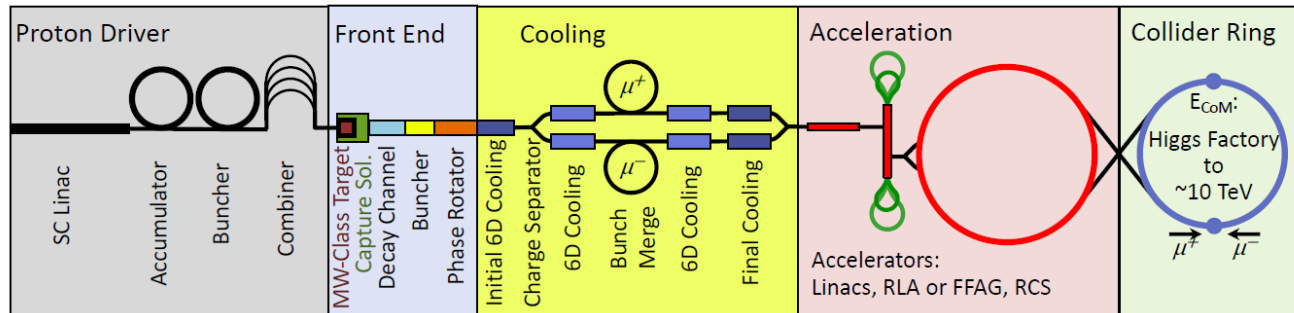
Skrinsky, Parkhomchuk, Sov.J.Part.Nucl.12(1981)223

Neuffer, Part.Accel.14 (1983) 75-90, AIP Conf.Proc.156(1987)201-208

Barger, Berger, Gunion, Han, PRL75(1995)1462-1465, Phys.Rept.286(1997)1-51

- Proton/positron driver scheme, e.g. proton

1901.06150



Muon  
Accelerator  
Program (MAP)

- Short lifetime ( $2 \mu\text{s}$ ) and **cooling**
- Luminosity scaling scheme:  $\sigma L \sim \text{const.}$  and luminosity goals

MICE collaboration,  
Nature 578(2020)53

$$L \gtrsim \frac{5 \text{ years}}{\text{time}} \left( \frac{\sqrt{s}_\mu}{10 \text{ TeV}} \right)^2 2 \cdot 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$$

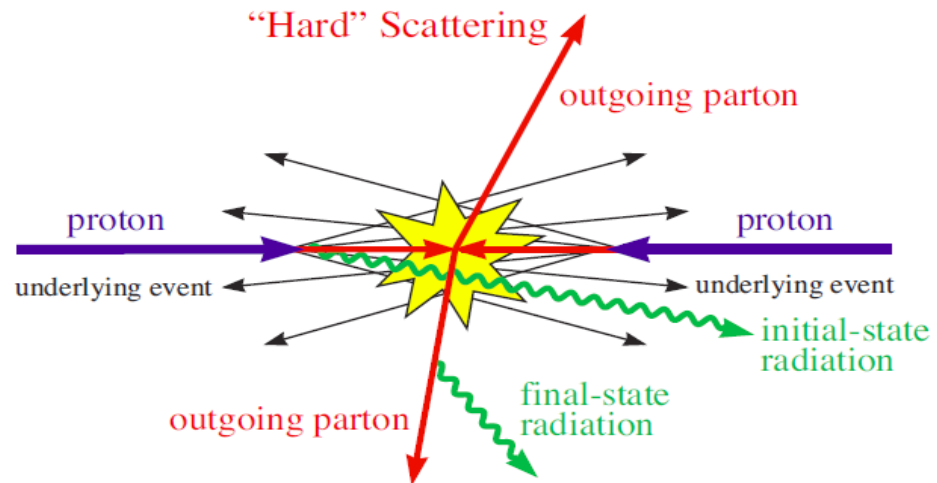
**1 ab<sup>-1</sup>/yr**

Target integrated luminosities	
$\sqrt{s}$	$\int \mathcal{L} dt$
3 TeV	1 ab <sup>-1</sup>
10 TeV	10 ab <sup>-1</sup>
14 TeV	20 ab <sup>-1</sup>

1901.06150

# Production at high-energy lepton colliders

- Recall the hadron colliders:  $pp(p\bar{p})$  collision at Tevatron or LHC



Factorization formalism: PDFs  $\otimes$  partonic cross sections

$$\sigma(AB \rightarrow X) = \sum_{a,b} \int dx_a dx_b f_{a/A}(x_a, Q) f_{b/B}(x_b, Q) \hat{\sigma}(ab \rightarrow X)$$

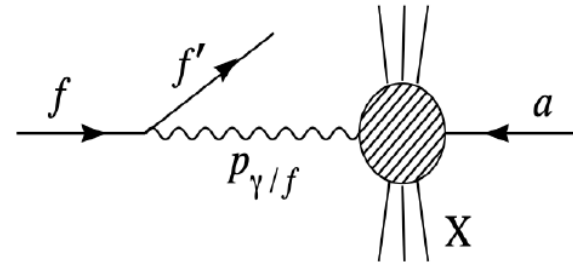
- $a, b$  are the “partons” from the beam particles  $A, B$
- $f_{a/A}(f_{b/B})$  are PDFs, defined as the probabilities of finding partons  $a$  ( $b$ ) from the beam particles  $A$  ( $B$ ) with the momentum fractions  $x_a(x_b)$

- The simplest parton of a lepton: photon
- “Equivalent photon approximation (EPA)”: collinear photon radiation off the high-energy leptons

C.F.von Weizsacker, Z.Phys.88,612(1934), E.J.Williams, Phys.Rev.45,729(1934)

$$\sigma(\ell^- + a \rightarrow \ell^- + X) = \int dx f_{\gamma/\ell} \hat{\sigma}(\gamma a \rightarrow X)$$

$$f_{\gamma/\ell, \text{EPA}}(x_\gamma, Q^2) = \frac{\alpha}{2\pi} \frac{1 + (1 - x_\gamma)^2}{x_\gamma} \ln \frac{Q^2}{m_\ell^2}$$



- Production cross section at lepton colliders

$$\sigma(\ell^+ \ell^- \rightarrow F + X) = \int_{\tau_0}^1 d\tau \sum_{ij} \frac{d\mathcal{L}_{ij}}{d\tau} \hat{\sigma}(ij \rightarrow F), \quad \tau = \hat{s}/s$$

Partonic luminosities

$$\frac{d\mathcal{L}_{ij}}{d\tau} = \frac{1}{1 + \delta_{ij}} \int_{\tau}^1 \frac{d\xi}{\xi} \left[ f_i(\xi, Q^2) f_j\left(\frac{\tau}{\xi}, Q^2\right) + (i \leftrightarrow j) \right]$$



# beyond the EPA

- Ultra-high energy  $Q \gg M_Z$ :  $\frac{v}{E} = \frac{v}{10 \text{ TeV}} \rightarrow 0$
- The SM gauge symmetry is restored and all EW states are dynamically activated.
- We should take into account the four EW gauge bosons ( $B, W^i$ ), EW partons emerge

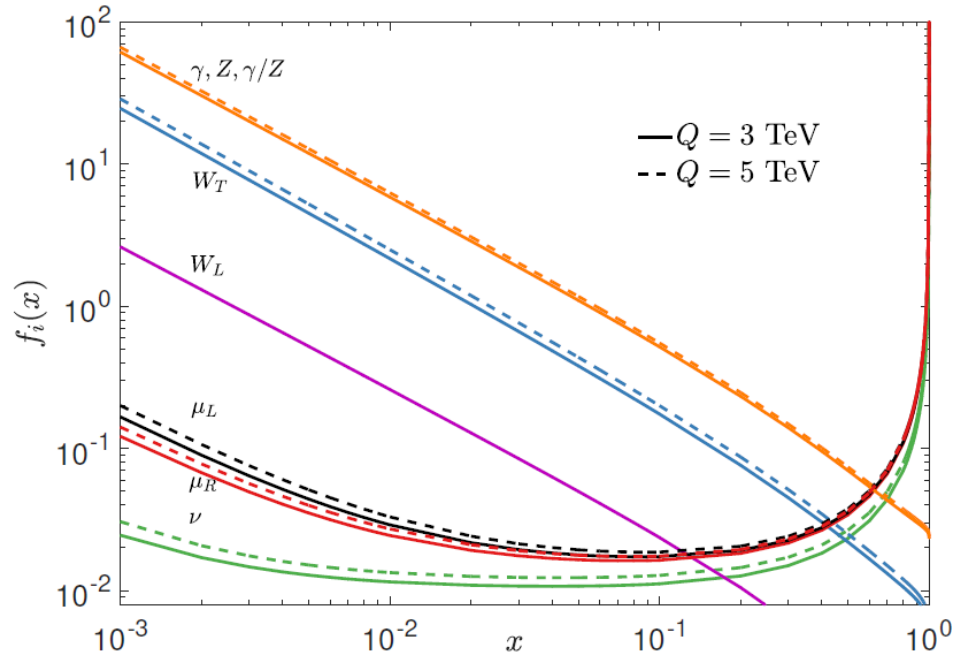
“Effective W Approximation (EWA)”: EW PDF

G.Kane, W.Repko, W.Rolnick, PLB148(1984)367; S.Dawson NPB 249(1985)42



- EW PDFs for muon collider

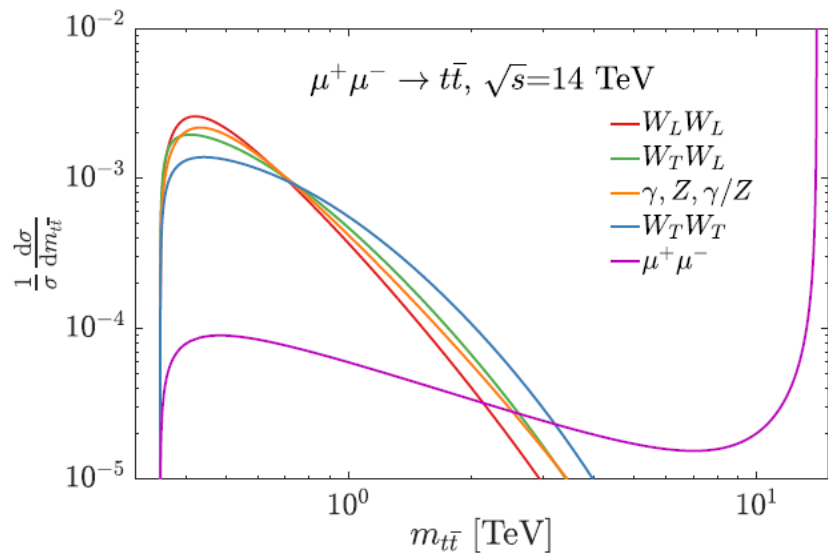
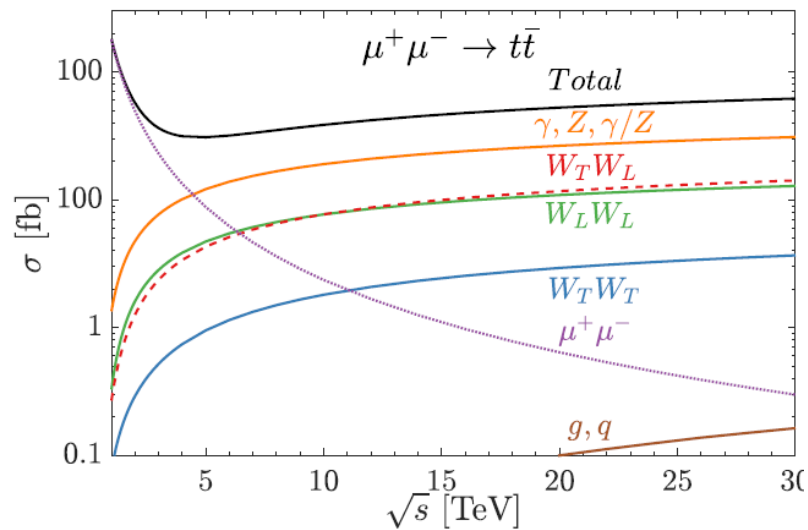
T. Han, Y. Ma, K. Xie, 2007.14300



- The muon PDF peaks at collider energy  $x \approx 1$ .
- The gauge boson PDFs are dominant at low partonic energy.

# Inclusive production cross section

T. Han, Y. Ma, K. Xie, 2007.14300



- sum over all partonic contributions and calculate the inclusive production cross section, e.g.  $t\bar{t}$
- The direct annihilation falls as  $1/s$  and VBF takes over it at high energies
- The invariant mass peaks at collider energy for annihilation and the VBF peaks above the threshold
- The contributions from polarized initial states are available to explore the underlying physics.

# New physics examples at muon collider

- A high-energy muon collider allows to probe unprecedented energy scales and explore many different directions
- Great interest in the theory community:

## High-energy searches:

resonances,  
di-boson, di-fermion,  
Dark Matter, etc

## High-rate measurement:

single Higgs, self coupling,  
rare Higgs decays, EFT, etc

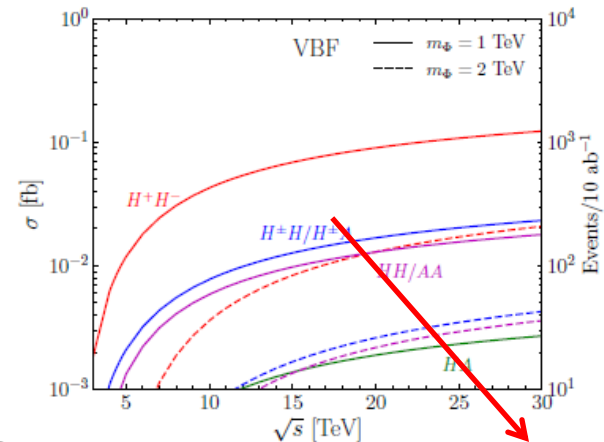
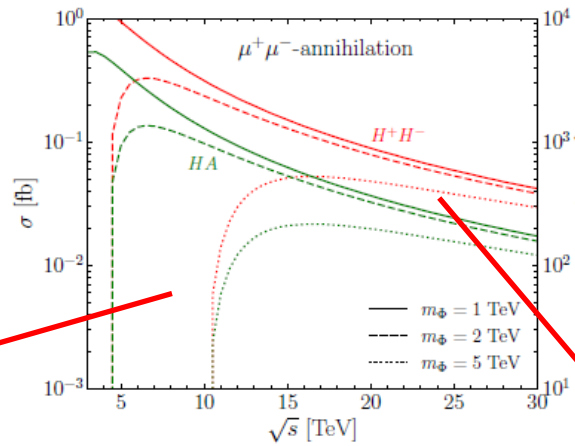
## Muon physics:

lepton flavor universality,  
muon  $g-2$ ,  $b \rightarrow s\mu\mu$ , etc

# Example 1: heavy particle search

- heavy higgs bosons

arXiv: 2102.08386

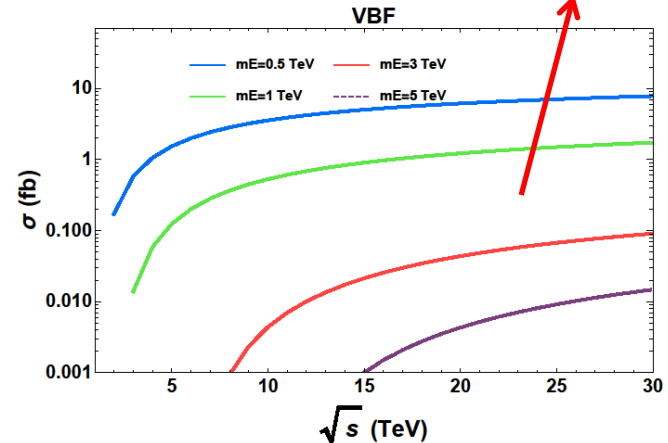
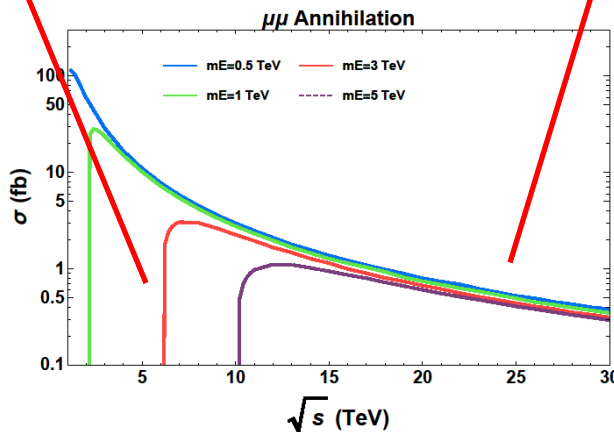


threshold behavior:  
 $\beta^3$  or  $\beta$  with  
 $\beta = \sqrt{1 - M^2/s}$

$\sigma \sim 1/s$

EW PDF threshold suppression:  $1/M^2$

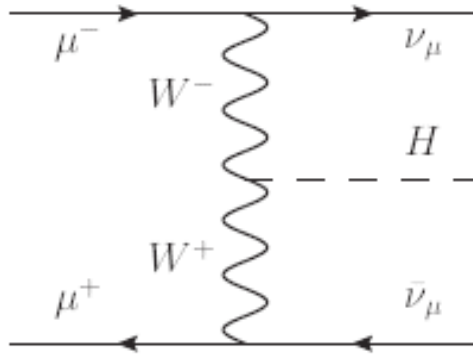
- heavy charged leptons



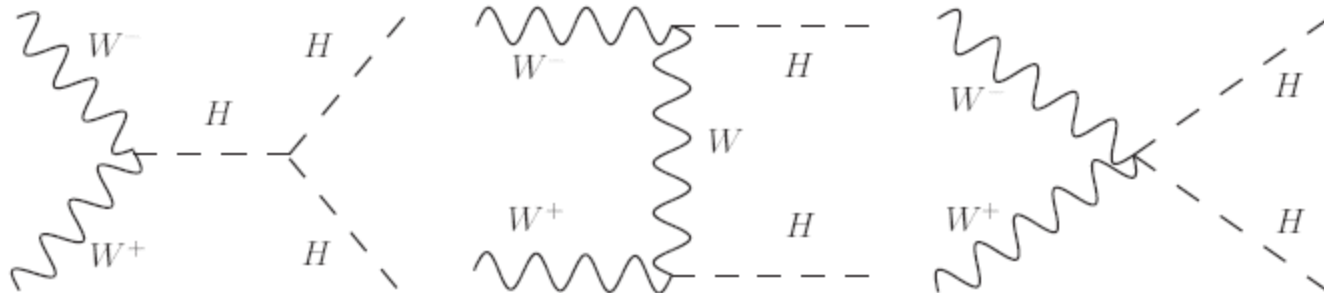
# Example 2: precision Higgs measurement

arXiv: 2008.12204

- $WWH/ZZH$  couplings: single production



- $HHH/WWHH$  couplings: pair production



$\sqrt{s}$ (lumi.)	3 TeV (1 ab <sup>-1</sup> )	6 (4)	10 (10)	14 (20)	30 (90)	Comparison
$WWH$ ( $\Delta\kappa_W$ )	0.26%	0.12%	0.073%	0.050%	0.023%	0.1% [41]
$\Lambda/\sqrt{c_i}$ (TeV)	4.7	7.0	9.0	11	16	(68% C.L.)
$ZZH$ ( $\Delta\kappa_Z$ )	1.4%	0.89%	0.61%	0.46%	0.21%	0.13% [17]
$\Lambda/\sqrt{c_i}$ (TeV)	2.1	2.6	3.2	3.6	5.3	(95% C.L.)
$WWHH$ ( $\Delta\kappa_{W_2}$ )	5.3%	1.3%	0.62%	0.41%	0.20%	5% [36]
$\Lambda/\sqrt{c_i}$ (TeV)	1.1	2.1	3.1	3.8	5.5	(68% C.L.)
$HHH$ ( $\Delta\kappa_3$ )	25%	10%	5.6%	3.9%	2.0%	5% [22, 23]
$\Lambda/\sqrt{c_i}$ (TeV)	0.49	0.77	1.0	1.2	1.7	(68% C.L.)

- Compared with the precision of other proposed colliders, muon collider can improve the measurements substantially

See also Junmou Chen's talk

# Summary

- High-energy muon colliders are potentially ideal machines in both energy and precision frontiers.
- Muon collider can become good candidate of future colliders and comprehensively cover SM and BSM physics of interest.



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Thank you!

- EW DGLAP equations

$$\frac{df_i}{d \log Q^2} = \sum_I \frac{\alpha_I}{2\pi} \sum_j P_{ij}^I \otimes f_j$$

- EW PDFs:  $f_i(x, Q^2)$
- $I$ : gauge group
- $P$ : splitting function