

# Probing the Majorana nature in radiative seesaw models at collider experiments

Shinya KANEMURA (U. of Toyama)

M. Aoki, SK and O. Seto, PRL 102, 051805 (2009).

M. Aoki, SK and O. Seto, PRD80, 033007 (2009).

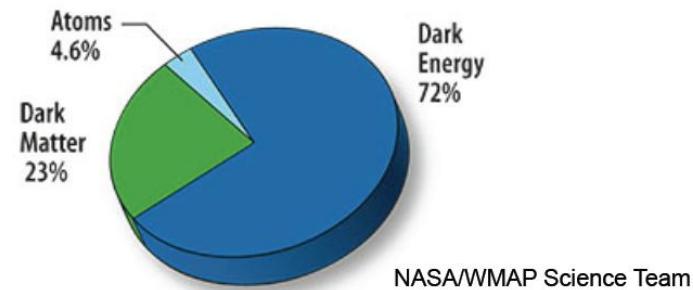
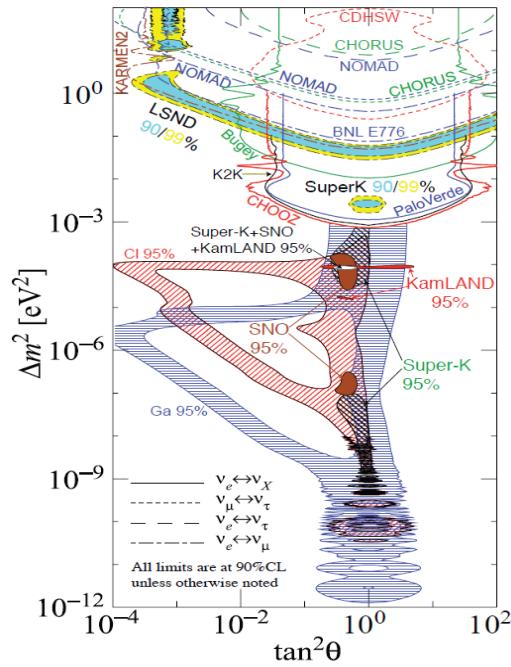
M. Aoki, SK, K. Tsumura, K. Yagyu, PRD80, 015017(2009).

M. Aoki and SK, arXiv: 1001.0092.

LCWS2010, Beijing, China, March 26-30. 2010

# Introduction

- Higgs sector remains unknown
    - Minimal/**Non-minimal** Higgs sector?
    - Higgs Search is the most important issue to complete the SM particle contents.
  - We already know BSM phenomena:
    - Neutrino oscillation
- $\Delta m^2 \sim 8 \times 10^{-5} \text{ eV}^2, \Delta m^2 \sim 3 \times 10^{-3} \text{ eV}^2$
- Dark Matter
- $\Omega_{\text{DM}} h^2 \sim 0.11$
- Baryon Asymmetry of the Universe
- $n_B/s \sim 9 \times 10^{-11}$



To understand these phenomena, we need to go beyond-SM

# Neutrino Mass

Neutirno Mass Term (= effective Dim-5 Operator)

$$L^{\text{eff}} = (c_{ij}/M) \bar{\nu}_L^i \nu_L^j \phi \phi$$

$$\langle \phi \rangle = v = 246 \text{ GeV}$$

Mechanism for tiny masses:

$$m_{ij}^\nu = [c_{ij} (v/M)] v < 0.1 \text{ eV}$$

Seesaw (tree level)

$$m_{ij}^\nu = y_i y_j v^2 / M$$

$$M \sim 10^{14} \text{ GeV} \text{ (for } y_i = O(1))$$

Quantum Effects (Radiative Seesaw) N-th order of perturbation

$$m_{ij}^\nu = [1/(16\pi^2)]^N C_{ij} v^2 / M \quad M = O(1) \text{ TeV}$$

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# Radiative Seesaw Model

A Neutrino Mass Generation Mechanism at Loop

Feature

1. Extended Higgs (scalar) sector
2. Majorana nature

Merit

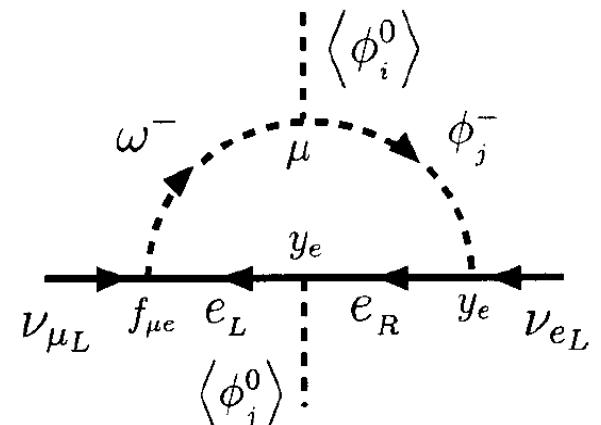
- A super high scale is not necessary.

Tiny  $m_\nu$  can naturally be deduced from TeV scale physics by higher order perturbation

- Physics at TeV:  
Testable at collider experiments

Zee Model

2HDM + (charged singlet  $\omega^+$ )  
Lepton # violating interaction  $\mu^- \omega^-$



Zee, PLB93,389 (1980)

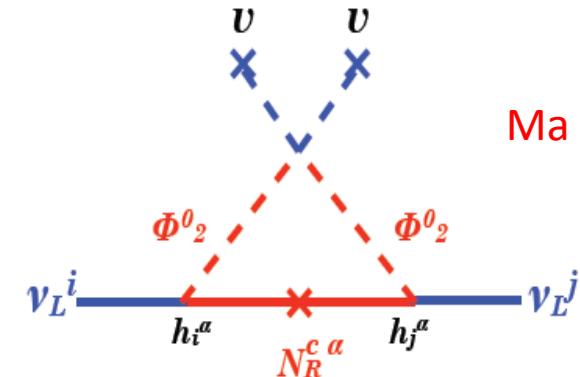
Excluded by the data

# Models of radiative $\nu\nu\phi\phi$ generation

Tiny  $\nu$ -Masses come from loop effects

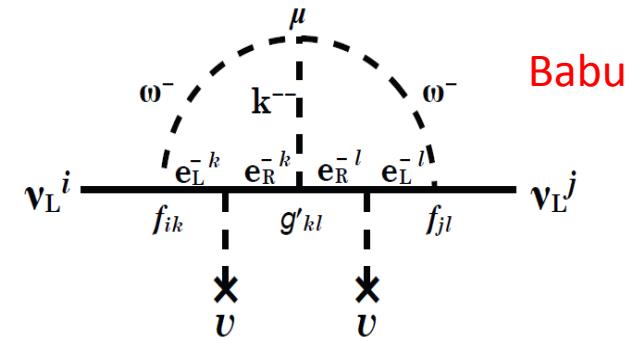
– Ma

(1-loop)  
Ma, PRD73,077301 (2006)



– Zee-Babu

(2-loop)  
Babu, PLB203,132(1988)



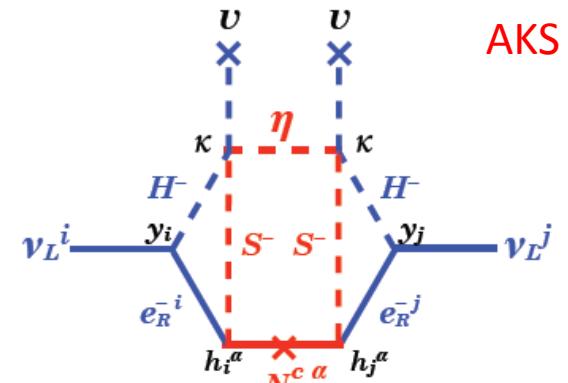
– Aoki-Kanemura-Seto (3-loop)  
PRL102, 051805(2009)

$$m_{ij}^\nu = [1/(16\pi^2)]^N C_{ij} \nu^2/M \quad M=O(1) \text{ TeV}$$

Common features

Extended Higgs sector

Source of the Majorana nature



# The Zee-Babu model

Model:

SM +  $\omega^+$ ,  $\kappa^{++}$  (charged scalar singlets: L#=2)

Babu, PLB203,132(1988)

Source of the Majorana nature:

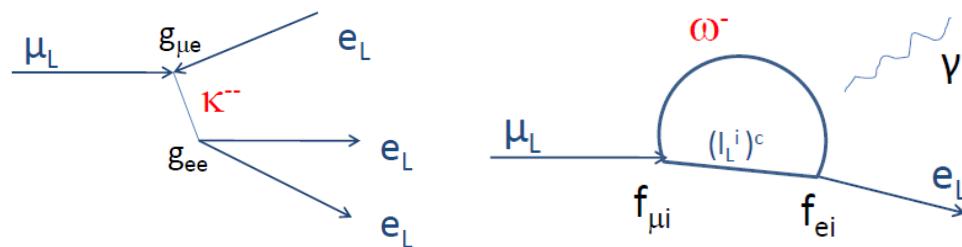
**LNV interaction ( $\mu$ )**

**Neutrino masses** generated at 2-loop

$$f_{\text{em}} \sim f_{e\tau} \sim f_{\mu\tau}/2 \quad (\text{Normal Hierarchy})$$

$$g_{\mu\mu} : g_{\mu\tau} : g_{\tau\tau} \sim 1 : m_\mu/m_\tau : (m_\mu/m_\tau)^2$$

**Constraints on couplings from LFV data**



Bound on the masses:  $m_\omega > 160 \text{ GeV}$ ,  $m_\kappa > 770 \text{ GeV}$  (for  $g_{\mu\mu} \sim 1$ )

Babu, Macesanu (2003), Aristizabal Sierra, Hirsch (2006)

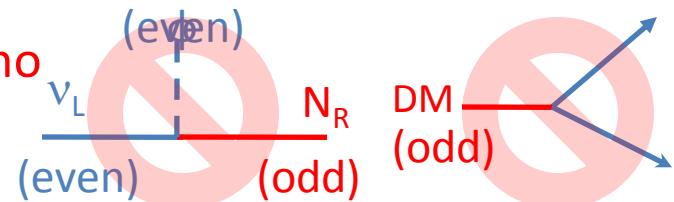
# The Ma model

Ma, PRD73,077301 (2006)

Source of the Majorana nature: TeV-scale RH neutrino

No tree-level neutrino Yukawa: Exact  $Z_2$ -parity

Model: 2HDM ( $Z_2$ -even  $\Phi_1$ ,  $Z_2$ -odd  $\Phi_2$ )  
+ RH-Neutrino ( $Z_2$ -odd  $N_R$ )



Neutrino masses generated at 1-loop

The lightest  $Z_2$  odd particle can be DM

DM candidate: Either  $\Phi_2^0$  ( $\xi_r^0, \xi_i^0$ ) or  $N_R$

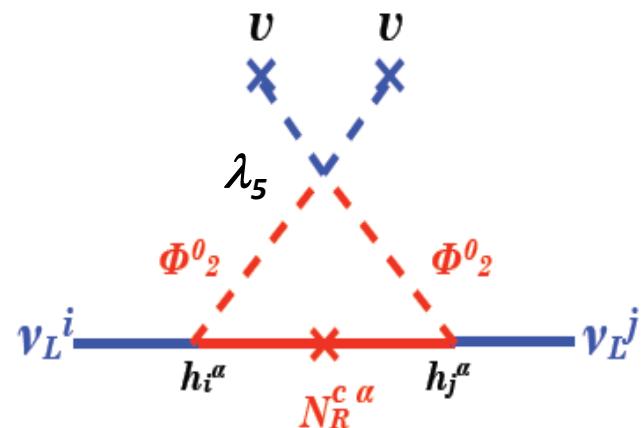
A special 2HDM:  $\Phi_2 = (\xi^+, \xi_r^0 + i \xi_i^0)$  does not receive VEV

The second doublet is so-called Inert Doublet, or Dark Doublet

Example of parameters that explain the neutrino data, LFV data and the WMAP:

$$M_N^\alpha = 3 \text{ TeV}, M_{\xi_r} = 50 \text{ GeV}, M_{\xi_i} = 60 \text{ GeV}, M_{\xi^+} = 100 \text{ GeV}$$

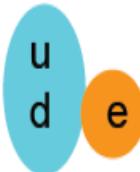
$$\lambda_5 = O(10^{-2}) \quad h_i^\alpha = O(10^{-5})$$



Type X

$\Phi_1$

$\Phi_2$



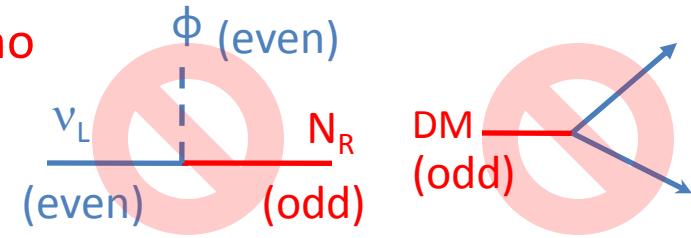
# The 3-loop model (AKS)

M.Aoki, SK, O.Seto, PRL 102,051805(2009)

Source of the Majorana nature: TeV-scale RH neutrino

Exact  $Z_2$ -parity : No tree-level neutrino Yukawa

Model: Type-X 2HDM ( $Z_2$ -even  $\Phi_1, \Phi_2$ )  
+ singlet scalars ( $Z_2$ -odd  $\eta, S$ -)  
+ RH-Neutrino ( $Z_2$ -odd  $N_R$ )



1. Neutrino masses are generated at 3-loop.

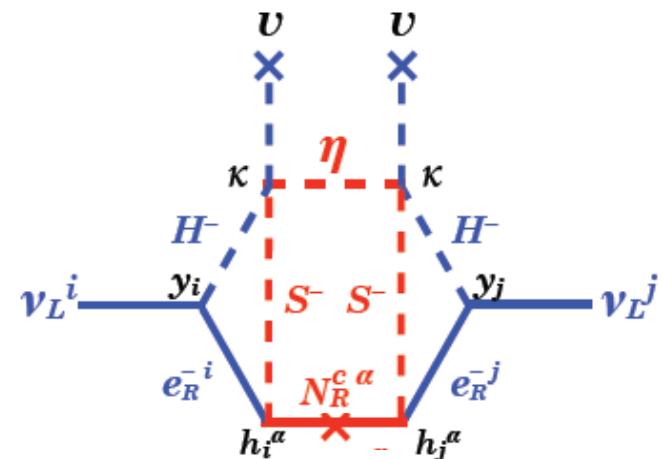
2. DM: the lightest  $Z_2$  odd particle .

DM candidate: Either  $\eta$  or  $N_R$

3. Electroweak Baryogenesis

1<sup>st</sup> order phase transition

Extra CP Phases

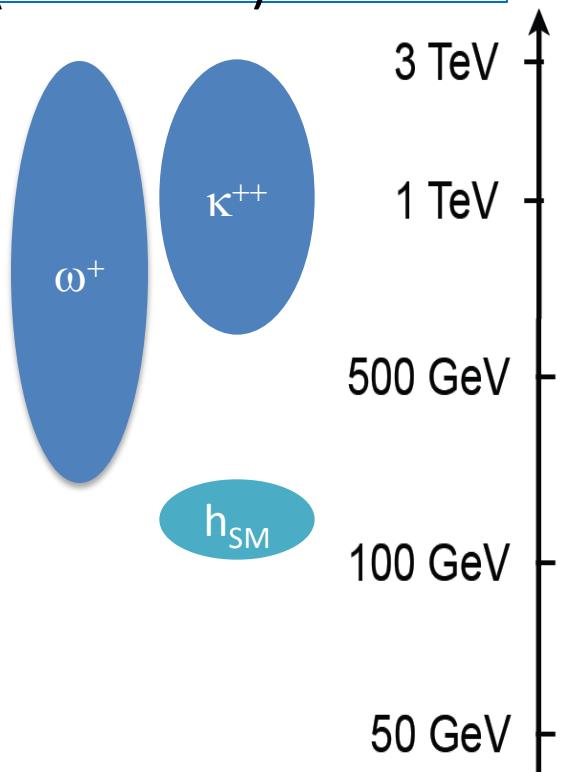


In addition, 3-loop generation may be more natural to explain tiny neutrino masses by the TeV-scale dynamics. [ with Coupling =  $O(1)$  ]

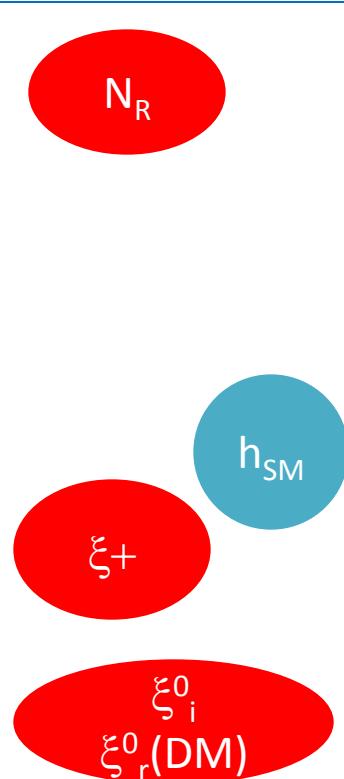
$$h_e^{1,2} = \kappa = O(1) \gg h_\mu^{1,2} \gg h_\tau^{1,2} \text{ for } M_{N_R}^\alpha = 3\text{TeV}, \dots$$

# Typical mass spectra in RSMs

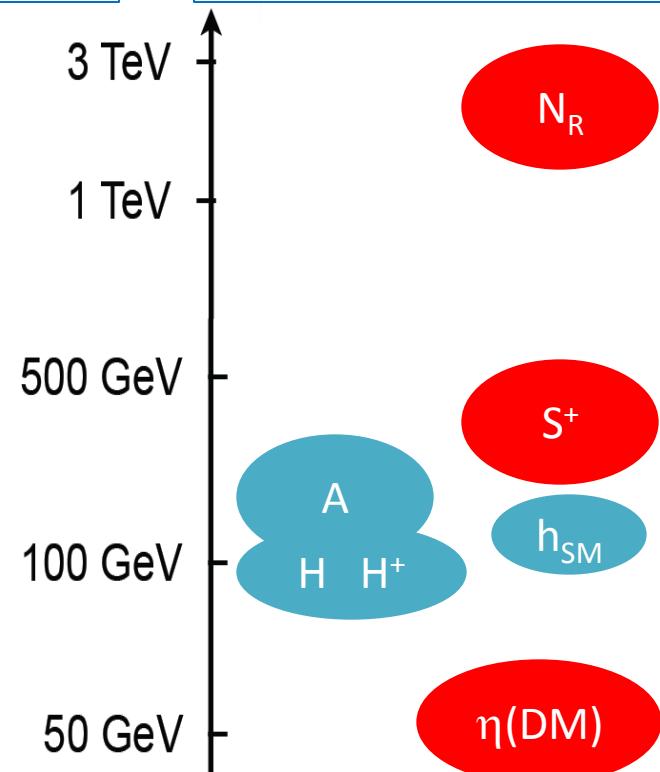
The 2-loop model  
(Zee-Babu)



The 1-loop model  
(Ma)



The 3-loop model  
(Aoki-Kanemura-Seto)



● L=2

● Normal

● Z<sub>2</sub>-odd

# Test of the models at collider experiments

Common features of the radiative seesaw models

## Extended Higgs sector

Charged Higgs physics (all)

Physics of  $\kappa^{++}$  (Zee-Babu model)

Scalar DM (Ma, AKS)  $\rightarrow$  invisible decay of the SM-like Higgs

## The Majorana nature

LNV couplings (Zee-Babu)

or TeV-scale  $N_R$  with  $Z_2$  parity (Ma, AKS)

LHC: pp

(7 TeV 1fb $^{-1}$ , 14 TeV 10-100fb $^{-1}$ )

Structure of Higgs sector,  
Invisible decay of Higgs can be  
explored

ILC:  $e^+e^-$ ,  $e^-e^+$

(E=300GeV-1TeV, 100fb $^{-1}$ -1ab $^{-1}$ )

Not only the Higgs sector and  
DM, but also Majorana nature  
can be explored

# Physics of Extra Higgs at LHC

Ma model

Cao, Ma, PRD76, 095011 (2007)

$$pp \rightarrow \xi_i^0 \xi_r^0 \rightarrow Z^* \xi_r^0 \xi_r^0 \rightarrow f\bar{f} \xi_r^0 \xi_r^0$$

$\mathcal{L} = 100 \text{ fb}^{-1}$

$m_{\xi^0} = 150 \text{ GeV}$

Signal:  $\text{II} + \cancel{E_T}$

	Basic	Optimal
signal	117	37
BG (WW,ZZ)	$1.3 \times 10^5$	62
$S/\sqrt{B}$	0.32	4.70

3-loop (AKS) model

Aoki, SK, Tsumura, Yagyu (2009)

$$pp \rightarrow AH^\pm \rightarrow \tau^+ \tau^- \tau \nu \quad (\text{Type-X Yukawa})$$

$\mathcal{L} = 100 \text{ fb}^{-1}$

(type-II 2HDM:  $b\bar{b}\tau\nu$ )

	Basic
$\tau^+ \tau^- \tau \nu$	$1.7 \times 10^4$
BG(ZW $^\pm$ )	$1.1 \times 10^4$
$S/\sqrt{B}$	162

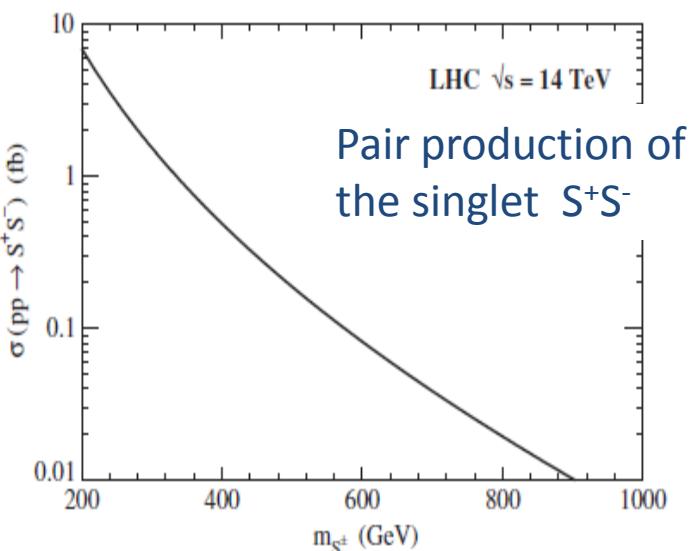
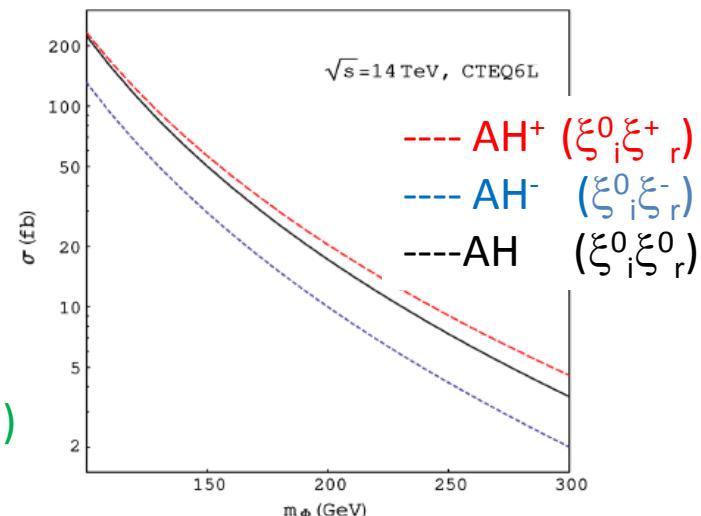
For the singlet  $S^+$ ,  
challenging @ LHC

$$pp \rightarrow S^+ S^- \rightarrow H^+ H^- \eta\eta \quad (0.37 \text{ fb})$$

$$pp \rightarrow H^+ H^- \quad (54 \text{ fb})$$

$m_S = 400 \text{ GeV}, m_{H^\pm} = 150 \text{ GeV}$

Pair production of  
the second doublet scalars



# Physics of Extra Higgs at LHC

## Zee-Babu model

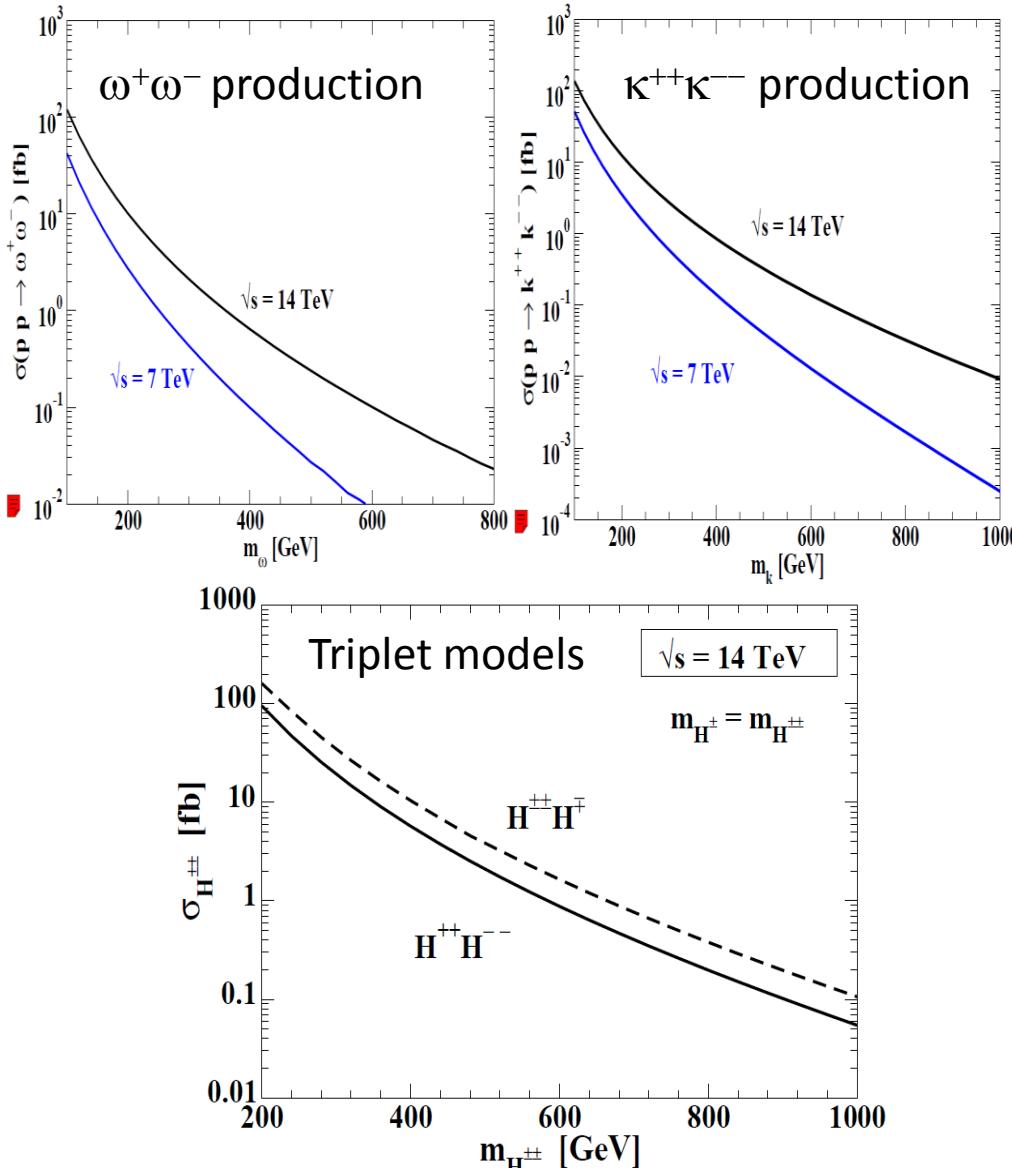
- Singly charged Higgs
- Doubly charged scalars can be discovered at LHC if it is lighter than 800 GeV

Discrimination from triplet models?

Triplet:  $(H^{++}, H^+, H^0)$

$W^+H^+H^{--}$  coupling is a useful probe

- Derivative gauge coupling in the triplet model
- No-such coupling in Zee-Babu model

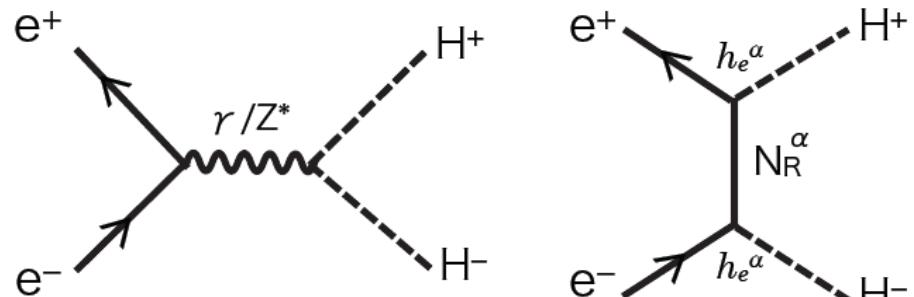
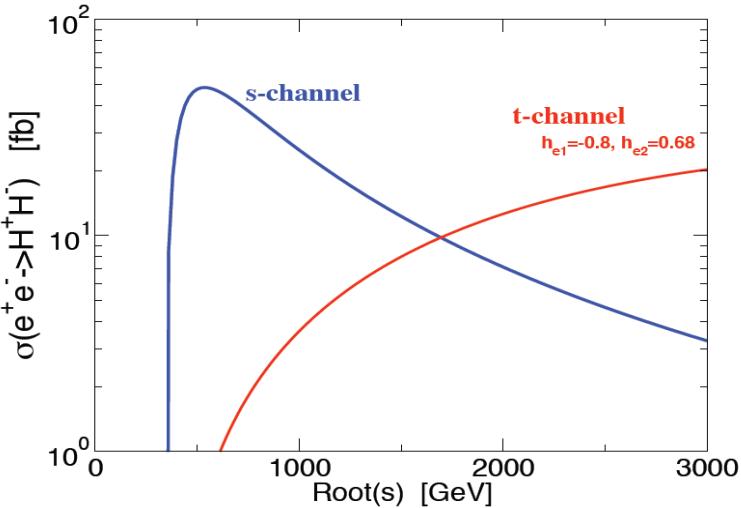


ILC

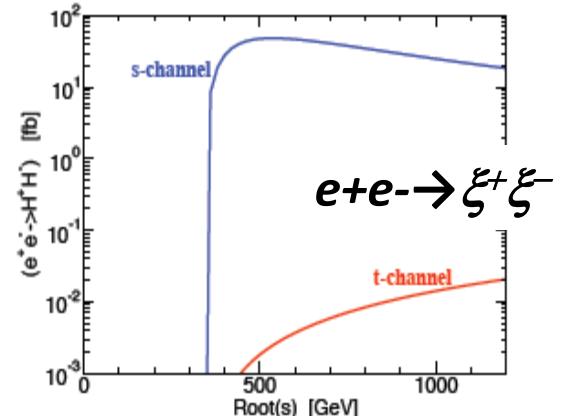
# TeV Right handed neutrinos at ILC

## Radiative Seesaw

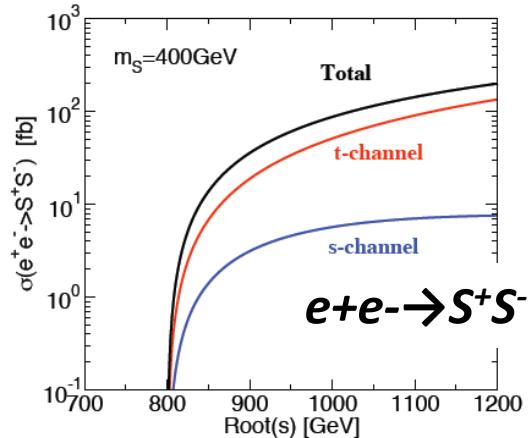
- $Z_2$ -odd RH neutrinos
- Differently from tree level seesaw scenario,  $h_e^\alpha$  coupling can be even  $O(1)$  in RSMs
- The t-channel NR mediation diagram can be significant



1-loop model  
(Ma)  
 $h_e^\alpha < 10^{-2}$   
s-channel dominannt



3-loop model  
(AKS)  
 $h_e^\alpha = O(1)$   
t-channel dominannt



# Ma model

$M_N^\alpha = 3 \text{ TeV}$ ,  $M_{\xi_r} = 50 \text{ GeV}$ ,  
 $M_{\xi_i} = 60 \text{ GeV}$ ,  $M_{\xi^+} = 100 \text{ GeV}$   
 $\lambda_5 = O(10^{-2})$     $h_i^\alpha = O(10^{-5})$

$\sigma(e^+e^- \rightarrow \xi^+\xi^-) = 92 \text{ (10) fb}$   
 $(m_{H^\pm} = 100 \text{ (150) GeV for } E=500\text{GeV})$

$e^+e^- \rightarrow \xi^+\xi^-$

$\rightarrow W^+W^- (*) \xi_r^0 \xi_r^0$

$\rightarrow jjjj \xi_r^0 \xi_r^0 (jj\mu\nu \xi_r^0 \xi_r^0)$

$m_{\xi^+} = 100 \text{ GeV}$

Signal:  $jj \mu + \cancel{E}$

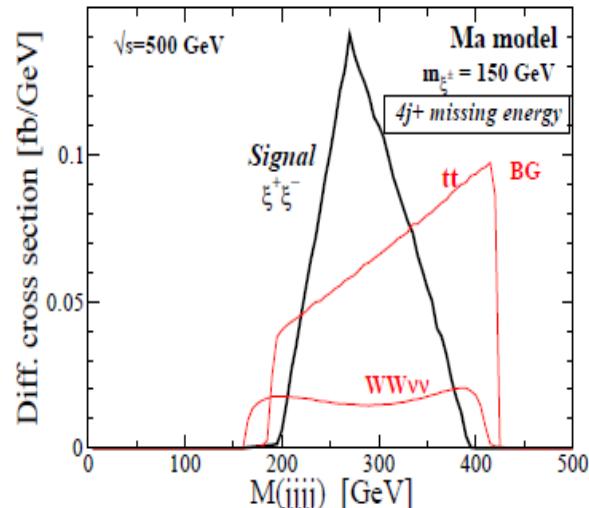
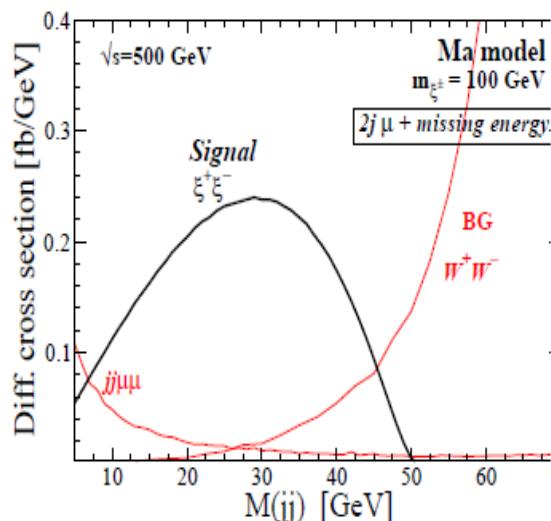
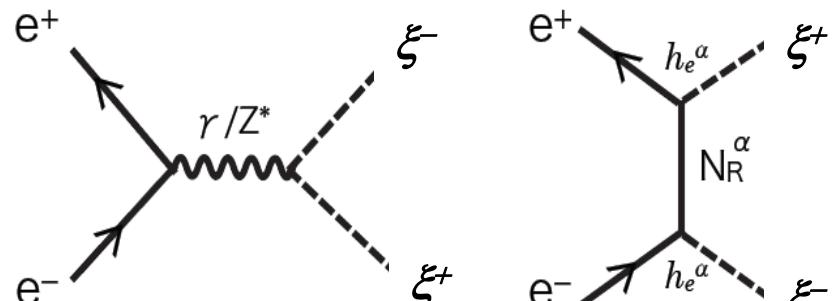
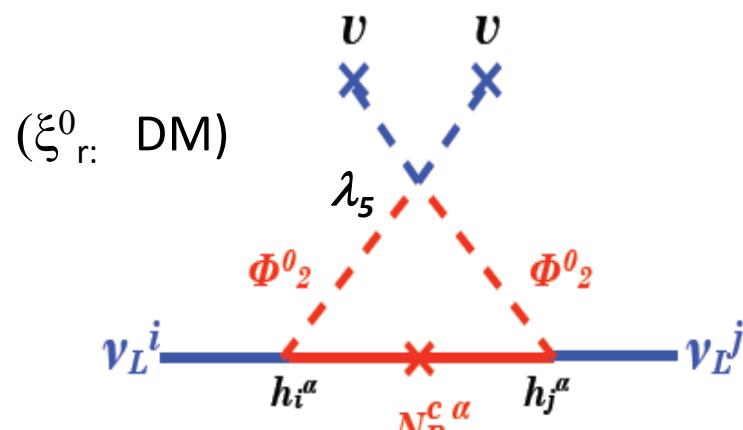
Main BG:  $WW^*$

$ZZ, \gamma\gamma, Z\gamma$  with a  $\mu$  missing

$m_{\xi^+} = 150 \text{ GeV}$

Signal:  $4 jjjj + \cancel{E}$

Main BG:  $WW vv, tt$



# 3-loop Model (AKS)

$h_e^{1,2} = \kappa = O(1) >> h_\mu^{1,2} >> h_\tau^{1,2}$   
 for  $M_{NR}^\alpha = 3\text{TeV}$ ,  $m_{H^\pm} = 100\text{ GeV}$ ,  $m_\eta = 50\text{GeV}$

t-channel effect dominant

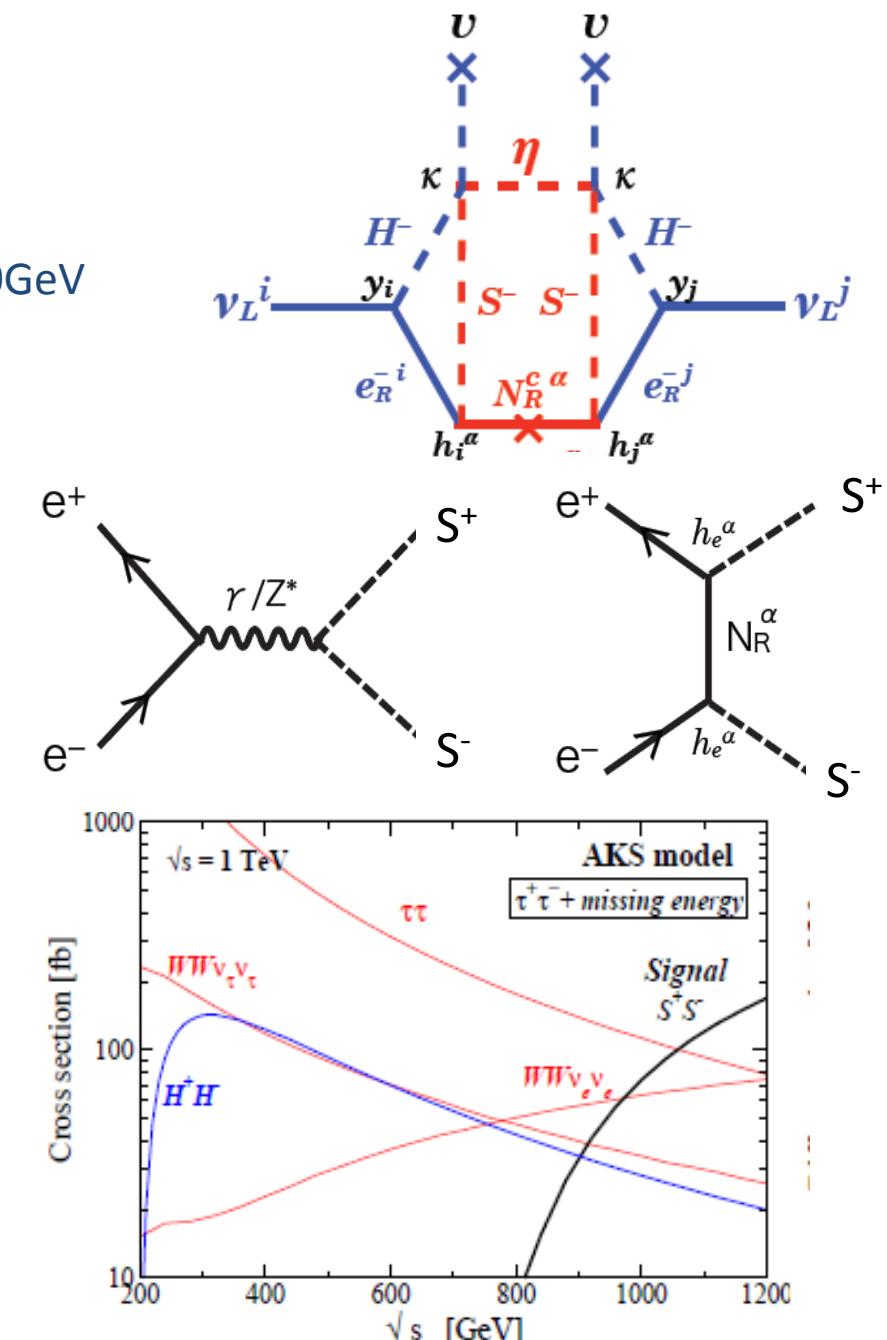
$\sigma(e^+e^- \rightarrow S^+S^-) = 87\text{ fb}$   
 $(m_{S^\pm} = 400\text{ GeV for } E=1\text{TeV})$

$B(S^+ \rightarrow H^+\eta) = 100\%$   
 $B(H^+ \rightarrow \tau^+\eta) \sim 100\%$

$e^+e^- \rightarrow S^+S^-$   
 $\rightarrow H^+H^- \eta\eta$   
 $\rightarrow \tau^+\tau^- \nu\nu \eta\eta$

Signal:  $\tau^+\tau^- + \cancel{E}$

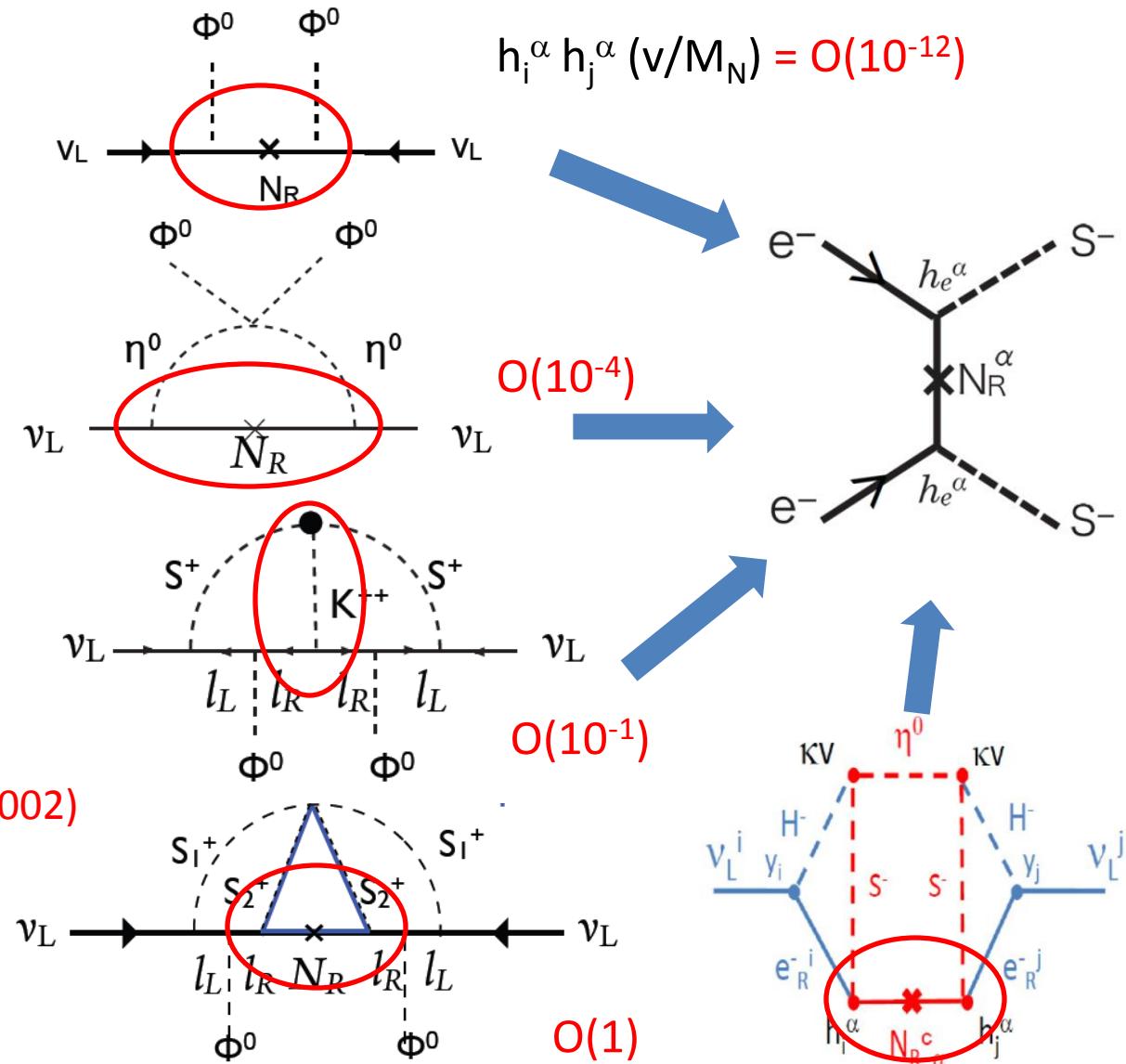
Main BG  $\tau^+\tau^-$ ,  $\tau^+\tau^- \nu\nu$ ,  
 $H^+H^-$



# Direct Test of Majorana Nature at e<sup>-</sup>e<sup>-</sup> collisions at ILC

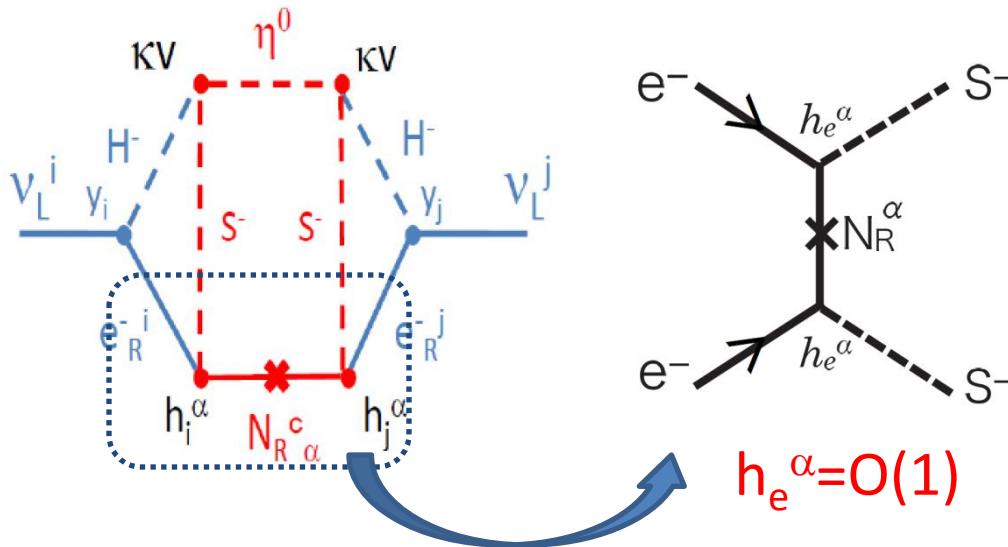
- Tree Seesaw
- 1-loop Seesaw  
E. Ma
- 2-loop Seesaw  
Zee-Babu
- 3-loop Seesaw

Krauss, Nasri, Trodden (2002)  
Aoki, SK, Seto (2009)



# Test the Majorana Nature at ILC

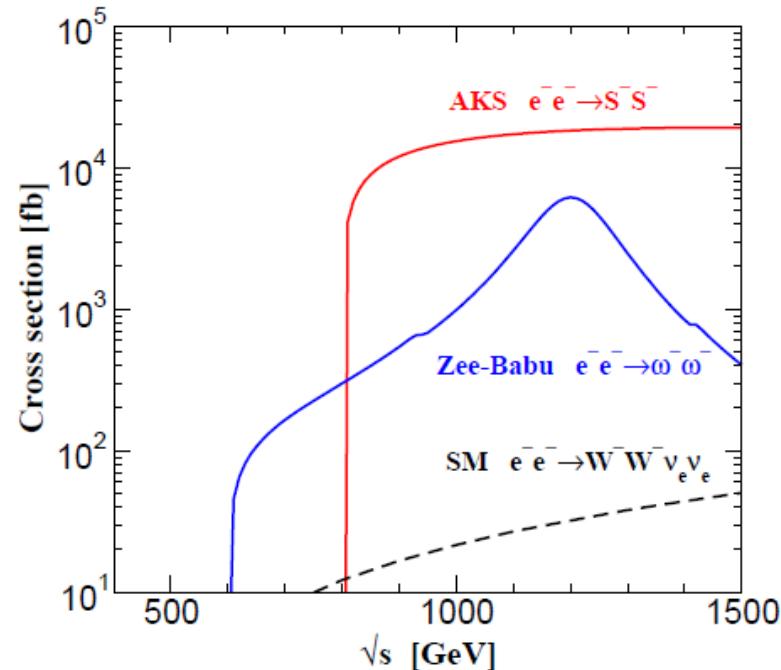
- The sub-diagram itself can be directly measured at the  $e^-e^-$  collision.



$$\sigma(e^-e^- \rightarrow S^-S^-) = \int_{t_{\min}}^{t_{\max}} dt \frac{1}{64\pi s} \left| \sum_{\alpha=1}^n (|h_e^\alpha|^2 m_{N_R^\alpha}) \left( \frac{1}{t-m_{N_R^\alpha}^2} + \frac{1}{u-m_{N_R^\alpha}^2} \right) \right|^2$$

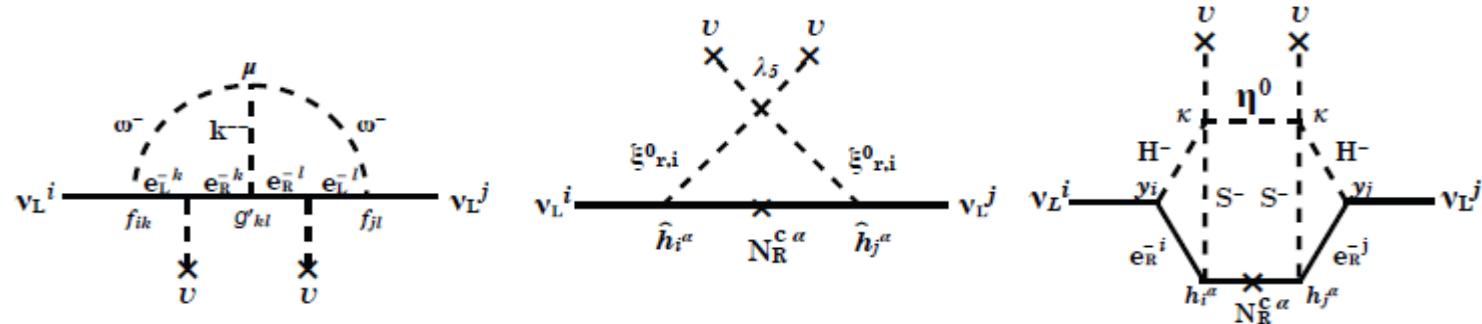
Signal:  $\tau^-\tau^- + \cancel{E}$  (AKS);  $\mu^-\mu^- + \cancel{E}$  (Zee-Babu)

Aoki, SK, arXiv:1001.0092



There is no substantial BG, the signals can be easily seen

# Summary



- **Radiative seesaw models** are interesting , where the scale of neutrino mass generation can be lowered to TeV scales.
- We discussed **collider phenomenology** in these models
- They are characterized by
  - Extended Higgs sector
  - The Majorana nature (LNV interaction, TeV RH neutrinos)
- At the LHC, the Higgs sectors can be tested at LHC.
- The Majorana nature can also be directly tested at the ILC.
- The combined study at LHC and ILC ( $e^+e^-$ ,  $e^-e^-$ ) can clarify the possibility of radiative seesaw scenarios.

# Backup

# Physics of $\eta$ (DM)

## Invisible Decay of $h$

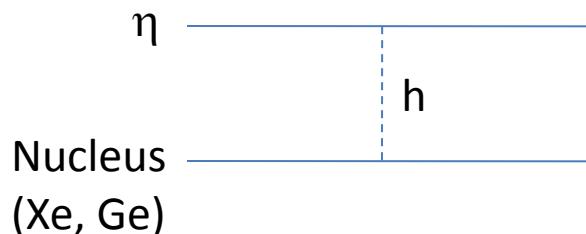
$h$  is the SM-like Higgs but can decay into  $\eta\eta$ .

$$B(h \rightarrow \eta\eta) = 36 \text{ (34)} \% \text{ for } m_\eta = 48 \text{ (55) GeV}$$

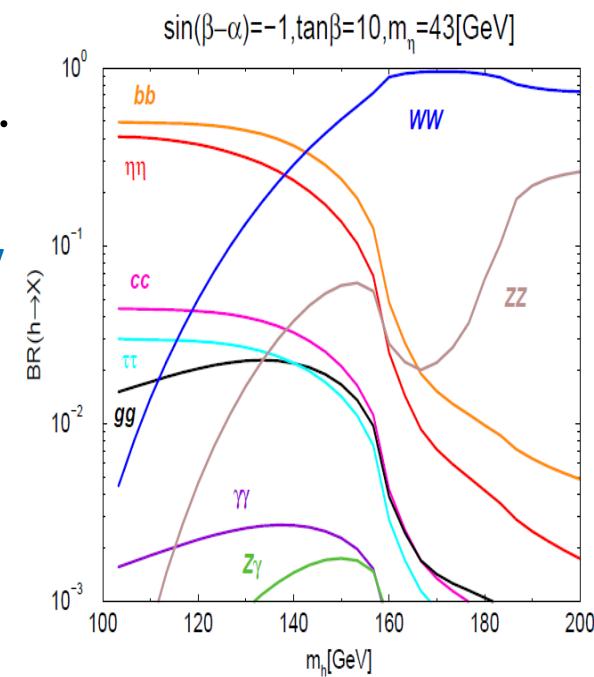
Testable via the invisible Higgs decay at LHC

## Direct Search

$\eta$  from the halo can basically be detected  
at the direct DM search (CDMS, XMASS)



Observing the release energy

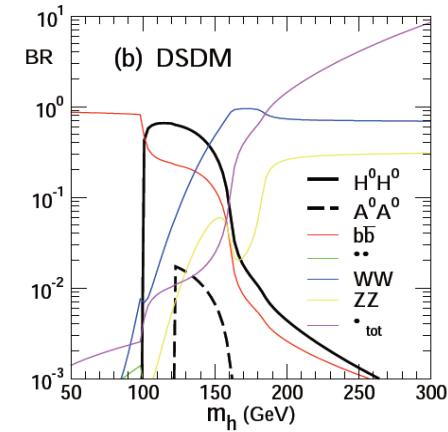
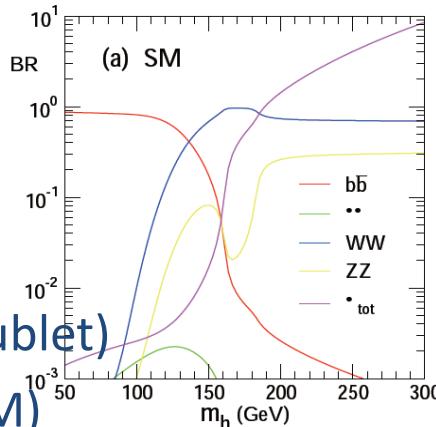


# Extended Higgs sector in RSMs

Higgs Invisible decay

$$\text{Ma} \quad h_{\text{SM}} \rightarrow \xi_r^0 \xi_r^0$$

$$\text{AKS} \quad h_{\text{SM}} \rightarrow \eta \eta$$



Extra Neutral Higgs bosons

$$\text{Ma} \quad \xi_i^0 \rightarrow Z^* \xi_r^0 \quad (\text{Inert doublet})$$

$$\text{AKS} \quad H^0 \rightarrow \tau \tau \quad (\text{Type-X 2HDM})$$

$$[\text{MSSM} \quad H^0 \rightarrow b\bar{b} \quad (\text{Type-II 2HDM})]$$

Singly charged Higgs bosons

$$\text{Zee-Babu} \quad \omega^+ \rightarrow \mu \nu, \tau \nu \quad (> e \nu)$$

$$\text{Ma} \quad \xi^+ \rightarrow l^+ \nu \xi_r^0 \quad (\text{Inert doublet})$$

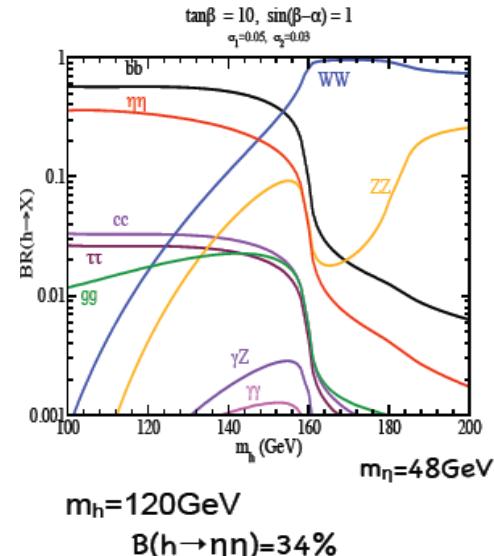
$$\text{AKS} \quad H^+ \rightarrow \tau \nu \quad (\text{Type-X 2HDM})$$

$$S^+ \rightarrow H^+ \eta \rightarrow \tau \nu \eta$$

$$[\text{MSSM} \quad H^+ \rightarrow t \bar{b}, \tau \nu \quad (\text{Type-II 2HDM})]$$

Doublely charged Higgs boson

$$\text{Zee-Babu} \quad \kappa^{--} \rightarrow \mu^- \mu^-$$

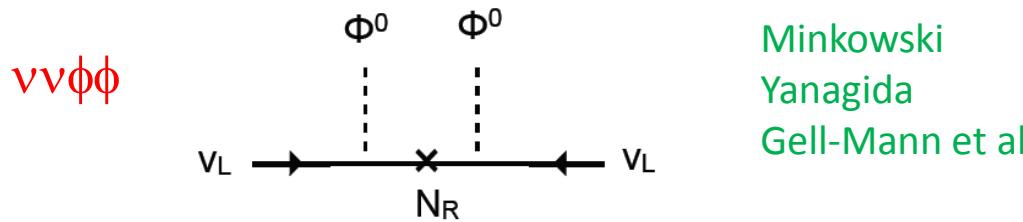


# Seesaw Mechanism?

Super heavy RH neutrinos ( $M_{NR} \sim 10^{10-15} \text{ GeV}$ )

- Hierarchy between  $M_{NR}$  and  $m_D$  generates that between  $m_D$  and tiny  $m_\nu$  ( $m_D \sim 100 \text{ GeV}$ )

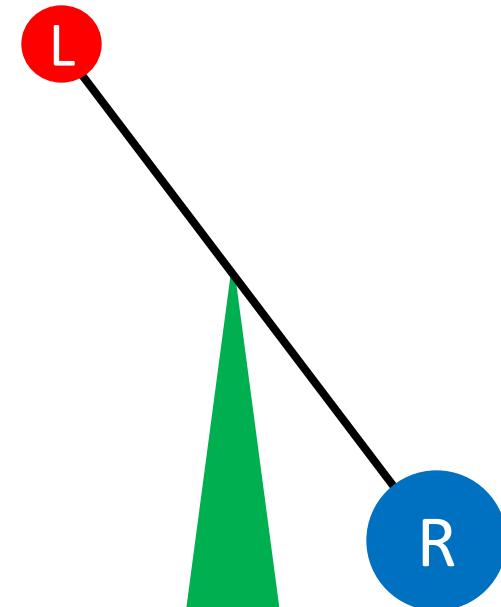
$$m_\nu = m_D^2 / M_{NR}$$



- Simple, compatible with GUT etc
- Introduction of a super high scale

Hierarchy for hierarchy!

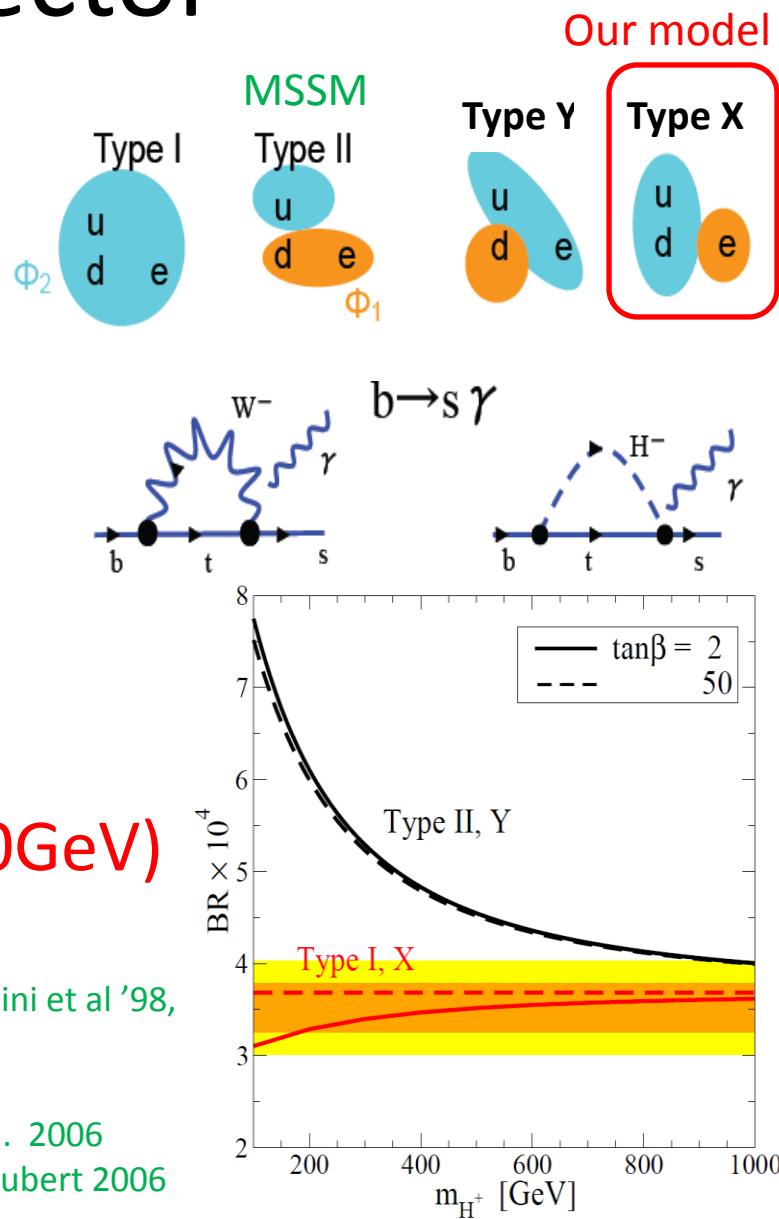
Far from experimental reach...



# The Higgs sector

- The Higgs sector  
 $\Phi_1, \Phi_2$  (2HDM) +  $S^+, \eta$  (singlets)
  - To avoid FCNC, additional softly-broken  $Z_2$  symmetry is introduced :  
 $\Phi_1 \rightarrow +\Phi_1, \Phi_2 \rightarrow -\Phi_2$   
by which each quark-lepton couples to only one of the Higgs doublets.
  - 4 types of Yukawa interactions!
- Neutrino data prefer a light  $H^+(< 200\text{GeV})$
- Choose Type-X Yukawa to avoid the constraint from  $b \rightarrow s\gamma$ .

$\Phi_1$  only couples to Leptons  
 $\Phi_2$  only couples to Quarks



# Lagrangian

$$SU(3) \times SU(2) \times U(1) \times Z_2 \times \tilde{Z}_2$$

$Z_2$  even(2HDM) +  $Z_2$  odd( $S^+$ ,  $\eta^0$ ,  $N_R^\alpha$ )

$Z_2$  (exact) : to forbid tree  $\nu$ -Yukawa  
and to stabilize DM  
 $\tilde{Z}_2$  (softly-broken): to avoid FCNC

$$\begin{aligned} V = & -\mu_1^2 |\Phi_1|^2 - \mu_2^2 |\Phi_2|^2 - (\mu_{12}^2 \Phi_1^\dagger \Phi_2 + \text{h.c.}) \\ & + \lambda_1 |\Phi_1|^4 + \lambda_2 |\Phi_2|^4 + \lambda_3 |\Phi_1|^2 |\Phi_2|^2 \\ & + \lambda_4 |\Phi_1^\dagger \Phi_2|^2 + \left\{ \frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \text{h.c.} \right\} \end{aligned}$$

$Z_2$  even 2HDM

$$+ \mu_s^2 |S|^2 + \lambda_s |S|^4 + \frac{1}{2} \mu_\eta \eta^2 + \lambda_\eta \eta^4 + \xi |S|^2 \eta^2$$

$Z_2$  odd scalars

$$+ \sum_{a=1}^2 \left\{ \rho_a |\Phi_a|^2 |S|^2 + \sigma_a |\Phi_a|^2 \frac{\eta^2}{2} \right\}$$

Interaction

$$+ \sum_{a,b=1}^2 \left\{ \kappa \epsilon_{ab} (\Phi_a^c)^\dagger \Phi_b S^- \eta + \text{h.c.} \right\}.$$

RH neutrinos

$$\mathcal{L}_Y = - \sum_{\alpha=1}^2 \sum_{i,j=1}^3 h_i^\alpha (e_R^i)^c N_R^\alpha S^- + \sum_{\alpha=1}^2 m_N^\alpha N_\alpha^c N_\alpha + \text{h.c..}$$

# Strong 1<sup>st</sup> Order Phase Transition

Effective Potential at high T

$$V_{\text{eff}} \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4$$

Sphaleron decoupling

$$\frac{\varphi_c}{T_c} \left( = \frac{2E}{\lambda_{T_c}} \right) \gtrsim 1 \quad \lambda_T \sim \frac{2m_h^2}{v^2}$$

SM  $E_{SM} \simeq \frac{1}{12\pi v^3} (6m_W^3 + 3m_Z^3)$   $m_h \lesssim 65 \text{ GeV}$

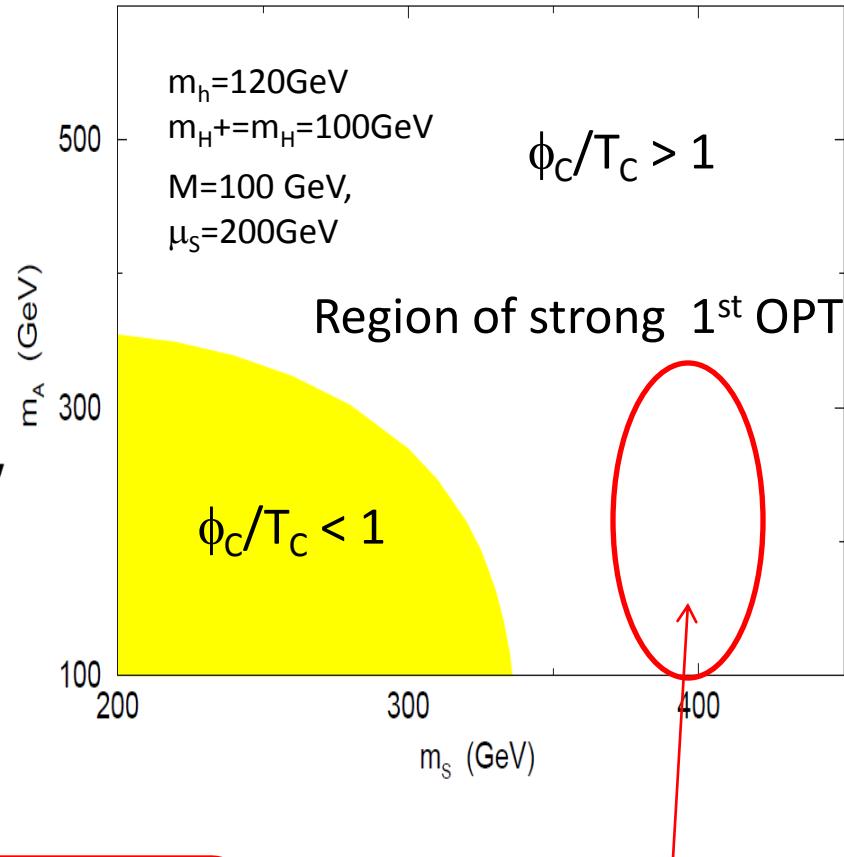
In SM,  $m_h$  is too smaller than LEP bound

Our Model

$$E \simeq \frac{1}{12\pi v^3} (6m_W^3 + 3m_Z^3 + \underline{m_A^3 + 2m_{S^\pm}^3})$$

The condition can be satisfied with  $m_h > 114 \text{ GeV}$ ,  
when A and/or  $S^\pm$  have  
non-decoupling property.

$$m_{S^\pm}^2 \sim \lambda_S v^2$$



This region is compatible with neutrino data and DM abundance.