

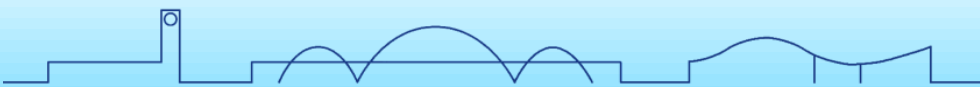
Detecting the pure triangle singularity effect through the decay of $\psi(2S)$

Jia-Jun Wu (UCAS)

Collaborators: Qi Huang, Chao-Wei Sheng

PRD 103 (2021) 1, 016014 arXiv: 2109.08349 [hep-ph]

The 10th International Workshop on Chiral Dynamics Nov-16-2021 IHEP(Online)

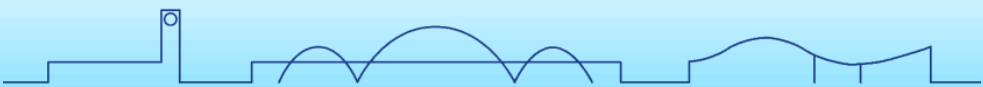


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Content

- What is Triangle Singularity?
- Why Triangle Singularity interesting ?
- How to confirm Triangle Singularity?
- Our two proposals
- Summary

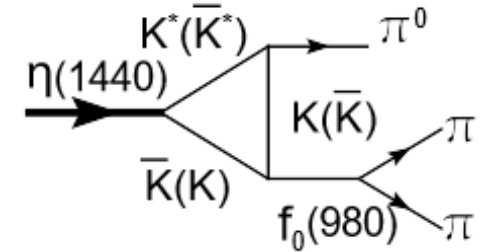
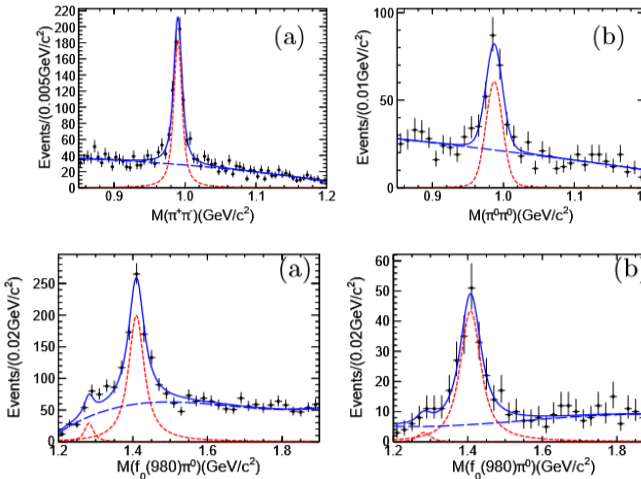
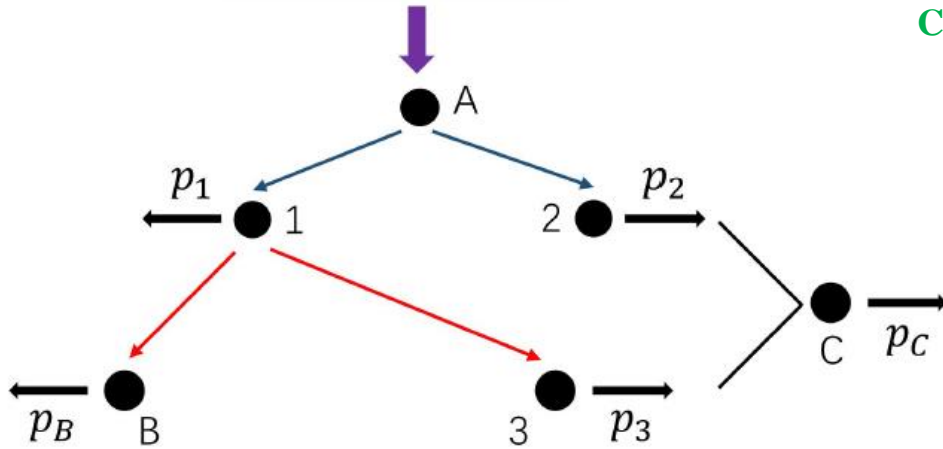
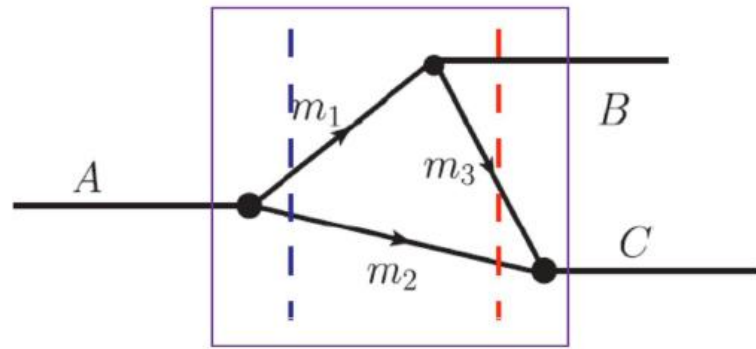


What is Triangle Singularity?

Actually Happened Process

- (1) All particles are on mass-shell;
- (2) Particle 3 catch up particle 2.

L. D. Landau, *NP* **13**, 181 (1960)
 S. Coleman, R.E. Norton, *Nuovo Cim.* **38**, 438 (1965)
 R. Karplus, C.M. Sommerfield, E.H. Wichmann, *PR* **111**, 1187 (1958).
 J.D. Bjorken, Ph.D. Thesis, Stanford University, Stanford, CA, USA, (1959).
 C. Schmid, *PR* **154**, 1363 (1967)



BESIII collaboration,
PRL **108**, 182001(2012)
 Wu, Liu, Zhao, Zou
PRL, **108**, 081803 (2012)



Why Triangle Singularity interesting ?

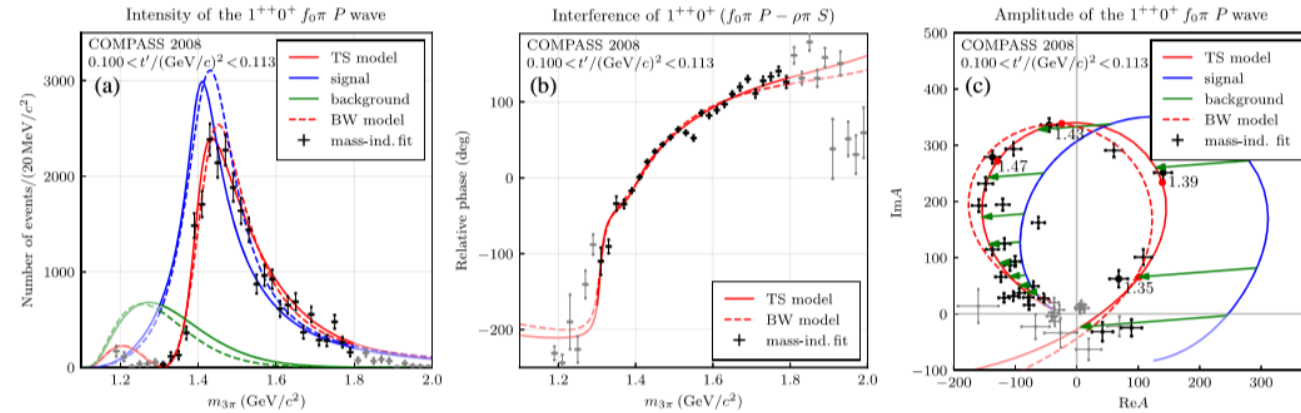
Guo, Liu, Sakai PPNP 112, 103757 (2020)

Structures	Processes	Loops	I/F	Refs.
2.1 GeV [141]	$\gamma p^+ \rightarrow N^*(2030) \rightarrow K^+ \Lambda(1405)$	$K^* \Sigma \pi$	I	[142]
2.1 GeV	$\pi^- p^+ \rightarrow K^0 \Lambda(1405), pp \rightarrow p K^+ \Lambda(1405)$	$K^* \Sigma \pi$	I	[143]
1.88 GeV	$\Lambda_c^+ \rightarrow \pi^+ \pi^0 \pi \Sigma$	$\bar{K}^* N \bar{K}$	I	[144, 145] ^a
$N(1700)$ [10]	$N(1700) \rightarrow \pi \Delta$	$\rho N \pi$	I	[146]
$N(1875)$ [10]	$N(1875) \rightarrow \pi N(1535)$	$\Sigma^* K \Lambda$	I	[147]
$\Delta(1700)$ [148-150]	$\gamma p \rightarrow \Delta(1700) \rightarrow \pi N(1535) \rightarrow p \pi^0 \eta$	$\Delta \eta p$	I	[151]
2.2 GeV [152]	$\Lambda_c^+ \rightarrow \pi^0 \phi p$	$\Sigma^* K^* \Lambda$	F	[153]
1.66 GeV [154, 155]	$\Lambda_c^+ \rightarrow \pi^+ K^- p$	$a_0 \Delta \eta, \Sigma^* \eta \Lambda$	F	[156]
$P_c(4450)$ [35]	$\Lambda_b^0 \rightarrow K^- J/\psi p$	$\Lambda(1890) \chi_{c1} P$	F	[157-160] ^b
		$N(1900) \chi_{c1} P$	F	[159]
peaks relevant for P_c	$\Lambda_b^0 \rightarrow K^- J/\psi p$	$D_{s1} \Lambda_c^+ \bar{D}^{(*)}$	F	[36, 158]

Structures	Processes	Loops	I/F	Refs.
$\rho(1480)$ [78, 79]	$\pi^- p \rightarrow \phi \pi^0 n$	$K^* \bar{K} K$	I	[80, 81]
$\eta(1405/1475)$ [82-86]	$\eta(1405/1475) \rightarrow \pi f_0$	$K^* \bar{K} K$	I	[87-91] ^{a,b}
$f_1(1420)$ [92]	$f_1(1285) \rightarrow \pi a_0/\pi f_0$	$K^* \bar{K} K$	I	[89, 93-95] ^b
$a_1(1420)$ [96, 97]	$a_1(1260) \rightarrow f_0 \pi \rightarrow 3\pi$	$K^* \bar{K} K$	I	[97-99]
1.4 GeV [100]	$J/\psi \rightarrow \phi \pi^0 \eta/\phi \pi^0 \pi^0$	$K^* \bar{K} K$	I	[101] ^b
1.42 GeV	$B^- \rightarrow D^{*0} \pi^- f_0(a_0), \tau \rightarrow \nu_\tau \pi^- f_0(a_0)$	$K^* \bar{K} K$	I	[102, 103]
	$D_s^+ \rightarrow \pi^+ \pi^0 f_0(a_0), B_s^0 \rightarrow J/\psi \pi^0 f_0(a_0)$	$K^* \bar{K} K$	I	[104, 105]
$f_2(1810)$ [10]	$f_2(1640) \rightarrow \pi \pi \rho$	$K^* \bar{K} K$	I	[106]
1.65 GeV	$\tau \rightarrow \nu_\tau \pi^- f_1(1285)$	$K^* \bar{K} K$	I	[107]
1515 MeV	$J/\psi \rightarrow K^+ K^- f_0(a_0)$	$\phi \bar{K} K$	I	[108]
2.85 GeV, 3.0 GeV	$B^- \rightarrow K^- \pi^- D_{s1}^0/K^- \pi^- D_{s1}$	$K^{*0} D^{(*)0} K^+$	I	[109, 110]
5.78 GeV	$B_s^+ \rightarrow \pi^0 \pi^+ B^0$	$\bar{K}^{*0} B^+ K$	F	[111]
[4.01, 4.02] GeV	$[D^{*0} D^{*0}] \rightarrow \gamma X$	$D^{*0} D^{*0} D^0$	I	[112]
4015 MeV	$e^+ e^- \rightarrow \gamma X$	$D^{*0} D^{*0} D^0$	I	[113, 114]
4015 MeV	$B \rightarrow K X \pi, pp/pp \rightarrow X \pi + \text{anything}$	$D^{*0} D^{*0} D^0$	I	[115, 116]
$\Upsilon(11020)$ [117, 118]	$e^+ e^- \rightarrow Z_0 \pi$	$B_1(5721) B B^+$	I	[119, 120]
3.73 GeV	$X \rightarrow \pi^0 \pi^+ \pi^-$	$D^{*0} D^0 D^0$	F	[121]
[4.22, 4.24] GeV	$e^+ e^- \rightarrow \gamma J/\psi \phi/\pi^0 J/\psi \eta$	$D_{s0(a1)}^+ D_s^{(*)-} D_s^{(*)-}$	F	[122]
[4.08, 4.09] GeV	$e^+ e^- \rightarrow \pi^0 J/\psi \eta$	$D_{s0(a1)}^+ D_s^{(*)-} D_s^{(*)-}$	F	[122]
$Z_c(3900)$ [31, 32]	$e^+ e^- \rightarrow J/\psi \pi^+ \pi^-$	$D_1 D^* D$	F	[119, 123-127] ^c
		$D_{s1}^*(2400) D^* D$	F	[128, 129]
$Z_c(4020, 4030)$ [33, 130]	$e^+ e^- \rightarrow \pi^+ \pi^- h_c(\psi)$	$D_{1(2)} \bar{D}^{(*)} D^{(*)}$	F	[125]
$X(4700)$ [131, 132]	$B^+ \rightarrow K^+ J/\psi \phi$	$K_1(1650) \psi \phi$	F	[133]
$Z_c(4430)$ [30, 134]	$\bar{B}^0 \rightarrow K^- \pi^+ J/\psi$	$\bar{K}^{*0} \psi(4260) \pi^+$	F	[135]
$Z_c(4200)$ [136, 137]	$\bar{B}^0 \rightarrow K^- \pi^+ \psi(2S)$	$\bar{K}_1^* \psi(3770) \pi^+$	F	[135]
	$\Lambda_b^0 \rightarrow p \pi^- J/\psi$	$N^* \psi(3770) \pi^-$	F	[135]
$X(4050)^{\pm}$ [138]	$\bar{B}^0 \rightarrow K^- \pi^+ \chi_{c1}$	$\bar{K}^{*0} X \pi^+$	F	[139]
$X(4250)^{\pm}$ [138]	$\bar{B}^0 \rightarrow K^- \pi^+ \chi_{c1}$	$\bar{K}_1^* \psi(3770) \pi^+$	F	[139]
$Z_b(10610)$ [34]	$e^+ e^- \rightarrow \Upsilon(1S) \pi^+ \pi^-$	$B_7^* \bar{B}^* B$	F	[128]

1. It is a pure kinematic effect \rightarrow Model independent
2. The effect of Loop \rightarrow Understand hadronic loop contribution
3. Provide a peak structure \rightarrow May mixing with resonance
4. Extract the nature of hadron \rightarrow Study the coupling at the energy point
5.

$$\pi p \rightarrow a_1(1420) \rightarrow f_0(980) \pi \rightarrow 3\pi$$



COMPASS Collaboration PRL 127, 082501 (2021)

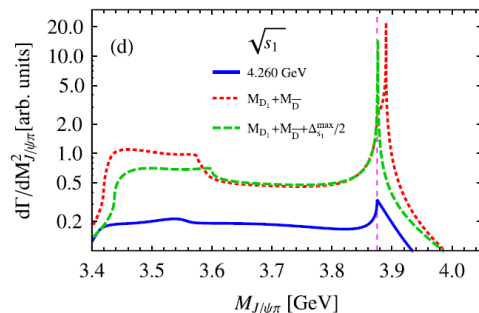
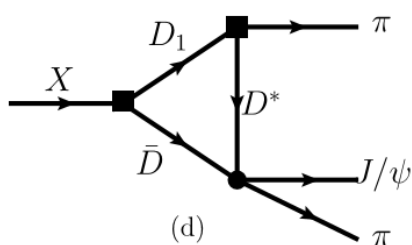
Mikhasenko, Ketzer, Sarantsev PRD 91, 094015 (2015)

But not confirm yet ...



How to confirm Triangle Singularity?

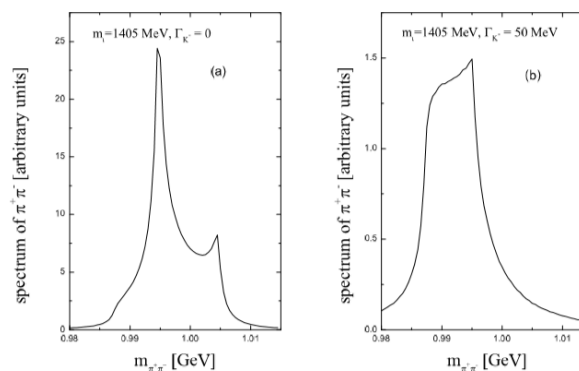
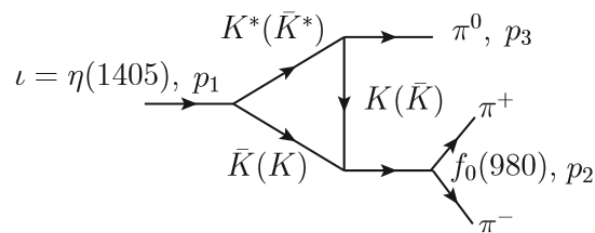
1. Threshold



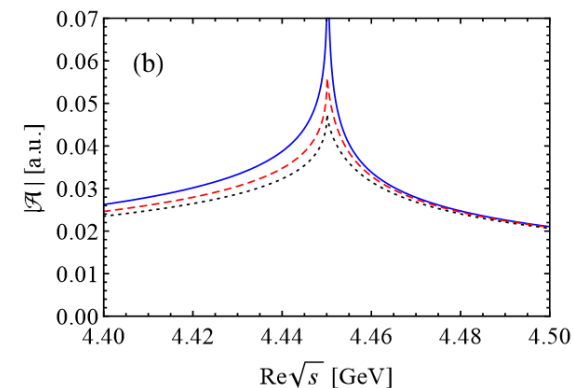
The corresponding values are listed in Table 1. The ATS peak will then stay close to the normal threshold, as illustrated in Fig. 4(d). In this sense, it would be difficult to distinguish the ATS peak from the pole structure in the invariant mass of the $J/\psi\pi$. We shall come back to the relevant issue later in this Section. It should be

X. H. Liu, M. Oka and Q. Zhao,
PLB 753, 297-302 (2016)

2. Width of the internal particle of the loop



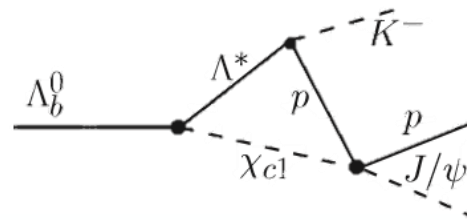
Achasov, Kozhevnikov, Sobolev IM,
Shestakov PRD 92 (2015) 3, 036003



3. Unknown vertex

Guo, Meißner, Wang, Yang,
PRD92, 071502 (2015)

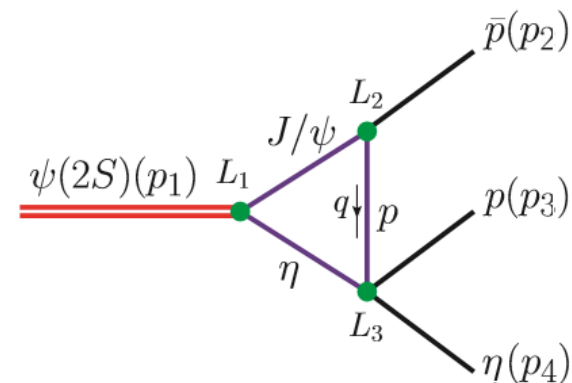
$$\begin{aligned} \Lambda_b &\rightarrow (c\bar{c})\Lambda^* \\ &\rightarrow (c\bar{c})\Lambda K^- \\ &\rightarrow J/\psi p K^- \end{aligned}$$



First proposal

1. Threshold

Far away from $p\eta$ threshold. Singularity point is 1.563 GeV of $p\eta$ invariant mass.

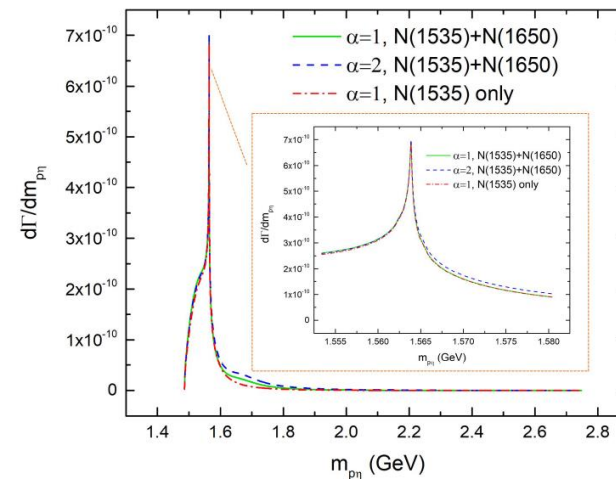


2. Width of the internal particle of the loop

All narrow internal particles, J/ψ , p , η

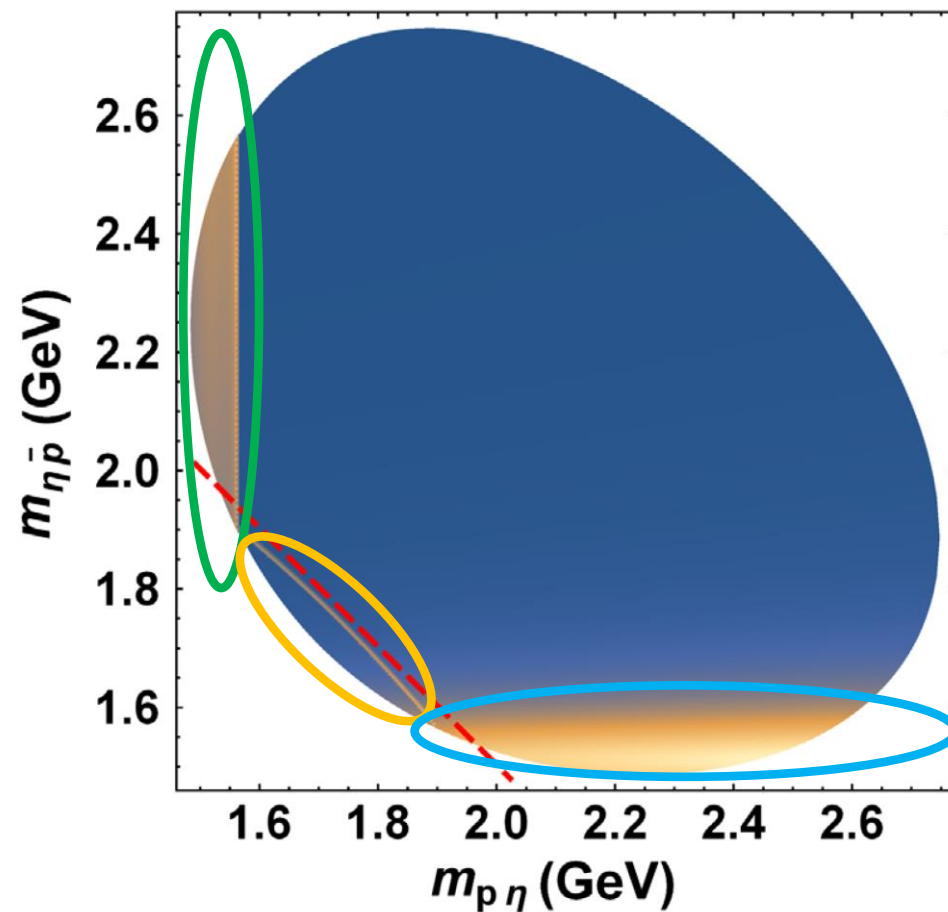
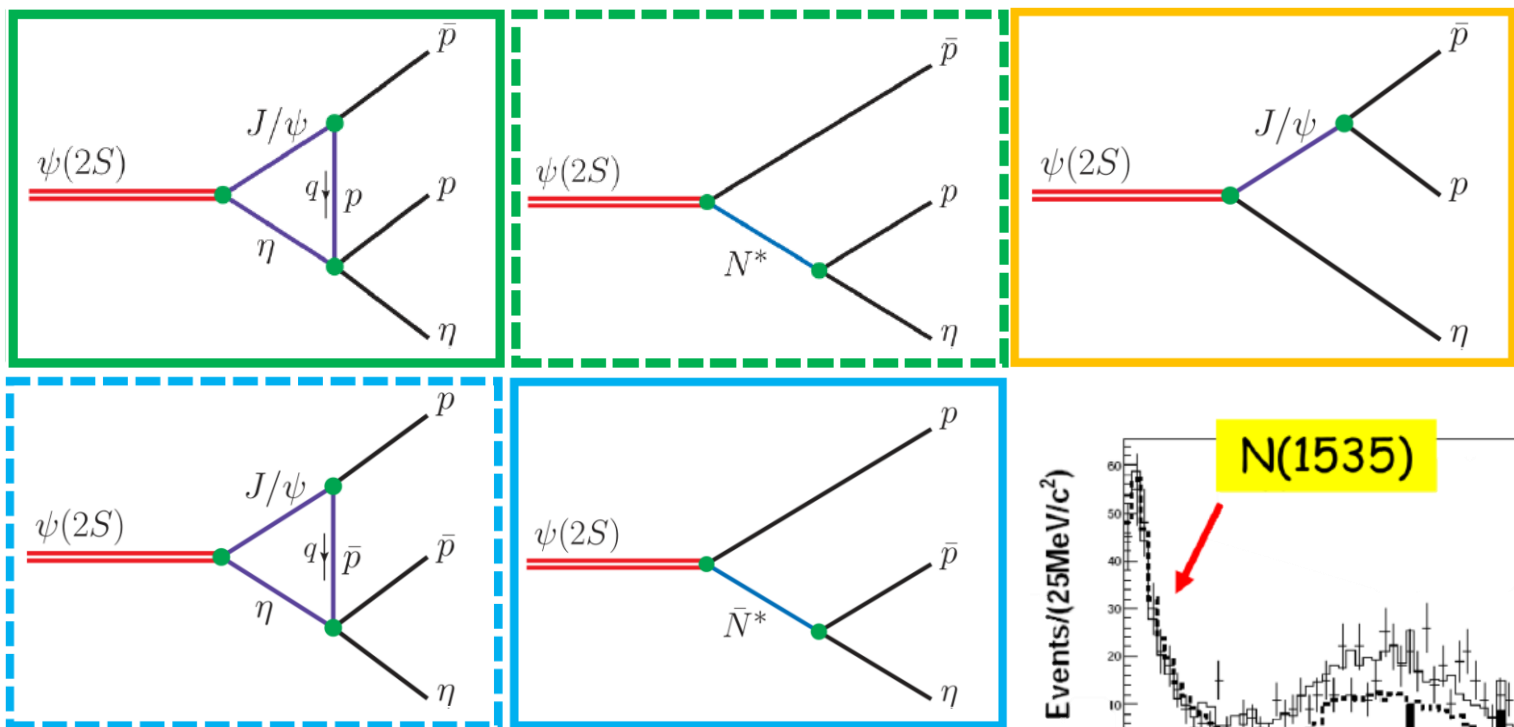
3. Unknown vertex

All vertices are constrained from experimental data



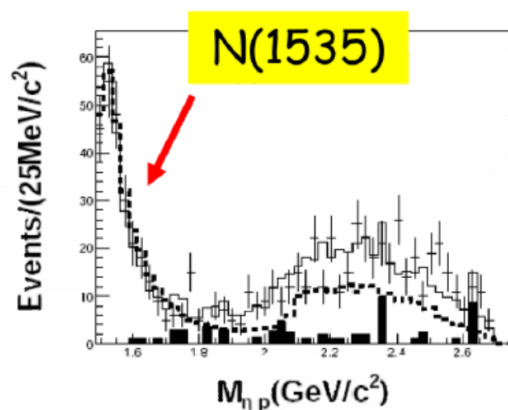
First proposal

Signal + Background



Take a cut to remove the contribution of J/ψ tree diagram as done in BESIII

$$m_{p\bar{p}} < 3.067 \text{ GeV}$$



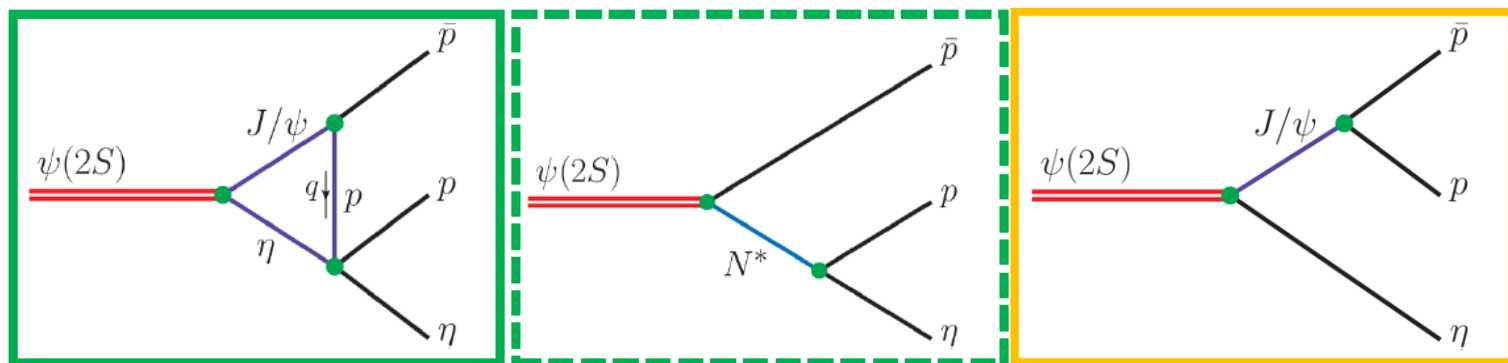
BESIII PRD 88, 032010 (2013)



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First proposal

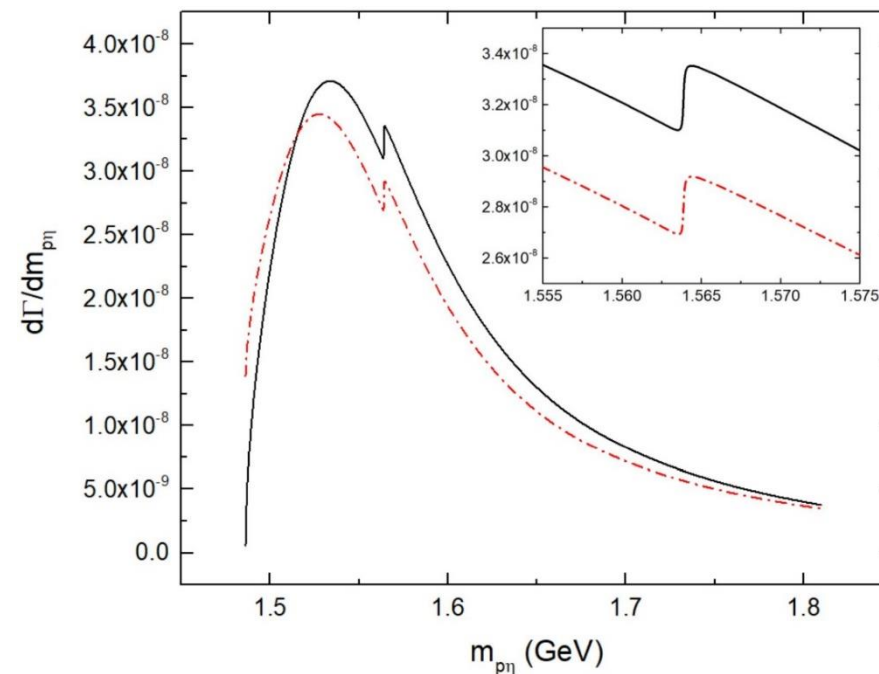
Signal + Background



1. There exists a visible enhancement at the right shoulder of N(1535).
2. The width of the peak is enlarged to 5 MeV.
3. The enhancement of the peak VS the tree diagram is about 10%.

Weakness:

1. Ask for high resolution, 2-3 MeV,
2. Generated from interference between TS and BG with an assumption that phase is 0.



4 billion $\psi(2S) \Rightarrow$ about 120 events.



Second proposal– Moving Triangle singularity

1.Threshold

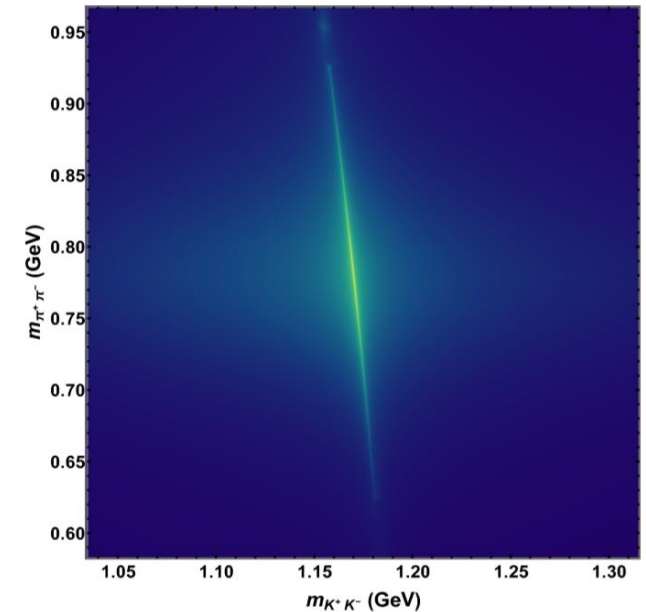
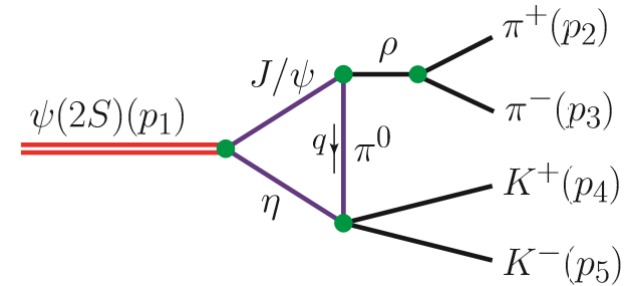
Far away from $\pi\eta$ threshold. Singularity point is from 1.158–1.181 GeV of $K\bar{K}$ invariant mass with the width of ρ .

2.Width of the internal particle of the loop

All narrow internal particles, J/ψ , π , η

3.Unknow vertex

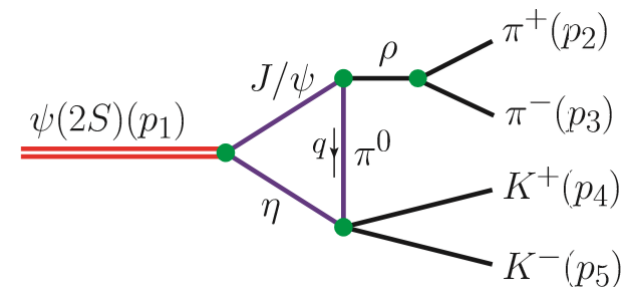
All vertices are constrained from experimental data



Second proposal– Moving Triangle singularity

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Far away from $\pi\eta$ threshold. Singularity point is from 1.158–1.181 GeV of $K\bar{K}$ invariant mass with the width of ρ .



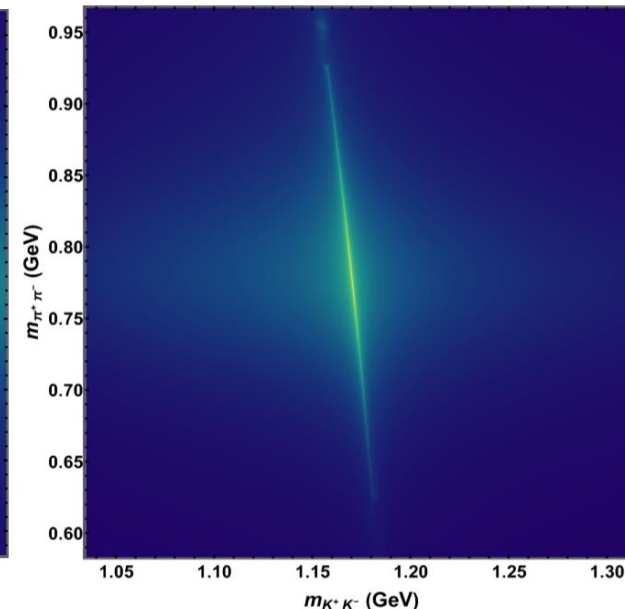
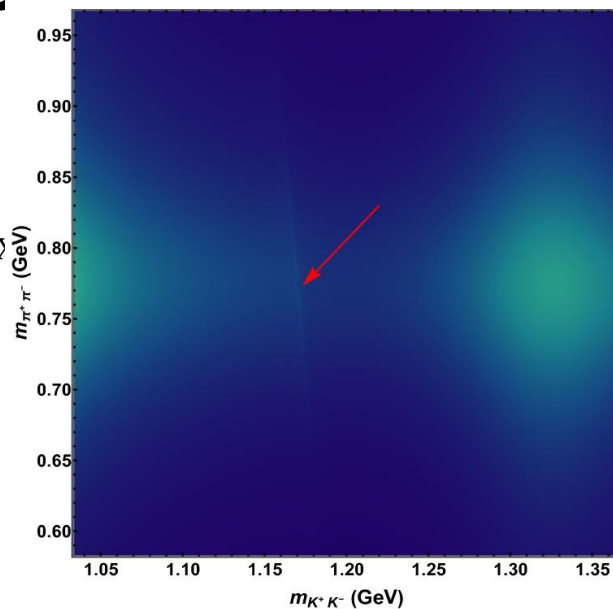
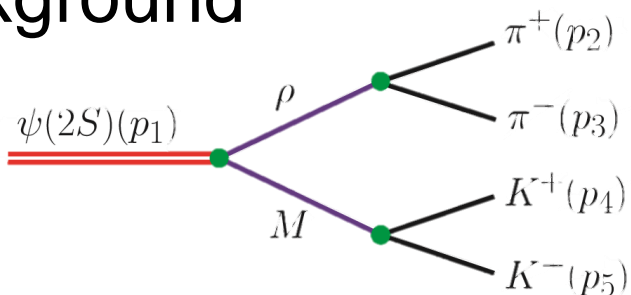
2.Width of the internal particle of the loop

All narrow internal particles, J/ψ ,

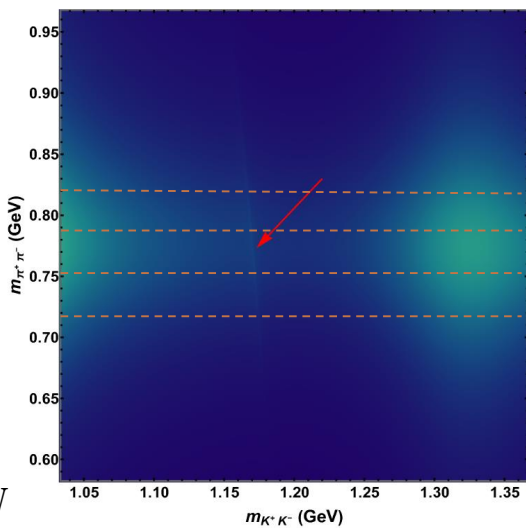
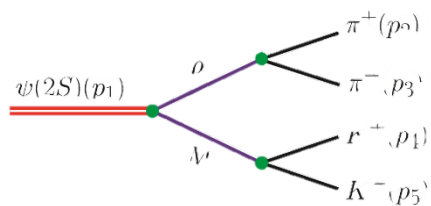
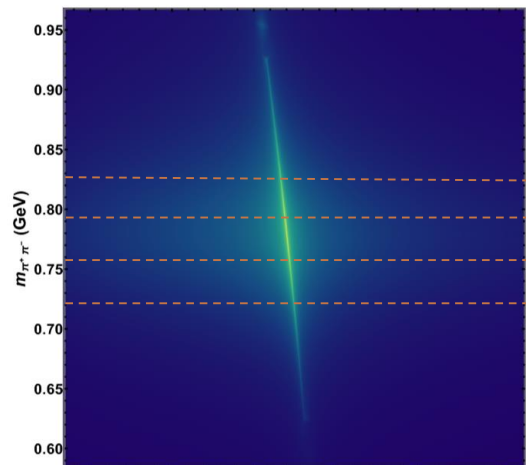
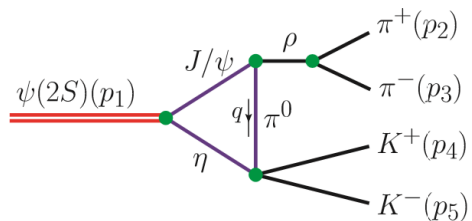
3.Unknow vertex

All vertices are constrained from ex

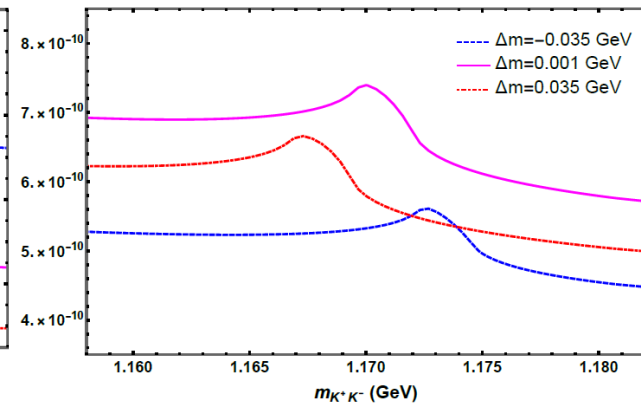
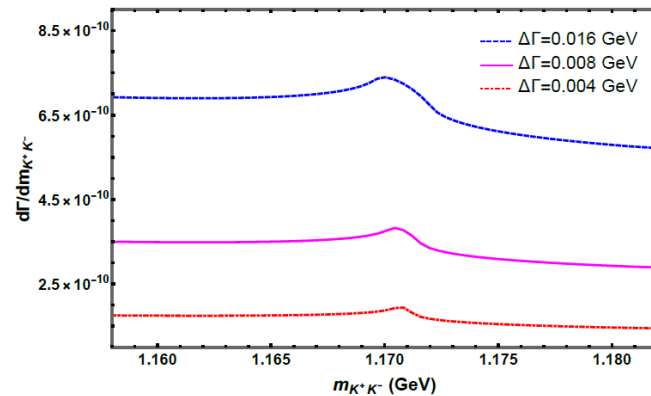
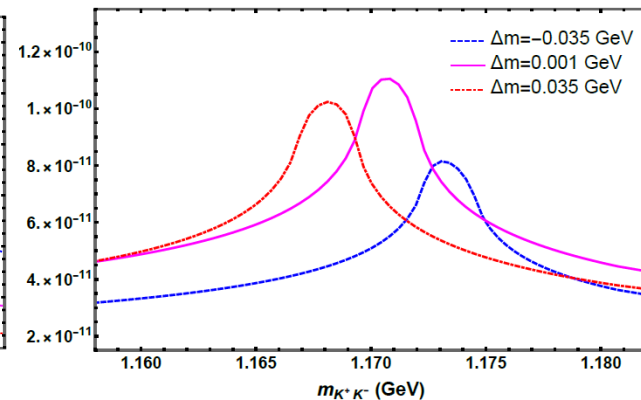
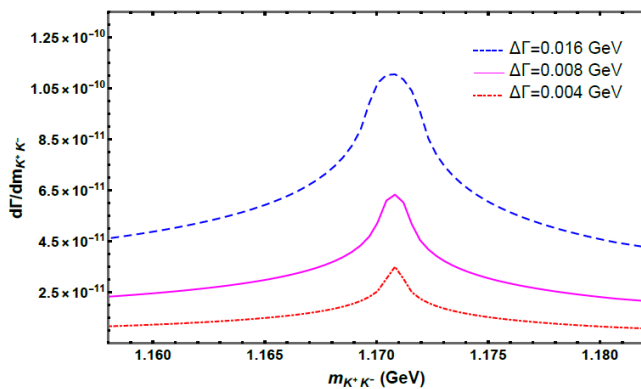
Background



Second proposal– Moving Triangle singularity



4 billion $\psi(2S)$
 \rightarrow about 10 events/MeV



Two important parameters,
 $\Delta\Gamma$: the width of bin; Δm : the distance from the
 center mass of ρ .



Summary

We discuss how to confirm the Triangle Singularity, we should consider the following three points,

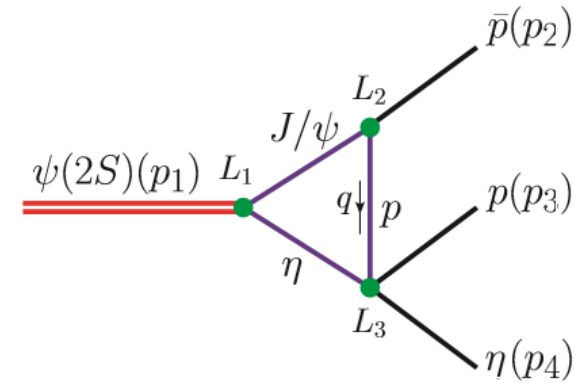
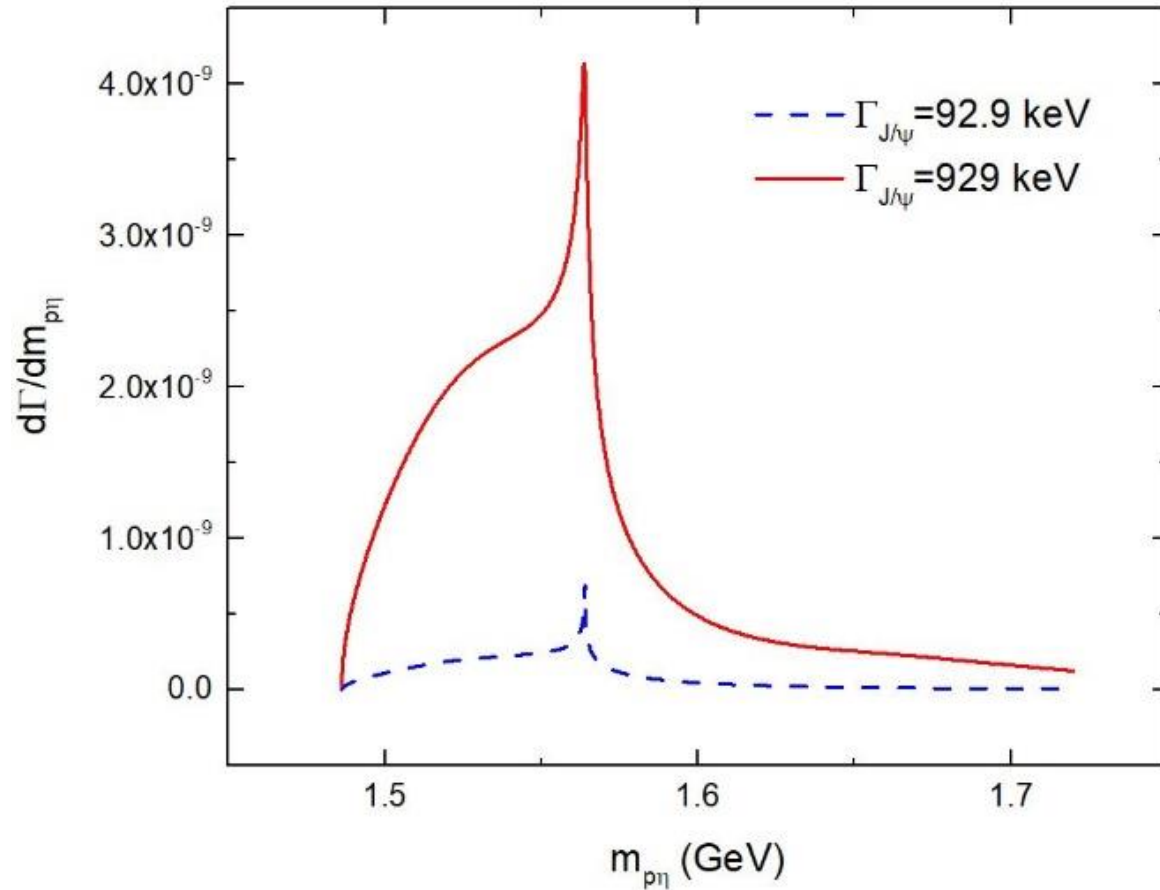
1. Threshold
2. Width of the internal particle of the loop
3. Unknow vertex

Then we propose two processes $\psi(2s) \rightarrow p \bar{p} \eta$ through J/ψ , p , η loop and $\psi(2s) \rightarrow \rho KK \rightarrow \pi\pi KK$ through J/ψ , π , η loop.

But the signals of both two processes are not very stronger. 🙄



More discussion



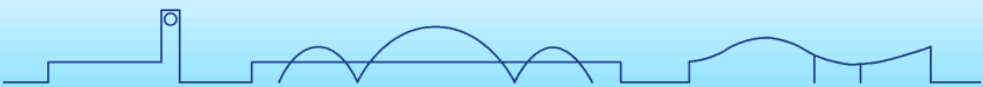
$$\sim \sqrt{\Gamma_{J/\psi \rightarrow p\bar{p}}} \ln \Gamma_{J/\psi}$$

V. R. Debastiani¹, S. Sakai, E. Oset EPJC 79, 69 (2019)

We will continue to find some broader states with width around 10 MeV.



Thanks for attention!



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