

Higgs potential and BSM opportunity 希格斯物理研讨会

Higgs Interactions in New Physics

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Peking University**

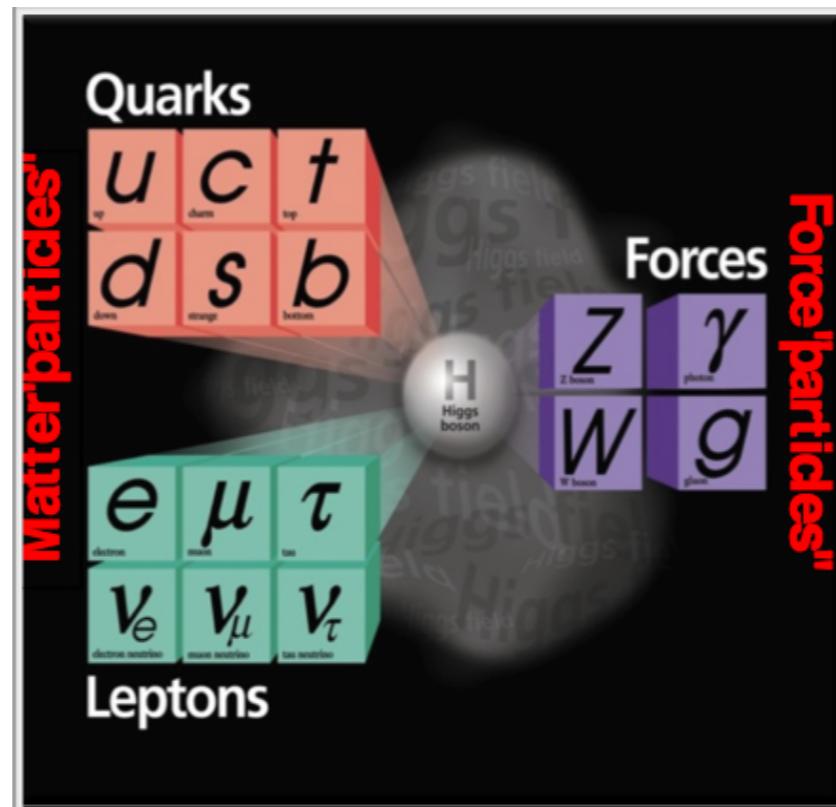
Aug 30, 2021

What can Higgs Boson tell us?

Higgs-self couplings
 HHH and $HHHH$

HFF coupling

Magnitude and CP



HVV coupling

Relation between
 M_W and M_Z
(custodial Symmetry)

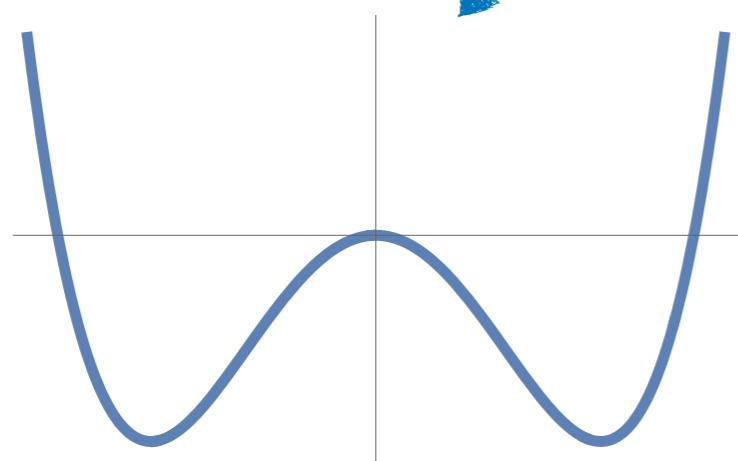
Relation between
 HVV and $HHVV$
couplings

The Higgs boson is important not only for EWSB,
but also as a WINDOW to NP beyond the SM.

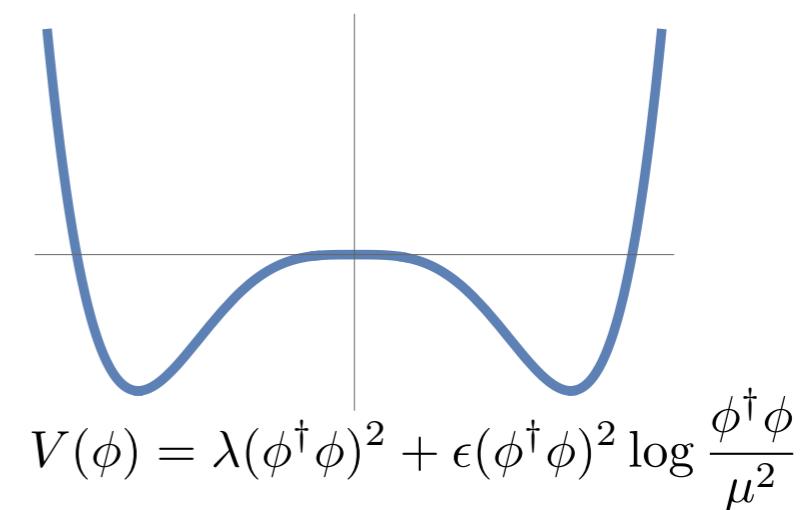
1. Higgs-self Interaction

(probing potential at electroweak scale)

$$V(\phi) = -\mu^2\phi^2 + \lambda(\mu)\phi^4 + \frac{\kappa(\mu)}{\Lambda^2}\phi^6 + \dots$$



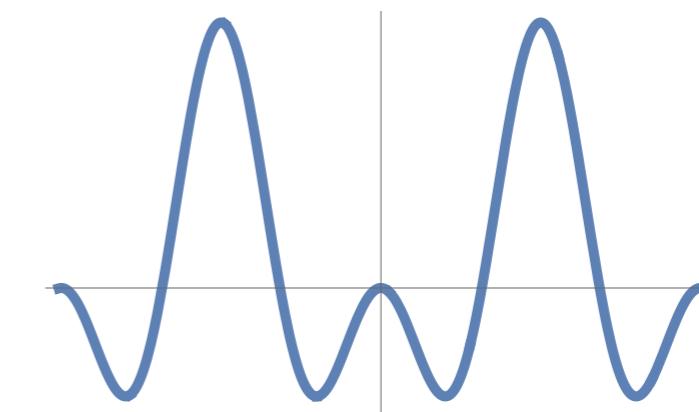
Coleman-Weinberg Higgs



Pseudo-Goldstone Higgs

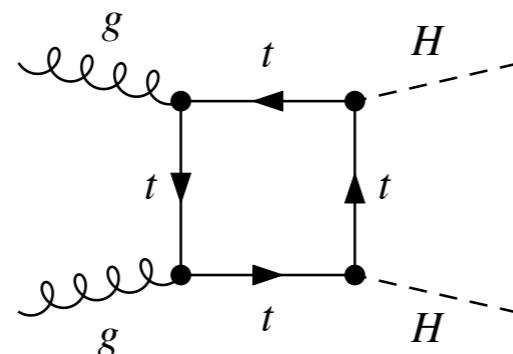
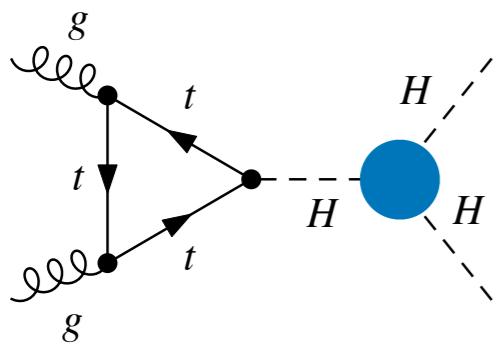


The LHC

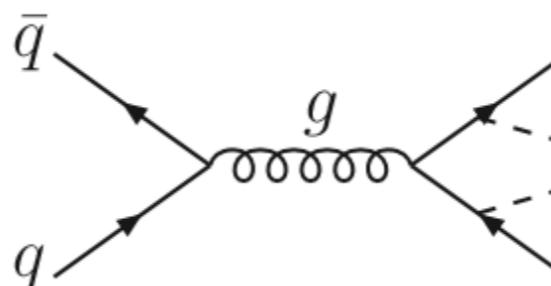
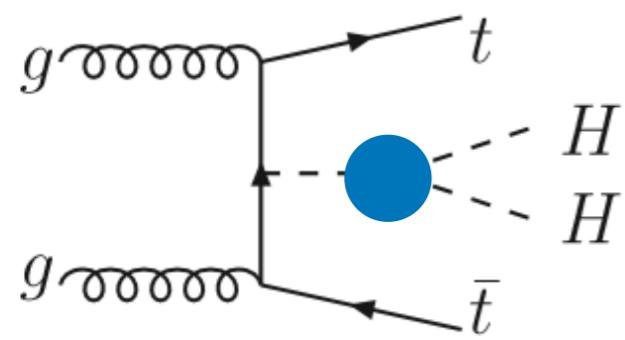


$$V(\phi) = a \sin^2(\phi/f) + b \sin^4(\phi/f)$$

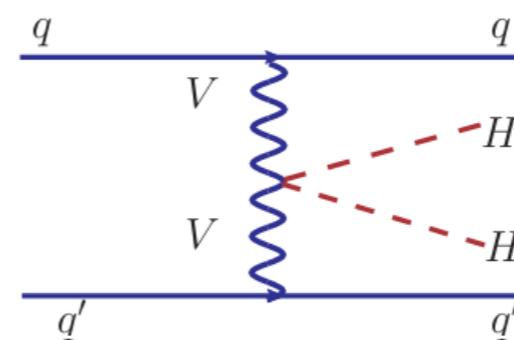
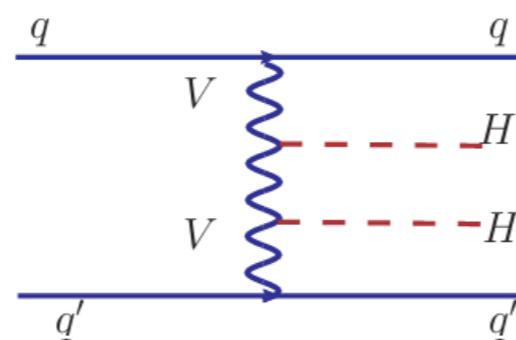
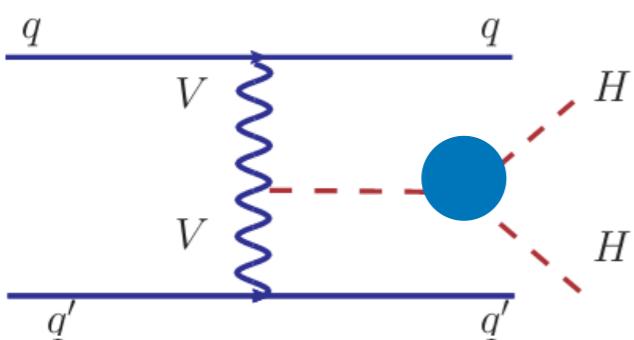
Measuring HHH coupling via Higgs Pair Productions



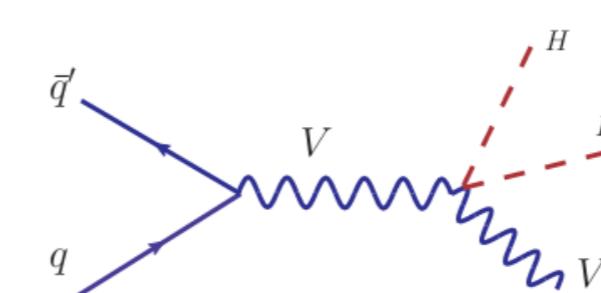
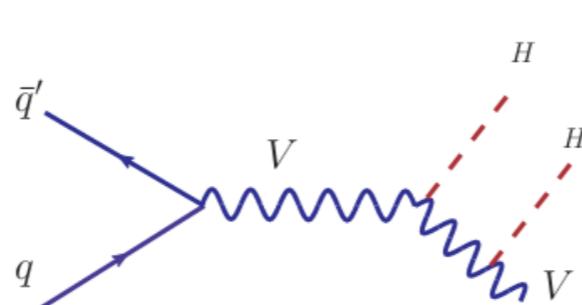
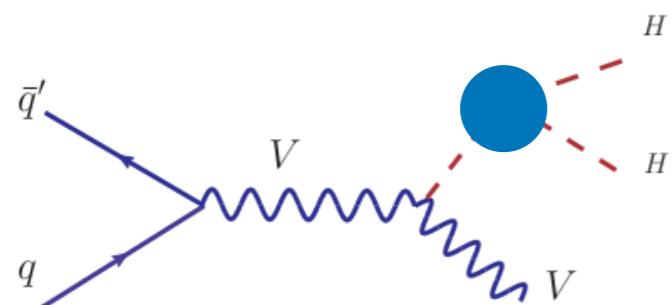
$gg \rightarrow HH$



$gg \rightarrow t\bar{t}HH$

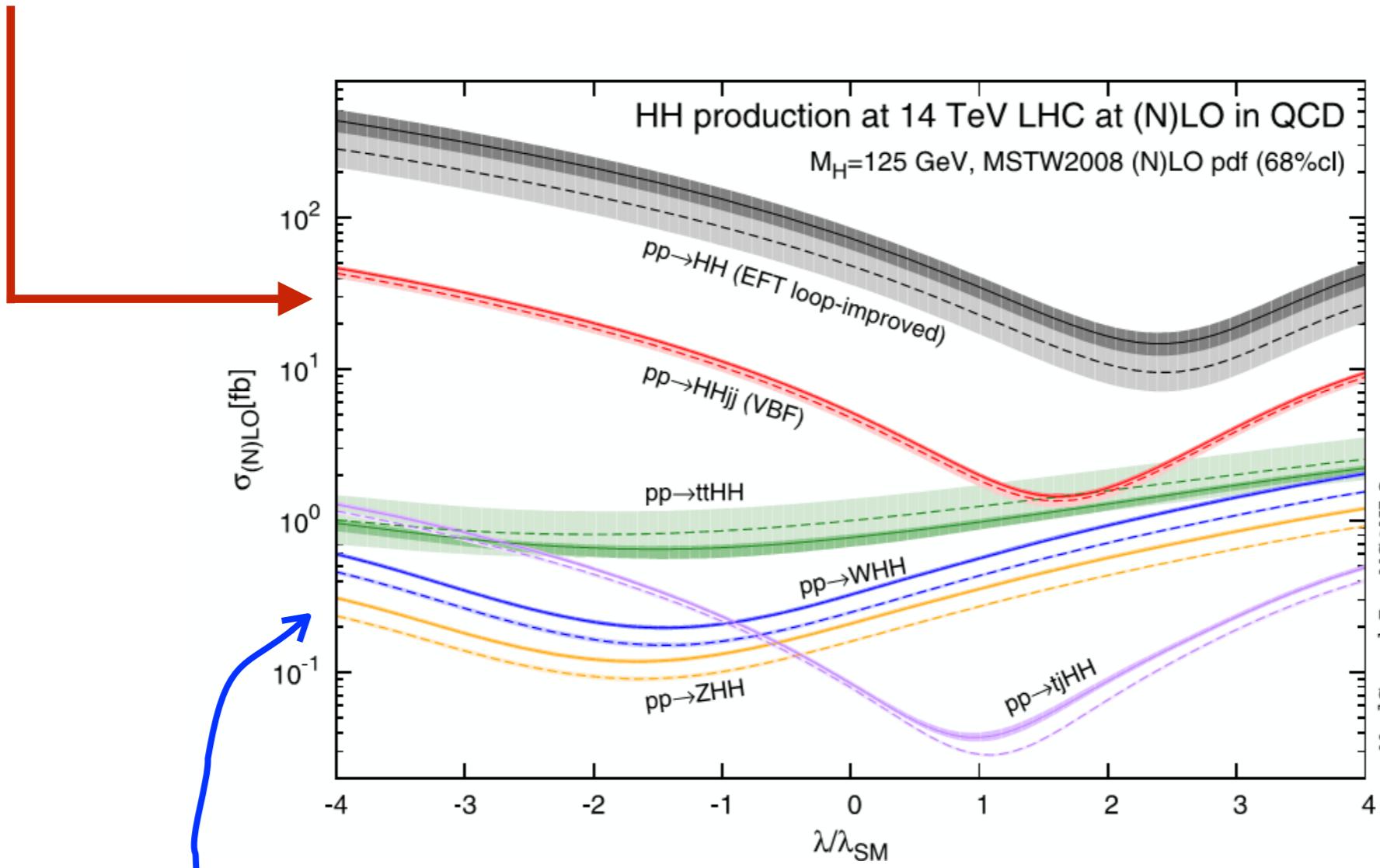
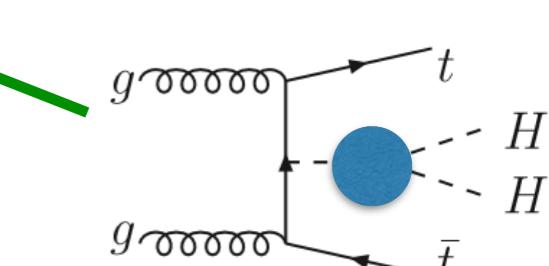
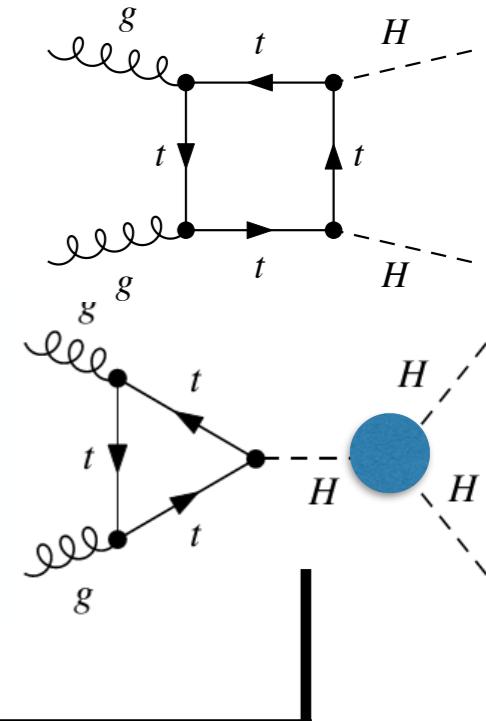
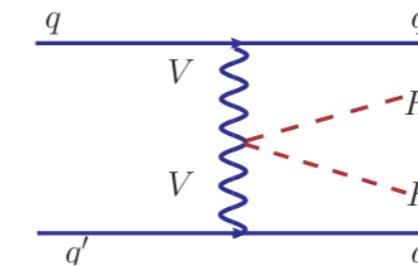
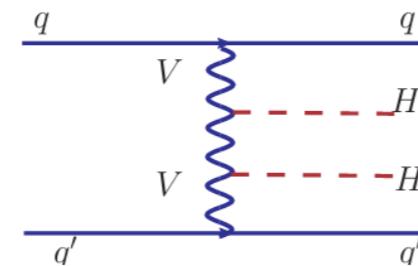
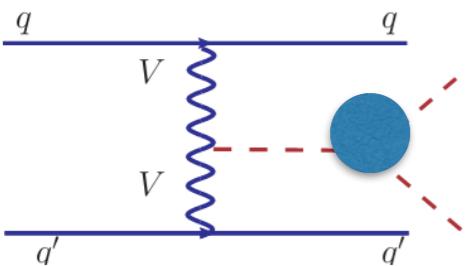


$qq' \rightarrow HHqq'$

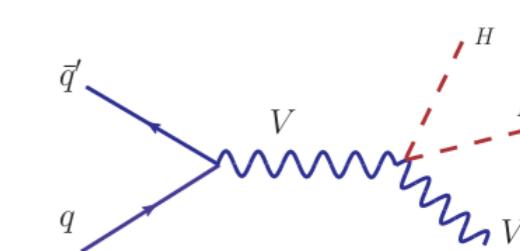
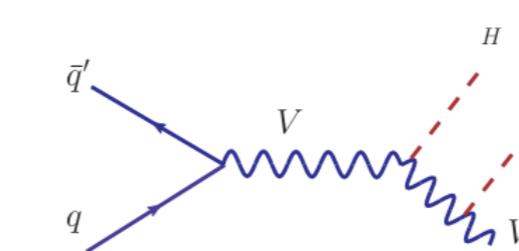
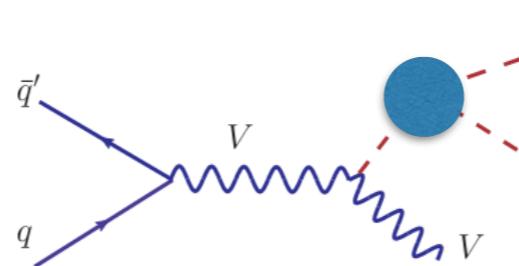


$q\bar{q}' \rightarrow VHH$

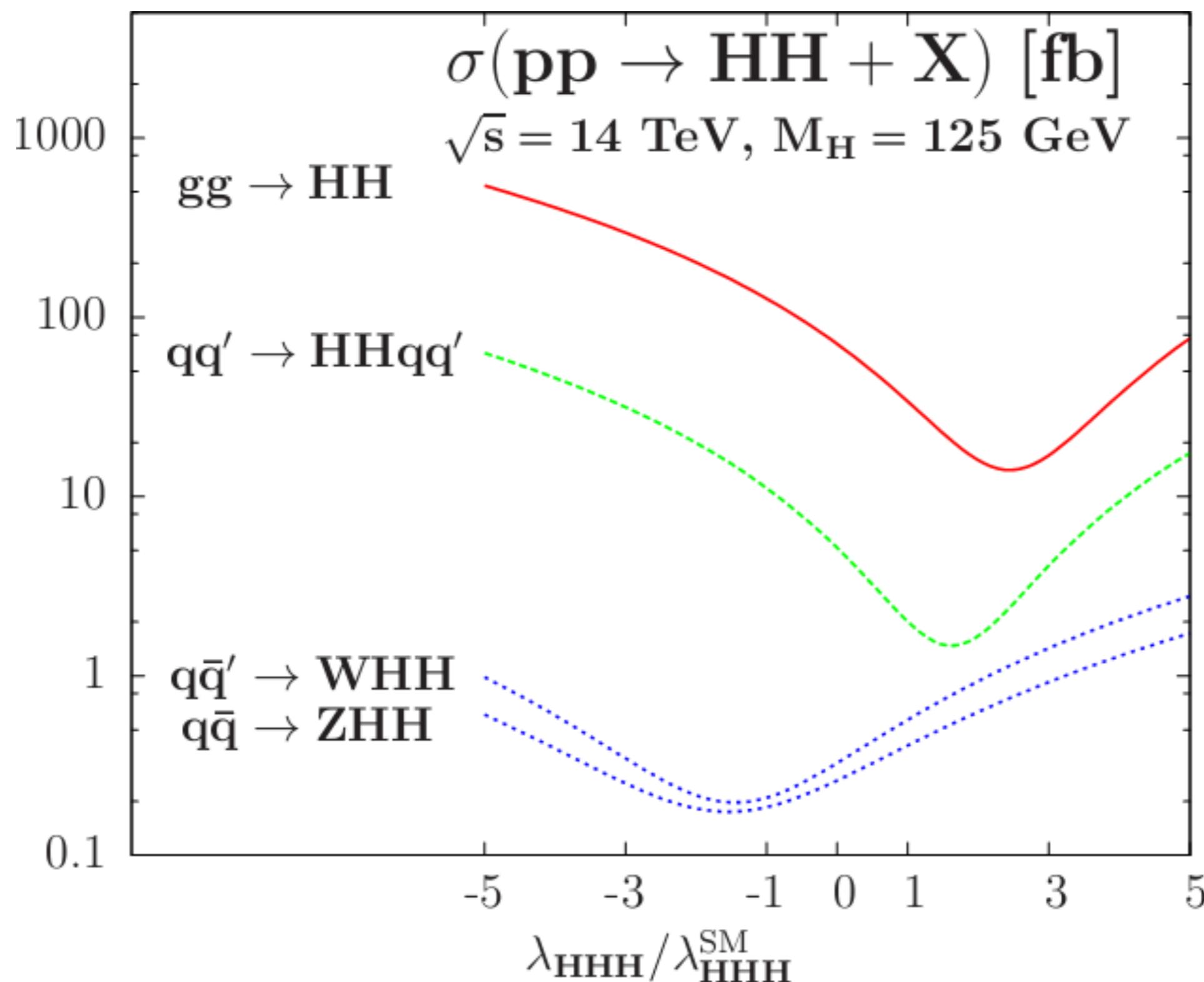
Higgs Boson Pair Production



MadGraph5_aMC@NLO



Sensitive to HHH coupling very differently



Sensitivity to HHH coupling: 1) gg->HH

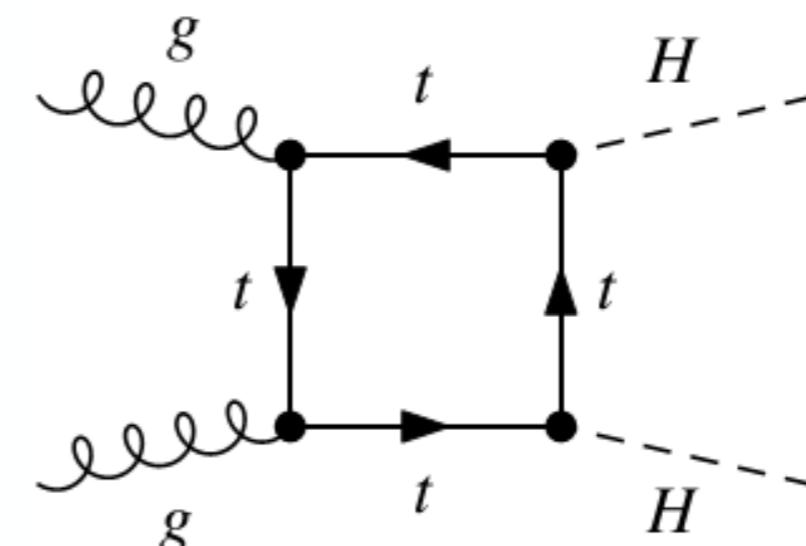
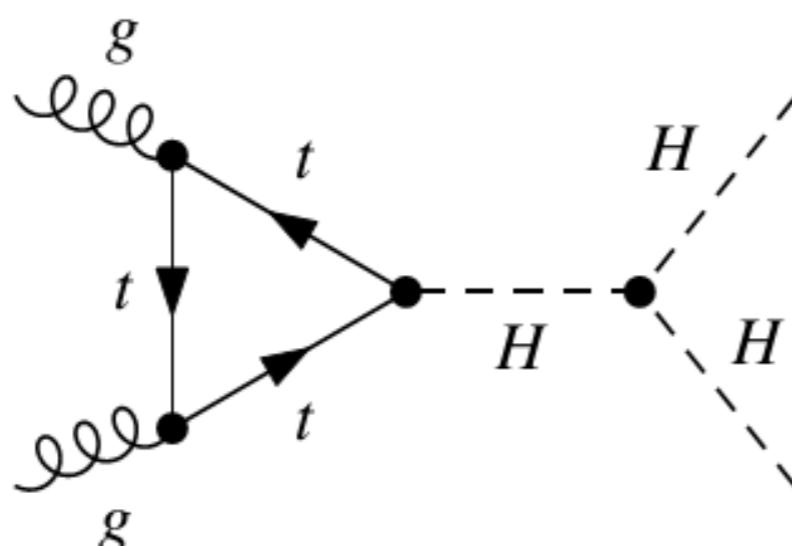
Low Energy Theorem

Shiftman, et al (1979)
Dawson and Haber (1989)

$$g \text{ (wavy line)} \rightarrow t \text{ (circle)} \rightarrow g$$

$$\sim -\frac{\alpha_s}{24\pi} G_{\mu\nu}^a G_a^{\mu\nu} \log \frac{\Lambda^2}{m_t^2}$$

$$y_t \frac{\partial}{\partial m_t} \rightarrow \frac{\alpha_s}{12\pi v} G_{\mu\nu}^a G_a^{\mu\nu} H$$



$$-\frac{\alpha_s}{24\pi} G^{a,\mu\nu} G_{\mu\nu}^a \sum_n \frac{y_t^n h^n}{n!} \frac{\partial^n}{\partial m_t^n} \log \left(\frac{\Lambda_{UV}^2}{m_t^2} \right)$$

n=1

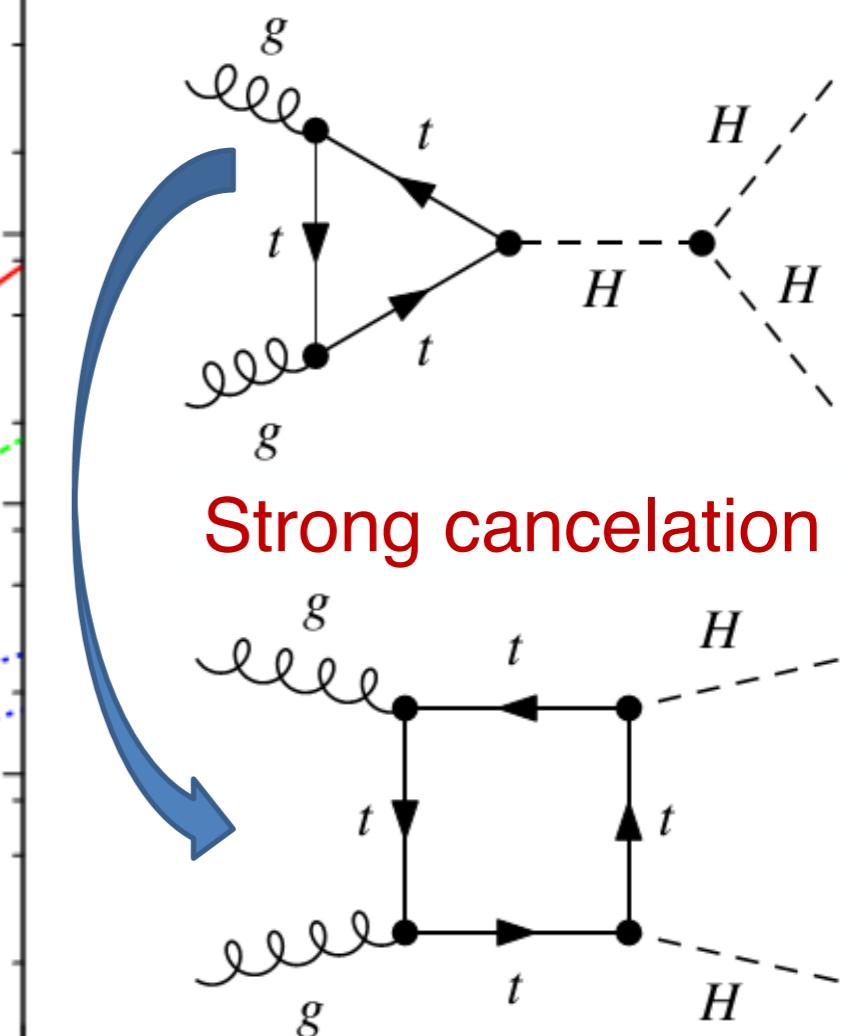
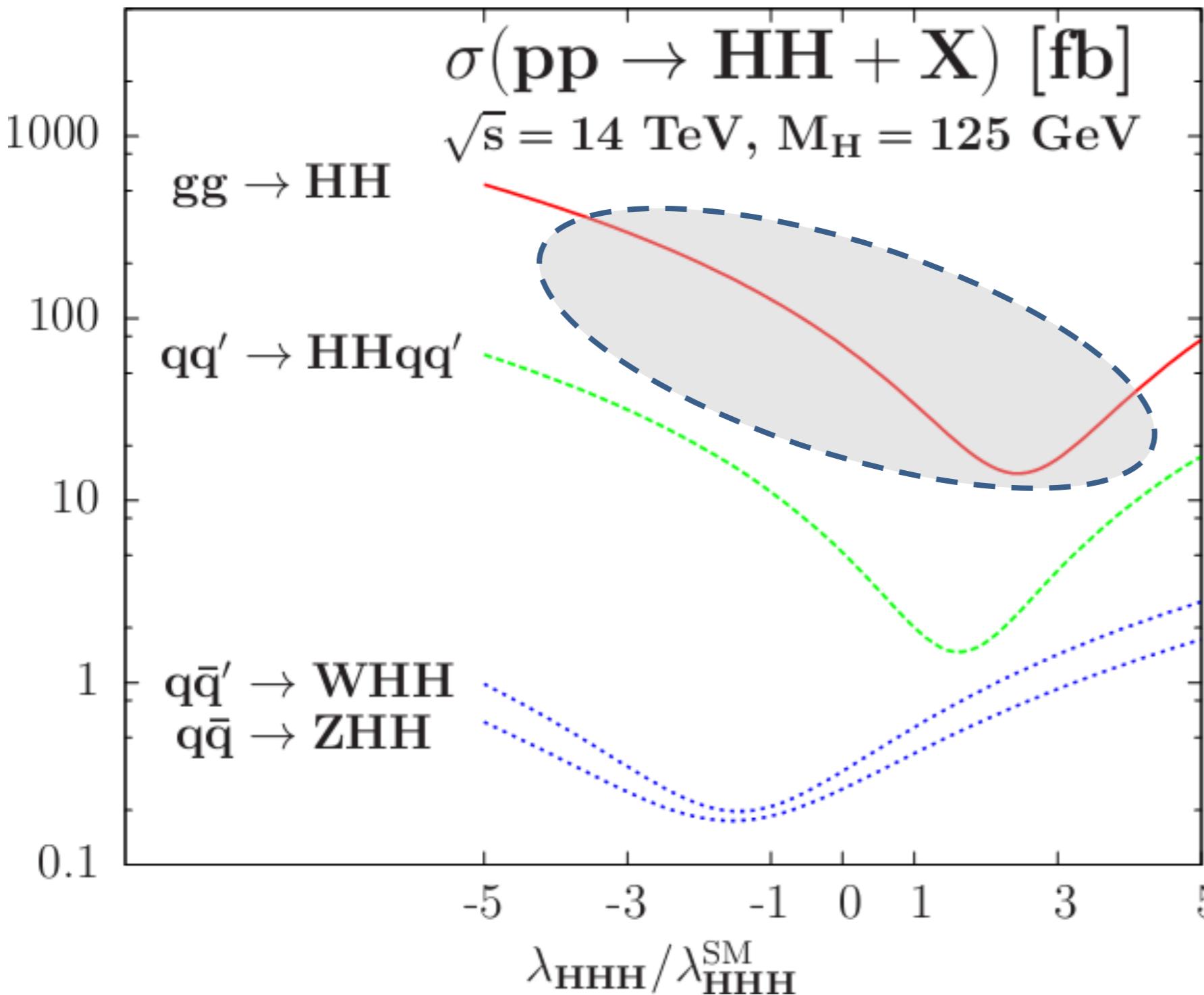
$$\frac{\alpha_s}{12\pi v} G^{a,\mu\nu} G_{\mu\nu}^a h$$

n=2

$$\frac{\alpha_s}{24\pi v^2} G^{a,\mu\nu} G_{\mu\nu}^a h^2$$

Strong cancellation

Sensitivity to HHH coupling: 1) gg->HH

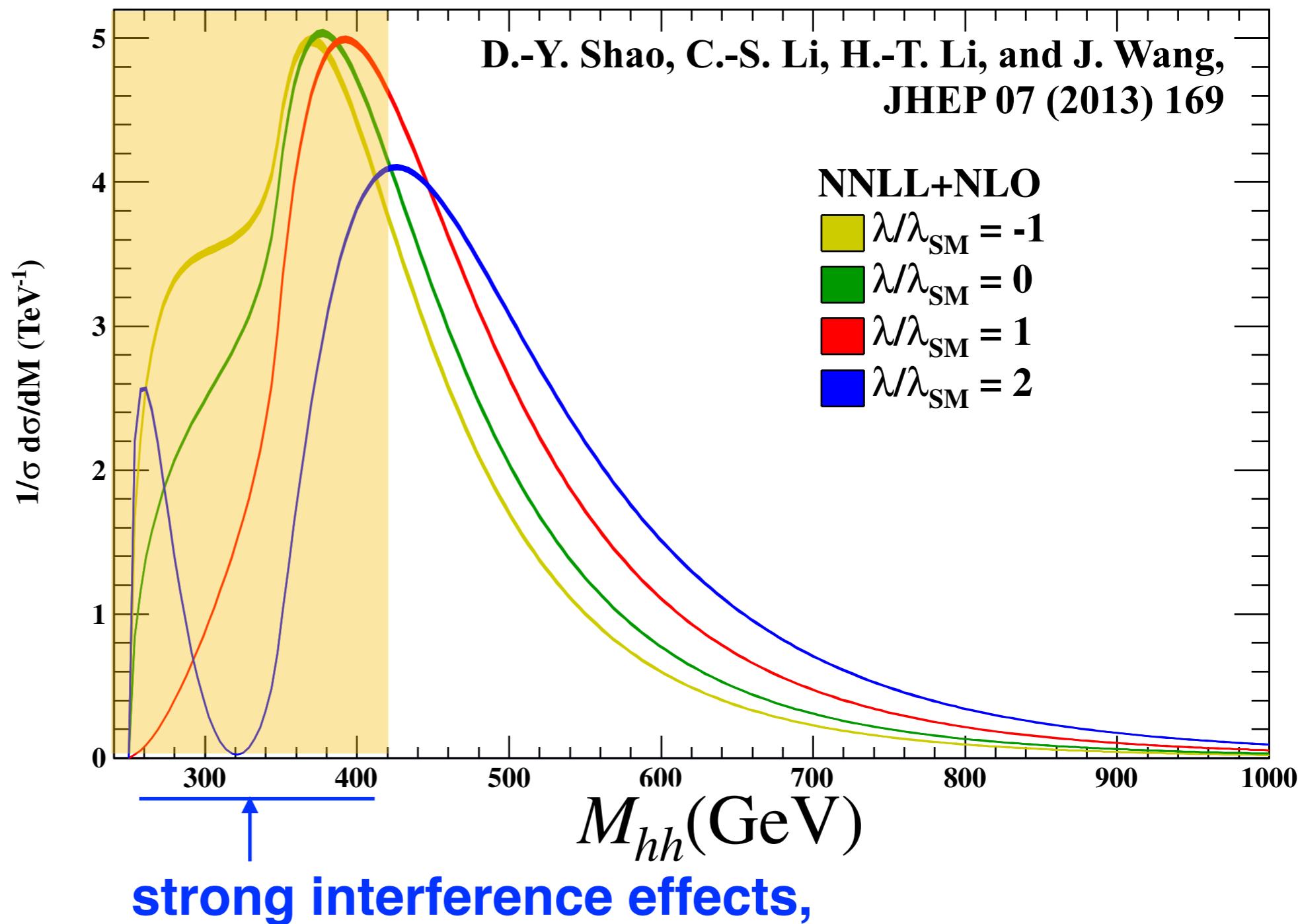
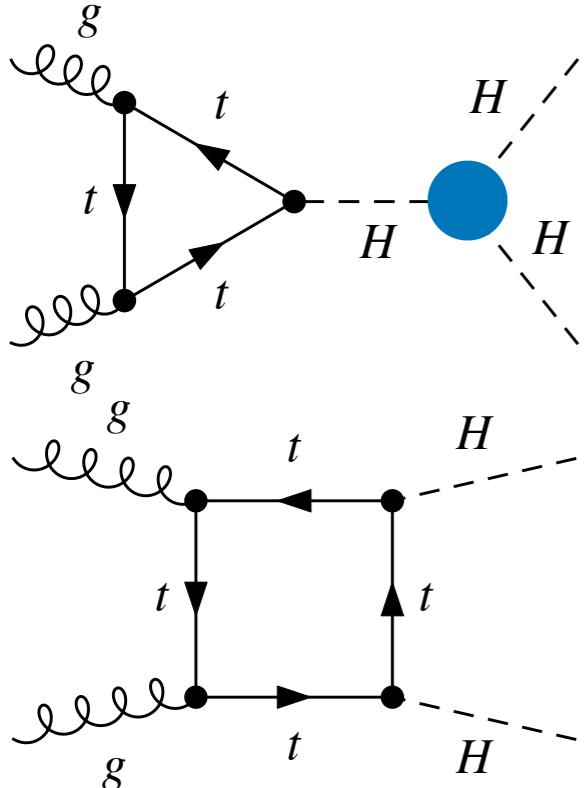


J. Baglio, A. Djouadi et al. JHEP 1304(2013)51

gg->HH: the leading channel

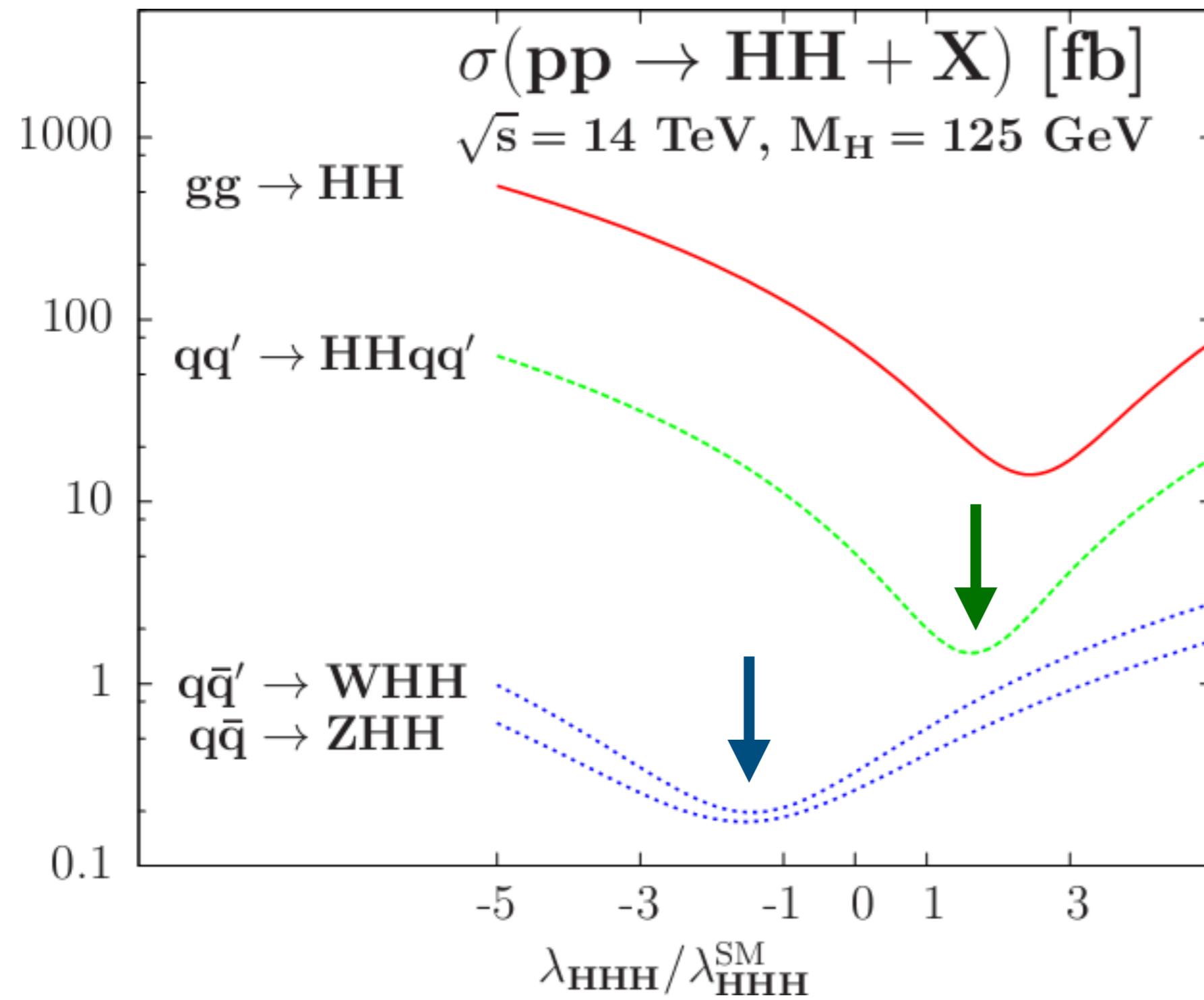
Unfortunately, it is not a easy job at the LHC or even at the SppC.

HH production

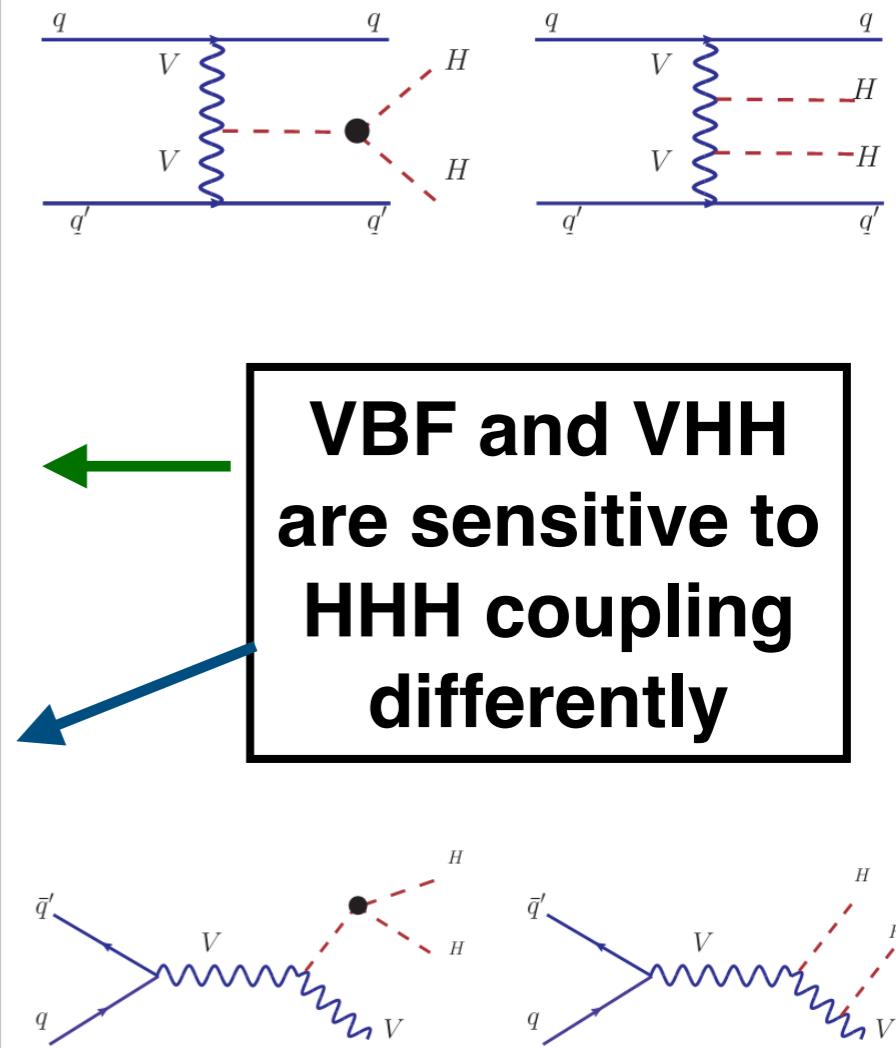


but not accessible at the LHC, due to hard cuts used by our experimental colleagues

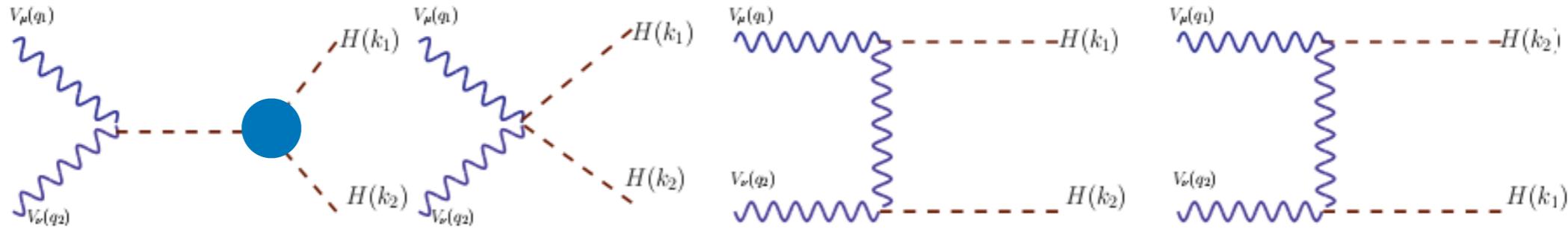
Sensitivity to HHH coupling: 2) VBF and VHH



**VBF and VHH
are sensitive to
HHH coupling
differently**



The VBF and VHH channels share the same subprocess but with different kinematics

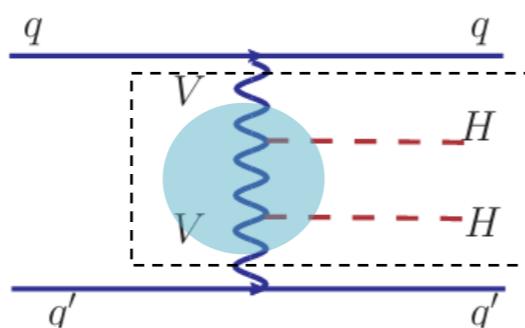


$$M^{\mu\nu} = \left[\frac{m_W^2}{\nu^2} \frac{6m_H^2}{\hat{s} - m_H^2} \frac{\lambda_{HHH}}{\lambda_{HHH}^{\text{SM}}} + \frac{2m_W^2}{\nu^2} + \frac{4m_W^4}{\nu^2} \left(\frac{1}{\hat{t} - m_W^2} + \frac{1}{\hat{u} - m_W^2} \right) \right] g^{\mu\nu} + \dots$$

Near the threshold of Higgs-boson pairs

VBF:

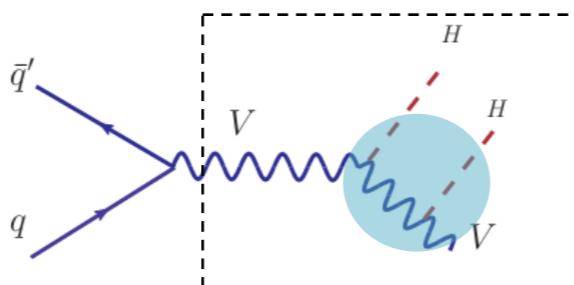
$$\hat{t} = \hat{u} = Q^2 < 0$$



$$M^{\mu\nu} \sim \frac{2m_V^2}{\nu^2} \left(\frac{\lambda_{HHH}}{\lambda_{HHH}^{\text{SM}}} - 3 \right) g^{\mu\nu} + \dots$$

VHH:

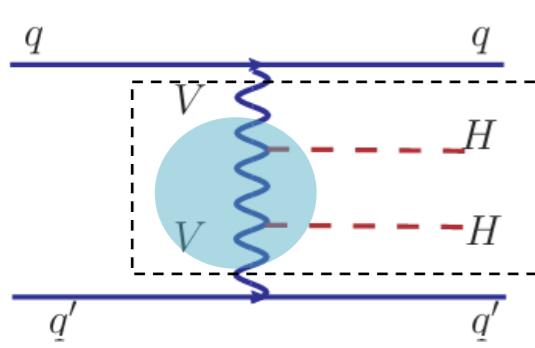
$$\hat{t} = \hat{u} = Q^2 > 0$$



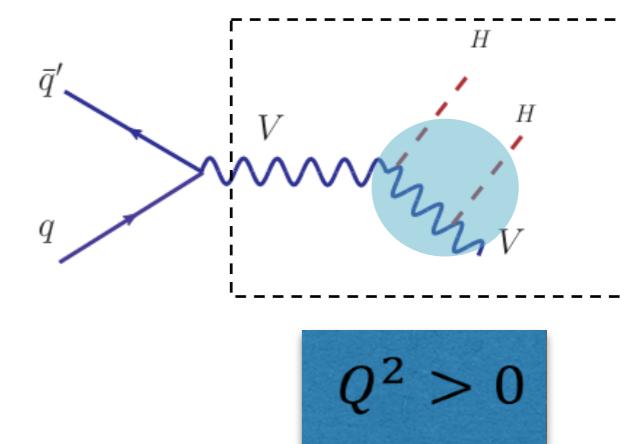
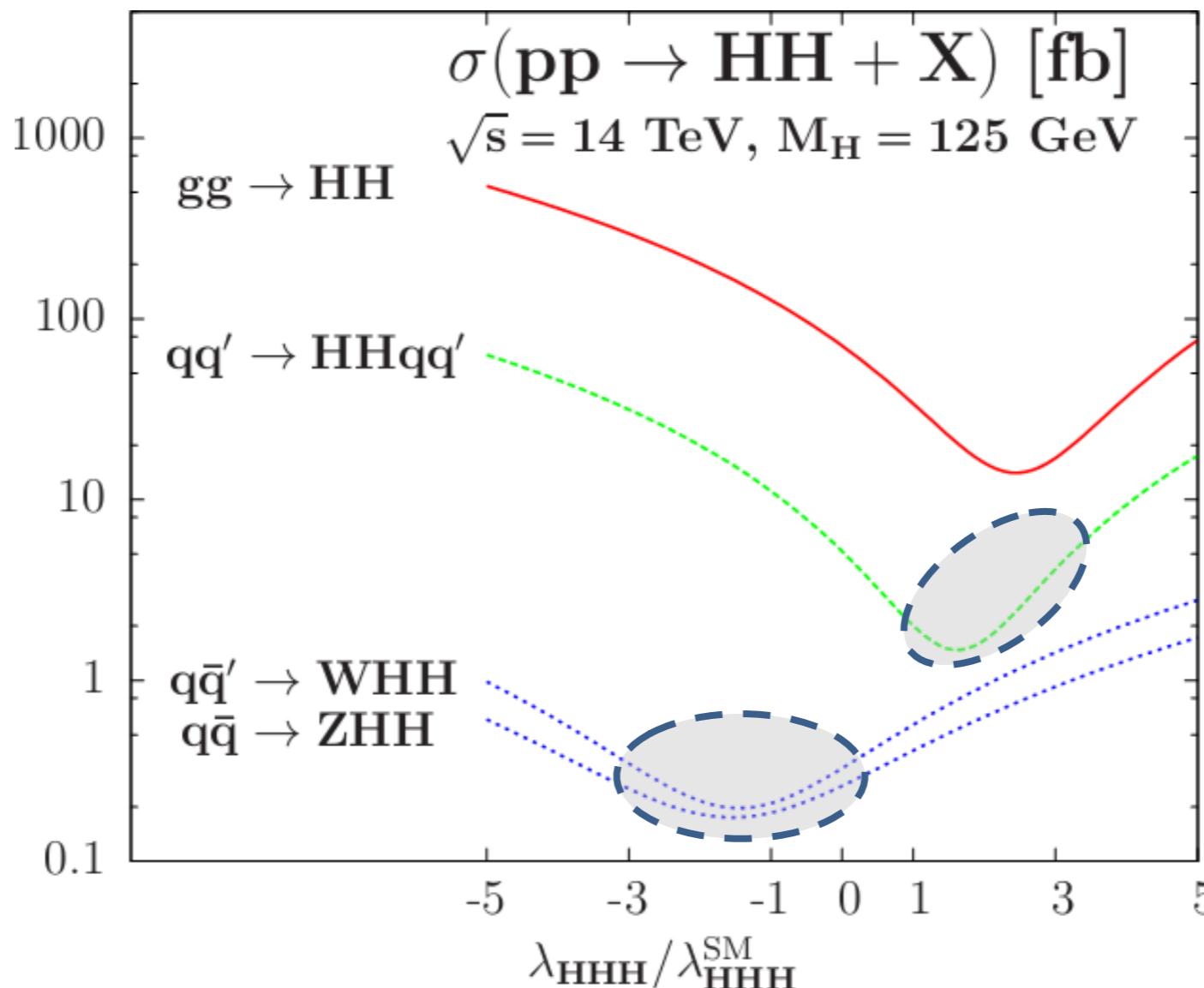
$$M^{\mu\nu} \sim \frac{2m_V^2}{\nu^2} \left(\frac{\lambda_{HHH}}{\lambda_{HHH}^{\text{SM}}} + 1 \right) g^{\mu\nu} + \dots$$

Sensitivity to HHH Coupling

VBF $M^{\mu\nu} \sim \frac{2m_V^2}{v^2} \left(\frac{\lambda_{HHH}}{\lambda_{HHH}^{\text{SM}}} - 3 \right) g^{\mu\nu} + \dots$



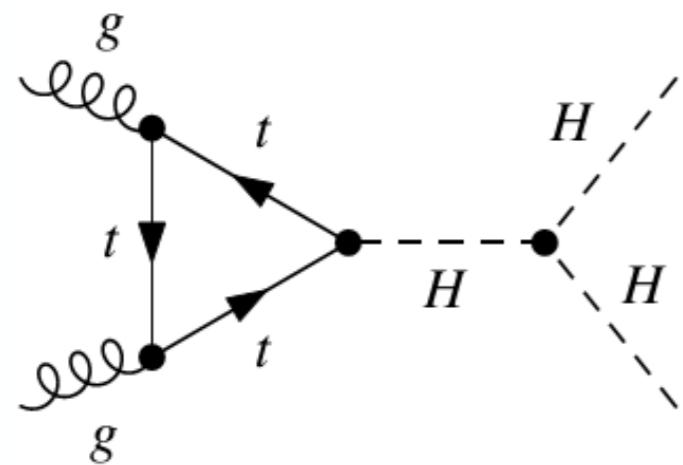
$Q^2 < 0$



$Q^2 > 0$

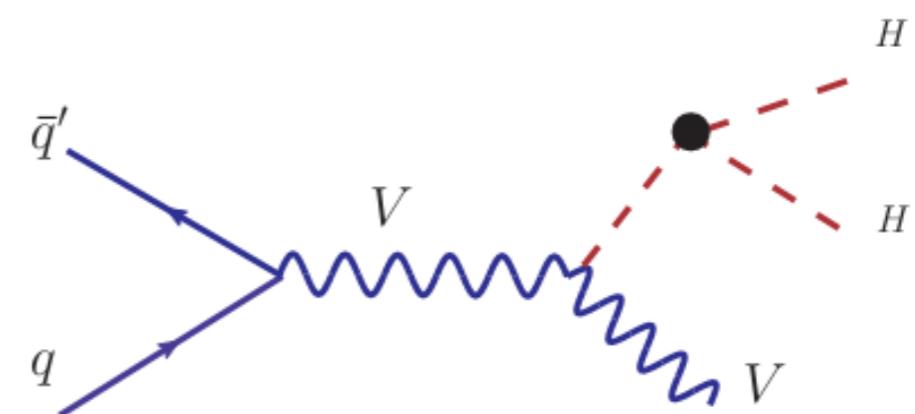
VHH $M^{\mu\nu} \sim \frac{2m_V^2}{v^2} \left(\frac{\lambda_{HHH}}{\lambda_{HHH}^{\text{SM}}} + 1 \right) g^{\mu\nu} + \dots$

HH and VHH @ HL-LHC



Cross section: 34 fb

VS



>>

Cross section: 0.57 fb

Final states: $bb\gamma\gamma$

$$Br(bb\gamma\gamma) = 1.3 \times 10^{-3}$$

$$\sigma \times Br(bb\gamma\gamma) = 0.044 \text{ fb} \quad \approx$$

Final states: $bbbb$

$$Br(bbbb\ell\nu) = 0.073$$

$$\sigma \times Br(bbbb\ell\nu) = 0.042 \text{ fb}$$

Huge backgrounds:

$b\bar{b}\gamma\gamma, c\bar{c}\gamma\gamma, b\bar{b}\gamma j, jj\gamma\gamma,$
 $b\bar{b}jj, t\bar{t}, t\bar{t}\gamma, ZH, t\bar{t}H$

Main backgrounds:

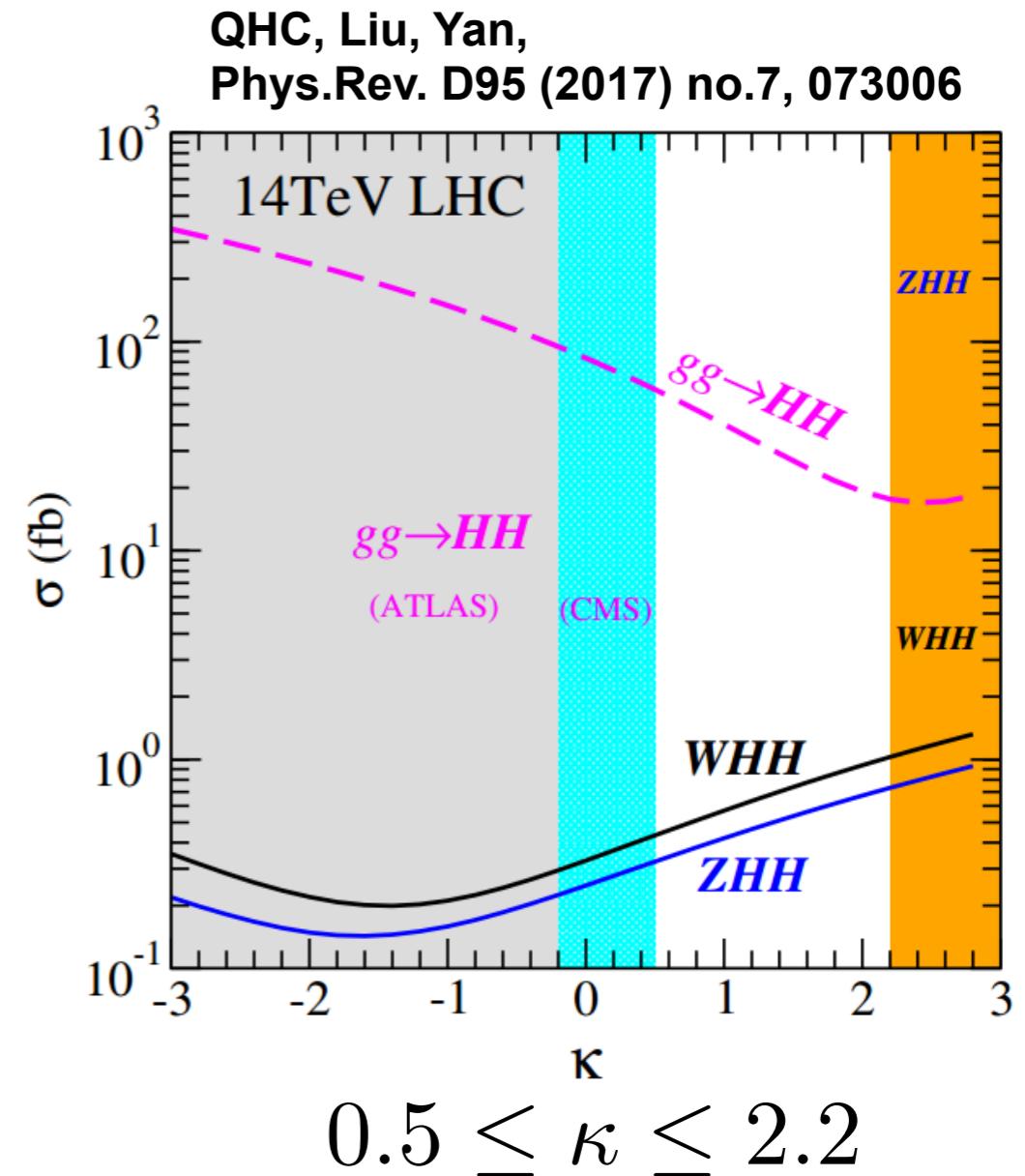
$Zbbbb, Wbbbb, t\bar{t}, t\bar{t}j,$
 $t\bar{t}H, t\bar{t}z, t\bar{t}bb$

W_HH and Z_HH Productions

TABLE III: The sensitivity to $\lambda_{HHH} = \kappa \lambda_{HHH}^{\text{SM}}$ in several production channels of Higgs boson pairs at the HL-LHC.

	SM ($\kappa = 1$)	5 σ discovery potential	2 σ exclusion bound
W _H H	1.29σ	$\kappa \leq -7.7, \kappa \geq 4.8$	$-5.1 \leq \kappa \leq 2.2$
Z _H H	1.32σ	$\kappa \leq -8.1, \kappa \geq 4.8$	$-5.4 \leq \kappa \leq 2.2$
GF($b\bar{b}\gamma\gamma$) [42]	1.19σ	$\kappa \leq -4.5, \kappa \geq 8.1$	$-0.2 \leq \kappa \leq 4.9$
GF($b\bar{b}\gamma\gamma$) [43]	1.65σ	$\kappa \leq -2.6, \kappa \geq 6.3$	$0.5 \leq \kappa \leq 4.1$
VBF [20]	0.59σ	$\kappa \leq -1.7, \kappa \geq 5.0$	$-0.4 \leq \kappa \leq 3.5$
$t\bar{t}HH$ [21, 22]	1.38σ	$\kappa \leq -11.4, \kappa \geq 6.9$	$-7.2 \leq \kappa \leq 2.5$

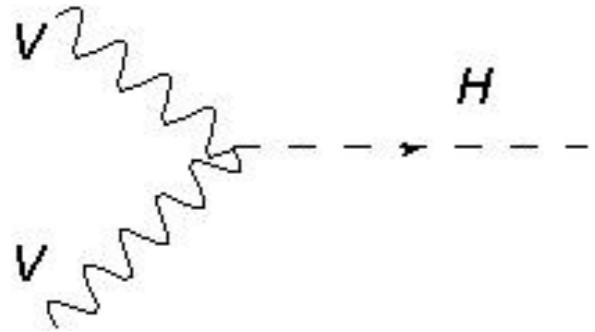
The discovery potential of triple Higgs coupling in VHH production is comparable to other channels.



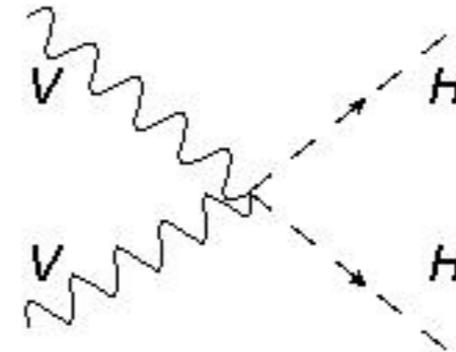
Nordstrom and Papaefstathiou (arXiv:1807.01571)
include full detector effects and show that measuring HHH coupling via W_HH and V_HH channels is still challenging at the HL-LHC

HVV versus HHVV

SM predicts a definite **ratio** between HVV and HHVV couplings



$$2i \frac{M_V^2}{\nu} g^{\mu\nu}$$

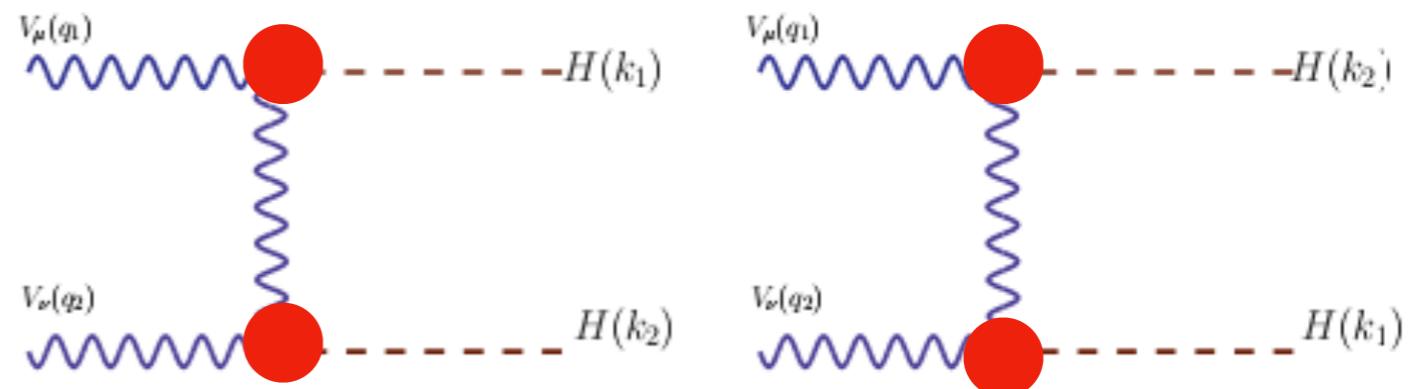
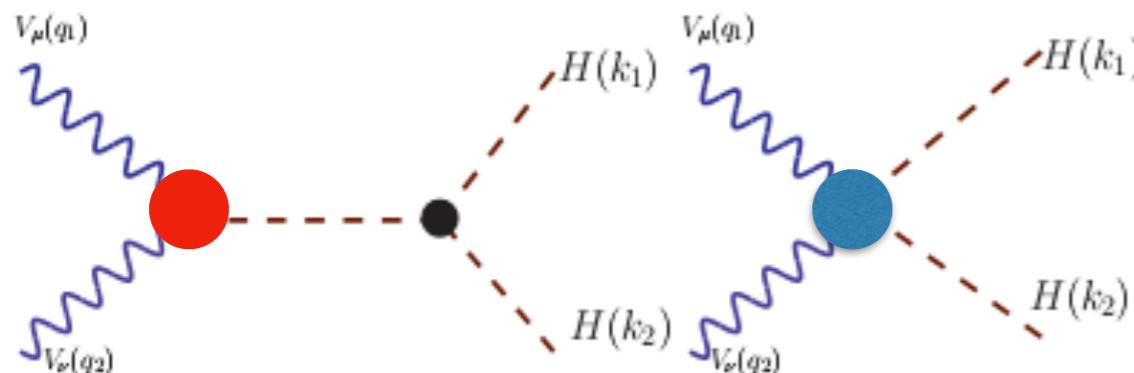


$$2i \frac{M_V^2}{\nu^2} g^{\mu\nu}$$

$$\frac{g_{hhVV}^{\text{SM}}}{g_{hVV}^{\text{SM}}} = \frac{1}{\nu}$$

$$\frac{g_{hhVV}^{\text{pNGB}}}{g_{hVV}^{\text{pNGB}}} = \frac{1}{\nu} \frac{1 - 2\xi}{\sqrt{1 - \xi}}$$

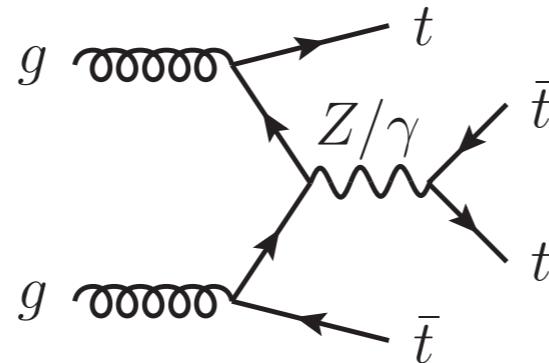
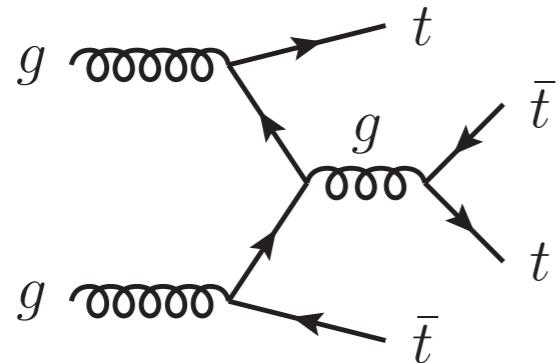
If the ratio is modified by NP, the unitarity of $VV \rightarrow HH$ is broken



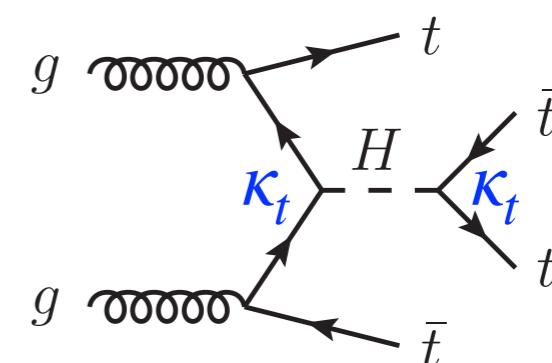
2. Top-Higgs Interactions

Four top quark production and the Higgs-top interaction

Barger, Stange, Phillips, 1991



QHC, Chen, Liu, 1602.01934



$$\sigma(t\bar{t}t\bar{t}) = \sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma} + \kappa_t^2 \sigma_{\text{int}}^{\text{SM}} + \kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H$$

LO

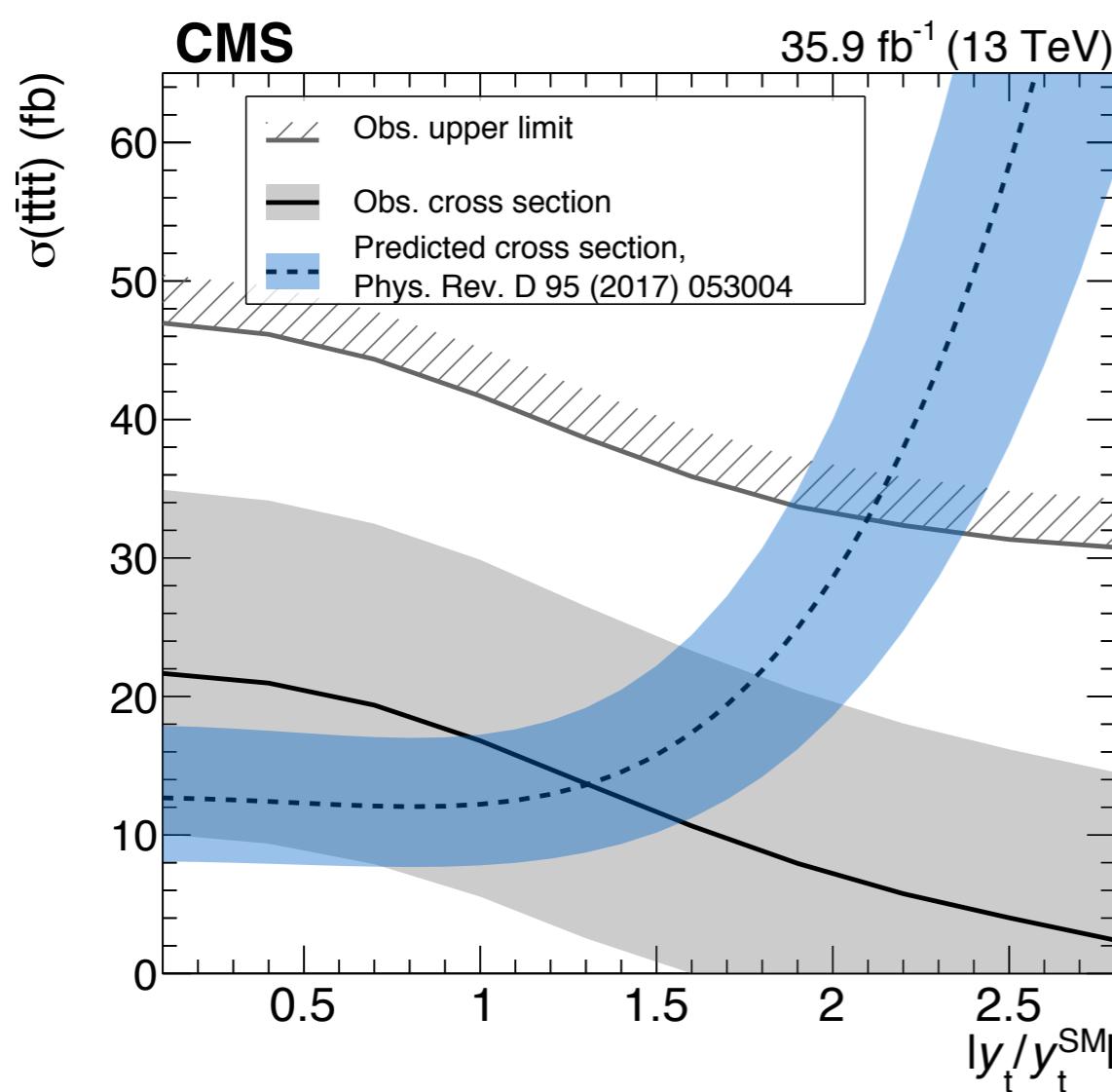
8 TeV	1.344	-0.224	0.171
13 TeV	9.997	-1.547	1.108
14 TeV	13.14	-2.007	1.515
27 TeV	115.1	-15.57	11.73
100 TeV	3276	-356.9	273.1

in unit
of fb

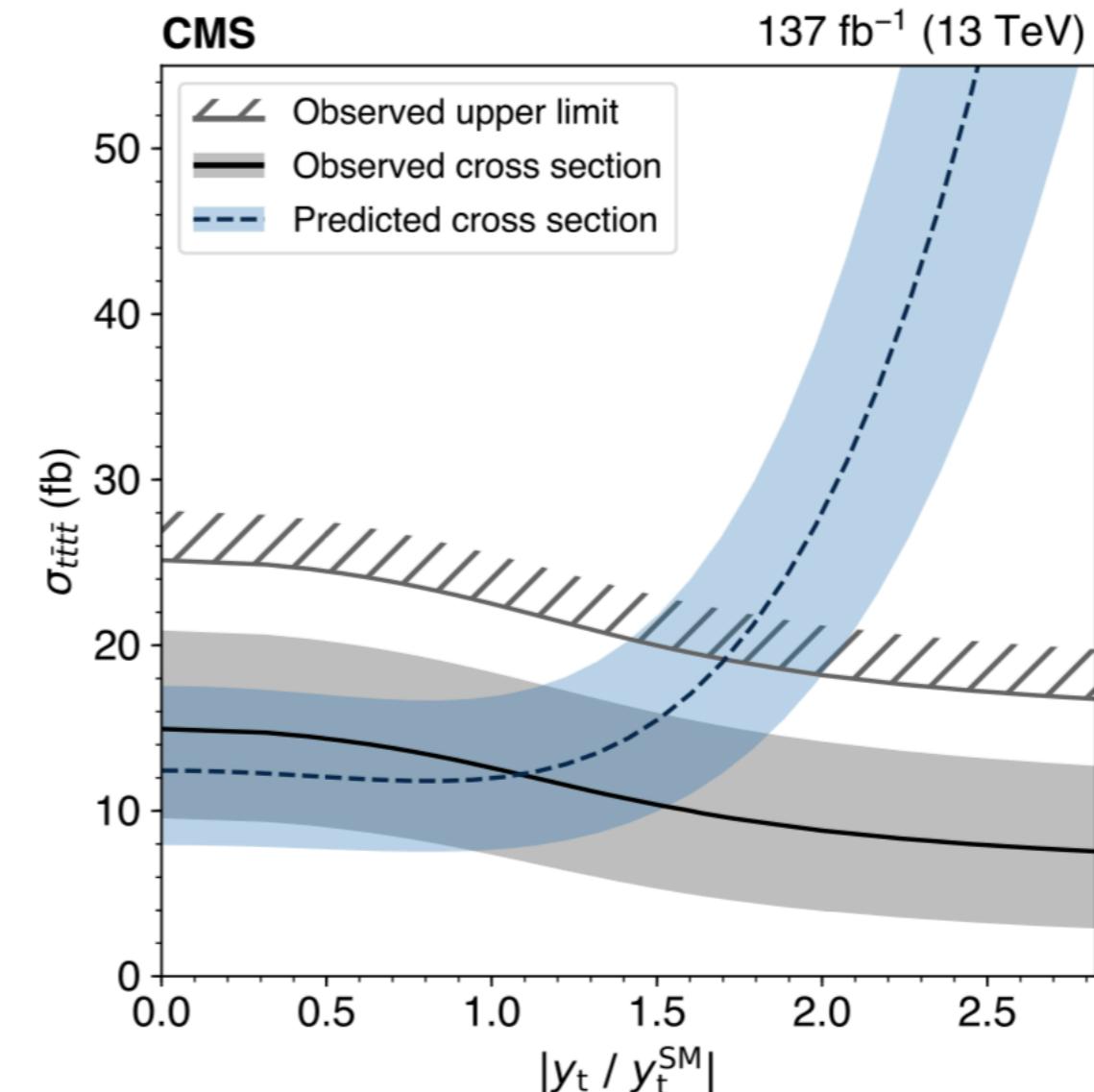
NLO corrections: Bevilacqua, Worek (2012);
Alwall et al (2014); Frederix, Pagani, Zaro (2017)

Four top quark productions

CP-even $\sigma(t\bar{t}t\bar{t}) = 9.997 - 1.547 \times y_t^2 + 1.108 \times y_t^4$ (fb)



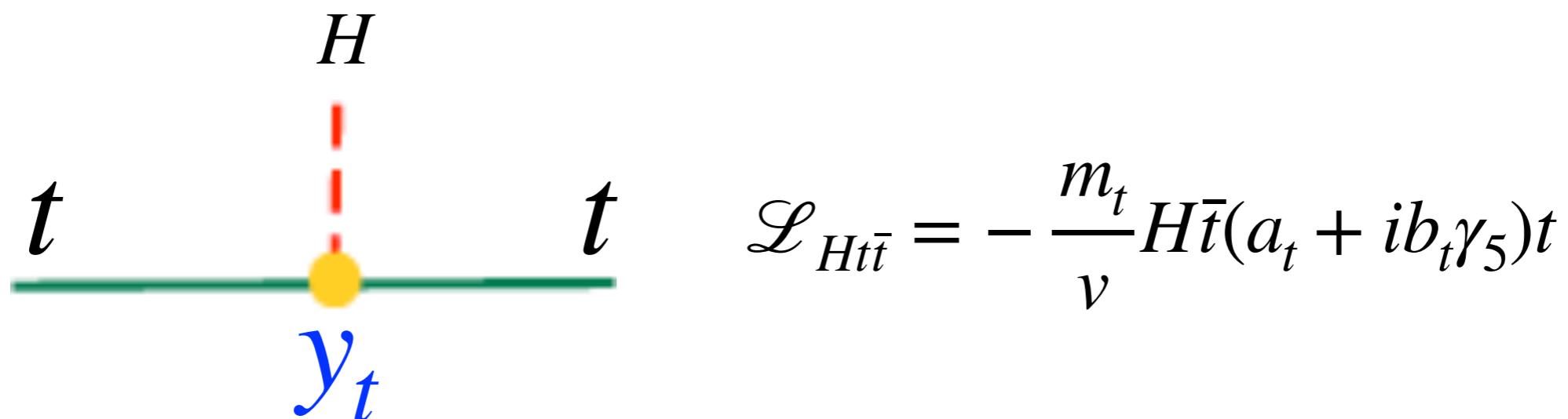
$$y_t \leq 2.1 \times y_t^{\text{SM}}$$
 1710.10614



$$y_t \leq 1.7 \times y_t^{\text{SM}}$$
 1908.06463
1909.05306

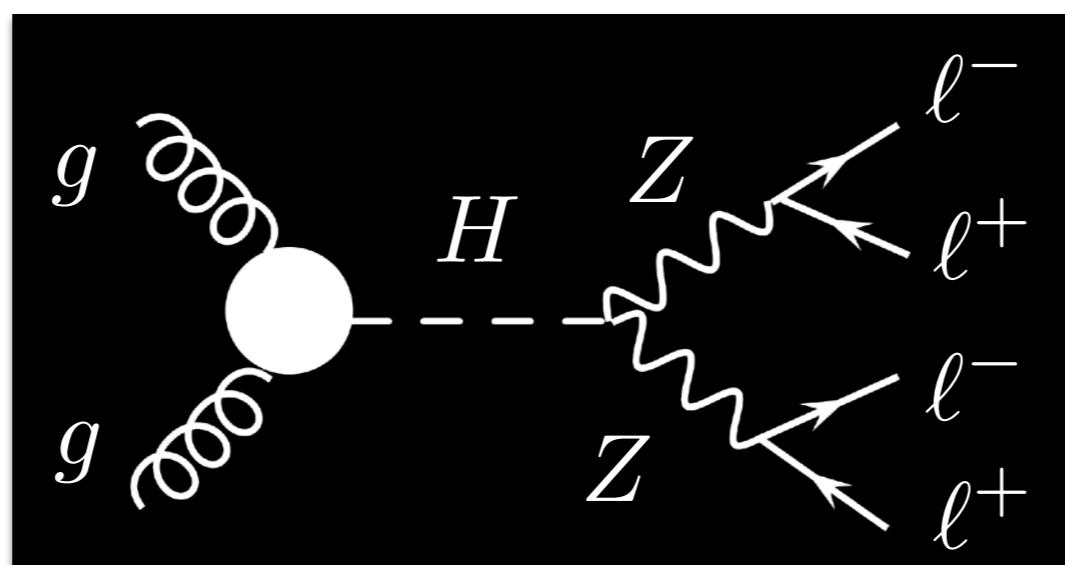
The channel is also sensitive to the CP property of top-Higgs interaction.

3. CP property of top-Higgs interaction



The CP property of the Hbb coupling is hard to measure due to the small bottom-quark mass.

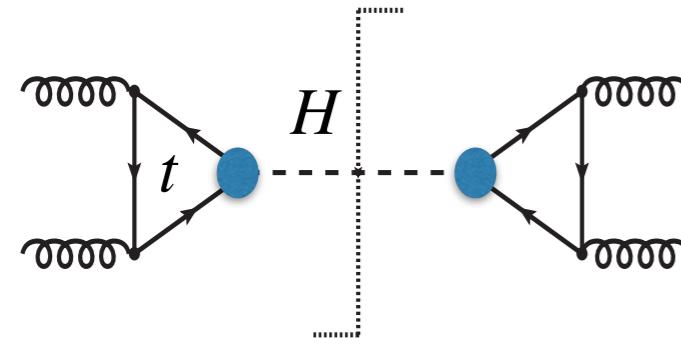
Different phase angle in the hVV and hFF vertices?



Higgs boson productions

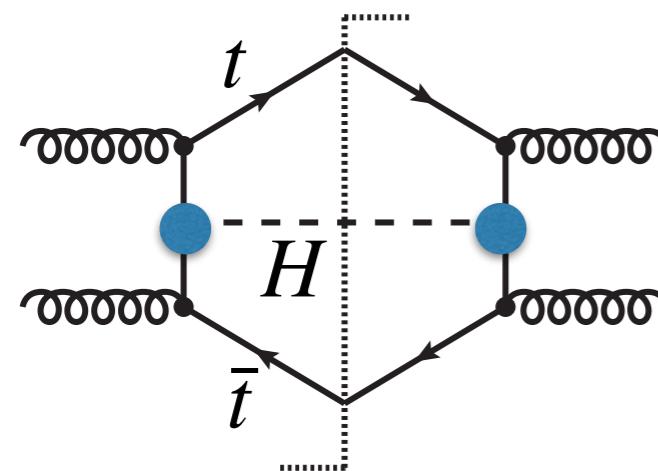
$$\mathcal{L}_{Ht\bar{t}} = - \frac{m_t}{v} H \bar{t} (a_t + i b_t \gamma_5) t$$

Boudjema, Godbole,
Guadagnoli, Mohan,
1501.03157



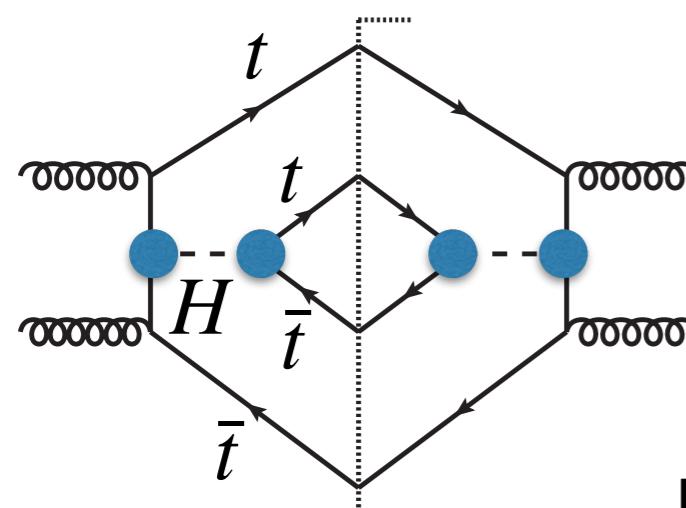
$$\frac{\sigma(gg \rightarrow H)}{\sigma(gg \rightarrow H)_{\text{SM}}} \sim a_t^2 + 2.26 b_t^2$$

↑ pseudo-scalar
dominates



$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} \sim a_t^2 + 0.42 b_t^2 \quad (14\text{TeV})$$

↑ scalar dominates



$$\begin{aligned} \sigma(t\bar{t}t\bar{t}H) = & 9.997 + 2.807 \times b_t^2 + 1.788 \times b_t^4 \\ & - 1.547 \times a_t^2 + 1.108 \times a_t^4 \quad (\text{fb}) \end{aligned}$$

Four tops — another way to probe top-Higgs coupling

CP property of top-Higgs interaction

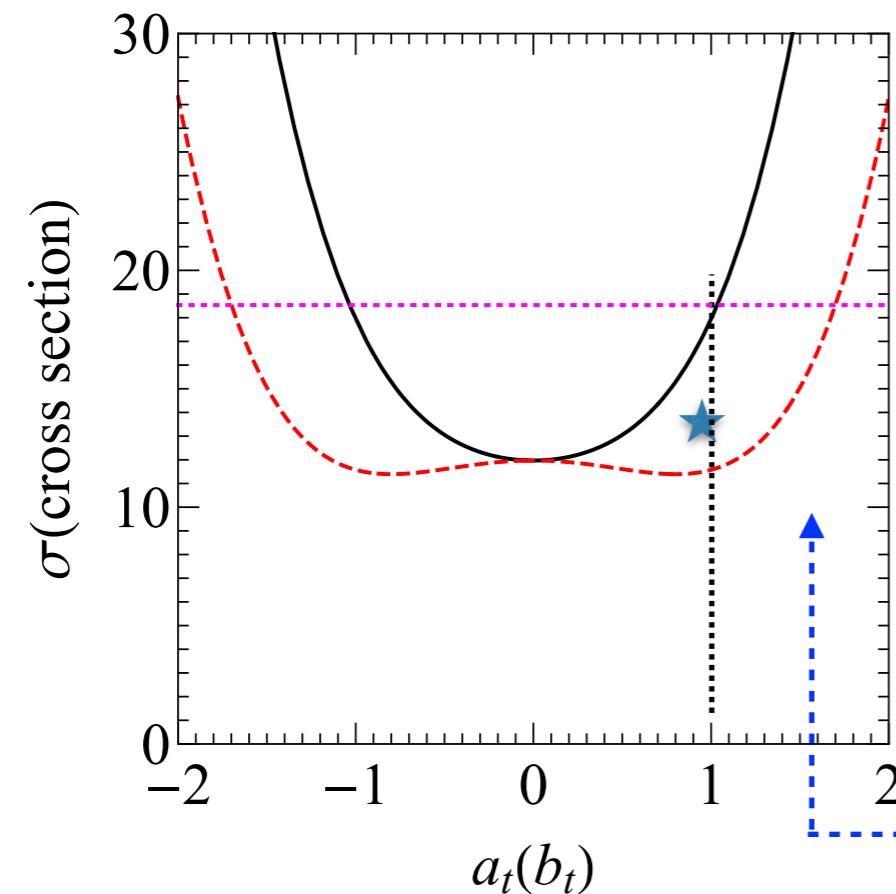
$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H \bar{t}(a_t + i b_t \gamma_5) t$$

Phys. Rev. D99 (2019) no.11, 113003
QHC, S.L Chen, Y. Liu, R. Zhang, Y. Zhang

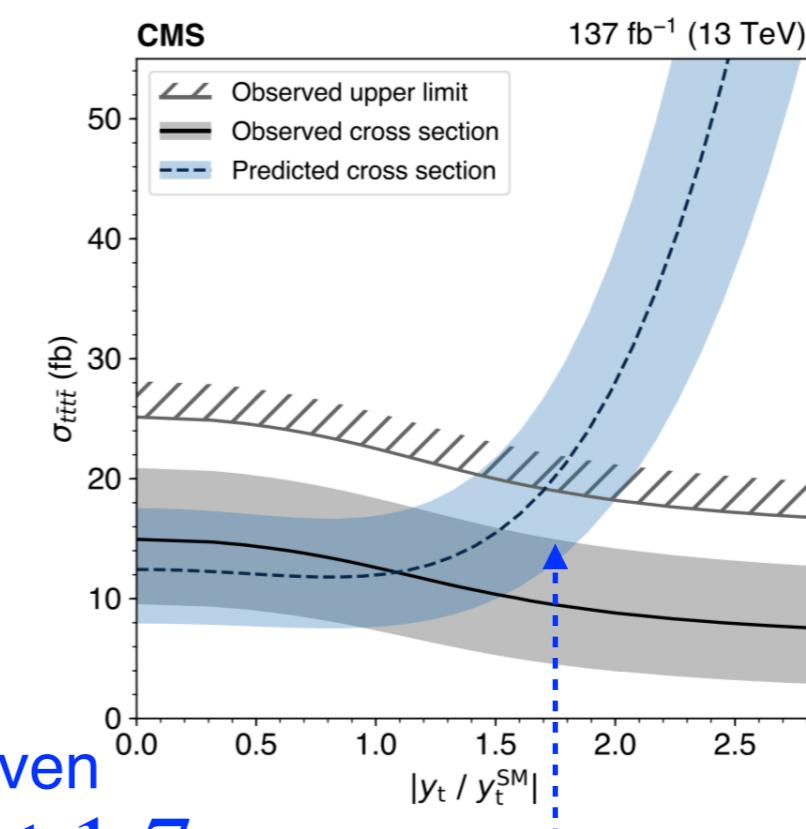
CP-odd
(a=0, b=1) $\sigma(t\bar{t}t\bar{t}) = 7.724 + 2.434 \times b_t^2 + 1.424 \times b_t^4$ (fb)

CP-even
(a=1, b=0) $\sigma(t\bar{t}t\bar{t}) = 7.724 - 1.164 \times a_t^2 + 0.910 \times a_t^4$ (fb)

$K_F = 1.55$ JHEP 02, 031 (2018) R. Frederix, D.Pagani, and M. Zaro

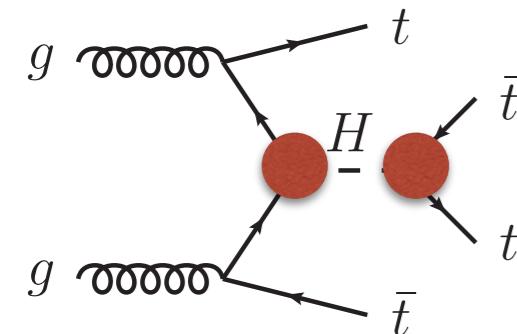


CP-even
 $\kappa_t \leq 1.7$

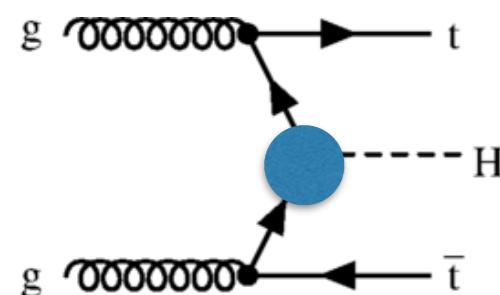


$b_t \leq 1.03$ for a pure CP-odd coupling

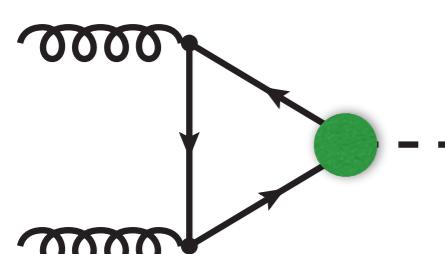
Global analysis of Top-Higgs interaction



137 fb^{-1}
CMS Collaboration arXiv:1908.06463



41.5 fb^{-1}
CMS-PAS-HIG-18-019



36.3 fb^{-1}

Eur.Phys.J. C79 (2019) no.5, 421 CMS

$$\sigma(t\bar{t}t\bar{t}) = 7.724 - 1.164a_t^2 + 2.434b_t^2 + 0.910a_t^4 + 2.183a_t^2b_t^2 + 1.424b_t^4$$

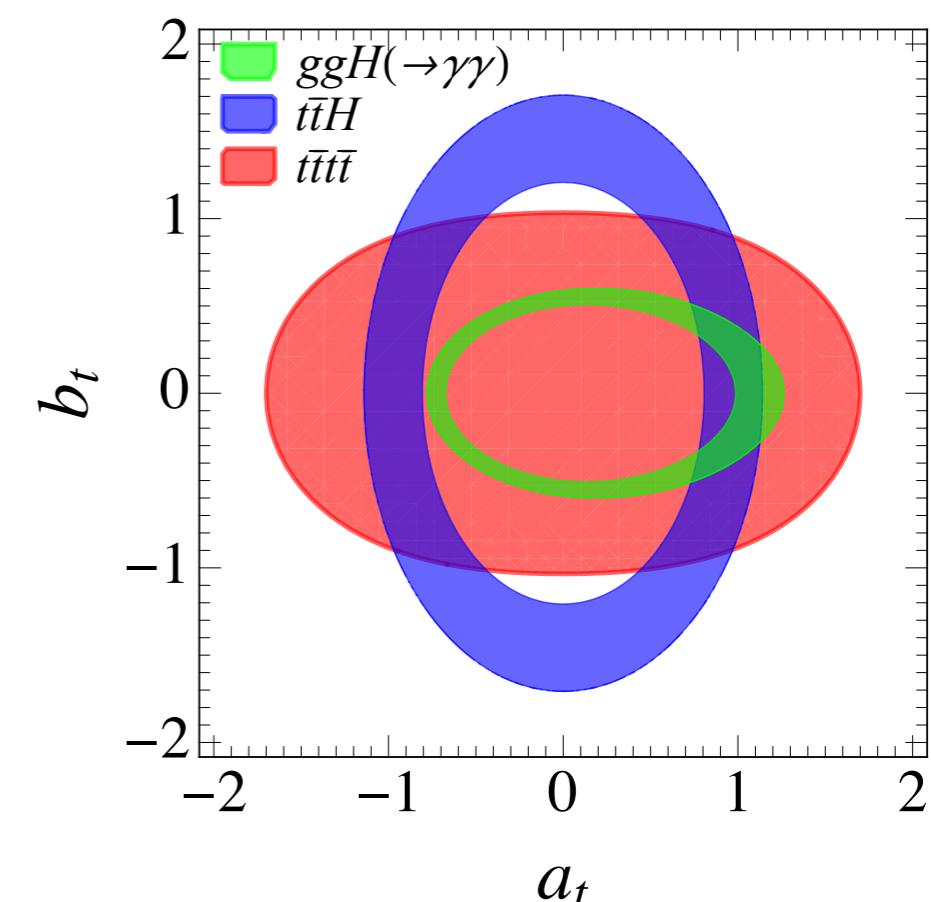
$K_F = 1.55$ JHEP 02, 031 (2018) R. Frederix, D.Pagani, and M. Zaro

$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} = (a_t^2 + 0.46b_t^2) \frac{1}{R_\Gamma}$$

$$\mu_{t\bar{t}H} = 0.96^{+0.34}_{-0.31}$$

$$\begin{aligned} & \frac{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)}{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)_{\text{SM}}} \\ &= (a_t^2 + 2.26b_t^2) \\ &\times \frac{0.035(-7.2 + 1.83a_t^2) + 0.27b_t^2}{R_\Gamma} \end{aligned}$$

$$\mu_{gg \rightarrow H \rightarrow \gamma\gamma} = 1.16^{+0.21}_{-0.18}$$



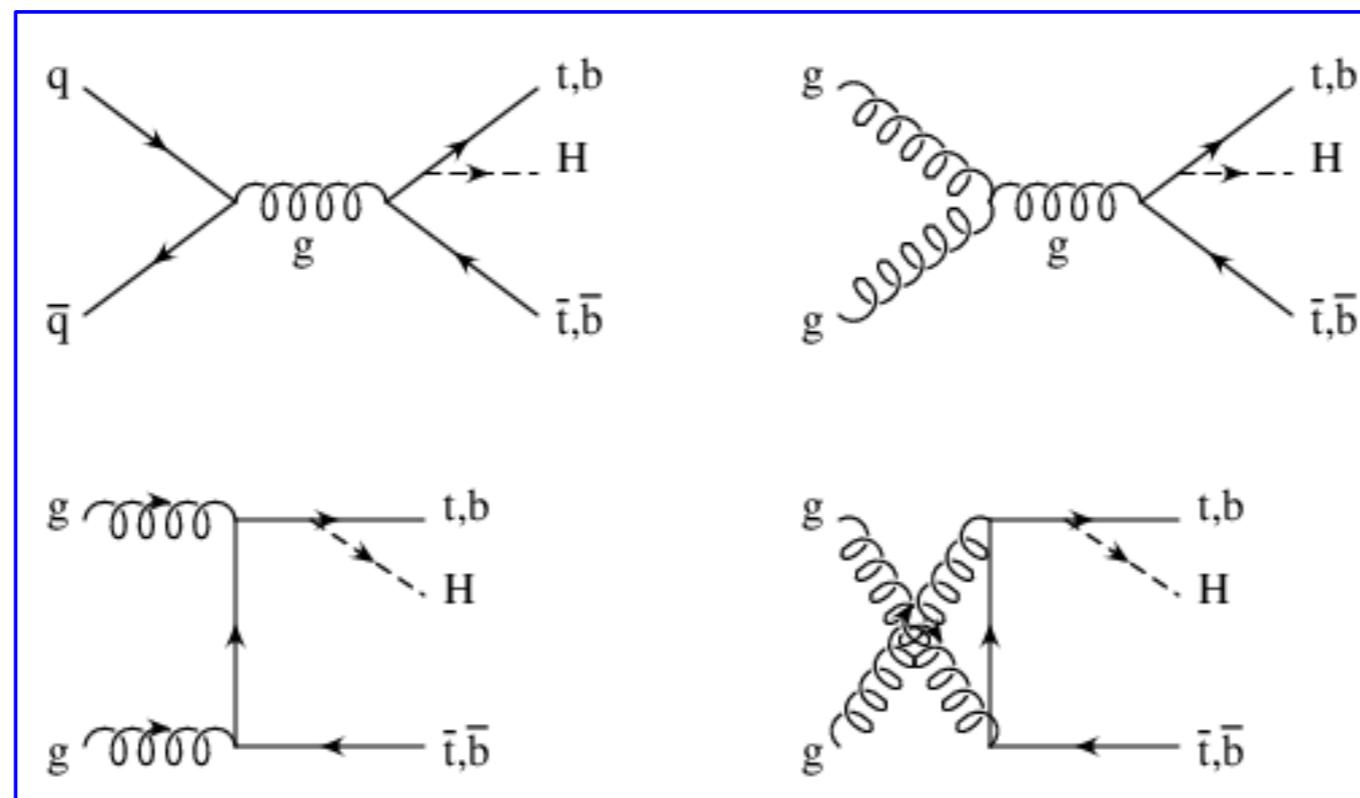
$$0.73 < a_t < 1.14, \quad -0.51 < b_t < 0.51$$

$$-\frac{\pi}{5} \leq \theta \leq \frac{\pi}{5}$$

We knew a little about the CP property of the Htt coupling **indirectly** from the cross sections of the single-Higgs production and ttH production.

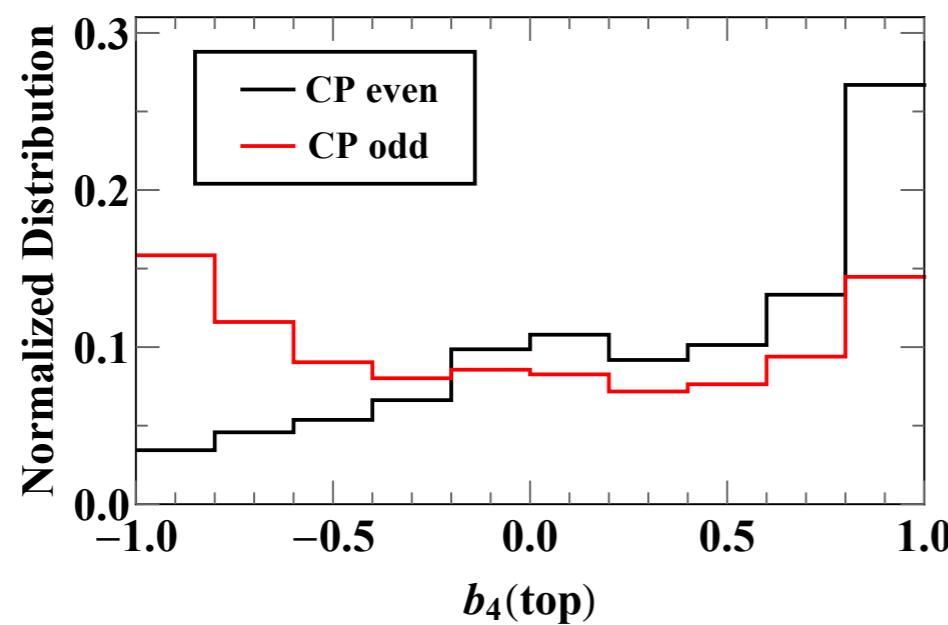
→ A pure CP-odd Htt coupling is not supported.

We still need measure it **directly** through the differential cross-sections of the ttH production.

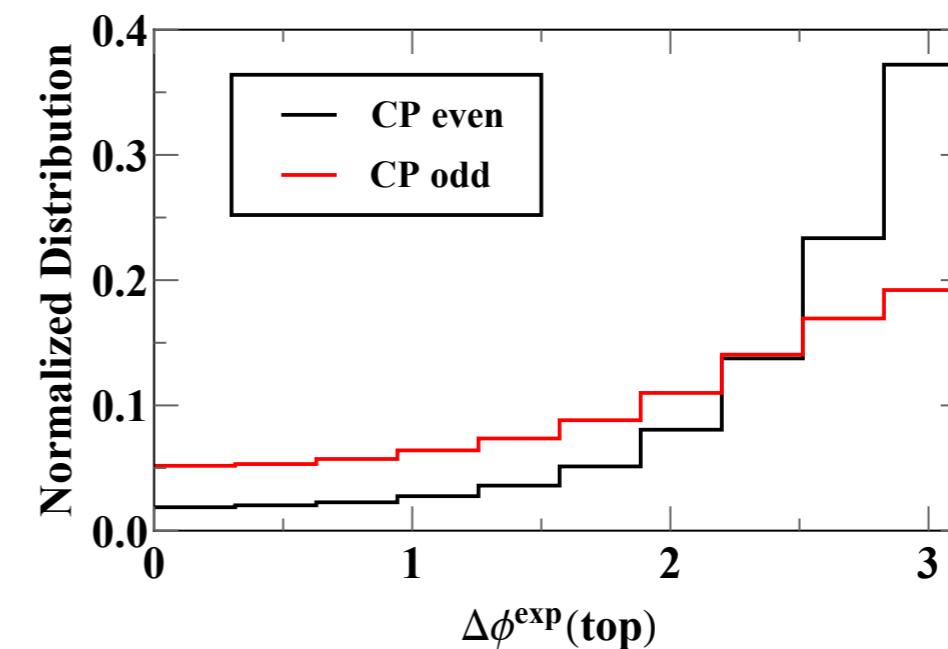


Measuring CP property of Htt coupling directly

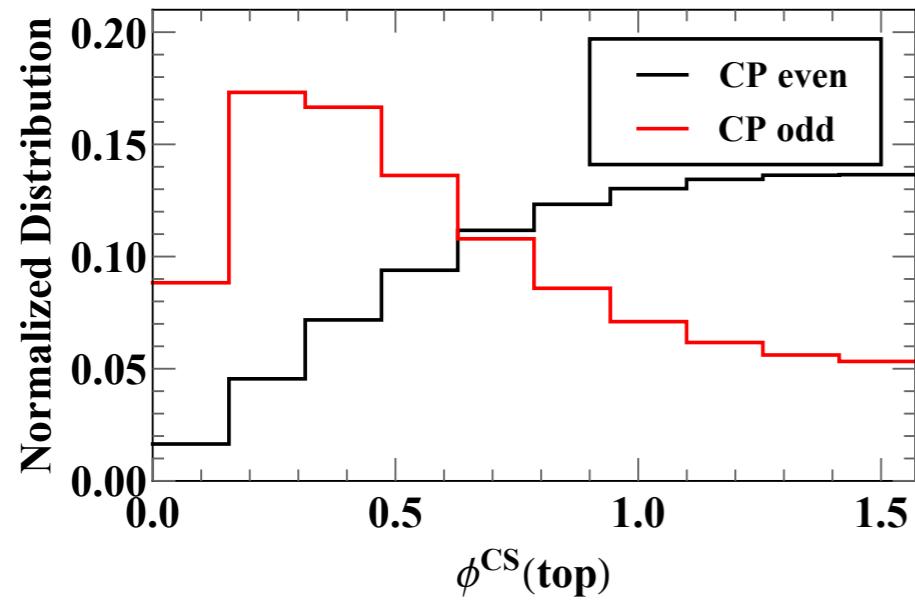
$$b_4(\text{top}) : \frac{p_t^z p_{\bar{t}}^z}{|p_t| |p_{\bar{t}}|}$$



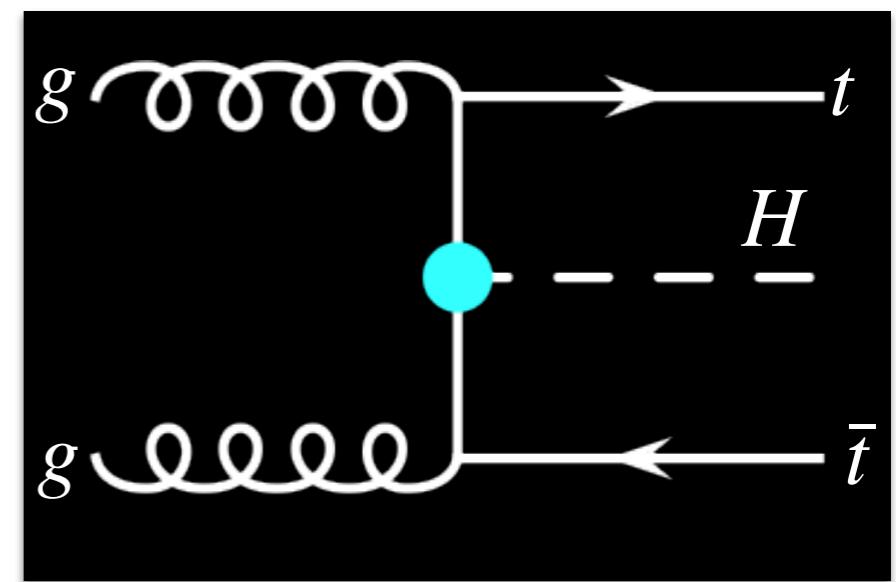
$$\Delta\phi^{\text{exp}}(\text{top}) : |\phi(t) - \phi(\bar{t})|$$



$$\phi^{\text{CS}}(\text{top}) : \left\langle \frac{\vec{p}_t}{|p_t|} - \frac{\vec{p}_{\bar{t}}}{|p_{\bar{t}}|}, \frac{\vec{p}_{g_1}}{|p_{g_1}|} - \frac{\vec{p}_{g_2}}{|p_{g_2}|} \right\rangle$$



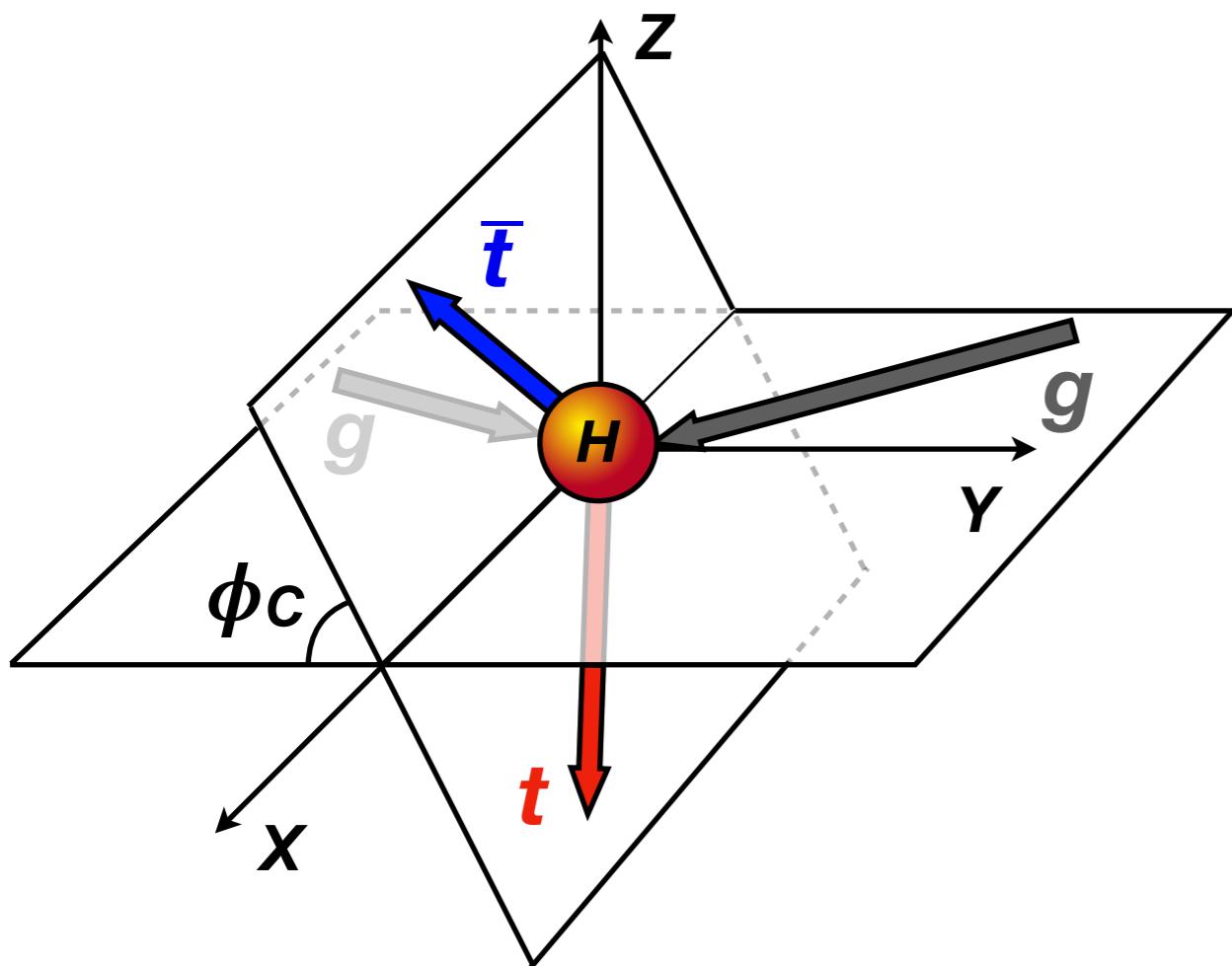
**open angle between
 $t\bar{t}$ line and external
bisector of gluons
in $t\bar{t}$ rest frame**



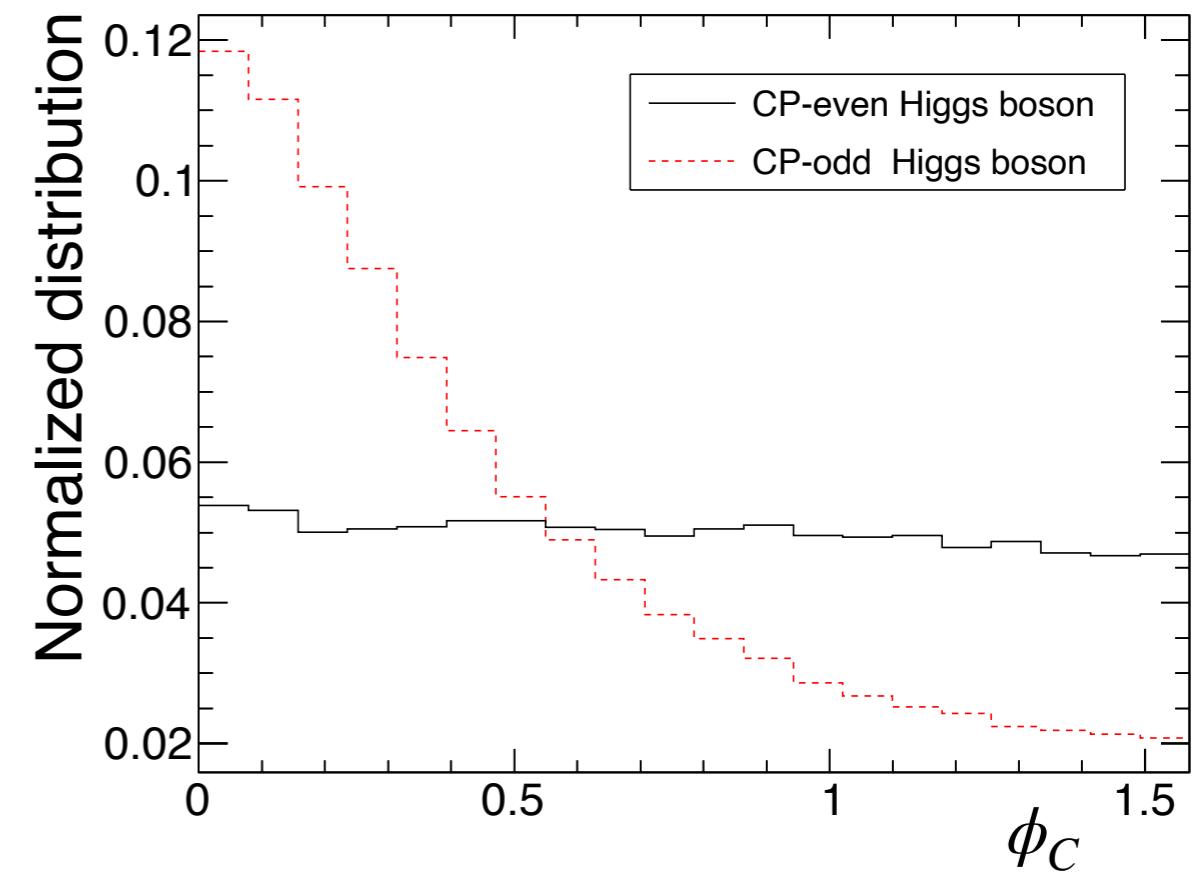
Decay plane correlation in ttH channel

QHC, Ke-Pan Xie, Hao Zhang, Rui Zhang, *Chin.Phys.C* 45 (2021) 2, 023117

- We propose a new observable which is very sensitive to the parity nature of the htt interaction.
- P transformation from the Higgs point of view.
 - A nature observable in the Higgs-rest frame:



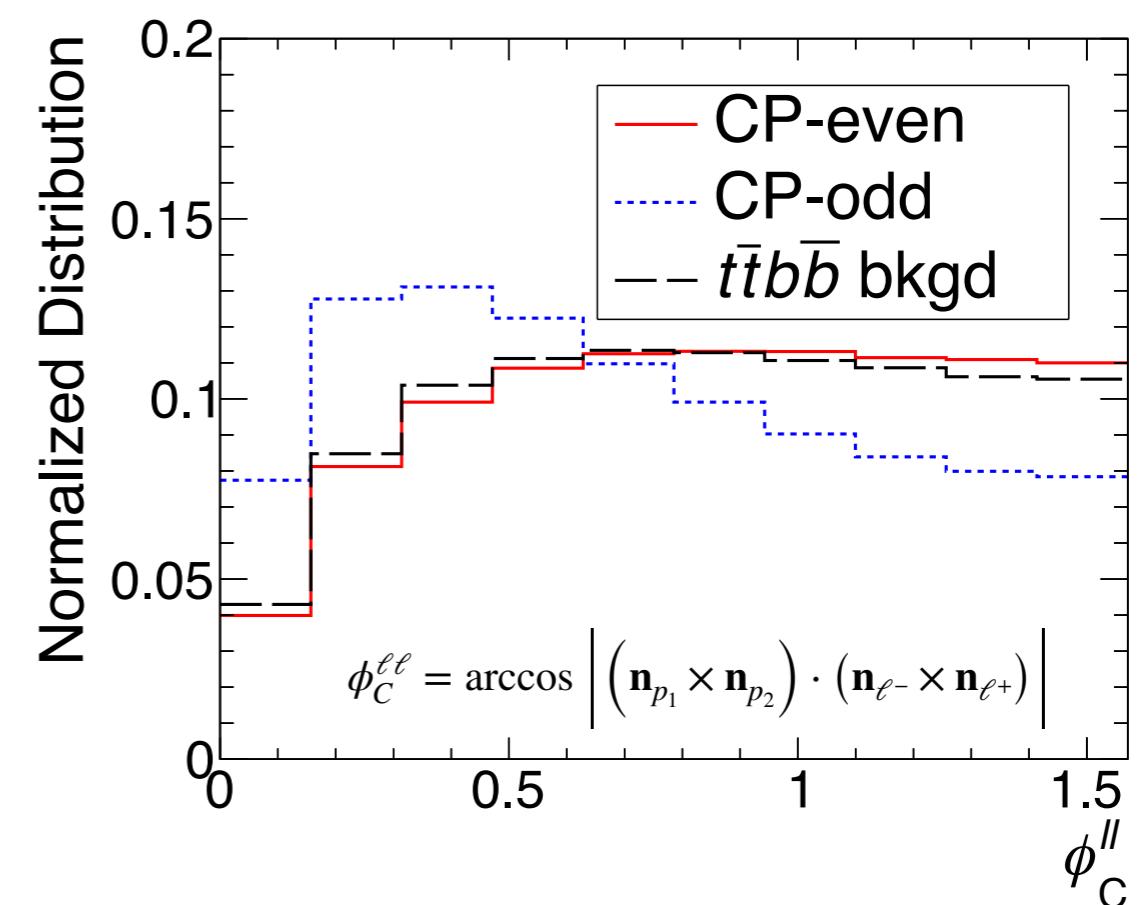
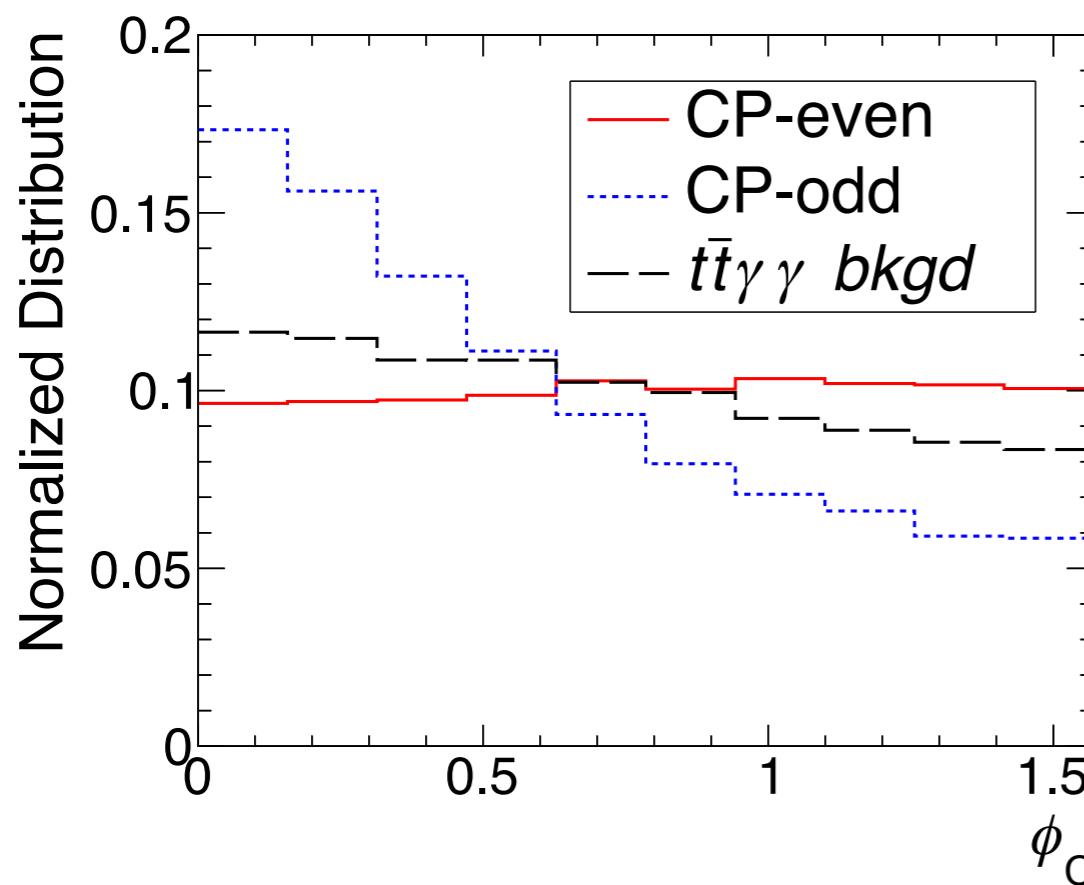
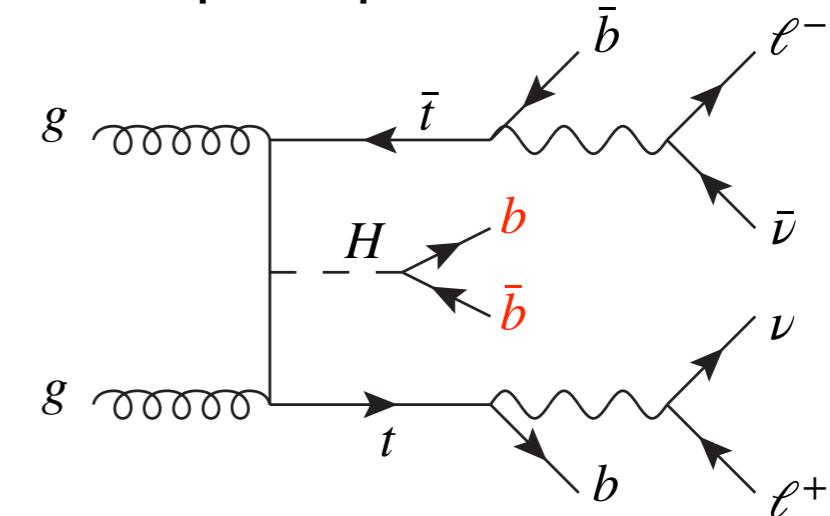
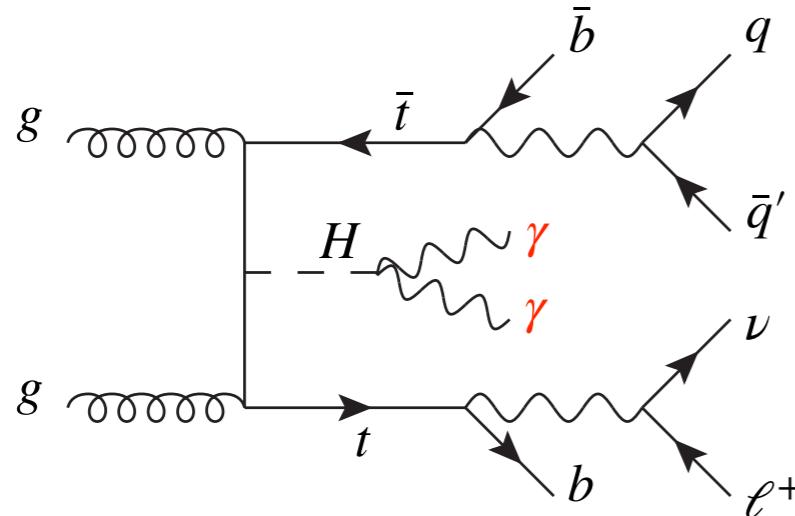
$$\phi_C = \arccos \left| (\mathbf{n}_{p_1} \times \mathbf{n}_{p_2}) \cdot (\mathbf{n}_t \times \mathbf{n}_{\bar{t}}) \right|$$



Diphoton Mode of Higgs decay

- Easy to reconstruct Higgs boson
- Clean signal but fewer events

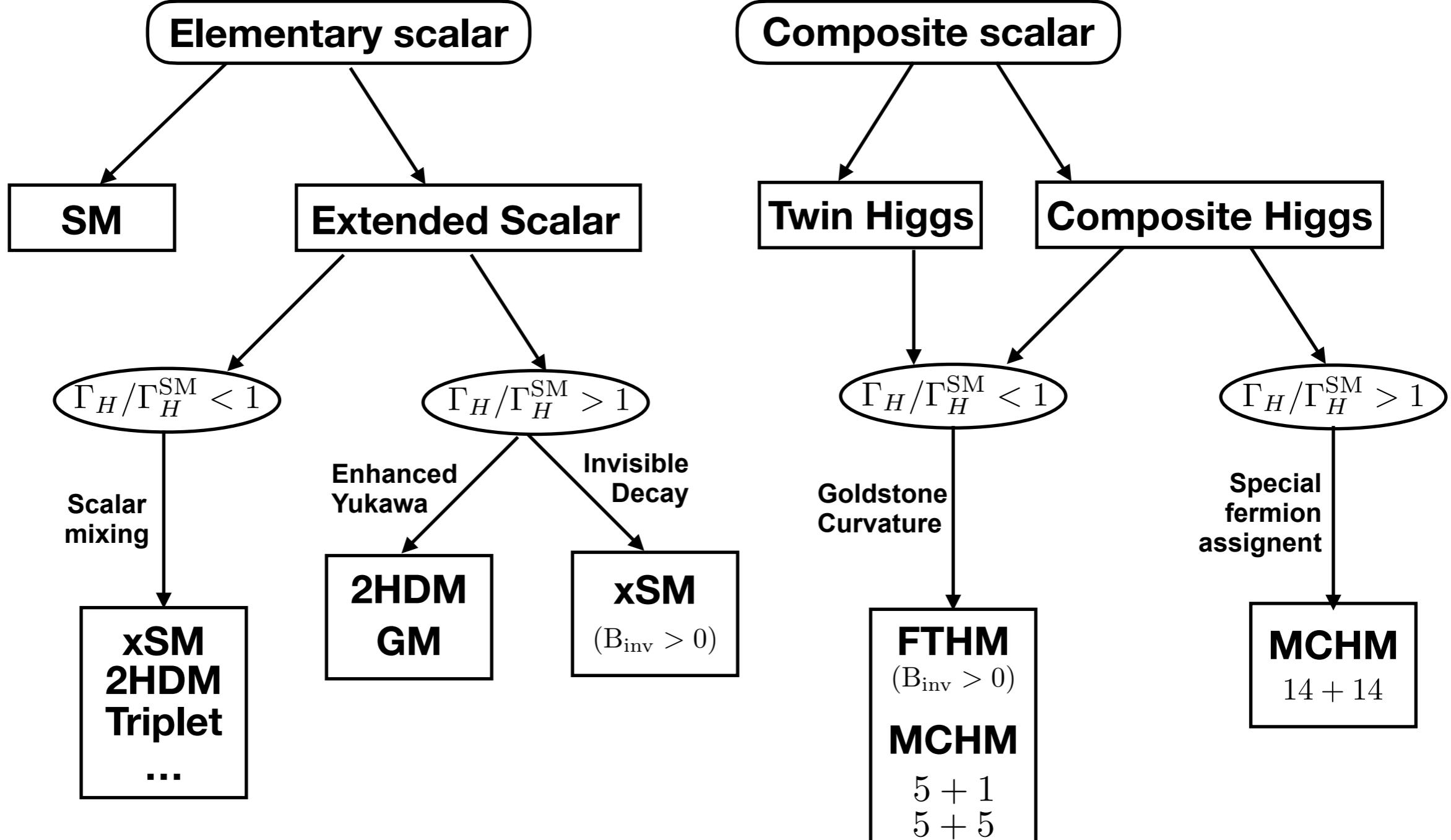
- Large event number.
- The top anti-top plane replaced by the dilepton plane.



4. Higgs boson width

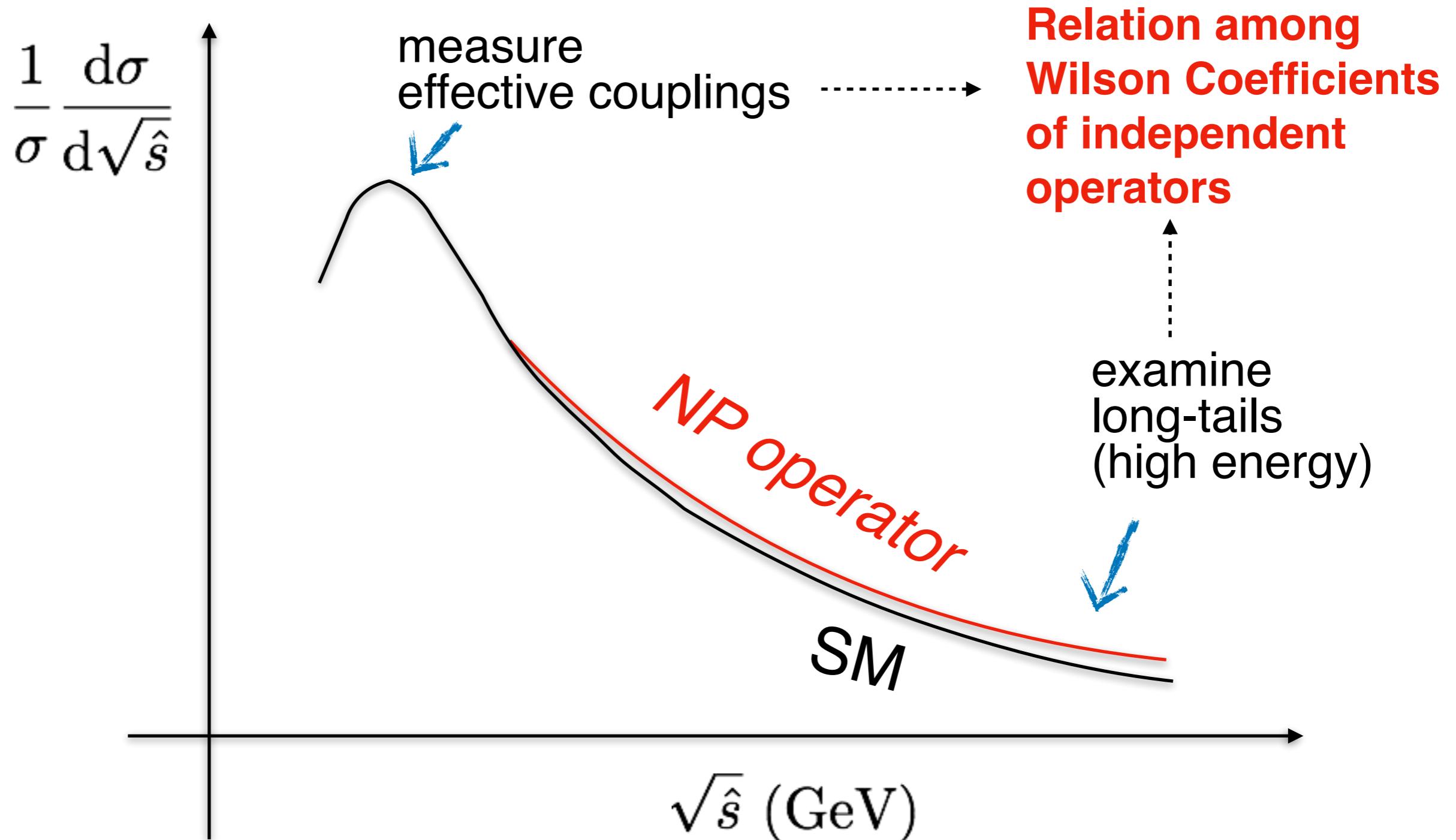
Nature of Higgs Boson

QHC, Li, Xu, Yu,
2107.08343

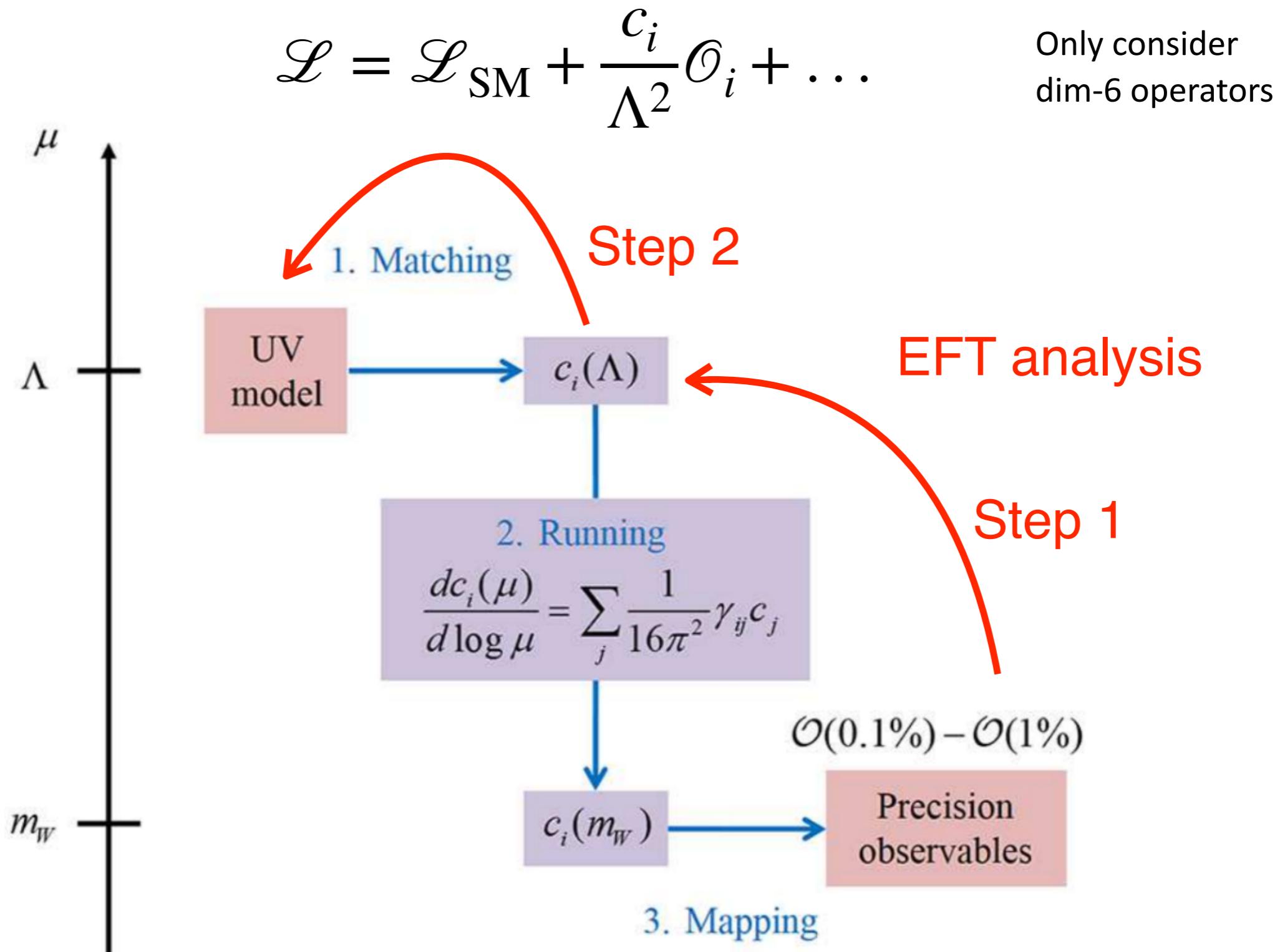


5. SMEFT analysis: Higgs & Top

in case of no new resonances found in next 10 years



Top-Higgs physics in SMEFT



SMEFT analysis

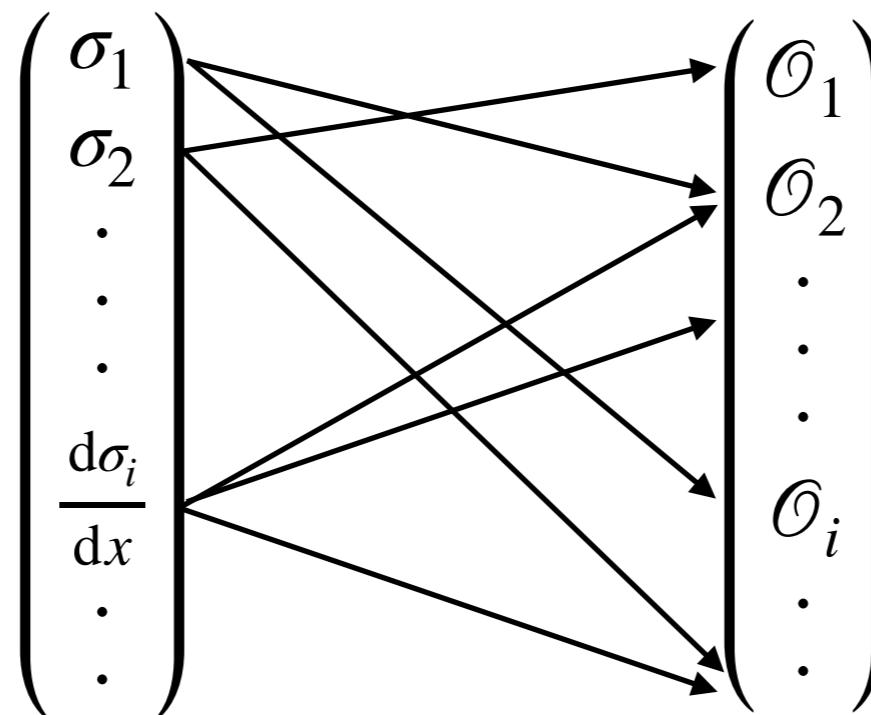
SMEFT

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i^{(6)} O_i^{(6)}}{\Lambda^2}$$

Measurements

$$o_n^{\text{EXP}} - o_n^{\text{SM}} = \sum_i \frac{a_{n,i}^{(6)}(\mu) c_i^{(6)}(\mu)}{\Lambda^2}$$

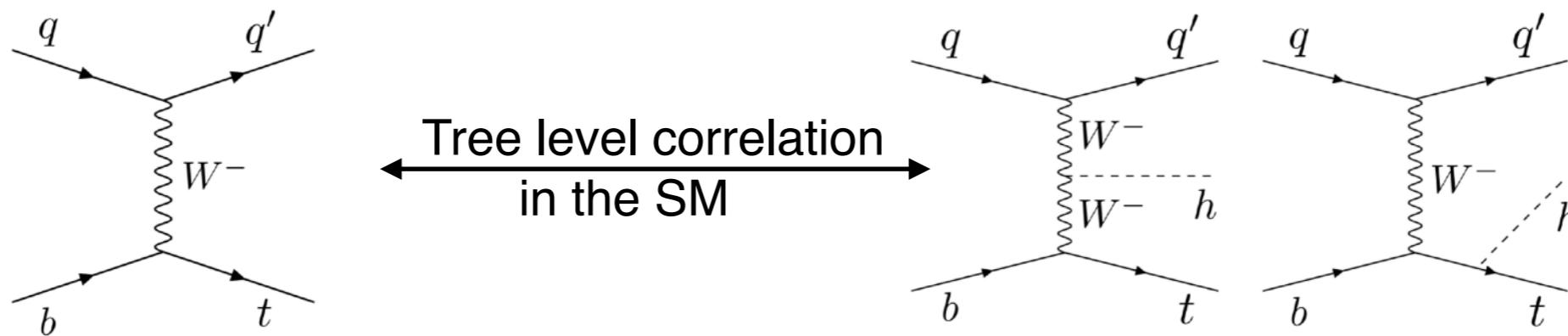
59 independent operators at dim-6



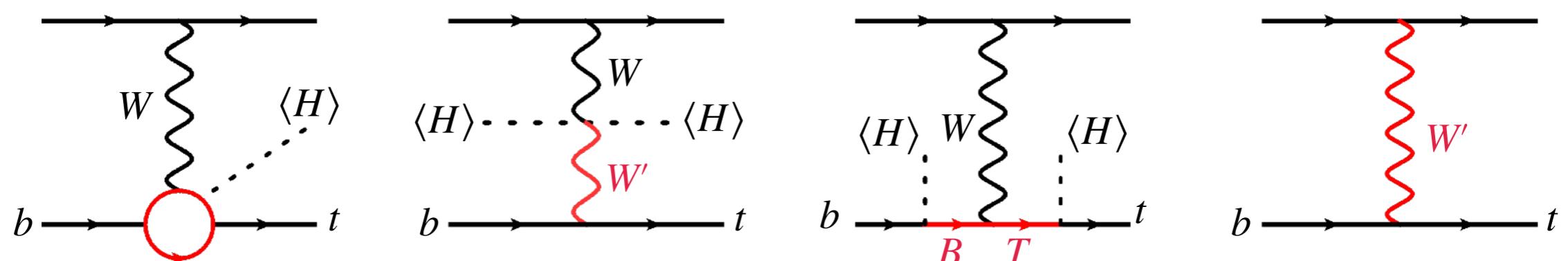
- 1) Linear (interference) or Quadratic (operator squared)? Dim-8?
- 2) RG running effect?
- 3) Operator Basis? Field and mass redefinitions?
- 4) QCD corrections? Operator mixings?

Single top production w/ and w/o a Higgs boson

QHC, Jiang, Zeng, 2105.04464



The correlation in the linear analysis in SMEFT



$$O_{uW} = (\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\phi} W_{\mu\nu}^I + h.c., \quad \text{WMD}$$

QHC, Wudka, Yuan, 0704.2809

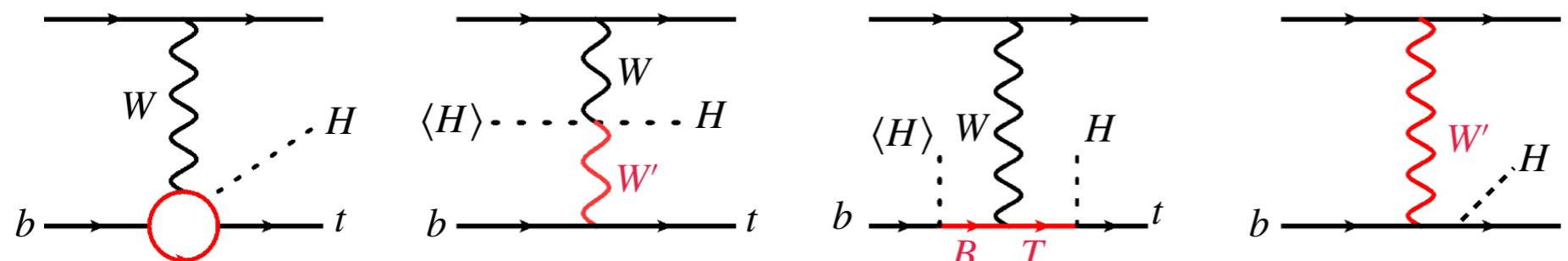
$$O_{\phi q}^{(3)} = (\phi^\dagger i \overset{\leftrightarrow}{D}_\mu^I \phi)(\bar{q}_p \tau^I \gamma^\mu q_r) + h.c., \quad \text{W-prime or Extra quarks}$$

$$\left. \begin{aligned} O_{qq}^{(1)} &= (\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t) + h.c., \\ O_{qq}^{(3)} &= (\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_p \gamma^\mu \tau^I q_r) + h.c.. \end{aligned} \right\} \rightarrow \begin{aligned} O_{3113}^{(1)} &= (\bar{q}_3 \gamma_\mu q_1)(\bar{q}_1 \gamma^\mu q_3) + h.c., \\ O_{3311}^{(3)} &= (\bar{q}_3 \gamma_\mu \tau^I q_3)(\bar{q}_1 \gamma^\mu \tau^I q_1) + h.c.. \end{aligned} \xrightarrow{\text{same interference}} O_{qq}^{(3)}$$

$$\sigma_t(\Lambda = 1 \text{TeV}) = \left[214_{-1}^{+2} - 13_{-1}^{+2} C_{qq}^{(3)} + 16_{-3}^{+2} C_{uW} + 13_{-2}^{+1} C_{\phi q}^{(3)} \right] \text{pb}$$

Single top production w/ and w/o a Higgs boson

Direct correlation induced by the three operators



For comprehensive EFT analysis of the tHq channel, see 1804.07773 (Degrande, Maltoni, Mimasu, Vryonidou, Zhang)

More operators involved in tHq channel but bounded

Operators

$$O_{\phi D} = (\phi^\dagger D^\mu \phi)^* (\phi^\dagger D_\mu \phi)$$

$$O_{\phi \square} = (\phi^\dagger \phi) \square (\phi^\dagger \phi)$$

$$O_{u\phi} = (\phi^\dagger \phi) (\bar{q}_p u_r \tilde{\phi}) + h.c.$$

$$O_{\phi W} = \phi^\dagger \phi W_{\mu\nu}^I W^{I\mu\nu}$$

Measurements

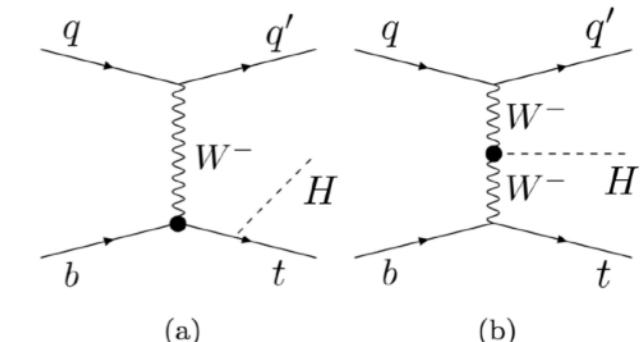
EWPT at LEP

$$gg \rightarrow H$$

$$H \rightarrow b\bar{b}$$

$$gg \rightarrow H, \quad gg \rightarrow t\bar{t}H$$

$$H \rightarrow ZZ^*/Z\gamma/\gamma\gamma$$



The same three operators contributing predominantly in the tHq channel

$$\sigma_{tHq}(\Lambda = 1 \text{ TeV}) = \left[70.0 - 11.3_{-0.3}^{+0.6} C_{qq}^{(3)} + 22_{-2}^{+1} C_{uW} - 2.6_{-0.2}^{+0.2} C_{\phi q}^{(3)} \right] \text{ fb}$$

Single top production w/ and w/o a Higgs boson

Three operators require at least three independent measurements; fortunately, single-top production provides richer info than expected.

$$\sigma_t = \sigma(tq) + \sigma(\bar{t}q) \longrightarrow O_{qq}^{(3)}, O_{uW'}, O_{\varphi q}^{(3)}$$

$$R_t \equiv \frac{\sigma(tq)}{\sigma(\bar{t}q)} \longrightarrow O_{qq}^{(3)}, O_{uW}$$

$$A_{FB} = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} \longrightarrow O_{uW}$$

$$\sigma_{tHq} = \left[-95.1 - 44.0 \times \frac{\sigma_{t+\bar{t}}}{\sigma_{t+\bar{t}}^{\text{SM}}} - 266.0 \times \frac{A_{\text{FB}}}{A_{\text{FB}}^{\text{SM}}} + 479.4 \times \frac{R_t}{R_t^{\text{SM}}} \right] \text{ fb}$$

Current ↓

$$\sigma_{tHq} = [106.8 \pm 64.8] \text{ fb}$$

HL-LHC ↓

$$\sigma_{tHq} = [74.3 \pm 45.4] \text{ fb}$$

The relation serves for checking the consistency of SMEFT.

Conclusion

It is very challenging but we need measure the HHH coupling from all possible ways to probe the scalar potential.

We are in the era of Higgs precision!

Precision measurements of Higgs couplings would shed lights on new physics beyond the SM.

Thank You!