

Nucleon and nuclear structure from muonic and normal atoms

Is the proton radius puzzle solved?



Randolf Pohl

Johannes Gutenberg
Universität Mainz



Chiral Dynamics Beijing
(virtual)
19. Nov. 2021



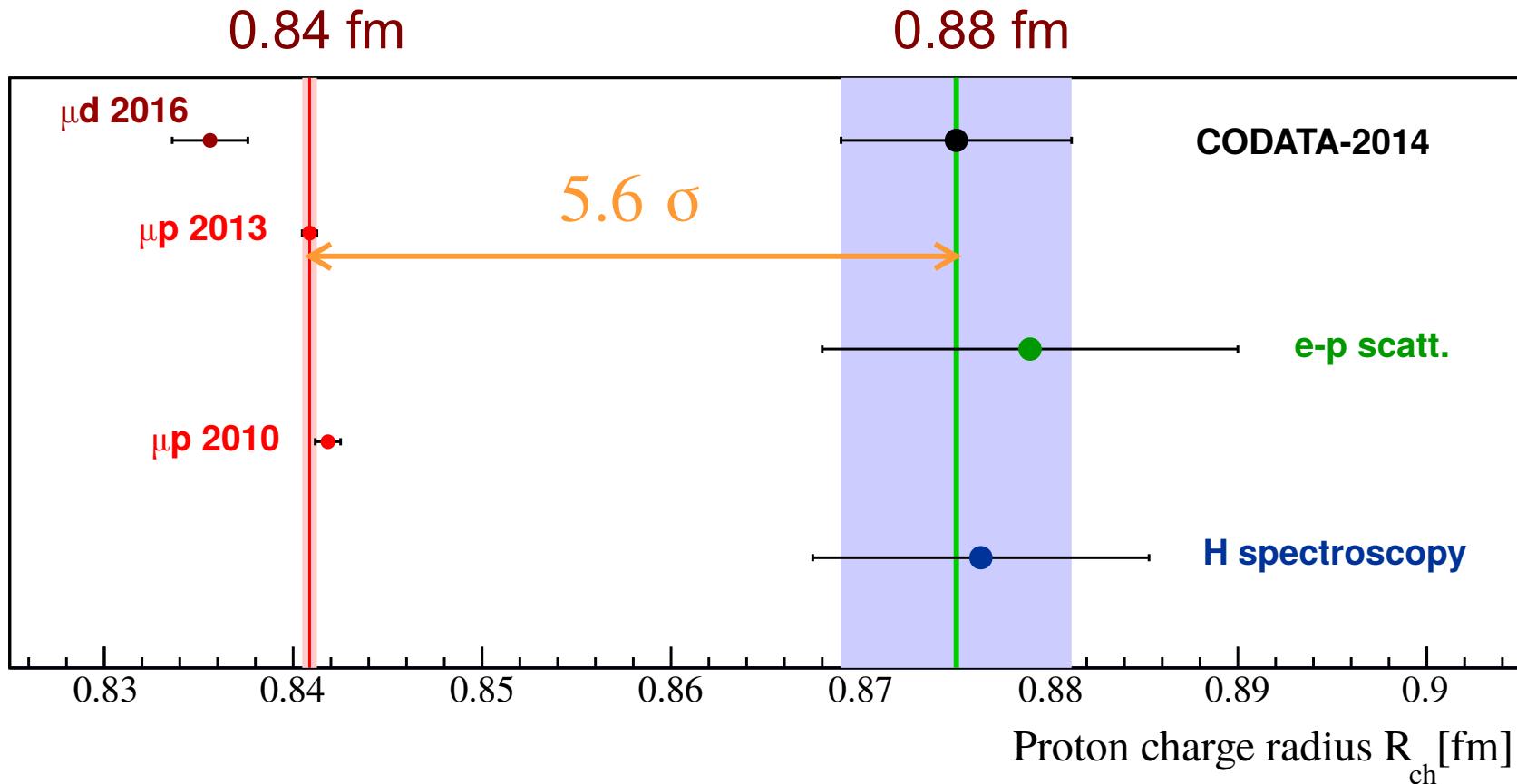
Group at JGU Mainz



The “Proton Radius Puzzle”

Measuring R_p using **electrons**: 0.88 fm ($\pm 0.7\%$)

using **muons**: 0.84 fm ($\pm 0.05\%$)



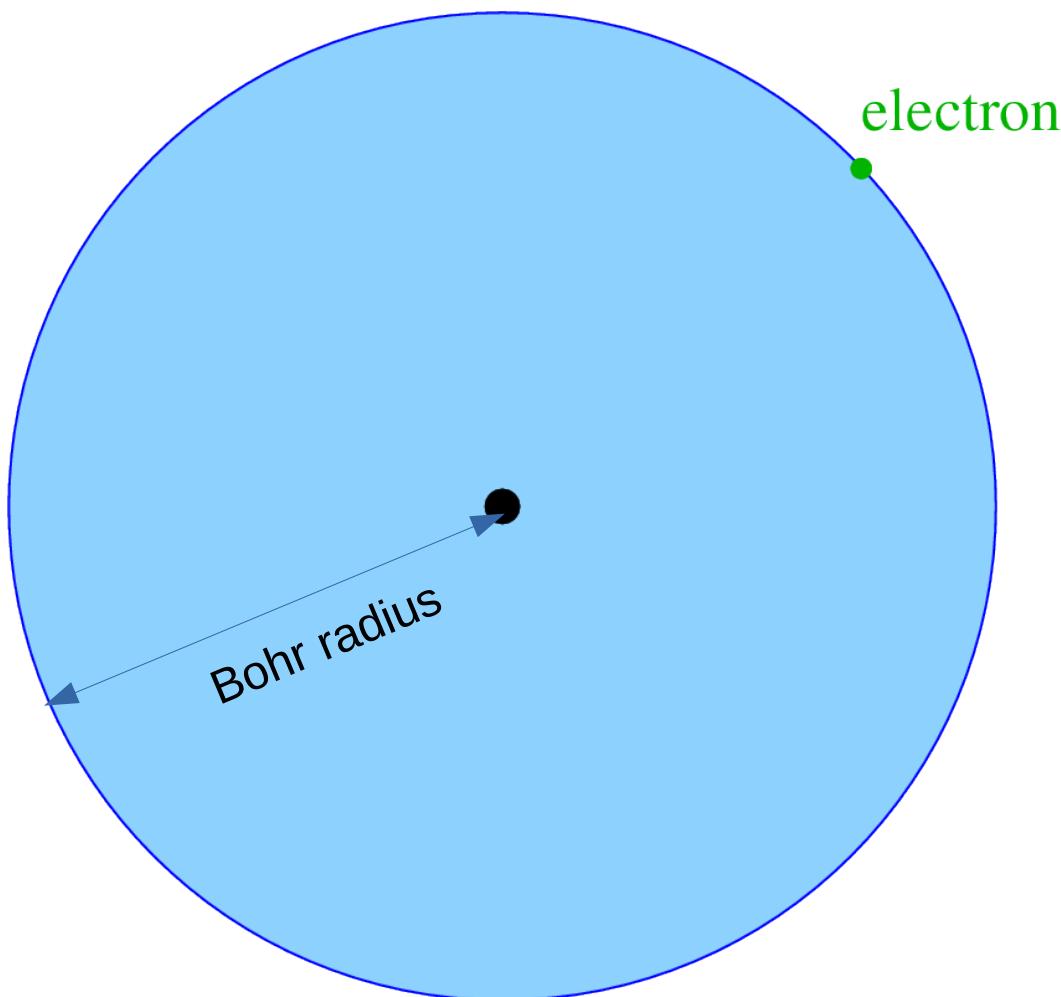
μd 2016: RP et al (CREMA Coll.) Science 353, 669 (2016)

μp 2013: A. Antognini, RP et al (CREMA Coll.) Science 339, 417 (2013)

Electronic and muonic atoms

Regular hydrogen:

Proton + Electron



Muonic hydrogen:

Proton + Muon

Muon mass = **200** * electron mass

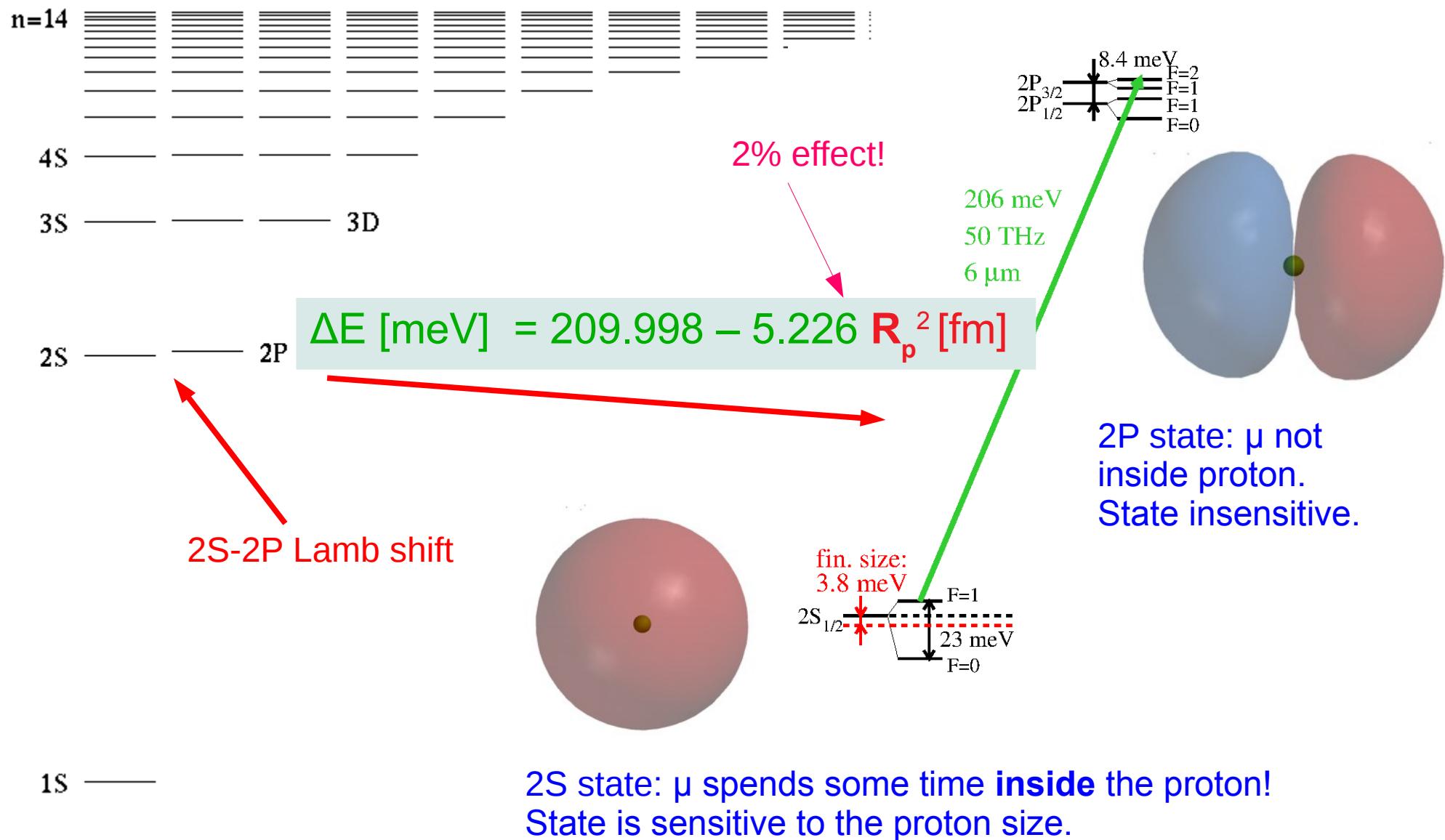
Bohr radius = **1/200** of H

200^3 = a **few million times**
larger wave function overlap
==
more sensitive to proton size

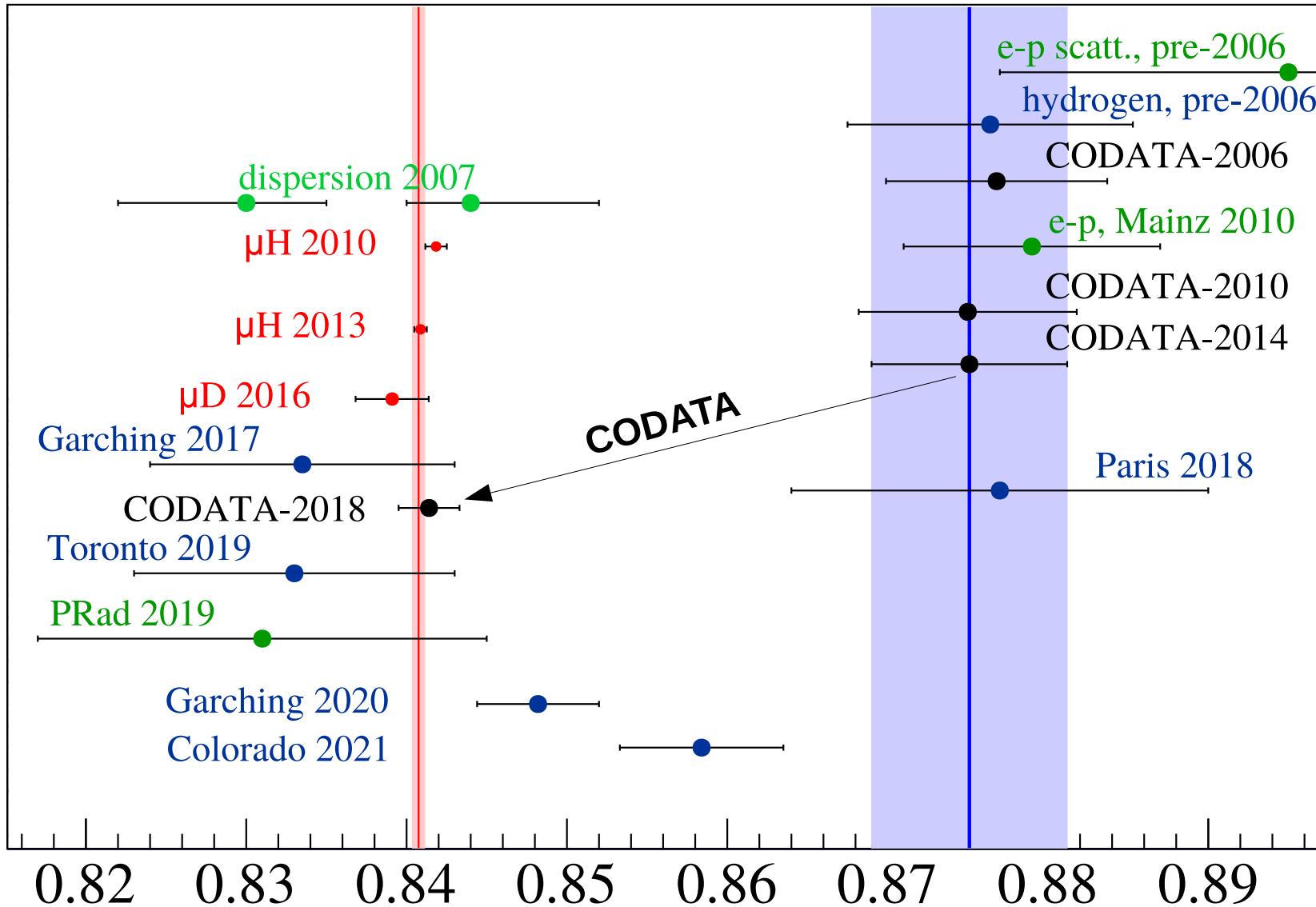


Vastly not to scale!!

Lamb shift in Muonic Hydrogen



The situation in 2021

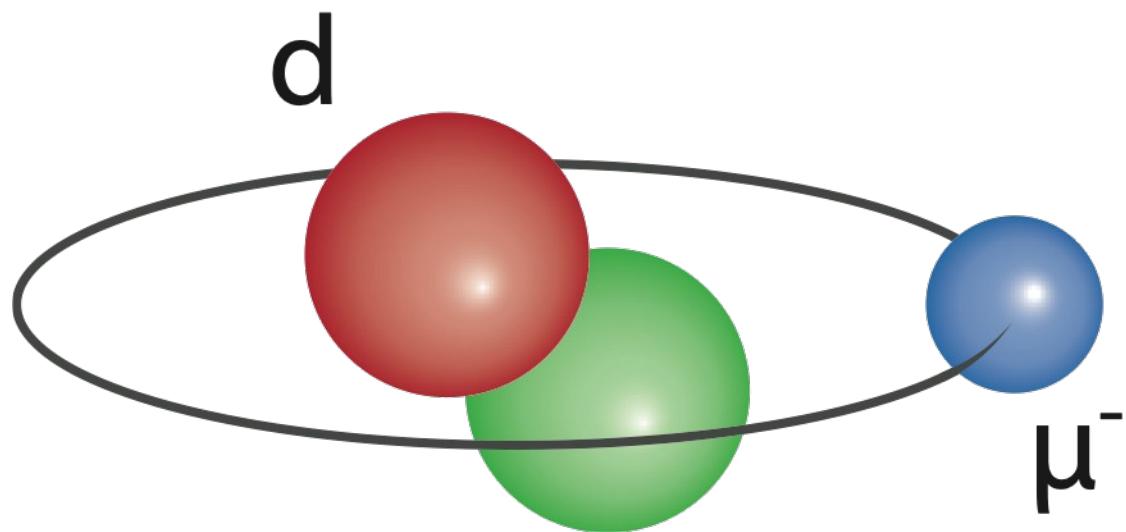


Colorado: Brandt et al., 2111.08554

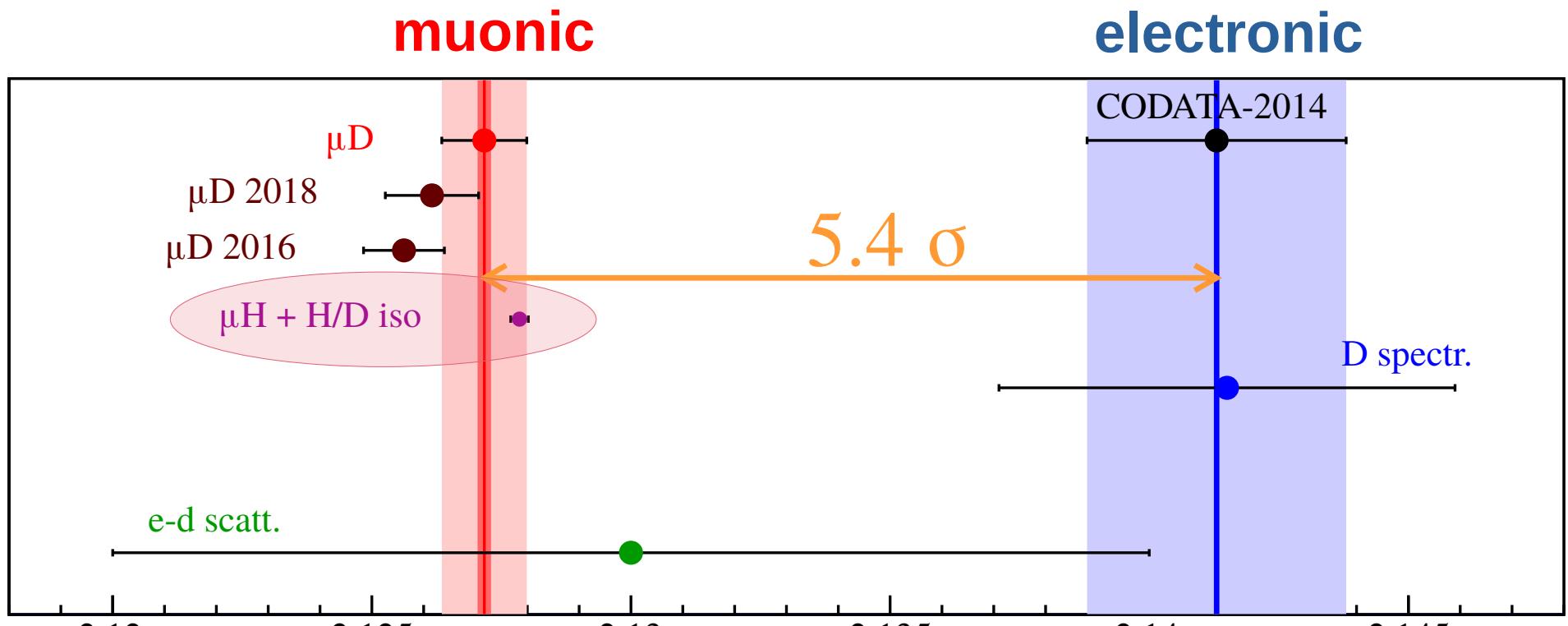
proton charge radius [fm]

Proton charge radius puzzle “solved”?

Muonic Deuterium



Muonic Deuterium



μD : $2.12717 \text{ (13)}_{\text{exp}} \text{ (82)}_{\text{theo}} \text{ fm}$ (theo = nucl. polarizability)

$\mu H + H/D(1S-2S)$: 2.12785 (17) fm

CODATA-2014: 2.14130 (250) fm

$$\text{H/D 1S-2S isotope shift: } r_d^2 - r_p^2 = 3.82070(31) \text{ fm}^2$$

Pachucki et al., PRA 97, 062511 (2018)

μD : RP et al. (CREMA) Science 353, 669 (2016)

H/D 1S-2S. Parthey, RP et al., PRL 104, 233001 (2010), PRL 107, 203001 (2011)

Theory in muonic D

$$\Delta E_{\text{Lamb}}^{\mu D} = 228.7854 \text{ (13) meV}_{\text{QED}} + 1.7500 \text{ (210) meV}_{\text{TPE}} - 6.1103 \text{ (3) meV/fm}^2 * R_d^2$$



ΔE_{TPE} (theo) = 1.7500 +- 0.0210 meV (Kalinowski, 2018)

vs. +- 0.0034 meV experimental uncertainty

(1) charge radius, using calculated TPE

$r_d(\mu D)$ = 2.12717 (13) _{exp} (82) _{theo} fm vs.

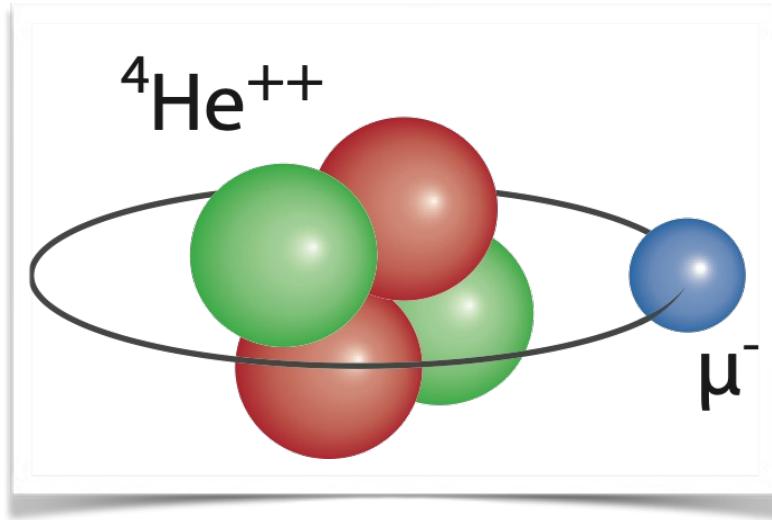
r_d (CODATA-14) = 2.14130 (250) fm

(2) polarizability, using charge radius from isotope shift

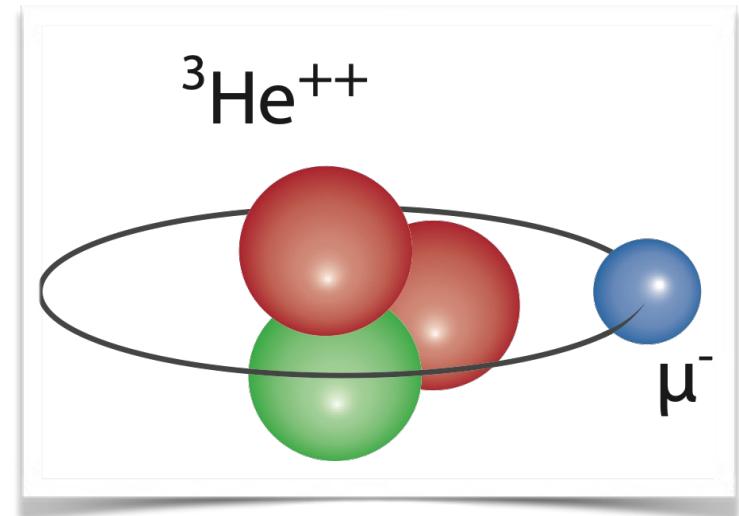
ΔE_{TPE} (theo) = 1.7500 (210) meV vs.

ΔE_{TPE} (exp) = 1.7591 (59) meV 3.5x more accurate

Muonic Helium



Krauth et al. (CREMA), Nature (2021)



Measured

Theory in muonic He-3

$$\Delta E_{\text{Lamb}}^{\mu^3\text{He}_-} = 1644.4820(149)_{\text{QED}} + 15.3000(5200)_{\text{TPE}} - 103.5184(10) * R_h^2 / \text{fm}^2 \quad [\text{meV}]$$

$$\Delta E_{\text{Lamb}}^{\mu^D} = 228.7854 (13)_{\text{QED}} + 1.7500 (210)_{\text{TPE}} - 6.1103 (3) * R_d^2 / \text{fm}^2 \quad [\text{meV}]$$

$$\Delta E_{\text{Lamb}}^{\mu^H} = 206.0336 (15)_{\text{QED}} + 0.0332 (20)_{\text{TPE}} - 5.2275(10) * R_p^2 / \text{fm}^2 \quad [\text{meV}]$$

Annals of Physics 331 (2013) 127–145

Annals of Physics 366 (2016) 168–196



Contents lists available at ScienceDirect
Eur. Phys. J. D (2017) 71: 341
DOI: 10.1140/epjd/e2017-80296-1

THE EUROPEAN
PHYSICAL JOURNAL D

Topical Review

Theory of the
splitting in muonic

Aldo Antognini^{a,*},
François Nez^b, Raïf

^a Institute for Particle Physics, E

^b Laboratoire Kastler Brossel, Éc

^c Max-Planck-Institut für Quan

Theory of the $n = 2$ levels in muonic helium-3 ions

Beatrice Franke^{1,2,a}, Julian J. Krauth^{1,3,b}, Aldo Antognini^{4,5}, Marc Diepold¹, Franz Kottmann⁴,
and Randolph Pohl^{3,1,c}

Theory of the $n = 2$ levels in muonic helium-3 ions

¹ Max-Planck-Institut für Quantenoptik, 85748 Garching, Germany

² TRIUMF, 4004 Wesbrook Mall, Vancouver, BC V6T 2A3, Canada

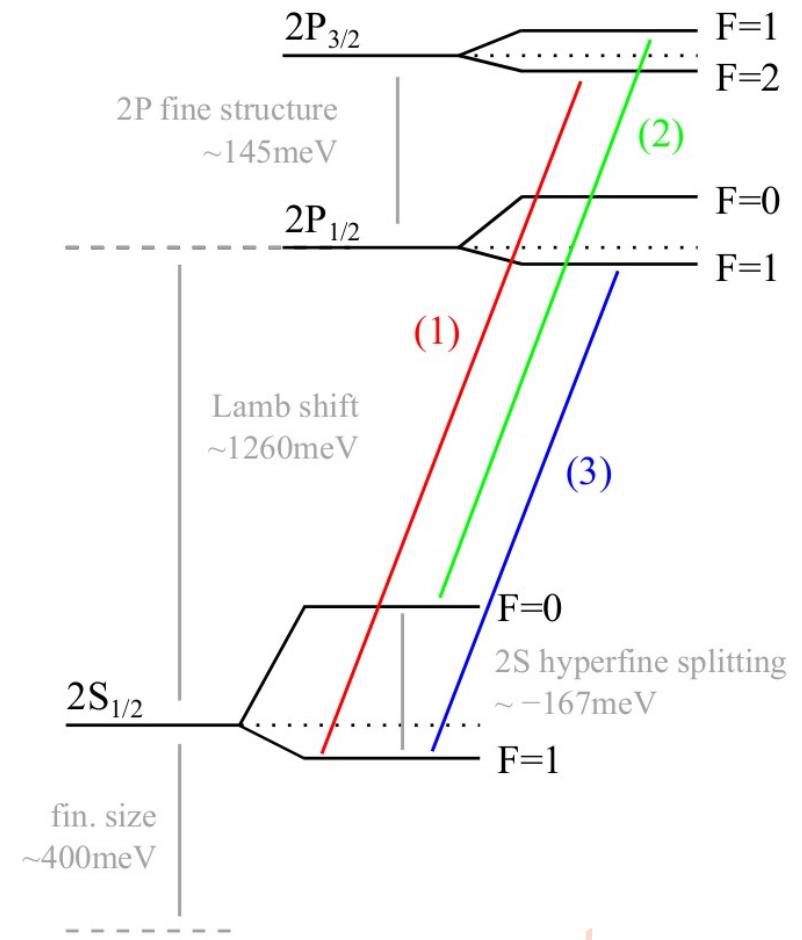
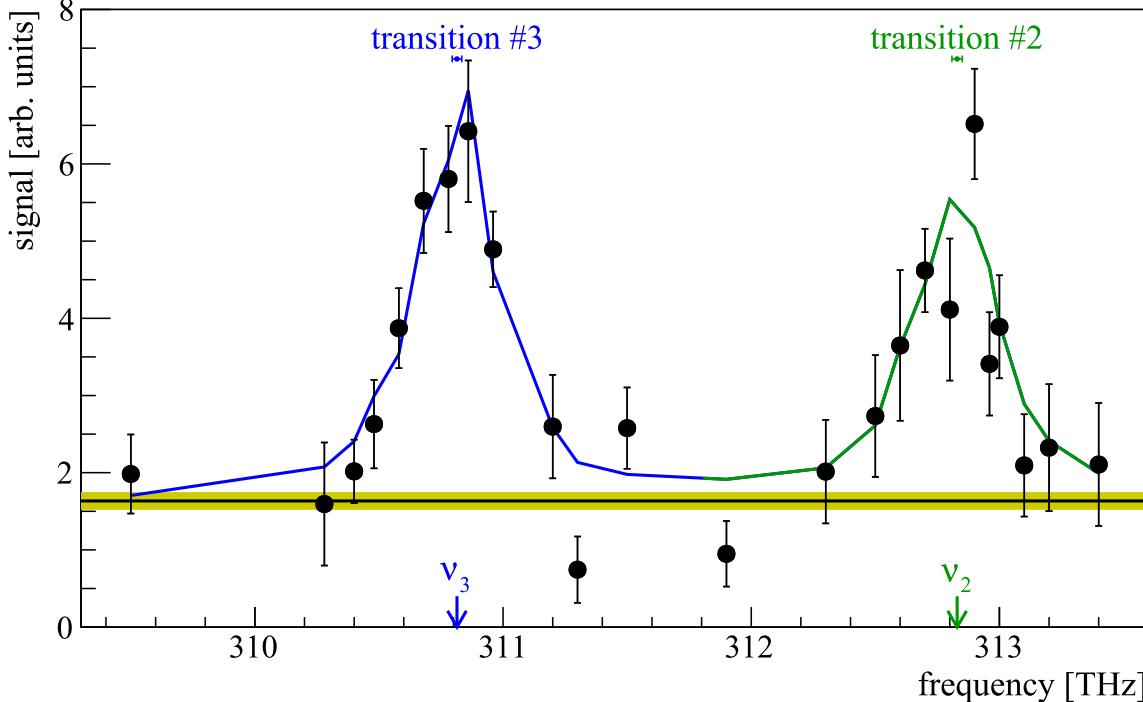
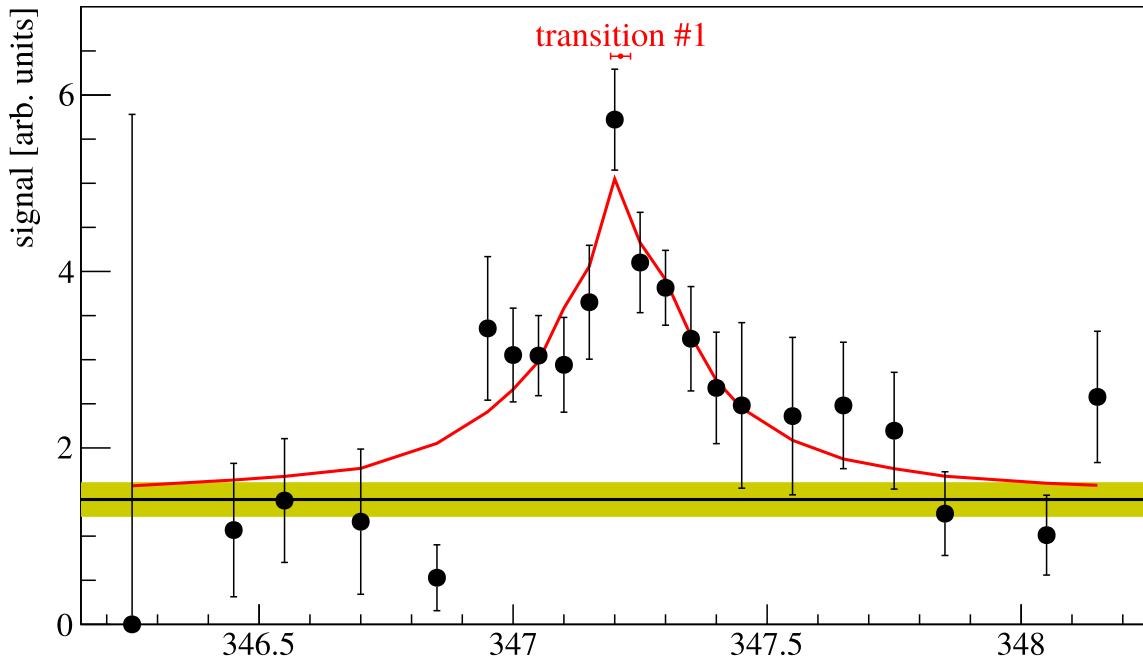
³ Johannes Gutenberg-Universität Mainz, QUANTUM, Institut für Physik & Exzellenzcluster PRISMA,
55099 Mainz, Germany

⁴ Institute for Particle Physics and Astrophysics, ETH Zurich, 8093 Zurich, Switzerland

⁵ Paul Scherrer Institute, 5232 Villigen, Switzerland

Three-photon contribution still missing (Pachucki et al., PRA 97, 052511 (2018))

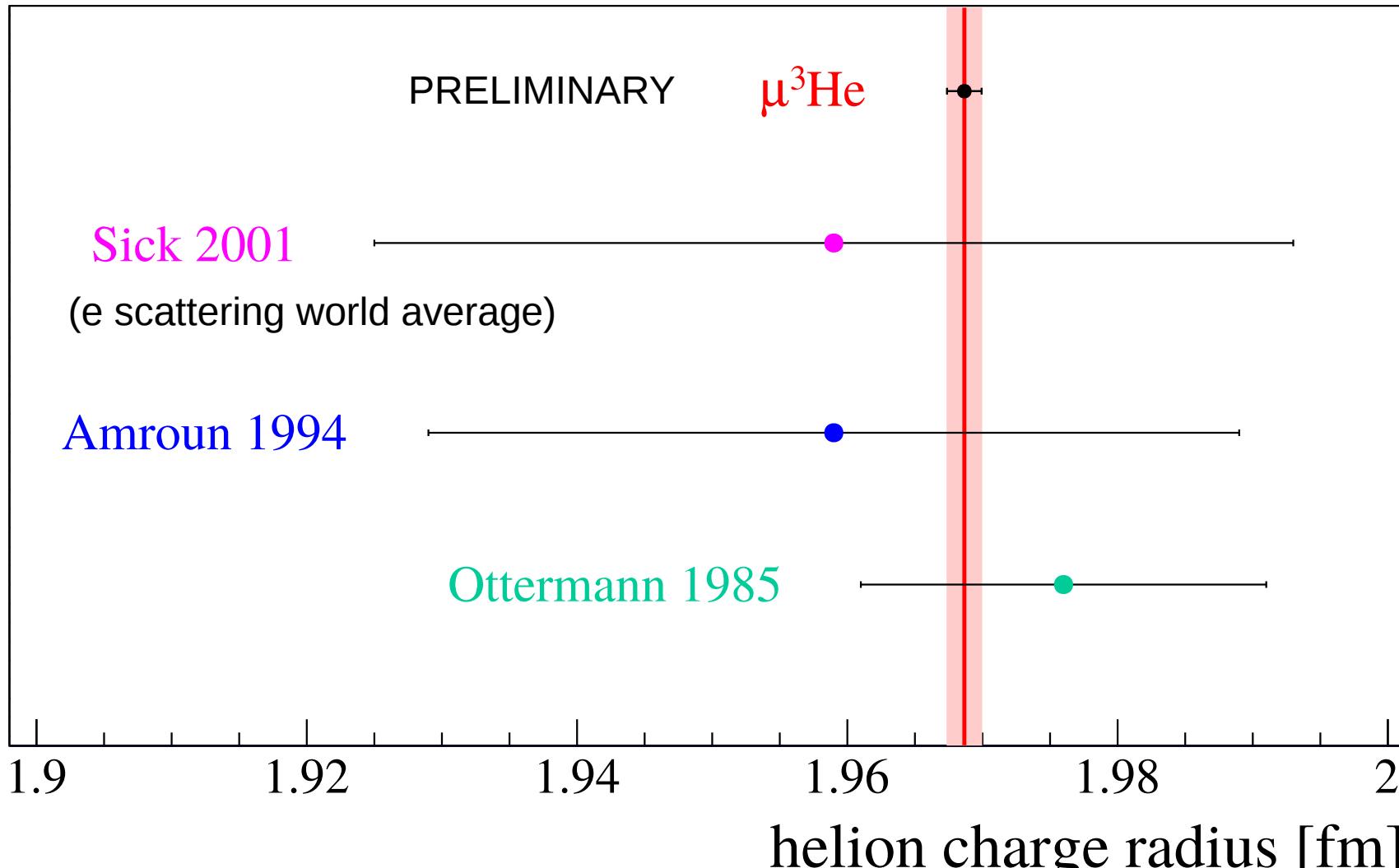
muonic ${}^3\text{He}$ ions



$$R({}^3\text{He}) = 1.96866 (12)_{\text{exp}} (128)_{\text{theo}} \text{ fm}$$

Theory: Franke et al., EPJD (2017),
but 3-photon (Pachucki et al.) ?!?!
PRELIMINARY

Muonic Helium-3



prel. accuracy: exp **+ - 0.00012 fm**, theo **+ - 0.00128 fm** (nucl. polarizability)

Theory: see Franke et al. EPJ D 71, 341 (2017) [1705.00352]

Theory in muonic He-4

$$\Delta E_{\text{Lamb}}^{\mu^4\text{He}} = 1668.5670(178)_{\text{QED}} + 9.9000(2800)_{\text{TPE}} - 106.3540(80) * R_\alpha^{-2} / \text{fm}^2 \quad [\text{meV}]$$

$$\Delta E_{\text{Lamb}}^{\mu^3\text{He}} = 1644.4820(149)_{\text{QED}} + 15.3000(5200)_{\text{TPE}} - 103.5184(10) * R_h^{-2} / \text{fm}^2 \quad [\text{meV}]$$

$$\Delta E_{\text{Lamb}}^{\mu\text{D}} = 228.7854 (13)_{\text{QED}} + 1.7500 (210)_{\text{TPE}} - 6.1103 (3) * R_d^{-2} / \text{fm}^2 \quad [\text{meV}]$$

$$\Delta E_{\text{Lamb}}^{\mu\text{H}} = 206.0336 (15)_{\text{QED}} + 0.0332 (20)_{\text{TPE}} - 5.2275(10) * R_p^{-2} / \text{fm}^2 \quad [\text{meV}]$$

Annals of Physics 331 (2013) 127–145

Annals of Physics 396 (2018) 220–244



Theory of the
splitting in muonic
He-4 ions

Aldo Antognini^{a,*},
François Nez^b, Raoul

^a Institute for Particle Physics, E
^b Laboratoire Kastler Brossel, Éc
^c Max-Planck-Institut für Quanten

Theory of the Lamb Shift and fine structure in muonic ^4He ions and the muonic ^3He – ^4He Isotope Shift

Julian J. Kraut¹, Aldo Antognini¹, Beatrice Franke^{1,2,a}, Julian Pohl^{3,1,c}

¹ Max-Planck-Institut für Quantenoptik, Garching, Germany
² TRIUMF, 4004 Wesbrook Mall, Vancouver, BC V6T 2A6, Canada
³ Johannes Gutenberg-Universität Mainz, D-55099 Mainz, Germany
^a Institute for Particle Physics, University of Bonn, Bonn, Germany
^b Paul Scherrer Institute, 5232 Villigen, Switzerland

Three-photon contribution estimation included (Pachucki et al., PRA 97, 052511 (2018))

Annals of Physics



Eur. Phys. J. D (2017) 71: 34
DOI: 10.1140/epjd/e2017-802

Topical Review

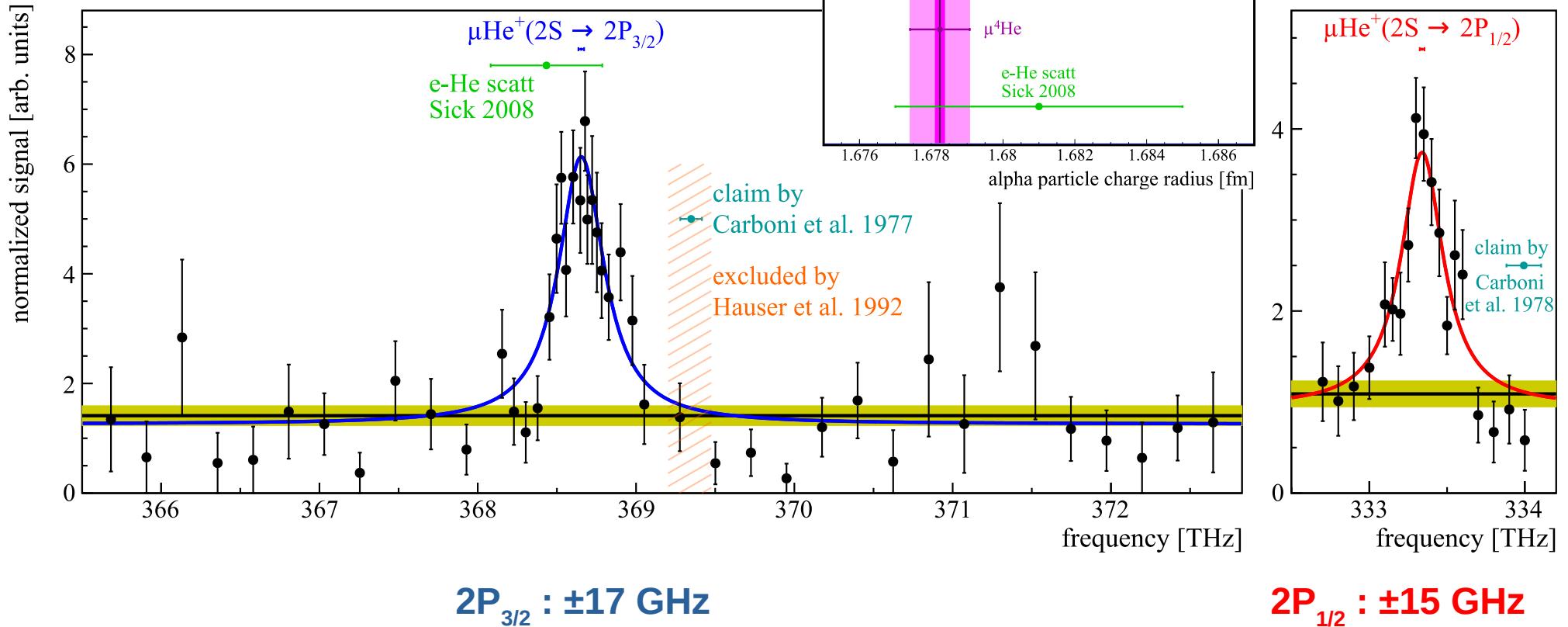


Contents lists available at ScienceDirect

Annals of Physics

journal homepage: www.elsevier.com/locate/aop

muonic ${}^4\text{He}$ ions



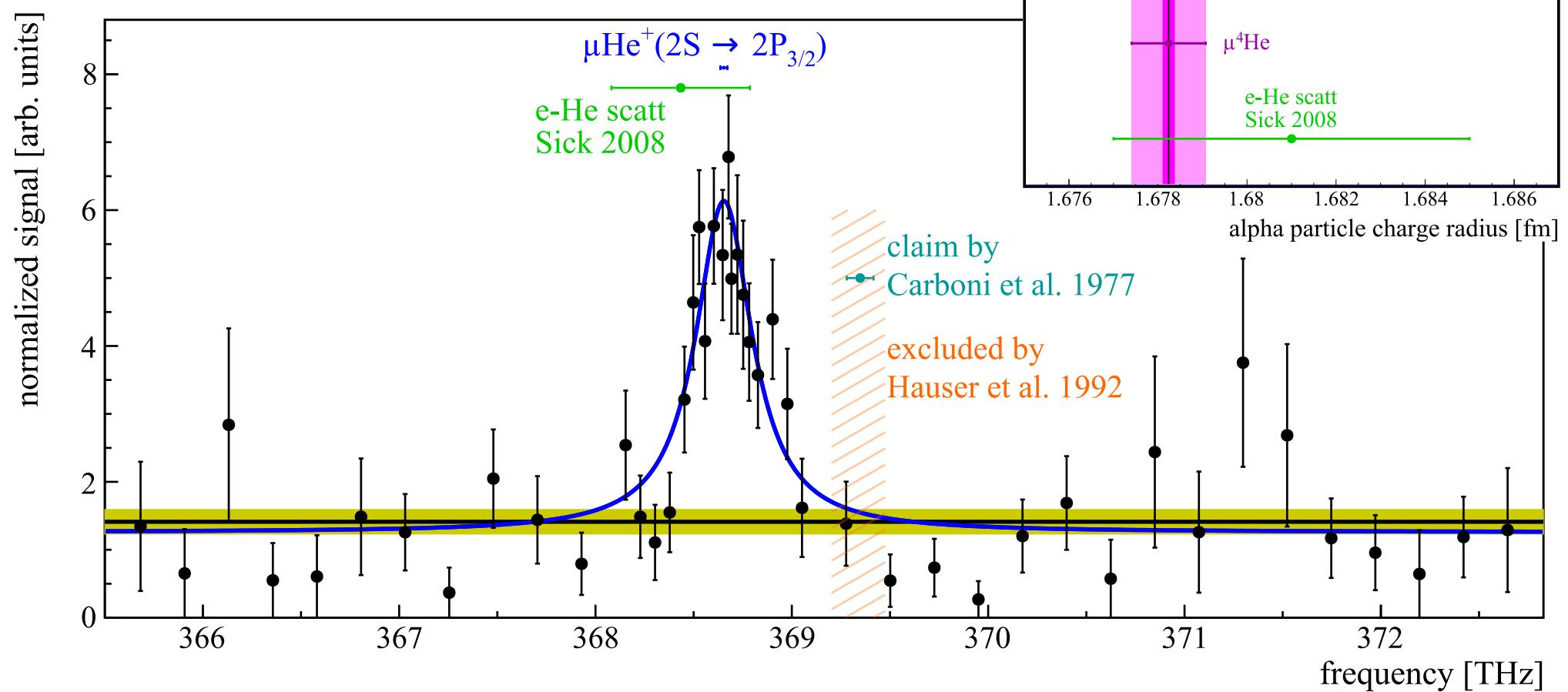
$$R({}^4\text{He}) = 1.67824 (13)_{\text{exp}} (82)_{\text{theo}} \text{ fm}$$

$$(82)_{\text{theo}} = (70)_{\text{2PE}} (42)_{\text{3PE}}$$

Theory: Diepold et al., Ann. Phys. (2018)
incl. 3-photon nuclear polarizability (Pachucki, 2018)

Krauth, RP et al. (CREMA Coll.)
Nature 589, 527 (2021)

muonic ${}^4\text{He}$ ions



$$R({}^4\text{He}) = 1.67824 (13)_{\text{exp}} (82)_{\text{theo}} \text{ fm}$$

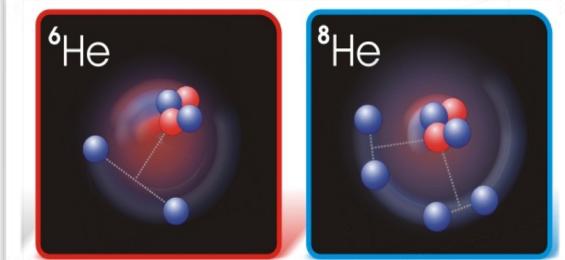
Krauth, RP et al. (CREMA Coll.)
Nature 589, 527 (2021)

Theory: Diepold et al., Ann. Phys. (2018)
incl. 3-photon nuclear polarizability (Pachucki, 2018)

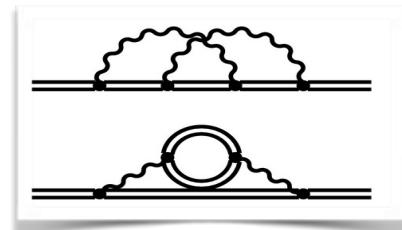
Impact of $\mu^4\text{He}^+$ measurements

Few-nucleon theories

- ▶ r_α represents a benchmark for few-nucleon theories.
- ▶ r_α can be used also to fix a low-energy constant of nuclear potential.
- ▶ r_α improves ${}^6\text{He}$ and ${}^8\text{He}$ radii

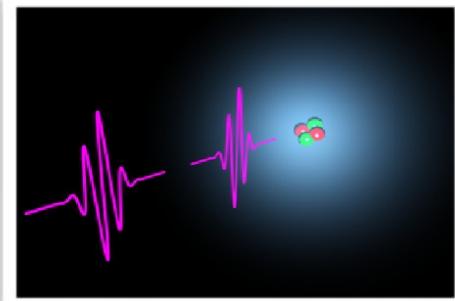


Müller, Lu



BSM physics

- ▶ Agreement constrains BSM models suggested to explain the R_p puzzle



Udem, MPQ
Eikema, LaserLab

Combined with upcoming He^+ (He) exp.

- ▶ bound-state QED test $\text{He}^+(1\text{S}-2\text{S})$:
60 kHz, $u_r = 6 \times 10^{-12}$
- ▶ Rydberg constant: 24 kHz
- ▶ **2PE+3PE in μHe with 0.1 meV uncertainty**

from A. Antognini

Conclusions

Muonic atoms / ions provide:

- **~10x more accurate charge radii**, when combined with
calculated polarizability

Conclusions

Muonic atoms / ions provide:

- **~10x more accurate charge radii**, when combined with **calculated polarizability**

^3He	^4He
1.9687* (13) 1.9730 (160)	1.6782 (8) 1.6810 (40)

^1H	^2D	^3T
0.8409 (4) 0.8751 (61)	2.1277 (2) 2.1413 (25)	1.7550 (860)

* = preliminary



The New York Times

Intermediate conclusions

Muonic atoms / ions provide:

- **~10x more accurate charge radii**, when combined with **calculated polarizability**
- few times more accurate **nuclear polarizability**,
when combined with **charge radius from regular atoms**

Muonic atoms are a novel tool for proton and new-nucleon properties!

Intermediate conclusions

Proton radius situation:

- smaller radii from **muonic hydrogen** and **deuterium** imply a **smaller Rydberg** constant
- new H(2S-4P), H(2S-2P), H(1S-3S) give a **smaller proton radius**
- new H(1S-3S) however **confirms large proton radius**

More data coming in!

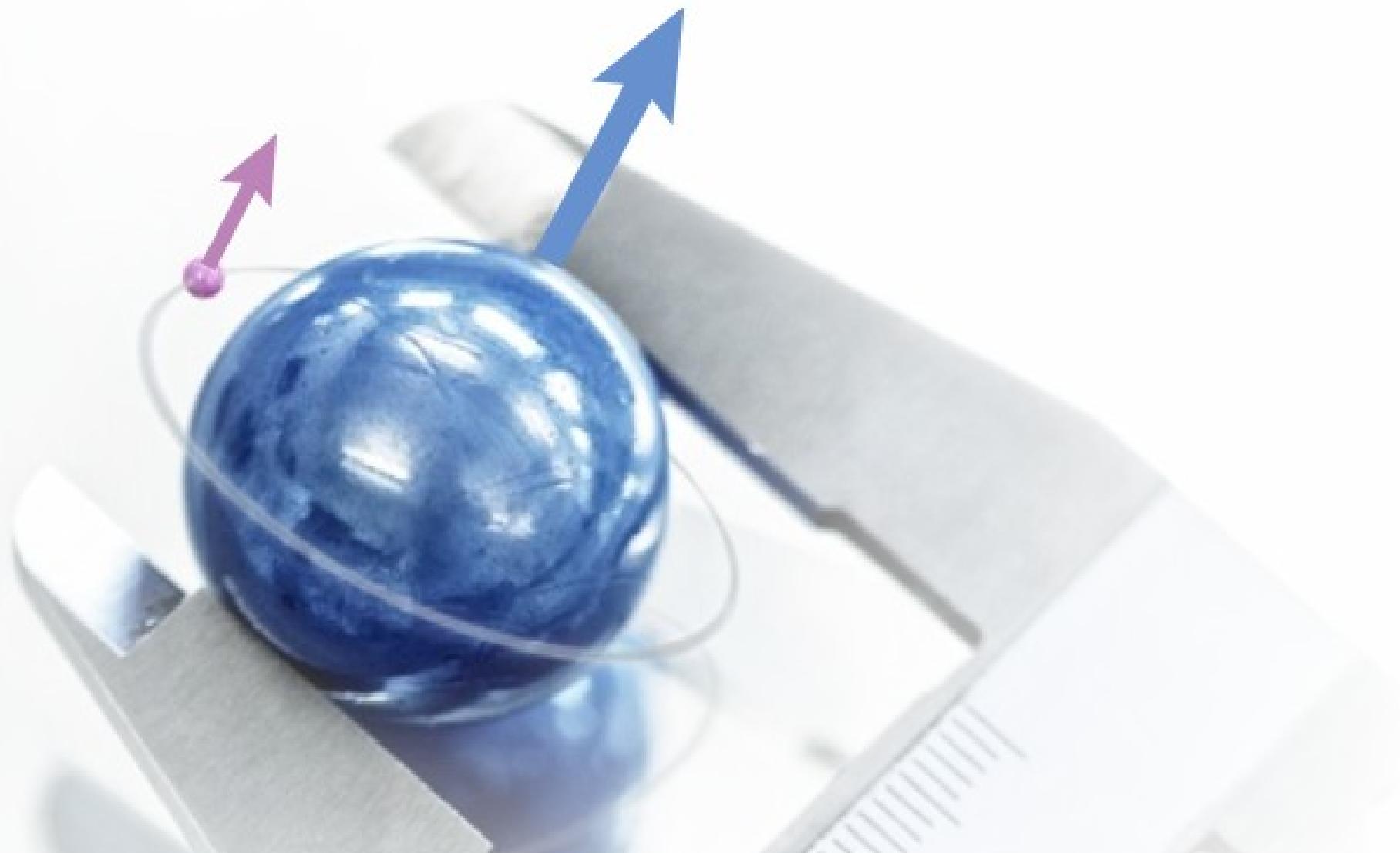
- H(2S – 6P, 8P, **9P**, ...) and D(2S-nl) underway in Garching and Colorado
- H(1S – 3S, 4S, ..) and D(1S-3S) underway in Paris and Garching
- Muonium at PSI, J-PARC
- Positronium (Cassidy @ UCL, Crivelli @ ETH)
- He⁺(1S-2S) underway in Garching (Udem) and Amsterdam (Eikema)
- HD⁺, H₂, etc. in Amsterdam (Ubachs), Paris (Hilico, Karr), Zurich (Merkt)
- He (Amsterdam), Li⁺ (Udem @ Garching)
- HCl, e.g. H-like Ne (Tan @ NIST)
- Rydberg-atoms, e.g. Rb (Raithel @ Ann Arbor)
- new low-Q² electron scattering at MAMI, JLab, MESA
- muon scattering: MUSE @ PSI, COMPASS / AMBER @ CERN
-

**Compare Rydberg values
to test QED and SM**

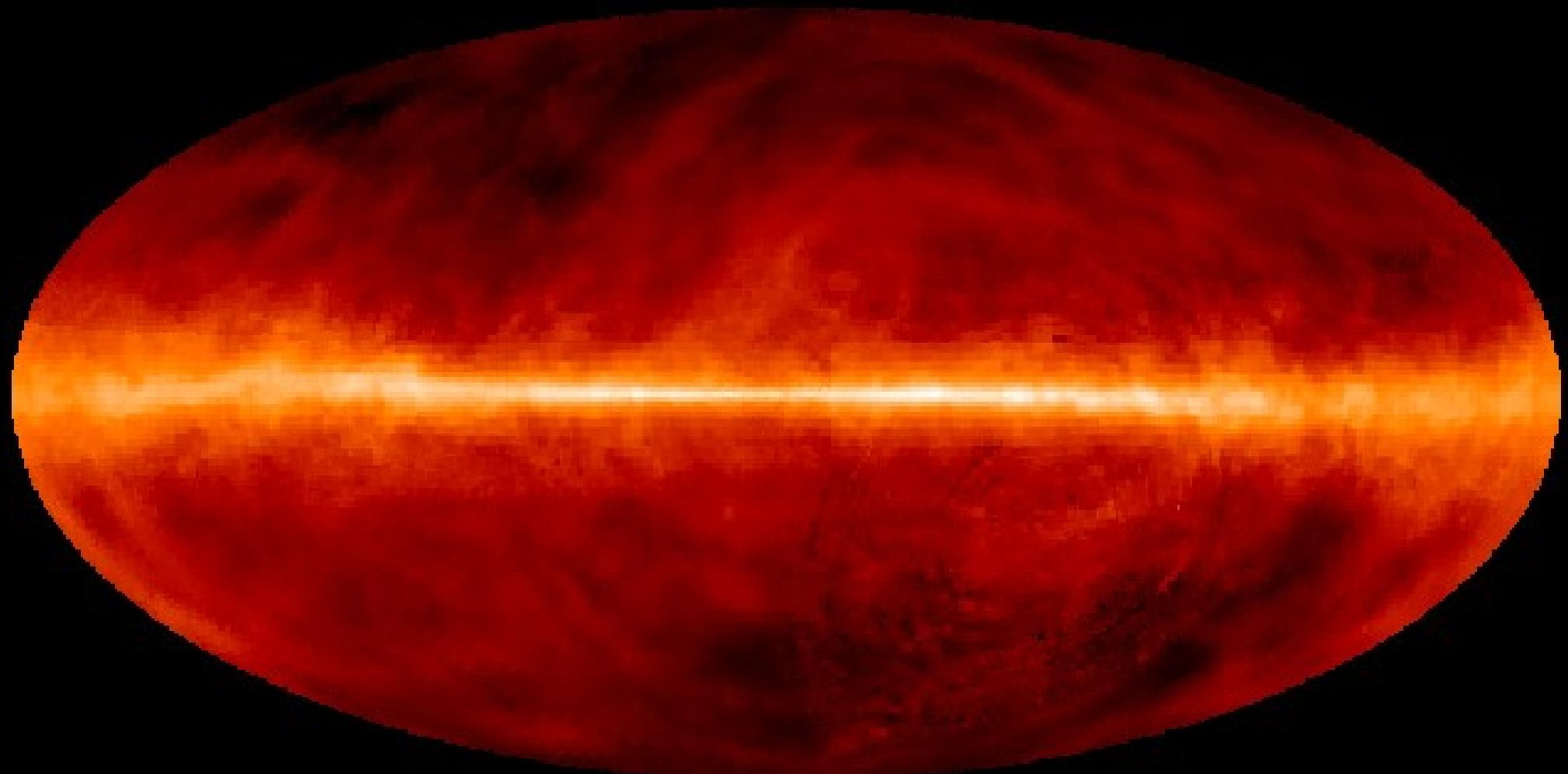
The Present

Hyperfine structure in muonic H

CREMA-3 / HyperMu at PSI
(R16.02)

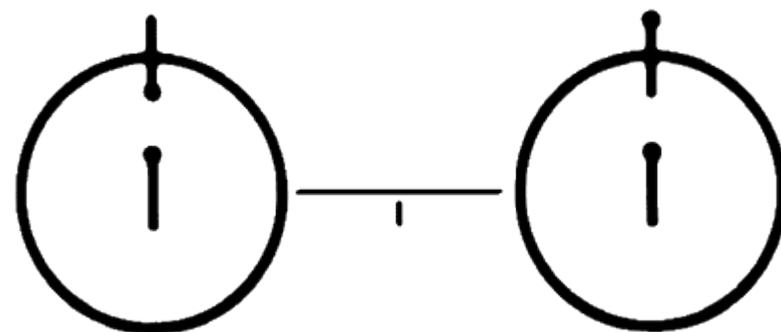


The sky in hydrogen



Hyperfine structure in H / μ p

The [21 cm line](#) in hydrogen (1S hyperfine splitting)



Hyperfine structure in H / μ p

The 21 cm line in hydrogen (1S hyperfine splitting) has been measured to 12 digits (0.001 Hz) in 1971:

$$v_{\text{exp}} = 1\ 420\ 405.\ 751\ 766\ 7 \pm 0.000\ 001 \text{ kHz}$$

Essen et al., Nature 229, 110 (1971)

QED test is limited to 6 digits (800 Hz) because of proton structure effects:

$$v_{\text{theo}} = 1\ 420\ 403.\ 1 \pm 0.6_{\text{proton size}} \pm 0.4_{\text{polarizability}} \text{ kHz}$$

Eides et al., Springer Tracts 222, 217 (2007)

Proton Zemach radius

HFS depends on “Zemach” radius:

$$\Delta E = -2(Z\alpha)m \langle r \rangle_{(2)} E_F$$

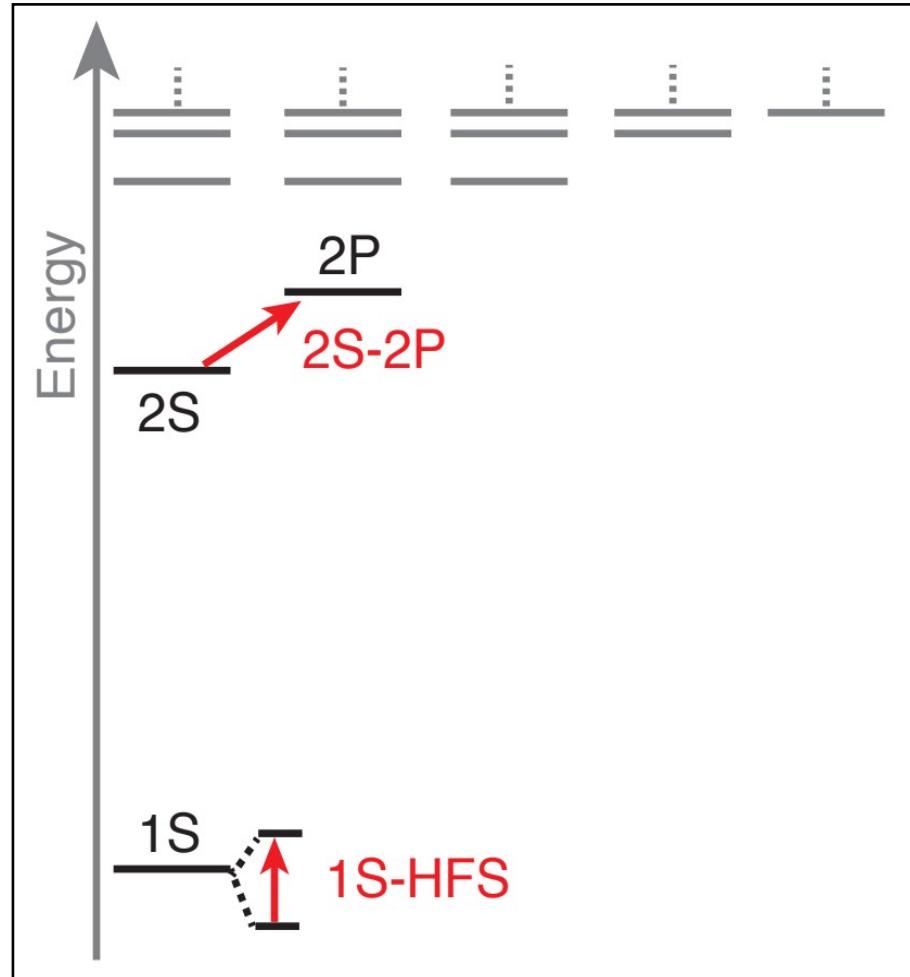
$$\langle r \rangle_{(2)} = \int d^3r d^3r' \rho_E(r) \rho_M(r') |r - r'|$$

Zemach, Phys. Rev. 104, 1771 (1956)

Form factors and momentum space

$$\Delta E = \frac{8(Z\alpha)m}{\pi n^3} E_F \int_0^\infty \frac{dk}{k^2} \left[\frac{G_E(-k^2) G_M(-k^2)}{1 + \kappa} \right]$$

From charge to magnetic properties



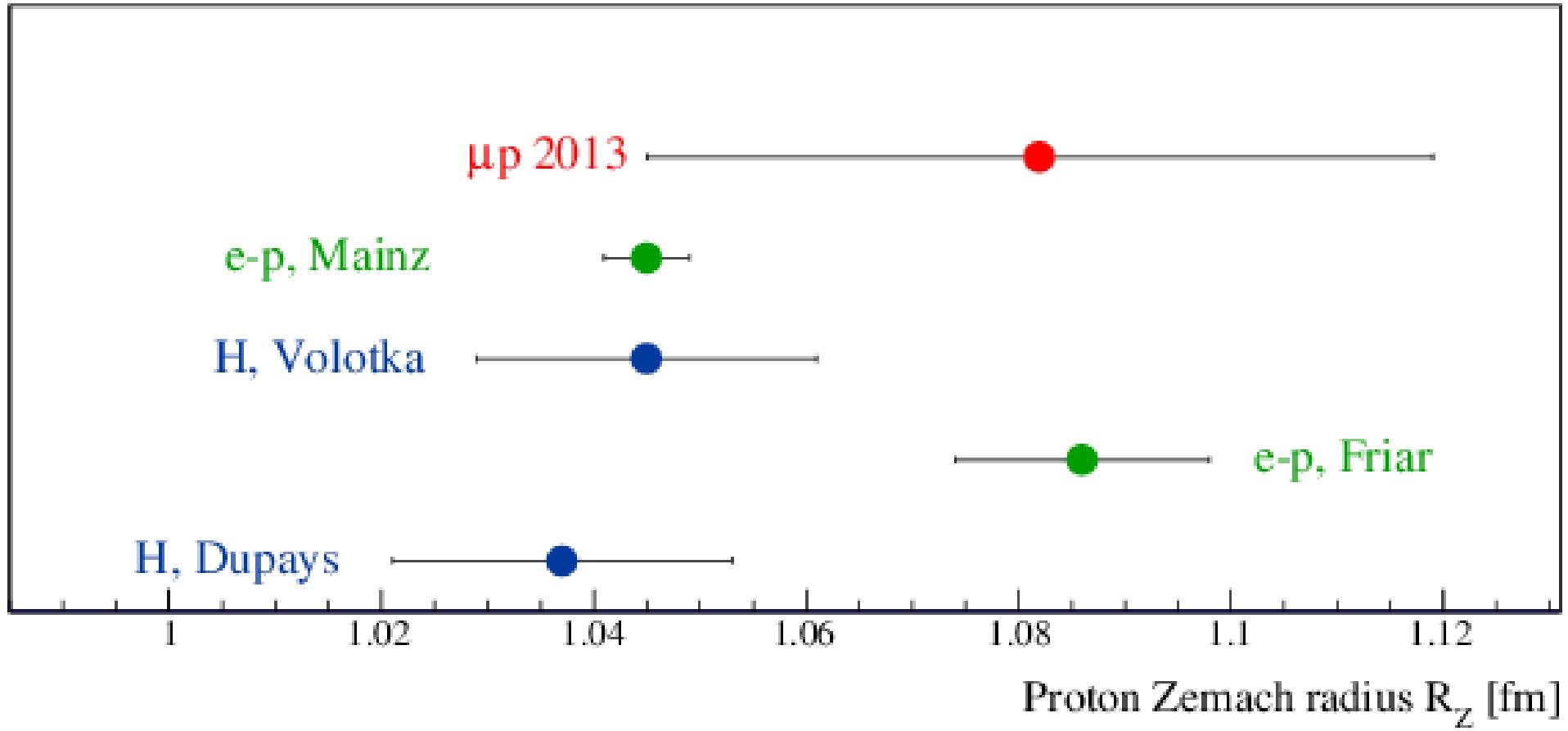
$2S-2P$ = Lamb shift

is sensitive to CHARGE radius

$1S$ -HFS = Hyperfine splitting

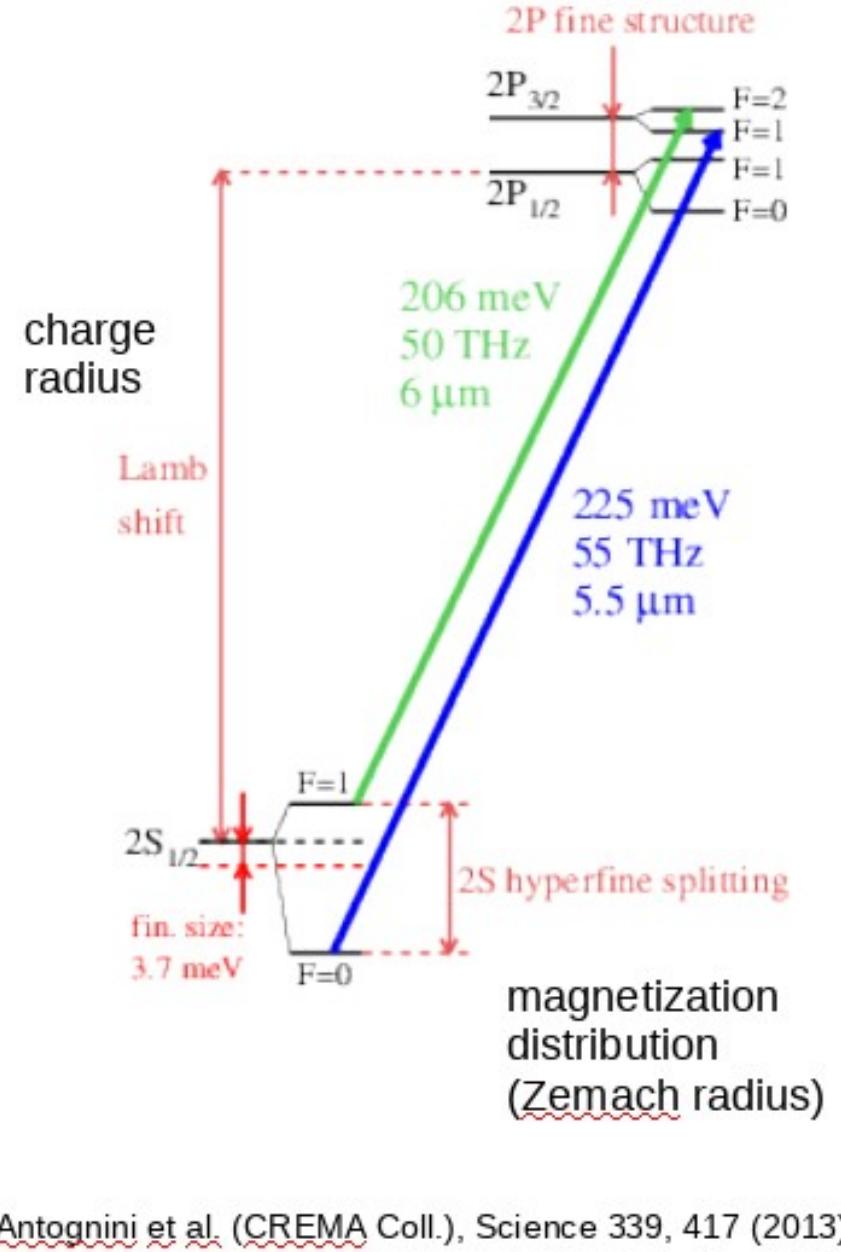
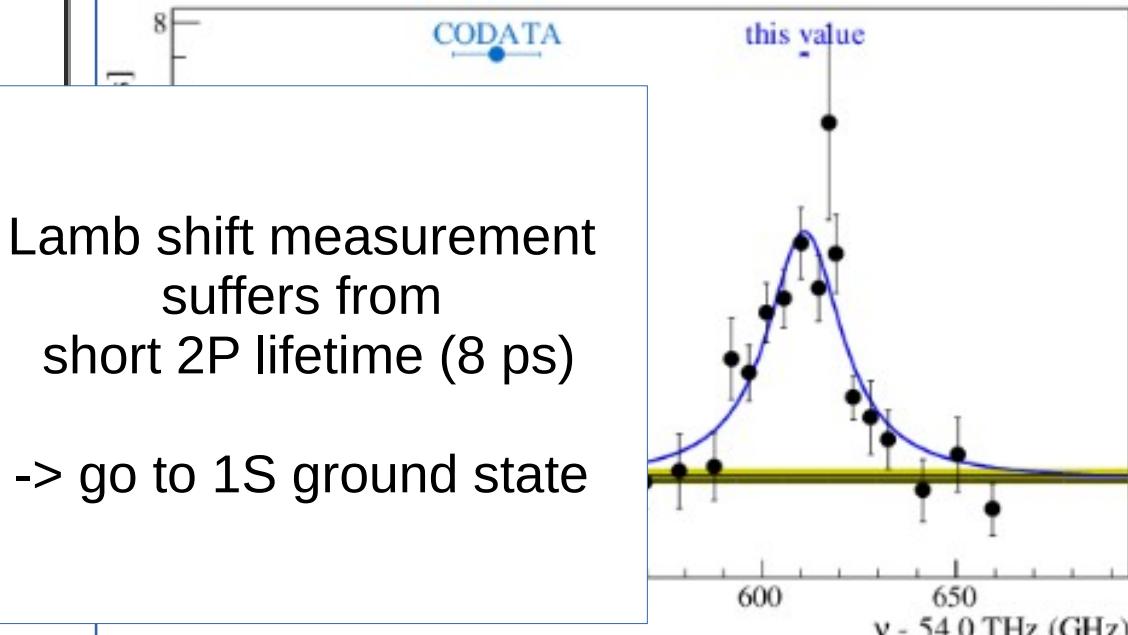
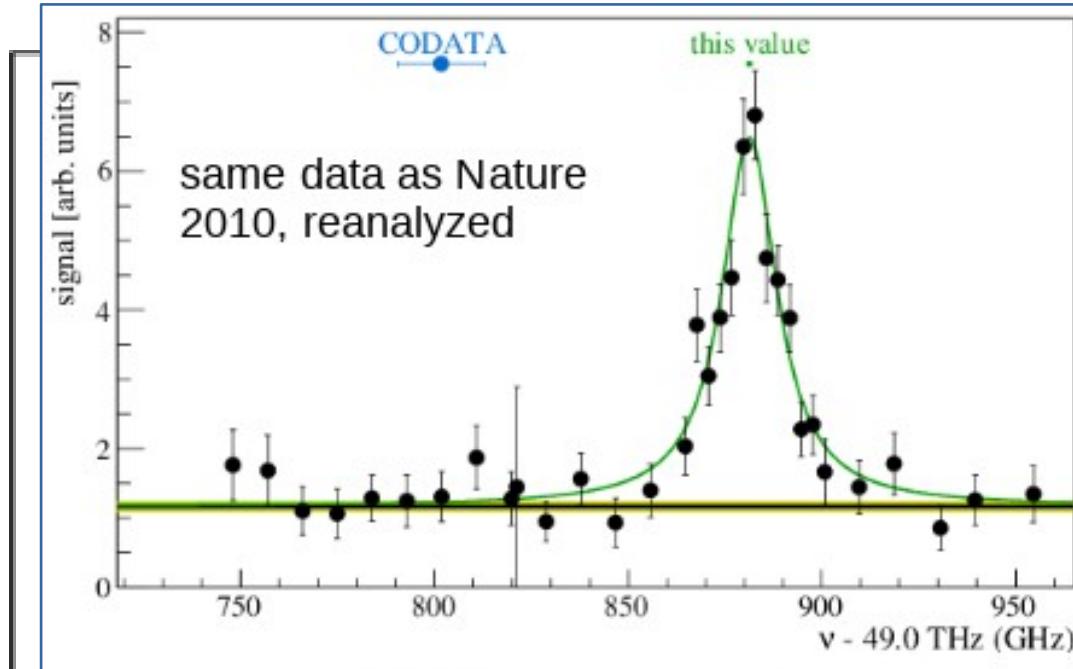
is sensitive to ZEMACH radius

Proton Zemach radius from μp

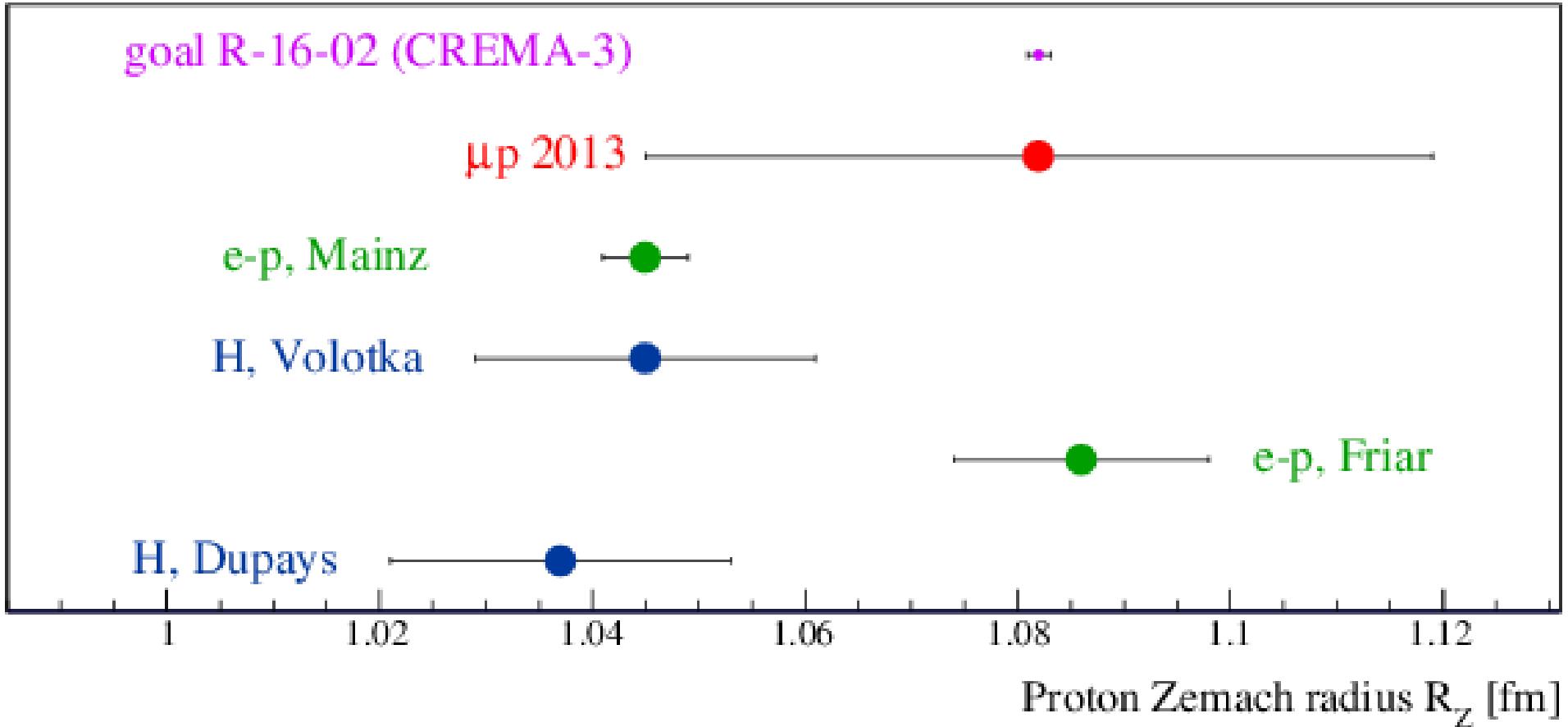


μp 2013: Antognini et al. (CREMA Coll.), Science 339, 417 (2013)

Proton Zemach radius from μ p



Proton Zemach radius from μp



PSI Exp. R-16-02: Antognini, RP et al. (CREMA-3 / HyperMu)

see e.g. Schmidt, RP et al., J. Phys. Conf. Ser 1138, 012010 (2018); arXiv 1808.07240

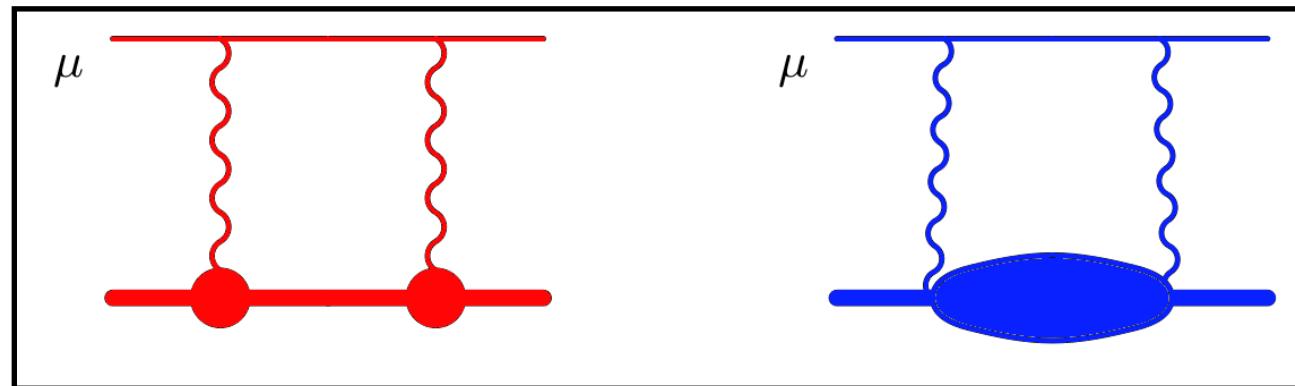
also: FAMU @ RIKEN/RAL, and a Collaboration at J-PARC

HFS in μ p

$$\Delta E_{\text{HFS}}^{\text{th}} = 182.819(10) - \underbrace{1.301 R_Z + 0.064(21)}_{\text{TPE}} + \dots \quad \text{meV}$$

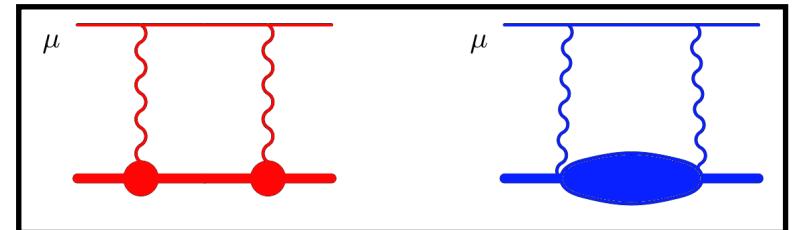
goal: measure HFS with 1 ppm relative accuracy

obtain TPE with 3×10^{-4} rel. accuracy



HFS in μp

$$\Delta E_{\text{HFS}}^{\text{th}} = 182.819(10) - \underbrace{1.301 R_Z + 0.064(21)}_{\text{TPE}} + \dots \text{ meV}$$



Measure the 1S–HFS in μp and μHe
with 1 ppm accuracy

TPE contributions with
 1×10^{-4} relative accuracy

Polarizability
<10% relative accuracy

Polarizability
from theory

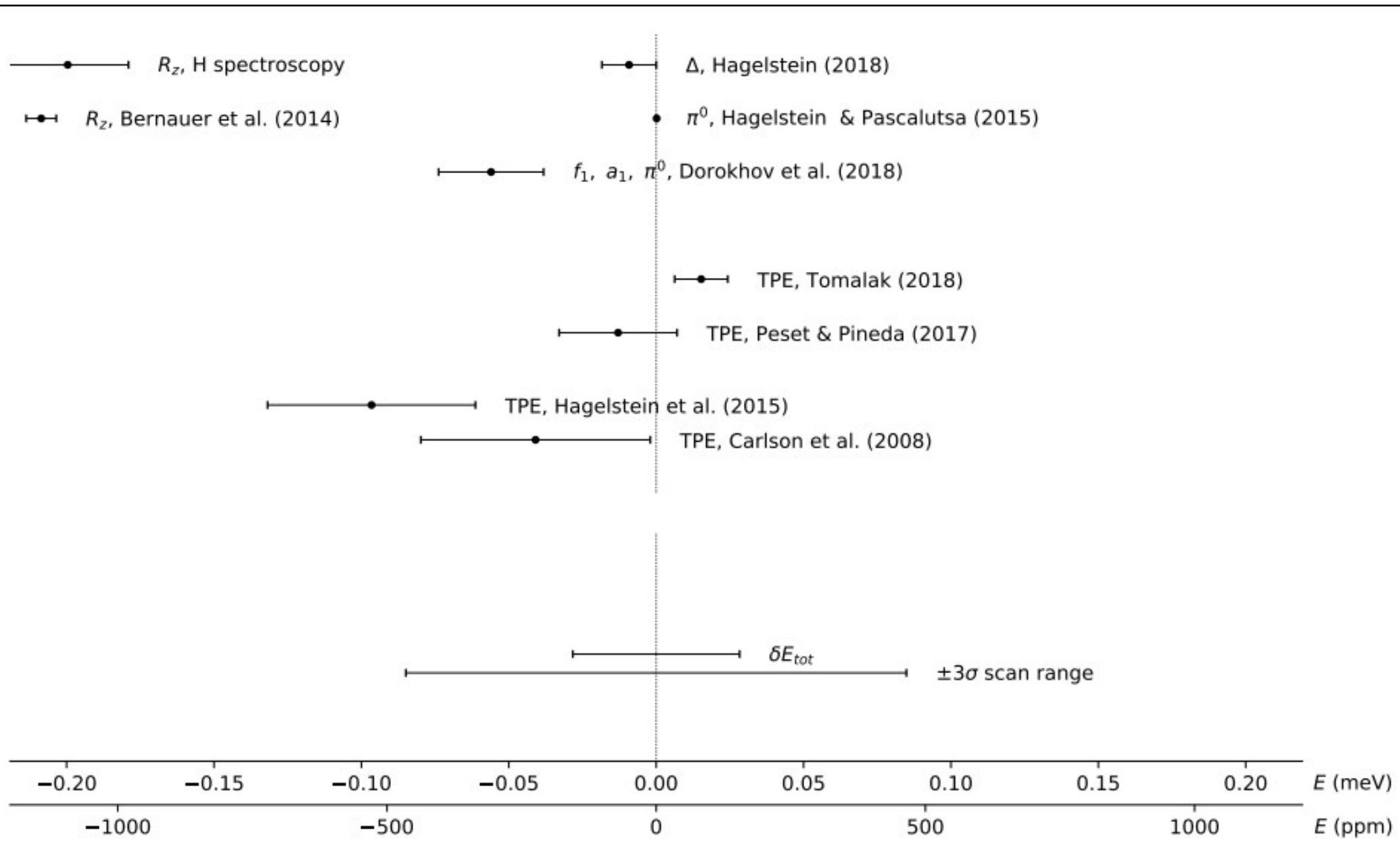
Zemach radii
 1×10^{-3} relative accuracy

Zemach radii
from scattering or H/He

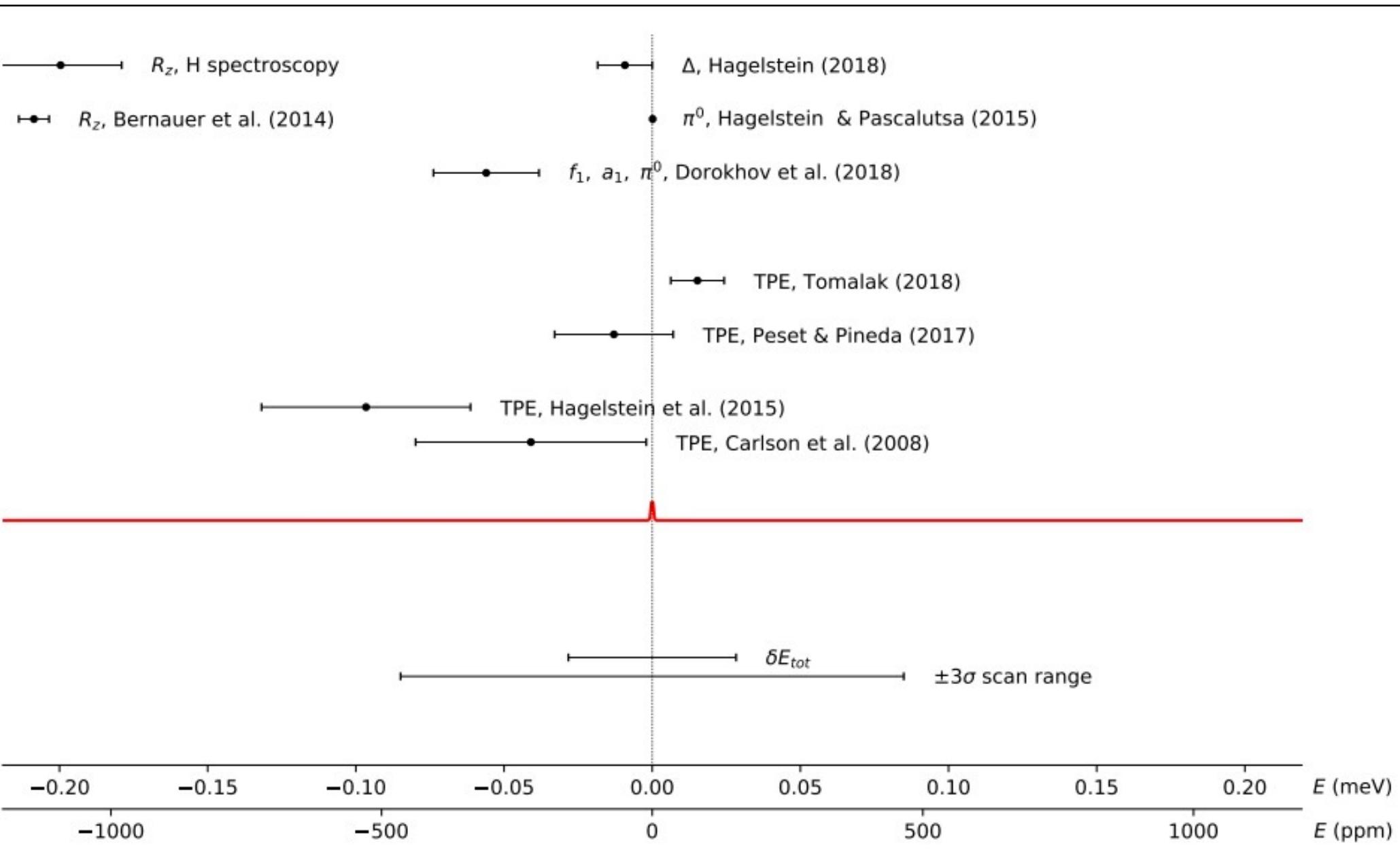
Magnetic radii

related proposals: FAMU at RIKEN/RAL, muonic H at J-PARC

Predicting the resonance position

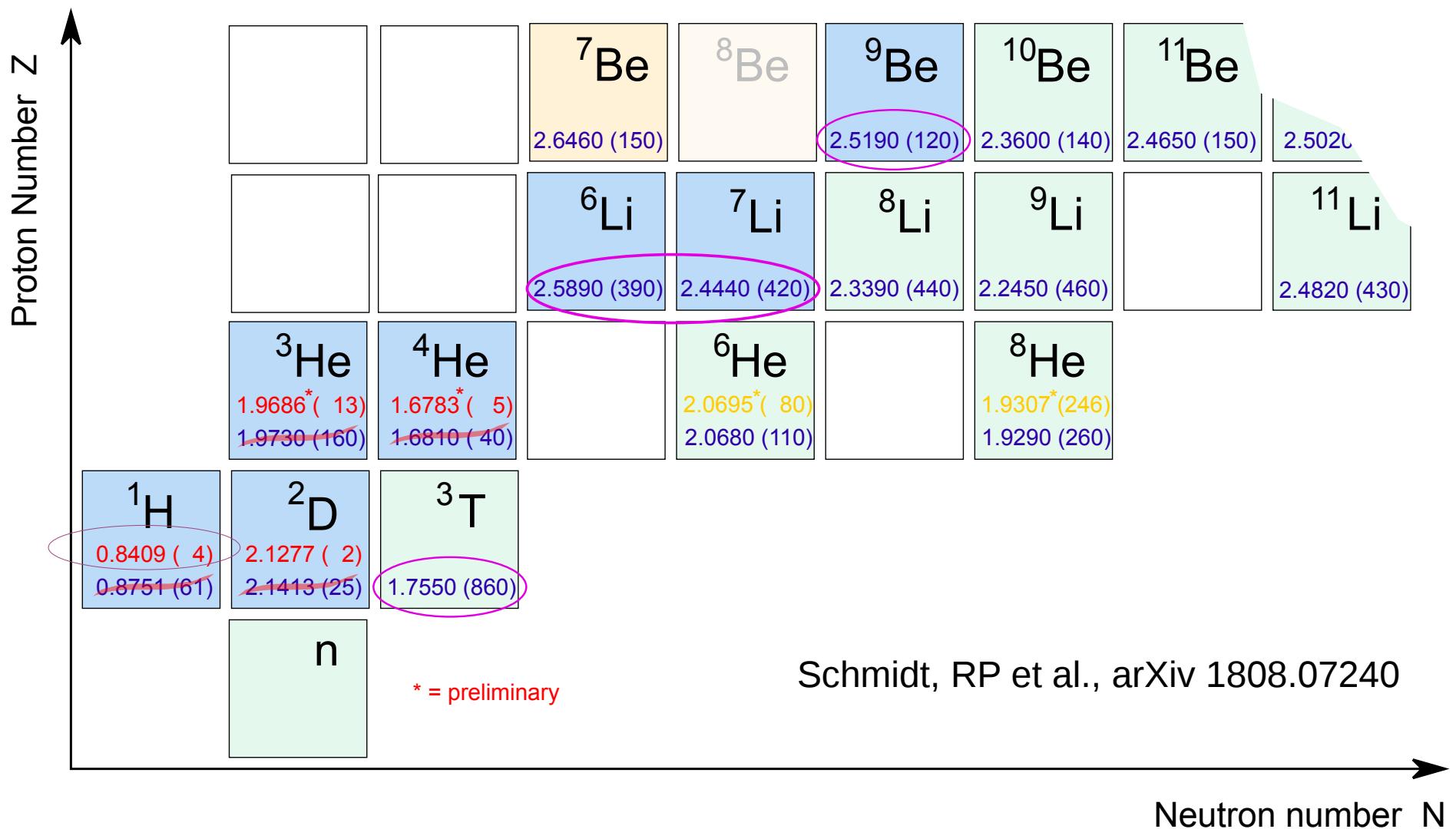


The resonance position

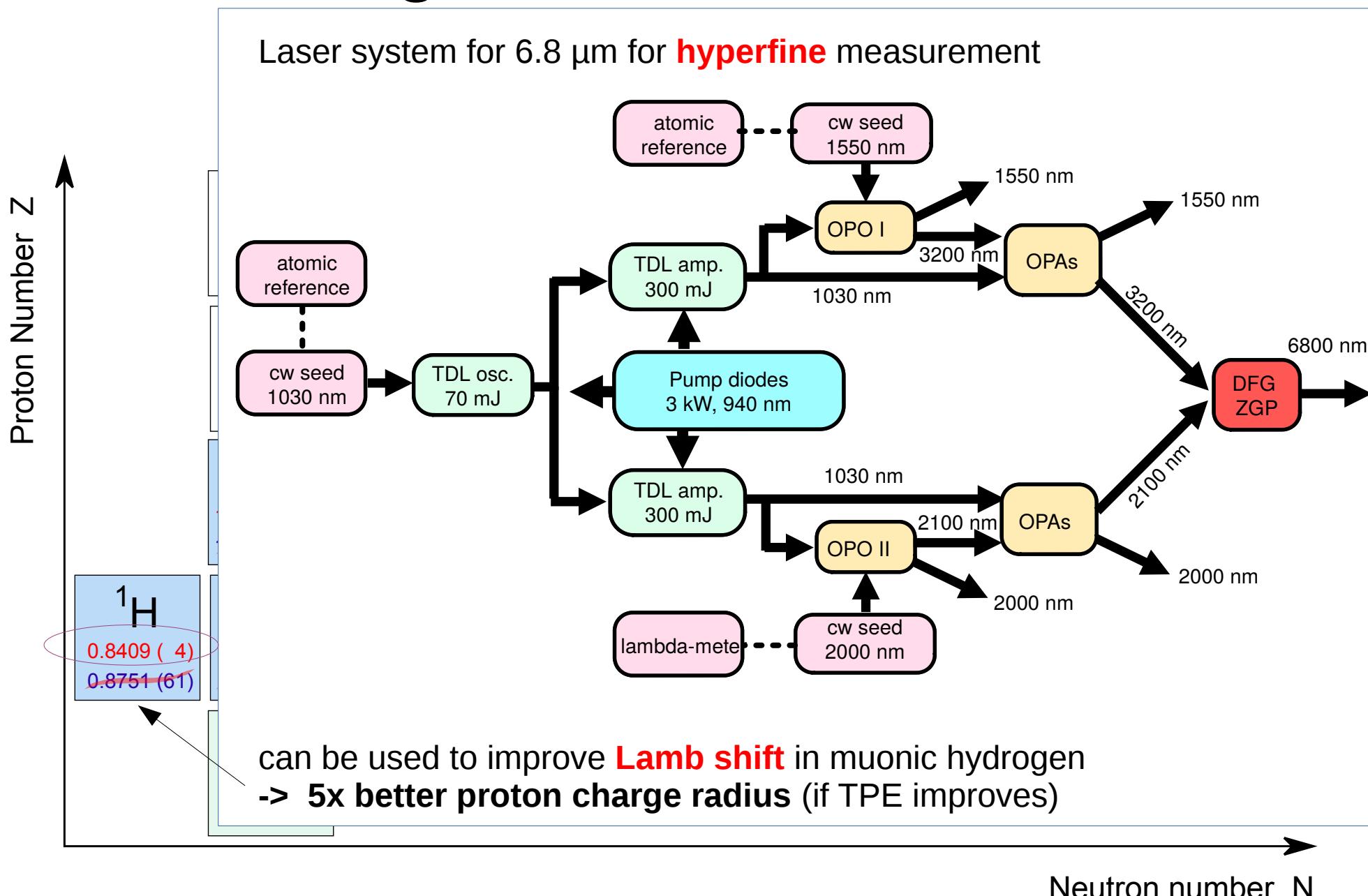


The Future

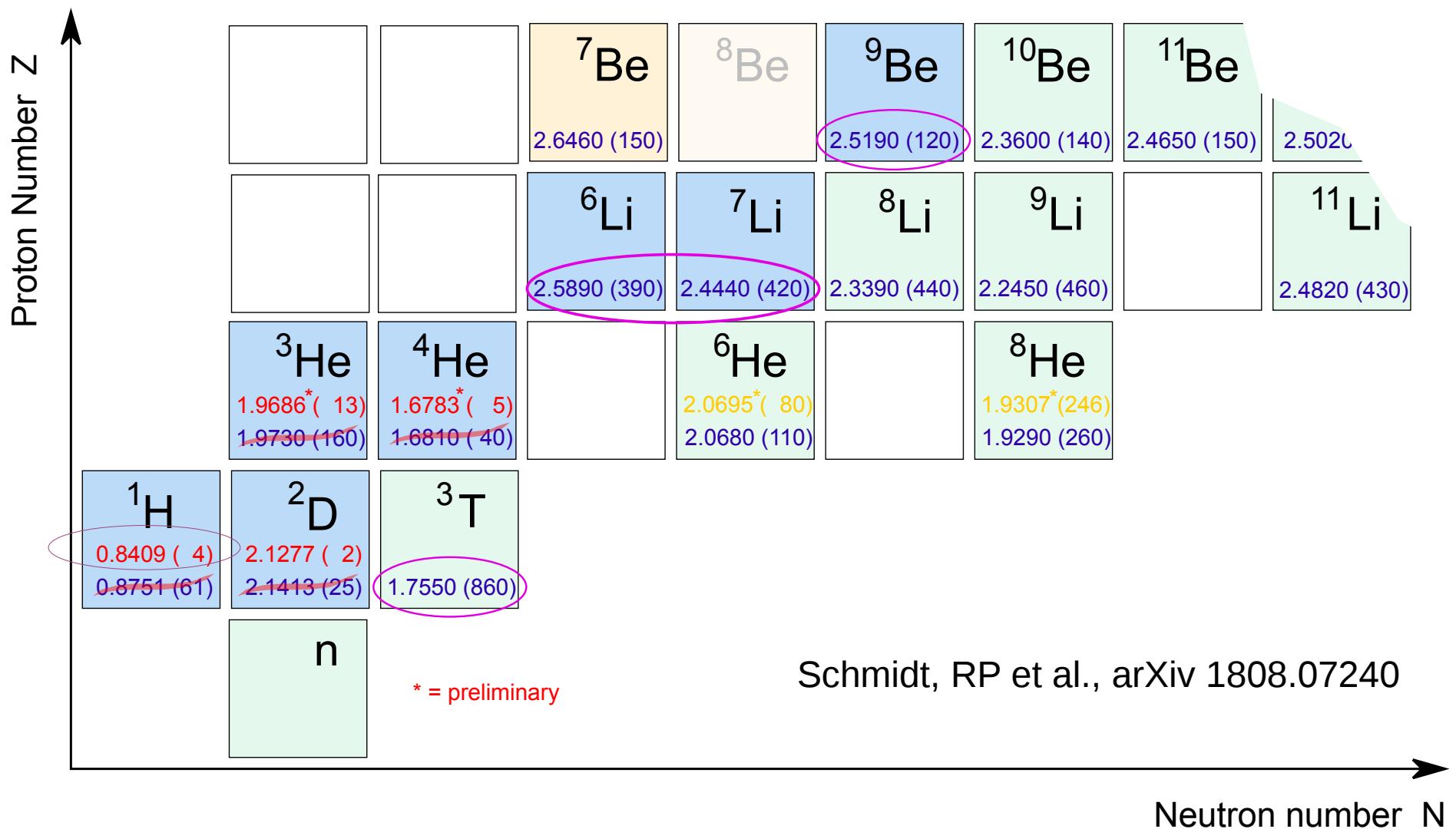
Charge radii: The future



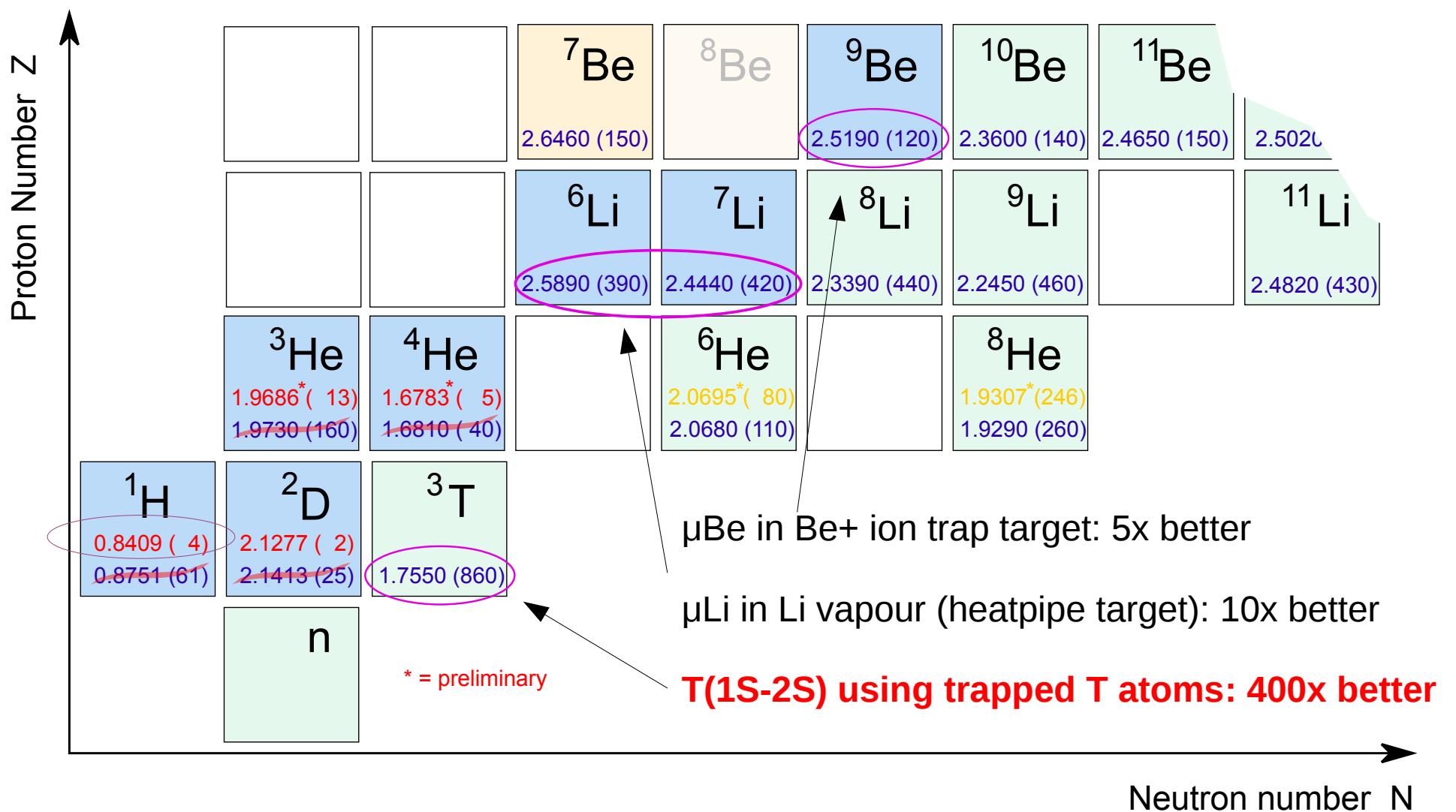
Charge radii: The future



Charge radii: The future

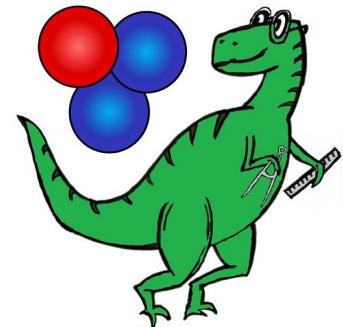


Charge radii: The future



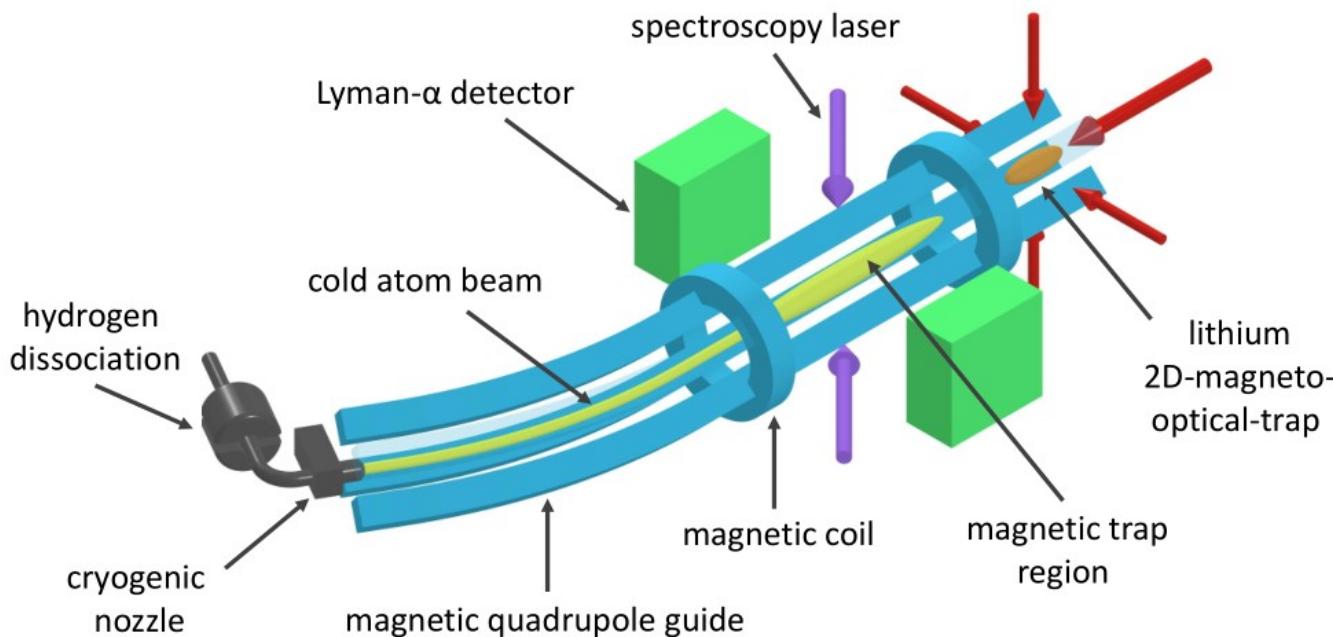
Tritium 1S-2S in a trap

^3He	^4He
1.9687* (13)	1.6778* (7)
1.9730 (160)	1.6810 (40)
^1H	^2D
0.8409 (4)	2.1277 (2)
0.8751 (61)	2.1413 (25)
^3T	
1.7xxx (2)	
1.7550 (860)	



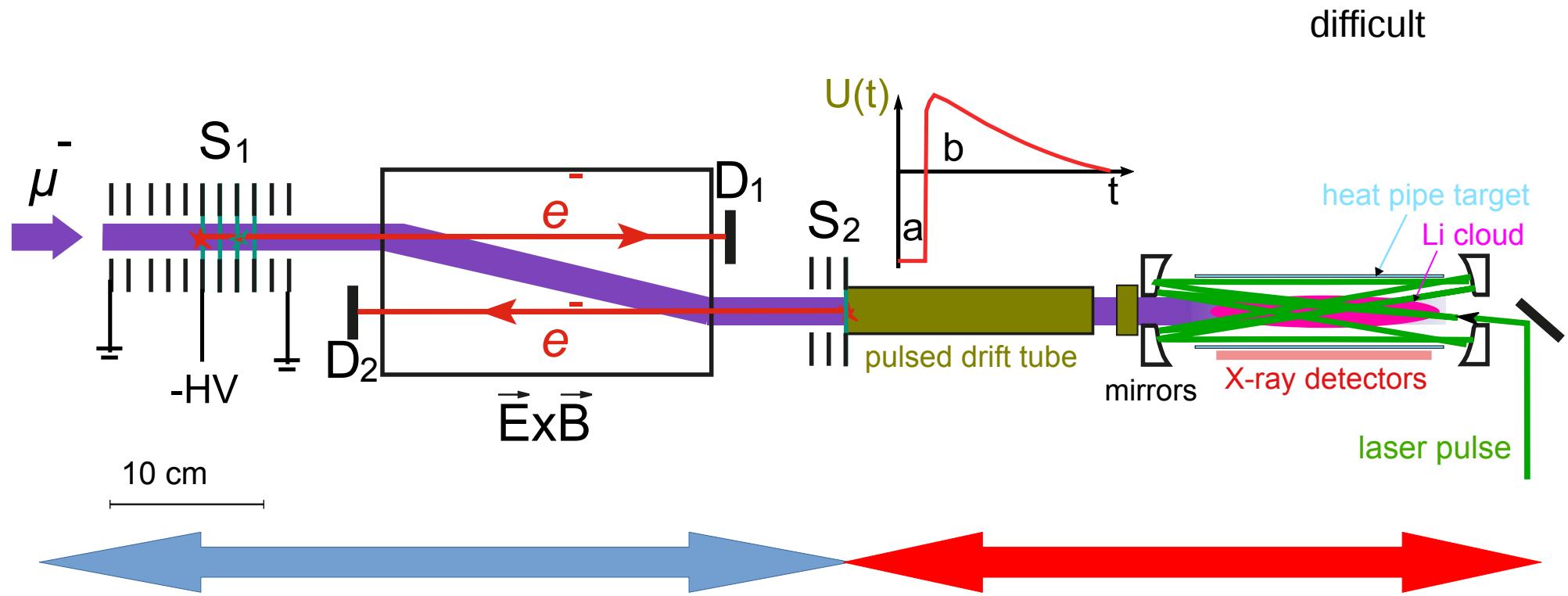
**Triton-Radius Experiment
Mainz**

**400x better radius
with 1 kHz measurement**
| (vs. 0.01 kHz for H, D)



- cryogenic H nozzle (4.2K)
- magnetic quadrupole guide
- Li MOT \rightarrow cold buffer gas
- magnetic trapping of H/D/T

muonic Li with heat pipe target

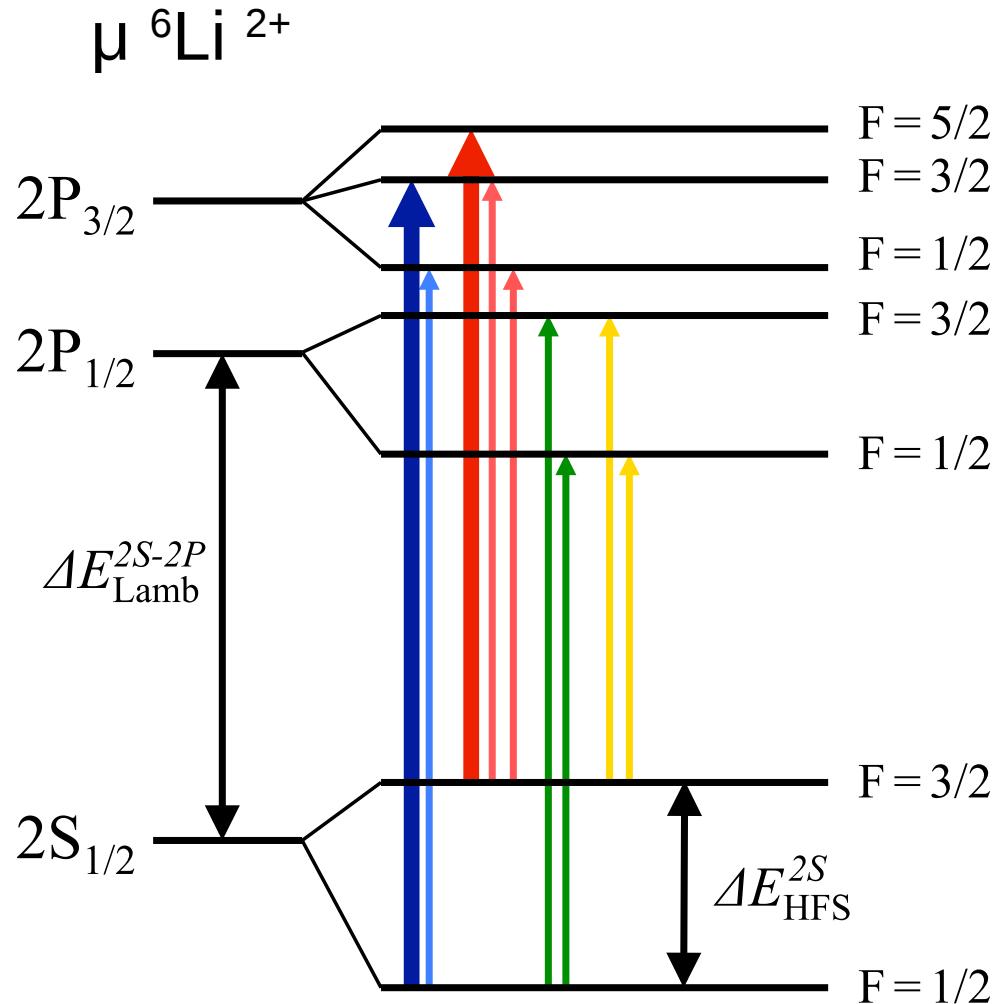


existing beam line:
1000/s at ~ 1 keV

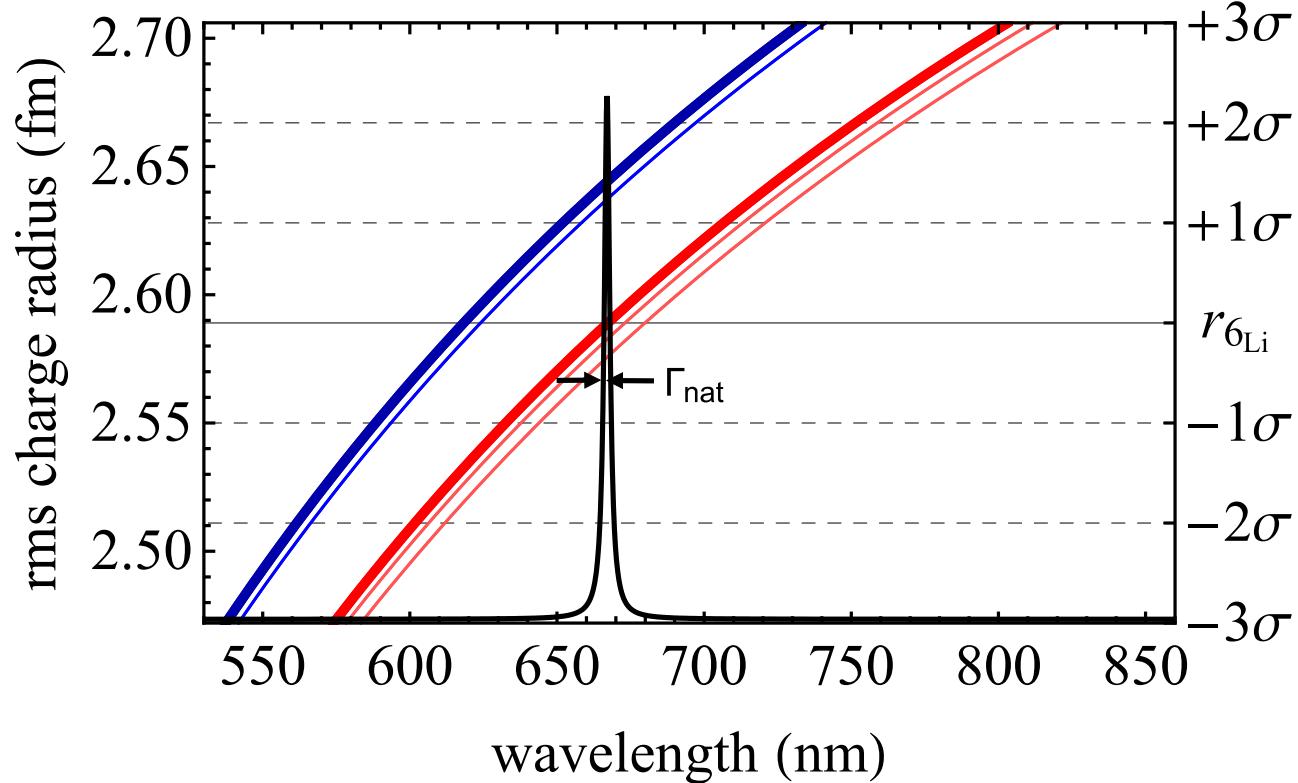
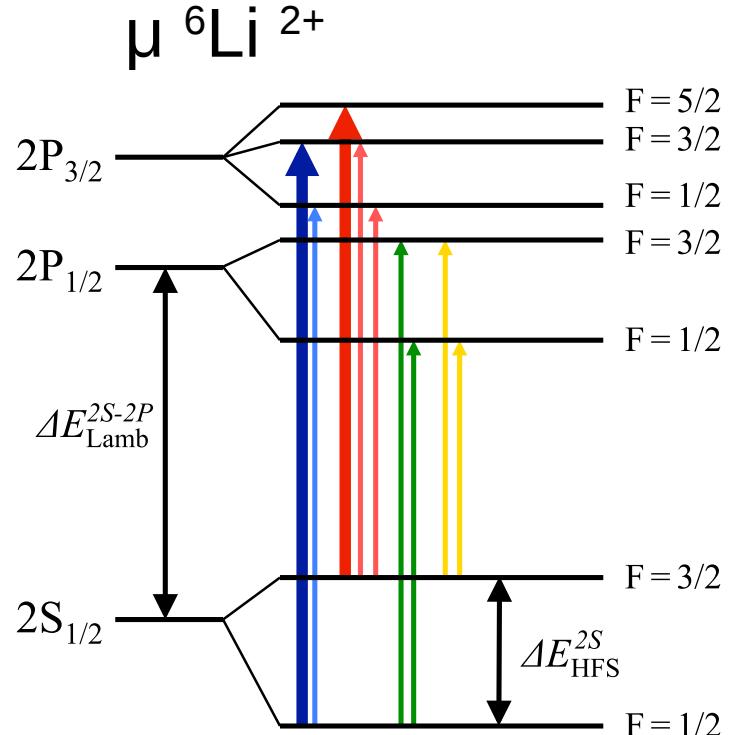
to be built:

drift tube to 100 .. 10 eV
lasers
detectors (easy)

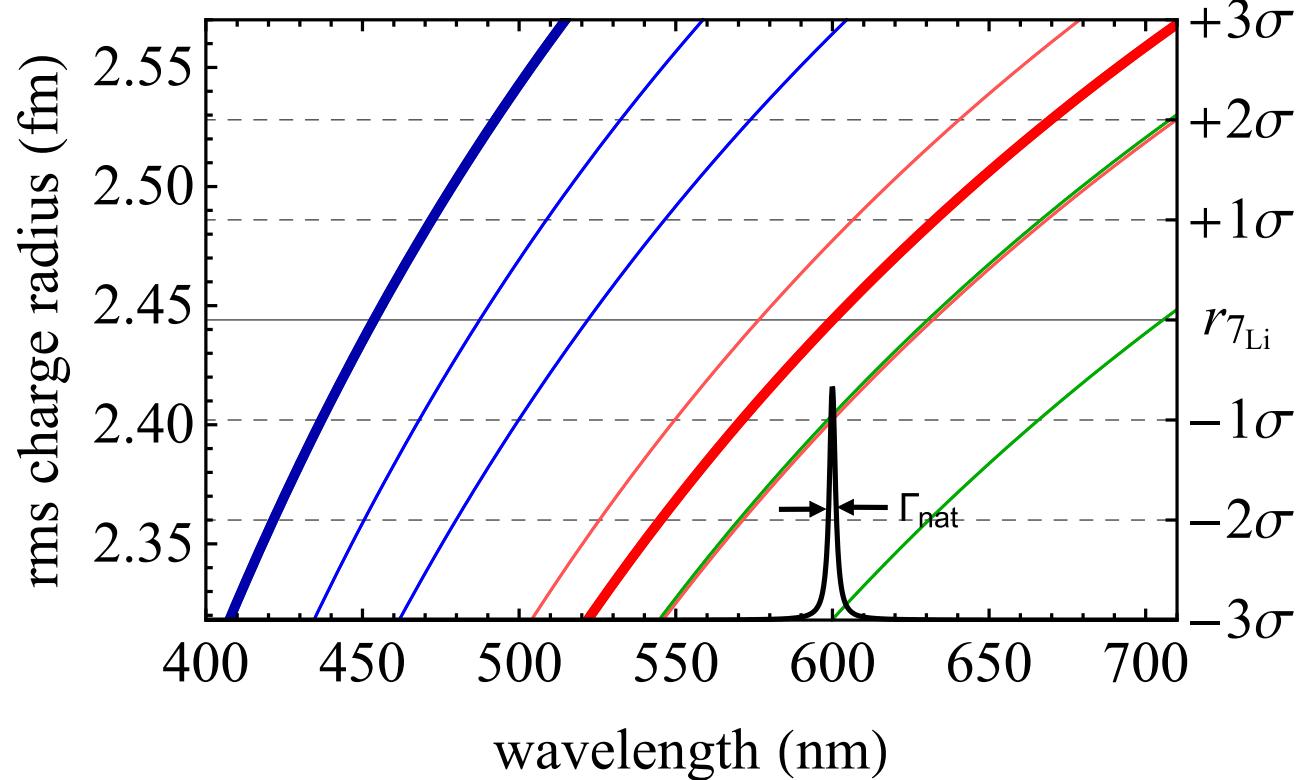
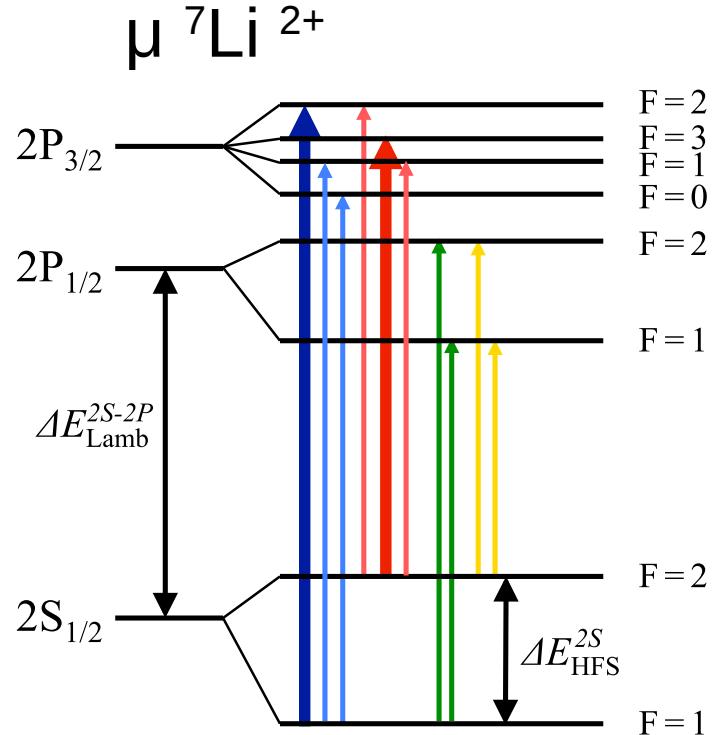
muonic Li with heat pipe target



muonic Li with heat pipe target



muonic Li with heat pipe target



muonic Li: theory and accuracy

Item	$(\mu^6\text{Li})^{2+}$	$(\mu^7\text{Li})^{2+}$
QED Lamb shift [meV]	4654.4(0.1)	4671.4(0.1)
finite size [meV]	-3712(112)	-3335(117)
nucl. shape (Friar moment) [meV]	223(-9)	191(-9)
nucl. polarizability [meV]	15(-4)	21(-4)
total Lamb shift [meV]	1162(112)(10)	1532(117)(10)
experimental accuracy goal ($\Gamma/10$) [meV]	0.7	0.7
wavelengths ($\pm 3\sigma$ in charge radius)	575-800 nm	520-710 nm

line width Γ (nm/meV)	2.3 nm \equiv 6.8 meV
K_α energy	18.7 keV
2S lifetime $\tau(2S)$	830 ns

$$r(^6\text{Li}) = 2.58900(\mathbf{3900}) \text{ fm} \quad [31] \rightarrow 2.58xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu^6\text{Li})^{2+}$$

$$r(^7\text{Li}) = 2.44400(\mathbf{4200}) \text{ fm} \quad [31] \rightarrow 2.44xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu^7\text{Li})^{2+}$$

exp: 100x better radius, but polarizability -> “only” 10x better

muonic Li and Li⁺

Item	$(\mu^6\text{Li})^{2+}$	$(\mu^7\text{Li})^{2+}$
QED Lamb shift [meV]	4654.4(0.1)	4671.4(0.1)
finite size [meV]	-3712(112)	-3335(117)
nucl. shape (Friar moment) [meV]	223(-9)	191(-9)
nucl. polarizability [meV]	15(-4)	21(-4)
total Lamb shift [meV]	1162(112)(10)	1532(117)(10)
experimental accuracy goal ($\Gamma/10$) [meV]	0.7	0.7

$$r(^6\text{Li}) = 2.58900(\mathbf{3900}) \text{ fm} \quad [31] \rightarrow 2.58xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu^6\text{Li})^{2+}$$

$$r(^7\text{Li}) = 2.44400(\mathbf{4200}) \text{ fm} \quad [31] \rightarrow 2.44xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu^7\text{Li})^{2+}$$

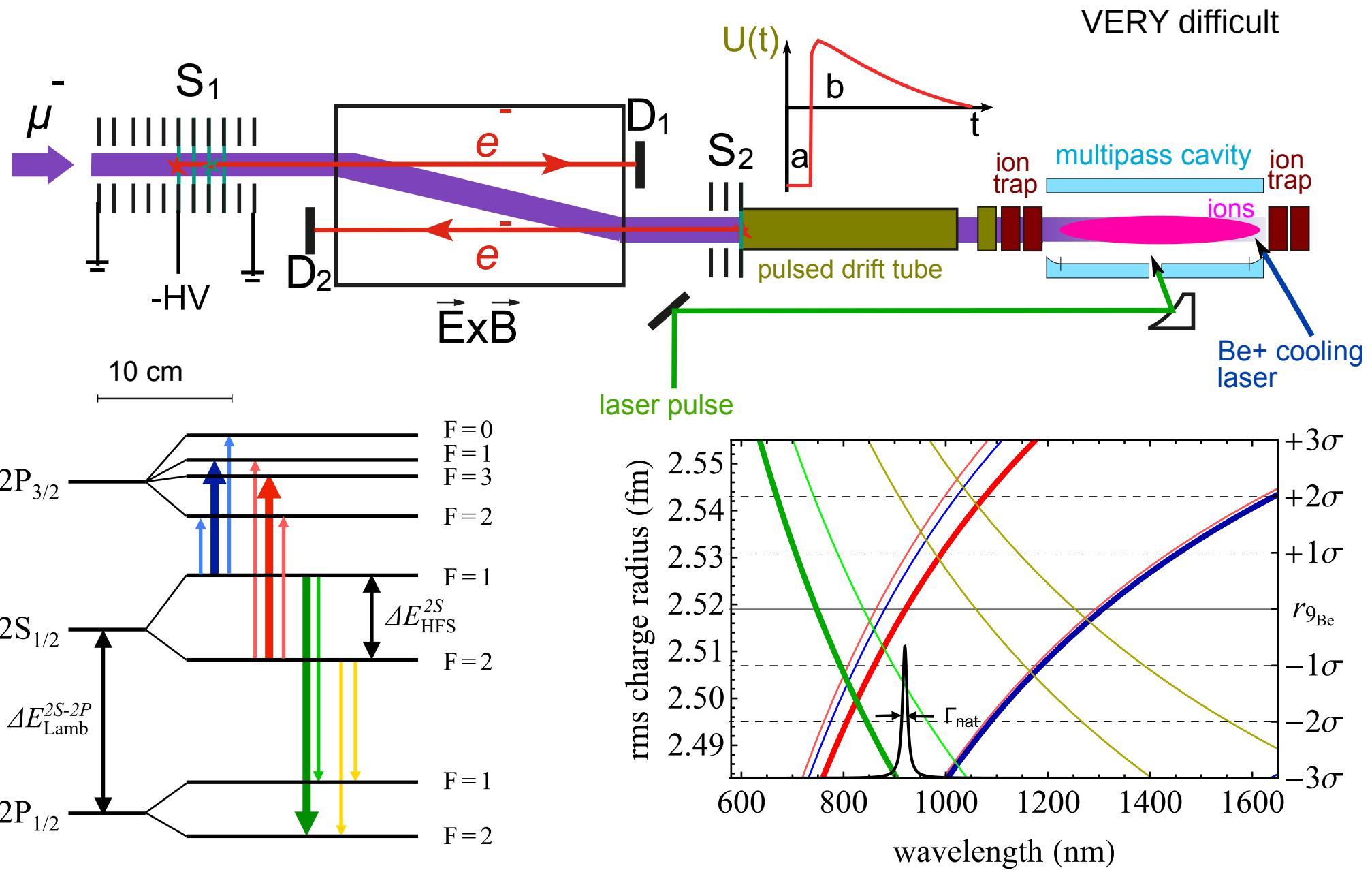
when combined with normal Li⁺ (Th. Udem)

-> QED test: He/ μ He vs. Li⁺/ μ Li and
H/ μ H vs. He⁺/ μ He

Rydberg constant H, He, Li, ...

100x better radius AND 10x better polarisability,

muonic Be with Penning trap target



muonic Li and Be ions

VERY difficult

$$r(^6\text{Li}) = 2.58900(\mathbf{3900}) \text{ fm} [31] \rightarrow 2.58xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu ^6\text{Li})^{2+}$$

$$r(^7\text{Li}) = 2.44400(\mathbf{4200}) \text{ fm} [31] \rightarrow 2.44xxx(\mathbf{40})^{\text{exp}}(\mathbf{400})^{\text{th}} \text{ fm} \quad (\mu ^7\text{Li})^{2+}$$

$$r(^9\text{Be}) = 2.51900(\mathbf{1200}) \text{ fm} [31] \rightarrow 2.51xxx(\mathbf{25})^{\text{exp}}(\mathbf{230})^{\text{th}} \text{ fm} \quad (\mu ^9\text{Be})^{3+}$$

Thanks a lot for your attention

My Mainz group:

Konrad Franz, Lukas Görner, Jan Haack, Merten Heppener, Jonas Klingelhöfer, Ahmed Ouf, Siddarth Rajamohanan, Gregor Schwendler, Hendrik Schürg, Benedikt Tscharn, Andreas Westerhoff, Marcel Willig

The Garching Hydrogen Team:

Axel Beyer, Lothar Maisenbacher, Vitaly Wirthl, Arthur Matveev, RP,
Ksenia Khabarova, Alexey Grinin, Tobias Lamour, Derya Taray,
Dylan C. Yost, Theodor W. Hänsch, Nikolai Kolachevsky, Thomas Udem

The CREMA Collaboration:

Aldo Antognini, Fernando D. Amaro, François Biraben, João M. R. Cardoso,
Daniel S. Covita, Andreas Dax, Satish Dhawan, Marc Diepold, Luis M. P.
Fernandes, Adolf Giesen, Andrea L. Gouvea, Thomas Graf, Theodor W.
Hänsch, Paul Indelicato, Lucile Julien, Paul Knowles, Franz Kottmann, Juilian
J. Krauth, Eric-Olivier Le Bigot, Yi-Wei Liu, José A. M. Lopes, Livia Ludhova,
Cristina M. B. Monteiro, Françoise Mulhauser, Tobias Nebel, François Nez,
Paul Rabinowitz, Joaquim M. F. dos Santos, Lukas A. Schaller, Karsten
Schuhmann, Catherine Schwob, David Taqqu, João F. C. A. Veloso, RP

The CREMA Collaboration

JOHANNES GUTENBERG
UNIVERSITÄT MAINZ



MAX-PLANCK-INSTITUT
FÜR QUANTENOPTIK
GARCHING



UNIVERSIDADE DE COIMBRA

