



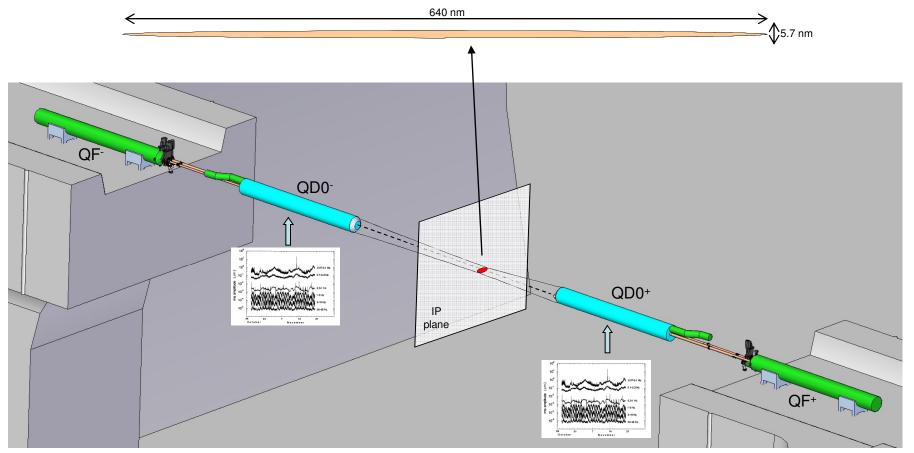
# Introduction



Sub-nanometric stability of the focusing system is required to maintain the luminosity to within a few percent of the design value.

Ground motion is a source of vibrations which would continuously misaligning the focusing elements.

The design of the support of the QD0 is a fundamental issue







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### Luminosity feedback systems and stability

Two Luminosity Feedback systems are implemented in ILC:

A 5 Hz to control the orbit in the BDS (low frequency)

A Intra-train system to address ground motion and mechanical disturbances (high frequency~1000 Hz)

The mechanical stability requirements of the QD0 are set by the capture range of the IP fast feedback, as written in the "Functional Requirements" document, ILC-Note-2009-050

 $\bullet$  QD0 alignment accuracy:  $\pm$  200 nm and 0.1  $\mu$ rad from a line determined by QF1s, stable over the 200ms time interval between bunch trains



• QD0 vibration stability:  $\Delta(QD0(e+)-QD0(e-)) < 50$  nm within 1ms long bunch train "

<sup>&</sup>quot;The QD0 mechanical alignment accuracy and stability after beam-based alignment and the QD0 vibration stability requirement are set by the capture range and response characteristics [8] of the inter-bunch feedback system.



### Ground motions (A.Seryi et al.)



Ground vibrations measurements are available for all the major accelerators sites in form of Power Spectrum Densities. Datasets available at <a href="http://vibration.desy.de">http://vibration.desy.de</a>

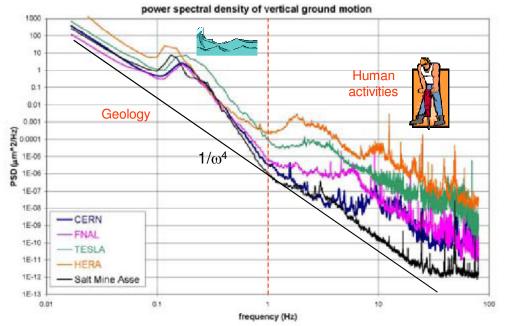
#### Main features:

Separation at ~few Hz between geology and human induced noise (pretty much the separation

between the slow and fast luminosity feedback)

Some site are quiet and some are noisy

Motion falls as  $1/\omega^4$ 



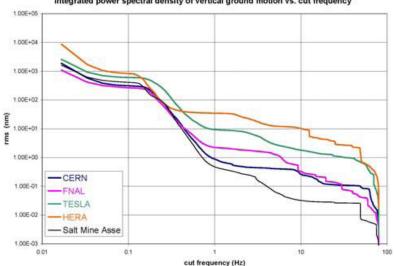
For a given a ground motion time history x(t), the PSD is defined as

$$P(f) = \lim_{T \to \infty} \frac{1}{T} \left| \int_{-T/2}^{T/2} x(t) e^{-i\omega t} dt \right|^2$$

i.e. *PSD* is the Fourier transform of the *autocorrelation* function R(0) of te signal x(t).

The main property of the PSD is that the variance of x(t) is given by:  $\begin{pmatrix} 2 & f_2 \\ -2 & f_3 \end{pmatrix}$ 

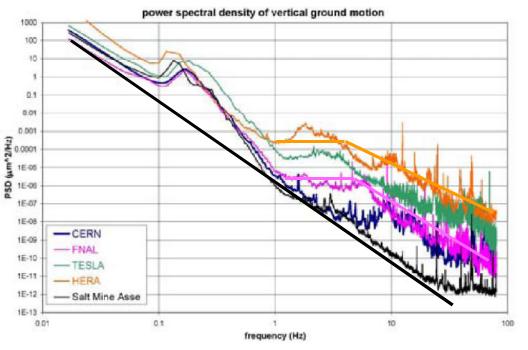
integrated power spectral density of vertical ground motion vs. cut frequency



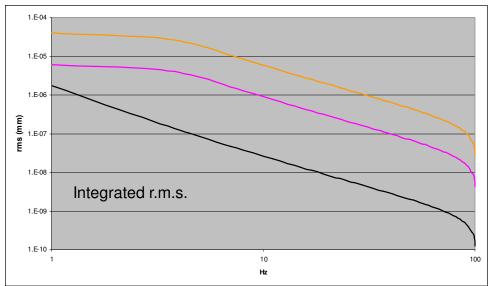


# Simplified PSD Models





$$P(f) \approx \frac{A}{f^4}$$



$$\sigma^2 = \langle x^2 \rangle = \int_{f_1}^{f_2} P(f) df$$

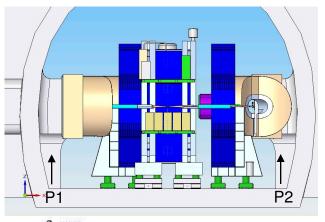
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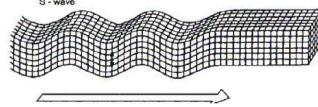


#### Coherence

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Coherence: 
$$N_{12}(f) = \frac{p_{12}}{\sqrt{p_1 p_2}} = J_0(\omega L/v)$$

If P1=P2, then:

Jo = 0th Bessel function

L= distance between points

v = speed of sound in rock, ~3 km/s

$$\rho(\omega,L) = p(\omega) 2\{1 - \text{Re}[N_{12}(\omega,L)]\}.$$

### Relative displacement spectrum

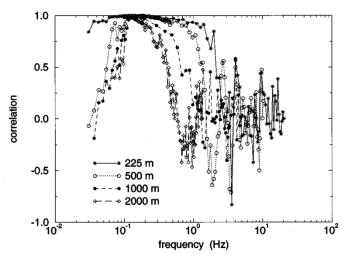


FIG. 3. Correlation spectra of ground motion measured at CERN in the LEP tunnel [7]. The distances between sensors were 225, 500, 1000, and 2000 m.

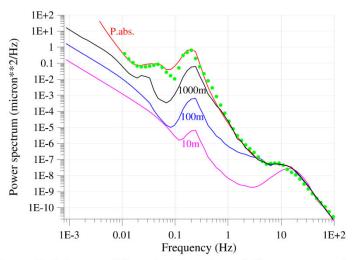


Figure 3: Measured (symbols) and modeling spectra  $p(\omega)$  of absolute motion and  $p(\omega,L)/2$  of relative motion for the 2 a.m. SLAC site ground motion model.



#### Random Vibration effects Metric

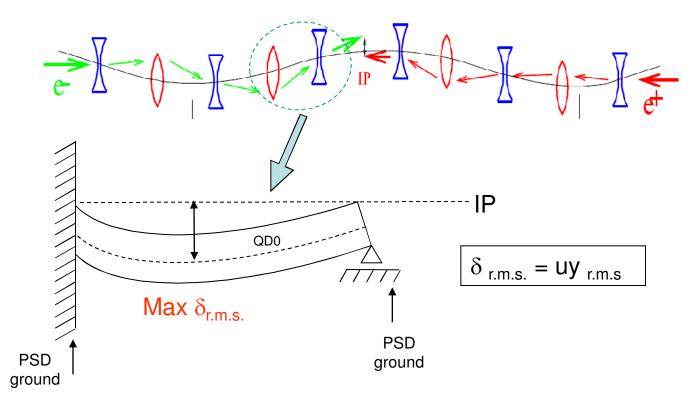


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Ground motion effects are usually accounted as perturbation of the lattice elements through the girders, the magnetic cells assumed point-like (rigid body)

Final Focusing element deforms along the full length under random vibration effects

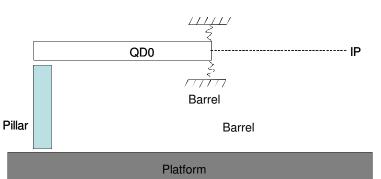
How define the metric of the net effect of the displacement at the IP?

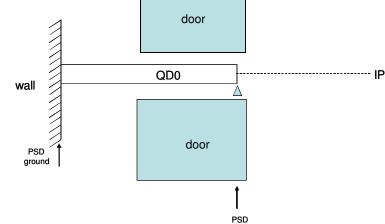




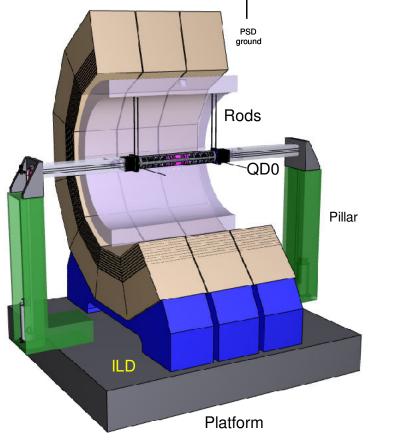


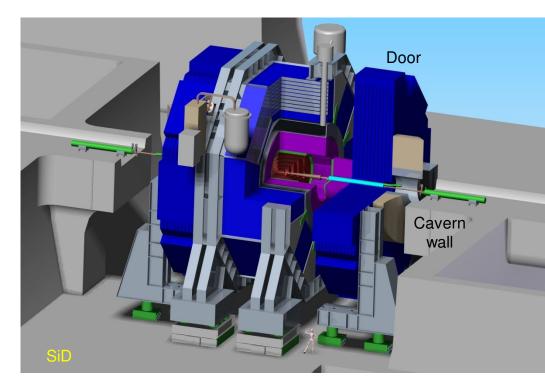
# QD0 supports for ILD and SiD





ground

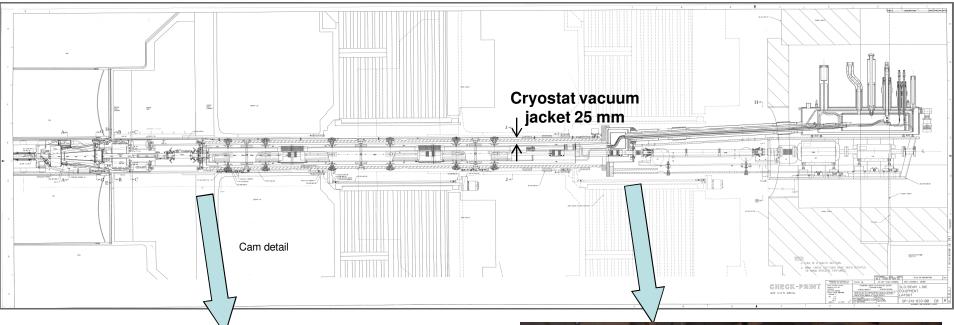






# QD0 integration and movement as in SLD





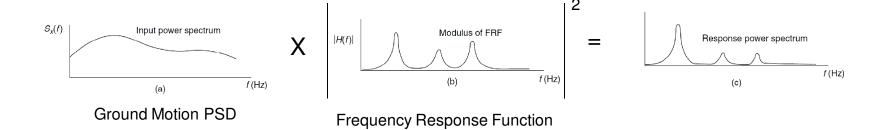






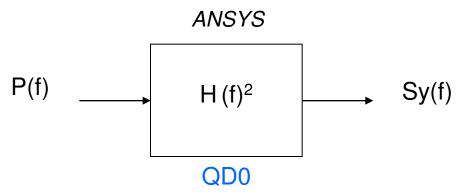
#### **Random vibrations model**





$$P(f) \times |H(f)|^2 = Sy(f)$$

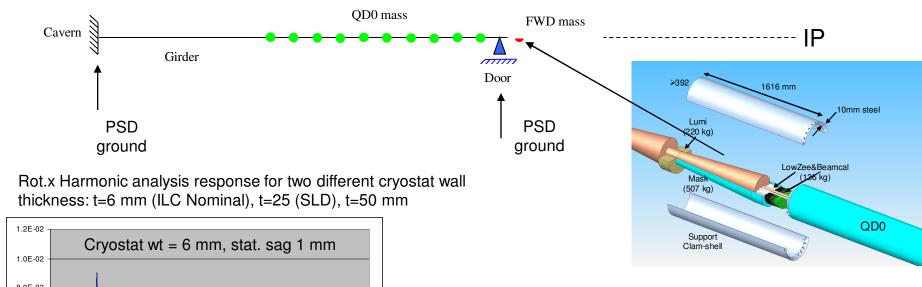
The Frequency Response Function for QD0 and SiD is obtained by FEA (e.g. ANSYS)

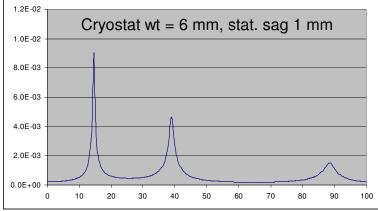


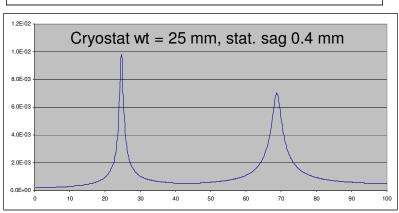


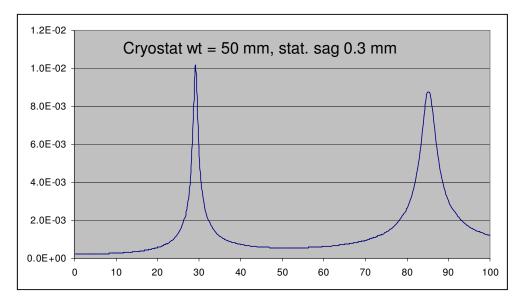
## Frequency Response Function of QD0 on the door







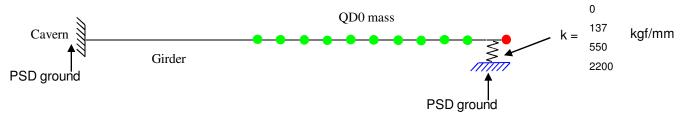


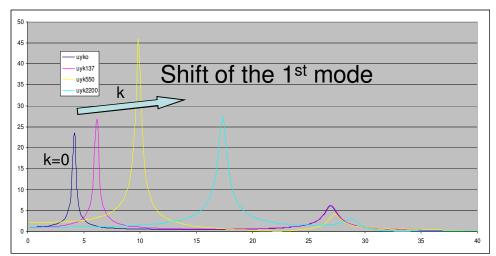


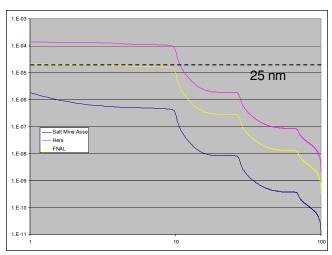


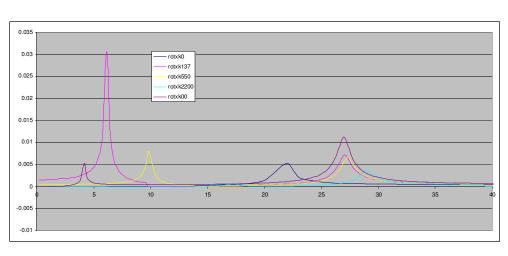


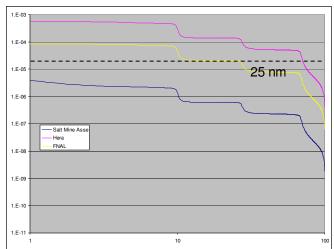
# QDO cantilevered + spring suspension from the barrel







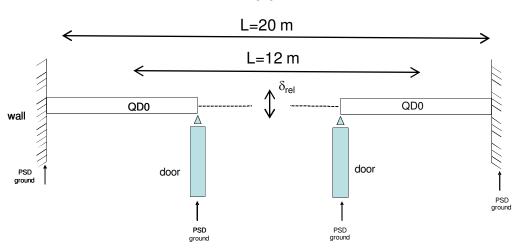


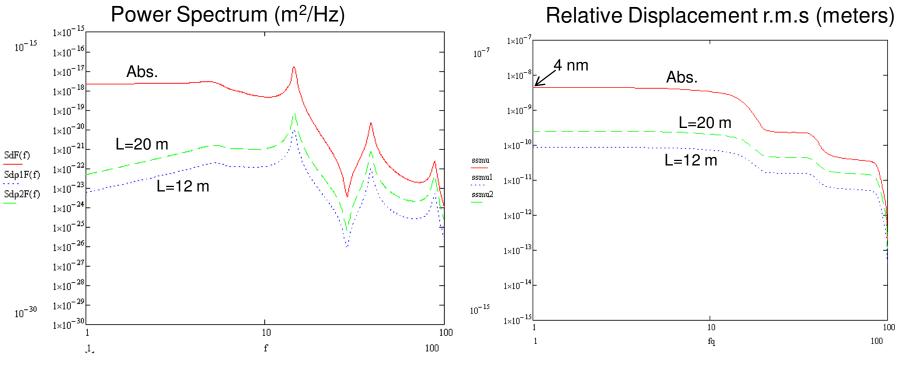






# Ends supported

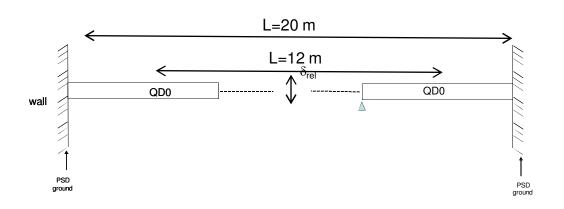




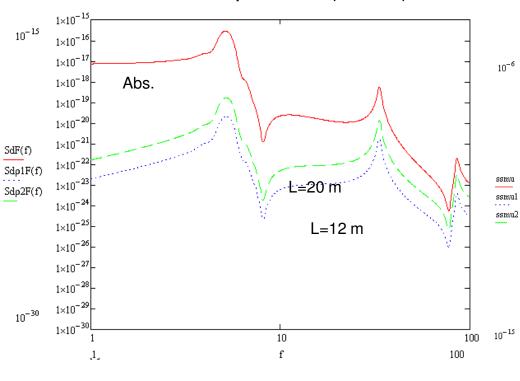


# Cantilevered

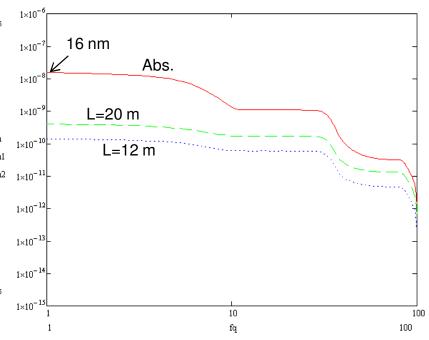




# Power Spectrum (m<sup>2</sup>/Hz)



# Relative Displacement r.m.s (meters)



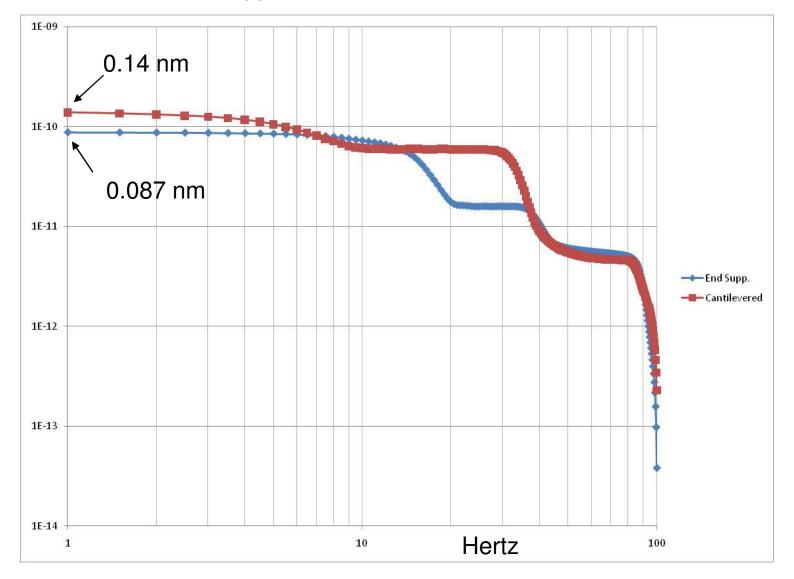


# Relative displacement (r.m.s.) meters



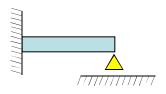
# End Supports vs. Cantilevered QD0

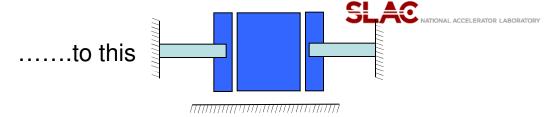


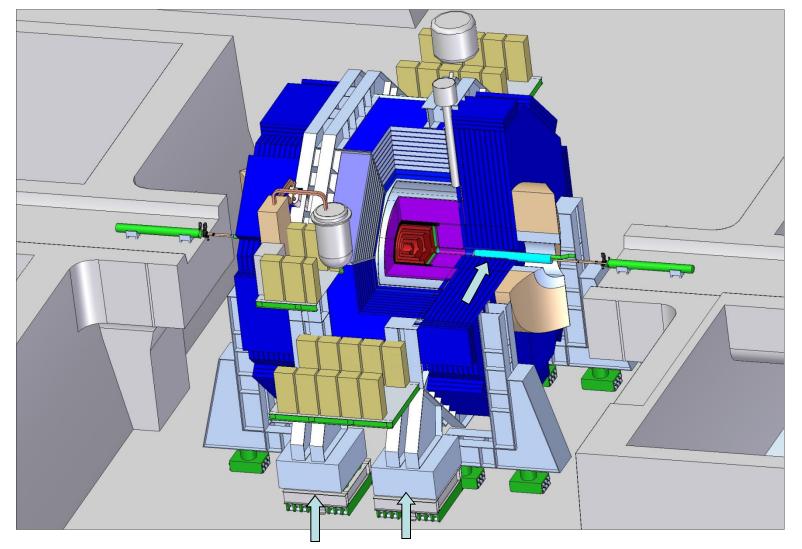




From this....



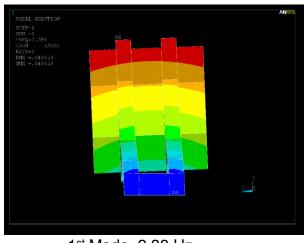




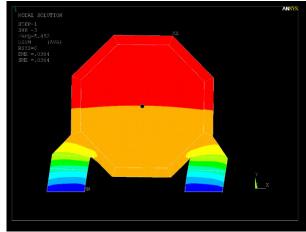
Ground motion through the feet



# SiD Free Vibration Mode



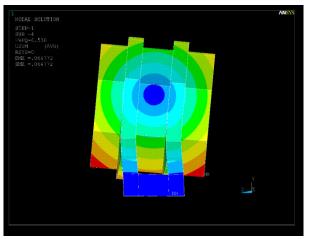
| Notal Sciution | Step-1 | Size -2 | Size -2

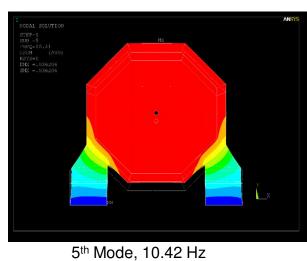


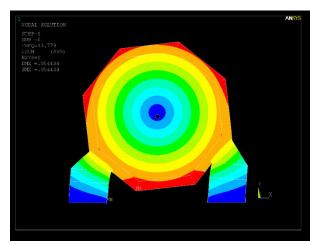
1st Mode, 2.38 Hz

2<sup>nd</sup> Mode, 5.15 Hz

3<sup>rd</sup> Mode, 5.45 Hz



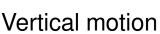




4th Mode, 6.53 Hz

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6th Mode, 13.7 Hz

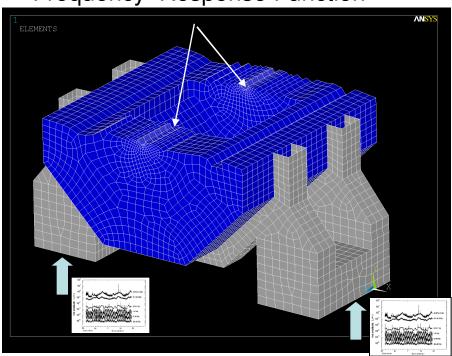


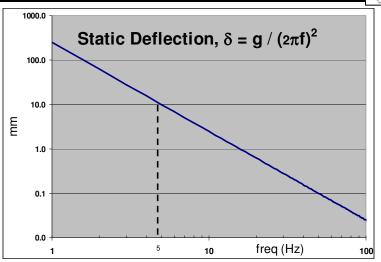


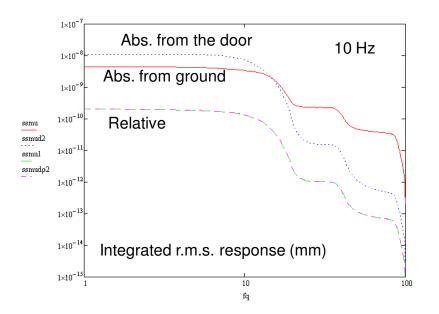
# Harmonic Analysis

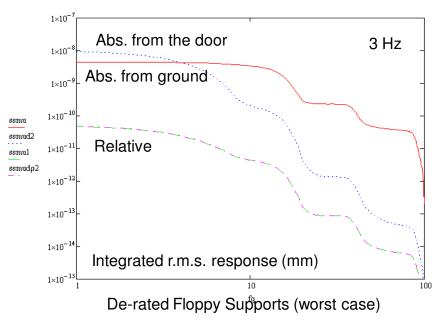


Frequency Response Function













# Conclusions

- Both End-Supports and cantilevered support scheme of the Final Focus show acceptable sub-nanometric relative vibration values.
- The End-Supports provide the lowest r.m.s. relative displacements.
- Providing supports from the doors (as in SiD) is perfectly compatible with the nanometric stability requirements.
- It improve the correlation of the PSD relative noise spectra
- It is a natural way to make a passive isolator (large door Mass low K feet), shifting the high static transmissibility at the floor-detector interface
- It has many advantages like:

Make the Final Focus system an integral part of the detector

Allow to get low L\*

Provide insurance of re-alignment in the push-pull

Simplify the push-pull operation