



A new interpretation for the $D_{s2}^*(2573)$, the prediction of novel exotic charmed mesons and narrow N^* , Λ^* resonances around 4.3 GeV

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Introduction

- Heavy quark symmetry framework (HQS): with $I = 1$ two doublets of D_s states are generated:
 - light quark $\rightarrow j_l = 3/2$, total angular momentum:
 $J^P = 1^+, 2^+$
 - light quark $\rightarrow j_l = 1/2$, total angular momentum:
 $J^P = 0^+, 1^+$
- The doublet with $J^P = 1^+, 2^+$ is identified with the $D_{s1}(2536)$ and $D_{s2}(2573)$ in HQS
- However, the doublet with $J^P = 0^+, 1^+$ and very broad states cannot be identified with the narrow states discovered: the $D_{s0}^*(2317)$ and the $D_{s1}(2460)$ (100 MeV lower in mass than the predictions)
- $D_{s0}^*(2317)$: strong s-wave Coupling to DK , E. van Beveren and G. Rupp, PRL (2003); Couple Channels: $D_{s0}^*(2317) \sim DK$, D. Gamermann, E. Oset, D. Strottmann, M. J. Vicente Vacas, PRD (2007); $D_{s1}(2460) \sim KD^*(\eta D_s^*)$, $D_{s1}(2536) \sim DK^*(D_s\omega)$ D. Gamermann and E. Oset, EPJA (2007)



The VV interaction Bando, Kugo, Yamawaki

$$\mathcal{L}_{III} = -\frac{1}{4} \langle V_{\mu\nu} V^{\mu\nu} \rangle$$

$$\mathcal{L}_{III}^{(3V)} = ig \langle (\partial_\mu V_\nu - \partial_\nu V_\mu) V^\mu V^\nu \rangle$$

$$\mathcal{L}_{III}^{(c)} = \frac{g^2}{2} \langle V_\mu V_\nu V^\mu V^\nu - V_\nu V_\mu V^\mu V^\nu \rangle$$

$V_{\mu\nu}, g$

$$V_{\mu\nu} = \partial_\mu V_\nu - \partial_\nu V_\mu - ig[V_\mu, V_\nu]$$

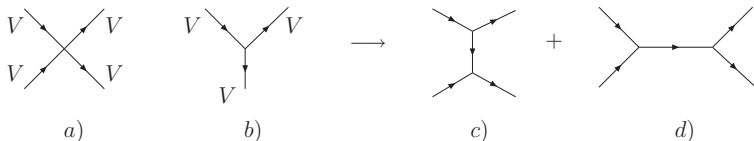
$$g = \frac{M_V}{2f}$$

V_μ

$$\begin{pmatrix} \frac{\rho^0}{\sqrt{2}} + \frac{\omega}{\sqrt{2}} & \rho^+ & K^{*+} & \bar{D}^{*0} \\ \rho^- & -\frac{\rho^0}{\sqrt{2}} + \frac{\omega}{\sqrt{2}} & K^{*0} & D^{*-} \\ K^{*-} & \bar{K}^{*0} & \phi & D_s^{*-} \\ D^{*0} & D^{*+} & D_s^{*+} & J/\psi \end{pmatrix}_\mu$$



The VV interaction



- The VV interaction comes from 1. a) and c)
- 1. d):
 - p-wave **repulsive** for equal masses (R. Molina, 2008)
 - minor component of s-wave for different masses (L. S. Geng, 2009)



Formalism: The VV interaction

Approximation

$$\epsilon_1^\mu = (0, 1, 0, 0)$$

$$\epsilon_2^\mu = (0, 0, 1, 0)$$

$$\epsilon_3^\mu = (|\vec{k}|, 0, 0, k^0)/m$$

$$k^\mu = (k^0, 0, 0, |\vec{k}|)$$

$$\vec{k}/m \simeq 0,$$

$$k_j^\mu \epsilon_\mu^{(l)} \simeq 0$$

$$\epsilon_1^\mu = (0, 1, 0, 0)$$

$$\epsilon_2^\mu = (0, 0, 1, 0)$$

$$\epsilon_3^\mu = (0, 0, 0, 1)$$

Spin projectors

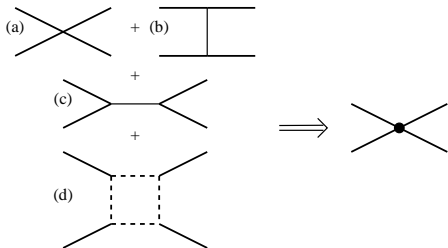
$$\mathcal{P}^{(0)} = \frac{1}{3} \epsilon_\mu \epsilon^\mu \epsilon_\nu \epsilon^\nu$$

$$\mathcal{P}^{(1)} = \frac{1}{2} (\epsilon_\mu \epsilon_\nu \epsilon^\mu \epsilon^\nu - \epsilon_\mu \epsilon_\nu \epsilon^\nu \epsilon^\mu)$$

$$\mathcal{P}^{(2)} = \left\{ \frac{1}{2} (\epsilon_\mu \epsilon_\nu \epsilon^\mu \epsilon^\nu + \epsilon_\mu \epsilon_\nu \epsilon^\nu \epsilon^\mu) - \frac{1}{3} \epsilon_\alpha \epsilon^\alpha \epsilon_\beta \epsilon^\beta \right\}$$



Formalism: The VV interaction



- (a) and (b) \rightarrow Pole mass and width
- (c) \rightarrow p-wave repulsive (not included)
- (d) \rightarrow Pole width

Bethe equation

$$T = [I - VG]^{-1} V$$

$$G = \int_0^{q_{max}} \frac{q^2 dq}{(2\pi)^2} \frac{\omega_1 + \omega_2}{\omega_1 \omega_2 [(P^0)^2 - (\omega_1 + \omega_2)^2 + i\epsilon]}$$



The VV interaction

1. $f_0(1370), f_2(1270) \sim \rho\rho$
R. Molina, D. Nicmorus and E. Oset, Phys. Rev. D **78**, 114018 (2008)
2. $f_0(1370), f_0(1710), f_2(1270), f_2'(1525) \sim \rho\rho, K^*\bar{K}^* \dots$
 $K_2^*(1430) \sim \rho K^*, \omega K^* \dots$
L. S. Geng and E. Oset, Phys. Rev. D **79**, 074009 (2009)
3. $D^*(2640), D_2^*(2460) \sim \rho(\omega)D^*$
R. Molina, H. Nagahiro, A. Hosaka and E. Oset, Phys. Rev. D **80**, 014025 (2009)
4. $Y(3940), Z(3930), X(4160) \sim D^*\bar{D}^*, D_s^*\bar{D}_s^*$
R. Molina and E. Oset, Phys. Rev. D **80**, 114013 (2009)



The VV interaction

- $C = 0; S = 1; I = 1/2$
(hidden charm):

$$D_S^* \bar{D}^*, J/\psi K^*$$

- $C = 1; S = -1; I = 0, 1$:

$$D^* \bar{K}^*$$

- $C = 1; S = 1; I = 0$:

$$D^* K^*, D_S^* \omega, D_S^* \phi$$

- $C = 1; S = 1; I = 1$:

$$D^* K^*, D_S^* \rho$$

- $C = 1; S = 2; I = 1/2$:

$$D_S^* K^*$$

- $C = 2; S = 0; I = 0, 1$:

$$D^* D^*$$

- $C = 2; S = 1; I = 1/2$:

$$D_S^* D^*$$

- $C = 2; S = 2; I = 0$:

$$D_S^* D_S^*$$



Convolution

Convolution due to the width of the ρ meson ($D_s^*\rho$ channel)

$$\tilde{G}(s) = \frac{1}{N} \int_{(m_\rho - 2\Gamma_\rho)^2}^{(m_\rho + 2\Gamma_\rho)^2} d\tilde{m}_1^2 \left(-\frac{1}{\pi}\right) \mathcal{I}m \frac{1}{\tilde{m}_1^2 - m_\rho^2 + i\Gamma \tilde{m}_1} G(s, \tilde{m}_1^2, m_{D_s^*}^2)$$

$$\Gamma(\tilde{m}) = \Gamma_\rho \left(\frac{\tilde{m}^2 - 4m_\pi^2}{m_\rho^2 - 4m_\pi^2} \right)^{3/2} \theta(\tilde{m} - 2m_\pi)$$

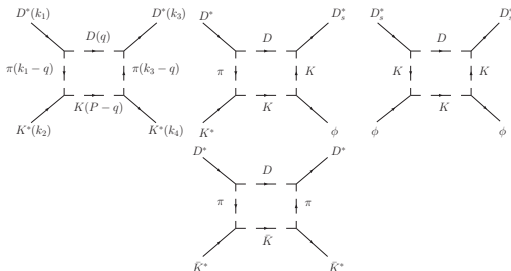
$$\begin{aligned} \Gamma_{D^*} &< 2.1 \text{ MeV} \\ \Gamma_\rho &= 146.2 \text{ MeV} \\ \Gamma_{K^*} &= 48 \text{ MeV} \end{aligned}$$

- The ρ^* -mass convolution gives $\Gamma \simeq 8 \text{ MeV}$ ($D_s^*\pi\pi$)
- The K^* -mass convolution gives $\Gamma \simeq 3 \text{ MeV}$ (or less) ($D_s^*\pi K$)



The PP decay mode

- The PP box diagram has only $J^P = 0^+$ and $J^P = 2^+$ quantum numbers
- We only find attractive interaction in the sectors:
 - $C = 1; S = -1; I = 0: D^* \bar{K}^*$
 - $C = 1; S = 1; I = 0: D^* K^*, D_S^* \phi, D_S^* \omega$
 - $C = 1; S = 1; I = 1: D^* K^*, D_S^* \rho$
 - $C = 2; S = 0; I = 0; J = 1: D^* D^*$
 - $C = 2; S = 1; I = 1/2; J = 1: D_S^* D^*$





The VV interaction

- Model A:

$$F_1(q^2) = \frac{\Lambda_b^2 - m_1^2}{\Lambda_b^2 - (k_1^0 - q^0)^2 + |\vec{q}|^2},$$

$$F_3(q^2) = \frac{\Lambda_b^2 - m_3^2}{\Lambda_b^2 - (k_3^0 - q^0)^2 + |\vec{q}|^2},$$

with $q^0 = \frac{s+m_2^2-m_4^2}{2\sqrt{s}}$, \vec{q} running variable, $\Lambda_b = 1.4, 1.5$ GeV and $g = M_\rho/2 f_\pi$

- Model B:

$$F(q^2) = e^{((q^0)^2 - |\vec{q}|^2)/\Lambda^2},$$

with $\Lambda = 1, 1.2$ GeV, $q^0 = \frac{s+m_2^2-m_4^2}{2\sqrt{s}}$, $g = M_\rho/2 f_\pi$,

$g_{D_s} = M_{D_s^*}/2 f_{D_s} = 5.47$ and $g_D = g_{D^* D\pi}^{\text{exp}} = 8.95$ (experimental value)



Couplings (g_a) in units of MeV

$$T_{ab} = \frac{g_a g_b}{s - s_p}$$

$C = 1; S = -1; l = 0$

$l[J^P]$	\sqrt{s}_{pole}	$g_{D^* \bar{K}^*}$
$0[0^+]$	2848	12227
$0[1^+]$	2839	13184
$0[2^+]$	2733	17379

$C = 1; S = 1; l = 1$

$l^G[J^{PC}]$	\sqrt{s}_{pole}	$g_{D^* K^*}$	$g_{D_s^* \rho}$
$1[2^+]$	2786	11041	11092

$C = 2; S = 0; l = 0$

$l[J^P]$	\sqrt{s}_{pole}	$g_{D^* D^*}$
$0[1^+]$	3969	16825

$C = 1; S = 1; l = 0$

$l[J^P]$	\sqrt{s}	$g_{D^* K^*}$	$g_{D_s^* \omega}$	$g_{D_s^* \phi}$
$0[0^+]$	2683	15635	-4035	6074
$0[1^+]$	2707	14902	-5047	4788
$0[2^+]$	2572	18252	-7597	7257

$C = 2; S = 1; l = 1/2$

$l[J^P]$	\sqrt{s}_{pole}	$g_{D_s^* D^*}$
$1/2[1^+]$	4101	13429



Summary

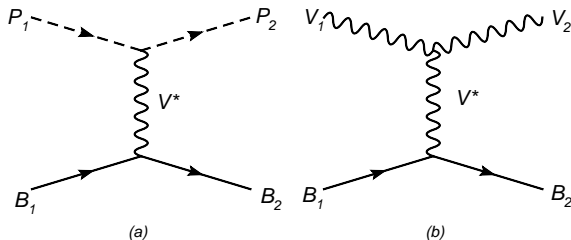
C, S	$I[J^P]$	\sqrt{s}	$\Gamma_A(\Lambda = 1400)$	$\Gamma_B(\Lambda = 1000)$	State	\sqrt{s}_{exp}	Γ_{exp}
1, -1	0[0 ⁺]	2848	23	25	$D_{s2}(2573)$	2572.6 ± 0.9	20 ± 5
	0[1 ⁺]	2839	3	3			
	0[2 ⁺]	2733	11	22			
1, 1	0[0 ⁺]	2683	20	44			
	0[1 ⁺]	2707	4×10^{-3}	4×10^{-3}			
	0[2 ⁺]	2572	7	18			
	1[2 ⁺]	2786	8	9			
2, 0,	0[1 ⁺]	3969	0	0			
2, 1	1/2[1 ⁺]	4101	0	0			

Table: Summary of the nine states obtained. The width is given for the model A, Γ_A , and B, Γ_B . All the quantities here are in MeV. Two values of α are used: -1.6 and -1.4 .



PB and VB resonances in the hidden charm sector

- $I = 1/2, S = 0$. Channels: $\bar{D}\Sigma_C, \bar{D}\Lambda_C^+, \eta_C N, \pi N, \eta N, \eta' N, K\Sigma, K\Lambda$
- $I = 0, S = -1$. Channels: $\bar{D}_S\Lambda_C^+, \bar{D}\Xi_C, \bar{D}\Xi'_C, \eta_C\Lambda, \pi\Sigma, \eta\Lambda, \eta'\Lambda, \bar{K}N, K\Xi$



$$\mathcal{L}_{BBV} = g(\langle \bar{B}\gamma_\mu [V^\mu, B] \rangle + \langle \bar{B}\gamma_\mu B \rangle \langle V^\mu \rangle)$$

$$t_{B_1 B_2 V} = \{g_{15_1} C_{15_1}(20' \otimes \bar{2}0') + g_{15_2} C_{15_2}(20' \otimes \bar{2}0') + g_1 C_1(20' \otimes \bar{2}0')\} \bar{u}_{r,r'}(p_2) \gamma \cdot \epsilon_{ur}(p_1)$$



$$T = [I - VG]^{-1}V \quad T_{ab} = \frac{g_a g_b}{\sqrt{s} - Z_R}$$

PB resonances

(I, S)	Z_R (MeV)	g_a		
$(1/2, 0)$		$\bar{D}\Sigma_c$	$\bar{D}\Lambda_c^+$	
	4269	2.85	0	
$(0, -1)$		$\bar{D}_s\Lambda_c^+$	$\bar{D}\Xi_c$	$\bar{D}\Xi'_c$
	4213	1.37	3.25	0
	4403	0	0	2.64

VB resonances

(I, S)	Z_R (MeV)	g_a		
$(1/2, 0)$		$\bar{D}^*\Sigma_c$	$\bar{D}^*\Lambda_c^+$	
	4418	2.75	0	
$(0, -1)$		$\bar{D}_s^*\Lambda_c^+$	$\bar{D}^*\Xi_c$	$\bar{D}^*\Xi'_c$
	4370	1.23	3.14	0
	4550	0	0	2.53



Prediction of narrow N^* and Λ^* resonances above 4.2 GeV

PB resonances (units in MeV)

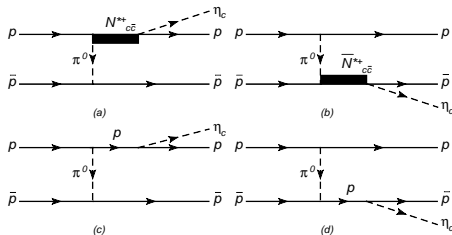
(I, S)	M	Γ	Γ_i					
$(1/2, 0)$			πN	ηN	$\eta' N$	$K\Sigma$	$\eta_c N$	
	4261	56.9	3.8	8.1	3.9	17.0	23.4	
$(0, -1)$			KN	$\pi\Sigma$	$\eta\Lambda$	$\eta'\Lambda$	$K\Xi$	$\eta_c\Lambda$
	4209	32.4	15.8	2.9	3.2	1.7	2.4	5.8
	4394	43.3	0	10.6	7.1	3.3	5.8	16.3

VB resonances

(I, S)	M	Γ	Γ_i					
$(1/2, 0)$			ρN	ωN	$K^*\Sigma$	$J/\psi N$		
	4412	47.3	3.2	10.4	13.7	19.2		
$(0, -1)$			K^*N	$\rho\Sigma$	$\omega\Lambda$	$\phi\Lambda$	$K^*\Xi$	$J/\psi\Lambda$
	4368	28.0	13.9	3.1	0.3	4.0	1.8	5.4
	4544	36.6	0	8.8	9.1	0	5.0	13.8



Production cross section of the N^* resonances at FAIR



- \bar{p} beam of 15 GeV/c, $\sqrt{s} = 5470$ MeV $\rightarrow M_X \simeq 4538$ MeV.

$$\frac{d\sigma_{p\bar{p} \rightarrow N_{c\bar{c}}^{*+}(4265)\bar{p} \rightarrow \eta_c p \bar{p}}}{d\cos\theta dM^2} = 0.3 \mu\text{b}/\text{GeV}^2$$
 at peak, $\sigma \simeq 0.07 \mu\text{b}$.
- $\sigma(p\bar{p} \rightarrow N_{c\bar{c}}^{*+}(4418)\bar{p} \rightarrow \eta_c p \bar{p}) \simeq 0.002 \mu\text{b}$.

This corresponds to an event production rate of 80000 and 1700 events per day for the $N_{c\bar{c}}^{*+}(4265)$ and $N_{c\bar{c}}^{*+}(4418)$ respectively for a Luminosity of $10^{31} \text{cm}^{-2} \text{s}^{-1}$.



Conclusions

- We studied dynamically generated resonances from **vector-vector interaction** in the charm-strange, hidden-charm and flavor exotic sectors and **meson-baryon resonances** with hidden charm
- In the present work we can assign one resonance to an experimental counterpart, which is the $D_2^*(2573)$
- We have found flavor exotic resonances with **double charm**, **double charm-strangeness** and new N^* , Λ^* states around 4.3 GeV that if observed cannot be accommodated in terms of $q\bar{q}$



References

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