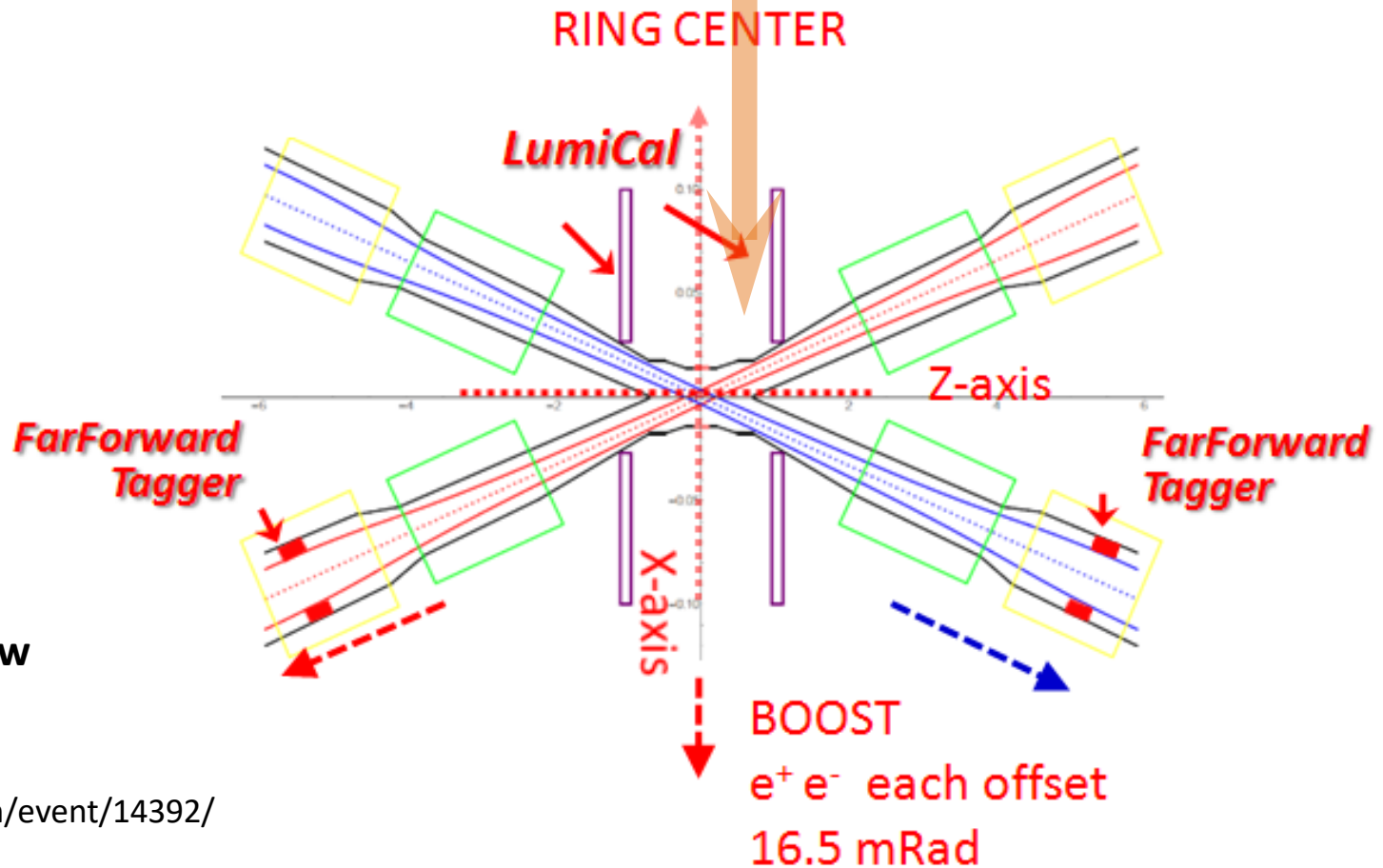
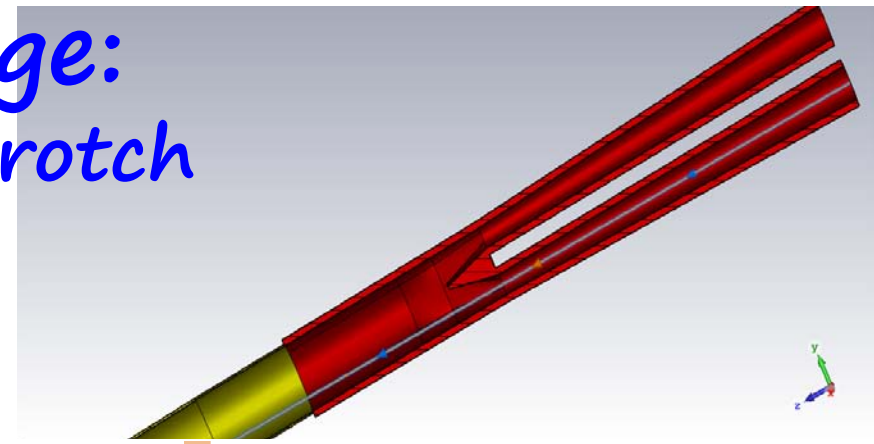


LumiCal behind Flange: 28-40 mm pipe with Y-crotch and dual 20mm pipes



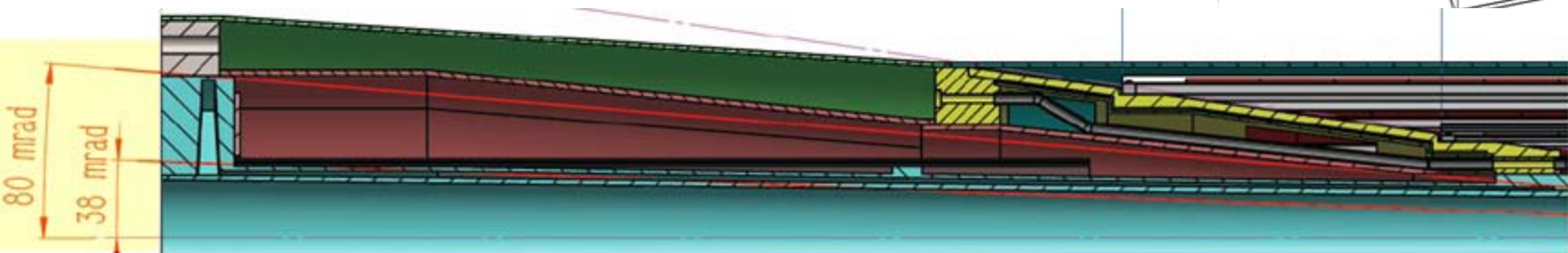
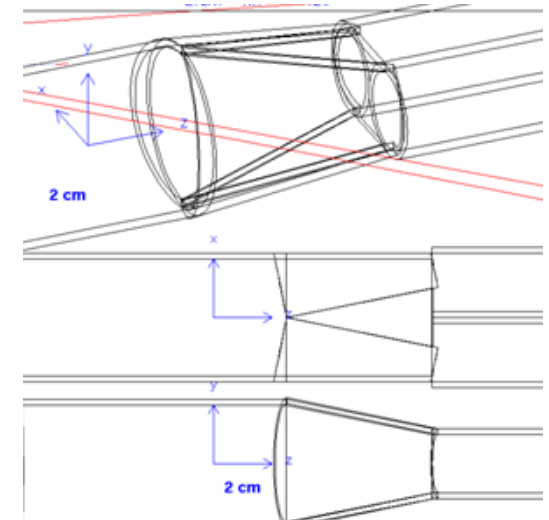
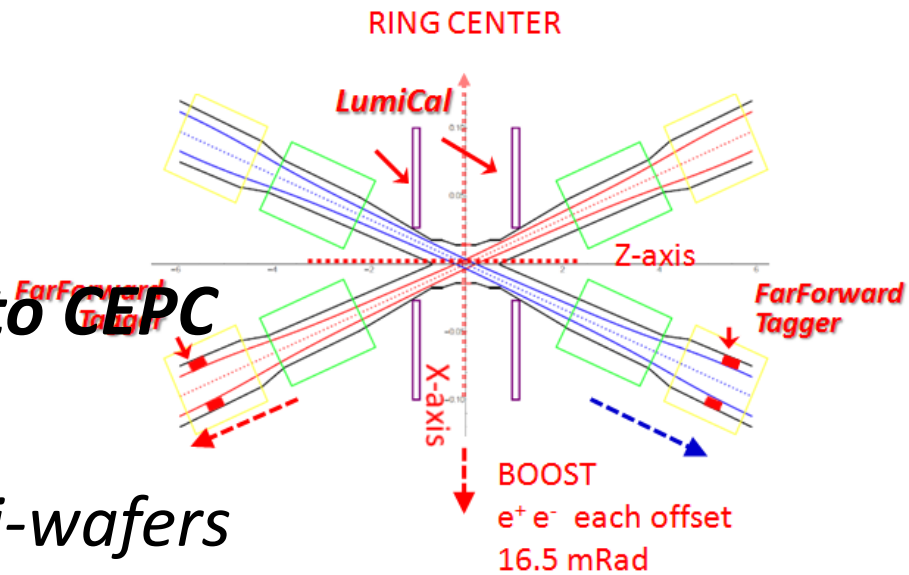
Suen Hou 侯書雲
suen@sinica.edu.tw

2021.10.22

<https://indico.ihep.ac.cn/event/14392/>

outline

- **Bhabha Luminosity basics to CEPC**
- **Multiple Scattering**
before Flange: inner Lumi Si-wafers
after Flange: Y-crotch, Q-pole front
- **Cross sections with 28-40 round pipe**
Y-crotch acceptance
- **Dual 20mm pipes gain cross section**



Luminosity by Bhabha

- **For Standard Model Cross sections**

Z-lineshape dominant: $e^+e^- \rightarrow Z \rightarrow q\bar{q}$

SM events: $N = \sigma \cdot \int L$

- **Luminosity L**

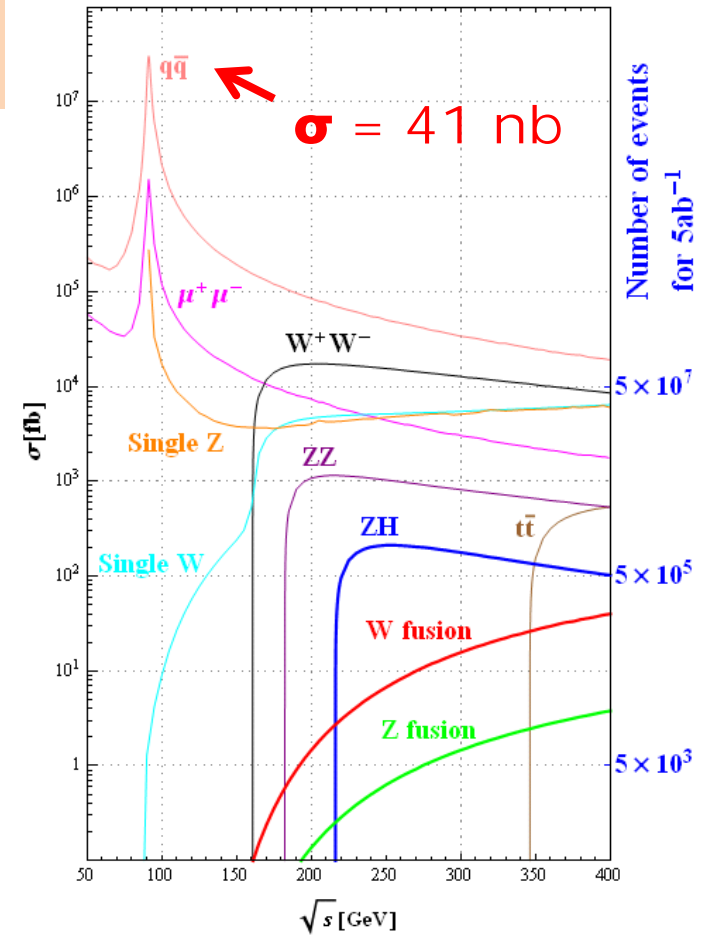
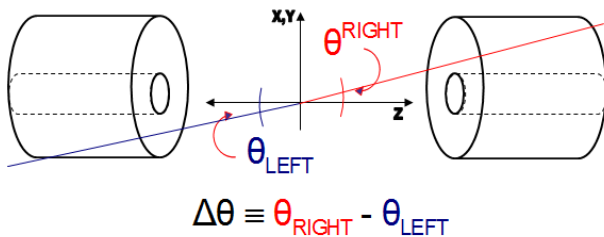
by counting Bhabha elastic scattering

$$e^+e^- \rightarrow e^+e^-$$

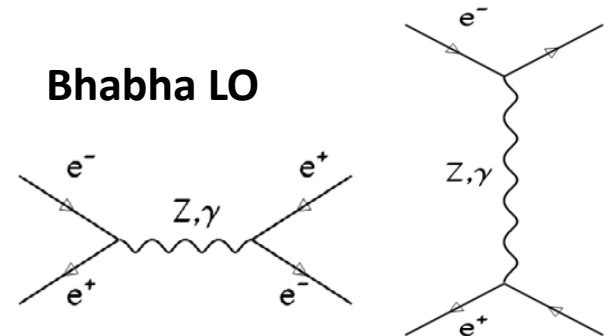
- QED process, *theoretical* < 0.1% precision
- detect a pair of *back-to-back* e^+e^-

Bhabha cross section

$$\mathcal{L} = \frac{1}{\epsilon} \frac{N_{\text{acc}}}{\sigma^{\text{vis}}} \quad \sigma = \frac{16\pi\alpha^2}{s} \cdot \left(\frac{1}{\theta_{\text{min}}^2} - \frac{1}{\theta_{\text{max}}^2} \right)$$



Bhabha LO



Luminosity precision

Systematic error, Center-of-Mass frame

$$\delta L/L \sim 2 \delta\vartheta/\vartheta_{\min}$$

$\delta L/L < 10^{-3}$ for Higgs factory

$$\rightarrow \delta\vartheta = 15 \mu\text{Rad} \quad @\vartheta_{\min} = 30 \text{ mRad}$$

\rightarrow **OFFSET** on the

“mean of fiducial edge”

cause for δN on Bhabha counting

@z = 1000 mm, $\delta\vartheta = 15 \mu\text{Rad}$

corresponds to

dz = 0.1 mm or dr = R $\times\vartheta$ = 3 μm

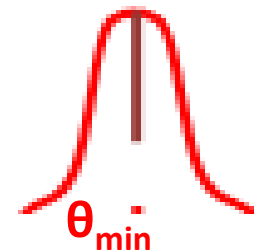
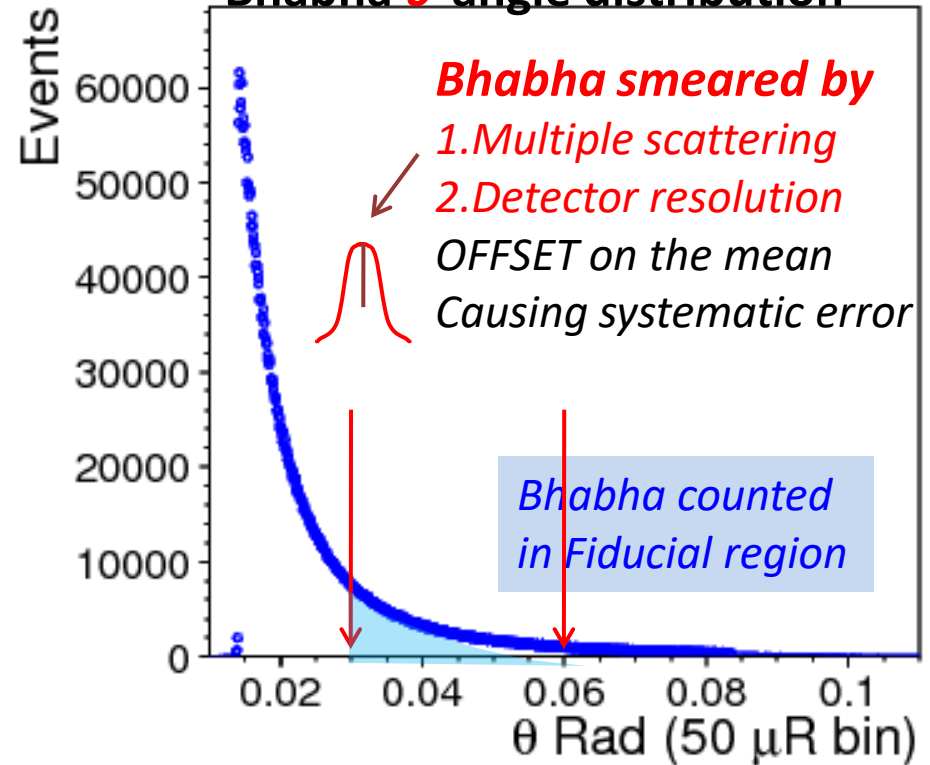
LumiCal design goal:

- Spatial resolution as sharp as possible
- Describe the **reso./MS** shape of $\delta\langle\theta_{\min}\rangle$
bin resolution $\sim 3 \mu\text{m}$ in r, or 100 μm in z

offset on the mean of θ_{\min}

\rightarrow **LUMINOSITY** error

Bhabha ϑ -angle distribution

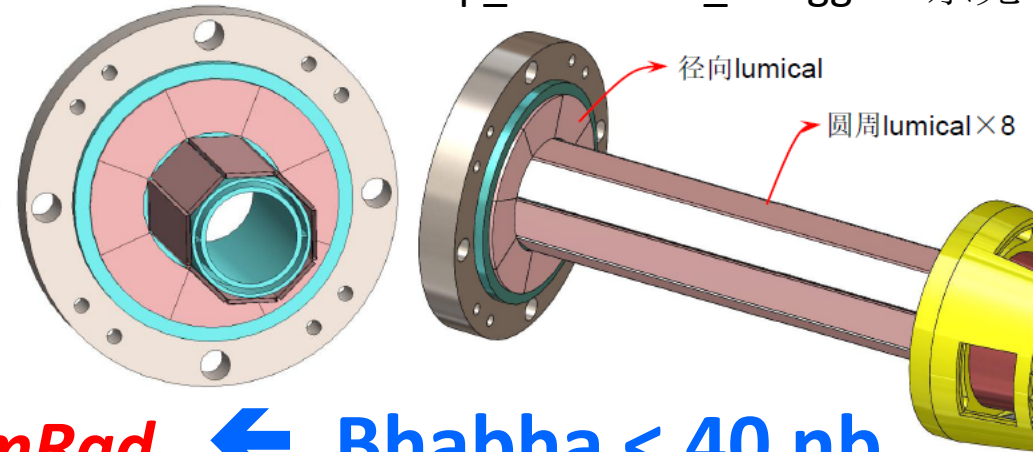


Beam-pipe, 28-40mm Round

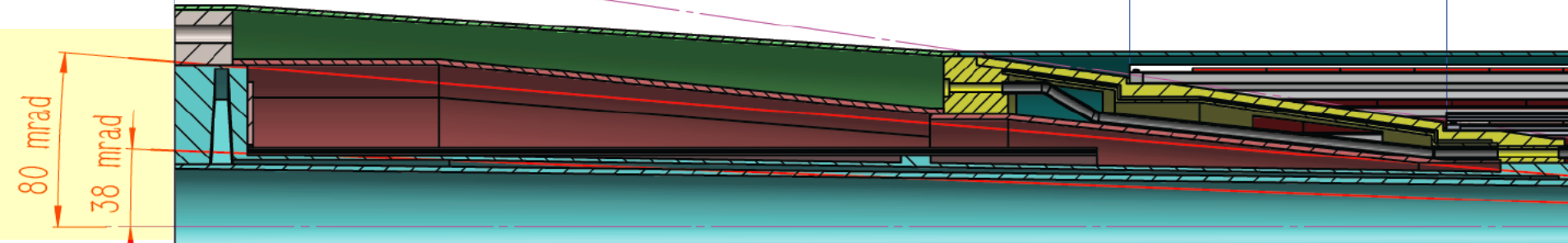
Workshop_20200828_Dongguan 东莞

5.5 Preliminary design of lumical

- Detection Angle range: 38~80mrad
- On the detection path, as little mass as possible
- The structure of lumical is not yet determined, so the support and cooling structure should be further optimized and improved.



LumiCal access, $\vartheta_{min} = 38 \text{ mRad}$ ← Bhabha $< 40 \text{ nb}$



Al pipe $x = 200 - 700 \text{ mm}$, inner 0.5 mm , outer 0.35 mm thick

Inner diameter @Z=200 $\varphi = 28 \text{ mm}$

Inner diameter @Z=675 $\varphi = 40 \text{ mm}$ → $\text{atan} = 29.6 \text{ mRad}$

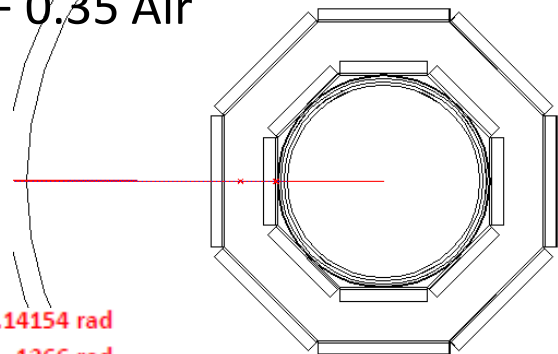
Flange z=675~700, dia.=40 mm flat

Corner of **38 mRad** @ Z=(700-25) mm

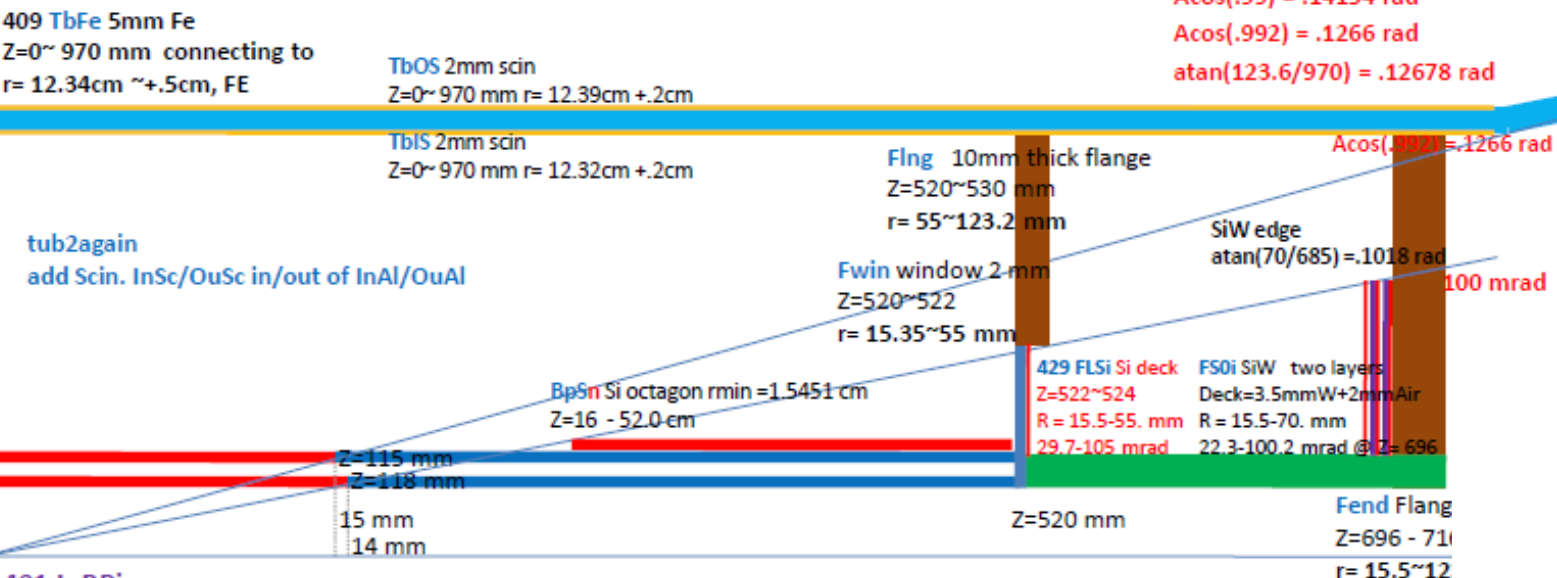
Radius = (700-25)*tan(.038) $r = 25.66 \text{ mm}$

1) Simple 28mm straight pipe

- Tube design, $\phi=28$ mm, thickness (mm): 0.5 Al – 0.5 Air – 0.35 Air
- Si wafer attacked tightly
- Scintillator layer surrounding Al pipe
- ➔ observe Multiple-Scattering within Al pipe, Δz in Al-pipe: 20 – 40 mm



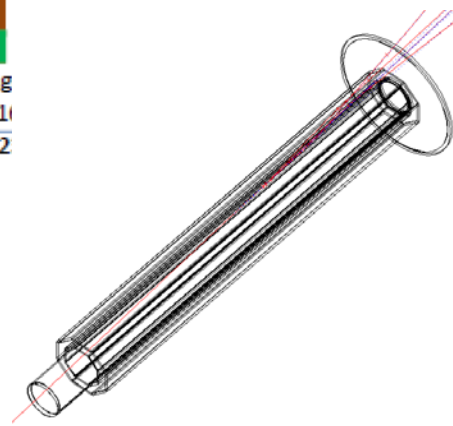
$\text{Acos}(.99) = .14154 \text{ rad}$
 $\text{Acos}(.992) = .1266 \text{ rad}$
 $\text{atan}(123.6/970) = .12678 \text{ rad}$



- 401 InBPipe**
- InBP Inner Be pipe**
Z=0~118 mm, inner diameter 28 mm 0.5mm thick
 - InAl Inner Cu pipe**
Z=118~500 mm, inner diameter 28 mm 0.5mm thick
 - OuBP outer Be pipe**
Z=0~115 mm, inner radius 28/2+1 mm 0.35mm thick
 - OuAl outer Al pipe**
Z=0~115 mm, inner r=28/2+1 mm, 0.35 mm thick

Fpip flange pipe 1.5 mm thick
Z= 522-716 mm
at Z=512 r= 14 – 15.5 mm

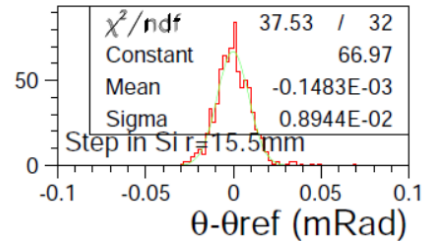
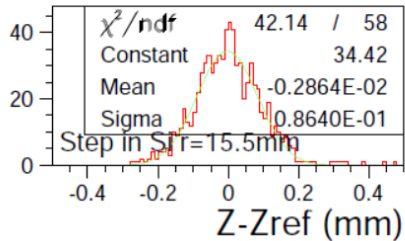
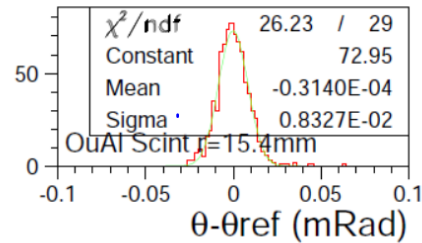
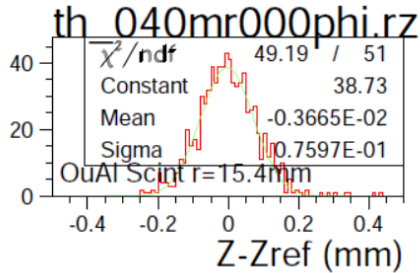
2020 LumiCal geom



1) 28mm pipe Multiple scattering

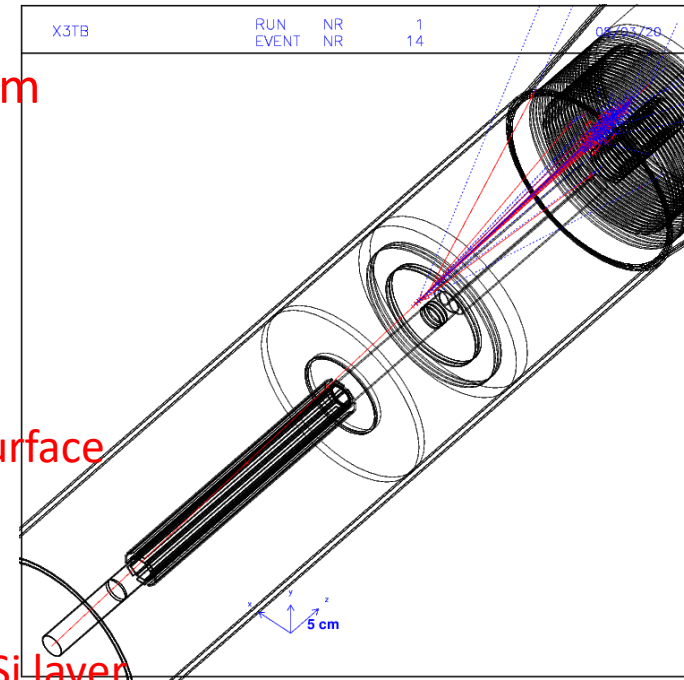
- **50 GeV electron** traversing Al-pipe (mm): 0.5 Al – 0.5 Air – 0.35 Air
@ fixed theta, phi=0°

- **Multiple scattering deviation** simulated for $\phi=28$ mm
 1. exiting Al-pipe (a Scintillator layer on surface)
 2. no air-gap, Si-layer attached



←
dz, dθ
on Al-pipe surface

←
dz, dθ
on Octagon Si layer



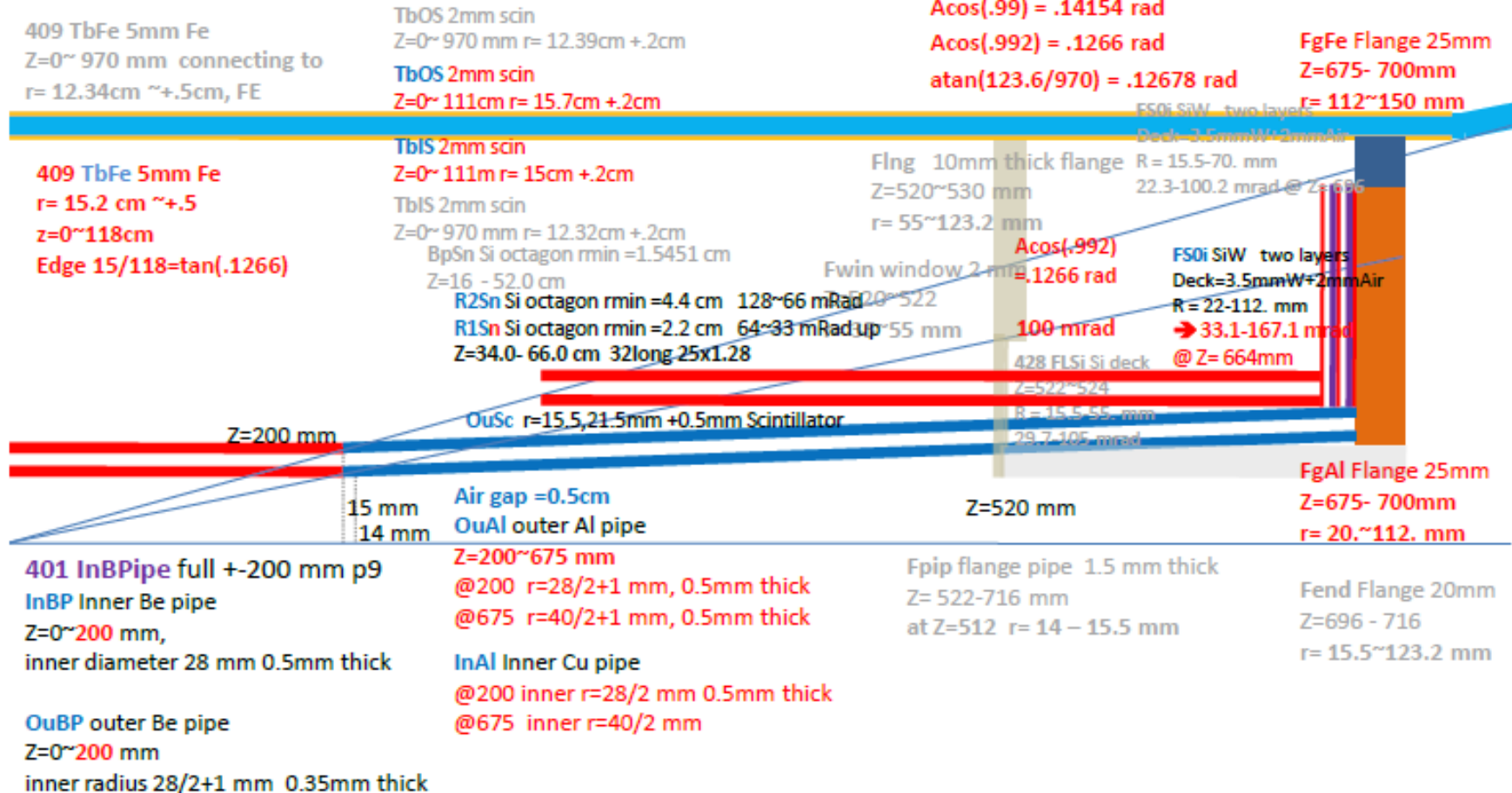
50 GeV (θ, ϕ)	$\sigma(Z)$	$\sigma(\theta)$	$1/\tan(\theta)$
e (40 mR, 0°)	86 μm	8.9 μRad	25.0
e (55 mR, 0°)	37 μm	7.3 μRad	18.2
e (60 mR, 0°)	28 μm	6.5 μRad	16.6
e (70 mR, 0°)	19 μm	5.8 μRad	14.3

θ to z: $r/z = \tan \theta$

2) 28-40mm cone pipe (2021)

- Tilt the Al pipe from $\phi=28$ mm to $\phi=40$ mm
- thickness (mm): 0.5 Al – 0.5 Air – 0.35 Air
- Si wafer parallel to z-axis $r_{min}=22$ mm
- ➔ air gap to Al-pipe, large Multiple Scattering

poor lumi si-wafer design !

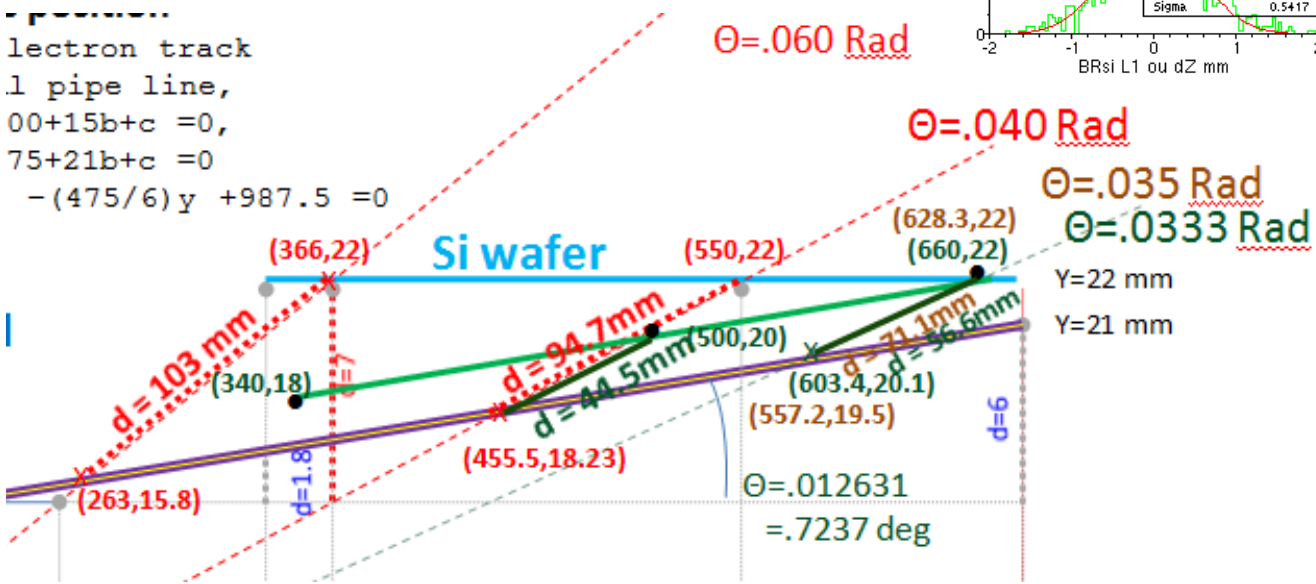
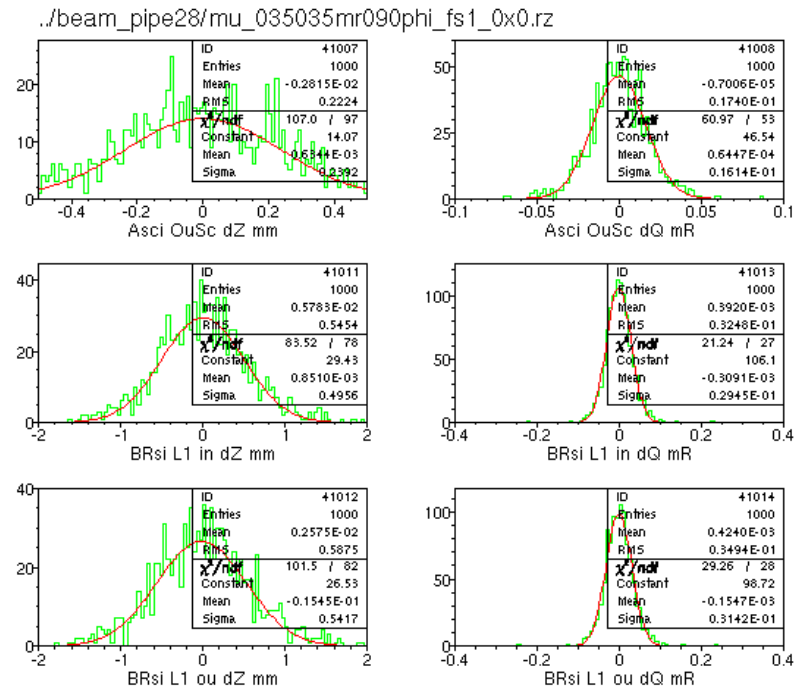


2) Multiple Scattering on Si ring (parallel)

- Al-pipe tilt 12.6 mRad ($\phi 28$ to 40 mm)
- Si-layer ($r=22\text{mm}$) parallel to z-axis
- ➔ air-gap from IP ~ 100 mm
- ➔ multiple scattering effect is magnified !!

Compare MS on Octagon Si layer, *primary track*

μ (θ, ϕ)	$\sigma(Z)$ Si ^{1st}	$\sigma(\theta)$ Si ^{1st}	$1/\tan(\theta)$
(35 mR, 90°)	542 μm	31 μRad	28.6
(40 mR, 90°)	489 μm	37 μRad	25.0
(55 mR, 90°)	291 μm	41 μRad	18.2

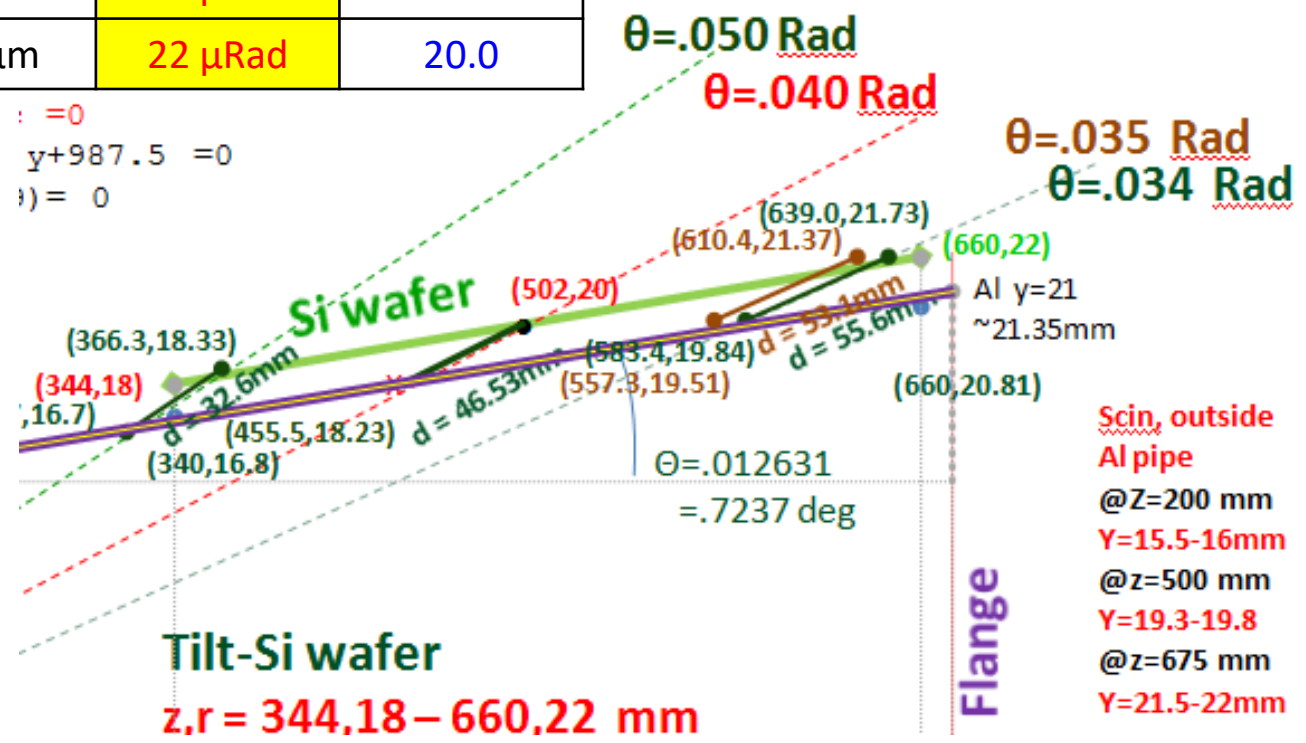
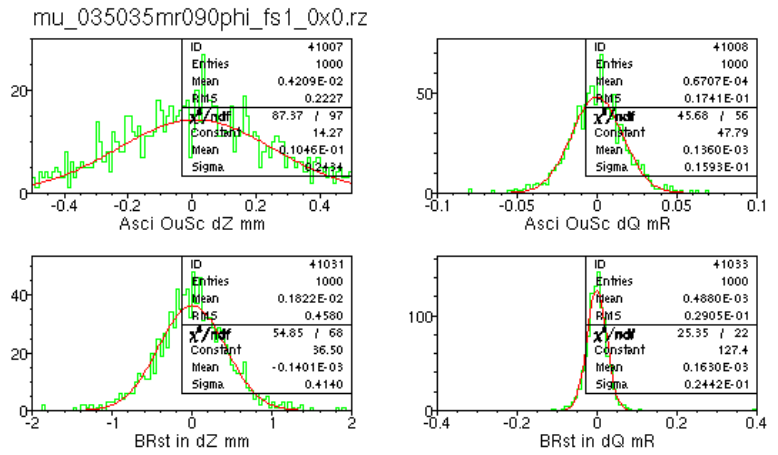


2) Multiple Scattering on Si ring (stick-on)

- Al-pipe tilt 12.6 mRad ($\phi 28$ to 40 mm)
- Si-layer parallel to Al-pipe, gap = 1mm
- ➔ air-gap from IP **~ 50 mm**

Compare MS on Octagon Si layer, **primary track**

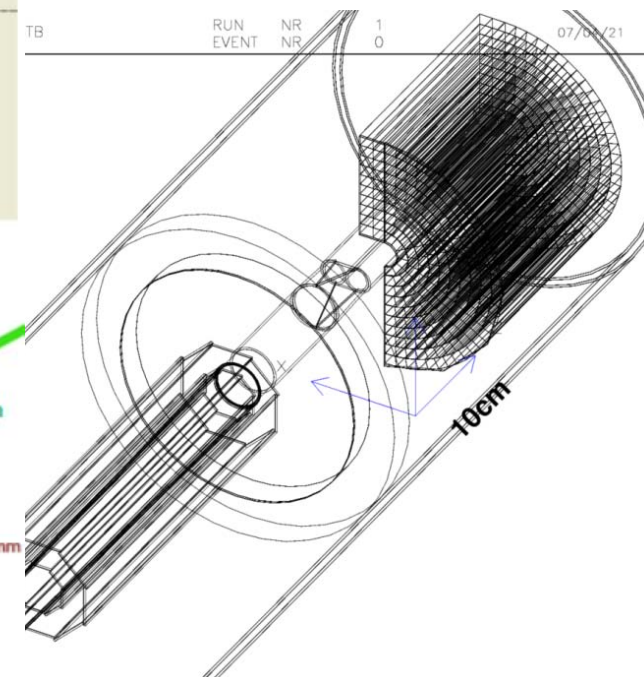
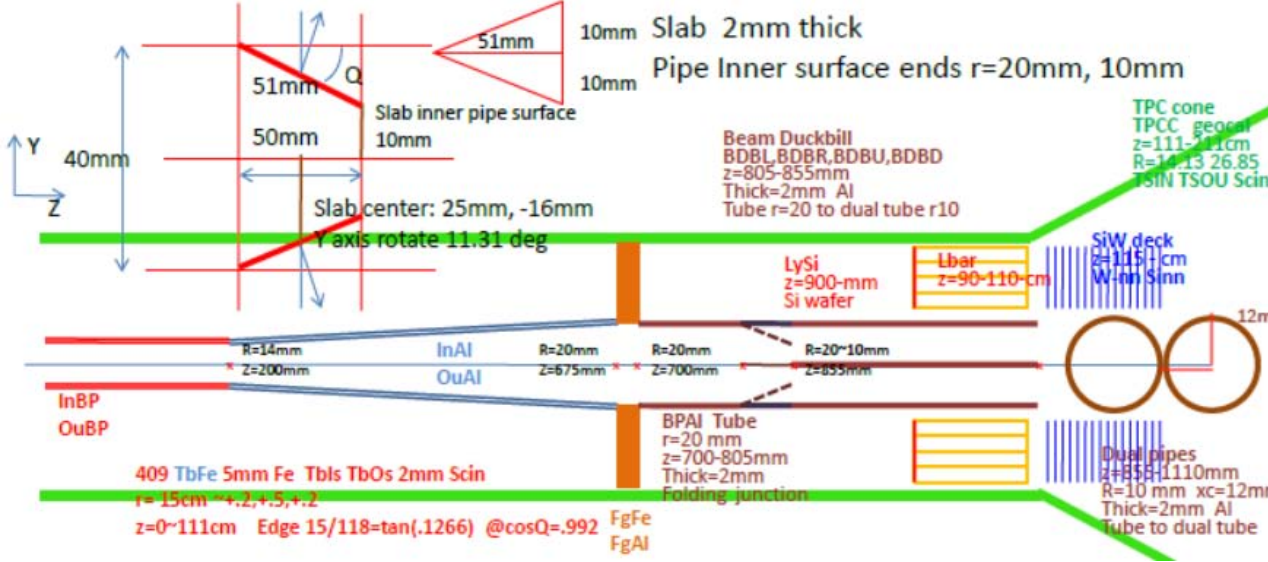
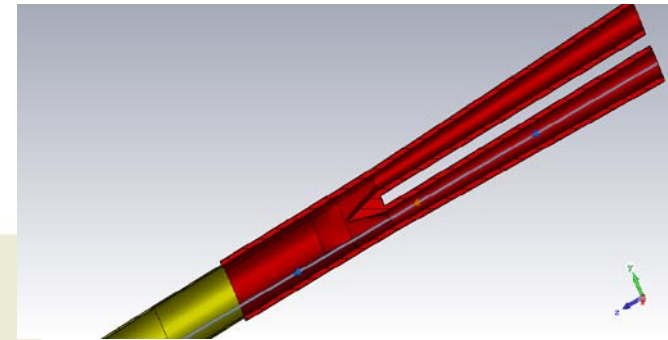
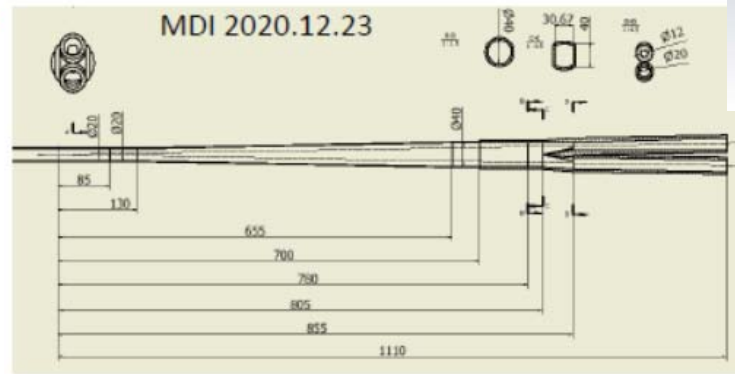
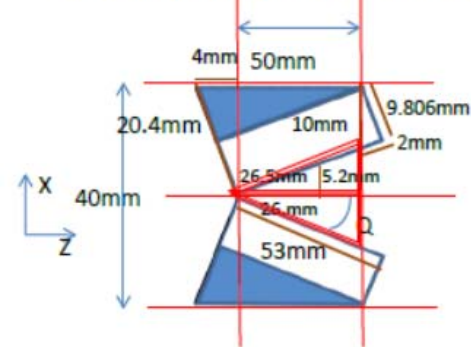
$\mu(\theta, \phi)$	$\sigma(Z) \text{ Si}^{1st}$	$\sigma(\theta) \text{ Si}^{1st}$	$1/\tan(\theta)$
(35 mR, 90°)	475 μm	28 μRad	28.6
(40 mR, 90°)	301 μm	24 μRad	25.0
(50 mR, 90°)	161 μm	22 μRad	20.0



Multiple Scattering behind the Flange

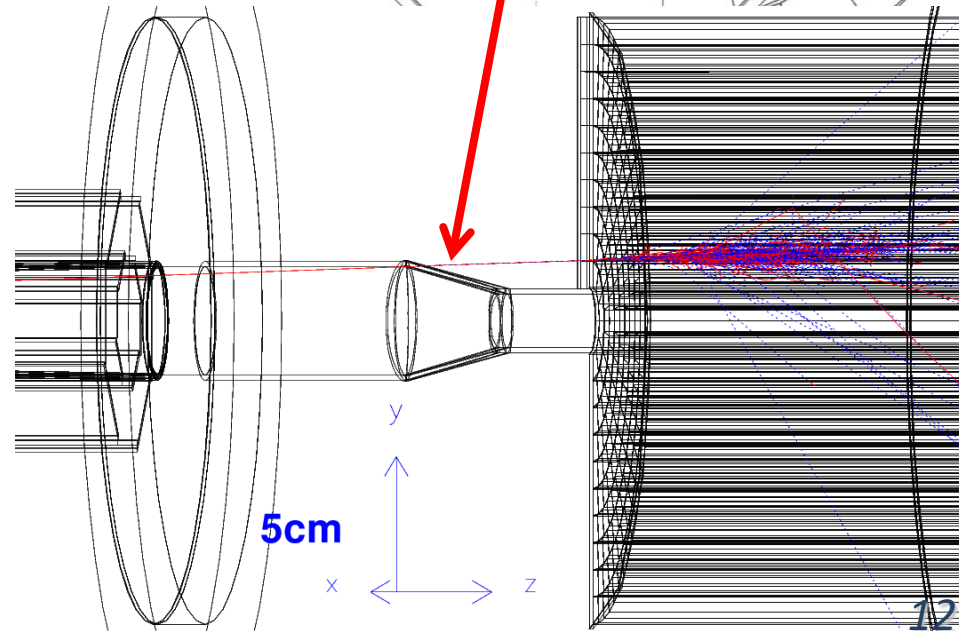
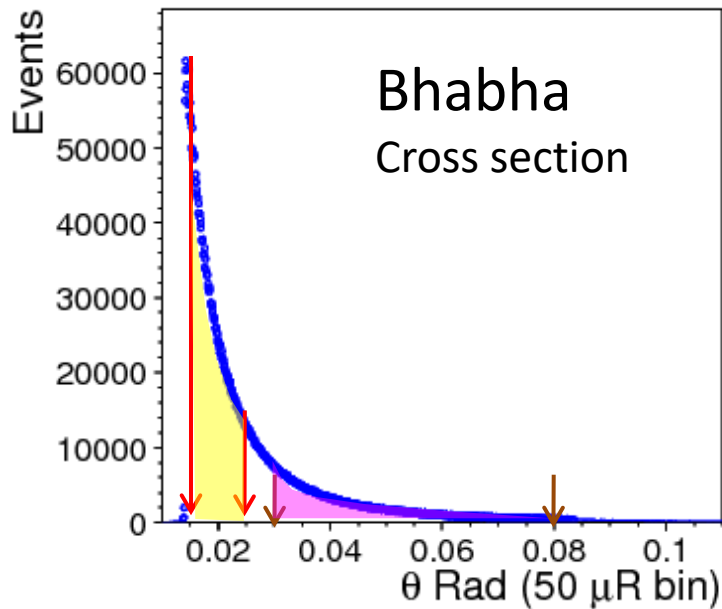
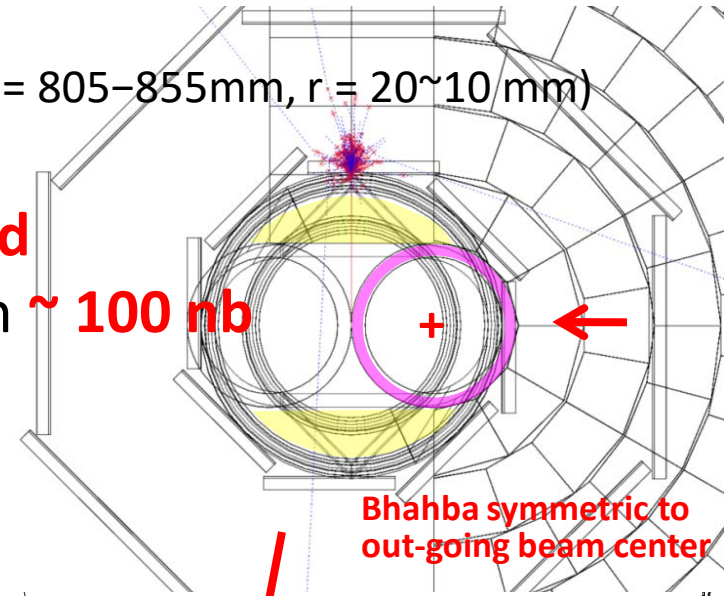
the **y-crotch** $\phi=40$ to dual 20 mm pipes is **a low-mass, high cross section** window for Bhabha

$$Q = \text{atan}(10/50) = .1974 = 11.31 \text{ deg}$$



3) γ -crotch window

- Duckbill slope on y-axis is **200 mRad**, ($z = 805-855\text{mm}$, $r = 20\sim 10\text{ mm}$)
electron traversing distance $\sim 10\text{ mm}$
- Window on lab y-axis: $\theta = 15 - 25\text{ mRad}$
- Bhabha cross section in clean phi region $\sim 100\text{ nb}$
- Electron θ measured by Si r- ϕ disk before LYSO



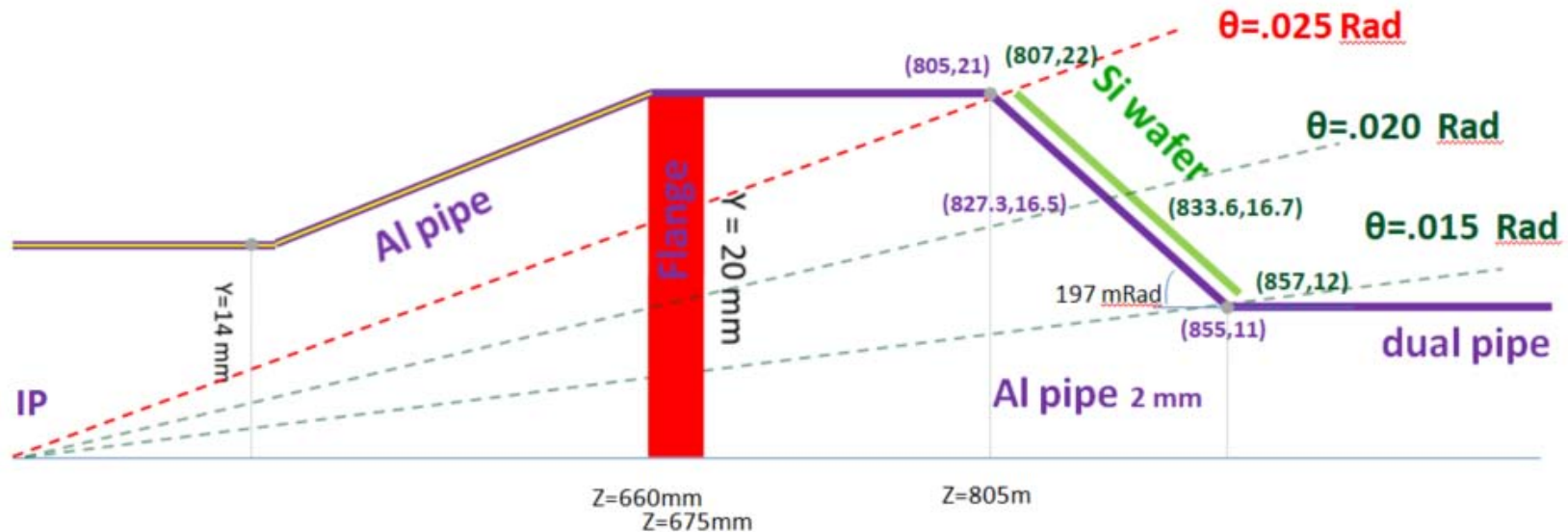
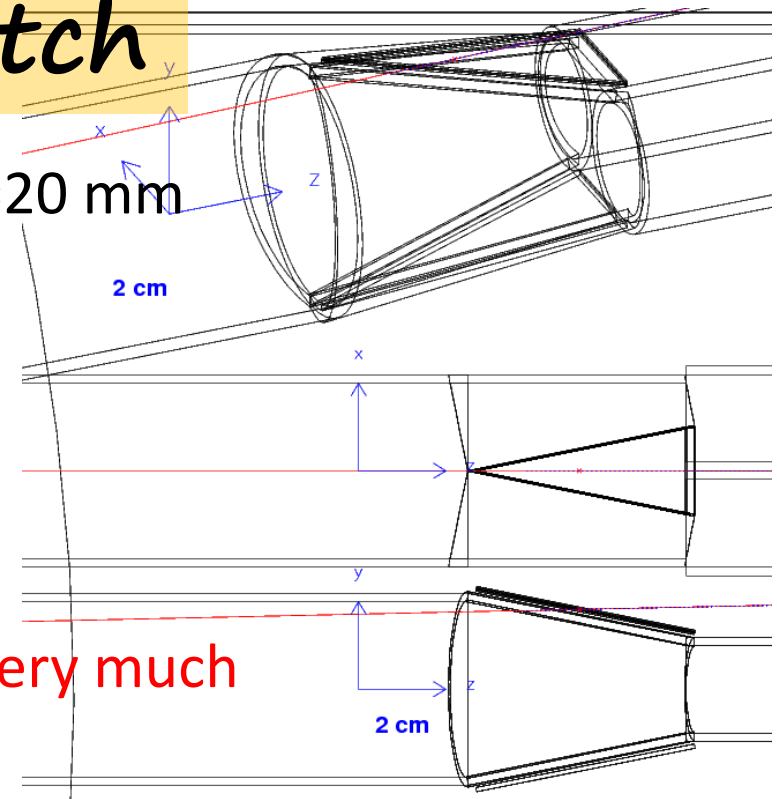
3) Si-wafers on Y-crotch

- Round pipe $\phi=40$ mm to dual pipes $\phi=20$ mm
Slabs on top/down of the Y-crotch
 $z= 805$ to 855 mm
slope = 197 mRad (11.3 deg)

- Si wafer 1 mm above

➔ air gap from IP: **$6\sim 6.5$ mm**

Multiple Scattering effect suppressed very much



3) LumiCal Si-wafer spatial resolution

50 GeV electron, *all hits* on Si wafers

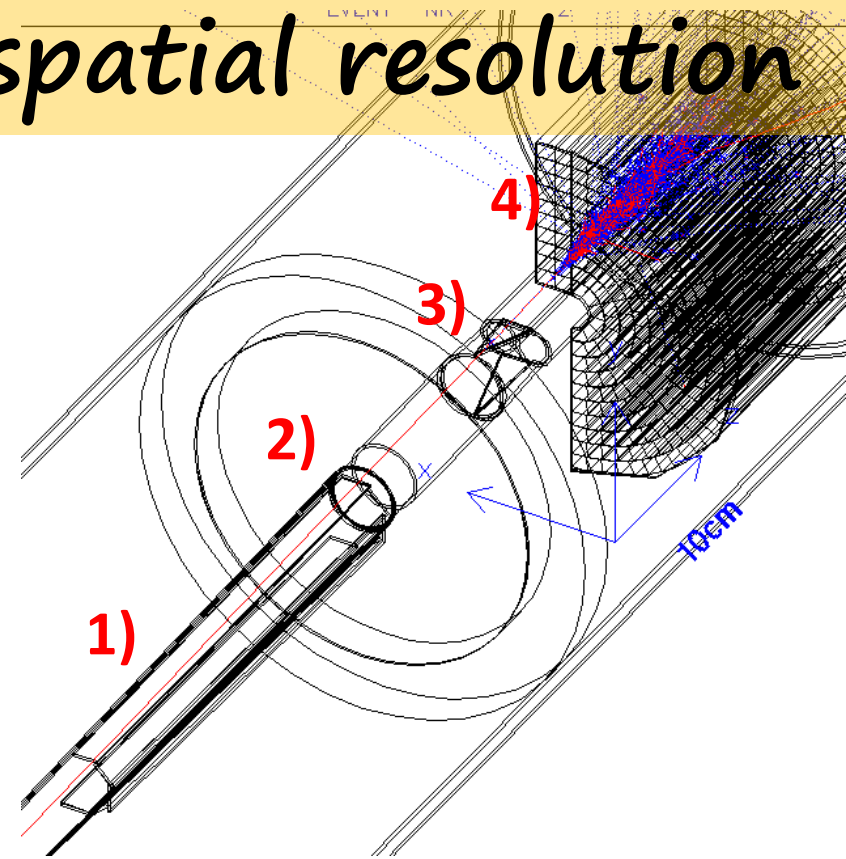
(primary e^- and secondaries)

Scan vertically $\phi = 90^\circ$

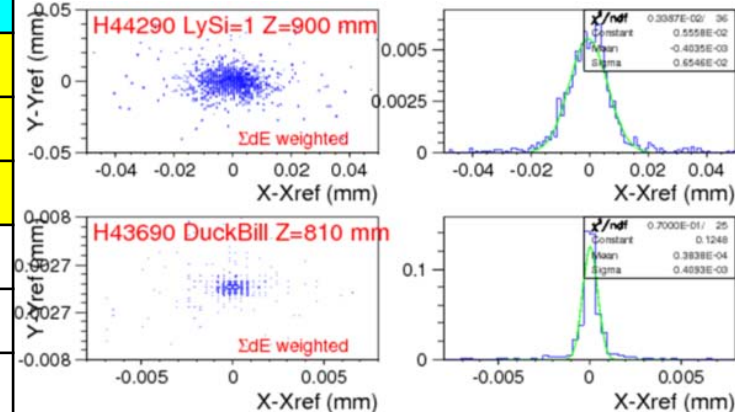
through Y-crotch window

Multiple scattering estimated on

- 1) Octagon surrounding Al-pipe
- 2) Flange Si-disk
- 3) Y-crotch up/down slabs
- 4) LYSO front Si-disk



Lab (θ, ϕ)	1) $\sigma(z)$ Oct Si	2) $\sigma(x)$ Flg Si	3) $\sigma(x)$ Y-cr. Si	4) $\sigma(x)$ Ly-Si
e (15 mR, 90°)	–	–	0.55 μm	5.3 μm
e (20 mR, 90°)	–	–	0.41 μm	6.5 μm
e (25 mR, 90°)	–	–	0.88 μm	9.8 μm
e (30 mR, 90°)	–	–		95 μm
e (40 mR, 90°)	620 μm	52 μm		129 μm
e (55 mR, 90°)	373 μm	58 μm		114 μm
e (60 mR, 90°)	308 μm	65 μm		111 μm



4) dual-20mm pipes, Lumical option

- round pipe $\phi < 20$ mm @IP
split slowly to dual pipes, $\phi = 20$ mm, at Y-crotch
- 1) LumiCal Si wafers, vertical y-axis $r_{\min} = 10$ mm
→ gain very much Bhabha X.section
- 2) Si wafers parallel to beam center
→ multiple scattering acceptable $\sigma(\theta) \sim 10 \mu\text{Rad}$

Boosted Bhabha distribution

- Bhabha symmetric to out-going beam center boosted by the 33 mRad beam crossing

$(x,y) = (16.5, 0) @ z = 1000 \text{ mm}$

- High cross-section, low mass region:

$\phi \sim 60^\circ \text{ to } 120^\circ \text{ to beam center}$

- Bhabha acceptance: both $e^+ e^-$ detected

Lab frame @ z = 1000 mm

dual beampipe: $r = 10 \text{ mm}$

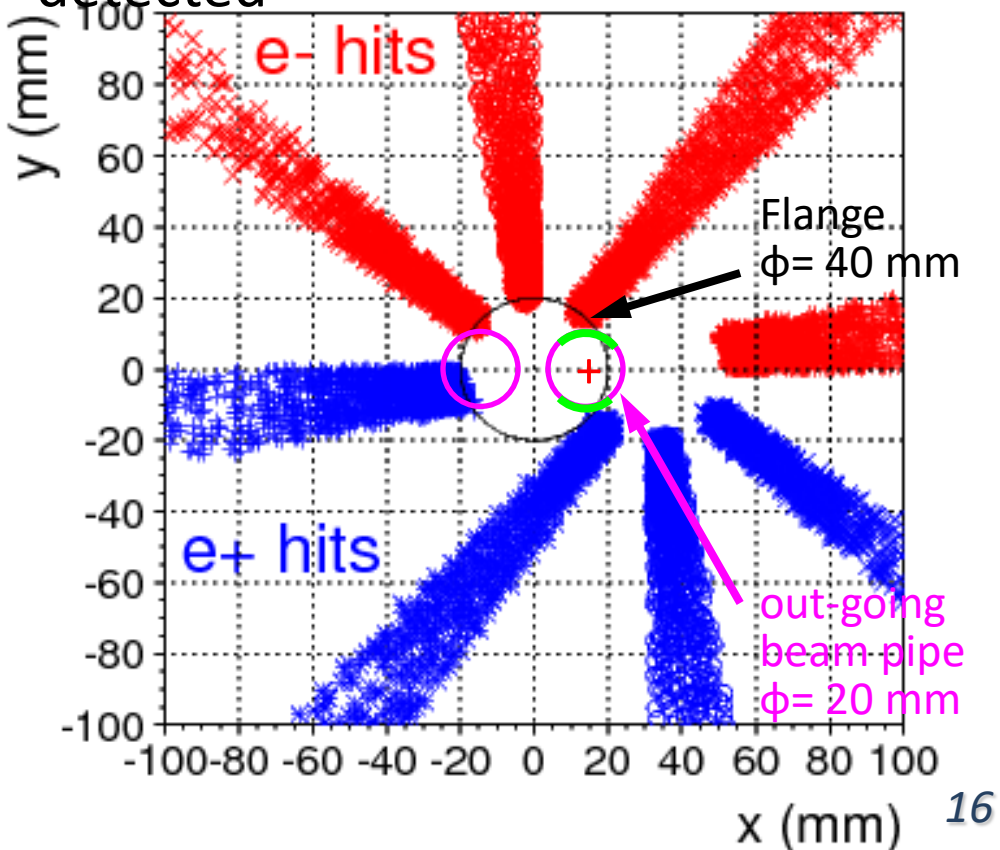
y-axis: $|y| > 10 \text{ mm}$,

x-axis: ($\pm 43 \text{ mRad}$ to out-going beam center)

Lab $\theta(e^+) > 26.5 \text{ mRad}$

Lab $\theta(e^-) > 59.5 \text{ mRad}$

Lab frame @z=1000
Bhabha distribution



Bhabha cross-section, BHLUMI calculation

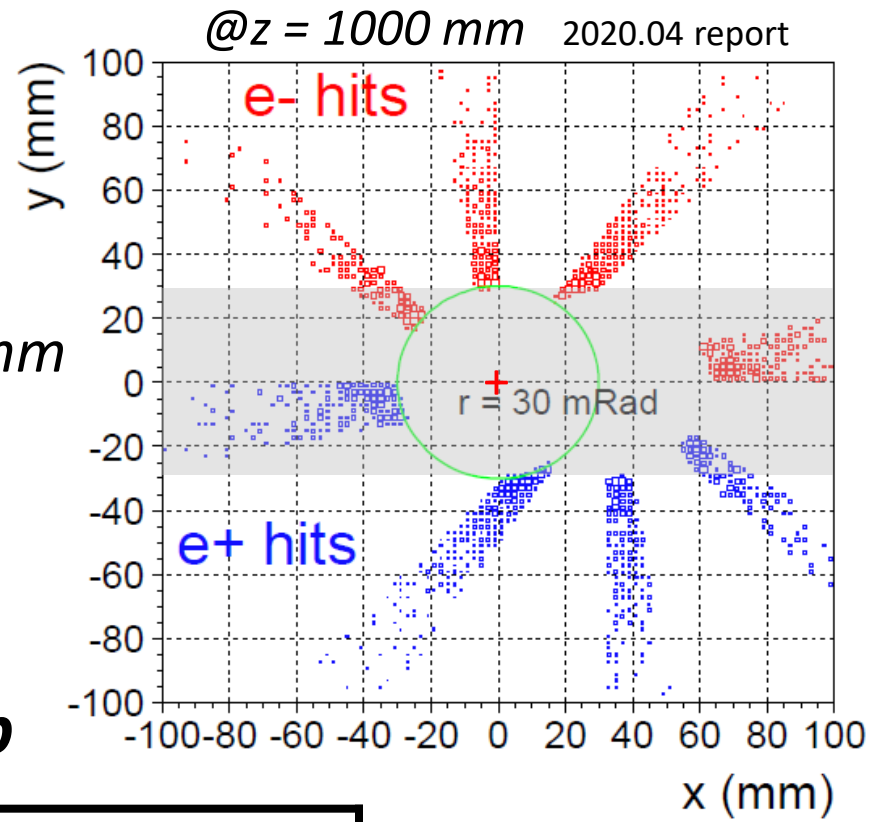
Beam crossing 33 mRad,

- $e^+ e^-$ boosted to +x, off ring center
- back-to-back symmetric to out-going beam center
 $(x,y) = (16.5, 0 \text{ mm})$ at $z = \pm 1000 \text{ mm}$

50 GeV beam, both $e^+ e^-$ detected
 In fiducial range of $r > 30 \text{ mRad}$

ϑ range = 30 – 80 mRad

Bhabha cross section > 50 nb



BHLUMI, 50 GeV Bhabha boosted for 33 mRad crossing			
CMS 10 ~ 80 mRad		LAB detect both electrons	
BARE1		off beampipe full phi coverage	off beampipe cut off $\pm 30 \text{ mm}$
Nevents	457232	29194	19216
Xsec (nb)	1168.3	74.60 nb	49.10 nb

Summary

- **To gain Bhabha X.section > 50 nB**
pushing for $\theta_{\min} < 30$ mRad, favoring vert. direction
- **Precision luminosity, $\Delta fL \sim 10^{-4}$**
minimal multiple scattering effect
- **LumiCal Si wafer**
before Flange, surrounding beampipe
behind Flange, on Y-crotch, extend toward Q-pole
- **Round 28-40 mm beampipe**
Y-crotch window within 40mm is favored
for X.sec and multi. scattering