

# Probing the Dark Axion Portal with Muon Anomalous Magnetic Moment

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**2104.03276**

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# • Introduction

## The new result on muon anomalous magnetic moment at Fermilab:

B. Abi et al. (Muon g - 2 Collaboration) Phys. Rev. Lett. 126, 141801 (2021)

$$a_{\mu}^{\text{exp}}(\text{FNAL}) = 116592040(54) \times 10^{-11}$$

$$a_{\mu}^{\text{exp}}(\text{BNL}) = 116592080(63) \times 10^{-11}$$

G. W. Bennett et al. al. [Muon g-2] Phys. Rev. D 73 (2006), 072003

## Combined value:

$$a_{\mu}^{\text{exp}} = 116592061(41) \times 10^{-11}$$

# • Introduction

SM prediction for muon anomalous magnetic moment:

Large uncertainty

$$a_{\mu}^{\text{SM}} = a_{\mu}^{\text{QED}} + a_{\mu}^{\text{EW}} + a_{\mu}^{\text{HVP}} + a_{\mu}^{\text{HLbL}}$$

$116584718.931(104) \times 10^{-11}$   
 $153.6(1.0) \times 10^{-11}$   
 $6845(40) \times 10^{-11}$   
 $92(18) \times 10^{-11}$

$$a_{\mu}^{\text{SM}} = 116591810(43) \times 10^{-11}$$

T. Aoyama et al , Phys. Rept. 887, 1- 166 (2020)

# • Introduction

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**The difference between the experimental value and SM prediction:**

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251(59) \times 10^{-11}$$

**4.2 $\sigma$  discrepancy between experiment and SM prediction!**

**New Physics??**

lepton flavor violation;  $Z'$ ; neutral scalars; ALP; leptoquarks;  
supersymmetry; dark photon; dark matter portals

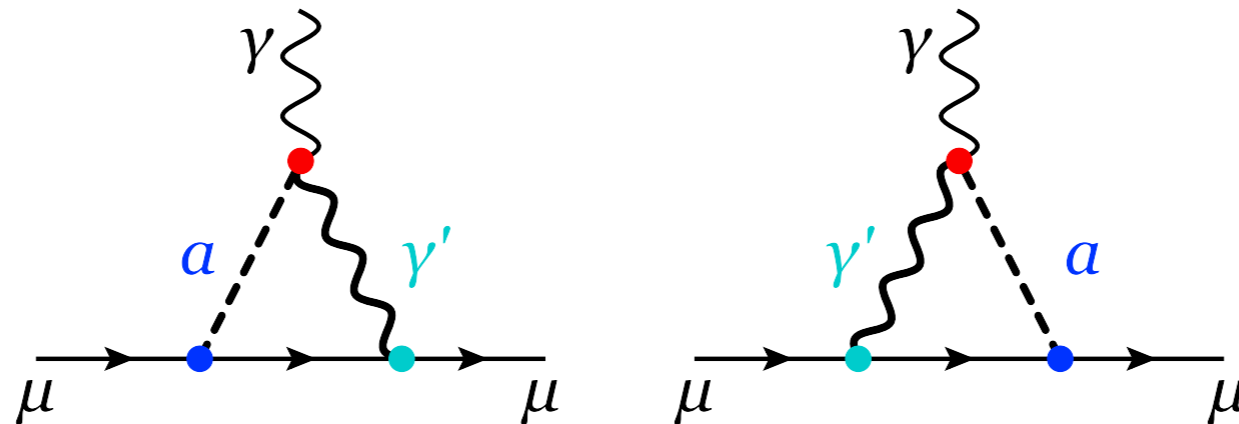
**+ more in old age**

- Dark axion portal to explain the  $\Delta a_\mu$

Consider TeV scale heavy NP:  $C_{a\gamma\gamma'} \sim \Lambda_{\text{NP}} \sim 1\text{TeV}^{-1}$

$$\mathcal{L} \ni \frac{1}{2} C_{a\gamma\gamma'} a F^{\mu\nu} \widetilde{X}_{\mu\nu} \longrightarrow \text{dark photon } \gamma'$$

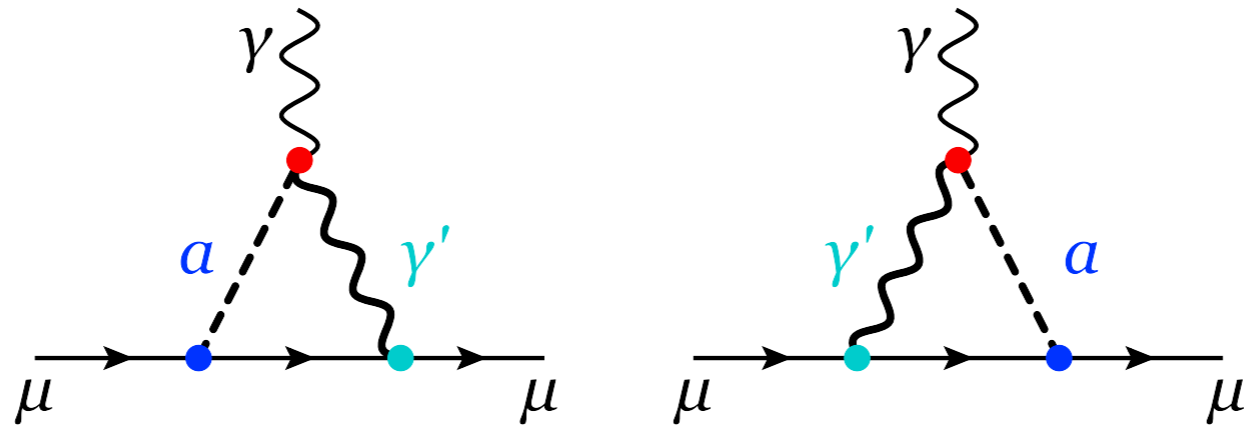
ALP: axion-like particle      **photon  $\gamma$**



$$\mathcal{L} \ni y_a^\mu a \bar{\mu} (i\gamma_5) \mu - \epsilon e \bar{\mu} \gamma^\nu \mu X_\nu$$

# • The Dark Axion Portal Contribution

$$\mathcal{L}_{\gamma\mu\mu} \equiv \Delta a_\mu \frac{e}{4m_\mu} \bar{\mu} \sigma_{\mu\nu} \mu F^{\mu\nu}$$

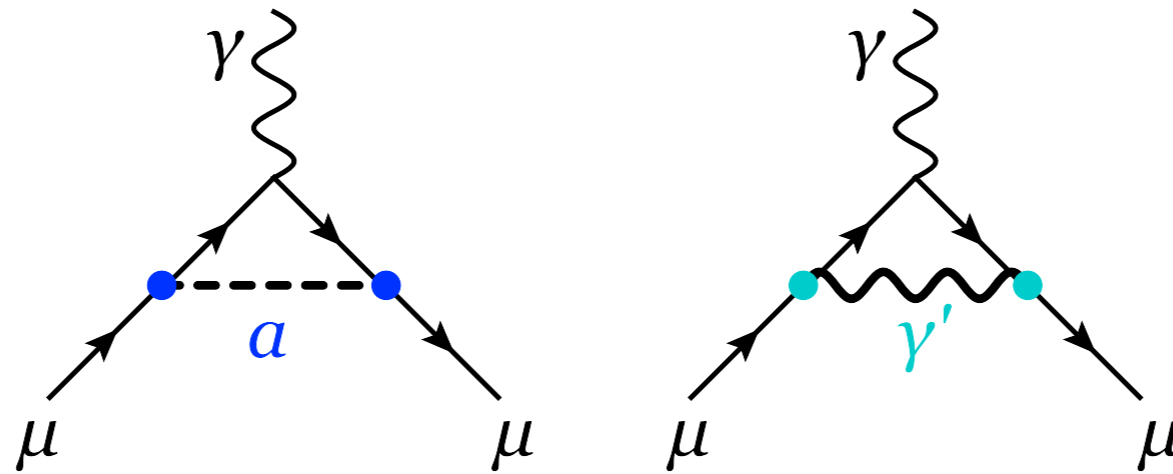


$$a_\mu = \frac{m_\mu}{4\pi^2} \epsilon y_a^\mu C_{a\gamma\gamma'} G \quad \longrightarrow \quad \text{linear in } m_\mu$$

$$G \equiv \int_0^1 dx \left[ (1-x) \left( \ln \frac{\Lambda^2}{(1-x)m_a^2 + x^2 m_\mu^2} - \frac{1}{2} \right) - \frac{(1-x)m_{\gamma'}^2 + 2x^2 m_\mu^2}{m_a^2 - m_{\gamma'}^2} \ln \frac{(1-x)m_a^2 + x^2 m_\mu^2}{(1-x)m_{\gamma'}^2 + x^2 m_\mu^2} \right]$$

cut-off scale to regularize UV divergence: same order as the UV scale  $\Lambda = 1 \text{ TeV}$

# • The Individual Contribution of $a$ or $\gamma'$



$$a_\mu^a = \frac{(y_p^\mu)^2}{4\pi^2} \frac{m_\mu^2}{m_a^2} F_a \left( \frac{m_\mu}{m_a} \right)$$

$$F_a(\eta) \equiv -\frac{1}{2} \int_0^1 dx \frac{x^3}{(1-x)(1-\eta^2 x) + \eta^2 x}$$

Always negative

$$a_\mu^{\gamma'} = \frac{e^2 e^2}{4\pi^2} \frac{m_\mu^2}{m_{\gamma'}^2} F_{\gamma'} \left( \frac{m_\mu}{m_{\gamma'}} \right)$$

$$F_{\gamma'}(\eta) \equiv \frac{1}{2} \int_0^1 dx \frac{2x^2(1-x)}{(1-x)(1-\eta^2 x) + \eta^2 x}$$

- No UV divergence.
- Each single contribution does not work!

# • Setup for searching for parameter space

$$\Delta a_\mu \equiv a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = 251(59) \times 10^{-11}$$

$$\chi^2 \equiv \left( \frac{\Delta a_\mu^{\text{cen.}} - \Delta a_\mu^{\text{NP}}}{\sigma(\Delta a_\mu)} \right)^2 < 5.99 \quad @ \quad 95\%$$

- **Central value:**  $\Delta a_\mu^{\text{cen.}}$
- **Uncertainty:**  $\sigma(\Delta a_\mu)$
- $C_{a\gamma\gamma'} = 3\text{TeV}^{-1}$  to satisfy the current bound from BaBar  $e^+e^- \rightarrow \gamma'a$

P. deNiverville, H. S. Lee and M. S. Seo Phys. Rev. D 98, no.11, 115011 (2018)



- Comparison

$$\frac{a_\mu}{a_\mu^a} \sim \frac{\epsilon}{y_a^\mu} \frac{m_a^2 C_{a\gamma\gamma'}}{m_\mu} \sim \frac{\epsilon}{10^{-3}} \frac{0.1}{y_a^\mu} \left( \frac{m_a}{100\text{GeV}} \right)^2$$

$$\frac{a_\mu}{a_\mu^{\gamma'}} \sim \frac{y_a^\mu}{\epsilon e^2} \frac{m_{\gamma'}^2 C_{a\gamma\gamma'}}{m_\mu} \sim 10^5 \frac{10^{-3}}{\epsilon} \frac{y_a^\mu}{0.1} \left( \frac{m_{\gamma'}}{100\text{GeV}} \right)^2$$

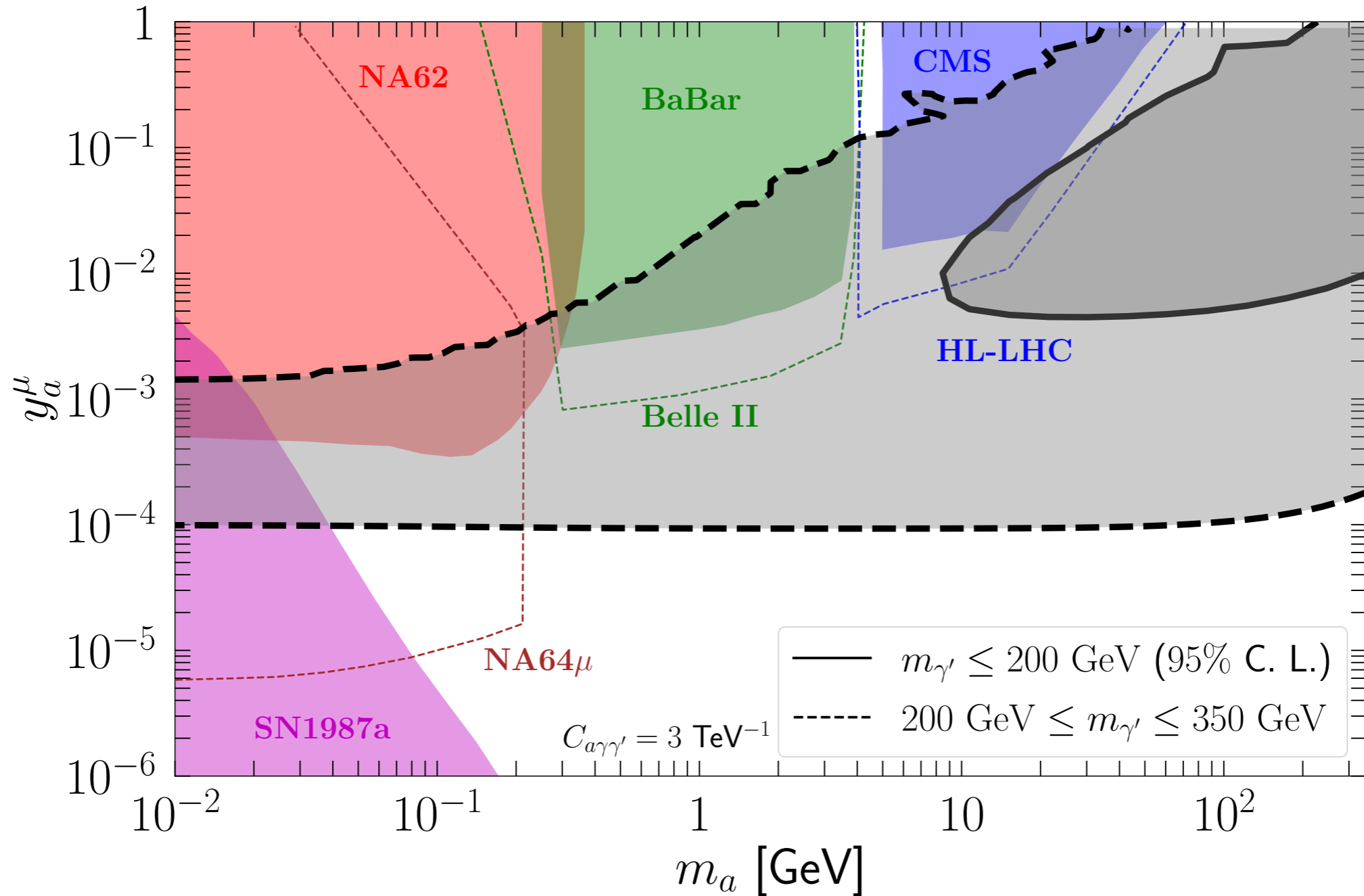


**If**  $a_\mu \gg a_\mu^a, a_\mu^{\gamma'} \Rightarrow m_a \gg \sqrt{y_a^\mu / \epsilon} 10\text{GeV}, m_{\gamma'} \gg \sqrt{\epsilon / y_a^\mu} \sqrt{10}\text{GeV}$



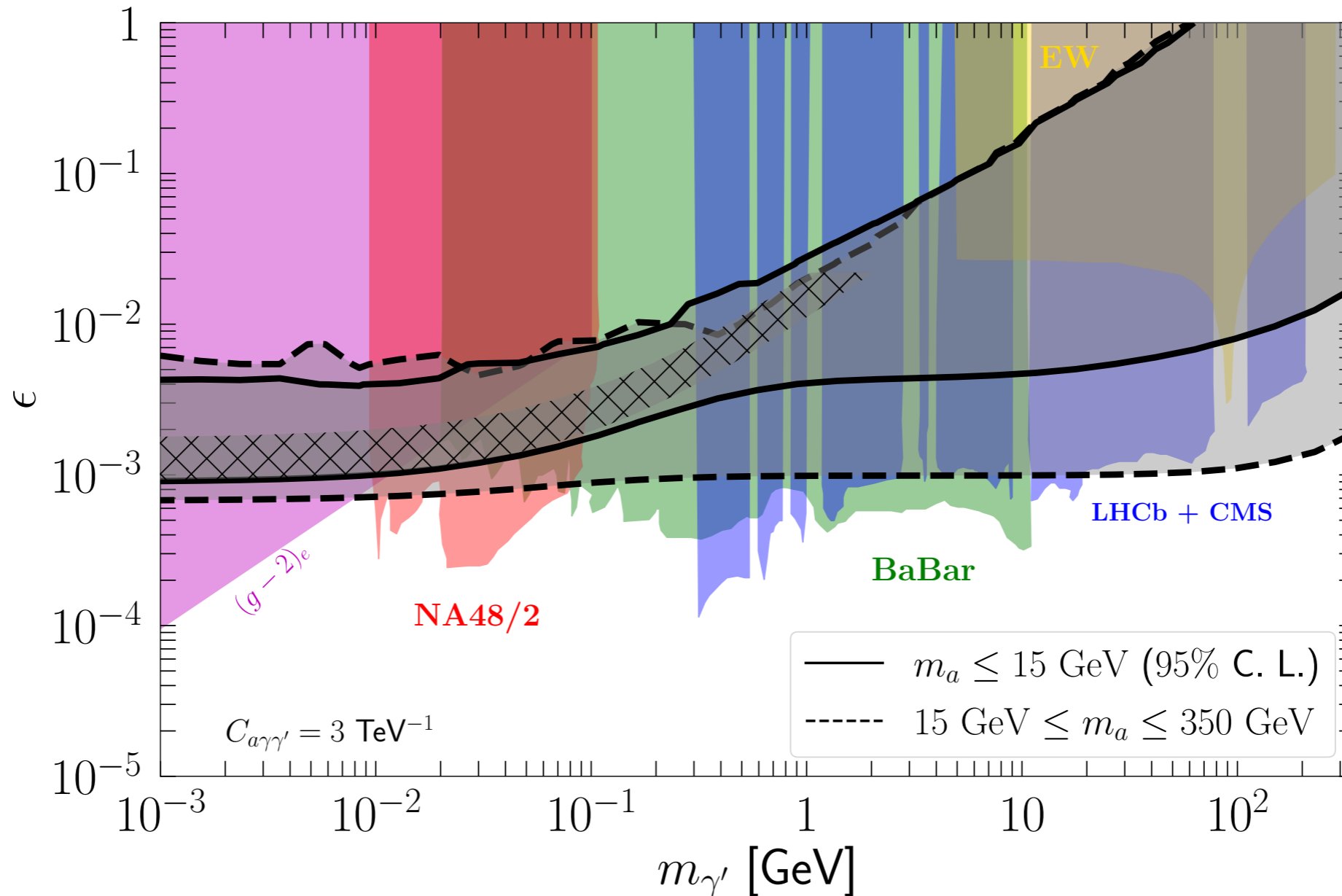
**For comparable couplings of  $\epsilon$  and  $y_a^\mu \Rightarrow$  **GeV** scale  $a$  and  $\gamma'$**

# Parameter space: $m_a - y_a^\mu$ plane



- **NA62:**  $K \rightarrow \mu\nu a$  [Croon, G. Elor, R. K. Leane and S. D. McDermott. JHEP 01, 107 \(2021\)](#)
- **SN1987a:**  $\nu + n(p) \rightarrow \mu^-(\mu^+) + p(n) \rightarrow \mu + \gamma \rightarrow a + \mu, \mu + X \rightarrow a + \mu + X$
- **BaBar:**  $e^+e^- \rightarrow \mu^+\mu^-a$  [B. Batell, N. Lange, D. McKeen, M. Pospelov and A. Ritz, Phys. Rev. D 95, no.7, 075003\(2017\)](#)
- **CMS:** rare  $Z$  decay [J. P. Lees et al. \[BaBar\], Phys. Lett. B 792 \(2019\), 345- 368](#)

# Parameter space: $m_{\gamma'} - \epsilon$ plane



- **Electron anomalous magnetic moment:  $(g - 2)_e$**  [0811.1030](#)
- **NA48: dark photon from pion decay** [1504.00607](#)
- **BaBar: resonant production of dark photon** [1406.2980](#)
- **LHCb+CMS: dark photon production from mesons + Higgs** [1603.08926](#), [1910.06926](#), [1912.04776](#)
- **Hashed: muon  $(g - 2)_\mu$  from single dark photon**

- **Dark photon to SM  $Z$**

$$\frac{1}{2} C_{a\gamma Z} a F_{\mu\nu} \tilde{Z}^{\mu\nu}$$

- $e\epsilon \rightarrow g_V = \frac{g}{c_W} \left( \frac{1}{4} - s_W^2 \right) \approx 4.5 \times 10^{-2} e;$

- **Two parameters  $m_Z$  and  $g_V$  are fixed;**

- $C_{a\gamma\gamma'} \rightarrow C_{a\gamma Z} \leq 0.03 \text{ TeV}^{-1}$  **from  $Z \rightarrow \gamma a$ ;**

K. Cheung, T. W. Kephart, W. Y. Keung and T. C. Yuan, Phys. Lett. B 662 (2008), 436-440

- **The contribution is negligibly small.**

## • Summary

- the Fermilab Muon  $g-2$  experiment enhances the  $\Delta a_\mu$  discrepancy with SM prediction from  $3.7 \sigma$  to  $4.2 \sigma$ ;
- The dark axion portal can surprisingly save the ALP and dark photon for explaining the muon anomalous magnetic moment;
- The observed muon anomalous magnetic moment provides a robust probe of the dark axion portal scenario.

*Thanks for your attention!*