

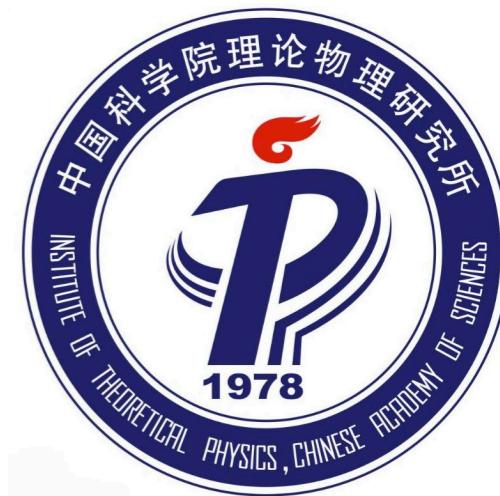
Global fit with operators in W/Z-pole and 4-fermion

Yong Du

email: yongdu@itp.ac.cn

CEPC2021, Nanjing, Nov 9, 2021

In collaboration with Jorge de Blas, Christophe Grojean, Jiayin Gu,
Michael Peskin, Junping Tian, Marcel Vos, Eleni Vryonidou



Overview

Number of operators is large, but usually it is $\mathcal{O}(10)$ if focusing on specific sectors (will see specific examples shortly).

In this talk, I will present our preliminary results from Z/W-pole observables and with the inclusion of 4-fermion operators from a personal view.

The big picture of this ongoing project? See, for example, Jiayin's recent [talk @ILCX2021](#)

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14:00	Anomalous HZZ, HWW couplings 18'	10:30	Towards complete two-loop EW e+e- to ZH 30'
	Speaker: Tomohisa Ogawa (KEK), (k)		Speaker: Dr. Qian Song (University of Pittsburgh)
14:18	Global measurement for Higgs 18'	12:00	Use machine learning to study aQGCs 30'
	Speaker: Gang Li (IHEP)		Speaker: 冀翀 杨 (辽宁师范大学)
16:00	Higgs bosons below 125 GeV at CEPC 22'		
	Speaker: Tania Robens (R)		
16:22	Theory precision for CEPC Higgs measurements 22'		<i>(Not covered)</i>
	Speaker: Sebastian Passehr (RWTH Aachen University)		
16:44	H125 coupling measurement: what to expect and what can we do with it 22'		
	Speaker: Prof. Shinya Kanemura (University of Toyama)		
17:06	Top yukawa couplings and related EFT at 360 GeV 22'		
	Speaker: Zhen Liu (FNAL)		

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Overview

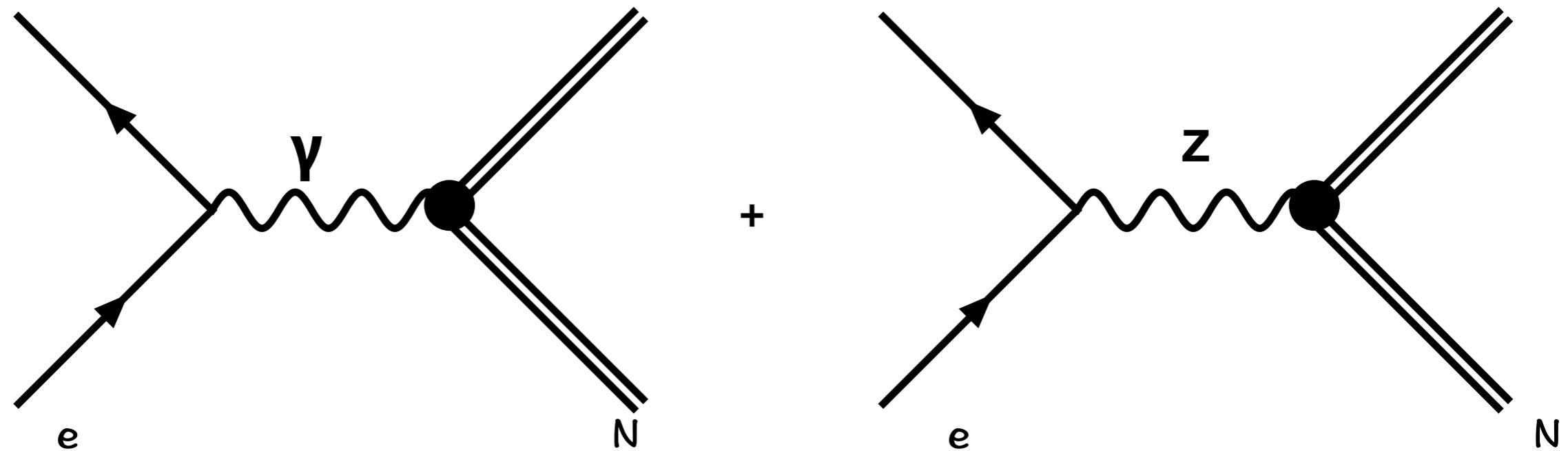
Question:

Why 4-fermion operators?

Short answer: It has not yet been done for future colliders.

Overview: PVES

Parity-violating electron scattering (PVES) has played an essential role in establishing the SM.



14:00

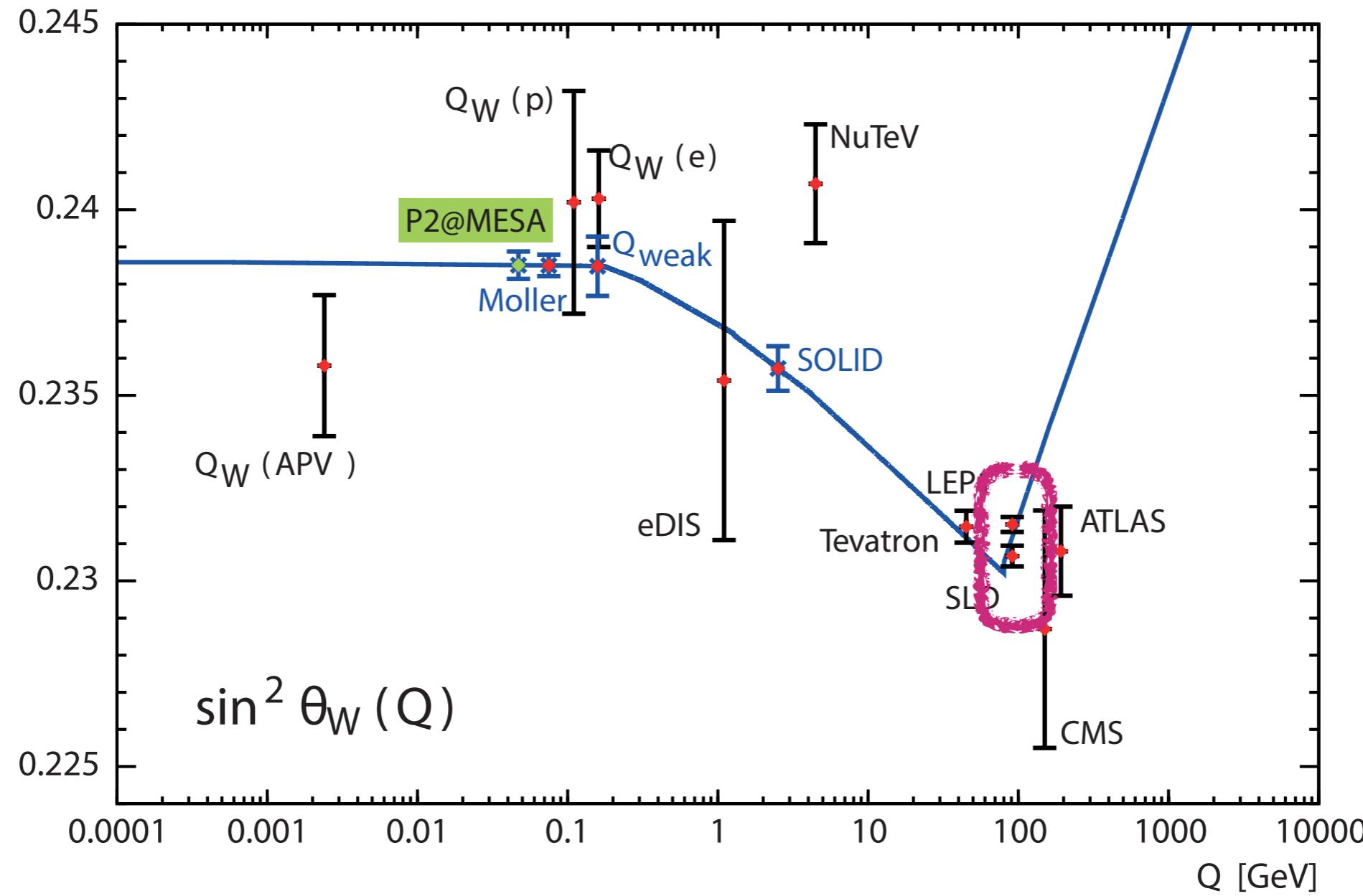
AFB measurement at hadron colliders & weak mixing angle at CEPC 25'

Speaker: 思奇 杨 (University of Science and Technology of China)

Overview: PVES

Future prospects

Aleksejevs et al, 2011, 2012, 2015

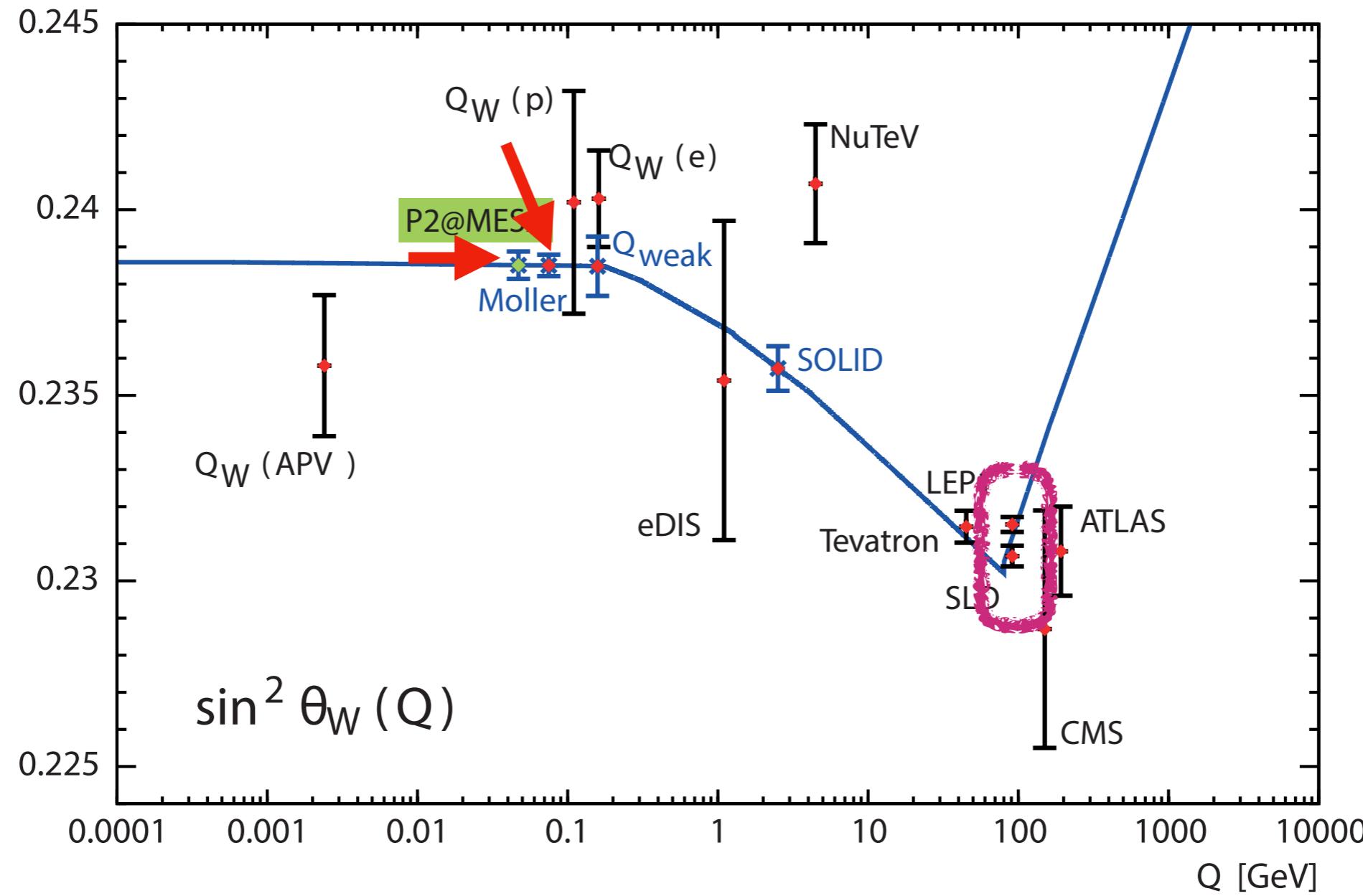


Berger et al, 1511.03934

Overview: PVES

Future prospects

Aleksejevs et al, 2011, 2012, 2015



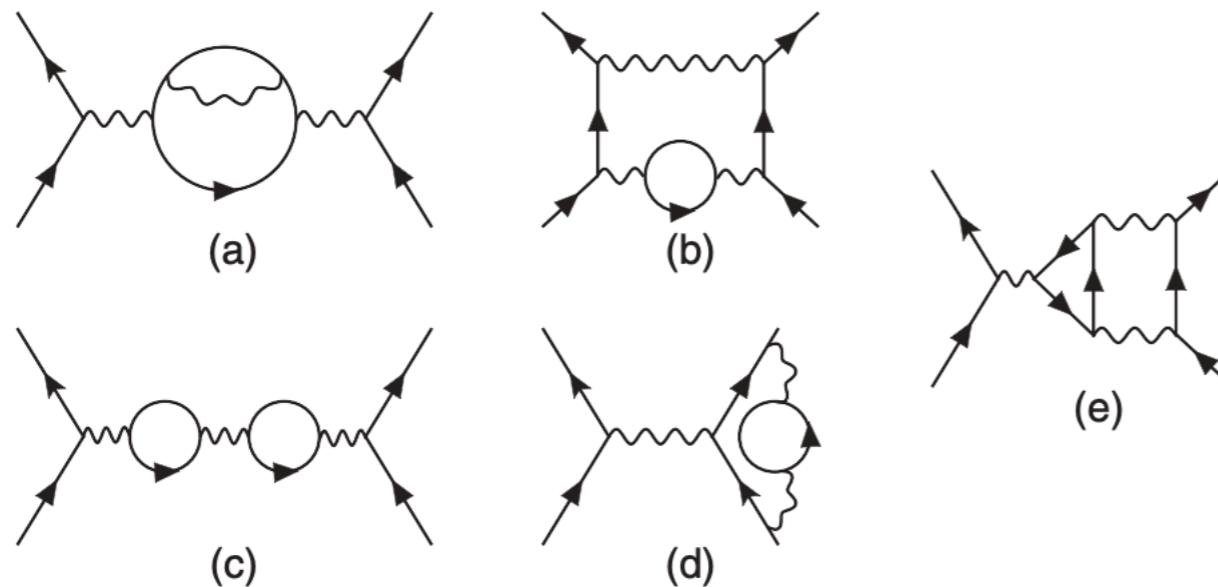
Berger et al, 1511.03934

Overview: PVES

LO: Derman and Marciano, 1979

NLO: Czarnecki and Marciano, 1996

NNLO: **YD**, Freitas, Patel, Ramsey-Musolf, PRL 2020



Quantity	Contribution ($\times 10^{-3}$)
$1-4 \sin^2\theta_W$	+74.4
$\Delta Q_{W(1,1)}^e$	-29.0
$\Delta Q_{W(1,0)}^e$	+3.1
$\Delta Q_{W(2,2)}^e$	$-0.18^{+0.0024}_{-0.0040}$
$\Delta Q_{W(2,1)}^e$	$+1.18^{+0.015}_{-0.010}$
$\Delta Q_{W(2,0)}^e$	± 0.13 (estimate)

$$\Delta Q_{W(i,j)}^e$$

i: Number of loops

j: Number of closed fermion

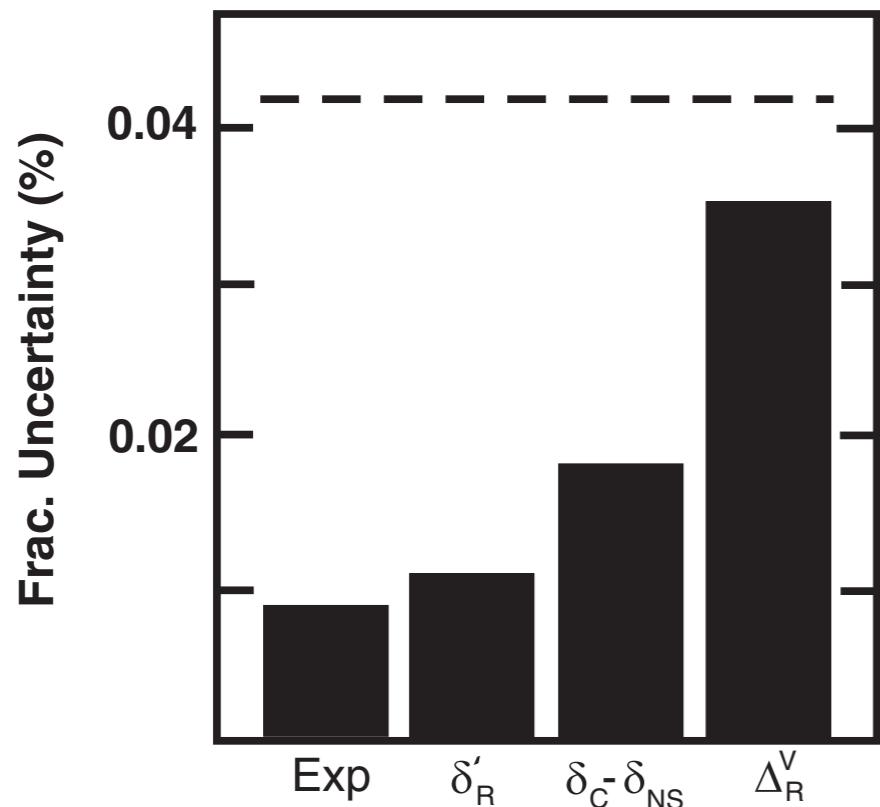
$$\Delta Q_{W(2,2)}^e + \Delta Q_{W(2,1)}^e = 1.00^{+0.012}_{-0.008} \times 10^{-3}$$

$$\Delta_{\text{exp}} Q_W^e = 1.1 \times 10^{-3}$$

Overview: *CKM unitarity*

Super-allowed β decay or free neutron decay

Towner & Hardy, 2015



Exp. : Experiment

$\delta_C - \delta_{NS}$: Nuclear structure dependent

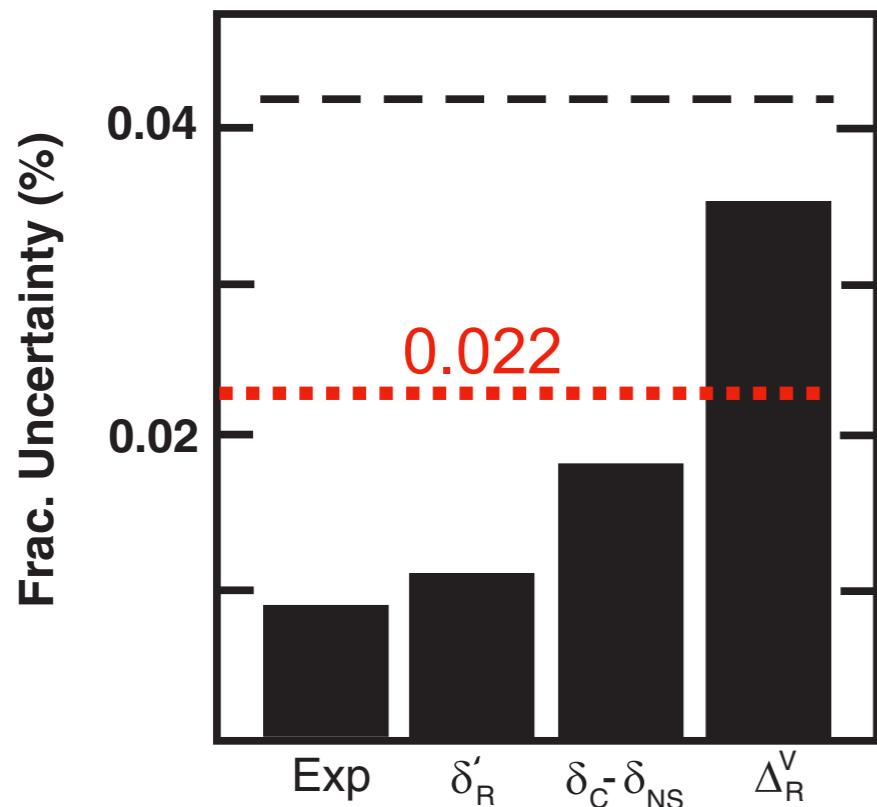
δ'_R : transition dependent radiative corrections

Δ_R^V : transition independent radiative corrections

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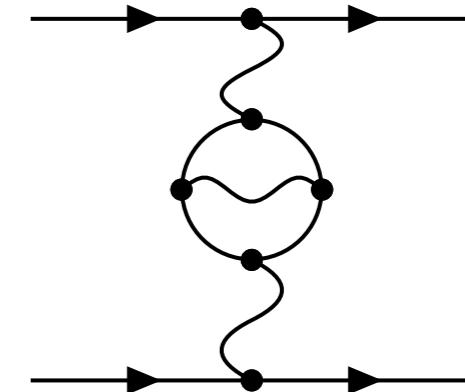
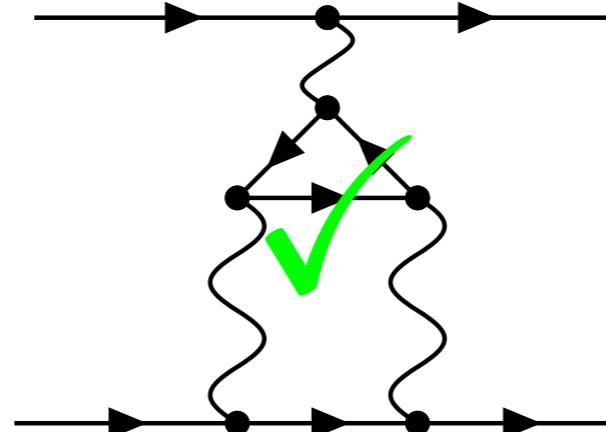
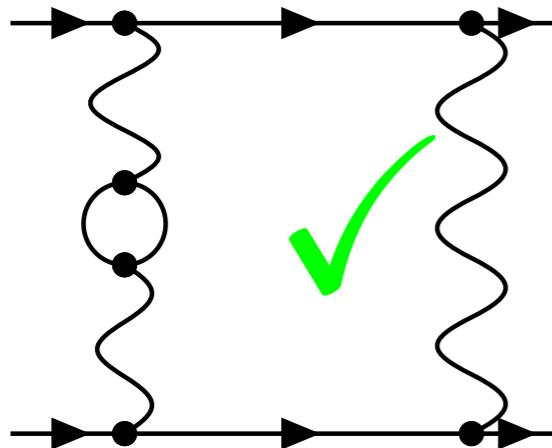
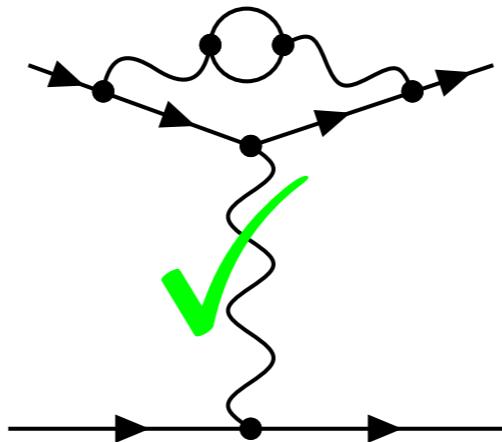
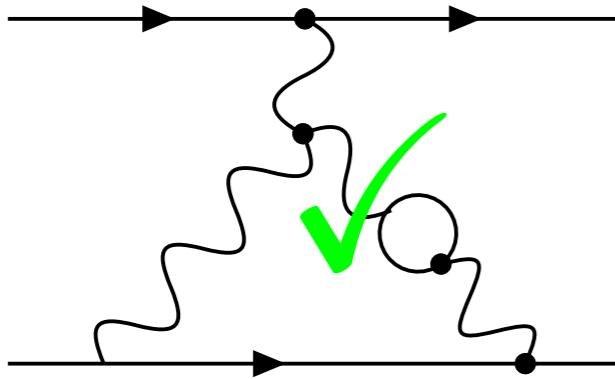
Seng, Gorchtein, Patel, Ramsey-Musolf, PRL 2018

Seng, Gorchtein, Ramsey-Musolf, PRD 2019

Overview: *CKM unitarity*

Current status:

* in progress, with Michael Ramsey-Musolf, Jia Zhou



Trivial and not necessary.

Remaining: Non-trivial $W\gamma$ boxes on the quark line.

Overview

What in common for PVES and neutron decay? *4-fermion operators!*

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PVES

$$\mathcal{O}_{le} = \frac{c_{\ell e}}{\Lambda^2} (\bar{\ell} \gamma_\mu \ell) (\bar{e} \gamma^\mu e)$$

Ignore flavor indices. Left-right symmetric model

$$\Lambda^{\text{Moller}} \gtrsim 10 \sim 50 \text{ TeV}$$

The MOLLER collaboration, 1411.4088

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Overview

What in common for PVES and neutron decay? *4-fermion operators!*

PVES

$$\mathcal{O}_{le} = \frac{c_{\ell e}}{\Lambda^2} (\bar{\ell} \gamma_\mu \ell) (\bar{e} \gamma^\mu e)$$

Ignore flavor indices. Left-right symmetric model

$$\Lambda^{\text{Moller}} \gtrsim 10 \sim 50 \text{ TeV}$$

Neutron decay

$$\mathcal{O}_{lq}^{(3)} = \frac{c_{\ell q}^{(3)}}{\Lambda^2} (\bar{\ell} \gamma_\mu \tau^I \ell) (\bar{q} \gamma^\mu \tau^I q)$$

Ignore flavor indices. Lepto-quark model

$$\Lambda^{\nu_\alpha \leftrightarrow \nu_\beta} \gtrsim \mathcal{O}(10) \text{ TeV}$$

The MOLLER collaboration, 1411.4088

Yong Du

YD, Li, Tang, Vihonen, Yu, 2011.14292

Overview

Including our recent three papers (neutrino oscillation + N_{eff} + CEvNS)

JHEP

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Non-standard interactions in SMEFT confronted with terrestrial neutrino experiments

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^aCAS Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences, Beijing 100190, P.R. China

^bAmherst Center for Fundamental Interactions, Physics Department, University of Massachusetts Amherst, Amherst, MA 01003 U.S.A.

^cSchool of Physics, Sun Yat-sen University, Guangzhou 510275, China

^dSchool of Physical Sciences, University of Chinese Academy, Beijing 100049, P.R. China

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PREPARED FOR SUBMISSION TO JHEP

27 Sep 2021 :2106.15800v2 [hep-ph]

Exploring SMEFT Induced Non-Standard Interactions from COHERENT to Neutrino Oscillations

Yong Du,^a Hao-Lin Li,^a Jian Tang,^c Sampsaa Vihonen,^c Jiang-Hao Yu^{a,d,e,f,g}

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^cSchool of Physics, Sun Yat-sen University, Guangzhou 510275, China

^dSchool of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, P.R. China

^eCenter for High Energy Physics, Peking University, Beijing 100871, China

^fSchool of Fundamental Physics and Mathematical Sciences, Hangzhou Institute for Advanced Study, UCAS, Hangzhou 310024, China

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ABSTRACT: We investigate the prospects of next-generation neutrino oscillation experiments DUNE, T2HK and JUNO including TAO within Standard Model Effective Field Theory (SMEFT). We also re-interpret COHERENT data in this framework. Considering both charged and neutral current neutrino Non-Standard Interactions (NSIs), we analyse dimension-6 SMEFT operators and derive lower bounds to UV scale Λ . The most powerful probe is obtained on $O_{ledq1211}$ with $\Lambda \gtrsim 450$ TeV due to the electron neutrino sample in T2HK. The lower bound is $\Lambda \gtrsim 100$ TeV for DUNE and JUNO due to the muon neutrino sample. T2HK is more

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Neutrino non-standard interactions meet precision measurements of N_{eff}

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^bSchool of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, P.R. China

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ITP CAS

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Questions:

Why 4-fermion operators?

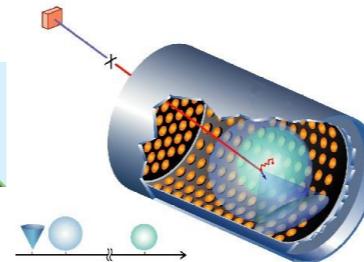
So the long answer is: Great potential in exploring new physics indirectly. More importantly, we have many experiments for them.

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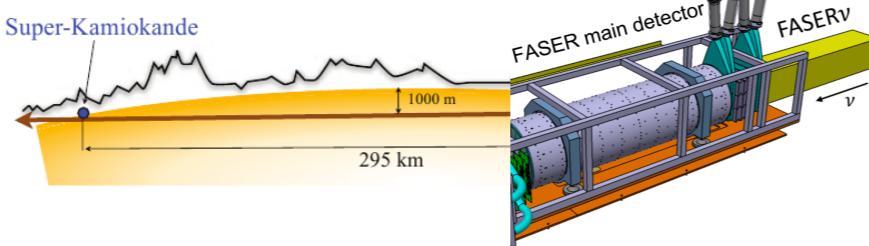
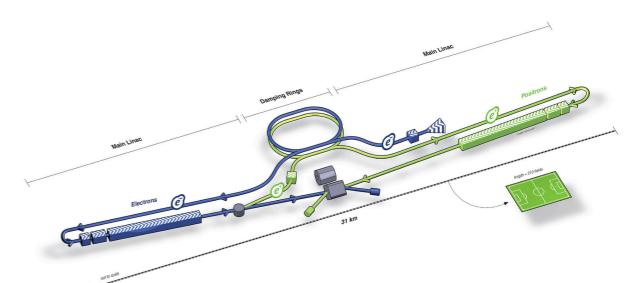
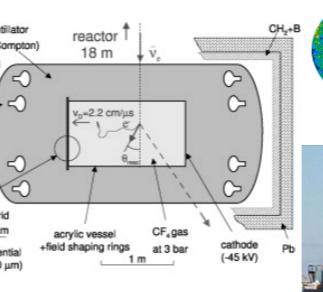
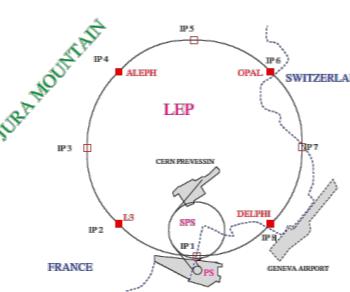
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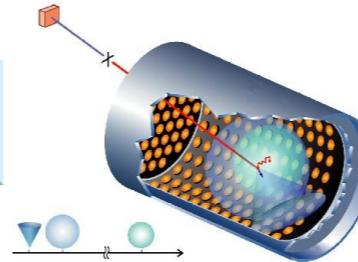
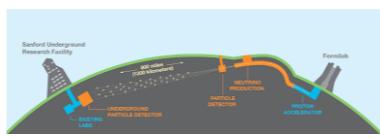
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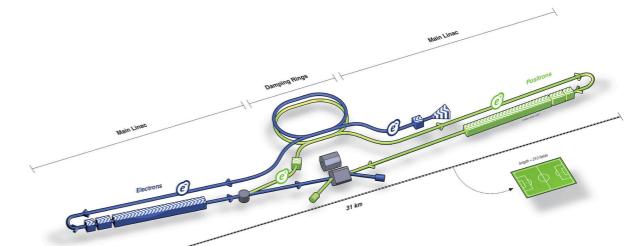
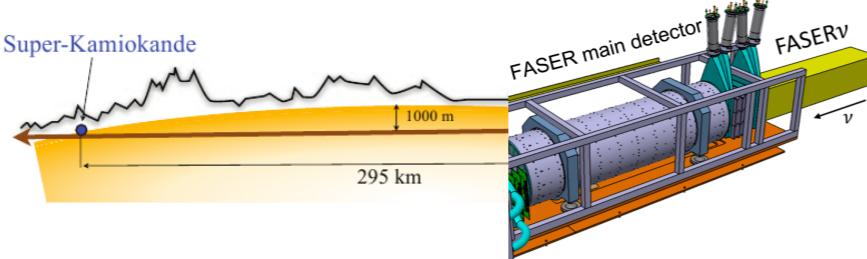
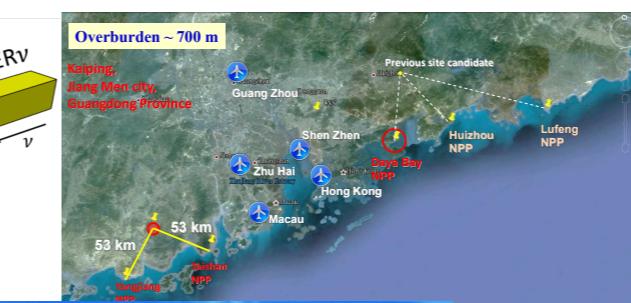
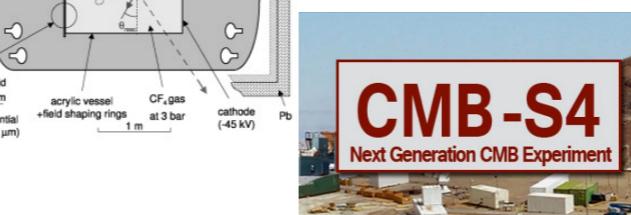
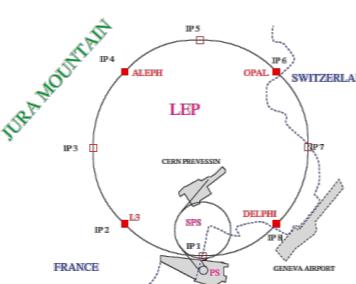
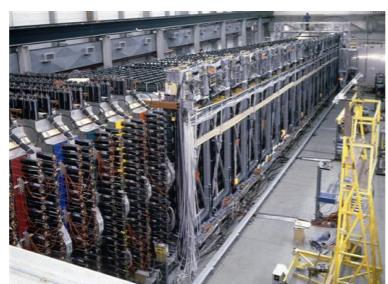
Why 4-fermion operators?

- 20:05 **Overview of the CEPC 25'**
Speaker: Haijun Yang (Shanghai Jiao Tong University)
- 20:30 **CEPC Higgs Physics Opportunities after the HL-LHC 30'**
Speaker: Sven Heinemeyer (IFT (CSIC))
- 21:00 **Status and Perspectives of the FCC 30'**
Speaker: Dr. Frank Zimmermann (CERN)

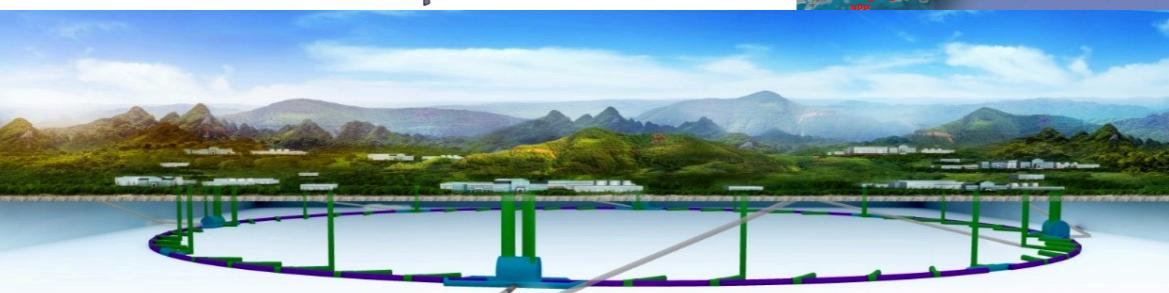
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IIP CAS

Framework

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$$\begin{aligned}\mathcal{L}_{\text{eff}}^{vff} = & eA_\mu \sum_{f \in u,d,e} Q_f (\bar{f}\bar{\sigma}_\mu f + f^c \sigma_\mu \bar{f}^c) + g_s G_\mu^a \sum_{f \in u,d} (\bar{f}\bar{\sigma}_\mu T^a f + f^c \sigma_\mu T^a \bar{f}^c) \\ & + \frac{g_L}{\sqrt{2}} \left(W_\mu^+ \bar{u} \bar{\sigma}_\mu (V + \delta g_L^{Wq}) d + W_\mu^+ \bar{u} \bar{\sigma}_\mu \delta g_R^{Wq} d_R + W_\mu^+ \bar{\nu} \bar{\sigma}_\mu (\mathbb{I} + \delta g_L^{W\ell}) e + \text{h.c.} \right) \\ & + \sqrt{g_L^2 + g_Y^2} Z_\mu \left[\sum_{f \in u,d,e,\nu} \bar{f} \bar{\sigma}_\mu \left(\mathbb{I} T_f^3 - \mathbb{I} s_\theta^2 Q_f + \delta g_L^{Zf} \right) f + \sum_{f^c \in u^c, d^c, e^c} f^c \sigma_\mu \left(-\mathbb{I} s_\theta^2 Q_f + \delta g_R^{Zf} \right) \bar{f}^c \right]\end{aligned}$$

$$m_W \rightarrow (1 + \delta m) m_W$$

Extra corrections to both Z/W-pole observables and fermion-pair production.

LHC Higgs Cross Section Working Group, 2017

Framework

One flavor ($I = 1 \dots 3$)	Two flavors ($I < J = 1 \dots 3$)
$[O_{\ell\ell}]_{IIII} = \frac{1}{2} (\bar{\ell}_I \bar{\sigma}_\mu \ell_I) (\bar{\ell}_I \bar{\sigma}_\mu \ell_I)$	$[O_{\ell\ell}]_{IIJJ} = (\bar{\ell}_I \bar{\sigma}_\mu \ell_I) (\bar{\ell}_J \bar{\sigma}_\mu \ell_J)$
$[O_{\ell e}]_{IIII} = (\bar{\ell}_I \bar{\sigma}_\mu \ell_I) (e_I^c \sigma_\mu \bar{e}_I^c)$	$[O_{\ell\ell}]_{IJJI} = (\bar{\ell}_I \bar{\sigma}_\mu \ell_J) (\bar{\ell}_J \bar{\sigma}_\mu \ell_I)$
$[O_{ee}]_{IIII} = \frac{1}{2} (e_I^c \sigma_\mu \bar{e}_I^c) (e_I^c \sigma_\mu \bar{e}_I^c)$	$[O_{\ell e}]_{IIJJ} = (\bar{\ell}_I \bar{\sigma}_\mu \ell_I) (e_J^c \sigma_\mu \bar{e}_J^c)$
	$[O_{\ell e}]_{JJII} = (\bar{\ell}_J \bar{\sigma}_\mu \ell_J) (e_I^c \sigma_\mu \bar{e}_I^c)$
	$[O_{\ell e}]_{IJJI} = (\bar{\ell}_I \bar{\sigma}_\mu \ell_J) (e_J^c \sigma_\mu \bar{e}_I^c)$
	$[O_{ee}]_{IIJJ} = (e_I^c \sigma_\mu \bar{e}_I^c) (e_J^c \sigma_\mu \bar{e}_J^c)$

Extra corrections to fermion-pair production

*Currently only flavor-conserving observables/operators are included in our fit.

LHC Higgs Cross Section Working Group, 2017

Input

$$G_F = 1.1663787 \times 10^{-5} \text{ GeV}^{-2}$$

$$m_Z = 91.1882 \text{ GeV}$$

$$\alpha(m_Z) = \frac{1}{127.952}$$

Observables: LEP-Z, W

Z-pole observables

$\Gamma_Z, \sigma_{\text{had}}, R_{e,\mu,\tau}, A_{\text{FB}}^{0,\{e,\mu,\tau\}}$

$R_b, R_c, A_b^{\text{FB}}, A_c^{\text{FB}}$

A_e, A_μ, A_τ

A_e, A_τ

A_b, A_c

A_s (SLD)

R_{uc} (PDG)

W-pole observables

m_W, Γ_W

$\text{Br}(W \rightarrow \ell\nu)$

$R_{W,c}$

R_σ

Observables: LEP-Z, W

Z-pole observables

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A_s (SLD)

R_{uc} (PDG)

$g_{V,A}^{u,d}$ (D0)

W-pole observables

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W-pole observables

m_W, Γ_W

$\text{Br}(W \rightarrow \ell\nu)$

$R_{W,c}$

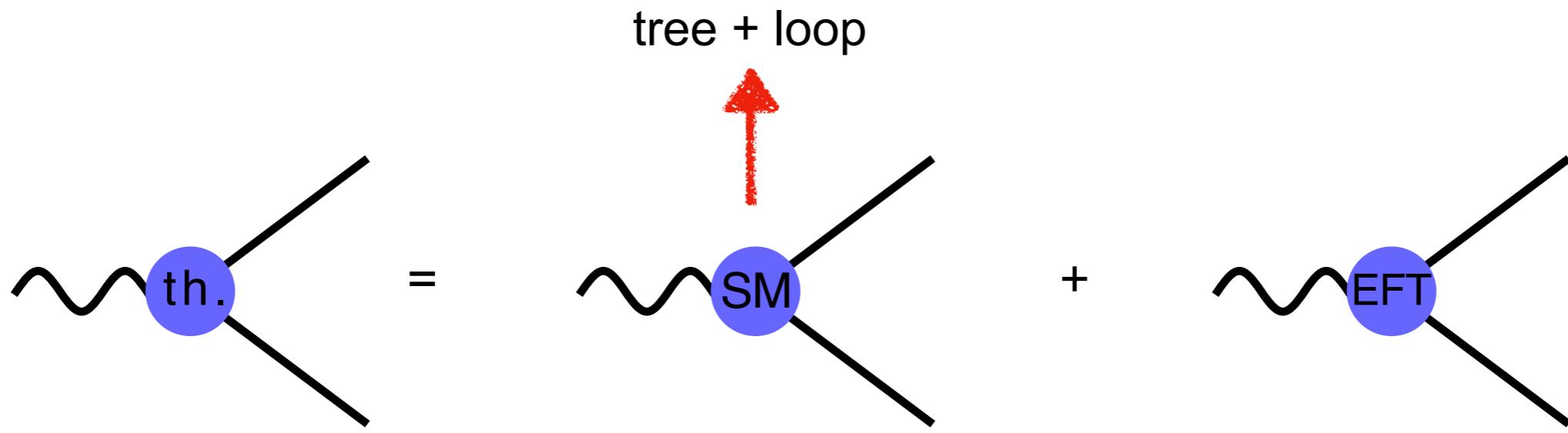
R_σ

- 15:15 **Electroweak precision pseudo-observables at the e+e- Z-resonance peak 25'**
Speaker: Dr. Johann Usovitsch (Mainz University)

- 11:00 **SMEFT at Z pole 30'**
Speaker: Jia Zhou (UMass Amherst)

- 11:30 **Z-mass measurement at CEPC 30'**
Speaker: LI Gang (EPC.IHEP)

Strategy: exemplified by pole observables



$$\begin{aligned}\mathcal{M}_{\text{th.}}^2 &= \mathcal{M}_{\text{SM}}^2 + 2\text{Re} \left(\mathcal{M}_{\text{SM}} \mathcal{M}_{\text{EFT}}^\dagger \right) + \mathcal{M}_{\text{EFT}}^2 \\ &\simeq \mathcal{M}_{\text{SM}}^2 + 2\text{Re} \left(\mathcal{M}_{\text{SM}}^{\text{tree}} \mathcal{M}_{\text{EFT}}^\dagger \right) + \mathcal{O}(\alpha^2 \delta g, \delta g^2)\end{aligned}$$

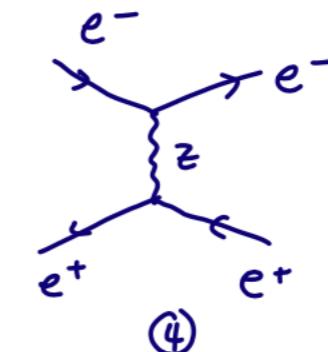
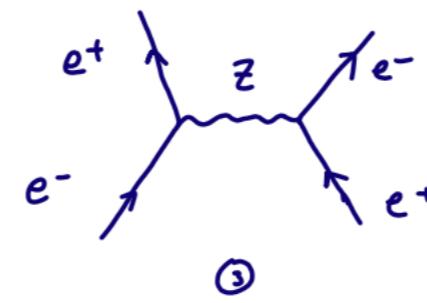
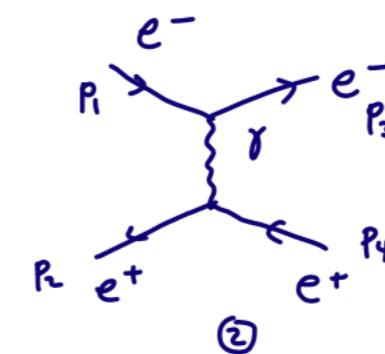
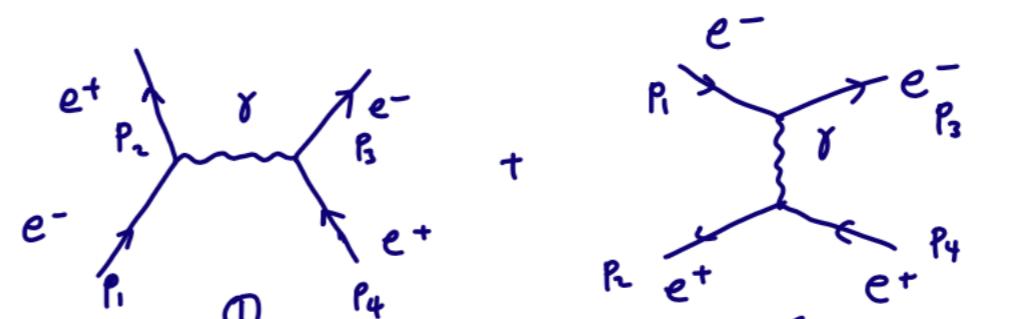
$$\chi^2 = \sum_{ij} [O_{i,\text{exp}} - O_{i,\text{th}}] \sigma_{ij}^{-2} [O_{j,\text{exp}} - O_{j,\text{th}}]$$

Observables: LEP-Z, W

Fermion-pair production: Bhabha scattering for example

(3) $e^-e^+ \rightarrow e^-e^+$

$$\frac{d\sigma}{d\cos\theta} \text{(Bhabha)}$$



$$+ \frac{1}{v^2} \left\{ [C_{ee}]_{\text{III}} [\mathcal{O}_{ee}]_{\text{III}} + [C_{ee}]_{\text{IIM}} [\mathcal{O}_{ee}]_{\text{IIM}} + [C_{ee}]_{\text{IMI}} [\mathcal{O}_{ee}]_{\text{IMI}} \right\}$$

Accidental flat direction for unpolarized beams at LEP lifted by PVES (SLAC-E158)

Observables: LEP-Z, W

Fermion-pair production

$$\sigma(e^+e^- \rightarrow \mu^+\mu^-), \quad \sigma_{\text{FB}}(e^+e^- \rightarrow \mu^+\mu^-)$$

— Flat direction lifted by $\overset{(-)}{\nu}_\mu e^-$ (CHARM-II)

$$\sigma(e^+e^- \rightarrow \tau^+\tau^-), \quad \sigma_{\text{FB}}(e^+e^- \rightarrow \tau^+\tau^-)$$

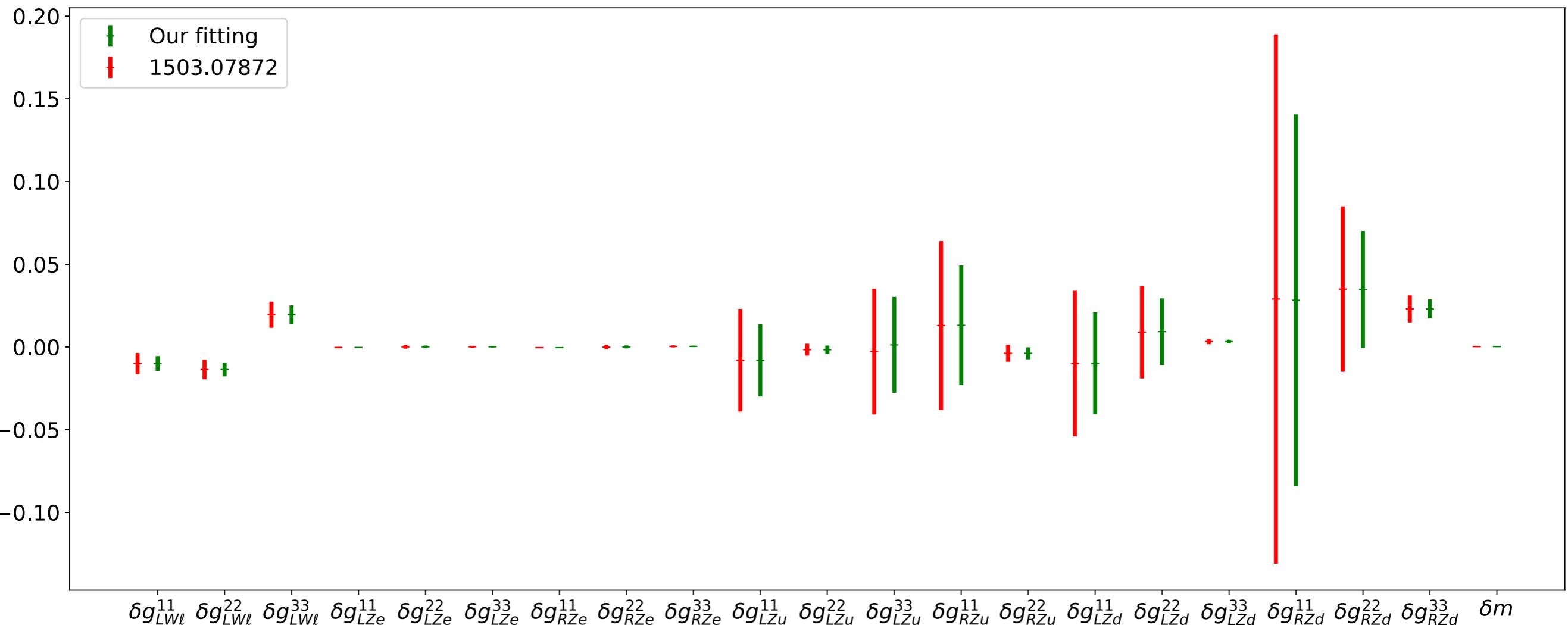
GF from τ decay (PDG)

Michel parameters from polarized muon decay (PSI)

— Michel parameters from polarized tau decay with upgraded SuperKEKB (Banerjee and Roney's [talk](#) at EF04 meeting last Friday)

Setup validation

Vertex part from pole observables



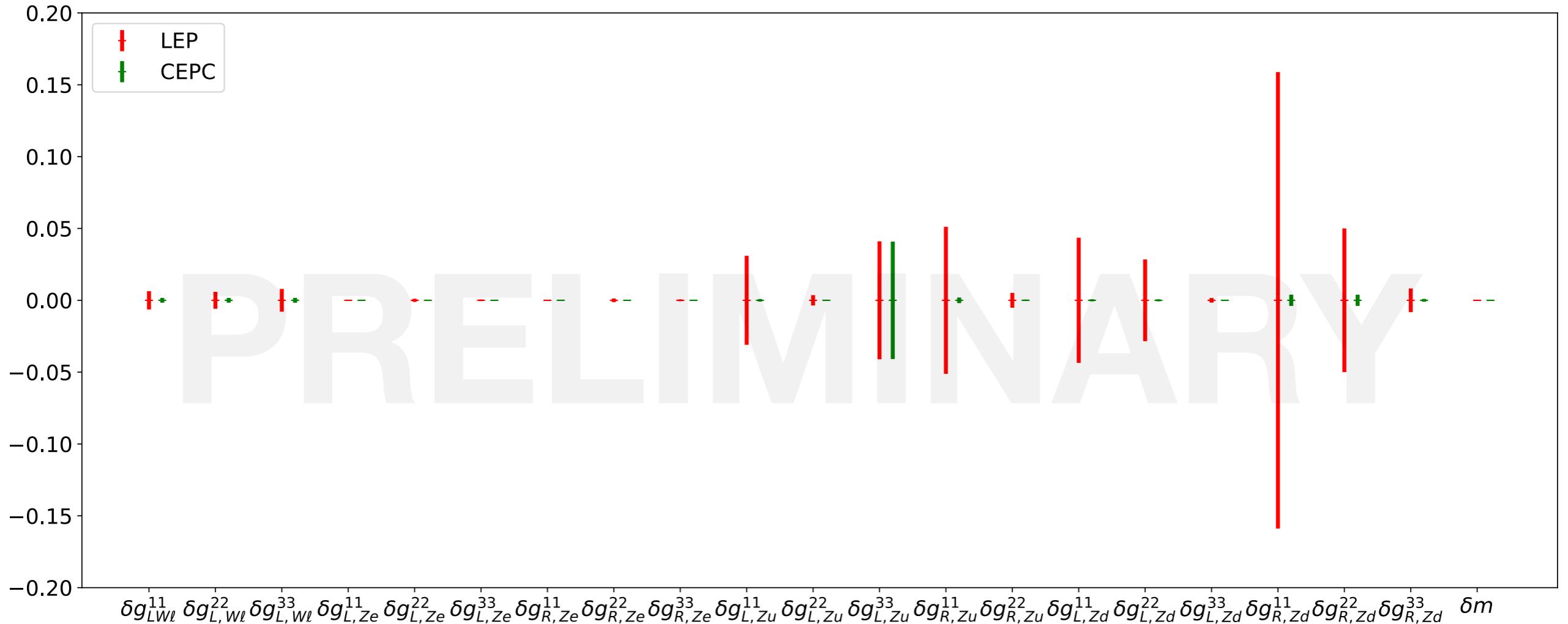
Observables: CEPC

CEPC CDR

de Blas, Durieux, Grojean, Gu, Paul, JHEP 2019

(10^{-3})	L/S	CEPC	(10^{-3})	L/S	CEPC
M_Z (GeV)	2.1	0.5	A_e^{**}	14.3	—
Γ_Z (GeV)	2.3	0.5	A_μ^{**}	102.0	—
σ_{had} (nb)	37.0	5.0	A_τ^{**}	102.0	—
R_e	2.41	0.6	R_b	3.06	0.2
R_μ	1.59	0.1	R_c	17.4	1.13
R_τ	2.17	0.2	$A_{\text{FB}}^{0,b}$	15.5	1.0
$A_{\text{FB}}^{0,e}$	154.0	5.0	$A_{\text{FB}}^{0,c}$	47.5	3.08
$A_{\text{FB}}^{0,\mu}$	80.1	3.0	A_b	21.4	—
$A_{\text{FB}}^{0,\tau}$	104.8	5.0	A_c	40.4	—
A_e^*	33.3	—	A_s	97.3	—
A_τ^*	29.2	—	source:	[60, 101]	[69]

Results: Vertex only



* No flavor assumption

Correlation matrix: Vertex only

δg_{Ld33}	δg_{LZe11}	δg_{LZe22}	δg_{LZe33}
1	-0.0359	-0.131	0.603
-0.0359	1	-0.39	-0.249
-0.131	-0.39	1	0.285
0.603	-0.249	0.285	1

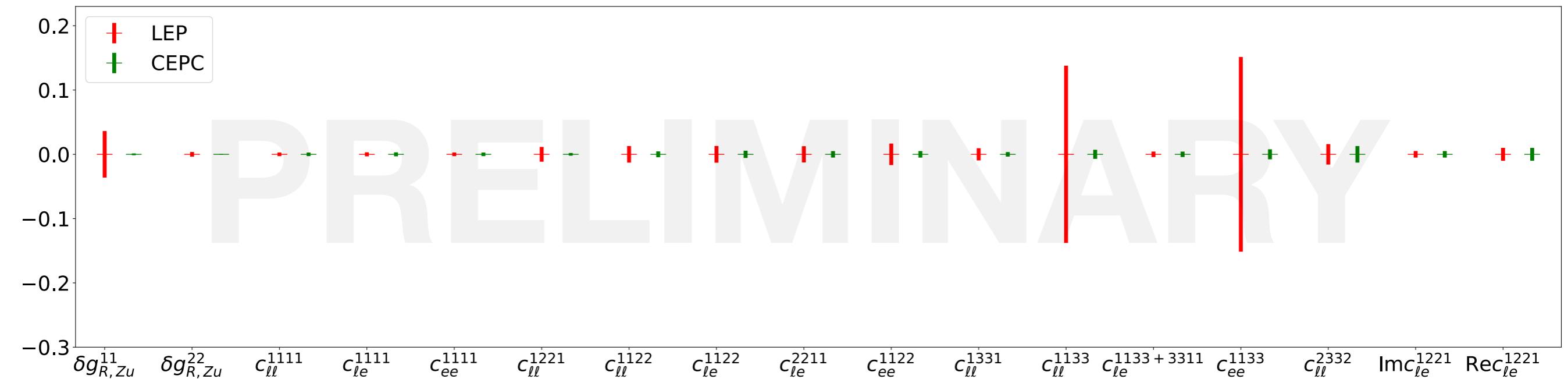
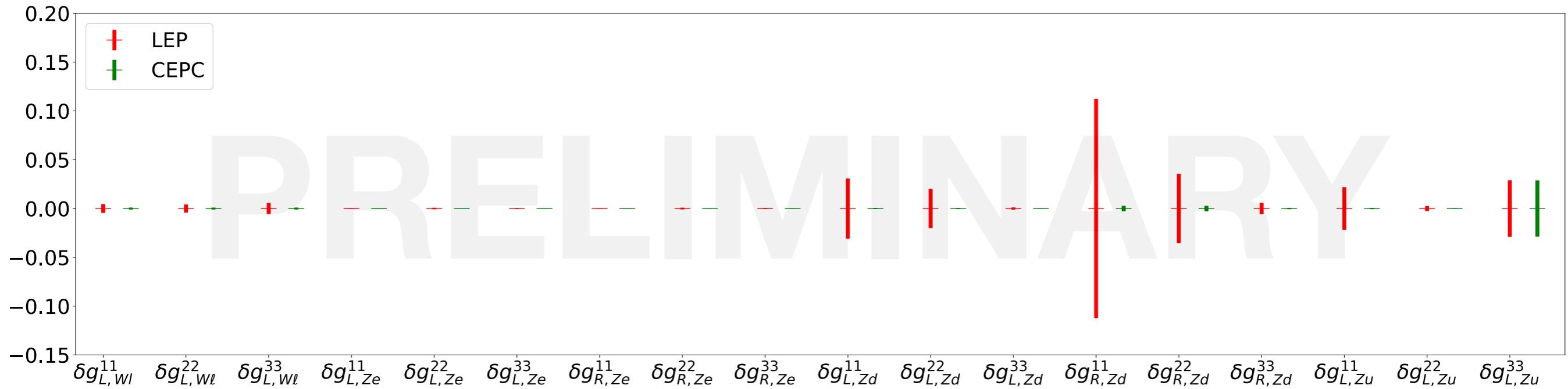
δg_{WL11}	δg_{WL22}	δg_{WL33}	δg_{Ld11}	δg_{Ld22}	δg_{Ld33}	δg_{LZe11}	δg_{LZe22}	δg_{LZe33}	δg_{LZu11}	δg_{LZu22}	δg_{LZu33}	δg_{Rd11}	δg_{Rd22}	δg_{Rd33}	δg_{RZe11}	δg_{RZe22}	δg_{RZe33}	δg_{RZu11}	δg_{RZu22}	δm
1	-0.447	-0.477	-0.11	0.0485	0.0225	0.106	-0.0579	-0.0487	-0.00657	-0.0139	0.000135	0.00328	0.0104	0.00874	0.00301	0.0288	-0.00262	-0.00375	-0.0083	0.0000107
-0.447	1	-0.471	-0.11	0.0476	0.0216	0.112	-0.0595	-0.0501	-0.00449	-0.0146	0.000108	0.00621	0.0118	-0.00088	0.00381	0.023	-0.00501	-0.00893	-0.0147	-0.0000476
-0.477	-0.471	1	-0.11	0.0494	0.024	0.108	-0.0579	-0.0477	-0.00253	-0.0164	0.000127	0.00552	0.00989	0.00518	0.00678	0.0271	-0.00582	-0.00173	-0.0105	-1×10^{-6}
-0.11	-0.11	-0.11	1	-0.331	-0.224	-0.32	-0.0842	-0.0548	0.011	0.223	-0.00231	-0.0149	0.226	-0.00803	-0.0156	-0.492	0.0107	0.0118	-0.435	0.0000218
0.0485	0.0476	0.0494	-0.331	1	0.34	-0.0626	0.281	-0.124	-0.0317	-0.234	0.00226	0.0321	-0.113	0.0287	0.0355	0.483	-0.0284	-0.0291	0.26	0.0000686
0.0225	0.0216	0.024	-0.224	0.34	1	-0.0359	-0.131	0.603	-0.0218	-0.157	0.00151	0.0217	-0.0733	0.019	0.0237	0.322	-0.0196	-0.0204	0.171	0.0000583
0.106	0.112	0.108	-0.32	-0.0626	-0.0359	1	-0.39	-0.249	-0.0117	0.171	-0.00195	0.0136	0.322	0.0143	0.00918	-0.415	-0.0131	-0.0145	-0.564	-0.000139
-0.0579	-0.0595	-0.0579	-0.0842	0.281	-0.131	-0.39	1	0.285	0.027	-0.0378	0.000637	-0.0268	-0.232	-0.0273	-0.021	0.136	0.0275	0.0285	0.376	0.0000512
-0.0487	-0.0501	-0.0477	-0.0548	-0.124	0.603	-0.249	0.285	1	0.0173	-0.0233	0.000399	-0.0177	-0.149	-0.0185	-0.0141	0.0851	0.0175	0.0179	0.242	0.0000459
-0.00657	-0.00449	-0.00253	0.011	-0.0317	-0.0218	-0.0117	0.027	0.0173	1	-0.0196	-0.0000729	0.195	0.00473	0.195	0.194	-0.0155	-0.19	-0.197	0.00282	-0.000315
-0.0139	-0.0146	-0.0164	0.223	-0.234	-0.157	0.171	-0.0378	-0.0233	-0.0196	1	-0.00155	0.0179	0.578	0.0217	0.0188	-0.331	-0.0178	-0.0183	-0.281	-0.000149
0.000135	0.000108	0.000127	-0.000231	0.000226	0.00151	-0.00195	0.000637	0.000399	-0.0000729	-0.00155	1	0.0000815	-0.0016	0.0000462	0.0001	0.00469	-0.0000588	-0.0000598	0.00418	2.7×10^{-6}
0.00328	0.00621	0.00552	-0.0149	0.0321	0.0217	0.0136	-0.0268	-0.0177	0.195	0.0179	0.0000815	1	-0.00589	-0.195	-0.189	0.0174	0.197	0.195	-0.00765	-0.000234
0.0104	0.0118	0.00989	0.226	-0.113	-0.0733	0.322	-0.232	-0.149	0.00473	0.578	-0.0016	-0.00589	1	-0.00196	-0.00657	-0.342	0.00487	0.00466	-0.409	-0.000135
0.00874	-0.00088	0.00518	-0.00803	0.0287	0.019	0.0143	-0.0273	-0.0185	0.195	0.0217	0.0000462	-0.195	-0.00196	1	-0.194	0.00988	0.196	0.191	-0.0077	0.000234
0.00301	0.00381	0.00678	-0.0156	0.0355	0.0237	0.00918	-0.021	-0.0141	0.194	0.0188	0.0001	-0.189	-0.00657	-0.194	1	0.0214	0.199	0.198	0.00445	0.000263
0.0288	0.023	0.0271	-0.492	0.483	0.322	-0.415	0.136	0.0851	-0.0155	-0.331	0.00469	0.0174	-0.342	0.00988	0.0214	1	-0.0126	-0.0128	0.892	0.000105
-0.00262	-0.00501	-0.00582	0.0107	-0.0284	-0.0196	-0.0131	0.0275	0.0175	-0.19	-0.0178	-0.0000588	0.197	0.00487	0.196	0.199	-0.0126	1	-0.193	0.00491	0.00029
-0.00375	-0.00893	-0.00173	0.0118	-0.0291	-0.0204	-0.0145	0.0285	0.0179	-0.197	-0.0183	-0.0000598	0.195	0.00466	0.191	0.198	-0.0128	-0.193	1	0.00525	0.000295
-0.0083	-0.0147	-0.0105	-0.435	0.26	0.171	-0.564	0.376	0.242	0.00282	-0.281	0.00418	-0.000765	-0.409	-0.0077	0.00445	0.892	0.00491	0.00525	1	0.000108
0.0000107	-0.0000476	-1×10^{-6}	0.0000218	0.0000686	0.0000583	-0.000139	0.0000512	0.0000459	-0.000315	-0.000149	2.7×10^{-6}	-0.000234	-0.000135	0.000234	0.000263	0.000105	0.00029	0.000295	0.000108	1

Correlation matrix: Vertex only

	$\delta gRZe22$	$\delta gRZe33$	$\delta gRZu11$	$\delta gRZu22$
	1	-0.0126	-0.0128	0.892
	-0.0126	1	-0.193	0.00491
	-0.0128	-0.193	1	0.00525
	0.892	0.00491	0.00525	1

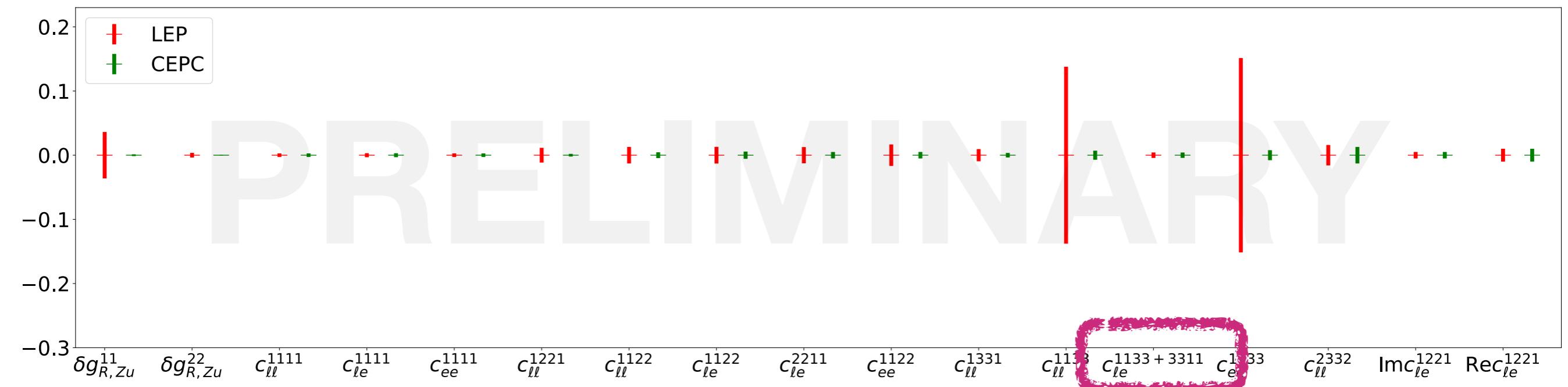
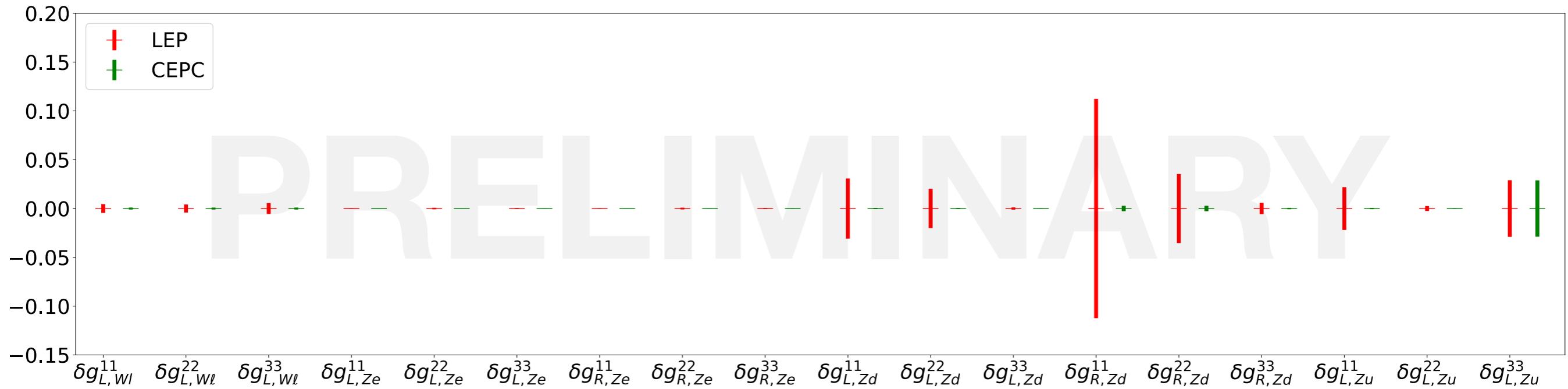
$\delta gLWl11$	$\delta gLWl22$	$\delta gLWl33$	$\delta gLZd11$	$\delta gLZd22$	$\delta gLZd33$	$\delta gLZell1$	$\delta gLZe22$	$\delta gLZe33$	$\delta gLZu11$	$\delta gLZu22$	$\delta gLZu33$	$\delta gRZd11$	$\delta gRZd22$	$\delta gRZd33$	$\delta gRZell1$	$\delta gRZe22$	$\delta gRZe33$	$\delta gRZu11$	$\delta gRZu22$	δm
1	-0.447	-0.477	-0.11	0.0485	0.0225	0.106	-0.0579	-0.0487	-0.00657	-0.0139	0.000135	0.00328	0.0104	0.00874	0.00301	0.0288	-0.00262	-0.0037	-0.0083	0.0000107
-0.447	1	-0.471	-0.11	0.0476	0.0216	0.112	-0.0595	-0.0501	-0.00449	-0.0146	0.000108	0.00621	0.0118	-0.00088	0.00381	0.023	-0.00501	-0.0085	-0.0147	-0.0000476
-0.477	-0.471	1	-0.11	0.0494	0.024	0.108	-0.0579	-0.0477	-0.00253	-0.0164	0.000127	0.00552	0.00989	0.00518	0.00678	0.0271	-0.00582	-0.011	-0.0105	-1. $\times 10^{-6}$
-0.11	-0.11	-0.11	1	-0.331	-0.224	-0.32	-0.0842	-0.0548	0.011	0.223	-0.00231	-0.0149	0.226	-0.00803	-0.0156	-0.492	0.0107	0.11	-0.435	0.0000218
0.0485	0.0476	0.0494	-0.331	1	0.34	-0.0626	0.281	-0.124	-0.0317	-0.234	0.00226	0.0321	-0.113	0.0287	0.0355	0.483	-0.0284	-0.21	0.26	0.0000686
0.0225	0.0216	0.024	-0.224	0.34	1	-0.0359	-0.131	0.603	-0.0218	-0.157	0.00151	0.0217	-0.0733	0.019	0.0237	0.322	-0.0196	-0.21	0.171	0.0000583
0.106	0.112	0.108	-0.32	-0.0626	-0.0359	1	-0.39	-0.249	-0.0117	0.171	-0.00195	0.0136	0.322	0.0143	0.00918	-0.415	-0.0131	-0.15	-0.564	-0.000139
-0.0579	-0.0595	-0.0579	-0.0842	0.281	-0.131	-0.39	1	0.285	0.027	-0.0378	0.000637	-0.0268	-0.232	-0.0273	-0.021	0.136	0.0275	0.05	0.376	0.0000512
-0.0487	-0.0501	-0.0477	-0.0548	-0.124	0.603	-0.249	0.285	1	0.0173	-0.0233	0.000399	-0.0177	-0.149	-0.0185	-0.0141	0.0851	0.0175	0.09	0.242	0.0000459
-0.00657	-0.00449	-0.00253	0.011	-0.0317	-0.0218	-0.0117	0.027	0.0173	1	-0.0196	-0.0000729	0.195	0.00473	0.195	0.194	-0.0155	-0.19	-0.17	0.00282	-0.000315
-0.0139	-0.0146	-0.0164	0.223	-0.234	-0.157	0.171	-0.0378	-0.0233	-0.0196	1	-0.00155	0.0179	0.578	0.0217	0.0188	-0.331	-0.0178	-0.033	-0.281	-0.000149
0.000135	0.000108	0.000127	-0.000231	0.000226	0.00151	-0.00195	0.000637	0.000399	-0.0000729	-0.00155	1	0.0000815	-0.0016	0.0000462	0.0001	0.00469	-0.0000588	-0.0000598	0.00418	2.7 $\times 10^{-6}$
0.00328	0.00621	0.00552	-0.0149	0.0321	0.0217	0.0136	-0.0268	-0.0177	0.195	0.0179	0.0000815	1	-0.00589	-0.195	-0.189	0.0174	0.197	0.195	-0.00765	-0.000234
0.0104	0.0118	0.00989	0.226	-0.113	-0.0733	0.322	-0.232	-0.149	0.00473	0.578	-0.0016	-0.00589	1	-0.00196	-0.00657	-0.342	0.00487	0.00466	-0.409	-0.000135
0.00874	-0.00088	0.00518	-0.00803	0.0287	0.019	0.0143	-0.0273	-0.0185	0.195	0.0217	0.0000462	-0.195	-0.00196	1	-0.194	0.00988	0.196	0.191	-0.0077	0.000234
0.00301	0.00381	0.00678	-0.0156	0.0355	0.0237	0.00918	-0.021	-0.0141	0.194	0.0188	0.0001	-0.189	-0.00657	-0.194	1	0.0214	0.199	0.198	0.00445	0.000263
0.0288	0.023	0.0271	-0.492	0.483	0.322	-0.415	0.136	0.0851	-0.0155	-0.331	0.00469	0.0174	-0.342	0.00988	0.0214	1	-0.0126	-0.0128	0.892	0.000105
-0.00262	-0.00501	-0.00582	0.0107	-0.0284	-0.0196	-0.0131	0.0275	0.0175	-0.19	-0.0178	-0.0000588	0.197	0.00487	0.196	0.199	-0.0126	1	-0.193	0.00491	0.00029
-0.00375	-0.00893	-0.00173	0.0118	-0.0291	-0.0204	-0.0145	0.0285	0.0179	-0.197	-0.0183	-0.0000598	0.195	0.00466	0.191	0.198	-0.0128	-0.193	1	0.00525	0.000295
-0.0083	-0.0147	-0.0105	-0.435	0.26	0.171	-0.564	0.376	0.242	0.00282	-0.281	0.00418	-0.000765	-0.409	-0.0077	0.00445	0.892	0.00491	0.00525	1	0.000108
0.0000107	-0.0000476	-1. $\times 10^{-6}$	0.0000218	0.0000686	0.0000583	-0.000139	0.0000512	0.0000459	-0.000315	-0.000149	2.7 $\times 10^{-6}$	-0.000234	-0.000135	0.000234	0.000263	0.000105	0.00029	0.000295	0.000108	1

Results: Vertex + 4f



* No flavor assumption

Results: Vertex + 4f



* No flavor assumption

Beam polarization @ILC, CLIC

Summary and outlook

- ❖ 4-fermion operators are very interesting in exploring new physics indirectly (PVES, CKM unitarity, neutrino NSIs, N_{eff} , etc)
- ❖ We validate our setup against results in literature for LEP and find excellent agreement.
- ❖ Preliminary results obtained using projections for CEPC, much smaller uncertainties would be expected as compared to those from LEP.
- ❖ More comprehensive results (with more operators) to be expected at the beginning of the coming year.

Backup

	δg_{LWI11}	δg_{LWI22}	δg_{LWI33}	δg_{LZe11}	δg_{LZe22}	δg_{LZe33}	δg_{RZe11}	δg_{RZe22}	δg_{RZe33}	δg_{LZd11}	δg_{LZd22}	δg_{LZd33}	δg_{RZd11}	δg_{RZd22}
δg_{LWI11}	1	-0.485	-0.463	-0.0792	0.0357	0.0167	0.0779	-0.0416	-0.035	0.00291	0.00284	0.0189	-0.00396	-0.00398
δg_{LWI22}	-0.485	1	-0.412	-0.103	0.0441	0.0205	0.103	-0.0553	-0.0459	0.00337	0.00361	0.0233	-0.00514	-0.00517
δg_{LWI33}	-0.463	-0.412	1	-0.195	0.085	0.0398	0.193	-0.104	-0.0865	0.00866	0.00848	0.0451	-0.00735	-0.00742
δg_{LZe11}	-0.0792	-0.103	-0.195	1	-0.327	-0.222	-0.306	-0.0949	-0.0635	-0.0103	-0.0102	-0.491	0.0123	0.0126
δg_{LZe22}	0.0357	0.0441	0.085	-0.327	1	0.339	-0.0724	0.287	-0.121	0.0297	0.0297	0.481	-0.0311	-0.0314
δg_{LZe33}	0.0167	0.0205	0.0398	-0.222	0.339	1	-0.0405	-0.129	0.606	0.0204	0.0203	0.321	-0.0211	-0.0214
δg_{RZe11}	0.0779	0.103	0.193	-0.306	-0.0724	-0.0405	1	-0.387	-0.246	0.0114	0.0114	-0.427	-0.0129	-0.0129
δg_{RZe22}	-0.0416	-0.0553	-0.104	-0.0949	0.287	-0.129	-0.387	1	0.282	-0.0254	-0.0254	0.141	0.0265	0.0265
δg_{RZe33}	-0.035	-0.0459	-0.0865	-0.0635	-0.121	0.606	-0.246	0.282	1	-0.0164	-0.0164	0.0887	0.0173	0.0172
δg_{LZd11}	0.00291	0.00337	0.00866	-0.0103	0.0297	0.0204	0.0114	-0.0254	-0.0164	1	-0.197	0.014	0.193	0.194
δg_{LZd22}	0.00284	0.00361	0.00848	-0.0102	0.0297	0.0203	0.0114	-0.0254	-0.0164	-0.197	1	0.0139	0.194	0.194
δg_{LZd33}	0.0189	0.0233	0.0451	-0.491	0.481	0.321	-0.427	0.141	0.0887	0.014	0.0139	1	-0.015	-0.0153
δg_{RZd11}	-0.00396	-0.00514	-0.00735	0.0123	-0.0311	-0.0211	-0.0129	0.0265	0.0173	0.193	0.194	-0.015	1	-0.196
δg_{RZd22}	-0.00398	-0.00517	-0.00742	0.0126	-0.0314	-0.0214	-0.0129	0.0265	0.0172	0.194	0.194	-0.0153	-0.196	1
δg_{RZd33}	-0.00804	-0.0115	-0.0209	-0.439	0.261	0.17	-0.571	0.378	0.242	-0.003	-0.0031	0.893	0.00281	0.00257

cLe1111	cee1111	cLL1221	cLL1122	cLe1122	cLe2211	cee1122	cLL1331	cLL1133	cLe1133	PcLe3311	cee1133	cLL2332	lmcLe1221	RecLe1221
1	-0.532	-0.00347	0.00085	0.000385	-0.000504	0.00075	-0.00269	0.000685	-9.69e-05	0.000671	-0.000944	1.91e-06	3.93e-06	
-0.532	1	-0.000114	4.94e-05	7.68e-05	-9.1e-05	1.08e-05	-9.44e-05	2.76e-05	-3.06e-06	2.52e-05	-2.33e-05	-3.67e-06	-4.01e-06	
-0.00347	-0.000114	1	-0.202	-0.00308	0.0132	-0.244	-0.142	0.0349	-0.00272	0.0347	-0.0511	1.06e-05	6.7e-07	
0.00085	4.94e-05	-0.202	1	-0.667	0.799	-0.874	0.0576	-0.0143	0.00111	-0.014	0.000827	-5.31e-06	-2.12e-06	
0.000385	7.68e-05	-0.00308	-0.667	1	-0.846	0.731	0.0983	-0.0242	0.00202	-0.0242	-0.0315	3.1e-07	4.31e-06	
-0.000504	-9.1e-05	0.0132	0.799	-0.846	1	-0.772	-0.113	0.0277	-0.00232	0.0277	0.0353	-4.98e-06	-9.61e-06	
0.00075	1.08e-05	-0.244	-0.874	0.731	-0.772	1	0.00573	-0.00126	8.23e-05	-0.0015	0.0218	-1.31e-06	-8.55e-08	
-0.00269	-9.44e-05	-0.142	0.0576	0.0983	-0.113	0.00573	1	-0.247	0.0206	-0.245	-0.0193	7.01e-06	5.19e-06	
0.000685	2.76e-05	0.0349	-0.0143	-0.0242	0.0277	-0.00126	-0.247	1	0.0716	-0.857	0.00472	-2.22e-06	-2.14e-06	
-9.69e-05	-3.06e-06	-0.00272	0.00111	0.00202	-0.00232	8.23e-05	0.0206	0.0716	1	0.08	-0.000358	-3.46e-06	-8.19e-06	
0.000671	2.52e-05	0.0347	-0.014	-0.0242	0.0277	-0.0015	-0.245	-0.857	0.08	1	0.00471	-2.24e-06	-2.19e-06	
-0.000944	-2.33e-05	-0.0511	0.000827	-0.0315	0.0353	0.0218	-0.0193	0.00472	-0.000358	0.00471	1	-1.81e-06	-6.79e-06	
1.91e-06	-3.67e-06	1.06e-05	-5.31e-06	3.1e-07	-4.98e-06	-1.31e-06	7.01e-06	-2.22e-06	-3.46e-06	-2.24e-06	-1.81e-06	1	-2.98e-06	
3.93e-06	-4.01e-06	6.7e-07	-2.12e-06	4.31e-06	-9.61e-06	-8.55e-08	5.19e-06	-2.14e-06	-8.19e-06	-2.19e-06	-6.79e-06	-2.98e-06	1	