

The analysis of $B_s \rightarrow \phi \nu \bar{\nu}$ At CEPC

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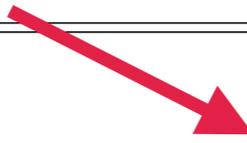
1. Introduction and Motivation
2. Signal and background
3. Reconstruction of ϕ
4. Events analysis
5. Results and conclusion

Luminosity and Statistics

CEPC scheme

operation mode	Z factory	WW threshold scan	Higgs factory
center-of-mass energy (GeV)	91.2	160	240
running time (yeas)	2	1	7
L ($10^{34} \text{cm}^{-2} \text{s}^{-1}$)	32	10	3
intergrated luminosity (ab^{-1})	16	2.6	5.6
Higgs yield	-	-	10^6
W yield	-	10^7	10^8
Z yield	10^{12}	10^8	10^8

Provides unique opportunities
for various **flavor measurements**



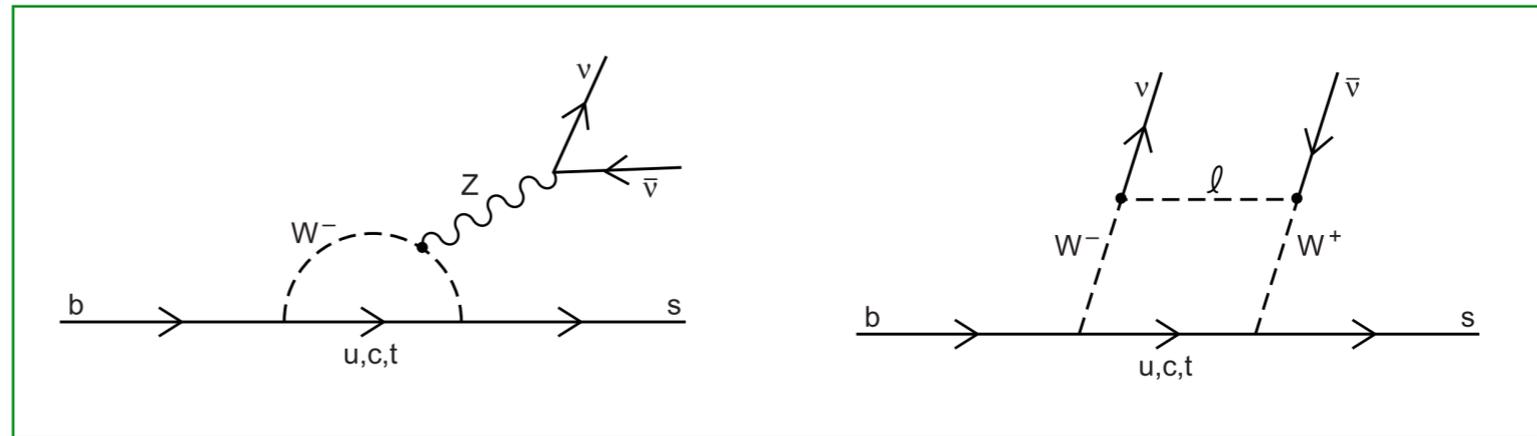
$$\begin{aligned}
 Z \rightarrow b\bar{b} & : \sim 1.5 \times 10^{11} \\
 Z \rightarrow c\bar{c} & : \sim 1.2 \times 10^{11} \\
 Z \rightarrow \tau^+\tau^- & : \sim 3.37 \times 10^{10}
 \end{aligned}$$

Huge B flavor physics potential of Tera-Z, especially B_s , B_c and Λ_b ...

Channel	Belle II	LHCb	Giga-Z	Tera-Z	10×Tera-Z
B^0, \bar{B}^0	5.3×10^{10}	$\sim 6 \times 10^{13}$	1.2×10^8	1.2×10^{11}	1.2×10^{12}
B^\pm	5.6×10^{10}	$\sim 6 \times 10^{13}$	1.2×10^8	1.2×10^{11}	1.2×10^{12}
B_s, \bar{B}_s	5.7×10^8	$\sim 2 \times 10^{13}$	3.2×10^7	3.2×10^{10}	3.2×10^{11}
B_c^\pm	-	$\sim 2 \times 10^{11}$	2.2×10^5	2.2×10^8	2.2×10^9
$\Lambda_b, \bar{\Lambda}_b$	-	$\sim 2 \times 10^{13}$	1.0×10^7	1.0×10^{10}	1.0×10^{11}

Rare decay $b \rightarrow s\nu\bar{\nu}$

The decay rates of exclusive channel by SM ranges from $10^{-6} \sim 10^{-5}$.



- Difficulty on the experimental

Direct measurement on $\nu\bar{\nu}$ system is difficult

Need the full reconstruction technique

Large luminosity

PFA algorithm at CEPC

- Main experiments attempted at B factory

None have been found

- The precise measurement are expected in the future e^+e^- collider

	Experimental [2]	SM Prediction [3, 4]
$\text{BR}(B^0 \rightarrow K^0 \nu\bar{\nu})$	$< 2.6 \times 10^{-5}$	$(2.17 \pm 0.30) \times 10^{-6}$
$\text{BR}(B^0 \rightarrow K^{*0} \nu\bar{\nu})$	$< 1.8 \times 10^{-5}$	$(9.48 \pm 1.10) \times 10^{-6}$
$\text{BR}(B^\pm \rightarrow K^\pm \nu\bar{\nu})$	$< 1.6 \times 10^{-5}$	$(4.68 \pm 0.64) \times 10^{-6}$
$\text{BR}(B^\pm \rightarrow K^{*\pm} \nu\bar{\nu})$	$< 4.0 \times 10^{-5}$	$(10.22 \pm 1.19) \times 10^{-6}$
$\text{BR}(B_s \rightarrow \phi \nu\bar{\nu})$	$< 5.4 \times 10^{-3}$	$(11.84 \pm 0.19) \times 10^{-6}$

DELPHI

Rare decay $b \rightarrow s\nu\bar{\nu}$

- Investigation of flavor-changing neutral current (FCNC) decays is of fundamental interest
- Large luminosity and advantage on the τ , B_s , B_c , Λ_b ... measurements especially the missing final state rare decay
- Rare FCNC decay $b \rightarrow s\nu\bar{\nu}$ is free from strong interaction effects and not affected by non-factorizable corrections, theoretically cleaner compared to $b \rightarrow \phi\ell\ell$ transitions.
- Observation of this decay could test the SM prediction and provide opportunity to explore new physics.
- Performance the benchmark of simulation and reconstruction at CEPC, such as charged lepton identify, $\phi(1020) \rightarrow K^+K^-$ reconstruction, boson mass resolution (BMR) and missing energy, mass.

The Signal Topology

Number of signal decay by SM prediction at CEPC :

$$N(B_s \rightarrow \phi(K^+K^-)\nu\bar{\nu}) \sim 1.8 \times 10^5 \times 0.492$$

Branch of $B_0 \rightarrow \phi\nu\nu$ is much smaller than $B_s \rightarrow \phi\nu\nu$ and thus **free of the B_0 influence.**

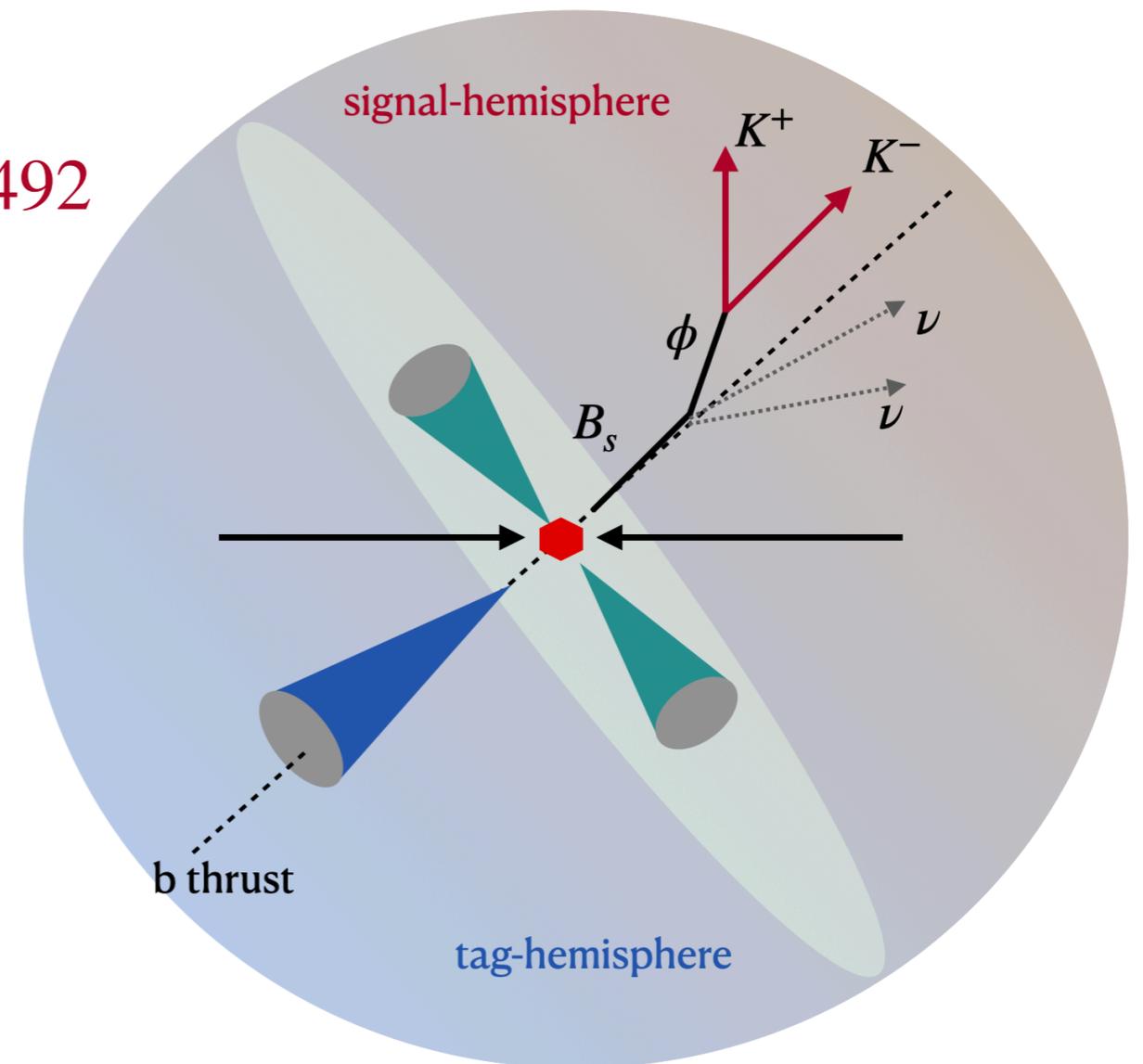
Signal ϕ reconstruction:

$$\phi \rightarrow K^+K^- \text{ (49.2\%)}$$

Signal samples:

10^6 signal events by Pythia8 with EvtGen

$$e^+e^- \rightarrow Z \rightarrow b\bar{b}, \bar{b} \rightarrow B_s X, B_s \rightarrow \phi\nu\bar{\nu}$$



The Background

Generator : CEPC official - whizard-1.9.5

General background

- The $q\bar{q}$ events especially the heavy-flavor $b\bar{b}$ and $c\bar{c}$
- $10^6 \sim 10^7$ full simulation samples for each channel

Main background

- The semi-leptonic decay of $B^{(*)}$ or $D^{(*)}$ decay
 $b\bar{b} : b \rightarrow B(B^*) \rightarrow D(D^*)\ell\nu_\ell$ with $D(D^*) \rightarrow \phi X$
- One or more ϕ produced and decay to K^+K^- pair
- Significant missing energy
- Full simulation samples generated corresponding to $\sim 3 \times 10^8$ for each heavy-flavor channel

At CEPC, with 1.5×10^{11} $b\bar{b}$ events, the expected advance?

- More than 5 higher order of magnitude than current limit ($2.844 \times 10^6 e^+e^- \rightarrow Z$)
- At least 2-3 order optimization for the branch limit
- Test the SM prediction precisely

ϕ reconstruction

Reconstruct the decay $\phi(1020) \rightarrow K^+K^-$

- Lose $\sim 50\%$ signal decay inevitable
- Take pairs of oppositely charged tracks in the jet chamber
- Assuming both tracks to be Kaons (**No Kaon PID yet**)
- Employ the kinematic fit package for ILC to reconstruct the secondary vertex

Suehara, T. & Tanabe, T. LCFIPlus: A framework for jet analysis in linear collider studies. *Nucl Instruments Methods Phys Res Sect Accel Spectrometers Detect Assoc Equip* **808**, 109–116 (2016).

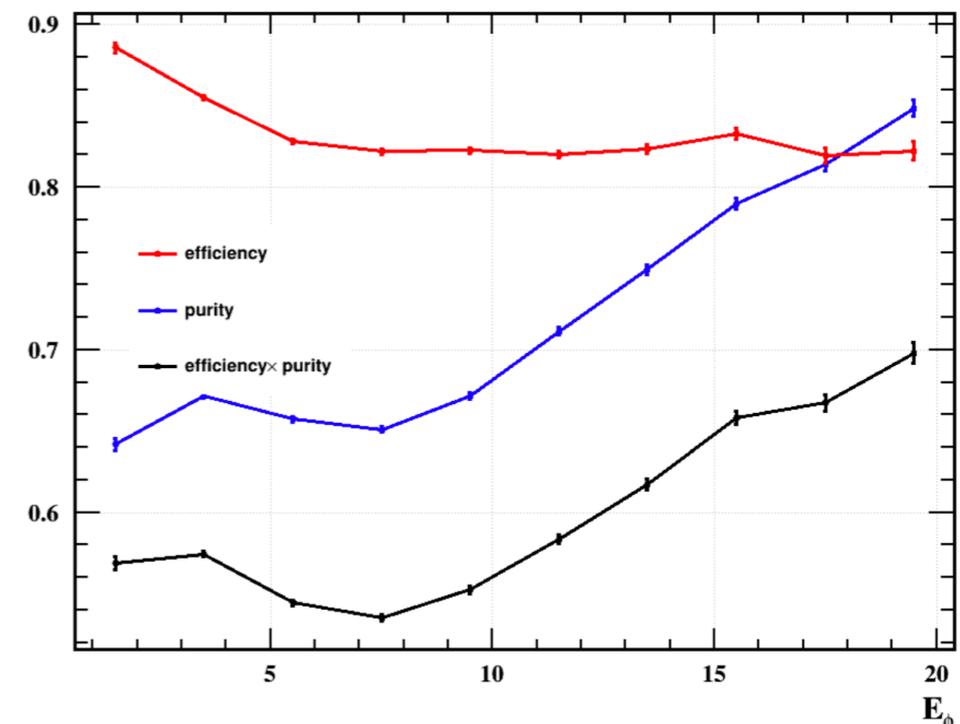
- Form their invariant mass

$$|M_{trk1,trk2} - M_\phi| < 0.01 \text{ GeV}$$

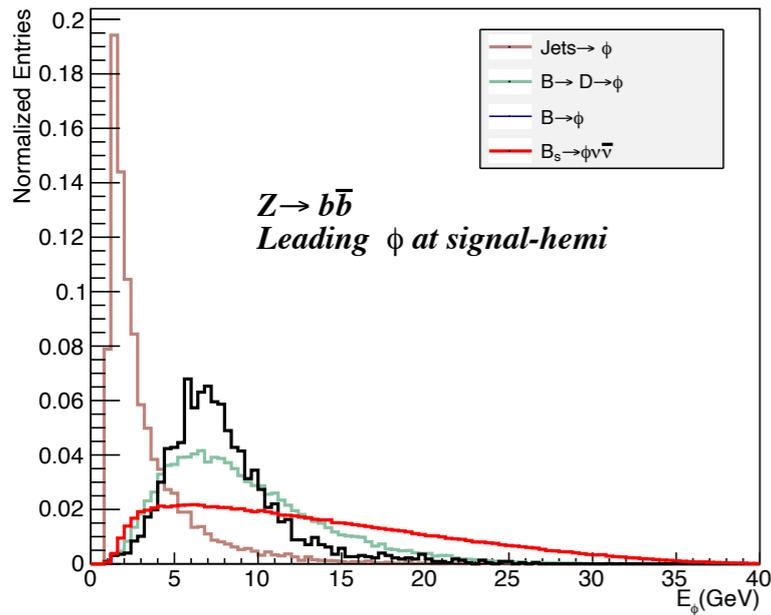
The ϕ reconstruction efficiency and purity for general background

$$\epsilon = \frac{\text{Number of correctly selected track pair candidates}}{\text{Number of } \phi \rightarrow K^+K^- \text{ events}}$$

$$p = \frac{\text{Number of correctly selected track pair candidates}}{\text{Number of selected track pair candidates}}$$

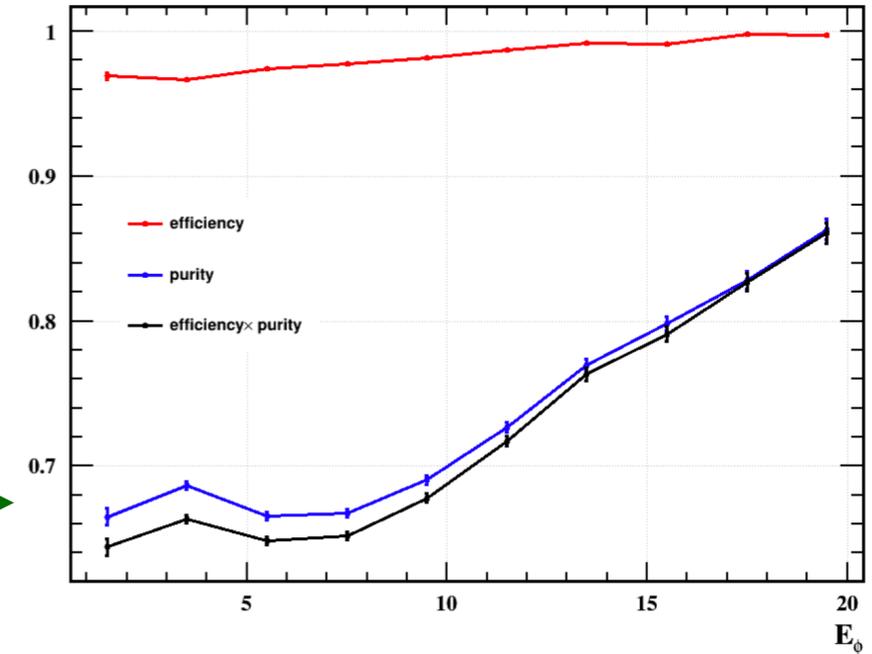


ϕ reconstruction



In the $B_s \rightarrow \phi \nu \bar{\nu}$ analysis

- ϕ in signal-hemisphere
- Leading energy one

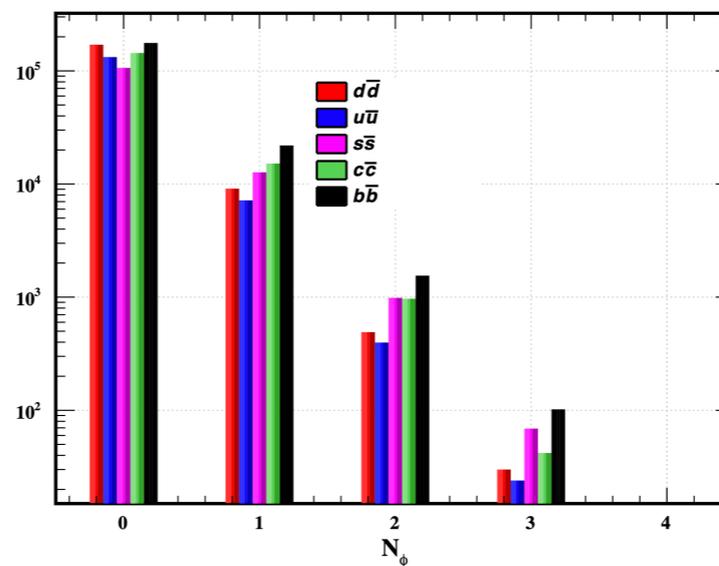


- Integrated efficiency and luminosity

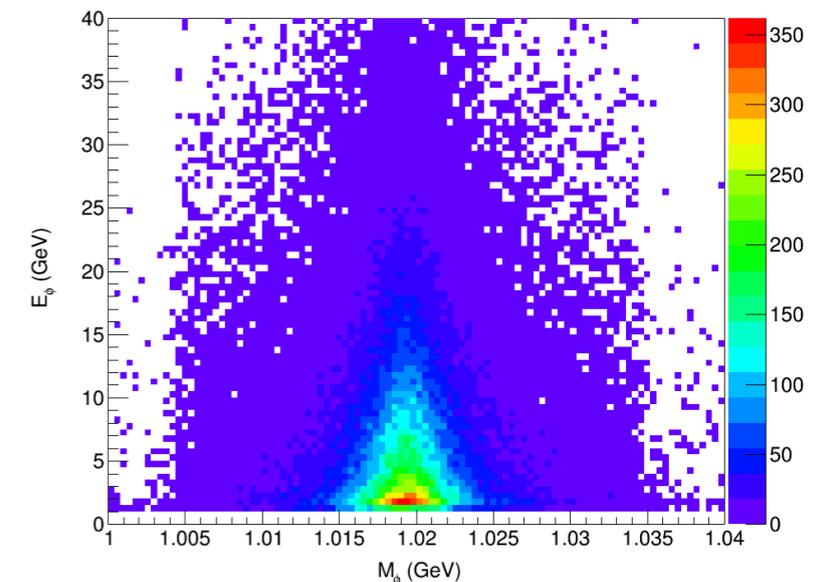
0.9790 and 0.7062

By ϕ with track pair decay in signal-sphere, background are suppressed by about 1/40

Potential optimization space for purity by Kaon PID ?



Number of ϕ distributions for each channel



Energy-Mass distribution of reconstructed ϕ

Events Analysis By ϕ

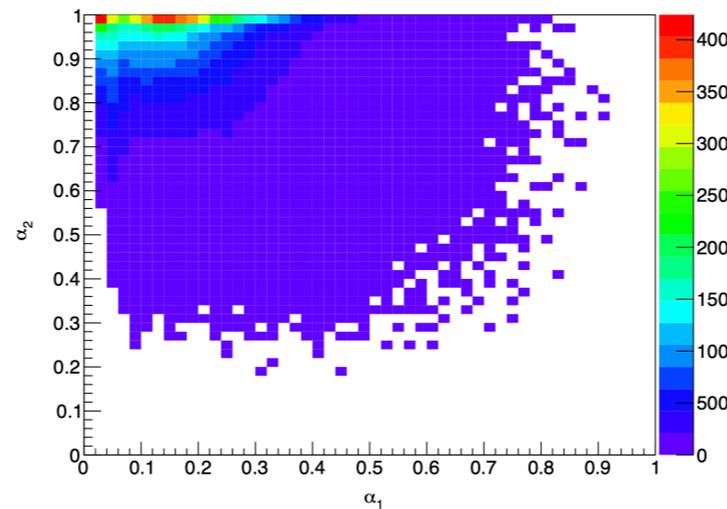
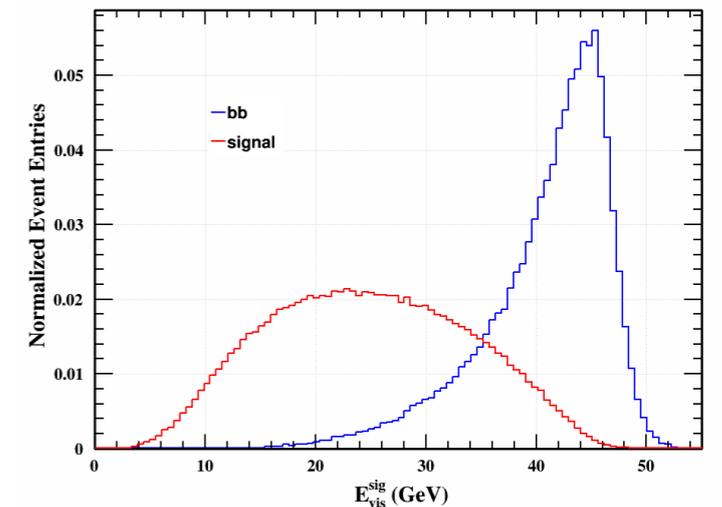
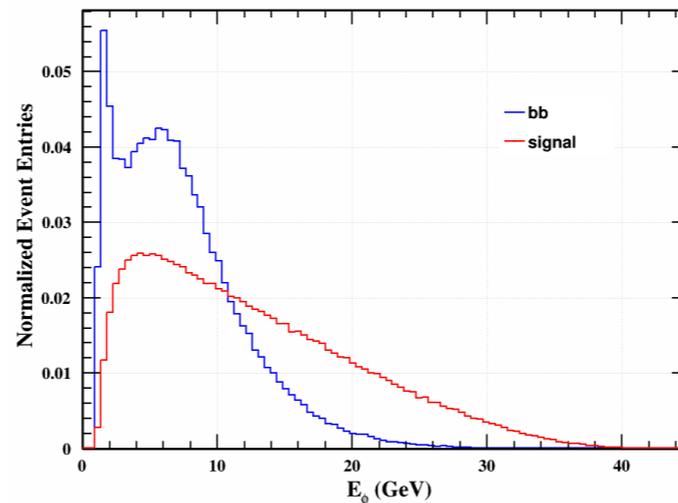
Now, we have a leading ϕ with its kinematic and vertex

Define the scaleless variables $\alpha_1 = \frac{E_\phi}{E_{vis}^{sig}}$ and $\alpha_2 = \frac{E_{vis}^{sig}}{E_{beam}}$

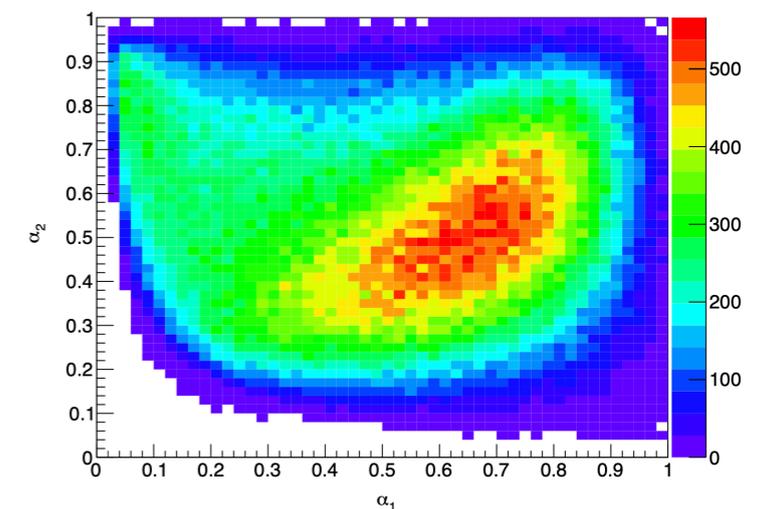
E_{vis}^{sig} is the energy of signal-hemisphere
and $E_{beam} = 45.6$ GeV

α_1 and α_2 show the strong
correlation between missing
energy, signal-hemi energy
and ϕ energy.

Significant difference of $\alpha_2 - \alpha_1$
distribution for background
and signal events.

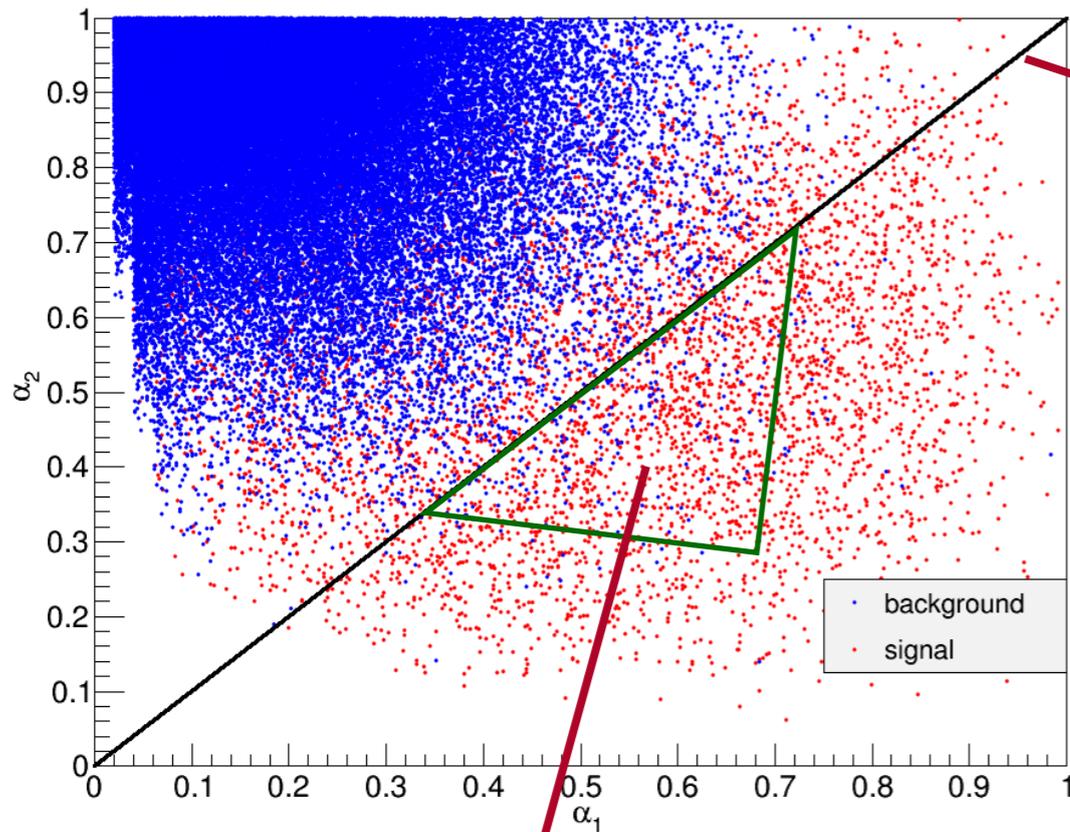


$b\bar{b}$ background



Signal events

Events Analysis By ϕ

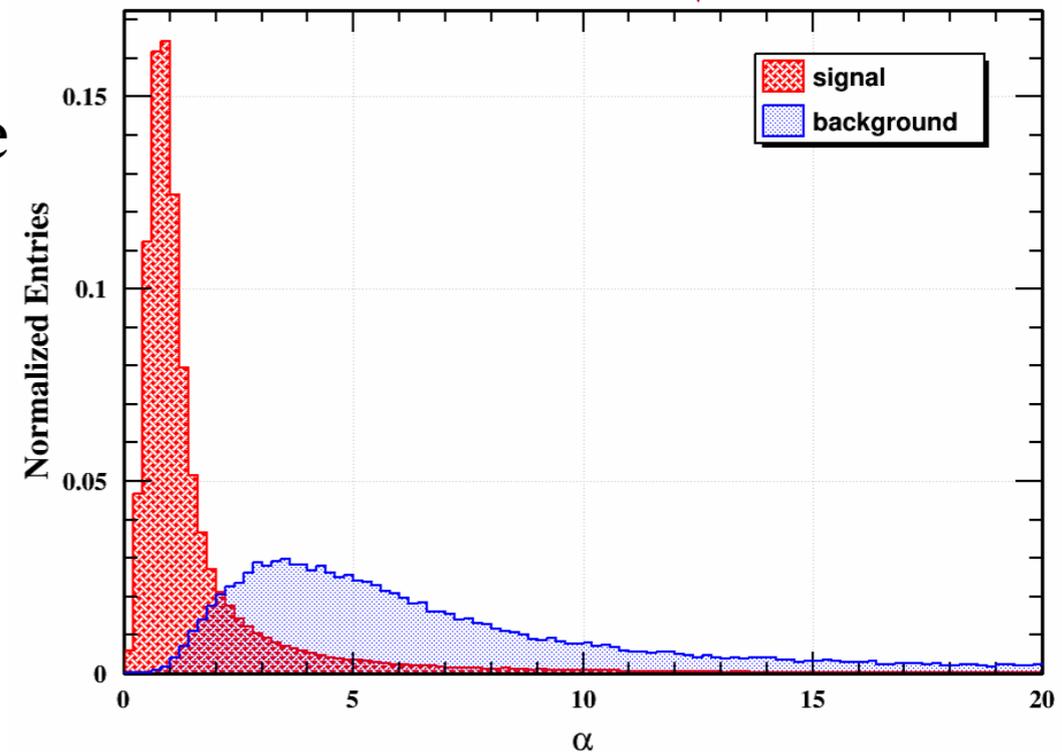


The other complex unlinear region will be analysis by BDT method of TMVA

Loose boundary defined by

$$\alpha = \frac{\alpha_2}{\alpha_1} = \frac{(E_{vis}^{sig})^2}{E_\phi \cdot E_{beam}}$$

The accuracy of α depend on the BMR (is about 4 % of CEPC in simulation)



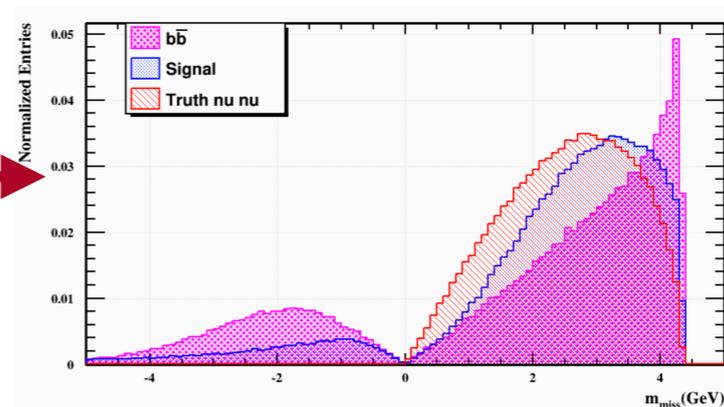
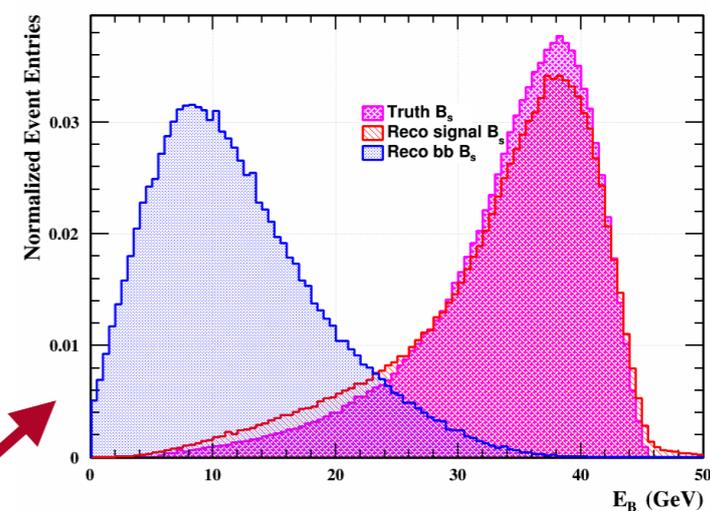
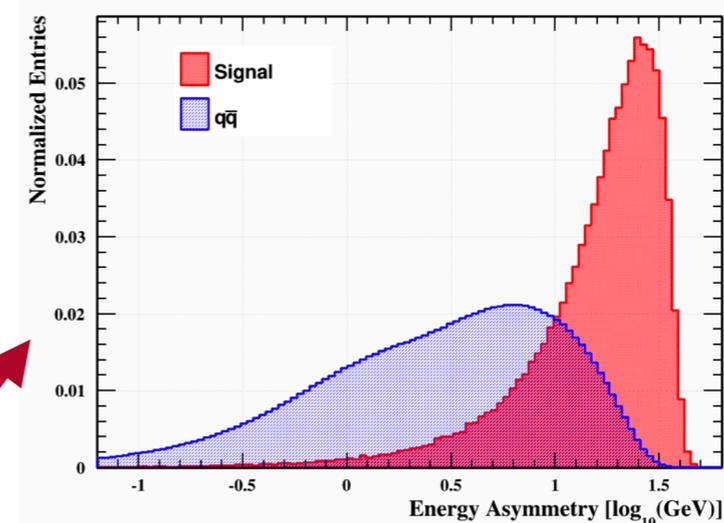
Analysis of $\nu\bar{\nu}$ System

Indirect measurement by the **full reconstruction**

The general missing energy in the whole events

The detail of missing energy origin.

- In the signal hemisphere, whether the missing energy count for mostly energy except ϕ . ($\alpha_1 = E_\phi/E_{sig}$)
- Whether the missing energy come from the signal-hemisphere. ($\alpha_2 = E_{sig}/E_{beam}$ and $E_{asymmetry}$)
- The possibility that missing energy come from the same mother particle as ϕ .
- An algorithm to get the signal energy of B_s and mass of $\nu\bar{\nu}$



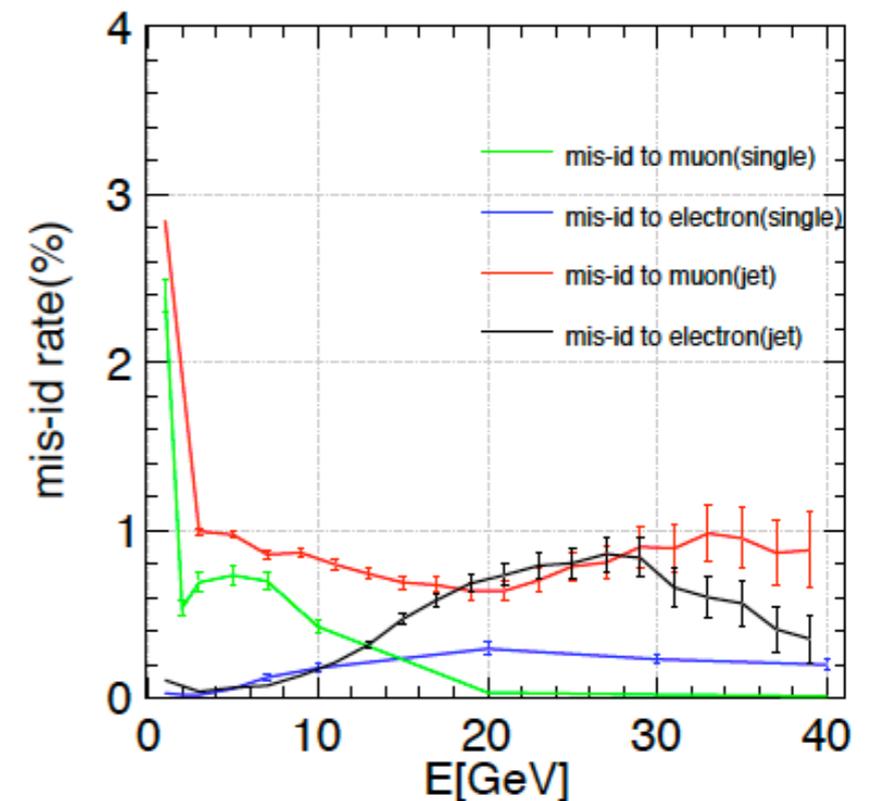
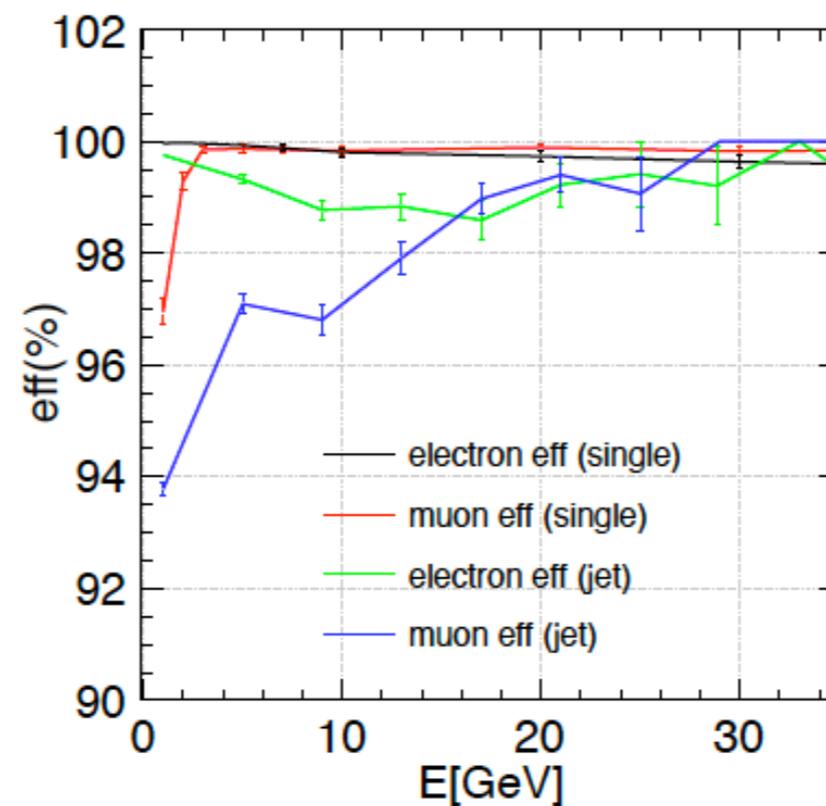
Analysis

Charged Lepton Identify

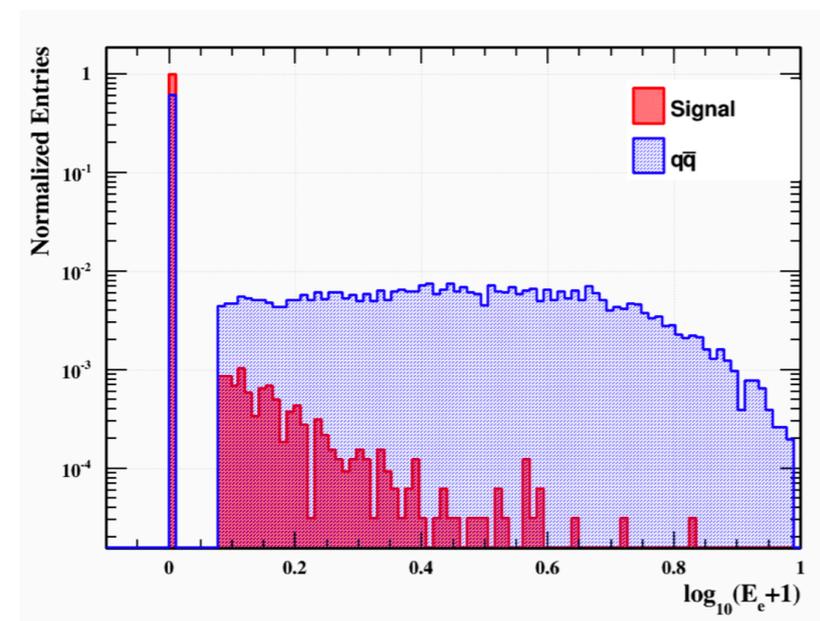
No charged lepton generated in the signal hemisphere for signal decay

Main background usually generated accompanied with a charged lepton

Good performance for the charged lepton as the energy larger than 1 GeV



Charged lepton (muon and electron) identify by DanYu.

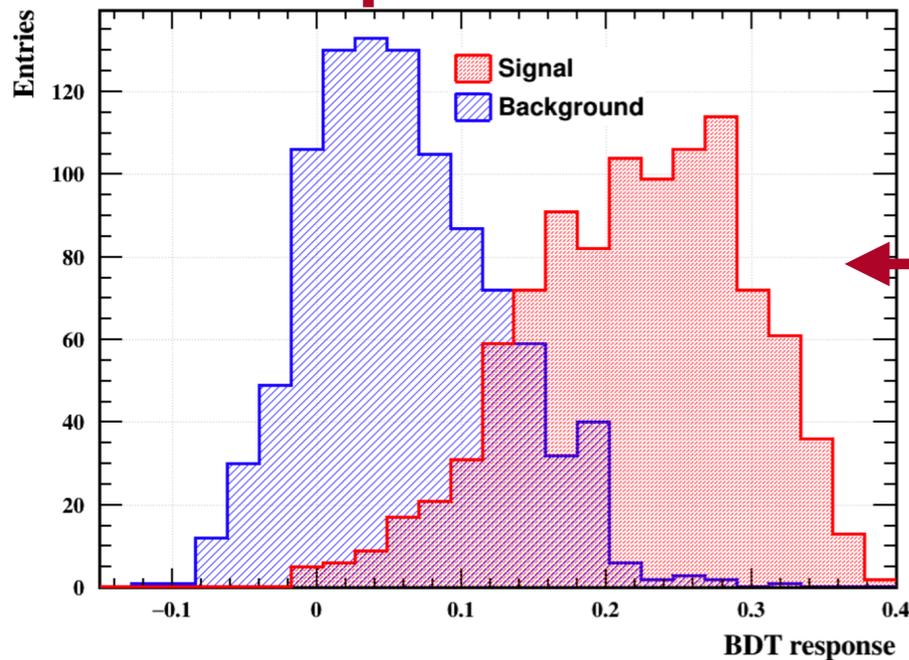


Samples satisfy $N_\phi > 0$ and $\alpha < 1.0$

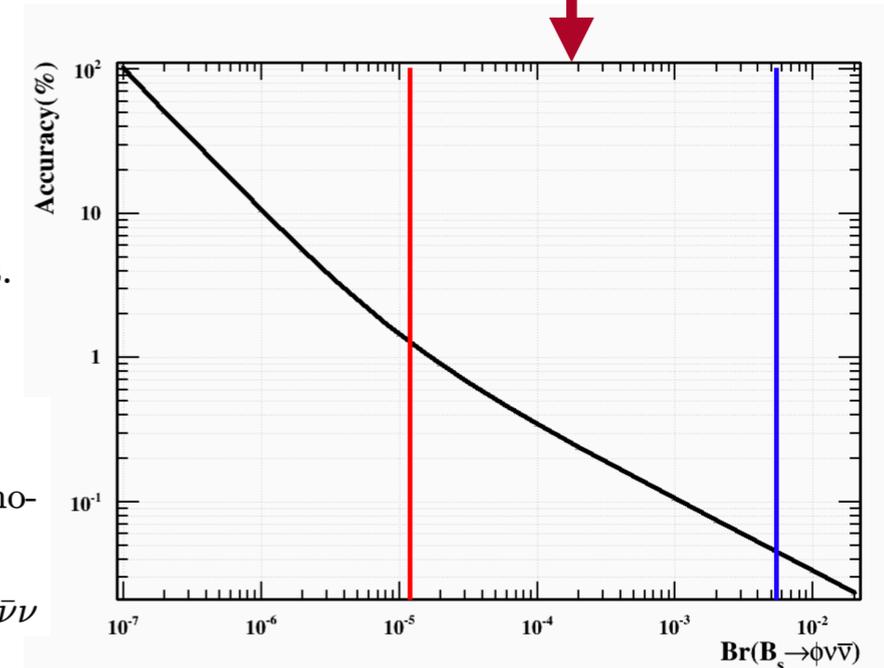
Cut chain and result

conditions	$B_s \rightarrow \phi\nu\bar{\nu}$	$u\bar{u}$	$d\bar{d}$	$s\bar{s}$	$c\bar{c}$	$b\bar{b}$	total bkg	$\sqrt{S+B}/S$ (%)
total generated	1.8e5	1.12e11	1.585e11	1.58511	1.20e11	1.51e11	7e11	464.81
b-tag > 0.6	1.359e5	8.0931e8	1.18558e9	1.1685e9	8.2392e9	1.1852e11	1.2992e+11	265.22
$N_{\phi(\rightarrow K^+K^-)} > 0$ at signal-hemisphere	51171	1.06277e7	1.30285e7	3.29526e7	2.15203e8	3.84348e9	4.11529e9	125.36
$E_\phi < 45$ GeV Kaon IP > 0.008 mm Energy asymmetry > 8 GeV	42054	3.3382e6	3.07042e6	6.26759e6	4.86347e7	1.04533e9	1.10665e9	79.10
Energy total < 85	40579	408759	746859	856441	1.28413e7	5.30604e8	5.45457e8	57.56
$E_{B_s} > 30$ GeV	32033	68126	0	38929	1.18081e6	4.93844e7	5.06723e7	22.23
$\alpha < 1.0$	22699	0	0	0	516605	7.70471e6	8.22132e6	12.65
$E_\mu < 1.1$ GeV and $E_e < 1.0$ GeV	20091	0	0	0	110922	2.18398e6	2.2949e6	7.57
$(1 - \alpha_1)/\theta_{<miss,\phi}> < 2.0$	13543	0	0	0	29060	426879	455940	5.06
BDT score > 0.20	7285	0	0	0	0	5240	5240	1.45
Efficiency(%)	4.687	0	0	0	0	3.47e-6	7.49e-7	

Good separation performance



- The scaleless ratio α_1 .
- The scaleless ratio α_2 .
- The invariant mass of all visible final states.
- The invariant mass of tag hemisphere.
- The invariant mass of signal hemisphere.
- The angle between missing momentum and ϕ momentum.
- The energy of signal B_s and invariant mass of $\bar{\nu}\nu$



Summary

- By 10^{12} Z decay, CEPC will produce $1.5 \times 10^{11} b\bar{b}$ and 1.8×10^5 rare decay $B_s \rightarrow \phi\nu\bar{\nu}$ under SM
- B_s Statistics : More than 5 higher order than the LEP (current up limit) and 2 higher order than Belle II
- Expected good accuracy to search the rare decay $B_s \rightarrow \phi\nu\bar{\nu}$.
Be the level of 1.5 % under SM
- More optimization and detector requirement.
 - PID: Necessary if one desires to separate π/K modes (0 – 45 GeV momentum range)
 - More full simulation samples to study rare decay and calorimeter
 - Missing mass performance?
- More measurement of flavor rare decay processes of B_s, B_c and Λ_b at CEPC are expected

End

Thanks