



# *Insights into EHM Using Pion and Kaon Targets*



# Phenomenon of Emergent Mass

- Empirical status:
  - proton is stable compound object formed from three valence light-quarks
  - proton electric and magnetic charge radii  $r_{em} \approx 0.85$  fm ... see Daniele Binosi's presentation
  - evidently, proton never decays (if it did, wouldn't be many of us here)
- Mass of proton  $m_p = 939$  MeV.
- Mass of valence quarks in proton = 9 MeV
  - **Missing mass = 930 MeV = 99%**
- Higgs mechanism of mass generation responsible for only 1% of proton mass
- **Where should science look to find the remaining 99% of visible mass in the Universe?**
- **Is the answer contained within the SM?**
- **How will science know when the answer is found?**

**What are the “smoking gun” signals?**

# Emergence of Hadron Mass

## ➤ Proton mass budget

Only 9 MeV/939 MeV is directly from Higgs

## ➤ Plainly, there is another phenomenon in Nature that is extremely effective in producing mass:

### Emergent Hadron Mass (EHM)

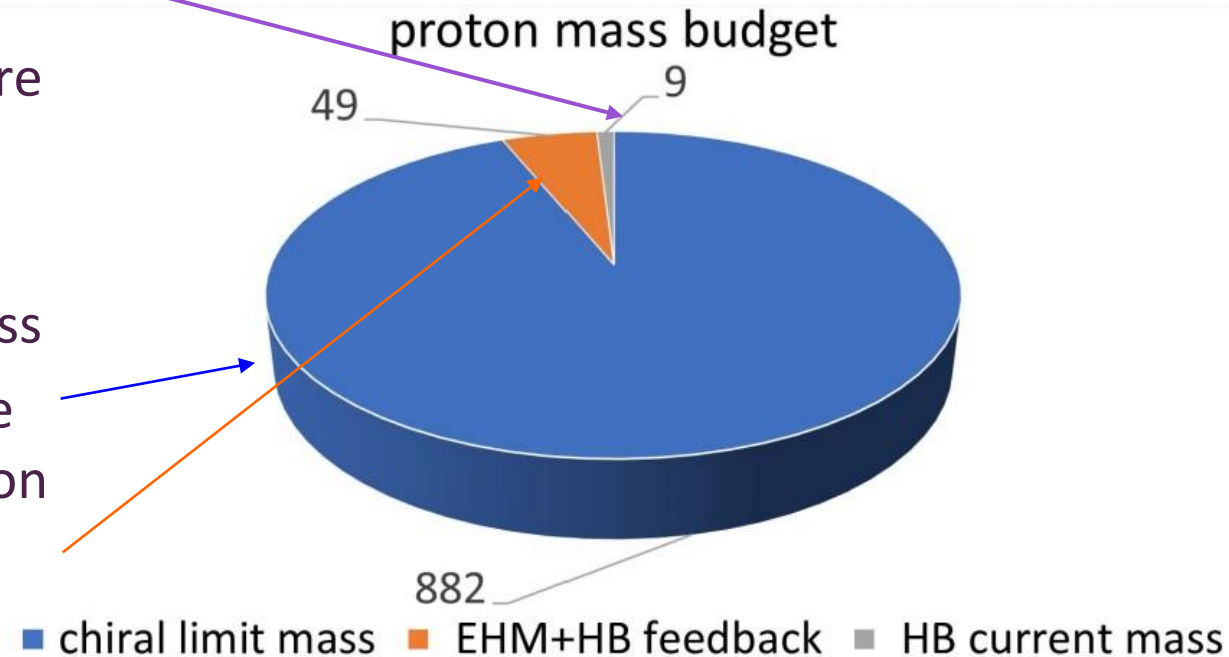
- ✓ Alone, it produces 94% of the proton's mass
- ✓ Remaining 5% is generated by constructive interference between EHM and Higgs-boson

### ✓ What is EHM?

### ✓ Does it have a reductionist explanation,

*i.e.* can it be explained by mere mechanisms, like a Swiss watch?

### ✓ If so, what are they?





# Emergent Hadron Mass (EHM)

- In quantum field theory, mass and  $\text{length}^{-1}$  are effectively the same thing
- Thus, asking for the origin of 99% of visible mass in the Universe is possibly/probably the same as asking what is the source of the proton's size
- *Confinement scale!*
- Confinement is far more than the statement that Nature contains only colour-singlet combinations of gluons and quarks
  - Those combinations have fm-scale sizes
  - This is crucial
  - It wouldn't be confinement if the scales were Å size
- *Confinement ...*
  - If one can't measure them, what are the gluons and quarks in the QCD Lagrangian?
  - Are they anything more than a theoretical artifice; useful things for calculations in perturbation theory, but practically irrelevant when resolving detectable hadrons?
  - What degrees-of-freedom should be used to compute and understand hadron properties?



# Phenomenon of Emergent Mass

## ➤ SM paradigm

- proton is described by QCD ... 3 valence quarks
- pion is also described by QCD ... 1 valence quark and 1 valence antiquark
- $\rho$ -meson is also described by QCD ... 1 valence quark and 1 valence antiquark

- Here  $m_p \approx 1.5 \times m_\rho$  ✓

- expect  $m_p \approx 1.5 \times m_\pi$  ... but, instead  $m_p \approx 7 \times m_\pi$  ✗

## ➤ *Why is $\approx 1$ GeV proton mass paired with $\approx 1/7$ GeV pion mass in the same theory of Nature?*

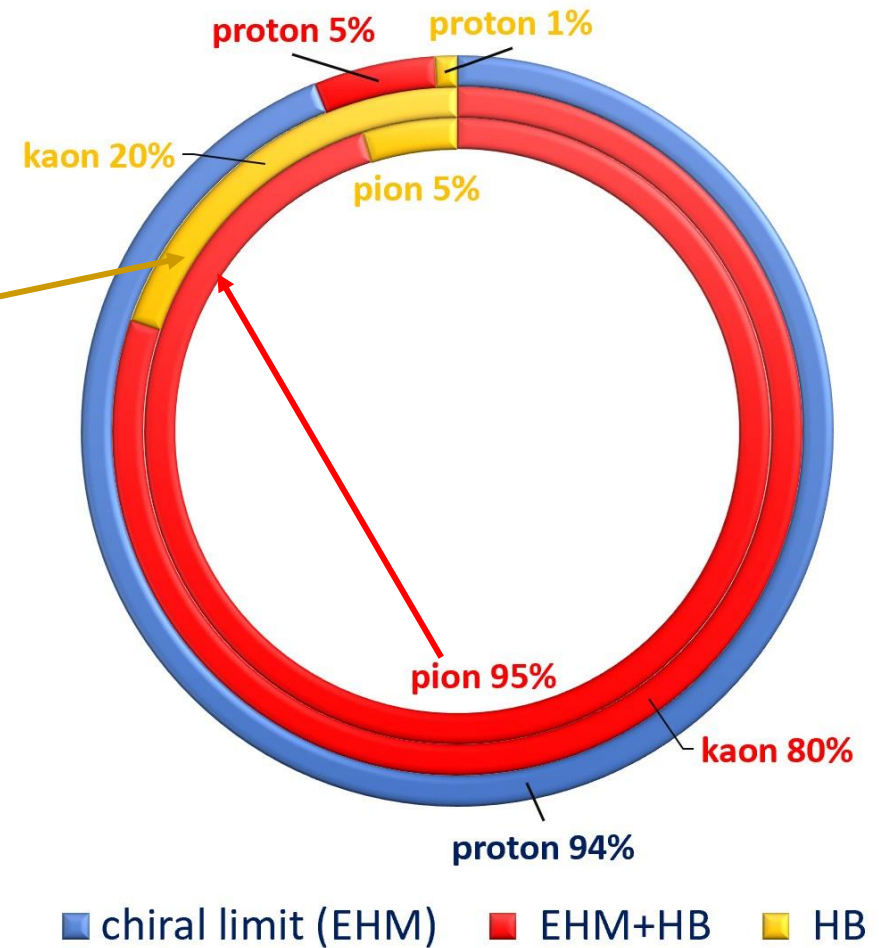
- How is this achieved?
- Does Nature fine tune?
- Is there something peculiar about the pion (and by logical extension, the kaon)?

## ➤ *Are the answers in QCD?*

# Emergence of Hadron Mass - Contrasts

- Compare proton and pion mass budgets
- Pion is a Nambu-Goldstone boson
  - So, massless in chiral-limit
  - No blue annulus
  - EHM+HB is 95% of the total
- Kaon is somewhere in between
  - HB = 20%
  - EHM+HB = 80%
- Critically, without Higgs mechanism of mass generation,  $\pi$  and K would be indistinguishable from each other
- Always distinguishable from proton.
- Yet, all states are supposed to be in QCD!
- **What is, wherefrom, whereto mass?**

## Mass Budgets



# Emergence of Hadron Mass - Basic Questions - How to Answer Them?

- $\pi$  &  $K$  are
  - Nature's most fundamental Nambu-Goldstone (NG) bosons
  - mesons ... In many respects = simplest bound-state problems in quantum field theory because only two valence bodies  $\Rightarrow$  modern QCD theory can be rigorous
- A (very) few things are empirically known about  $\pi$
- But (almost) nothing is known about  $K$  – even  $K$  radius is no better than an educated guess
- NG modes predicted 80 years ago
  - Yet, today, their structure is still a mystery
  - $\pi$  is crucial to nuclear binding; yet “no one” has charted its features
  - $K$  is completely unknown. Possibly plays a role in compact astrophysical objects; but “no one” can be certain
- Progress toward understanding needs synergy between experiment + phenomenology + theory

# EHM & QCD

$$L = \frac{1}{4} G_{\mu\nu}^a(x) G_{\mu\nu}^a(x) + \bar{\psi} \left[ \gamma \cdot \partial_x + m + ig \frac{\lambda^a}{2} \gamma \cdot A^a(x) \right] \psi(x)$$
$$G_{\mu\nu}^a(x) = \partial_\mu A_\nu^a(x) - \partial_\nu A_\mu^a(x) - f^{abc} A_\mu^b(x) A_\nu^c(x)$$

- Can a one-line Lagrangian produce almost all visible mass in the Universe ...
- If so ...

A large, 3D, red, glossy text graphic that reads "HOW?". The letters are thick and have a slight shadow underneath, giving it a three-dimensional appearance. The text is slanted slightly to the right.



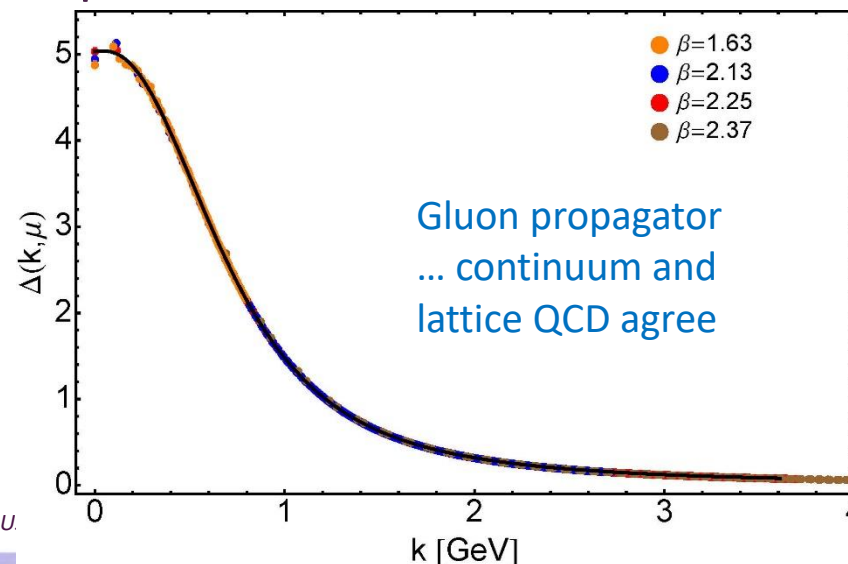
# Pure gauge QCD

- QCD doesn't need quarks to be an interacting quantum field theory
  - Gluon self-interactions at tree-level, i.e., in the Lagrangian
- Gluons are massless in perturbation theory
- **Not preserved non-perturbatively!**

*No symmetry in Nature protects four-transverse gluon modes ...*

$$q_\mu \Pi_{\mu\nu}(q) \equiv 0$$

- Gluons acquire a running mass, which is large at infrared momenta  
⇒ Prediction: Gluon two-point function is nonzero and finite at  $q^2 = 0$



*Truly mass from nothing  
An interacting theory, written in terms of massless gluon fields, produces dressed gluon fields that are characterised by a mass function that is large at infrared momenta*

*Dynamical mass generation in continuum quantum chromodynamics*  
J.M. Cornwall, Phys. Rev. D **26** (1981)  
1453 ... ~ 1000 citations

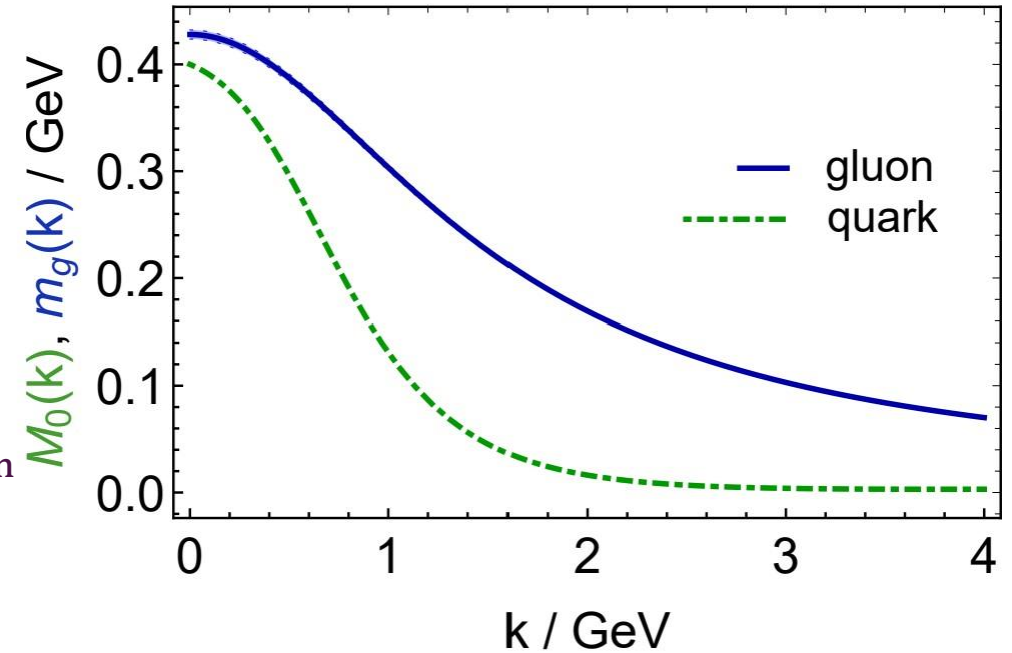
*The Gluon Mass Generation Mechanism: A Concise Primer*  
A.C. Aguilar, D. Binosi, J. Papavassiliou, Front. Phys. **11** (2016) 111203

# Prediction: Gluon Mass Function

- Gluon mass function characterised by renormalisation group invariant IR mass

$$\hat{m}_0 = 0.43(1) \text{ GeV} \approx \frac{1}{2} m_{\text{proton}}$$

- The value is a prediction in the sense that it is  $\frac{1}{2} m_{\text{proton}}$
- But the value of  $m_{\text{proton}}$  is taken from experiment
- As written, the SM doesn't "know" any of its mass scales.
- Nature does.
- Once these scales are given, how much predictive power does the SM deliver?
- SM Theory reveals that a gluon mass scale is possible. It can then reveal all its consequences
- Experiment can verify those predictions
- Then the mechanism of EHM is exposed

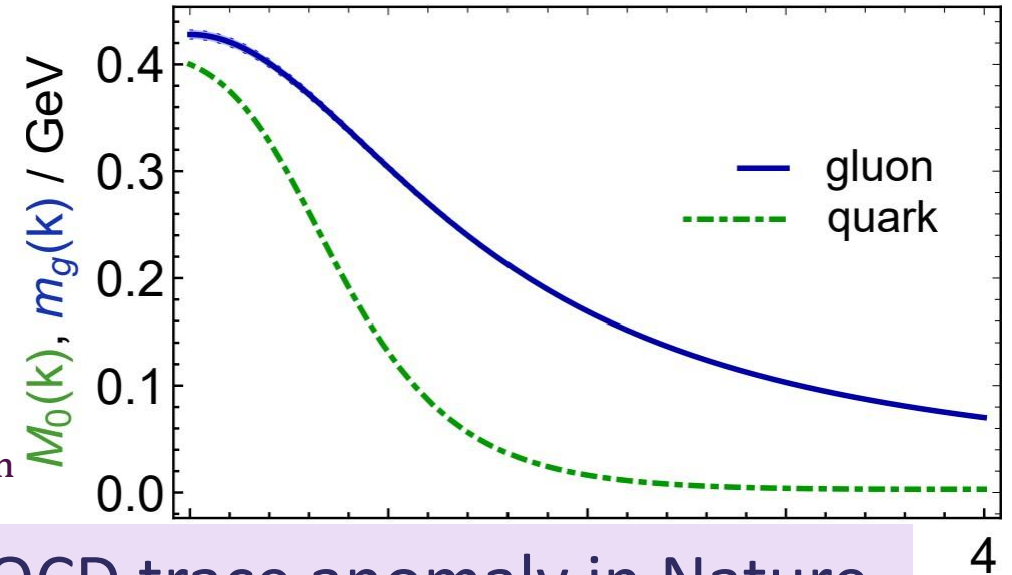


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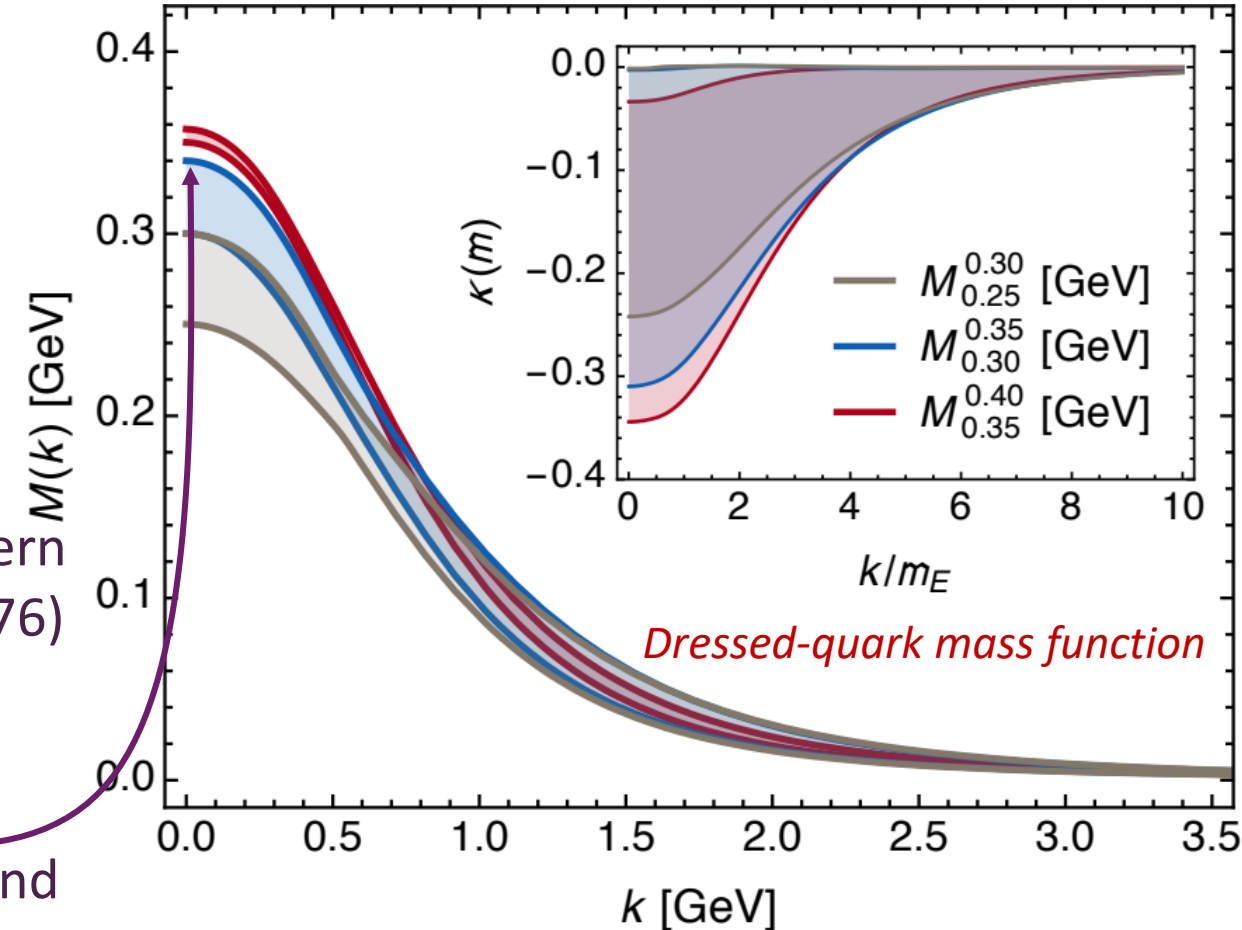


- B ✓ Most fundamental expression of the QCD trace anomaly in Nature
- A
  - Massless gauge bosons become massive
  - And that mass is of nuclear size.
- N

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# Prediction: Mass is generated for matter

- $\widehat{\alpha}_0(s=0) = 0.97(4) \pi$
- Sufficient to drive constructive feedback in dressed-quark gap (Dyson) equation so that quark quasiparticles emerge
- Characterised by a running mass  $M(k)$ 
  - Vanishes in ultraviolet, following the pattern predicted by Lane (1974) and Politzer (1976)
  - Large at infrared momenta,  
*i.e.*  $M(0) \approx \frac{1}{3}m_p$
  - Just like constituent quark of Gell-Mann and Zweig
- Dressed-quark is a bare parton at ultraviolet momenta
  - But that parton carries a cloud of sea and glue with it in the infrared

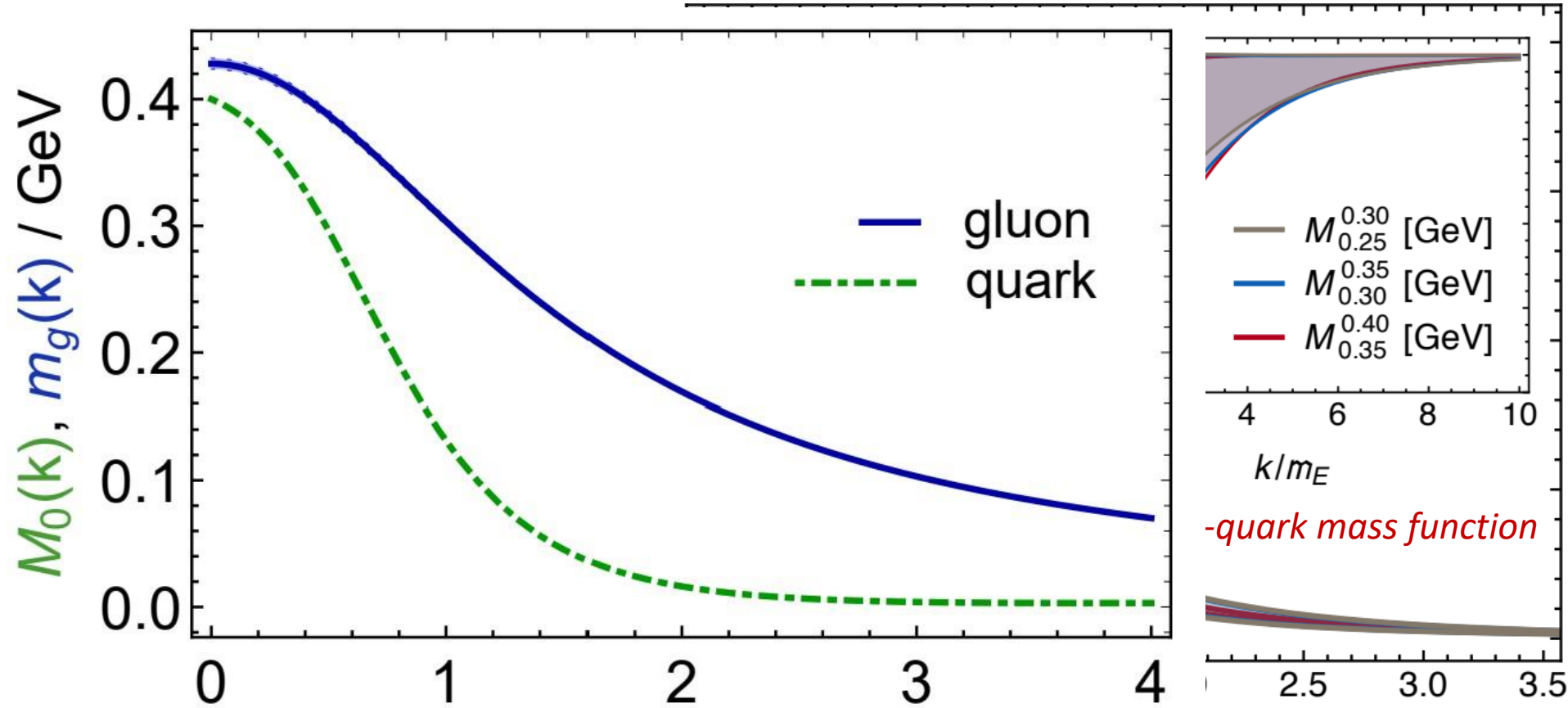


Natural constraints on the gluon-quark vertex, Daniele Binosi, Lei Chang, Joannis Papavassiliou, Si-Xue Qin and Craig D. Roberts, [arXiv:1609.02568 \[nucl-th\]](https://arxiv.org/abs/1609.02568), Phys. Rev. D **95** (2017) 031501(R)/1-7



# Prediction: Mass is generated for matter

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- Dressed-quark
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Emergence of mass, with hadron-like scale, in one-body subspace of QCD's gauge and matter sectors

# Prediction

## Pion (Nambu-Goldstone modes) and mass

- Higgs boson couplings  $\rightarrow 0$
- Pion exists and is massless
- Pion Bethe-Salpeter amplitude

*EHM demands equivalence between one-body mass and two-body correlation strength in Nature's most fundamental Nambu-Goldstone bosons*

$$f_{\pi} E_{\pi}(p^2) = B(p^2)$$

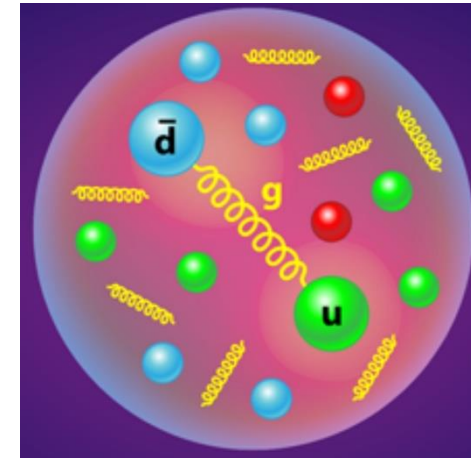
Pion wave function

quark mass function

- **Enigmatically, properties of the nearly massless pion are the cleanest expression of EHM in the Standard Model !**

# Nambu-Goldstone Bosons

- Pions and kaons were discovered 80 years ago
- They're unstable, via weak decays; difficult to use as targets
- Besides masses, lifetimes, (almost) NOTHING has been learnt about their structure
  - Without pions and kaons, there could be no nuclei
  - If they were heavier than they are, there would be no nuclei and no us
  - If they were lighter than they are, there would be no nuclei and no us
- Nambu-Goldstone bosons are somehow different from “ordinary” hadrons.
  - How?
    - Size?
    - Mass distribution?
    - Gluon Distribution?
    - Pressure Distribution?
- Dawn of new era is visible ... modern facilities with capability of probing into the heart of Nambu-Goldstone bosons



# What visible “scars” do these symmetry-demanded cancellations leave on the body of pion observables?

## Nambu-Goldstone Bosons

### ➤ SM Theory

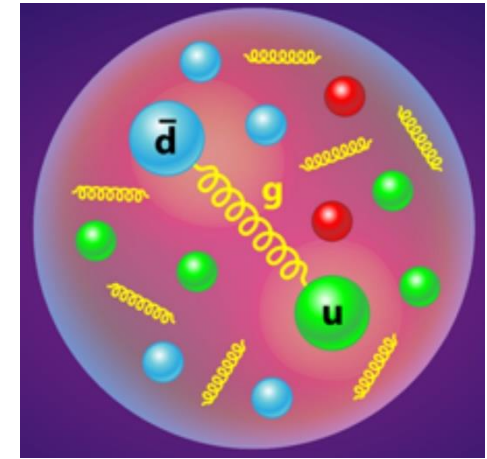
- Pions and kaons: bound states of valence-quark & valence-antiquark
  - In being bound states, they are just like all other hadrons
- Cannot be emphasized too strongly ...
  - In the continuum and on the lattice, pions and kaons emerge as poles in the quark+antiquark scattering matrix.
  - Just like the proton appears as a pole in the quark+quark+quark scattering matrix
- Difference between proton and pion is that in the chiral limit, owing to dynamical chiral symmetry breaking, a basic corollary of EHM:

In pion: 2 × one-body-mass + 1 × two-body binding energy ≡ 0

Away from chiral limit, a small part of the 2 × one-body contributions is not cancelled.

Cancellations happen in proton, but no dynamics and symmetry forces them to be exact

$$M_Q + M_{\bar{Q}} + U_{Q\bar{Q}} \equiv 0$$

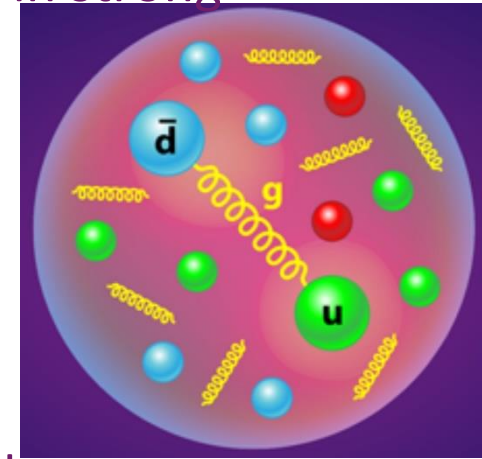




# What visible “scars” do these symmetry-demanded cancellations leave on the body of pion observables?

## Nambu-Goldstone Bosons

- SM Theory
  - Pions and kaons: bound states of valence-quark & valence-antiquark
    - In being bound states, they are just like all other hadrons
- Formulated correctly, the  $\pi$  and K define the simplest bound-state problems in strong interactions
  - Rigorous continuum predictions are available
    - More are being developed
  - Lattice-regularised QCD is beginning to deliver
- Precision tests of strong QCD and EHM are becoming possible
  - No room for parameters to be varied so theorists can hide from null results
- *Chapters will be closed in textbooks that will be written*



# Get off the ground!



## ➤ *Basic message*

- The ground state proton is not enough
- Ground state of the hydrogen atom did not give us QED
- Studies of the proton alone cannot reveal all the wonders of QCD, if QCD is truly the theory of strong interactions in the Standard Model
- Modern and planned high-luminosity facilities provide unprecedented opportunities to move beyond the 100-year focus on the structure of just one (or two = neutron) hadron(s)
- How much richer will be our store of knowledge once insights into the full array of Nature's hadrons is in our hands
- Numerous presentations during these next few days will demonstrate the truth of these statements





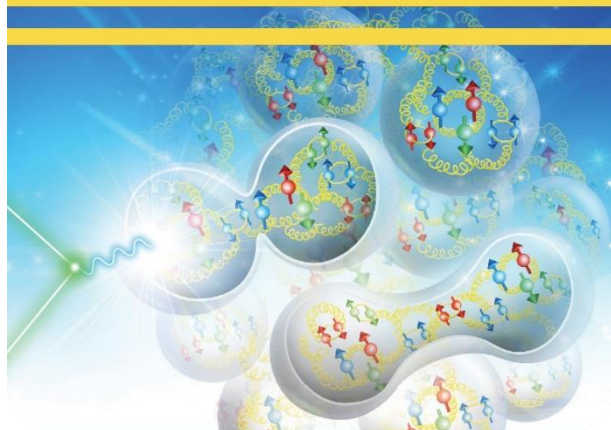
## AMBER

A new QCD facility at the  
M2 beam line of the  
CERN SPS



## ELECTRON-ION COLLIDER

EIC Yellow Report



# Potential of Existing and Future Facilities

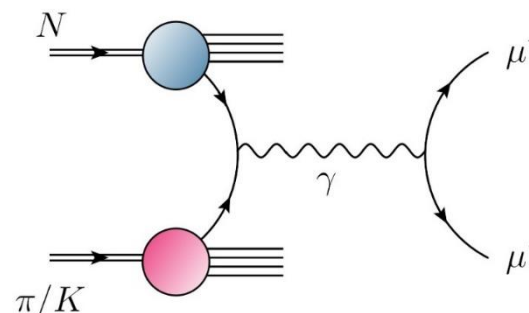
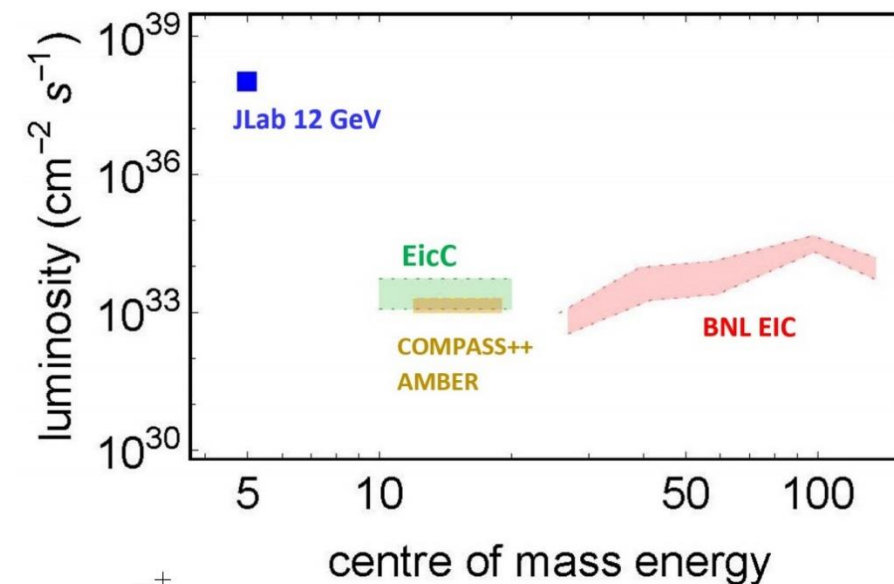
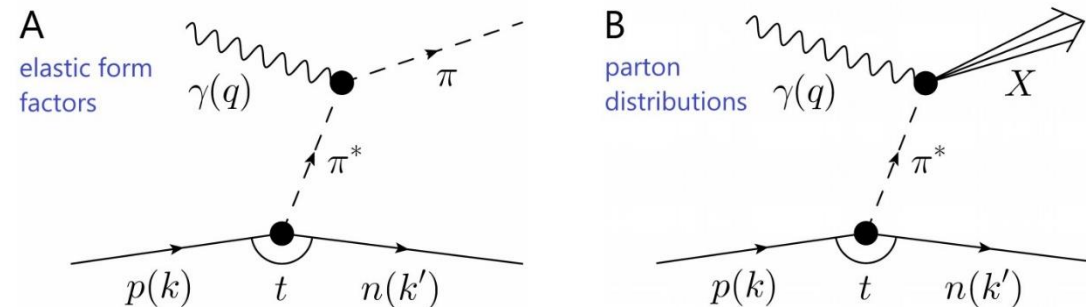
# Era of Meson Targets

## ➤ JLab & EIC & EicC

- High luminosity electron ( + ion) beams
- Access to meson targets via the Sullivan Process, i.e., a baryon's “meson cloud”

## ➤ AMBER @ CERN SPS

- High-intensity beams of pions  
( $\gtrsim 10^7$  pions/sec in Phase-1 = approved)  
and kaons ( $5 \times 10^6$  kaons/sec Phase-2 = proposal  
being prepared)
- Drell-Yan,  $J/\psi$  production, prompt photon production  
... from proton and nuclear targets

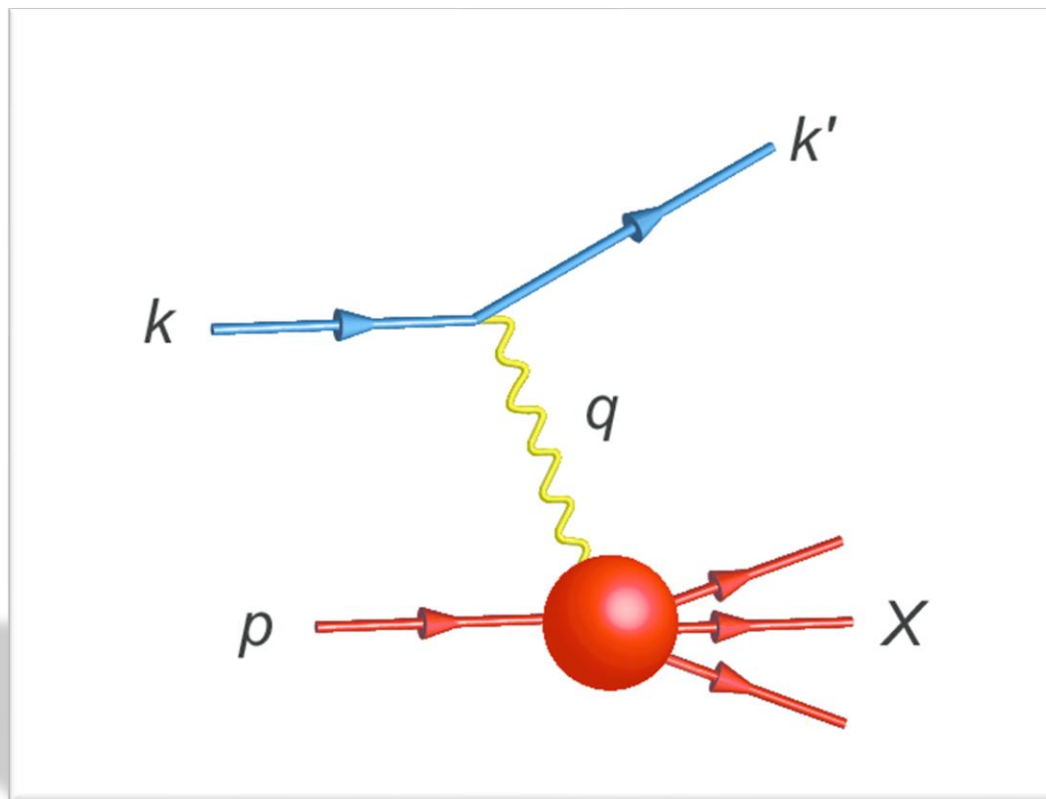




# Plans and Goals

- ✓ Letter of Intent: [A New QCD facility at the M2 beam line of the CERN SPS](#). This document covers all ideas for future experiments as of January 2019.
- ✓ Proposal for Phase-1: [COMPASS++/AMBER: Proposal for Measurements at the M2 beam line of the CERN SPS Phase-1: 2022-2024](#). This document covers the three phase-1 experiments (start in 2022).
- ✓ *Pion and Kaon Structure at the Electron-Ion Collider*, Arlene C. Aguilar *et al.*, NJU-INP 001/19, [arXiv:1907.08218](#) [nucl-ex], Eur. Phys. J. A **55** (2019) 190/1-15
- ✓ *Strong QCD from Hadron Structure Experiments*, S. J. Brodsky *et al.*, [arXiv:2006.06802 \[hep-ph\]](#), [Int. J. Mod. Phys. E 29 \(2020\) 08, 2030006/1-122](#)
- ✓ *Selected Science Opportunities for the EicC*, Xurong Chen, Feng-Kun Guo, Craig D. Roberts and Rong Wang, NJU-INP 022/20, [arXiv:2008.00102 \[hep-ph\]](#), Few Body Syst. **61** (2020) 4, 43/1-37. Invited contribution to the Special Issue: "New Trends in Hadron Physics: a Few-Body Perspective"
- ✓ *Insights into the Emergence of Mass from Studies of Pion and Kaon Structure*, Craig D. Roberts, David G. Richards, Tanja Horn and Lei Chang, NJU-INP 034/21, [arXiv: 2102.01765 \[hep-ph\]](#), Prog. Part. Nucl. Phys. (2021) *in press*
- ✓ *Electron-Ion Collider in China*, D. P. Anderle *et al.*, NJU-INP 035/21, [arXiv:2102.09222 \[nucl-ex\]](#), Front. Phys. (China) *in press*
- ✓ *Revealing the structure of light pseudoscalar mesons at the Electron-Ion Collider*, John Arrington *et al.*, NJU-INP 036/21, [arXiv: 2102.11788 \[nucl-ex\]](#), J. Phys. G (*in press*)





# *Parton Distribution Functions*

# NG Boson Distribution Functions

*Insights into the Emergence of Mass from Studies of Pion and Kaon Structure*, Craig D. Roberts, David G. Richards, Tanja Horn and Lei Chang, NJU-INP 034/21, [arXiv: 2102.01765](https://arxiv.org/abs/2102.01765) [[hep-ph](#)], Prog. Part. Nucl. Phys. (2021) *in press*

## ➤ Physics Goals:

- Precise data that can be used to determine Pion and Kaon Distribution Functions – valence, sea and glue
- Provide the first complete charts of the internal structure of Nature's most fundamental Nambu-Goldstone bosons.

## ➤ Today:

- Existing pion data are more than 40-years-old
- That data only covers the valence-quark domain
- A forty-year controversy, with doubts persisting over whether the data agree with QCD predictions or challenge the verity of QCD
- Regarding the kaon, worldwide, only 10 points of data exist



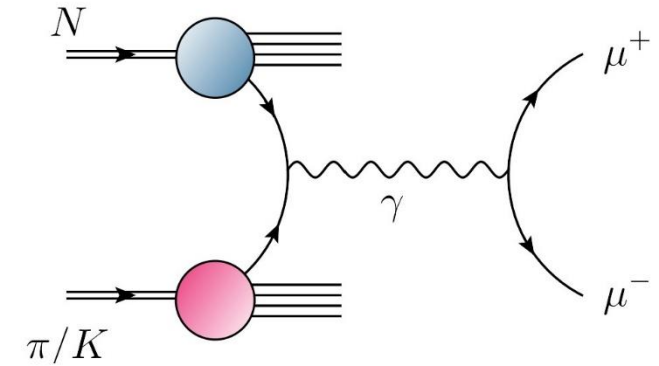
# NG Boson Distribution Functions

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## ➤ Future:

- JLab, EIC, EicC
  - ⇒ pion and kaon elastic electromagnetic form factors ... reveal and quantify scaling violations in hard exclusive processes ... hard prediction of QCD, never seen
  - ⇒ pion and kaon valence quark distribution functions at large  $x_B$
- AMBER
  - precision data to chart of  $\pi$  and  $K$  structure: DFs of valence, sea and glue.
  - Glue is particularly important ... because controversial, yet prominent theory predicts that pions contain (almost) zero glue.





# Controversy over pion valence DF

- QCD-improvement of parton model leads to the following statement:  
At any  $\zeta > \zeta_H$  for which experiment can be interpreted through parton distributions, then
$$x \simeq 1 \Rightarrow q^\pi(x; \zeta) \propto (1 - x)^{\beta=2+\gamma}, \gamma > 0$$
- Consequence
  - Any analysis of DY, DIS, etc. experiment which returns  $\beta < 2$  conflicts with QCD.
- Observations
  - All existing internally-consistent calculations preserve connection between large- $k^2$  behaviour of interaction and large- $x$  behaviour of DF:  $J=0 \dots (1/k^2)^n \Leftrightarrow (1-x)^{2n}$
- No existing calculation with  $n=1$  produces anything other than  $(1-x)^2$
- Internally-consistent calculation that preserve RG properties of QCD,  
then  $2 \rightarrow 2+\gamma, \gamma>0$ , at any factorisation-valid scale
- Controversy:
  - **Ignore** threshold resummation – typical of all contemporary phenomenology, despite Aicher *et al.*, then data analysis yields  $(1-x)^{1+\gamma}$
  - **Include** threshold resummation, then data analysis yields  $(1-x)^{2+\gamma}$

Craig Roberts. [cdroberts@nju.edu.cn](mailto:cdroberts@nju.edu.cn) "Insights into EHM Using Pion and Kaon Targets"



# $\pi$ valence-quark distributions

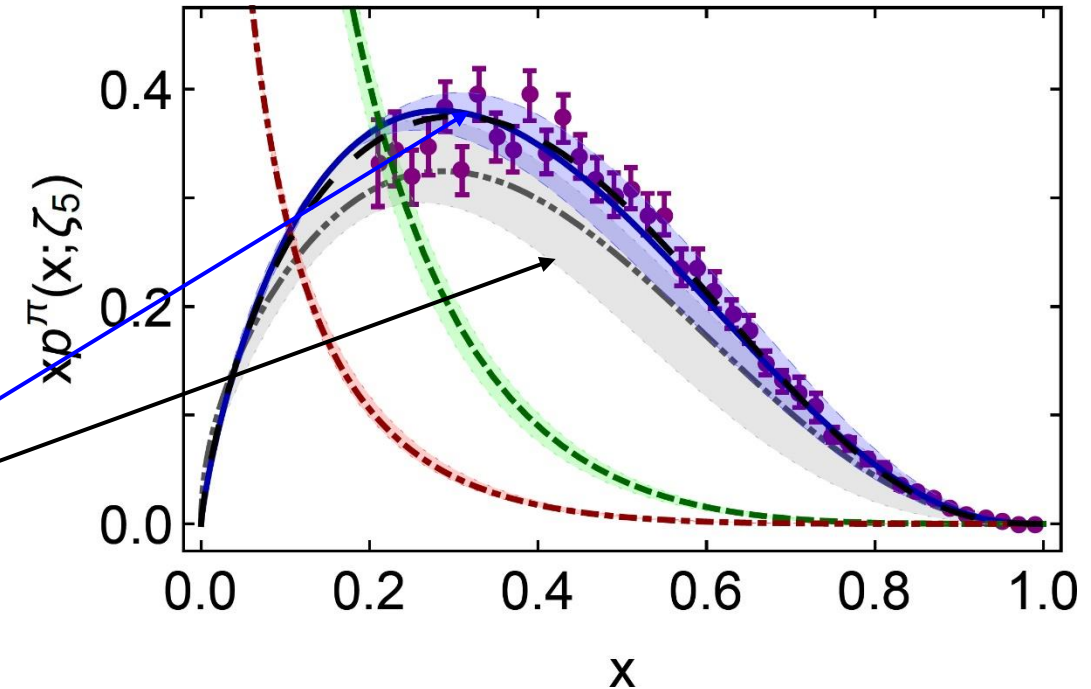
## 20 Years of Evolution $\rightarrow$ 2019

- Novel lattice-QCD algorithms beginning to yield results for pointwise behaviour of  $u^\pi(x; \zeta)$
- Developments in continuum-QCD have enabled 1<sup>st</sup> parameter-free predictions of **valence**, **glue** and **sea** distributions within the pion
  - Reveal that  $u^\pi(x; \zeta)$  is hardened by EHM
- Agreement between new **continuum** prediction for  $u^\pi(x; \zeta)$  [Ding:2019lwe] and recent lattice-QCD result [Sufian:2019bol]
- Real strides being made toward understanding pion structure.
- Standard Model prediction: stronger than ever before
- *After 30 years – new era dawning in which the ultimate experimental checks can be made:*

*JLab12 ... M2 beam-line @ CERN ... EIC ... EicC(?)*

$$\beta^{\text{contm}}(\zeta_5) = 2.66(12)$$

$$\beta^{\text{lattice}}(\zeta_5) = 2.45(58)$$



# $\pi$ distribution functions ... Comparison with JAM fits

## ➤ Valence:

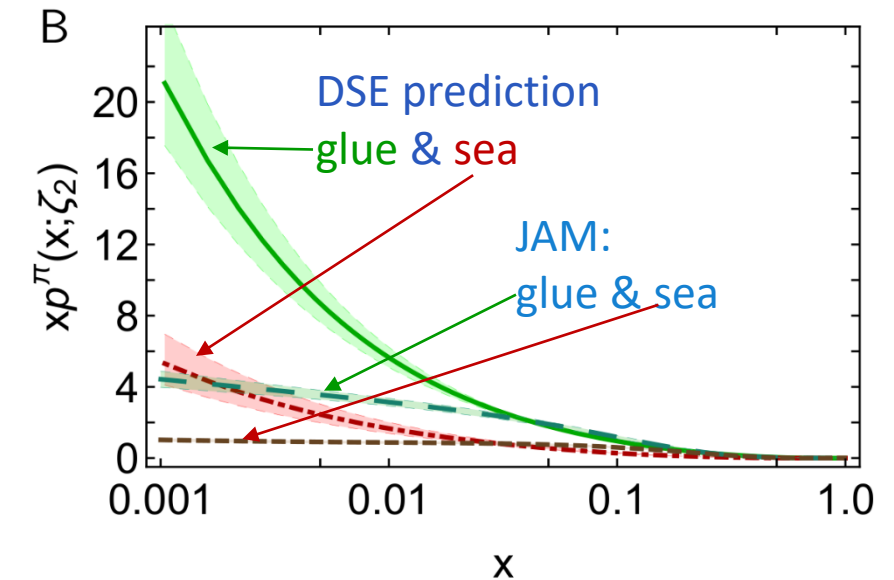
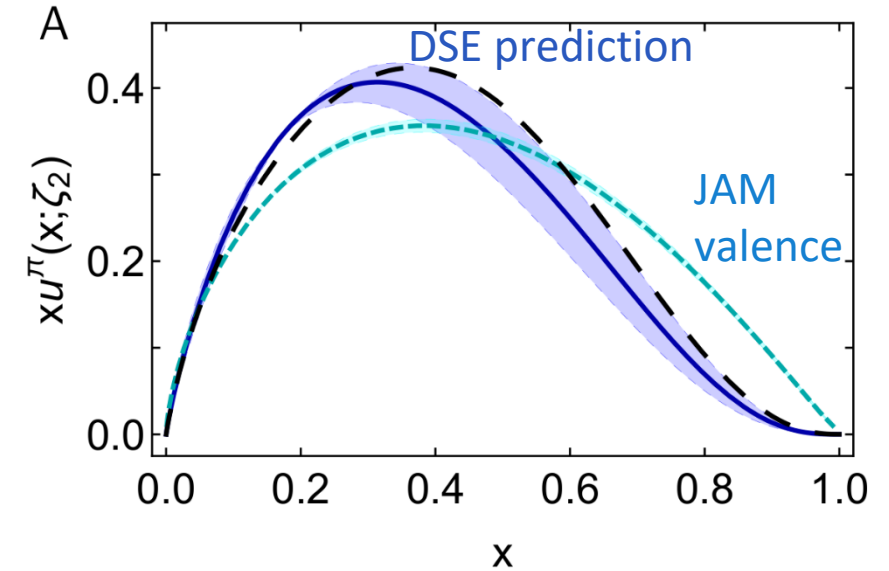
- momentum fraction similar
- JAM ... publication ignores NLL resummation ... profile much harder & inconsistent with QCD prediction

## ➤ Glue:

- Similarities on  $x \geq 0.05$ , but marked disagreement on important complementary domain
- Both continuum prediction and JAM fit are very different from early phenomenology
- Should be tested in new experiments that are directly sensitive to the pion's gluon content.
- Perhaps, prompt photon &  $J/\Psi$  production

## ➤ Sea:

- Prediction and fit disagree on entire  $x$ -domain
- If pion's gluon content is considered uncertain, then fair to describe sea-quark distribution as empirically unknown
- Motivation for the collection and analysis of DY data with  $\pi^\pm$  beams on isoscalar targets



# $\pi$ distribution functions ... Comparison with JAM fits

## ➤ Valence:

- momentum fraction similar
- JAM ... publication ignores NLL resummation ... profile much

Breaking news ...

1<sup>st</sup> exploratory LQCD results for pion's gluon DF have been released

important complementary domain

### Gluon Parton Distribution of the Pion from Lattice QCD

Zhouyou Fan (Michigan State U.), Huey-Wen Lin (Michigan State U.)

Apr 13, 2021

10 pages

e-Print: [2104.06372](#) [hep-lat]

Report number: MSUHEP-21-004

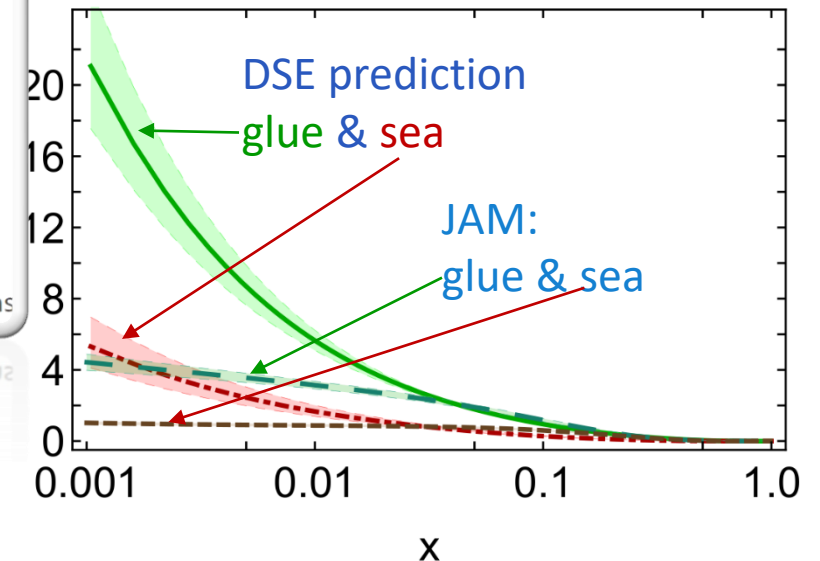
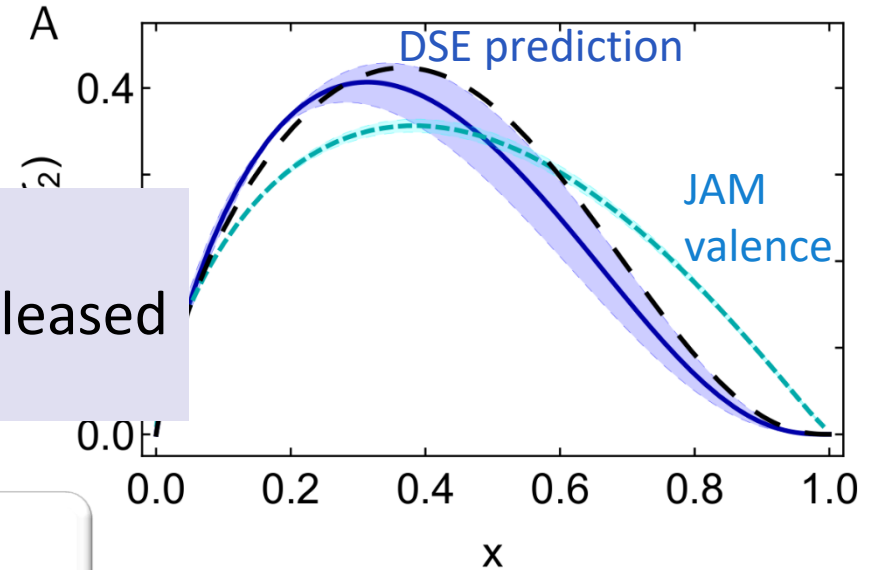
View in: [ADS Abstract Service](#)

[pdf](#) [cite](#)

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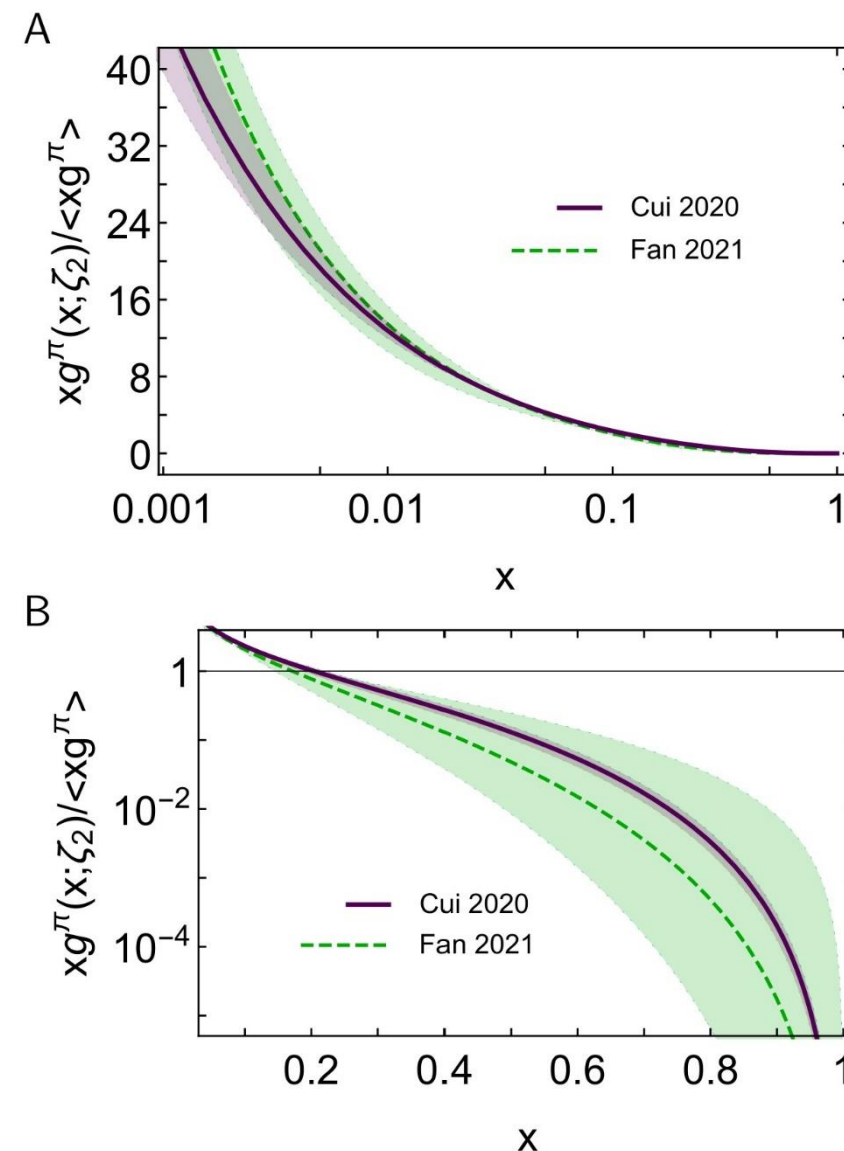


Craig Roberts. [cdroberts@nju.edu.cn](mailto:cdroberts@nju.edu.cn) "Insights into EHM Using Pion and Kaon Targets"

# Breaking news for glue in $\pi$ : Continuum ([Eur. Phys. J. C 80 \(2020\) 1064/1-20](#)) & Lattice Predictions ([arXiv:2104.06372](#))

## Two distinct approaches to solving QCD Agreeing quantitatively on $g^\pi(x)$

- JAM and xFitter phenomenological analyses (both ignore NLL corrections to hard scattering kernel)  
exhibit qualitatively different behaviour and are disfavoured by this comparison
- Highlights need for new data and improved phenomenology in order to turn that data into a real test of QCD and our understanding of Nambu-Goldstone modes.
- AMBER is uniquely placed to provide the necessary precision data.



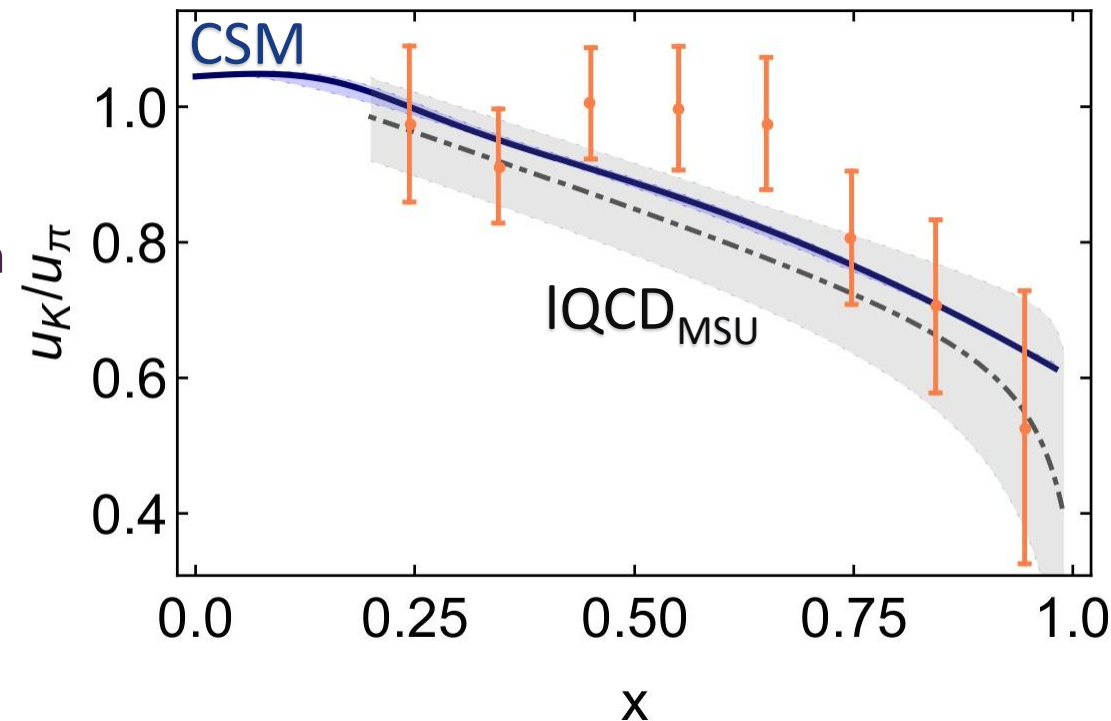


# Status: Kaon

- Little empirical information available on K DFs  $\Rightarrow$  no recent phenom. inferences.
  - Valence-quark distributions: results from models and a single, recent IQCD study
  - Kaon's glue and sea distributions: no results
- One piece of available experimental information:

$$u_K(x)/u_\pi(x)$$

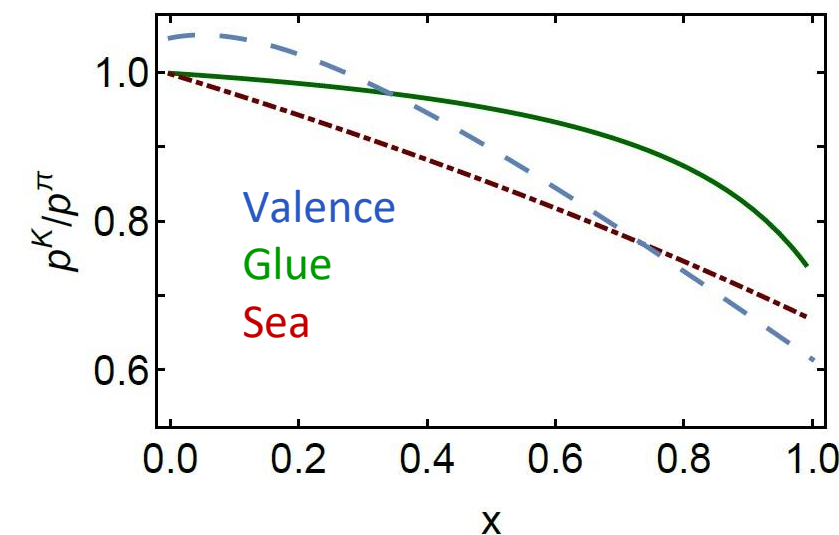
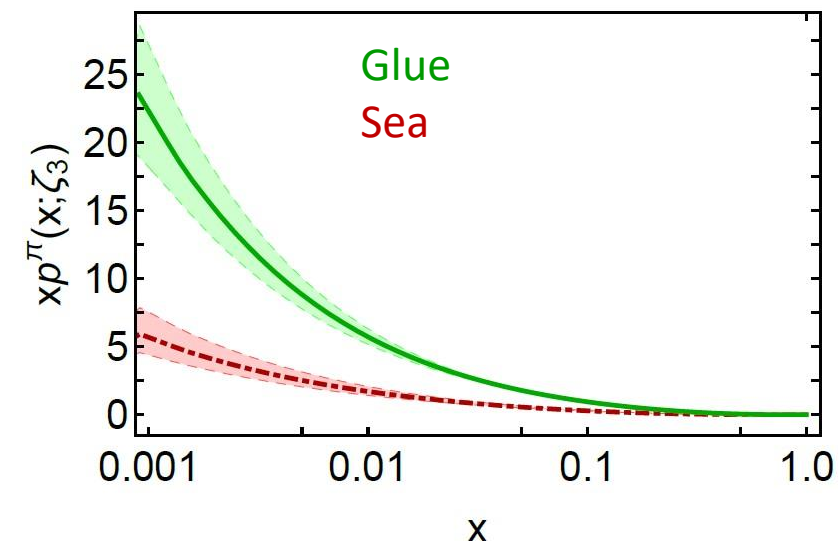
- Continuum prediction for ratio is consistent with data.
- But, given large errors, this ratio is very forgiving of even large differences between various calculations of the individual DFs used to produce the ratio.
  - New, precise data critical if this ratio to be used as path to understanding the Standard Model's Nambu-Goldstone modes;
  - Results for  $u_\pi(x;\zeta_5)$ ,  $u_K(x;\zeta_5)$  separately = better.



# Status: Kaon

Kaon parton distributions, Z.-F. Cui et al., arXiv:2006.14075 [hep-ph], [Eur. Phys. J. C 80 \(2020\) 1064/1-20](#)

- Little empirical information available on K DFs  $\Rightarrow$  no recent phenom. inferences.
  - Valence-quark distributions: results from models and a single, recent IQCD study
  - Kaon's glue and sea distributions: no results until now
- Glue and Sea – Predictions:
  - DFs very similar to those in the pion
  - Detailed comparison requires the use of mass-dependent splitting functions.
  - Development underway ... Preliminary conclusions:
    - i. Light-front momentum fraction carried by s-quarks in the kaon increases by  $\sim 5\%$ ;
    - ii. Compensated by a commensurate decrease in fractions carried by glue ( $-1\%$ ) and sea ( $-2\%$ ).



$$\Psi(x, t)$$

## *Hadron Wave Functions*

# Wave Functions of Nambu Goldstone Bosons

*Insights into the Emergence of Mass from Studies of Pion and Kaon Structure*, Craig D. Roberts, David G. Richards, Tanja Horn and Lei Chang, NJU-INP 034/21, [arXiv: 2102.01765 \[hep-ph\]](https://arxiv.org/abs/2102.01765), Prog. Part. Nucl. Phys. (2021) *in press*

## ➤ Physics Goals:

- Pion and kaon distribution amplitudes (DAs –  $\varphi_{\pi,K}$ )
- Nearest thing in quantum field theory to a Schrödinger wave function
- Consequently, fundamental to understanding  $\pi$  and  $K$  structure.

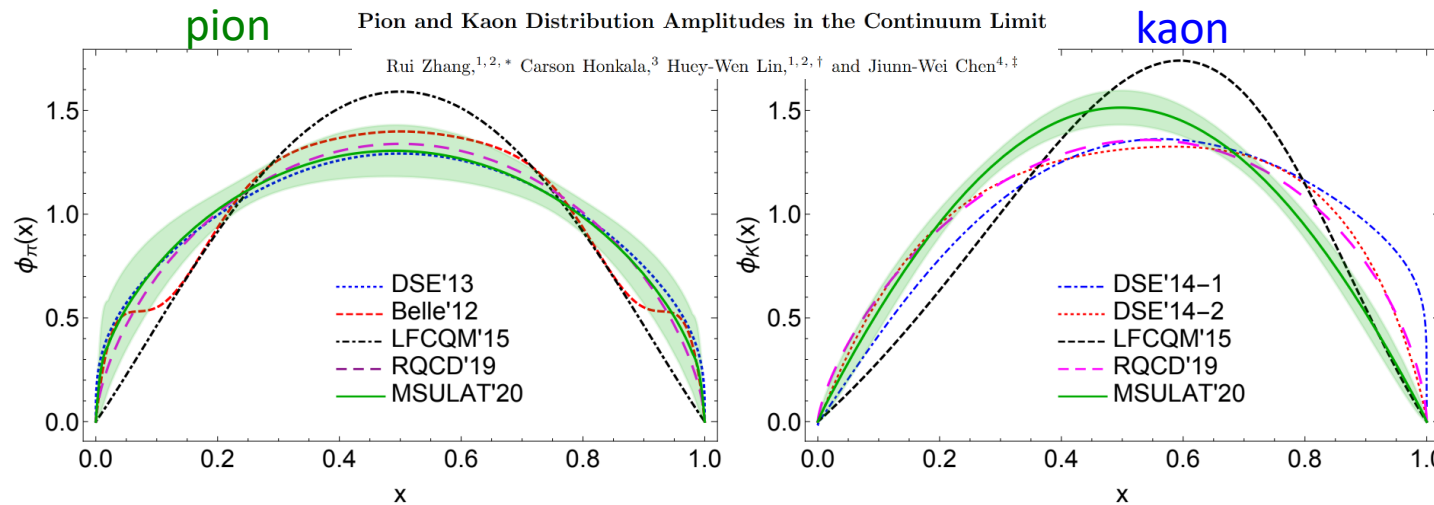
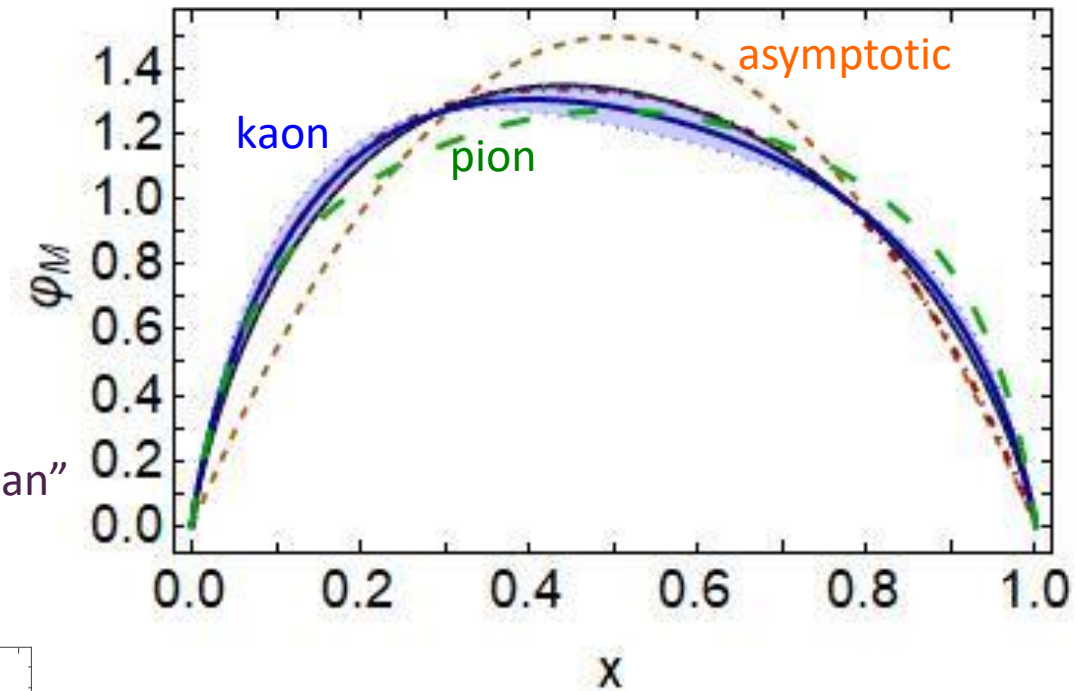
## ➤ Scientific Context:

- For 40 years, the  $x$ -dependence of the pion's dominant DA has been controversial.
- Modern theory predicts that EHM is expressed in the  $x$ -dependence of pion and kaon DAs
- Pion DA is a direct measure of the dressed-quark running mass in the chiral limit.
- Moreover, the kaon DA is asymmetric around the midpoint of its domain of support ( $0 < x < 1$ )
- Degree of asymmetry is signature of constructive interference between EHM and HB mass-generating mechanisms



# Meson leading-twist DAs

- Continuum results exist & IQCD results arriving
  - Common feature = broadening
  - Origin = EHM
- NO differences between  $\pi$  & K if EHM is all there is
  - Differences arise from Higgs-modulation of EHM mechanism
  - “Contrasting  $\pi$  & K properties reveals Higgs wave on EHM ocean”



- Kaon DA vs pion DA
  - almost as broad
  - peak shifted to  $x=0.4(5)$
  - $\langle \xi^2 \rangle = 0.24(1)$ ,  $\langle \xi \rangle = 0.035(5)$
- ERBL evolution logarithmic
- Broadening & skewing persist to very large resolving scales – beyond LHC

FIG. 10. Fit of the  $P_z = 4\frac{2\pi}{L}$  pion (left) and kaon (right) data to the analytical form in Bjorken- $x$  space, compared with previous calculations (with only central values shown). Although we do not impose the symmetric condition  $m = n$ , both results for the pion and kaon are symmetric around  $x = 1/2$  within error.

Craig Roberts. [cdroberts@nju.edu.cn](mailto:cdroberts@nju.edu.cn) "Insights into EHM Using Pion and Kaon Targets"



# Wave Functions of Nambu Goldstone Bosons

## ➤ Scientific Context:

- Today, finally, continuum and lattice theory are delivering consistent predictions for  $\varphi_{\pi,K}(x)$
- Can signature features of interference between EHM and HB, which are manifest in low-order Mellin moments of the DAs, be probed experimentally?

## ➤ Data: Existing

- One 20-year-old experiment at Fermilab [E791 – Aitala:2000hb] delivered results on the pion DA that have become controversial.
- In some ways, the data are internally inconsistent.

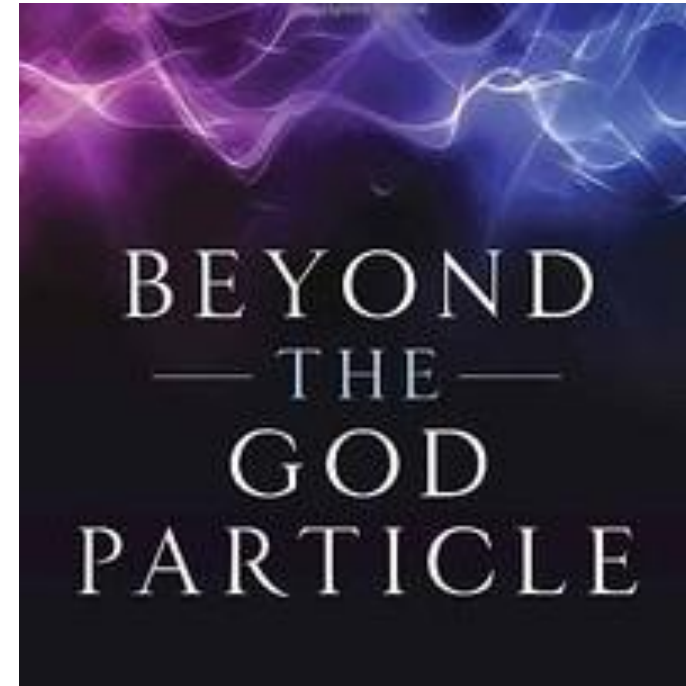
## ➤ *Data: Future ... $x$ -dependence or moments of Nambu-Goldstone boson DAs*

- *JLab & EIC & EicC  $\Rightarrow$  access to moments via elastic form factors at large  $Q^2$*
- *AMBER @ CERN with high-intensity  $\pi$  and  $K$  beams  $\Rightarrow$  potential access via diffractive production of jets to  $x$ -dependence or via two-meson final states to moments*



# Epilogue

- Nature has two sources of mass
  - Higgs mass-generating mechanism = understood
  - Phenomenon of Emergent Hadron Mass = much to learn
- EHM (possibly/probably?) lies within the Standard Model, i.e., in strong QCD
- Basic predictions:
  - Gluons acquire mass  $\Rightarrow$  running coupling saturates on infrared domain, restoring approximate conformal behaviour
  - Enigmatically, the unusually light Nambu-Goldstone bosons provide the clearest windows onto the Emergence of Mass in Nature
- With modern and on-the-horizon facilities having the capacity to deliver practical pion and kaon “targets”, science can finally move beyond the proton and study an entirely different form of hadron matter = the mesons without which observable Universe could not exist



# Get off the Ground!

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*Thankyou*



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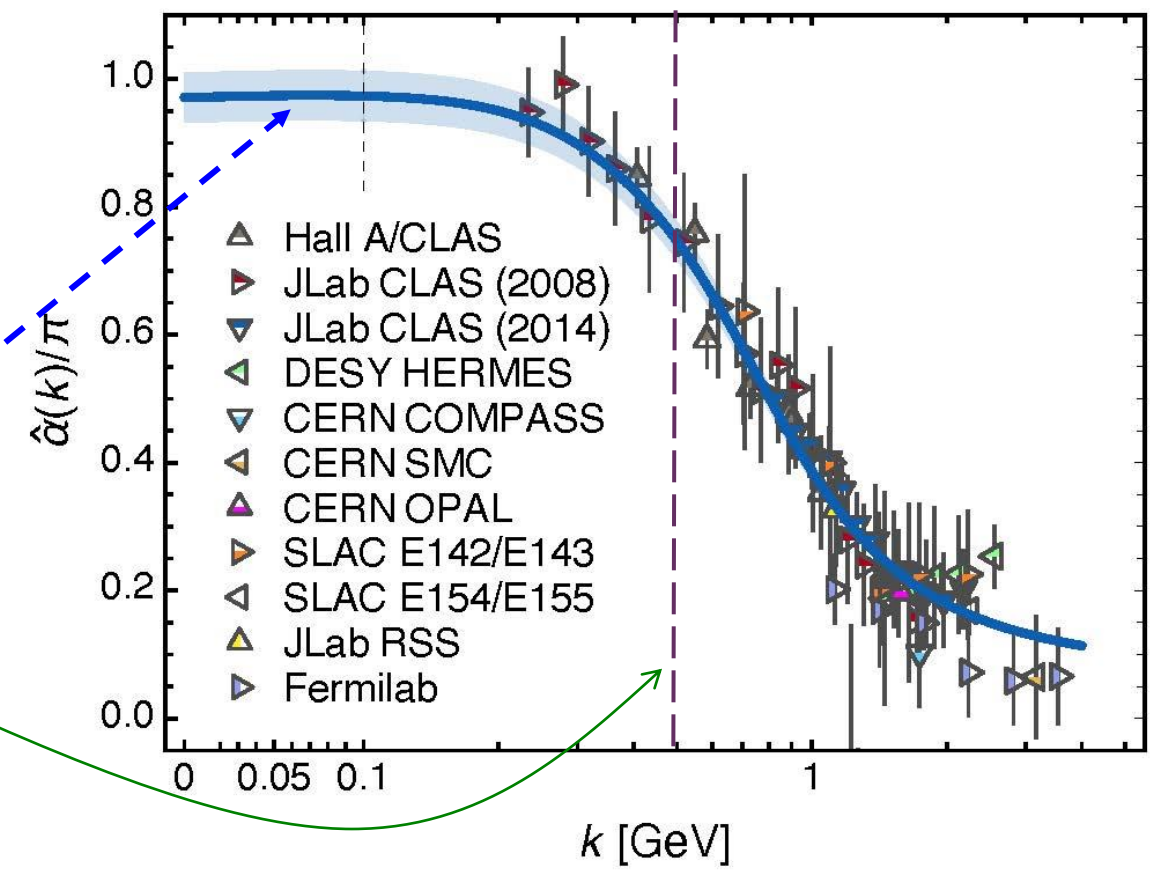






# Prediction: Process-independent effective-charge in QCD

- Modern continuum & lattice methods for analysing gauge sector enable QCD analogue “Gell-Mann – Low” running charge to be defined and calculated
- Combined analysis of QCD’s gauge sector yields a *parameter-free prediction*
- N.B. Qualitative change in  $\hat{\alpha}_p(k)$  at  $k \approx \frac{1}{2} m_p$
- No Landau Pole
  - “Infrared Slavery” picture is not correct
- Below  $k \sim \hat{m}_0$ , interactions become scale independent, just as they were in the Lagrangian; so, QCD becomes practically conformal again



Data = process dependent effective charge [Grunberg:1982fw]:  $\alpha_{g1}$ , defined via Bjorken Sum Rule