



# Long-baseline Neutrino Oscillation Results and Machine Learning in NOvA

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## Neutrino

- Neutrinos are elementary particles with little mass and no charge
- Postulated by Pauli in 1930 to reconcile beta decay with energy conservation, first observed in 1950s by Cowan and Reines
- Very abundant, many sources can generate neutrinos
- But very elusive  $\rightarrow$  need gigantic detectors to find them



Nuclear Reactors



Astrophysical (SuperNova/Big Bang)



Cosmic Ray Showers



The Earth (Radioactive Elements)



The Sun



Accelerators
NOvA and DUNE

# Neutrino

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## **Neutrino Oscillation**

- There are 3 flavors of neutrinos:  $v_e$ ,  $v_\mu$ ,  $v_\tau$ , their antiparticles:  $\bar{v}_e$ ,  $\bar{v}_\mu$  and  $\bar{v}_\tau$
- Neutrino oscillation: neutrinos produced in a specific lepton flavor can change to a different flavor during their travel (2015 Nobel Prize)
- The rate of change depends on the neutrino energy E and travel distance (baseline) L



## **Neutrino Oscillation**

The neutrino flavor eigenstates (ν<sub>e</sub>, ν<sub>μ</sub>, ν<sub>τ</sub>) are not mass eigenstates (ν<sub>1</sub>, ν<sub>2</sub>, ν<sub>3</sub>):

$$\begin{vmatrix} \mathbf{v}_{e} \\ \mathbf{v}_{\mu} \\ \mathbf{v}_{\tau} \end{vmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \begin{bmatrix} \mathbf{v}_{1} \\ \mathbf{v}_{2} \\ \mathbf{v}_{3} \end{bmatrix}$$

 $U_{\alpha i}$ : an element of the *PMNS mixing matrix* 

• As neutrinos propagate, the phases of the three mass states  $|v_{i=1,2,3}\rangle$  advance at different rates. Therefore the flavor eigenstates oscillate:

$$\left| \boldsymbol{v}_{\alpha}(L) \right\rangle = U_{\alpha 1} e^{-i \underline{m}_{1}^{2} L/2E} \left| \boldsymbol{v}_{1}(0) \right\rangle + U_{\alpha 2} e^{-i \underline{m}_{2}^{2} L/2E} \left| \boldsymbol{v}_{2}(0) \right\rangle + U_{\alpha 3} e^{-i \underline{m}_{3}^{2} L/2E} \left| \boldsymbol{v}_{3}(0) \right\rangle$$

$$P(\boldsymbol{v}_{\alpha} \rightarrow \boldsymbol{v}_{\beta}) = \left| \left\langle \boldsymbol{v}_{\beta} \left| \boldsymbol{v}_{\alpha}(t) \right\rangle \right|^{2} = \left| \sum U_{\alpha i}^{*} U_{\beta i} e^{-i \underline{m}_{i}^{2} L/2E} \right|^{2}$$

$$\left| \boldsymbol{v}_{\alpha} \rangle, \ \alpha = e, \ \mu \text{ or } \tau \text{-} \text{ flavor eigenstates}$$

$$\left| \boldsymbol{v}_{i} \rangle, \ i = 1, 2, 3 \text{-} \text{ mass eigenstates with a definite mass } m_{i}$$

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• Oscillation probability depends on squared mass differences  $\Delta m_{ij}^2 = m_i^2 - m_j^2$  and PMNS mixing matrix U

$$P(v_{\alpha} \rightarrow v_{\beta}) = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*})\sin^{2}(\Delta m_{i j}^{2}L/4E)$$
 For anti-neutrinos,  
+ 
$$2\sum_{i>j} \operatorname{Im}(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*})\sin(\Delta m_{i j}^{2}L/2E)$$
 (Assuming CPT invariance)

• In the case of CP violation  $P(\overline{v_{\alpha}} \to \overline{v_{\beta}}) = P(v_{\alpha} \to v_{\beta}, U^*) \neq P(v_{\alpha} \to v_{\beta}, U)$ , need a non-zero phase  $\delta_{CP}$  in the mixing matrix U

## **Neutrino Oscillation**

• For the three-flavor case the PMNS matrix is most commonly parameterized by three real mixing angles  $\theta_{12}$ ,  $\theta_{23}$  and  $\theta_{13}$  and a single phase  $\delta_{CP}$ 



Including two independent squared mass differences  $\Delta m_{21}^2 = m_2^2 - m_1^2$  and  $\Delta m_{32}^2 = m_3^2 - m_2^2$ , there are 6 free parameters that determine the neutrino oscillation.

## **Neutrino Oscillation Parameters**

From previous experiments:

- $\sin^2 2\theta_{12}$ ,  $\sin^2 2\theta_{13}$  and  $\sin^2 2\theta_{23}$  have been measured
- $\Delta m_{21}^2$  and  $|\Delta m_{32}^2|$  have been measured, we know that  $m_1$  and  $m_2$  are very close, but difference in  $m_3$  and  $m_{1,2}$  is much larger
- $\Sigma m < 0.3 \text{ eV}$  (total mass of the 3 generations of neutrino)



# **Remaining Fundamental Questions**

CP phase  $\delta_{CP}$ : whether neutrinos and antineutrinos behave the same way in oscillation? Implications for matter-antimatter asymmetry in the universe



# **Remaining Fundamental Questions**

• Mass ordering (hierarchy): sign of  $\Delta m_{31(2)}^2 = m_3^2 - m_{1(2)}^2$ ,  $m_3 > m_{1,2}$  or  $m_{1,2} > m_3$ ? Implications for absolute neutrino masses, grand unified theories and neutrino-less double beta decay searches



Long baseline accelerator neutrino experiments are designed to solve these questions

# **Long-Baseline Accelerator Neutrino Oscillation Experiments**

Use man-made neutrino beam with known flavor to measure oscillation probability as function of neutrino energy



#### **Accelerator Neutrino Beams at Fermilab Near Chicago**



#### **Accelerator Neutrino Beams at Fermilab Near Chicago**



### **Long-Baseline Neutrino Oscillation**

 $\left(\frac{\Delta m_{32}^2 L}{4E}\right)$ 

 $v_{\mu}$  disappearance:

$$P(\nu_{\mu} \rightarrow \nu_{\mu}) \approx 1 - \sin^2 2\theta_{23} \sin^2$$

- Measure ν<sub>μ</sub> (anti-ν<sub>μ</sub>) survival probability with ν<sub>μ</sub> and anti-ν<sub>μ</sub> neutrino beam
  Provide high precision |Δm<sup>2</sup><sub>32</sub>| and sin<sup>2</sup>2θ<sub>23</sub>

$$P(v_{\alpha} \rightarrow v_{\beta}) = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*})\sin^{2}(\Delta m_{i j}^{2}L/4E)$$
 For anti-neutrinos,  

$$P(\overline{v_{\alpha}} \rightarrow \overline{v_{\beta}}) = P(v_{\alpha} \rightarrow v_{\beta}, U^{*})$$

$$+ 2\sum_{i>j} \operatorname{Im}(U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}U_{\beta j}^{*})\sin(\Delta m_{i j}^{2}L/2E)$$
 (Assuming CPT invariance)  

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos\theta_{23} & \sin\theta_{23} \\ 0 & -\sin\theta_{23} & \cos\theta_{23} \end{pmatrix} \begin{pmatrix} \cos\theta_{13} & 0 & \sin\theta_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin\theta_{13}e^{i\delta_{CP}} & 0 & \cos\theta_{13} \end{pmatrix} \begin{pmatrix} \cos\theta_{12} & \sin\theta_{12} & 0 \\ -\sin\theta_{12} & \cos\theta_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

## **Long-Baseline Neutrino Oscillation**

4E

$$v_{\mu}$$
 disappearance:  
 $P(v_{\mu} \rightarrow v_{\mu}) \approx 1 - \sin^2 2\theta_{23} \sin^2 \left( \frac{\Delta m}{4} \right)$ 

- Measure  $v_{\mu}$  (anti- $v_{\mu}$ ) survival probability with  $v_{\mu}$  and anti- $v_{\mu}$  neutrino beam
- Provide high precision  $|\Delta m^2_{32}|$  and  $\sin^2 2\theta_{23}$



$$P(\nu_{\mu} \rightarrow \nu_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \cos \Delta - 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = +G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad C_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

- Measure  $v_e$  (anti- $v_e$ ) appearance probability with  $v_{\mu}$  and anti- $v_{\mu}$  neutrino beam
- Determine mass hierarchy,  $\delta_{CP}$  and octant of  $\theta_{23}$

#### $v_e$ appearance

$$P(v_{\mu} \rightarrow v_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \cos \Delta - 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = +G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad C_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

Depends on  $\theta_{13}$ 

$$P(\nu_{\mu} \rightarrow \nu_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \cos \Delta - 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = +G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad G_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

Depends on  $\theta_{13}$ Depends on  $\delta_{CP}$ 

$$P(v_{\mu} \rightarrow v_{e}) \approx \sin^{2} 2\theta_{13} \frac{\sin^{2} \theta_{23}}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \cos \Delta$$
$$2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \cos \Delta$$

$$- 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = +G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad G_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

Depends on  $\theta_{13}$ Depends on  $\delta_{CP}$ Depends on octant of  $\theta_{23}$ 

$$P(\nu_{\mu} \rightarrow \nu_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \cos \Delta$$
$$- 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2}$$

$$\Delta = \frac{\Delta m_{31}^2 L}{4E}$$

A=+
$$G_f N_e \frac{L}{\sqrt{2}\Delta}$$

 $G_f$ =Fermi constant  $N_e$  =electron density

Matter effect is the correction to neutrino effective masses, when they travel through matter and scatter on electrons

Depends on  $\Delta m_{31}^2$ The difference between normal hierarchy ( $\Delta > 0$ ) and inverted hierarchy ( $\Delta < 0$ ) is enlarged by matter effect (A) Matter effect increases with travel distance L

#### $v_e$ appearance

$$P(\overline{\nu_{\mu}} \rightarrow \overline{\nu_{e}}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos(-\delta_{CP}) \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \cos \Delta - 2\alpha \sin \theta_{13} \sin(-\delta_{CP}) \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin(A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = -G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad G_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

For anti-neutrinos, flip signs on  $\delta_{CP}$  and matter effect A

$$P(v_{\mu} \rightarrow v_{e}) \approx \sin^{2} 2\theta_{13} \sin^{2} \theta_{23} \frac{\sin^{2} (A-1)\Delta}{(A-1)^{2}} + 2\alpha \sin \theta_{13} \cos \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \cos \Delta - 2\alpha \sin \theta_{13} \sin \delta_{CP} \sin 2\theta_{12} \sin 2\theta_{23} \frac{\sin A\Delta}{A} \frac{\sin (A-1)\Delta}{(A-1)} \sin \Delta$$

$$\alpha = \frac{\Delta m_{21}^2}{\Delta m_{31}^2} \qquad \Delta = \frac{\Delta m_{31}^2 L}{4E} \qquad A = +G_f N_e \frac{L}{\sqrt{2\Delta}} \qquad C_f = \text{Fermi constant} \\ N_e = \text{electron density}$$

- Measure  $\nu_e$  (anti- $\nu_e)$  appearance probability with  $\nu_\mu$  and anti- $\nu_\mu$  neutrino beam
- Determine mass ordering,  $\delta_{CP}$  and octant of  $\theta_{23}$
- $\sin^2 2\theta_{13}$  measured by reactor experiments
- $|\Delta m_{23}^2|$  and  $\sin^2 2\theta_{23}$  constraint by  $v_{\mu}$  disappearance
- $P(\nu_{\mu} \rightarrow \nu_{e})$  difference between  $\Delta m_{31}^{2} > 0$  and  $\Delta m_{31}^{2} < 0$  enlarged by matter effect ( $\propto L$ ) Matter effect is the correction to neutrino effective masses, when they travel through matter and scatter on electrons

# $v_e$ appearance - $v_e$ vs anti- $v_e$ events

- Inverted hierarchy gives a slight suppression in both.
- CP violation causes opposite effects in neutrinos and antineutrinos.
- Matter effects also produce
   opposite effects in neutrinos and antineutrinos.
- 4. The octant of  $\theta_{23}$  causes either a **suppression** or **enhancement**.



# $v_e$ appearance - $v_e$ vs anti- $v_e$ events



# **Neutrino Detection (~MeV)**

- Inverse beta decay (IBD) Cowan-Reines Experiment (first observation of neutrinos), DayaBay (θ<sub>13</sub>), JUNO (mass hierarchy), etc
- Neutrino capture on radioactive nuclei (Davis experiment in South Dakota 1970-1994, first to detect and count solar neutrinos, discrepancy in results created the solar neutrino problem → neutrino oscillation)
- Coherent scattering (recently developed, high cross-section, low energy signal)

Detector (inverse beta decay)

Source (beta decay)  $n \rightarrow p^+ + e^- + \bar{v}_e$ 



Nuclear Reactors





DayaBay: liquid scintillator, ~8x20 tons, first measured  $\theta_{13}$  in 2012

 $JUNO \sim 20 kt$ 

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1995 Cd capture neutrons, ~10 tons

## **Neutrino Detection (~GeV)**

- Charged-Current interactions are the "signal" events that allow the neutrino flavor to be identified, via identification of the charged lepton flavor
- Due to the small  $v_{\mu} \rightarrow v_{e}$  probability (~5%), background processes can greatly confuse  $v_{e}$  appearance measurements
- For example, Neutral Current (NC  $\pi^0$ ) events where a  $\pi^0$  is produced can fake CC  $v_e$



"appearance" signal

"appearance" background

## **Charged-Current Signal - Interaction Modes**





2 particle-2 hole (2p-2h) effect: dominated by Meson Exchange Current (MEC), Interactions with more than one nucleon contribute

# **Charged-Current Signal- Cross Sections**

- Accelerator neutrino oscillation experiments in the 0.1-10GeV transition region
- Multiple types of interactions with complicated final states and topology
- Requirements:
  - High performance detector
  - Excellent Event reconstruction
  - Well understood neutrino flux and interaction models







## **Cherenkov Detectors**

- Particles traversing medium faster than light (v > c/n) emit Cherenkov light at a characteristic angle.
- Cherenkov light collected and produces signals on PhotoMultiplier Tubes (PMTs)
  - Muons: straight trajectories lead to crisp rings
  - Electrons: showering and multiple scattering produce fuzzy rings
  - $\pi^0$ s: decay into two gammas, which each appear as electron-like rings



# **Scintillator Tracking Detectors**

- Use scintillator distributed throughout detector that produces light when particles pass through
- Collect scintillator light via fiber optic readout that connects to a APD
- Reconstruct event in 3D by merging information from alternate coordinate views
- Low-Z and low-density, good for  $e^-$  vs  $\pi^0$  separation



#### Neutrino Interaction in scintillator detector (NOvA)



The muon is a long minimum ionizing particle, the electron ionizes in the first few planes then starts to shower and the photon is a shower with a gap in the first few planes.

#### Liquid Argon Time Projection Chamber (LArTPC)

- Liquid Argon Time Projection Chamber (LArTPC) is promising for the next generation of neutrino experiments
  - Image quality of a bubble-chamber, improving sensitivity by better background rejection and resolution
  - Scalable to multi-kiloton detectors
  - Not infinitely expensive
  - Fast electronic readout





**ProtoDUNE-SP** 

1 GeV Pion Interaction (Absorption  $\rightarrow$  2p)

## NuMI Off-Axis v<sub>e</sub> Appearance Experiment (NOvA)



- Muon neutrino beam at Fermilab near Chicago
- Longest baseline in operation (810 km), large matter effect, sensitive to mass ordering
- Far/Near detector sited 14 mrad off-axis, narrow-band beam around oscillation maximum

#### **NuMI Off-Axis Beam**

Charge select pions to get 96% (83%) pure muon-neutrino, (anti-muon-neutrino) beam.



### **NuMI Off-Axis Beam**



- NOvA detectors are sited 14 mrad off the NuMI beam axis
- Beam v are produced by  $\pi$  and K decays. Neutrino energy depends on the decay angle and  $\pi/K$  energy
- The off-axis angle provides a narrow 2-GeV v energy spectrum around the  $v_{\mu} \rightarrow v_{e}$  oscillation maximum
- Reduces beam NC and  $\nu_e$ CC backgrounds while maintaining high  $\nu_\mu$  flux at 2 GeV for the oscillation signal



#### **Neutrino Beam Performance**


# **NOvA Detectors**

3.87 cm

#### Far Detector (FD):

- 14-kton, fine-grained
- 344k detector cells
- 0.3-kton functionally identical Near Detector (ND), ~20k cells

Far Detector, 14 kt, 60 m x 15.6 m x 15.6 m

> Near Detector 14.3mx4.1mx4.1m



- Each cell: filled with liquid scintillator, has wavelength-shifting fiber (WLS) routed to Avalanche Photodiode (APD)
- Cells arranged in planes, assembled in alternating vertical and horizontal directions
   → 3-D information of neutrino interactions

6.0 cm

To APD Readout

Scintillation Light

Particle Trajectory

Plane of vertical cells

Plane of horizontal cells

Waveshifting

Fiber Loop

## **NOvA Detectors**

#### Far Detector (FD):



## **NOvA Detectors**





### **Outfitted Far Detector**





# **Oscillation Analysis Process**

Measure neutrino flavor change vs. energy over a long travel distance to determine oscillation parameters:

- Identify  $v_e$  and  $v_{\mu}$  charge current events from cosmic rays and beam backgrounds (PID)
- Reconstruct neutrino energy and other kinematic variables
- Observe differences between data and MC simulation at Near Detector (ND), extrapolate them to Far Detector (FD) to correct FD MC
- Infer oscillation parameters by fitting oscillation-weighted FD MC to FD data

+ Tune interaction models based on ND data and external data, mitigating uncertainties on neutrino flux, cross sections, and detector response

## **Neutrino Interaction Tuning**

- Upgrade to GENIE 3.0.6 in 2020 (more models)
- Chose the most "theory-driven" available set of models along with GENIE's re-tune of some parameters
- Custom tuning for both central values and systematics:
  - Final State Interactions: external  $\pi$ -scattering data
  - Meson Exchange Current (MEC, Multi-nucleon interaction, 2p2h): amount tuned in 2D space to match NOvA ND data  $(q_0 = E_v - E_\mu, |q| = |p_v - p_\mu|)$



T. Katori, AIP Conf. Proc. 1663, 030001 (2015)]

Process	Model	Reference
Quasielastic	Valencia plus Z- expansion form factor	A. Meyer, M. Betancourt, R. Gran, R. Hill, Phys. Rev. D 93 (2016)
MEC	Valencia <mark>w/ custom tune</mark>	R. Gran, J. Nieves, F. Sanchez, M. Vicente Vacas, Phys. Rev. D88 (2013)
Resonance	Berger-Sehgal	Ch. Berger, L. M. Sehgal, Phys. Rev. D76 (2007)
DIS	Bodek-Yang	A. Bodek and U. K. Yang, NUINT02, Irvine, CA (2003)
Final State Interactions	hN w/ custom tune	S. Dytman, Acta Physica Polonica B 40 (2009)

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T. Katori, AIP Conf. Proc. 1663, 030001 (2015)]

#### **NOvA Preliminary**





### **Event clustering**



- Because NOvA is on surface, hits in a trigger window are a combination of cosmic and beam events.
- First step in reconstruction is to cluster hits by space-time coincidence to separate neutrino hits and Jianming Bian - UCI 43

### **Event clustering**



Event clusters that contain neutrino interactions can be correctly selected in the neutrino spill timing window
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## **NOvA Event Topologies**



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### **Deep-Learning based neutrino classifier (PID)**

- CVN: a convolutional neural network (CNN), based on modern image recognition technology
- Extract features directly from pixel maps
- Statistical power equivalent to 30% more exposure than previous neutrino classifiers *CVN output in the far detector MC*



### **Event Reconstruction**



<u>Vertexing</u>: Find lines of energy depositions with Hough transform. Then determine the vertex that all lines converge to <u>Shower Clustering</u>: Based on the vertex and the lines, showers are reconstructed by angular clustering

**Tracking:** Trace particle trajectories with **Kalman filter** tracker

### **NOvA Events**



### Reconstruction



## **Energy Reconstruction and Extrapolation**



- Signal neutrino energy is the sum of muon/electron and hadronic energy.
- Observe data-MC differences in neutrino energy spectrum at the ND, extrapolate them to modify the FD MC prediction (significantly reduce systematics)
- Systematic uncertainties determined in ND also extrapolated to FD

## **Energy reconstruction and Extrapolation**





- "Functionally identical" is not "identical"
  the ND and FD are very different sizes.
- Containment limits the range of lepton angles more in the ND than in the FD.
  - An avenue for cross-section mismodeling to not cancel between detectors.
- Can be mitigated by extrapolating in bins of transverse momentum, p<sub>t</sub>.
  - Component of the *lepton's* momentum transverse to the v-beam direction.
  - Split the ND sample into 3 bins of  $p_{\nu}$  extrapolate each separately to the FD.

## **Energy reconstruction and Extrapolation**



1. ND Data Reco  $E_v$  2. ND Reco-to-True  $E_v$  Weighting 3. ND True  $E_v$  4. Far / Near Ratio 5. Oscillations Probability 6. FD True Ev 7. FD True-to-Reco  $E_v$  Weighting 8. Predicted FD Reco  $E_v$ 

- The extrapolation for  $v_{\mu}$  disappearance is divided into 4 bins in hadronic energy fraction called quartiles, each bin
- For  $v_e$  appearance the ND  $v_{\mu}$  CC data and intrinsic beam  $v_e$  background are extrapolated separately

## **Energy reconstruction and Extrapolation**



- Signal neutrino energy is the sum of muon/electron and hadronic energy.
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# $v_{\mu}$ and $\bar{v}_{\mu}$ Data at Far Detector

- FD selection:
  - Additional Boosted Decision Tree (BDT) to reduce cosmic backgrounds



Neutrino beam:

- Observe 211 events
- Total bkg prediction: 9.3 events



Anti-Neutrino beam:

- Observe 105 events
- Total bkg prediction: 2.8 events 54

## $v_{\rho}$ and $\bar{v}_{e}$ Data at Far Detector



- ND data split into low and high PID ranges and extrapolate to FD
- FD selection: Add a region close to detector top with tighter cosmic ray cuts to count more signal events

Neutrino beam:

- Observe 82  $v_e$  like events
- Total bkg prediction: 26.8:1.0 wrong sign, 22.7 beam bkg, 3.1 cosmic

Anti-Neutrino beam:

- Observe 33  $\bar{\nu}_e$  like events
- Total bkg prediction: 14.0: 2.3 wrong sign, 10.2 beam bkg, 1.6 cosmic

#### >4 $\sigma \bar{\nu}_{\rho}$ appearance

Extract oscillation parameters by fitting oscillation-weighted FD MC to FD data

## **Oscillation parameter fit**



- All results come from a joint fit to neutrinos + antineutrinos,  $v_e + v_{\mu\nu}$  reactorconstrained sin<sup>2</sup>2 $\theta_{13} = 0.085 \pm 0.003$ .
- We perform a frequentist analysis and use the Feldman-Cousins method to ensure proper coverage in all contours and intervals.
- We perform blind analyses, finalizing all analysis elements before looking at the FD data.

### **Joint Appearance and Disappearance**



- Use frequentist analysis Feldman-Cousins method to infer oscillation parameters
- $\sin^2\theta_{13} = 0.085 + 0.005$  from PDG avg. of reactor data
  - Best fit:
    - Normal Mass Hierarchy
    - $\sin^2 \theta_{23} = 0.57 + 0.03 0.04 (\text{UO})$
    - $\Delta m_{32}^2 = (2.41 + 0.07 0.07) * 10^{-3} \text{ eV}^2$
- Disfavor maximal mixing ( $\theta_{23}=45^\circ$ ) at 1.1  $\sigma$
- Disfavor lower octant ( $\theta_{23} < 45^{\circ}$ ) at 1.2  $\sigma$



### **Joint Appearance and Disappearance**



- Best fit:
  - Normal Mass Hierarchy (m<sub>3</sub>>m<sub>1,2</sub>)
  - $\quad \delta_{CP} = 0.82 \ \pi$
  - $\sin^2 \theta_{23} = 0.57 + 0.03 0.04$ (UO)
  - $\Delta m_{32}^2 = (2.41 + 0.07 0.07) * 10^{-3} \text{ eV}^2$
- Exclude  $\delta_{CP} = \pi/2$  in IH at  $> 3\sigma$
- Disfavor (NH,  $\delta_{CP}=3\pi/2$ ) at  $\sim 2\sigma$
- Consistent with all  $\delta_{CP}$  values in Norma Mass Ordering at  $< 1.1\sigma$
- Disfavor Inverted Mass Ordering at 1.0σ





### **Joint Appearance and Disappearance**



- We see no strong asymmetry between the appearance of  $v_e$  and  $\bar{v}_e$ .
- Strongly disfavor "extreme" *combinations*, but can be consistent with any  $\delta$ , hierarchy, or octant if probed individually.

Exclude IH $\delta = \pi/2$ at >3 $\sigma$
Disfavor NH $\delta = 3\pi/2$ at $\sim 2\sigma$

Prefer				
Normal Hierarchy at	1.0σ			
Upper Octant at	1.2σ			
Non-maximal Mixing at	1.1σ			

# **Compare with Other Experiments**

NOvA's allowed 90% C.L. regions are compatible to other experiments



Agreement across many precision measurements about values of "atmospheric" parameters



- Apparent tension in allowed values of  $\delta_{CP}$
- NOvA & T2K are working on a fully selfconsistent joint fit (including systs)

# **NOvA Results Summary**



- NOvA is running through 2025, test beam program and potential accelerator improvement to enhance ultimate reach
- Optimistically, if  $\delta_{CP}=3\pi/2$ , 4-5  $\sigma$  sensitivity to Mass Ordering by 2025
- >=3 $\sigma$  sensitivity to Mass Ordering for 30-50% of  $\delta_{CP}$  values (depends on  $\theta_{23}$  and true ordering) <sup>61</sup>

# Artificial Neural Network (ANN)

- Artificial Neural Network (ANN) provides a general framework for estimating non-linear functional mapping between a set of input variables  $x(x_1, x_2, ..., x_N)$  and a set of output variables without requiring a prior mathematical description of how the output formally depends on the inputs.
- All layers in a traditional ANN are fully connected, meaning that the inputs of the activation function in each node are the weighted sums of the outputs of all nodes in the previous layers.
- The weights and biases are determined by training ANN with large simulated data samples in which true outputs values are known (supervised learning).



$$x_j^k = A(w_{0j}^k + \sum_{i=1}^{M_{k-1}} w_{ij}^k \cdot x_i^{k-1})$$

• Traditional ANNs can not use raw data (e.g., the pixels of a image) directly as inputs because of the computational complexity and over fitting problems, encountered when the number of layers increases.

# **Convolutional Neural Network**

- CNNs are convenient for taking images as inputs, as they use translationally invariant filters to look for features
- CNNs can be utilized in 2 ways:
- 1. Classification (Particle ID, Event ID): Output layer will have a sigmoid activation function, which outputs a number between 0 and 1, or softmax, it's generalization to an arbitrary number of classes
- 2. Regression (Particle Momentum/Energy, Event Energy, Vertex): Output layer has a linear activation function



CNNs take raw pixel inputs, using all detector information with acceptable computing cost

Traditional artificial neural network

Convolutional neural network

## **Convolutional Neural Network**



## **Convolutional Neural Network**



phys.org



antineutrino oscillation

phys.org

1. Design neural network architecture

2. Provide many simulated neutrino examples to train neural network

phys.org

3. Parameters in neural network trained to give event identification, neutrino energy, interaction position etc.



## **Input Images - NOvA**

- NOvA detector cells arranged in planes, assembled in alternating X and Y directions
- Produce a pair of pixel maps (Cell Number vs. Plane Number) for the X and Y view of each interaction
- Input images are 151 cells by 141 planes





# **CNN based Event Classifier (CVN)**



Classify neutrino events using two tower network, **Convolutional Visual Network**, based on googlenet.

Each view of the event is examined separately for most of feature extraction.

NOvA was the first experiment to apply CNNs to a HEP result in its 2016 analysis.

Yielded an effective **30%** increase in exposure.

Aurisano et al., "A Convolutional Neural Network Neutrino Event Classifier", JINST 11, P09001 (2016).

# **CNN based Event Classifier (CVN)**



### **Example Data Check: MRE**





#### Muon Removed - Electron Added:

Select a muon neutrino interaction.

Remove the muon hits and replace with a simulated electron.

	Pre Selection	Full Selection	Efficiency
Data Events	486083	316009	0.6501
MC Events	511287	341119	0.6672

### **Particle Classification**



Single particles are currently separated using geometric reconstruction methods.

Classify particles using both views of the **particle** and both views of the entire **event**.

This shows the network **contextual information** about single particles.



Phys.Rev.D 100 (2019) 7, 073005

### **Particle Classification**



### Example Data Check: π<sup>0</sup> Mass Peak



 $\pi^0$  mass reconstructed using invariant mass of pairs of photons identified using the single particle classifier.

Shows a 60% reduction in backgrounds over previous techniques.
# **Regression CNNs for Energy Estimation**



Phys. Rev. D 99, no. 1, 012011 (2019) doi:10.1103/PhysRevD.99.012011

Cell

# $v_{e}$ Energy Performance

- Energy regression results for  $v_e$  CC results are shown here
- Calorimetric method is based on adding up calorimetric energy per cell and applying an overall factor
- The kinematic method is based on a fit using electromagnetic and hadronic clustering:



Also trained for electron energy, hadronic energy,  $\nu_{\mu}$  Energy, etc





• The CNN resolution keeps the edge over calorimetric and kinematic based energy estimators from 1 GeV and up



## $v_{e}$ Energy Performance



- CNN based method shows good stability over different interaction types
- This shows robustness a CNN model can provide with a large degrees of freedom



 $v_{e}$  Systematics

- To quantify systematic uncertainties arising from simulation, we vary cross section uncertainties
- CNN event energy estimator is also very robust to cross section systematics, as well as the better performance



**Cluster** and **classify** objects simultaneously using **instance aware semantic segmentation**.

Use machine learning to reconstruct an event **hit by hit**.

Three outputs:

- 1. Bounds
- 2. ID Score
- 3. Clusters



Using an implementation of Mask R-CNN: K. He, G. Gkioxari, P. Dollar, and R. Girshick. Mask R-CNN. arXiv:1703.06870, 2017.

**Bounds** - Look for individual particles within the event and construct bounding boxes containing each.



**ID Score** - Use a softmax function to classify the particle contained within each box.



**Clusters** - Group together hits within each box to make clusters for each particle.





# Transformer

- Recently developed for Natural Language Processing in CS
- Deals with variable number of inputs to combine particle level information
- Ideal to combine kinematics/ID of final state particles, make each step in ML/AI based reconstruction checkable and explainable



# **Comparing Networks**



A receiver operating characteristic (ROC) curve shows the network performance for one event class vs all others. The transformer's ROC curves for event predictions are nearly identical to those of NOvA's CNN.

# **Oscillation parameter fit: Confidence Interval**

• Typically, using Likelihood Ratio Test (LRT) to estimate confidence interval

$$\Delta \chi^2 = -2 \log \frac{L(\theta_0)}{\arg \max_{\theta} L(\theta)}$$

• In asymptotic case (large sample, etc), test statistic  $\Delta \chi^2$  following a  $\chi^2$  distribution (Wilks Theorem), so confidence interval can be directly calculated from  $\Delta \chi^2$ 



**Table 38.2:** Values of  $\Delta \chi^2$  or  $2\Delta \ln L$  corresponding to a coverage probability  $1 - \alpha$  in the large data sample limit, for joint estimation of *m* parameters.

$(1 - \alpha)$ (%)		m = 1	m=2	m = 3
1σ	68.27	1.00	2.30	3.53
	90.	2.71	4.61	6.25
	95.	3.84	5.99	7.82
2σ	95.45	4.00	6.18	8.03
	99.	6.63	9.21	11.34
<u>3σ</u>	99.73	9.00	11.83	14.16

#### From the PDG Review on Statistics

Figure 40.4: Illustration of a symmetric 90% confidence interval (unshaded) for a Gaussiandistributed measurement of a single quantity. Integrated probabilities, defined by  $\alpha = 0.1$ , are as shown.

# Feldman-Cousins (FC) Method

- Due to the small sample size in neutrino data and physical boundaries on the oscillation parameters, the asymptotic distribution is unreliable
- Explicitly simulate distribution using lots of pseudo-experiments
- Find p-value associated with for each point in parameter space
- In practice, FC conducts a grid-search over the entire parameter space with many toy Monte-Carlo (MC)



#### **Gaussian Process to Enhance Oscillation Parameter Inference**

- The Feldman-Cousins (FC) approach is a frequentist method widely used by neutrino experiments for oscillation parameter inference.
- FC search a grid over the entire parameter space with many toy simulated events to integrate and obtain p-values → very time- and computing resource-consuming.
- A Gaussian Process (GP) is a special case of Bayesian learning that can use existing data points to predict the values for unseen points with posterior mean and posterior standard deviation.
- Use GP to approximate the FC P-value surface non-parametrically based on a small fraction of grid points and toy simulated events





- Oscillation contours produced by GP 10 times faster than the standard FC algorithm while keeping the accuracy at 99%.
- GP algorithm implemented in NOvA's software framework, working on parallelize the algorithm to fit NOvA oscillation parameters at DOE's National Energy Research Scientific Computing Center (NERSC)

# Machine Learning to Boost Neutrino Oscillation Measurements

Measure neutrino flavor change vs. energy in over a long travel distance to determine oscillation parameters:

- Identify  $v_e$  and  $v_{\mu}$  charge current events from cosmic rays and beam backgrounds (PID)
- Reconstruct neutrino energy and other kinematic variables
- Observe differences between data and MC simulation at Near Detector (ND), extrapolate them to Far Detector (FD) to correct FD MC
- Infer oscillation parameters by fitting oscillation-weighted FD MC to FD data

#### **BLUE: Apply machine learning**



# **Neutrino Oscillation**

- Neutrino oscillate because their flavor (interaction) eigenstates ( $v_e$ ,  $v_\mu$ ,  $v_\tau$ ) are not mass eigenstates ( $v_1$ ,  $v_2$ ,  $v_3$ )
- As neutrinos propagate, the phases of the three mass states  $|v_{1,2,3}\rangle$  advance at different rates. Therefore the flavor eigenstates oscillate.

$$3-\text{flavor standard}_{\text{model neutrinos}} \begin{bmatrix} v_e \\ v_\mu \\ v_\tau \end{bmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

$$PMNS \text{ matrix}_{\text{Parameterized by mixing angles } \theta_{12}, \theta_{23} \text{ and } \theta_{13} \text{ and phase } \delta_{CP}$$

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta_{23} & \sin \theta_{23} \\ 0 & -\sin \theta_{23} & \cos \theta_{23} \end{pmatrix} \begin{pmatrix} \cos \theta_{13} & 0 & \sin \theta_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix} \begin{pmatrix} \cos \theta_{12} & \sin \theta_{12} & 0 \\ -\sin \theta_{13} e^{i\delta_{CP}} & 0 & \cos \theta_{13} \end{pmatrix}$$

 $V_{\tau}$   $V_{3}$ 

Including two squared mass differences  $\Delta m_{21}^2 = m_2^2 - m_1^2$  and  $\Delta m_{32}^2 = m_3^2 - m_2^2$ , there are 6 free parameters that determine neutrino oscillation probabilities.

# Fermi Constant G<sub>f</sub>



Fermi's interaction showing the 4-point fermion vector current, coupled under Fermi's Coupling Constant  $G_{\rm F}$ . Fermi's Theory was the first theoretical effort in describing nuclear decay rates for  $\beta$  decay.

The most precise experimental determination of the Fermi constant comes from measurements of the muon <u>lifetime</u>, which is inversely proportional to the square of  $G_{\rm F}$  (when neglecting the muon mass against the mass of the W boson).<sup>[19]</sup> In modern terms:<sup>[3][20]</sup>

$$G_{
m F}^{0} = rac{G_{
m F}}{(\hbar c)^{3}} = rac{\sqrt{2}}{8} rac{g^{2}}{M_{
m W}^{2} c^{4}} = 1.1663787(6) imes 10^{-5} ~{
m GeV^{-2}} pprox 4.5437957 imes 10^{14} ~{
m J^{-2}}$$

Here g is the coupling constant of the weak interaction, and  $M_W$  is the mass of the W boson, which mediates the decay in question. In the Standard Model, the Fermi constant is related to the Higgs vacuum expectation value

$$v = \left(\sqrt{2}\,G_{
m F}^0
ight)^{-1/2} \simeq 246.22~{
m GeV}.^{ extsf{21}}$$

More directly, approximately (tree level for the standard model),

$$G_{
m F}^0 \simeq rac{\pi lpha}{\sqrt{2} \ M_{
m W}^2 (1-M_{
m W}^2/M_Z^2)}.$$

This can be further simplified in terms of the Weinberg angle using the relation between the W and Z Bosons with  $M_{\rm Z}=rac{M_{
m W}}{\cos heta_{
m W}}$ , so that

$$G_{
m F}^0 \simeq rac{\pi lpha}{\sqrt{2}~M_{
m Z}^2\cos^2 heta_{
m W}\sin^2 heta_{
m W}}$$

#### Accelerator Neutrino Beams at Fermilab Near Chicago



# **Neutrino Oscillation**

- There are 3 flavors of neutrinos:  $v_e$ ,  $v_\mu$ ,  $v_\tau$ , their antiparticles:  $\bar{v}_e$ ,  $\bar{v}_\mu$  and  $\bar{v}_\tau$
- Neutrino oscillation: a neutrino created with a certain flavor has a probability of being detected later with a different flavor during their travel



# **Neutrino Energy**

• Second task: Reconstruct Neutrino Energy



## $v_{\mu}$ Near Detector (ND) Spectrum

- Select  $v_{\mu}$  ( $\bar{v}_{\mu}$ ) CC in ND from neutrino (antineutrino) beam with CVN
- $E_{\nu} = E_{\mu} + E_{had}$ , data split in 4 equal energy quartiles based on  $E_{had}/E_{\nu}$ , resolution varies from 5.8% (5.5%) to 11.7% (10.8%) for neutrino (antineutrino) beam.
- Normalize ND simulation to data in each  $E_v$  bin, then extrapolate the 4 quantiles to FD





### **Joint Appearance and Disappearance**

 $v_e/\overline{v}_e$  appearance event counts and best fit from  $v_e/\overline{v}_e + v_\mu/\overline{v}_\mu$  combined analysis



- Disfavor maximal mixing ( $\theta_{23}$ =45°) at 1.1  $\sigma$
- Disfavor lower octant ( $\theta_{23} < 45^{\circ}$ ) at 1.2  $\sigma$
- Consistent with all  $\delta_{CP}$  values in NH at  $< 1.1\sigma$
- Exclude  $\delta_{CP} = \pi/2$  in IH at >  $3\sigma$
- Disfavor (NH,  $\delta_{CP}=3\pi/2$ ) at  $\sim 2\sigma$
- Disfavor inverted mass ordering at  $1.0\sigma$

# **NOvA Detectors**

- Segmented liquid scintillator detectors.
  - Allows both 3D tracking and calorimetry
- Good time resolution (few ns) and spatial resolution (few cm)
  - Allows clear separation of individual interactions



• Optimized for electron showers: ~6 samples per  $X_0$  and ~60% active



### **Selection: Cosmic Rejection**



- **Cosmic rejection** is critical at the Far Detector.
  - 11 billion cosmic rays/day in the Far Detector on the surface.
- We require:
  - Vertices in the fiducial volume, events contained in the detector.
  - Pass a BDT tuned to reject cosmics.
- For the v<sub>e</sub> sample, we add a second "peripheral" sample which contains high-confidence v<sub>e</sub> events close to the detector walls.

t-SNE

#### t-Distributed Stochastic Neighbor Embedding



#### t-SNE

#### Example Event Topologies





### $v_{e}$ CC Electron Energy



- An electron energy estimator was also developed
- The input images for this estimator are only hits from the electron part of v<sub>e</sub> CC events
- The CNN based estimator sees an improvement over the traditional method based on summing up calibrated hit energy

# $v_{\mu}$ CC Events

- We can also apply regression CNNs to v<sub>u</sub> CC events
- Muon tracks are long, so the v<sub>e</sub> pixelmap size would not contain the full event
- We can specialize to estimating the hadronic part of energy, then use:
- $E(v_{\mu}) = E_{\mu} + E_{hadronic}$
- Then we combine our CNN hadronic energy estimator with the traditional, length based muon energy estimator to estimate v<sub>µ</sub> event energy





Here is a simulated  $v_{\mu}$  CC event, with a long muon track and hadronic shower

### Hadronic Energy

- Here we show the resolution of the hadronic energy
- We apply a weighting to the hadronic energy spectrum
- The traditional method is found by adding up visible calorimetric energy from the hadron, then applying a calibration factor





# $v_{\mu}$ Energy

- We estimate the  $v_{\mu}$  event energy with:
- $E(v_{\mu}) = E_{\mu} + E_{hadronic}$
- Traditional method of muon energy is based on length of muon prong
- We do this using both the traditional and CNN reconstructed hadron energy







- Here we look at Mean and RMS of  $v_{\mu}$  energy resolution over ranges of true  $v_{\mu}$  energy
- The CNN has a smaller bias at lower energies
- The CNN's RMS does about as well or better everywhere







- Energy bars here are systematic uncertainties
- CNN is more robust to cross section systematics from 1 GeV onward