



Heavy flavor jets and their substructure

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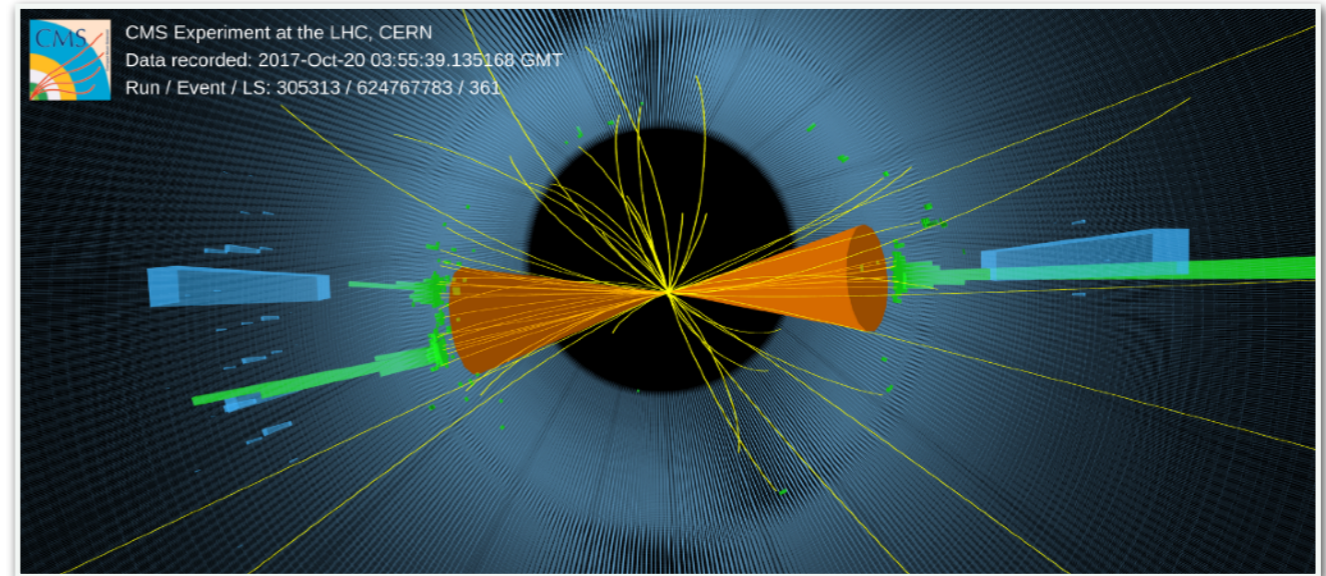
Motivation

Heavy flavor jet production is crucial in both QCD and EW/BSM physics

EW/BSM: b-jet signature is common in many EW/BSM processes, top quark, Higgs ...

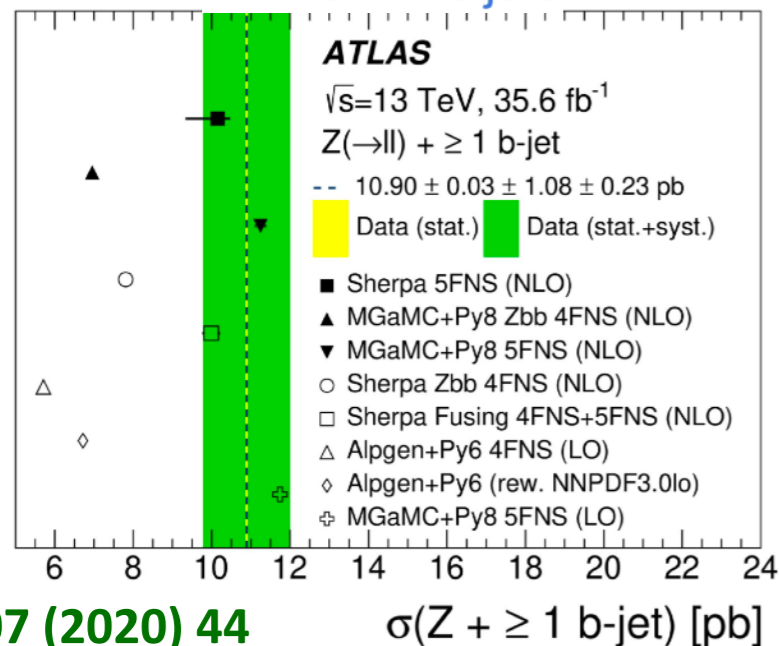
Q: Can you distinguish these two jets?

A: left is a Higgs jet, right is a standard QCD jet. Higgs jet has two prongs inside the jet [b + b-bar jets]

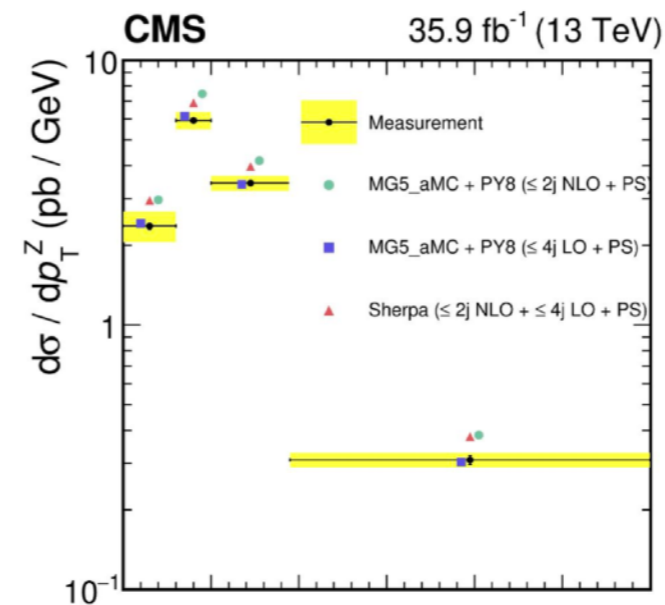


QCD: understanding heavy quark effects; mass corrections; flavor schemes ...

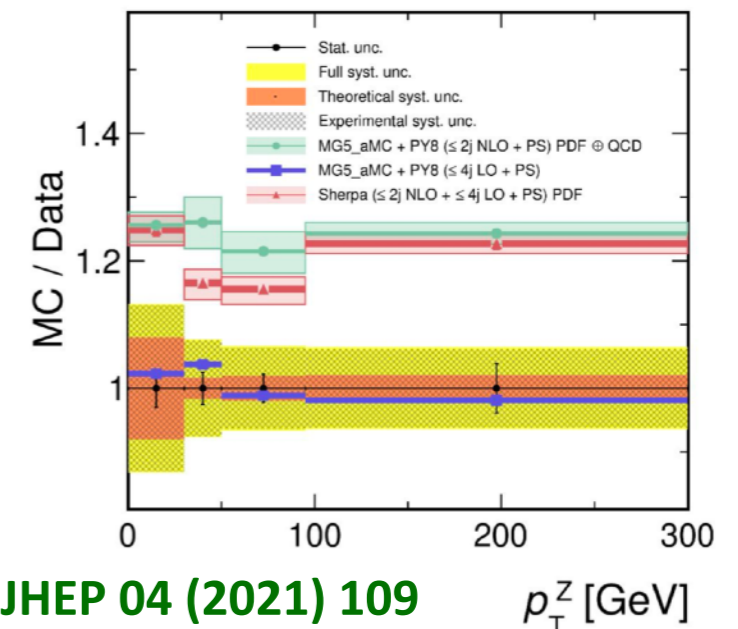
ATLAS Z + b-jets



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CMS Z+c

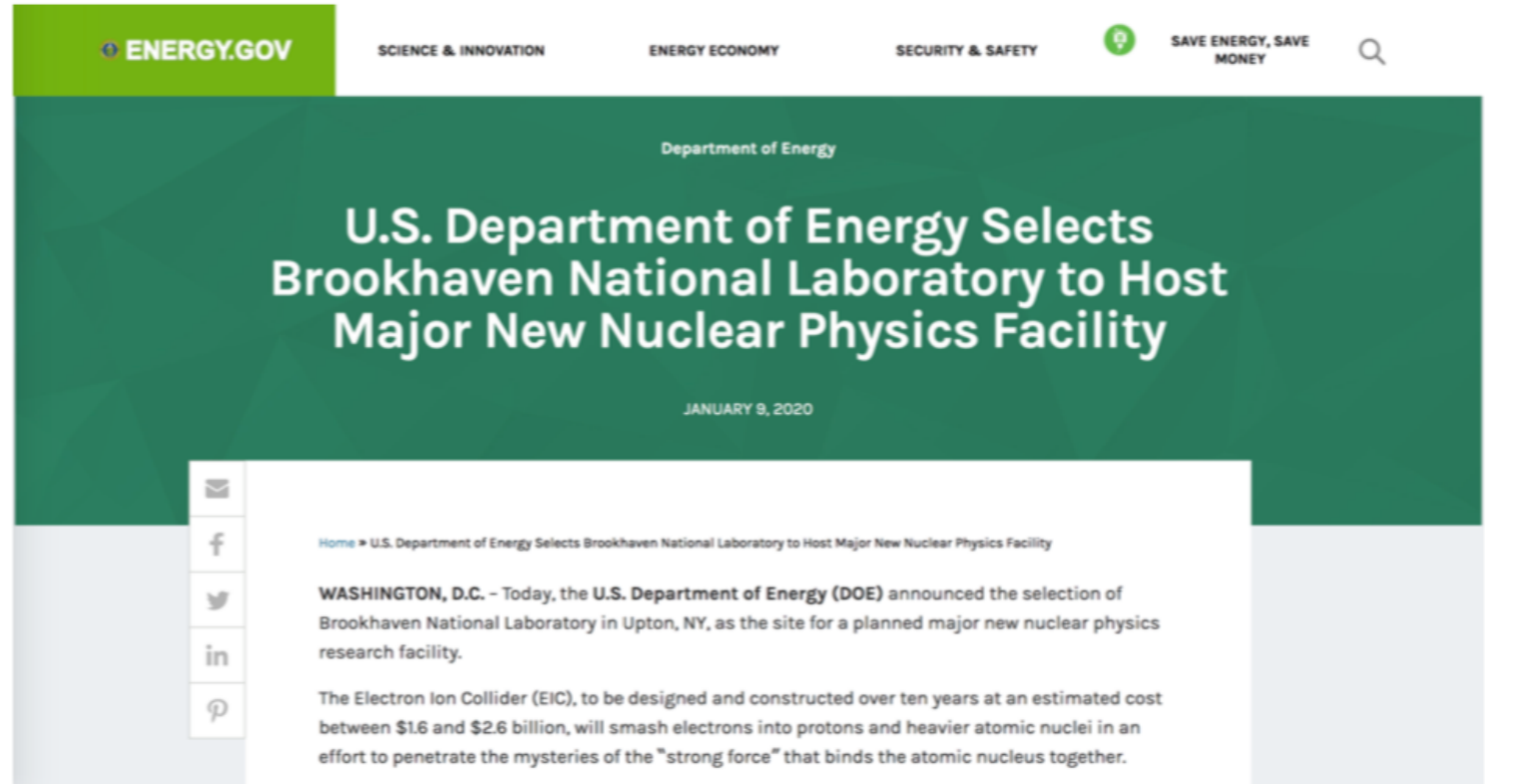


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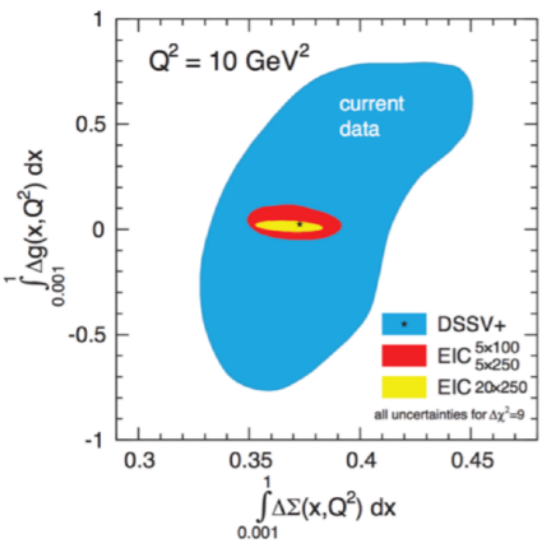
The Electron-Ion Collider

January 9, 2020

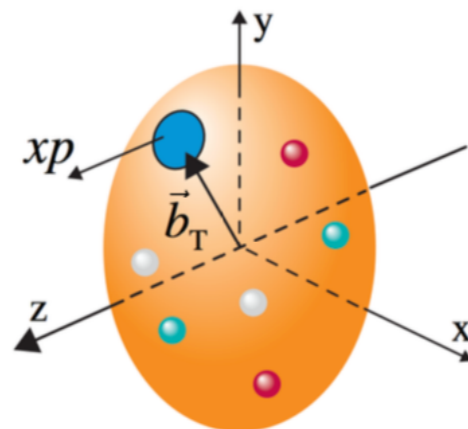
- High luminosity
 $10^{33-34} \text{ cm}^{-2} \text{ s}^{-1}$
- Center-of-mass energy
 $\sqrt{s} = 20 - 140 \text{ GeV}$
- Highly polarized beams
- Electron-proton/nucleus collisions



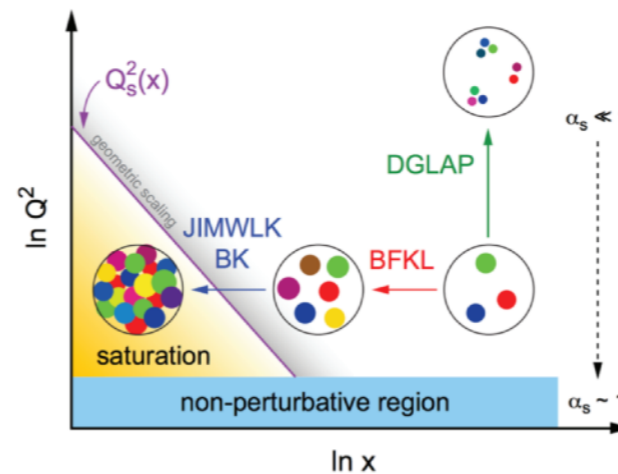
Proton spin



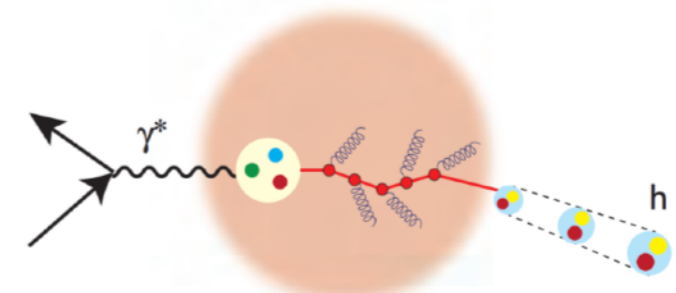
3D nucleon tomography



gluon saturation

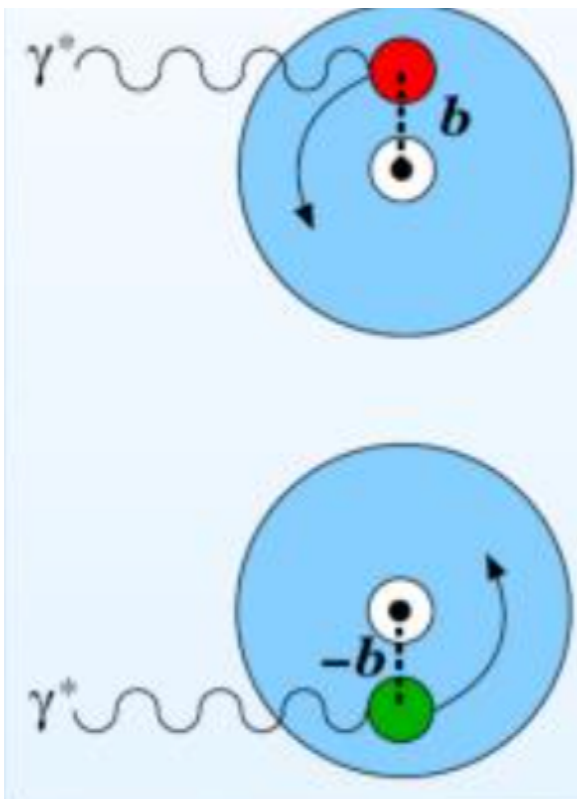


hadronization in the nucleus



3D imaging of the proton

- Both longitudinal and transverse motion
- Large Lorentz boost in longitudinal direction, but not in transverse momentum
- Correlation between nucleon **spin** with parton(quark, gluon) **orbital angular momentum**



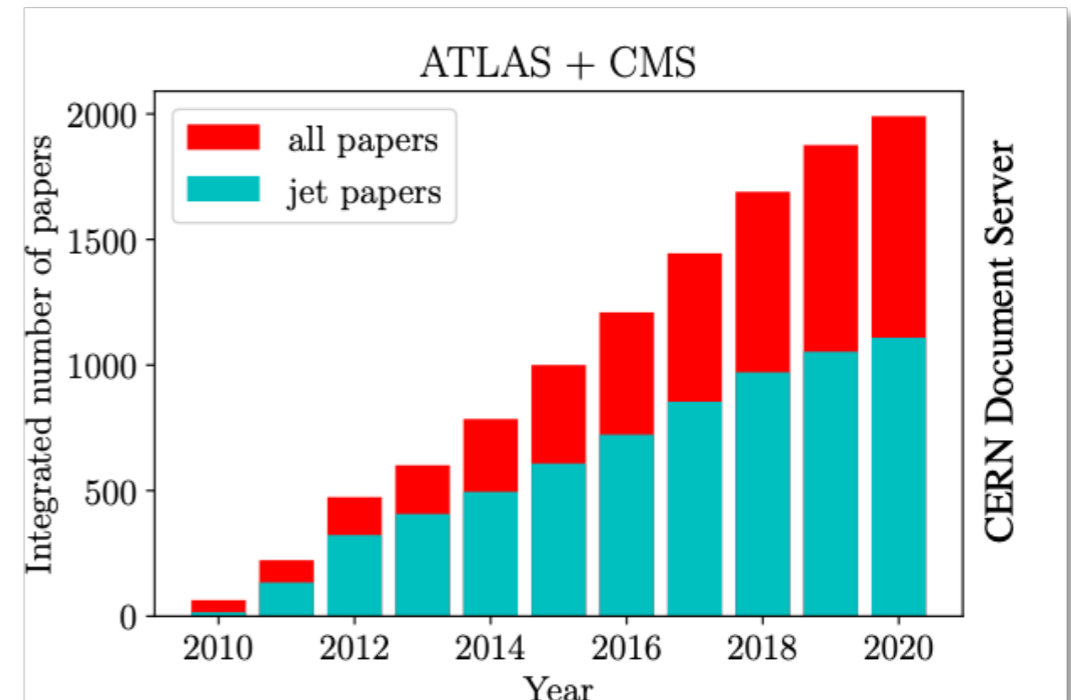
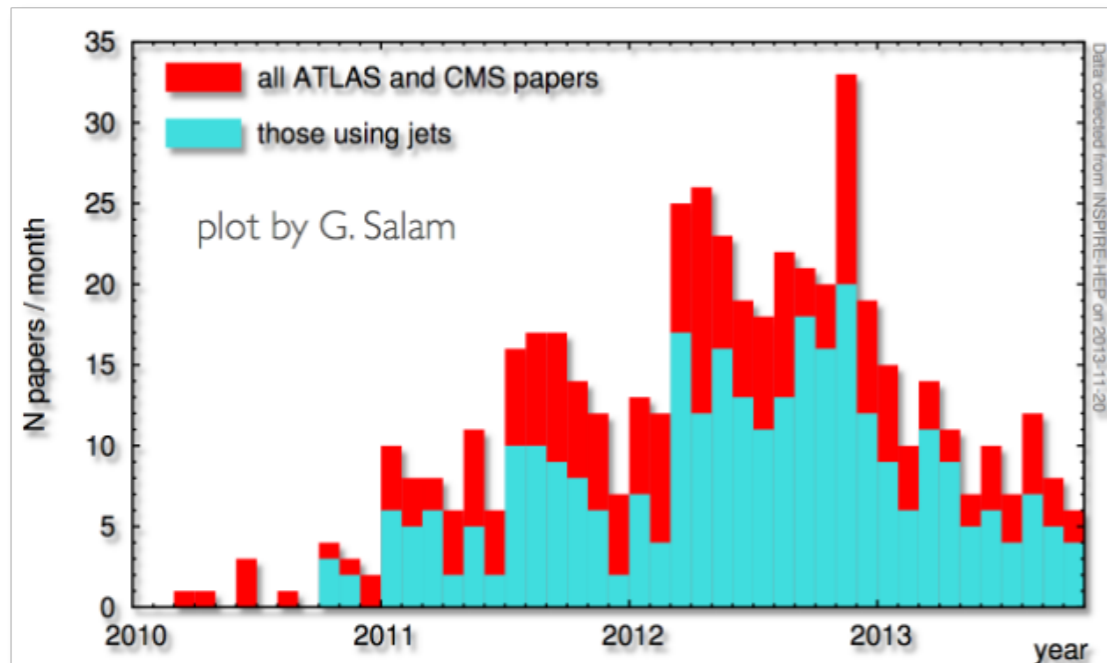
TMDs		Quark Polarization		
		Unpolarized (U)	Longitudinally polarized (L)	Transversely polarized (T)
Nucleon Polarization	U	f_1 unpolarized		h_1^\perp Boer-Mulders
	L		g_{1L} helicity	h_{1L}^\perp longi-transversity
	T	f_{1T}^\perp Sivers	g_{1T} trans-helicity	h_1 transversity h_{1T}^\perp pretzelosity

Nucleon spin
 Quark spin

Figure 2.5: The leading-twist quark TMD distributions.

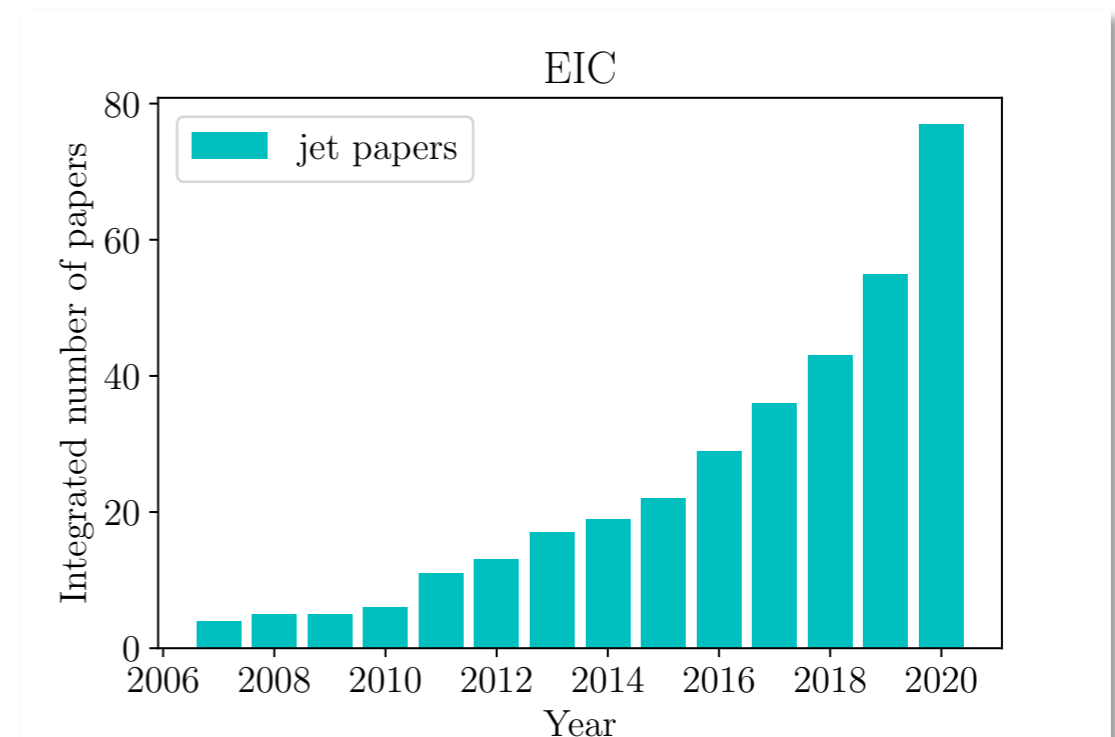
Jets are most common at the LHC

At the LHC, 70% of ATLAS & CMS papers use jets in their analysis



Active study at the EIC

EIC jet papers grow exponentially



Gluon Sivers function (GSF)

- Gauge link** dependent gluon Transverse-momentum-dependent PDFs

$$\Gamma^{[U,U']\mu\nu}(x, p_T; n) = \int \frac{d\xi \cdot P d^2\xi_T}{(2\pi)^3} e^{ip \cdot \xi} \langle P, S | F^{n\mu}(0) U_{[0,\xi]} F^{n\nu}(\xi) U'_{[\xi,0]} | P, S \rangle \Big|_{\text{LF}}$$

- GSF: T-odd object; two gauge links; process dependence more involved**
- For any process GSF can be expressed in terms of two functions:**

$$f_{1T}^{\perp g[U]}(x, \mathbf{k}_\perp^2) = \sum_{c=1}^2 C_{G,c}^{[U]} f_{1T}^{\perp g(Ac)}(x, \mathbf{k}_\perp^2)$$

(Buffing, Mukherjee, Mulders'13)

- $f_{1T}^{\perp g(f)}$ **f-type, C-even**
- $f_{1T}^{\perp g(d)}$ **d-type, C-odd**

calculable for each channel



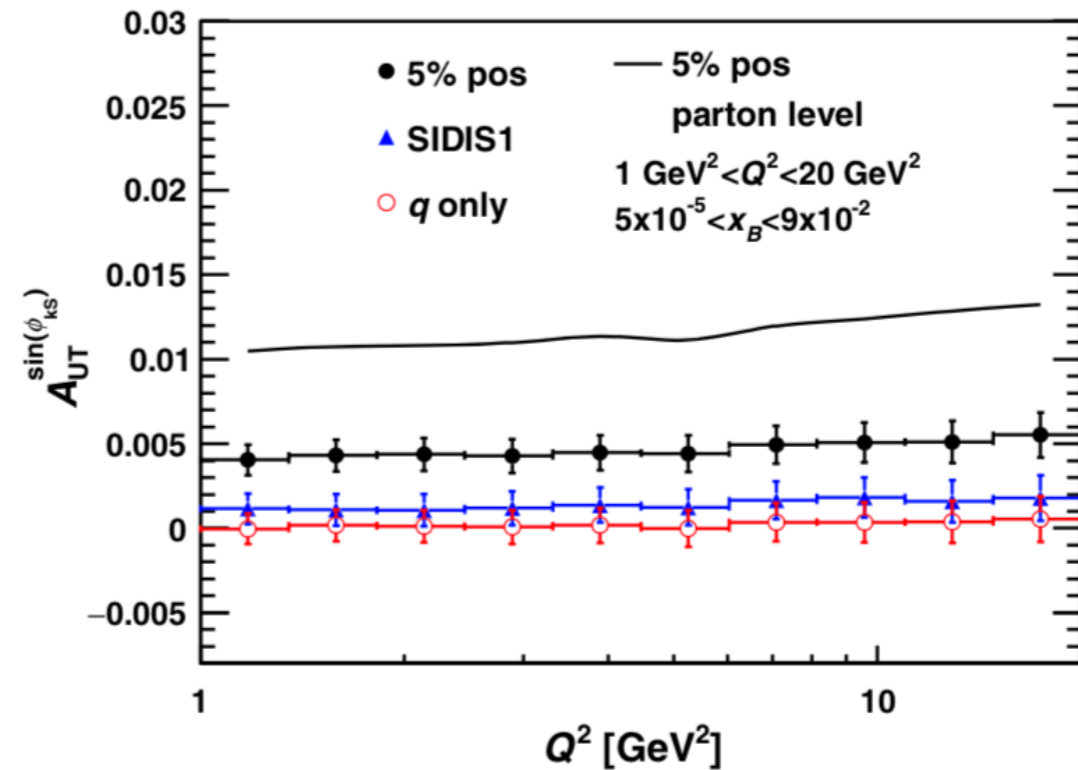
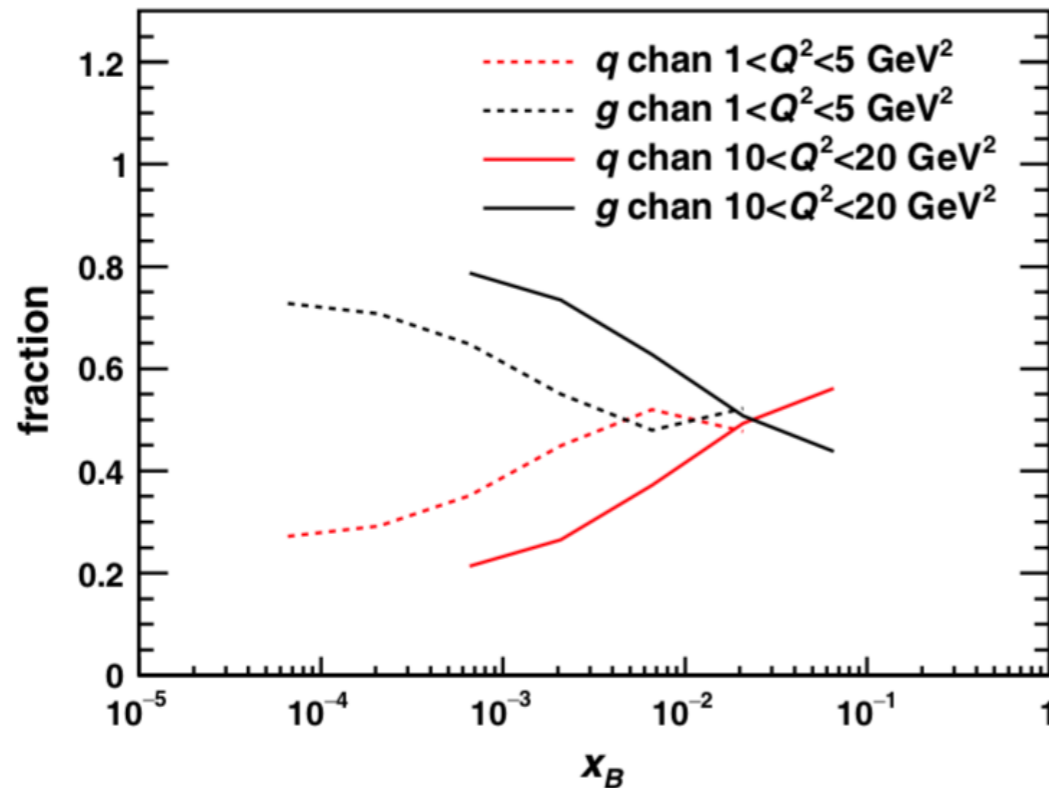
$$f_{1T}^{\perp g[e p^\uparrow \rightarrow e' Q\bar{Q} X]}(x, p_T^2) = -f_{1T}^{\perp g[p^\uparrow p \rightarrow \gamma\gamma X]}(x, p_T^2)$$

GSF and spin asymmetry in di-jet at the EIC

At the EIC , accessing of GSF via high- p_T dihadron, open di-charm, di-D-meson and dijet has been investigated using PYTHIA and reweighing methods in Zheng, Aschenauer, Lee, Xiao, Yin '18

- They find that dijet process is the most promising channel

At the LO di-jet production in DIS involves two processes: $\gamma^* q \rightarrow qg$ $\gamma^* g \rightarrow q\bar{q}$

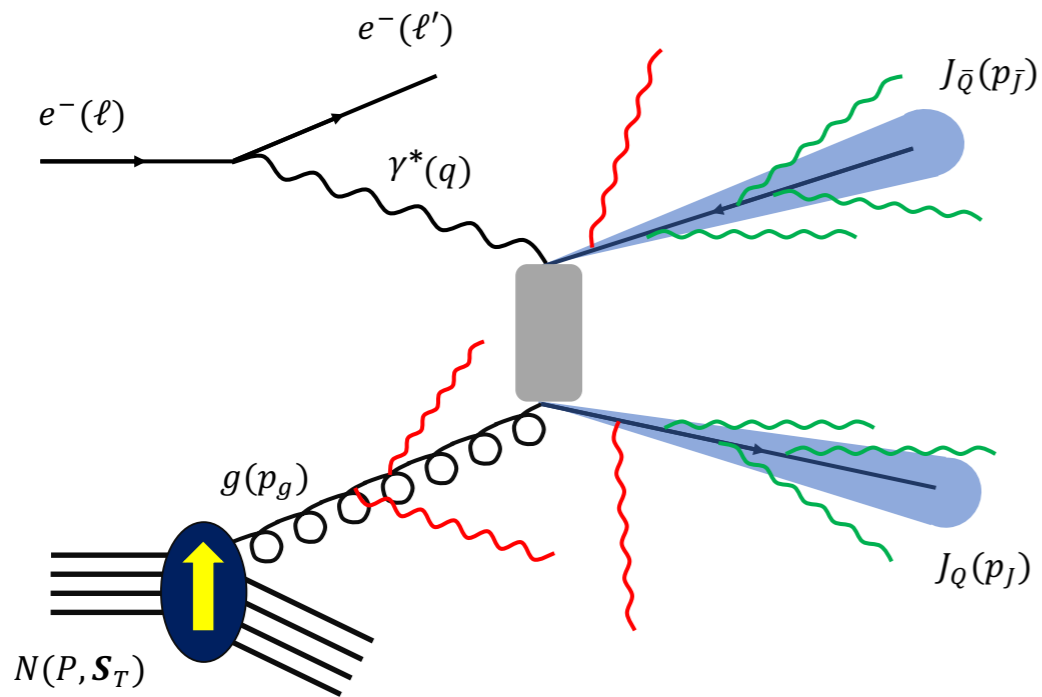


- to distinguish different TMDs
 - jet charge tagging “different quark TMDs” (Kang, Liu, Mantry, DYS '20 PRL)
 - Heavy-flavor tagging, where q-channel starts to contribute beyond the LO (Kang, Reiten, DYS, Terry '21 JHEP)

TMD factorization for heavy-flavor dijet production in DIS

(Kang, Reiten, **DYS**, Terry '21 JHEP)

$$e(\ell) + N(P, S_T) \rightarrow e(\ell') + J_Q(p_J) + J_{\bar{Q}}(p_{\bar{J}}) + X$$



In the Breit frame, the dijet imbalance is defined as $q_T = p_{JT} + p_{\bar{J}T}$

$$q_T R \ll q_T \lesssim m_Q \lesssim p_T R \ll p_T$$

R: Jet radius; m_Q : heavy quark mass

Construction of the theory formalism

- Multiple scales in the problem
- Rely on effective field theory: SCET + **Jet Effective Theory** (Becher, Neubert, Rothen, **DYS** '16 PRL, ...)

the factorized form of the spin-independent cross section

$$d\sigma^{UU} \sim H(Q, p_T) J_Q(p_T R, m_Q) J_{\bar{Q}}(p_T R, m_Q) S(\lambda_T) f_g(k_T) S_Q^c(l_{QT}) S_{\bar{Q}}^c(l_{\bar{Q}T}) \delta^{(2)}(k_T + \lambda_T + l_{QT} + l_{\bar{Q}T} - q_T)$$

- Hard and **soft** functions are the same as light-jet cases, since $p_T \gg m_Q$
- **Jet** and **collinear-soft** functions are new, which receive finite quark mass correction

Heavy quark mass corrections in the evolution equation

Anomalous dimension for the HF quark jet function: see also (Kim '20)

$$\Gamma^{jQ}(\alpha_s) = -C_F \gamma^{\text{cusp}}(\alpha_s) \ln \frac{m_Q^2 + p_T^2 R^2}{\mu^2} + \gamma^{jQ}(\alpha_s) \quad \gamma_0^{jQ} = 2C_F \left(3 - \frac{2m_Q^2}{m_Q^2 + p_T^2 R^2} \right)$$

Anomalous dimension for the HF collinear-soft function

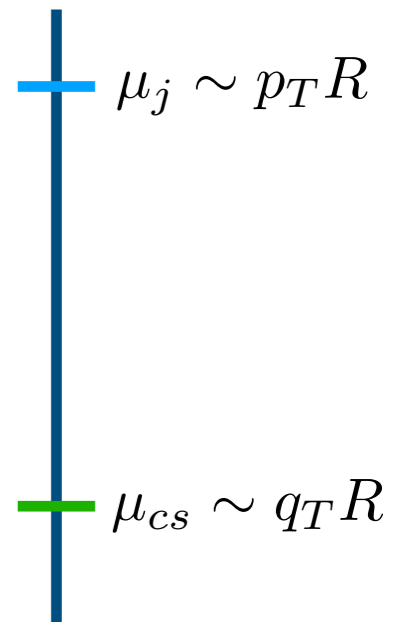
$$\Gamma^{csQ}(\alpha_s) = C_F \gamma^{\text{cusp}}(\alpha_s) \ln \frac{R^2 \mu_b^2}{\mu^2} + \gamma^{csQ}(\alpha_s) \quad \gamma_0^{csQ} = -4C_F \left[2 \ln [-2i \cos(\phi_b - \phi_J)] - \frac{m_Q^2}{m_Q^2 + p_T^2 R^2} - \ln \frac{m_Q^2 + p_T^2 R^2}{p_T^2 R^2} \right]$$

Heavy-quark mass dependence cancels out in

$$\Gamma^{jQ} + \Gamma^{csQ} = \Gamma^{j_q} + \Gamma^{cs_q}$$

Heavy quark mass will contribute the RG evolution between jet and collinear-soft function

different from the case for the inclusive HF quark jet production Dai, Kim, Leibovich '18



Spin dependent cross section

- Resummation formula:

$$\frac{d\sigma^{UT}(\mathbf{S}_T)}{dQ^2 dy d^2\mathbf{q}_T dy_J d^2\mathbf{p}_T} = \sin(\phi_q - \phi_s) H(Q, p_T, y_J, \mu_h) \int_0^\infty \frac{b^2 db}{4\pi} J_1(b q_T) f_{1T, g/p}^\perp(x_g, \mu_{b*})$$

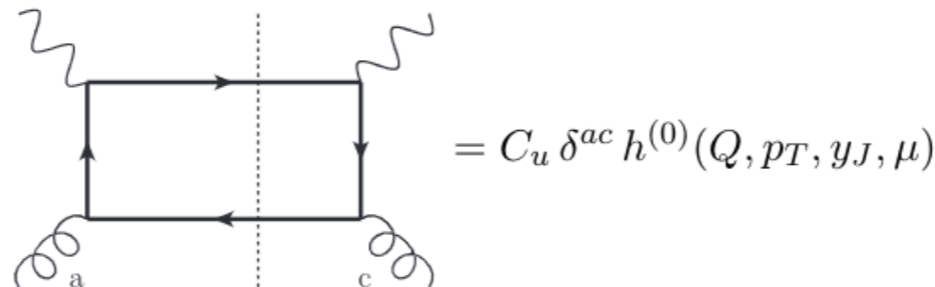
$$\times \exp \left[- \int_{\mu_{b*}}^{\mu_h} \frac{d\mu}{\mu} \Gamma^h(\alpha_s) - 2 \int_{\mu_{b*}}^{\mu_j} \frac{d\mu}{\mu} \Gamma^j(\alpha_s) - 2 \int_{\mu_{b*}}^{\mu_{cs}} \frac{d\mu}{\mu} \Gamma^{cs}(\alpha_s) \right]$$

$$\times \exp \left[-S_{\text{NP}}^\perp(b, Q_0, n \cdot p_g) \right]$$

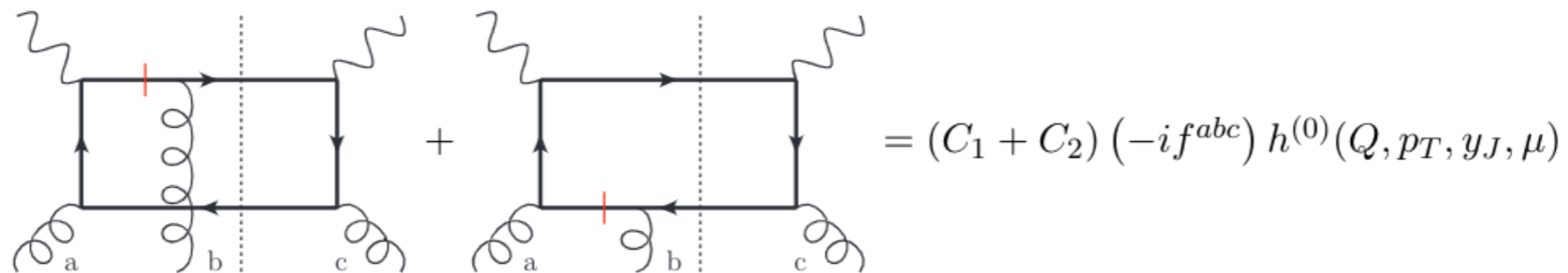
- Polarized hard function:** For the polarized process, we must consider the attachment of an additional gluon from gauge link in GSF

Qiu, Vogelsange, Yuan '07;
Kang, Lee, **DYS**, Terry, '20 JHEP ...

unpolarized:



polarized:



polarized and unpolarized hard functions are the same $C_1 + C_2 = C_u$

f-type gluon Sivers function

Numerical results

Anti- k_T , $R=0.6$

c-jets: $5 \text{ GeV} < p_T < 10 \text{ GeV}$, $|\eta_J| < 4.5$,

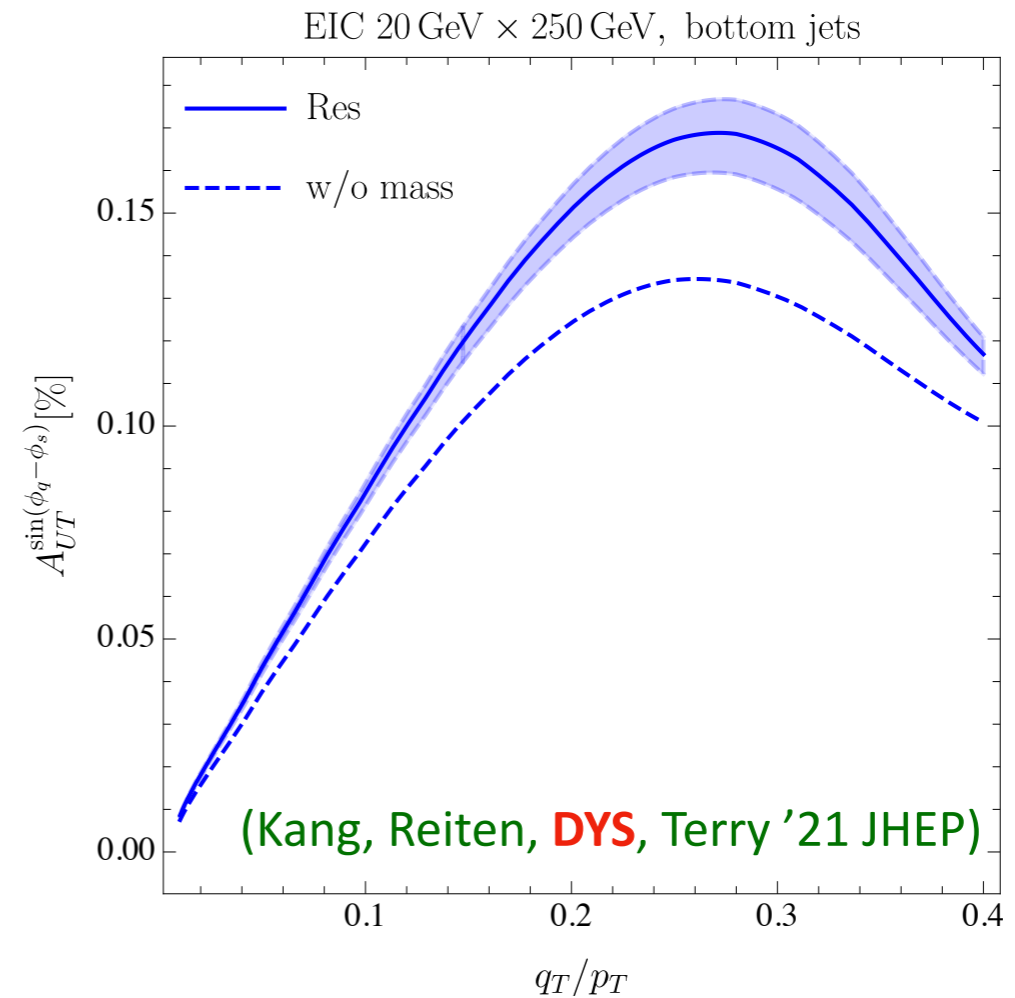
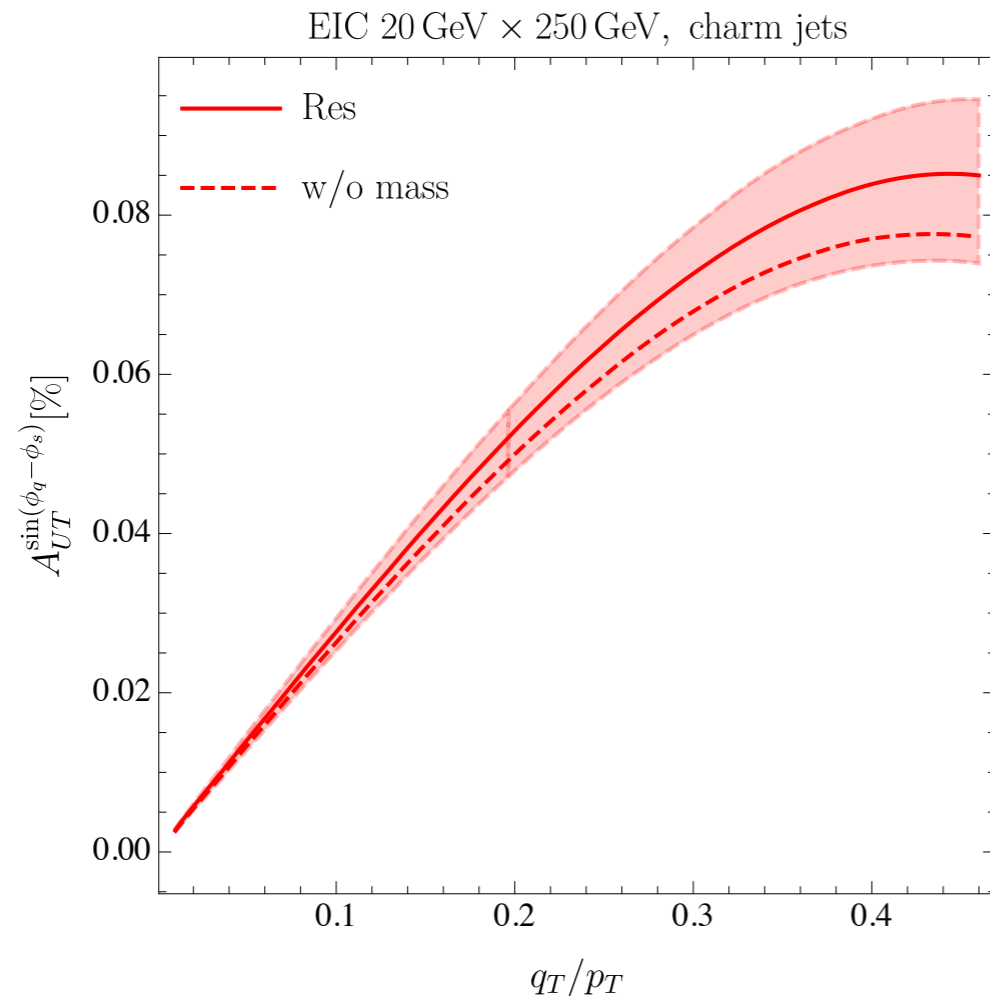
b-jets: $10 \text{ GeV} < p_T < 15 \text{ GeV}$, $|\eta_J| < 4.5$,

$$d\sigma(\mathcal{S}_T) = d\sigma^{UU} + \sin(\phi_q - \phi_s) d\sigma^{UT}$$

$$A_{UT}^{\sin(\phi_q - \phi_s)} = \frac{d\sigma^{UT}}{d\sigma^{UU}}$$

GSF: SIDIS1 set

D'Alesio, Murgia, Pisano '15



Heavy quark mass can give sizable corrections to the predicted asymmetry

Summary

- **Heavy flavor jets offer new opportunity to understand nucleon inner structures**
- **We develop the TMD factorization formalism for heavy flavor dijet production in electron polarized proton collisions.**
 - **Theory tools: EFT of QCD in collinear and soft limit (e.g. SCET)**
- **Flavor tagging provides a novel probe of flavor structure in the nucleon spin program**
 - **It enhances the sensitivity of spin asymmetries to gluon, which opens new avenues of exploration for the nucleon spin program**
- **The application of our theory framework at the LHC&RHIC is in progress**

Thank you