



## Chung-Yao Chao Fellowship Interview 2021

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**Co-Advisor:** Assoc. Prof. Xiaorong Zhou

*University of Science and Technology of China*

June 5, 2021

- Self-Introduction
- Publication and Achievements
- **Research Experience**
  - Physics Motivation
  - Study of P-wave  $\chi_{cJ}(J = 0, 1, 2)$  decays
  - Study of  $e^+e^- \rightarrow \Sigma^0\bar{\Sigma}^0$ , using Rscan data
  - **Summary and Outlooks**
- **Future Work Plan**
  - Physics Motivation
  - Phase between the Strong and Electromagnetic Amplitudes of  $J/\psi(\psi(2S)) \rightarrow \Sigma\bar{\Sigma}$  Decays, using  $J/\psi(\psi(2S))$  scan data
  - **Preliminary Results**
  - **Future Prospects**

## Work Experience:

- June 2020 - Present: Postdoctoral researcher at USTC, China
- June 2013 - 2014: Visiting Lecturer at Punjab University, Pakistan
- June 2014 - 2016: Teacher Trainer at KIPS College, Pakistan

## Education:

- June 2016 - 2020: (CAS-TWAS fellowship)
  - Ph.D student in Nuclear and Particle Physics at USTC, China
- June 2011 - 2013: (CGPA 4.0/4.0)
  - Masters's Degree in High Energy Particle Physics at Punjab University, Pakistan
- June 2006 - 2010: (Gold Medal)
  - Bachelor's Degree in High Energy Particle Physics at Punjab University, Pakistan

## Research Areas:

- BESIII Collaboration since 2017, I have joined USTC working on:
  - Charmonium Physics → Radiative transition of  $\psi(2S)$
  - $\tau$ -QCD → Form factor and Relative Phase measurements
- Regularly presented work at BESIII Collaboration meeting and Workshops

Today I will focus on the recent results achieved at USTC and future plans

## Publication

- First measurements of  $\chi_{cJ} \rightarrow \Sigma^- \bar{\Sigma}^+$  ( $J = 0, 1, 2$ ) decays  $\rightarrow$  M. Ablikim *et al.* (BESIII Collaboration), Phys. Rev. D **101**, 092002 (2020) [link](#)

## Work Under Review

- Measurement of the  $e^+e^- \rightarrow \Sigma^0 \bar{\Sigma}^0$  cross section from production threshold to 3.02 GeV at BESIII [link](#). ([BAM-00441 at Collaboration Wide Review stage](#))

## Internal Referee

- Study of  $\Xi^-$  Baryon Polarization in  $\psi(3686) \rightarrow \Xi^- \bar{\Xi}^+$  decay at BESIII ([BAM-00487](#)) [link](#).

## Achievements

- Participate in **Hadron Physics Summer School** in winter, presented a talk on "**Improve the detector simulation techniques in Hadron Spectroscopy**", JUFA Julich, Germany, September, 2018.
- [CAS-TWAS President's Fellowship](#) awarded for Ph.D study.
- [University Gold Medal](#) for obtaining first position in Bachelors in HEP.

# Previous Work-I

Measurement of BFs of  $\chi_{cJ} \rightarrow \Sigma^- \bar{\Sigma}^+$  (J=0,1,2) decays

Models that can predicts the decay rates of  $\chi_{cJ} \rightarrow B\bar{B}$ :

- **Color Octet Mechanism (COM)**

- The next higher Fock state in the p-wave charmonium so-called **color octet**
- **This higher state is made up of the  $c\bar{c}$  plus a gluon**

- **Helicity Selection Rule (HSR)**

- When charmonium meson  $J_{c\bar{c}}$  decaying into two light mesons  $h_1$  and  $h_2$ , the perturbative method gives the asymptotic behavior of the branching ratio as follows:

$$\text{BR}[J_{c\bar{c}}(\lambda) \rightarrow h_1(\lambda_1)h_2(\lambda_2)] \sim \left(\frac{\Lambda_{\text{QCD}}^2}{m_c^2}\right)^{|\lambda_1+\lambda_2|+2}$$

- **If  $\lambda_1 + \lambda_2 \neq 0$ , which will violate the HSR and it is supposed to be suppressed**

- **Quark Creation Model (QCM)**

- The **limits of the helicity conservation rule can be removed**, so that some **forbidden** decay processes, *i.e.*  $\chi_{c0} \rightarrow B\bar{B}$  can be investigated.
- **This model strengthened decay channels  $\chi_{cJ} \rightarrow \Lambda\bar{\Lambda}$  ( $J=0,2$ ) are understood, by including only the color singlet contribution.**

- **Large BF's of  $\psi(2S) \rightarrow \gamma\chi_{cJ}$  make  $e^+e^-$  collisions at the  $\psi(2S)$  resonance a very clean environment for  $\chi_{cJ}$  investigation.**

# Theoretical and Phenomenological Results

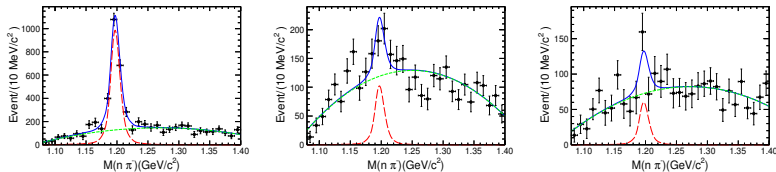
BFs comparison for various  $\chi_{cJ} \rightarrow B\bar{B}$  in units of  $10^{-5}$

Mode		$\chi_{c0}$	$\chi_{c1}$	$\chi_{c2}$
$p\bar{p}$	BES	$27.1^{+4.3}_{-3.9} \pm 4.7$	$5.7^{+1.7}_{-1.5} \pm 0.9$	$6.5^{+2.4}_{-2.1} \pm 1.0$
	PDG	$22.1 \pm 0.08$	$7.60 \pm 0.34$	$7.33 \pm 0.33$
	Theory	...	6.4	7.7
$\Lambda\bar{\Lambda}$	BESIII	$33.3 \pm 2.0 \pm 2.6$	$12.2 \pm 1.1 \pm 1.1$	$20.8 \pm 1.6 \pm 2.3$
	PDG	$33.0 \pm 4.0$	$11.8 \pm 1.9$	$18.6 \pm 2.7$
	Theory	$(93.5 \pm 20.5^a, \mathbf{22.1 \pm 6.1^b})$ (QCM)	...	$(15.2 \pm 1.7^a, 4.3 \pm 0.6^b)$
		<b>11.9 – 15.1 (COM)</b>	3.9	3.5
$\Sigma^0\bar{\Sigma}^0$	BESIII	$47.7 \pm 1.8 \pm 3.5$	$4.3 \pm 0.5 \pm 0.3$	$3.9 \pm 0.5 \pm 0.3$
	PDG	$44.0 \pm 4$	$< 4.0$	$< 6.0$
	Theory	$(\mathbf{25.1 \pm 3.4^a}, \mathbf{18.7 \pm 4.5^b})$	...	$(38.9 \pm 8.8^a, 4.2 \pm 0.5^b)$
		...	3.3	5.0
$\Sigma^+\bar{\Sigma}^-$	BESIII	$50.4 \pm 2.5 \pm 2.7$	$3.7 \pm 0.6 \pm 0.2$	$3.5 \pm 0.7 \pm 0.3$
	PDG	$39.0 \pm 7.0$	$< 6.0$	$< 7.0$
	Theory	<b>5.6 – 6.9 (COM)</b>	3.3	5.0
$\Xi^-\bar{\Xi}^+$	BESIII	$53.0 \pm 2.7 \pm 0.9$	$< 3.4$	$< 3.7$
	PDG	$48.0 \pm 7.0$	$8.0 \pm 2.1$	$< 10.0$
	Theory	<b>23.0 <math>\pm</math> 7.0 (QCM)</b>	...	$4.8 \pm 2.1$
		...	2.4	3.4
$\Xi^0\bar{\Xi}^0$	BESIII	$46.7 \pm 1.9 \pm 2.3$	$7.5 \pm 1.1 \pm 0.5$	$18.3 \pm 1.5 \pm 1.4$
	PDG	$31.0 \pm 8.0$	$< 6.0$	$< 10.0$
	Theory	<b>23.0 <math>\pm</math> 7.0 (QCM)</b>	...	$4.8 \pm 2.1$
		...	2.4	3.4

- Experimentally, there are no BF results of  $\chi_{cJ} \rightarrow \Sigma^-\bar{\Sigma}^+$ , necessary to further test the validity of **COM, HSR, QCM** and prediction of **isospin symmetry**.

# Summary of $\mathcal{B}(\chi_{cJ} \rightarrow \Sigma^- \bar{\Sigma}^+)$

**Fit Results:** The fitted signal yields of  $\psi(3686) \rightarrow \gamma \chi_{cJ}$  as a function of  $M(n\pi^-)$ .



**BF measurements of  $\chi_J \rightarrow \Sigma^- \bar{\Sigma}^+$ :**

- **First measurement ever**, due to difficult reconstruction of  $n\bar{n}\pi^+\pi^-$ .
- Prove the **isospin symmetry in strong interaction** comparing to  $\chi_{cJ} \rightarrow \Sigma^+ \bar{\Sigma}^-$ .
- **BF of  $\chi_{c0} \rightarrow \Sigma^- \bar{\Sigma}^+$  do not vanish**, which **demonstrates a strong violation of the HSR**.
- **Both COM and QCM fails to describe our measured result.**

**Results of the BFs (in units of  $10^{-5}$ ) for the measurement of  $\chi_{cJ} \rightarrow \Sigma^- \bar{\Sigma}^+$**

Channel	This work	$S(\sigma)$	BESIII	Theoretical predictions	
				COM	QCM
	$\chi_{cJ} \rightarrow \Sigma^- \bar{\Sigma}^+$		$\chi_{cJ} \rightarrow \Sigma^+ \bar{\Sigma}^-$		
$\chi_{c0} \rightarrow \Sigma^- \bar{\Sigma}^+$	$51.3 \pm 2.4 \pm 4.1$	$30\sigma$	$50.4 \pm 2.5 \pm 2.7$	5.9-6.9	$18.1 \pm 3.9$
$\chi_{c1} \rightarrow \Sigma^- \bar{\Sigma}^+$	$5.7 \pm 1.4 \pm 0.6$	$5.8\sigma$	$3.7 \pm 0.6 \pm 0.2$	3.3	...
$\chi_{c2} \rightarrow \Sigma^- \bar{\Sigma}^+$	$4.4 \pm 1.7 \pm 0.5$	$3.6\sigma$	$3.5 \pm 0.7 \pm 0.3$	5.0	$4.3 \pm 0.4$

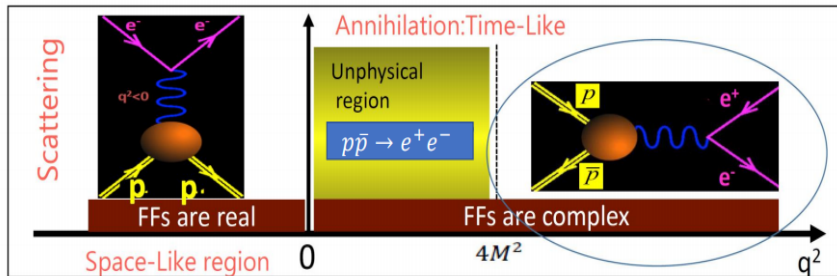


# Work Under Review-II

Study of  $\Sigma^0\bar{\Sigma}^0$  from  $\sqrt{s} = 2.3864$  to  $3.0200$  GeV using R-scan data

# Space- and Timelike EMFFs

- EMFFs are accessed in kinematical regions of (transferred squared four-momentum)  $q^2$  through study of space- and timelike processes.
- Hyperons are difficult to study in the SL region but TL form factors offers the best opportunity to study of Hyperons.
- Time-like baryons EMFFs is accessible in  $e^+e^-$  collision.
- **Our aim to probe the cross section near threshold of hyperon pairs experimentally.**

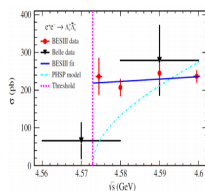
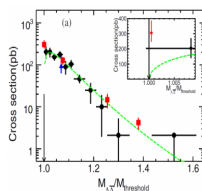
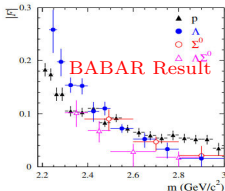
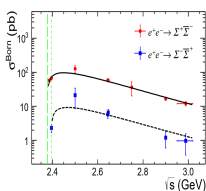


# Baryon Form Factors (EMFFs)

## Spin 1/2 Baryons:

- Two independent EMFFs:  $G_E(s), G_M(s)$  ( $s = q^2$ , four momentum transfer).
- In one-photon exchange: ( $\tau = \frac{q^2}{4m_B^2}, \beta = \sqrt{1 - \frac{4m_B^2}{q^2}}$ , Coulomb factor C)
  - Total cross section:  $\sigma_{B\bar{B}}(s) \equiv \frac{4\pi\alpha^2\beta C}{3s} [|G_M(s)|^2 + \frac{1}{2\tau}|G_E(s)|^2]$
  - Effective FFs:  $|G_{\text{eff}}(s)| = \sqrt{\frac{\sigma(s)}{\frac{4\pi\alpha^2\beta C}{3s} [1 + \frac{1}{2\tau}]}}$
- **Observed Threshold Enhancement:** For example  $p\bar{p}, \Lambda\bar{\Lambda}, \Lambda_c\bar{\Lambda}_c, \dots$
- Hyperons FFs are hardly explored. The precision of hyperons FFs are quite poor and better results to be demanded in future.

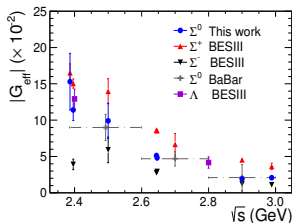
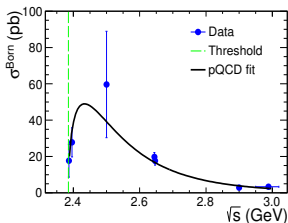
[<https://docbes3.ihep.ac.cn/DocDB/0007/000742/004/sigsig.pdf>]



# Summary of $e^+e^- \rightarrow \Sigma^0 \bar{\Sigma}^0$

## Outlooks:

- Cross section lineshape for  $e^+e^- \rightarrow \Sigma^0 \bar{\Sigma}^0$  is well fitted by **pQCD-motivated function**.
- Improved precision compared to BaBar's measurements over **50% above  $\sqrt{s} \geq 2.5000$  GeV**.
- **Novel method** has applied at production threshold, **no significant signal is observed at 2.3864 GeV**.
- An **asymmetry of isospin triplet** is observed, and consistent with their **incoherent sum of squared of charges of valence quarks**.
- Cross section between  $\Lambda$  and  $\Sigma^0$  is shown to provide the **proof for diquark-correlation**.
- **For complete determination of FFs more data sets will be needed in future at BESIII**.



- Our results provide a valuable experimental inputs to understand the **hyperons-antihyperons** production in both **strong and EM** interactions.

# Proposed Work joint effort of USTC and Ferra group Itlay

Phase between the Strong and Electromagnetic Amplitudes of  
 $J/\psi(\psi(2S)) \rightarrow \Sigma\bar{\Sigma}$  Decays, using  $J/\psi(\psi(2S))$  scan data

## $J/\psi$ Strong and EM Decay Amplitudes:

### Resonant contributions:

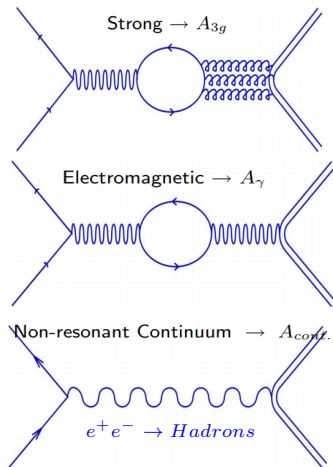
- pQCD: all amplitudes almost real<sup>[1,2]</sup>
- QCD  $\rightarrow$  small phases foreseen  $\Phi_{3g,\gamma} \sim 10^\circ$
- Experimental observation  $\rightarrow$  Large Phase foreseen

### Non-resonant continuum:

In pQCD regime

- $A_\gamma \in \mathcal{R}$
- If both real, continuum and resonant amplitudes must interfere
- Phase b/w  $A_{3g}, A_\gamma \rightarrow (\Phi_{3g,\gamma} \sim 0^\circ/180^\circ)$

$\rightarrow$  No theory can give the satisfactory explanation of the origin of  $\Phi_{3g,\gamma} \rightarrow$  better knowledge of it may lead profound understanding of charmonia decays.



Phys.Lett. B **791**, 375 (2019)

[1] Phys. Rev. Lett. **59**, 621 (1987)

[2] Nucl. Phys. B **246**, 52 (1984)

## Theoretical predication:

- **Model depended approach** using SU(3) flavor symmetry suggested:
  - $\Phi_{3g,\gamma} \sim 90^\circ \rightarrow$  **No interference**

## Experimental results:

- **Indirect results based on SU(3)**
  - $J/\psi \rightarrow N\bar{N} (1/2^+ 1/2^-)$      $\Phi_{3g,\gamma} = (88.7 \pm 8.1)^\circ$ <sup>[1]</sup>
  - $J/\psi \rightarrow VP (1^- 0^-)$      $\Phi_{3g,\gamma} = (106 \pm 10)^\circ$ <sup>[2]</sup>
  - $J/\psi \rightarrow PP (0^- 0^-)$      $\Phi_{3g,\gamma} = (89.6 \pm 9.9)^\circ$ <sup>[3]</sup>
  - $J/\psi \rightarrow VV (1^- 1^-)$      $\Phi_{3g,\gamma} = (138 \pm 37)^\circ$ <sup>[3]</sup>
  - $\psi(2S) \rightarrow PP (0^- 0^-)$      $\Phi_{3g,\gamma} = (95 \pm 15)^\circ$ <sup>[4]</sup>
  - $\psi(2S) \rightarrow N\bar{N} (1/2^+ 1/2^-)$      $\Phi_{3g,\gamma} = (-98 \pm 25)^\circ$  or  $(134 \pm 25)^\circ$
  - $\psi(2S) \rightarrow VP (1^\pm 0^-)$      $\Phi_{3g,\gamma} \sim 0^\circ$  **No evidence for large phase**
- **Direct results through lineshape scan**
  - $J/\psi \rightarrow 5\pi$      $\Phi_{3g,\gamma} = (84 \pm 3.6)^\circ$  or  $(-84.9 \pm 3.6)^\circ$
- **All analyses revealed that a relative orthogonal phase exist b/w  $A_{3g}$  and  $A_\gamma$**

[1] Phys. Rev. D **86**, 032014 (2012)

[2] Phys. Rev. D **41**, 01389 (1990)

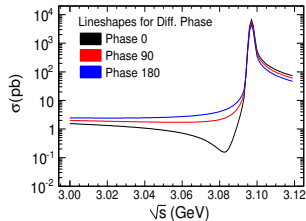
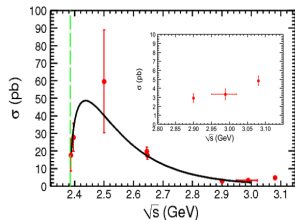
[3] Phys. Rev. D **60**, 051501 (1999)

[4] Phys. Rev. D **74**, 011105 (2006)

# Why this measurement is important?

- Jump has been observed while studied  $e^+e^- \rightarrow \Sigma^0 \bar{\Sigma}^0$  at BESIII.
- $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$  decays the phase may not be compatible with  $90^\circ$ .
- Scan below and at  $J/\psi(\psi(2S))$  resonance data provides unique opportunity **for the first ever phase measurement of hyperon-antihyperon ( $\Sigma^0 \bar{\Sigma}^0$ )** at BESIII.
- It should be a bed-test for **perturbative QCD (pQCD)** model predictions, **SU(3) symmetry** and **SU(3) symmetry breaking hypotheses**.
- **With a model independent fit to study the interference pattern**

BAM-00441





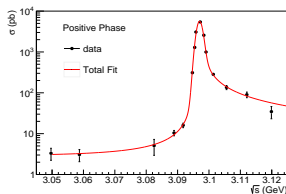
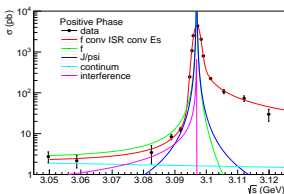
# Phase Measurement

## Preliminary Results

# Preliminary Results by $J/\psi$ lineshape

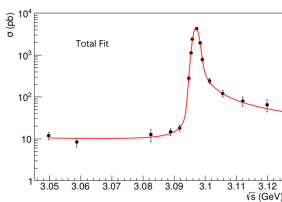
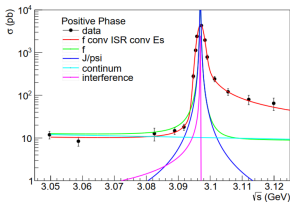
## 1. Fitting Result for $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$

Preliminary value of phase:  $\Phi_{3g,\gamma} \approx \pm(157.0 \pm 49.3)^\circ \rightarrow$  [Ref.link1](#)



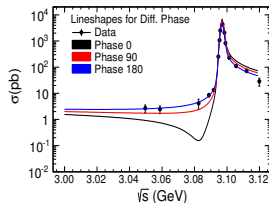
## 2. Fitting Result for $J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$

Preliminary value of phase:  $\Phi_{3g,\gamma} \approx \pm(114.5 \pm 12.7)^\circ \rightarrow$  [Ref.link2](#)



# Summary of Phase determination

- Preliminary results reveal that  $\Phi_{3g,\gamma}$  amplitudes of  $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$  decay is not compatible with  $\sim 90^\circ$ .
- Current result is inconsistent with prediction based on SU(3) octet baryons and favor to the pQCD.
- First measurement ever, since we always treated the phase for SU(3) octet baryons to be same as  $\sim 90^\circ$ .
- Large relative phase value brings a new challenge for theoretician to deeply understand the quarkonium dynamic.
- Since phase  $90^\circ$  is virtually impossible in  $\psi(2S)$  decays as predicted. So, it is matter of great concern the large phase is consistent with the  $\psi(2S)$  data.



## Summary – Outlooks

- Exciting 4-years of PhD at USTC and China.
- I have joined BESIII Collaboration since 2017 and published one article in Physical Review D and completed one Memo-BAM-00441.
- Starting from June 2020 till now, I am postdoctoral researcher at USTC.
- On-going analysis BAM-00441 is in CWR stage at BESIII and intended general to be Physics Letters B.
- At present, I am assigning internal referee of BAM-00487 at BESIII.
- **Responsible for phase project at USTC and already achieved preliminary results for two process  $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$  and  $J/\psi \rightarrow \Sigma^+ \bar{\Sigma}^-$ .**

### Future plan

- Active participation in Physics measurements using BESIII data and focus on phase study through  $J/\psi(\psi(2S))$  lineshape scan (direct approach).
- Our plan to present the phase measurement  $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$  in upcoming BESIII Workshop held in Lanzhou University.
- **Use my expertise in hyperon reconstruction to explore new aspects by studying  $\psi(2S) \rightarrow \Sigma^0 \bar{\Sigma}^0$  lineshape.**

Thanks for your attention!

# Back up

# $J/\psi$ Phase Scan – Real Data

Ecm (GeV)	RunID	BEMS ECM(GeV)	$L_{\text{int}}(\text{nb}^{-1})$
3.0500	28312 – 28346	$3.050206 \pm 0.000026$	$14919 \pm 161$
3.0600	28347 – 28381	$3.059257 \pm 0.000028$	$15060 \pm 161$
3.0830	28382 – 28387, 28466 – 28469	$3.083060 \pm 0.000023$	$4769 \pm 55$
3.0900	28388 – 28416, 28472 – 28475	$3.089418 \pm 0.000022$	$15558 \pm 165$
3.0930	28417 – 28453, 28476 – 28478	$3.092324 \pm 0.000025$	$14910 \pm 160$
3.0943	28479 – 28482	$3.095261 \pm 0.000084$	$2143 \pm 25$
3.0952	28487 – 28489	$3.095994 \pm 0.000081$	$1816 \pm 21$
3.0958	28490 – 28492	$3.096390 \pm 0.000075$	$2135 \pm 25$
3.0969	28493 – 28495	$3.097777 \pm 0.000076$	$2069 \pm 26$
3.0982	28496 – 28498	$3.098904 \pm 0.000075$	$2203 \pm 25$
3.0990	28499 – 28501	$3.099606 \pm 0.000093$	$756 \pm 11$
3.1015	28504 – 28505	$3.101923 \pm 0.000106$	$1612 \pm 21$
3.1055	28506 – 28509	$3.106144 \pm 0.000090$	$2106 \pm 25$
3.1120	28510 – 28511	$3.112615 \pm 0.000093$	$1720 \pm 21$
3.1200	28512 – 28513	$3.120442 \pm 0.000115$	$1264 \pm 16$

B.X. Zhang, Luminosity measurement for  $J/\psi$  phase and lineshape study

- **Analysis Environment:** Under the BOSS 6.6.4.p01

Ecm (GeV)	RunID	Number of Run	Data taken time	$\mathcal{L}$ (pb <sup>-1</sup> )
3.5815	55375 – 55461	83	180505 – 180508	84.604 ± 0.082
3.6702	55462 – 55541	80	180508 – 180512	83.582 ± 0.084
3.6081	55542 – 55635	91	180512 – 180515	83.060 ± 0.083
3.6828	55636 – 55662	26	180516 – 180516	28.175 ± 0.049
3.6842	55663 – 55690	28	180517 – 180518	27.840 ± 0.048
3.6853	55691 – 55716	25	180519 – 180519	25.342 ± 0.046
3.6865	55717 – 55737	20	180519 – 180520	24.481 ± 0.045
3.6914	55738 – 55795	57	180520 – 180523	68.647 ± 0.076
3.7098	55796 – 55859	60	180523 – 180525	69.326 ± 0.077

**B.X. Zhang, Luminosity measurement for  $\psi(2S)$  phase and lineshape study**

- **Analysis Environment:** Under the BOSS 7.0.4

# Lineshape of $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$

## To Fit the Lineshape:

- The cross section of  $e^+e^- \rightarrow \Sigma^0 \bar{\Sigma}^0$  is expressed as:

$$\sigma(W) = \left| D \frac{S e^{i\phi} + E}{M_{J/\psi} - W - i\Gamma_{J/\psi}/2} - C \right|^2$$

- $B_{J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0} = \text{constant} \times |S e^{i\phi} + E|^2$
- where constant =  $1/0.3894 \times 10^9$  (pb-to-  $\text{GeV}^{-2}$  conversion factor)
- $J/\psi \rightarrow e^+e^-$  **Amplitude:**  $D = \frac{\Gamma_{J/\psi}/2}{M_{J/\psi}} \sqrt{12\pi B_{J/\psi \rightarrow e^+e^-}}$

## For Continuum Amplitude:

- $\sigma_{\text{cont}}(W) = \sigma_o \left(\frac{W_o}{W}\right)^{\text{pQCD}} = C^2$
- $C = \sqrt{\sigma_o(3\text{GeV})} \left(\frac{3\text{GeV}}{W}\right)^{\frac{\text{pQCD}}{2}} = 5$

**Electromagnetic Amplitude:** EM contribution to the Feynman diagram, we look at ratio b/w  $B_{\text{out}}$  of the final state and  $B_{\mu\mu}$ . EM amplitude simplified as:

- $E = \sqrt{\frac{C^2}{\sigma_{e^+e^- \rightarrow \mu^+\mu^-}}} B_{J/\psi \rightarrow \mu^+\mu^-}$



# Fitting Procedure

**To Fit the Lineshape:** To incorporating the the effect of radiative function  $F(x, W)$  and Energy Spread  $S_E$  in the fit, the dressed Born cross section is modified as;

- **Step1.** Incorporating the radiative correction  $F(x, W)$ :

$$\sigma'(W) = \int_0^{1 - \left(\frac{W_{\min}}{W}\right)^2} dx F(x, W) \sigma(W \sqrt{1-x})$$

- **Step2.** Energy spread  $S_E$  is included by convolving with Gaussian function by set the width of  $S_E$ . The Born cross section becomes:

$$\sigma''(W) = \int_{W-nS_E}^{W+nS_E} \frac{1}{\sqrt{2\pi}S_E} \exp\left(-\frac{(W-W')^2}{2S_E^2}\right) \sigma'(W') dW'$$

**Minimization Function:** The fitting parameters are obtained by means of  $\chi^2$ -minimization as:

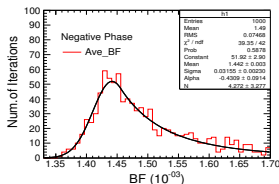
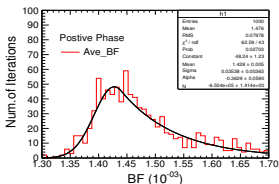
$$\chi_{\min}^2 = \sum_{i=1}^{15} \frac{(\sigma_i^{\text{obs}} - \sigma''(W_i))^2}{(\Delta\sigma_i^{\text{obs}})^2 + \left[ (\sigma''(W_i + \frac{\Delta W_i}{2}) - \sigma''(W_i - \frac{\Delta W_i}{2})) \right]^2},$$

where error along  $X$ -axis, is projected along the  $Y$ -axis.

# Preliminary Result $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$ - Solution-I,II

## Branching Fractions:

- Since the parameters are high correlated therefore, the error in the BF( $J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0$ ) is obtained after parametrized the value of each parameter.



## This Work

- In PDG:  $\text{BF} = (1.172 \pm 0.031) \times 10^{-3}$
- For +ve phase:  $\text{BF} = (1.428 \pm 0.035) \times 10^{-3}$
- For -ve phase:  $\text{BF} = (1.442 \pm 0.032) \times 10^{-3}$
- Floating all parameters in a fit such as; Strong, Continuum,  $\Phi_{3g,\gamma}$  and  $S_E$ .

Solution	$\Delta\Phi_{3g,\gamma}(\circ)$	SE (MeV)	$\text{BF}(J/\psi \rightarrow \Sigma^0 \bar{\Sigma}^0)$	$\chi^2 / \text{ndf}$
Sol-I	$157.0 \pm 49.3$	$0.915 \pm 0.0004$	$(1.428 \pm 0.035) \times 10^{-3}$	9.36/11.0
Sol-II	$-156.7 \pm 47.4$	$0.915 \pm 0.0004$	$(1.442 \pm 0.032) \times 10^{-3}$	9.36/11.0

Fitting results on  $J/\psi$  lineshape from  $\Sigma^0 \bar{\Sigma}^0$  with statistical error only.