

Beam-beam simulations and measurements at SuperKEKB

Demin Zhou

Accelerator theory group, Accelerator laboratory, KEK

Acknowledgements

K. Ohmi, Y. Zhang, and SuperKEKB team

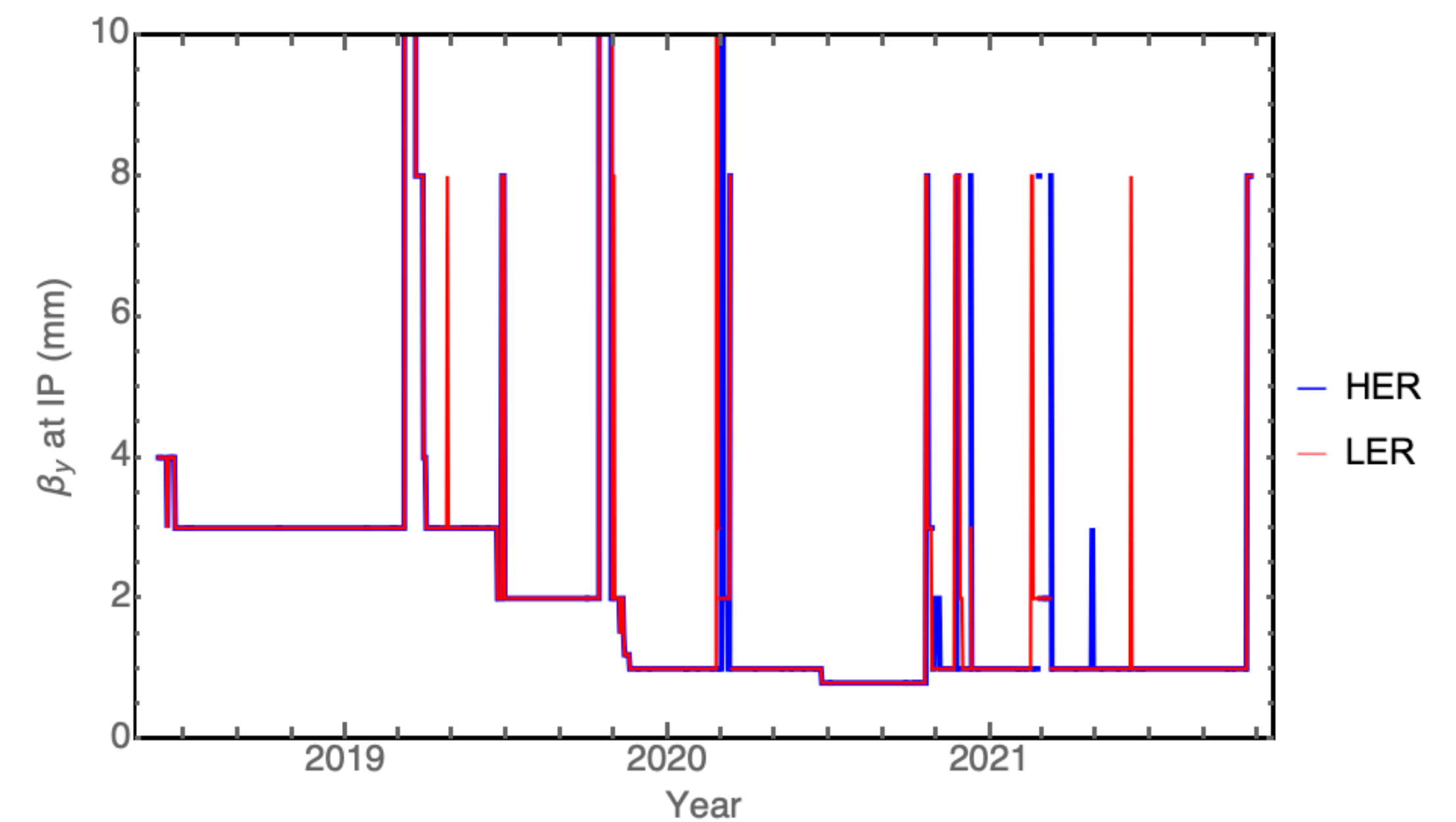
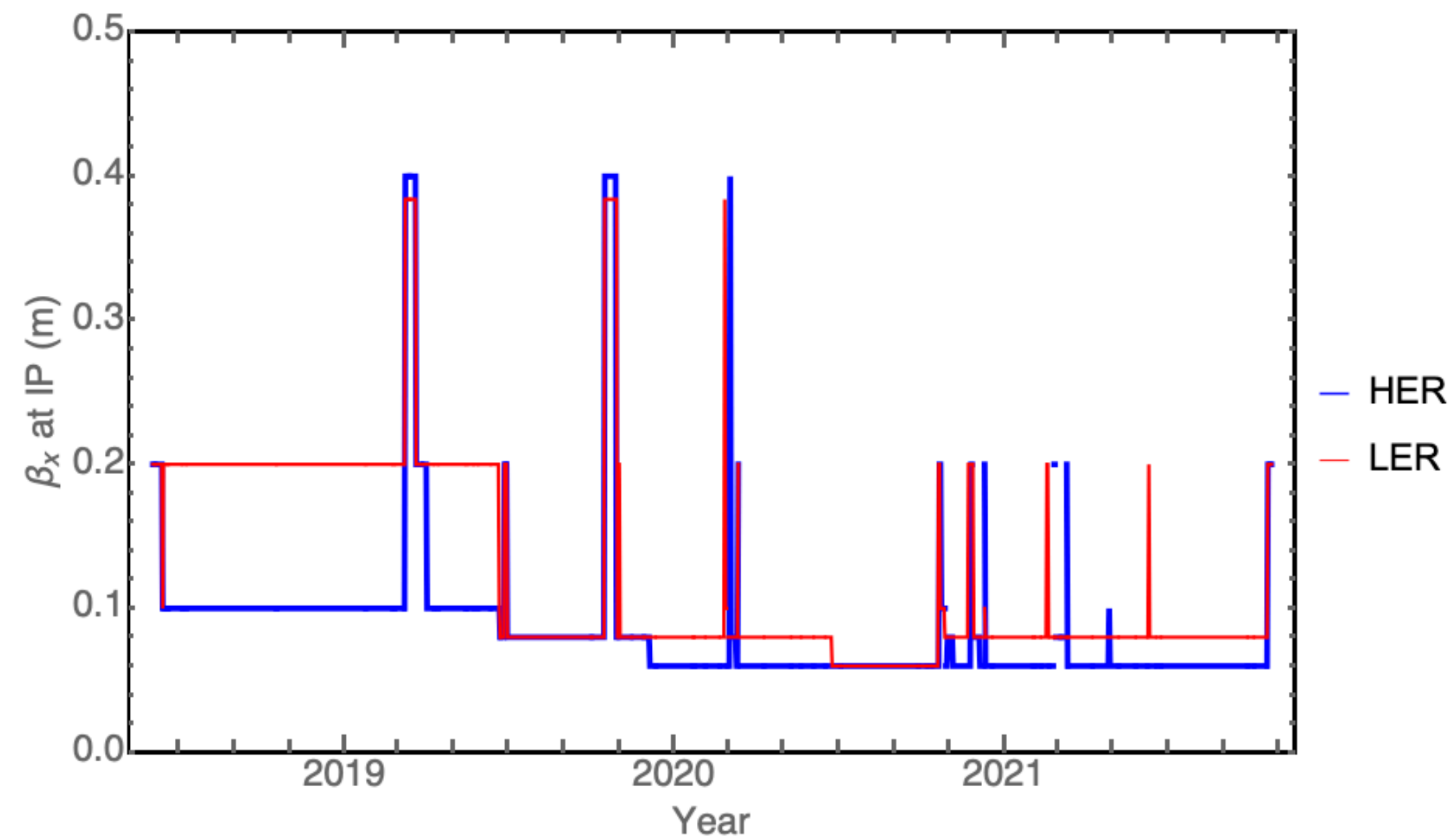
Outline

- Introduction
- Beam-beam simulations for SuperKEKB
- Summary and outlook

Introduction

- Phase-2 and Phase-3

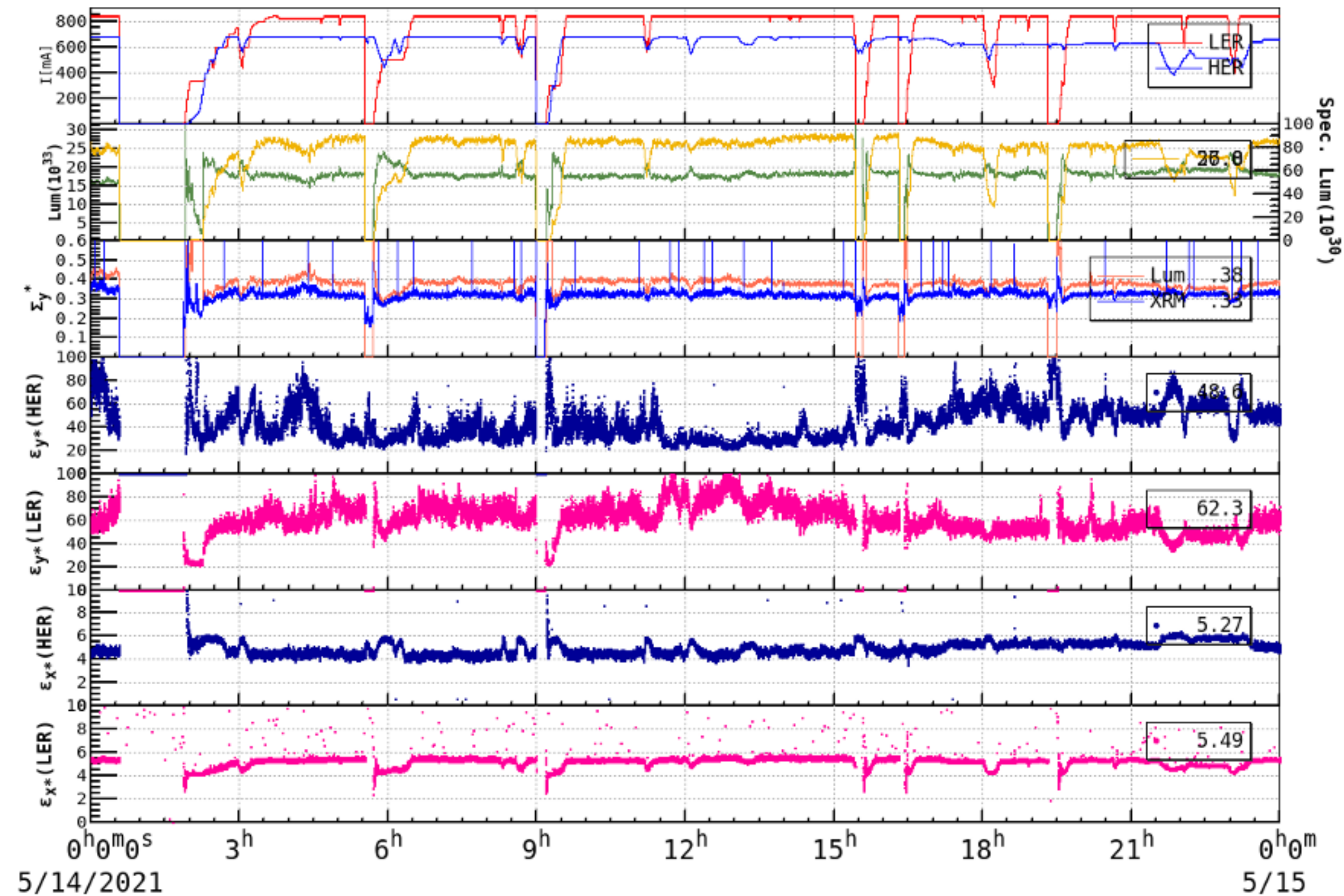
- Phase-2 started in March 2018 with Belle2 detector.
- Phase-3 started in March 2019 with VXD detector.
- Crab waist (FCC-ee scheme) was introduced to SuperKEKB since March 2020.
- Since Phase-2, $\beta_{x,y}^*$ were gradually squeezed as machine tuning improved.



History of $\beta_{x,y}^*$ at SuperKEKB since Mar 2018

Beam-beam simulations for SuperKEKB

- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - Crab waist suppresses beam-beam resonances but vertical blowup still exists.



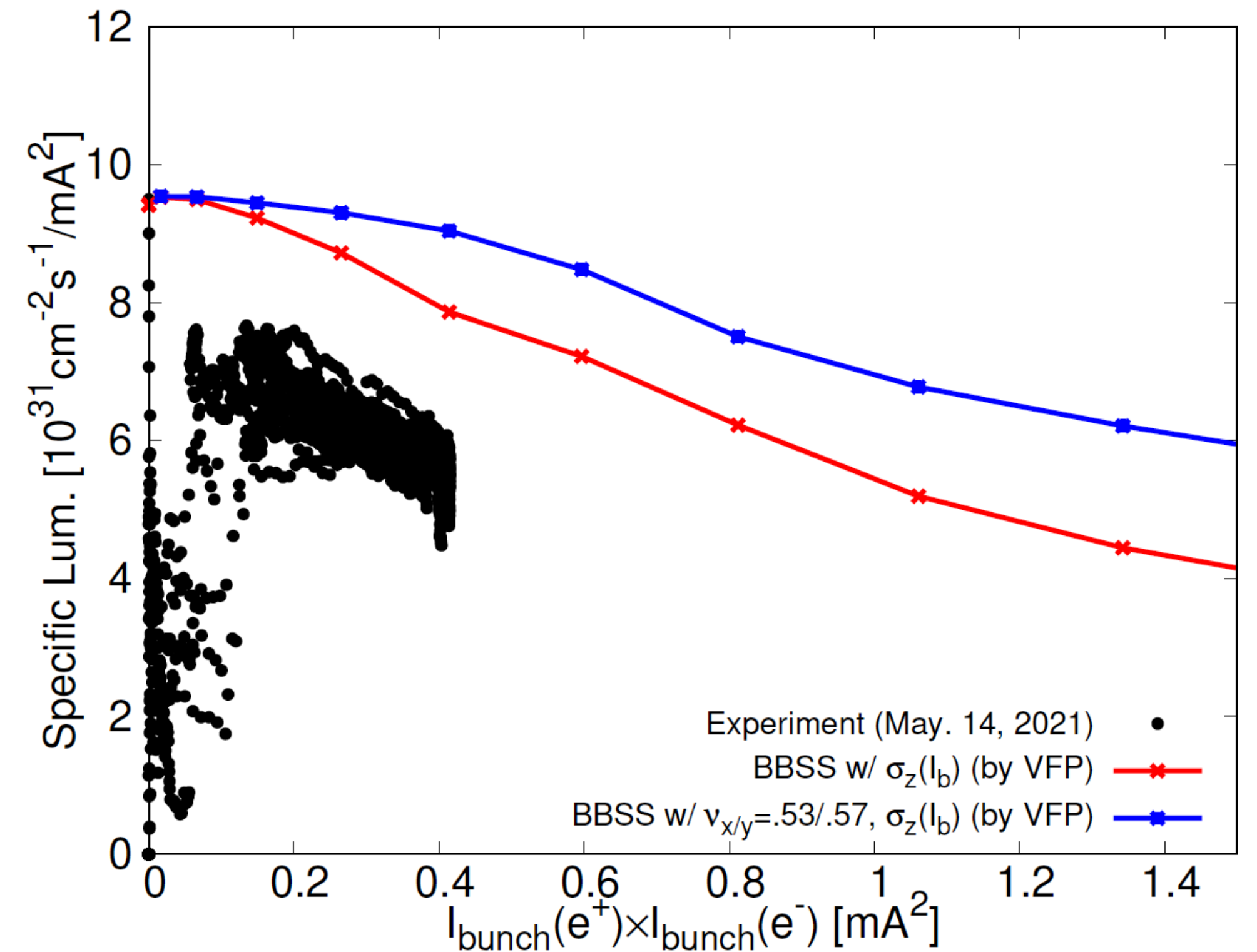
One-day history of luminosity and beam parameters of SuperKEKB

Beam-beam simulations for SuperKEKB (cont'd)

- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - Taking into account bunch lengthening by impedance and non-optimal working point, BBSS predicted a luminosity about 20% higher than the measured value at bunch current product $\sim 0.4 \text{ mA}^2$.
 - At bunch current products higher than 0.4 mA^2 , the discrepancy between BBSS simulation and measurement becomes worse.

	2021.05.14		Comments
	HER	LER	
I_b (A)	0.68	0.84	
# bunch	1174		
ϵ_x (nm)	4.6	4.24	w/ IBS
ϵ_y (pm)	22.5	22.5	Estimated from XRM data
β_x (mm)	60	80	Calculated from lattice
β_y (mm)	1	1	Calculated from lattice
σ_z (mm)	6	6	w/ bunch lengthening by impedance
σ_y (μm)	0.15	0.15	Observed from XRM
ν_x	45.52989	44.5247	Measured tune of pilot bunch
ν_y	43.59055	46.57279	Measured tune of pilot bunch
ν_s	0.02719	0.02212	Calculated from lattice
Crab waist	40%	80%	Lattice design

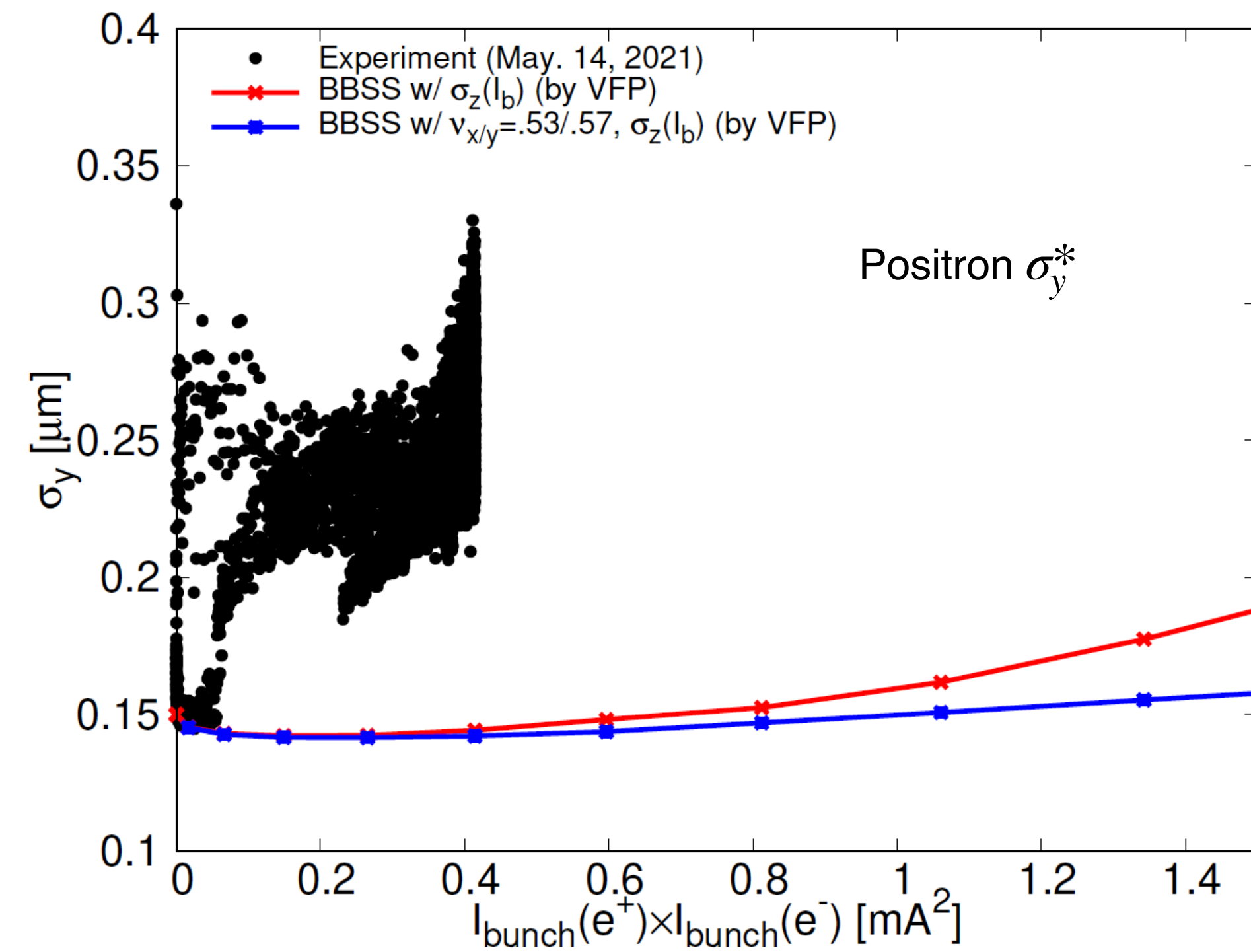
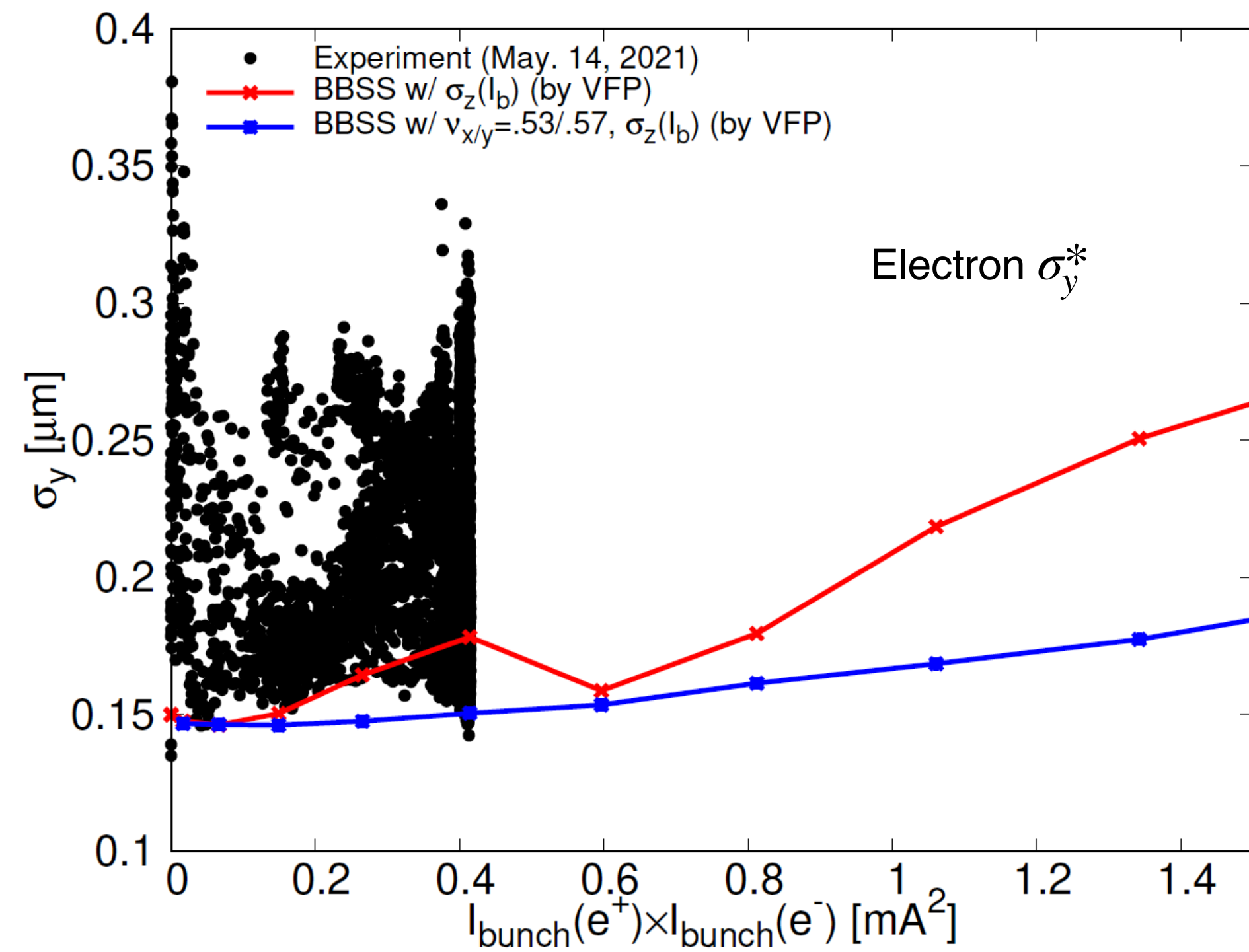
Beam parameters of SuperKEKB on May 14, 2021



Specific luminosity: BBSS simulation compared to observations

Beam-beam simulations for SuperKEKB (cont'd)

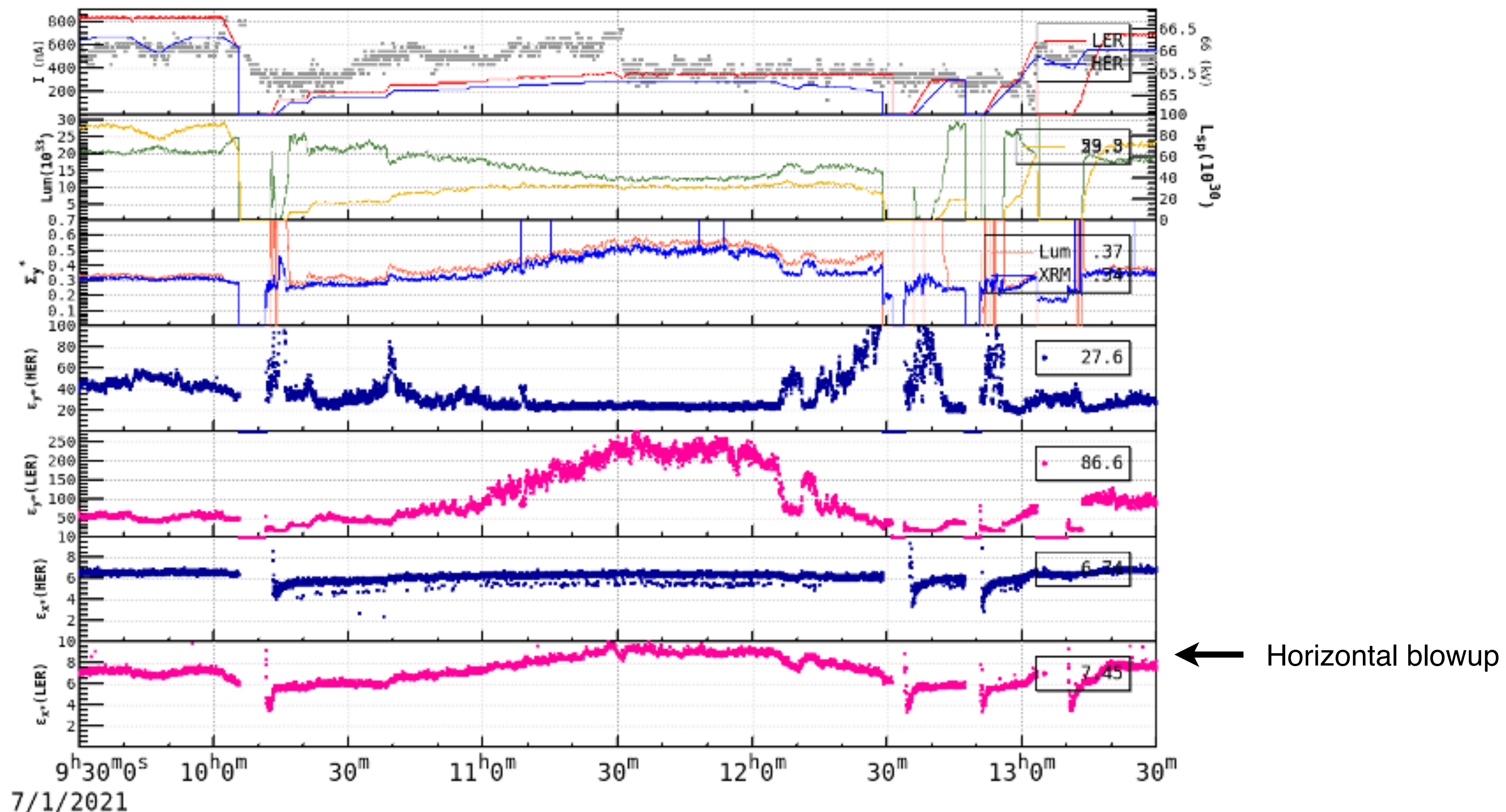
- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - The observed blowup of σ_y^* of both electron and positron beams were complicated. BBSS simulations did not well predict the trends of σ_y^* blowup.



Vertical beam sizes: BBSS simulation compared to observations on May 14, 2021

Beam-beam simulations for SuperKEKB (cont'd)

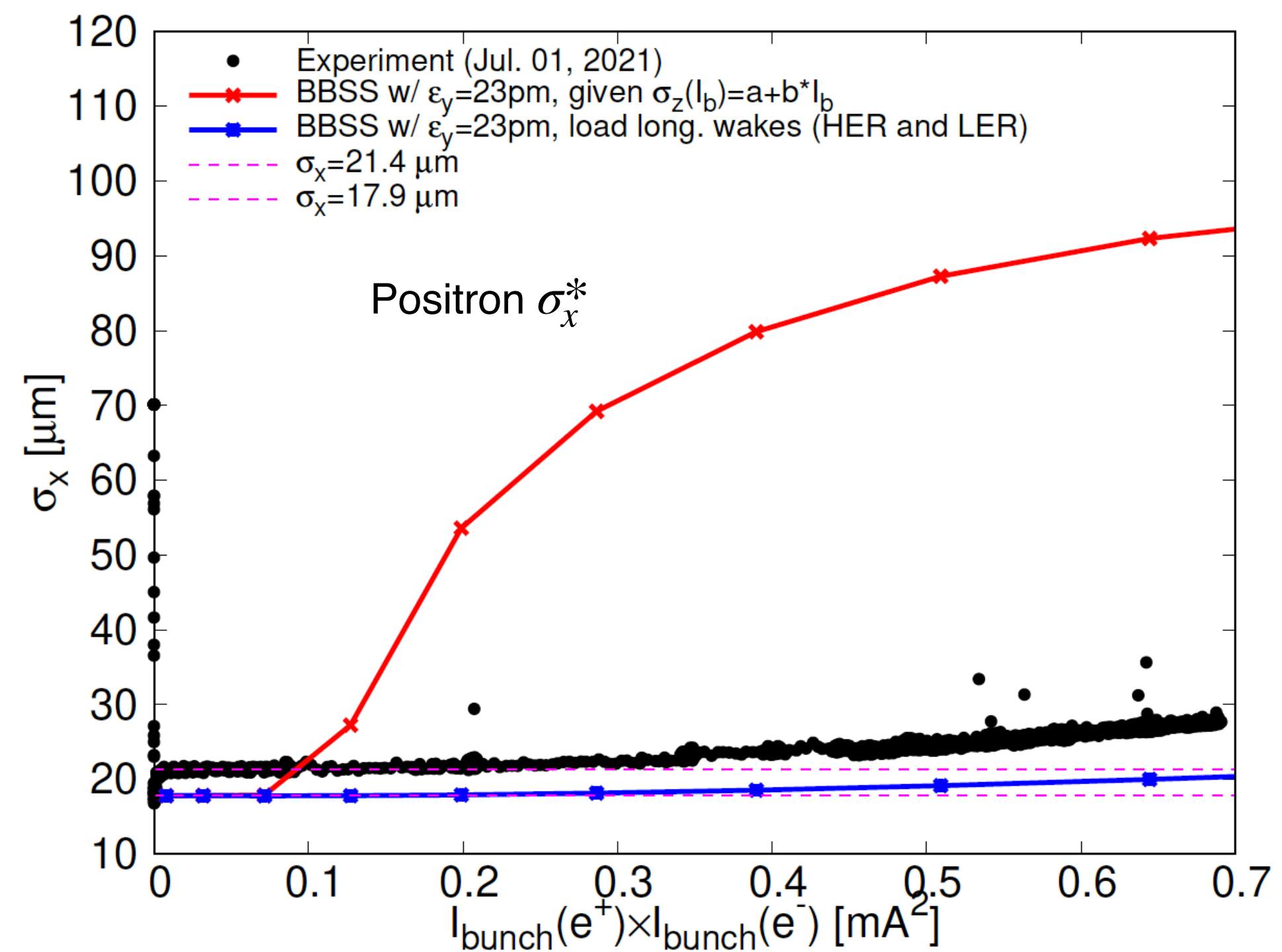
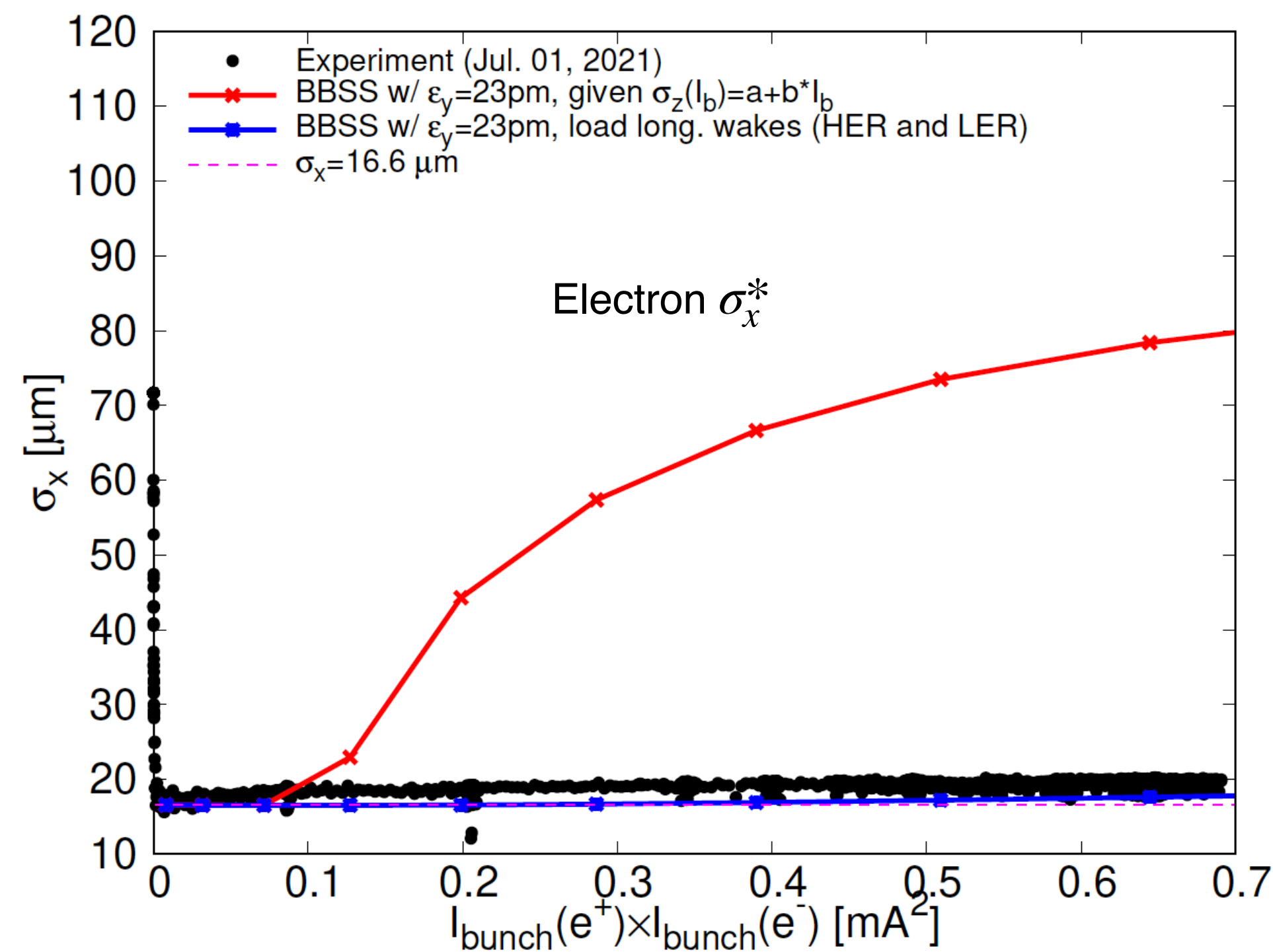
- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - Beam-beam can also drive horizontal blowup in SuperKEKB.
 - BBSS simulations with inclusion of longitudinal wakes in a self-consistent way were done to compare the observations of high-bunch current machine study.



History of luminosity and beam parameters during high-bunch current machine study on Jul. 1, 2021

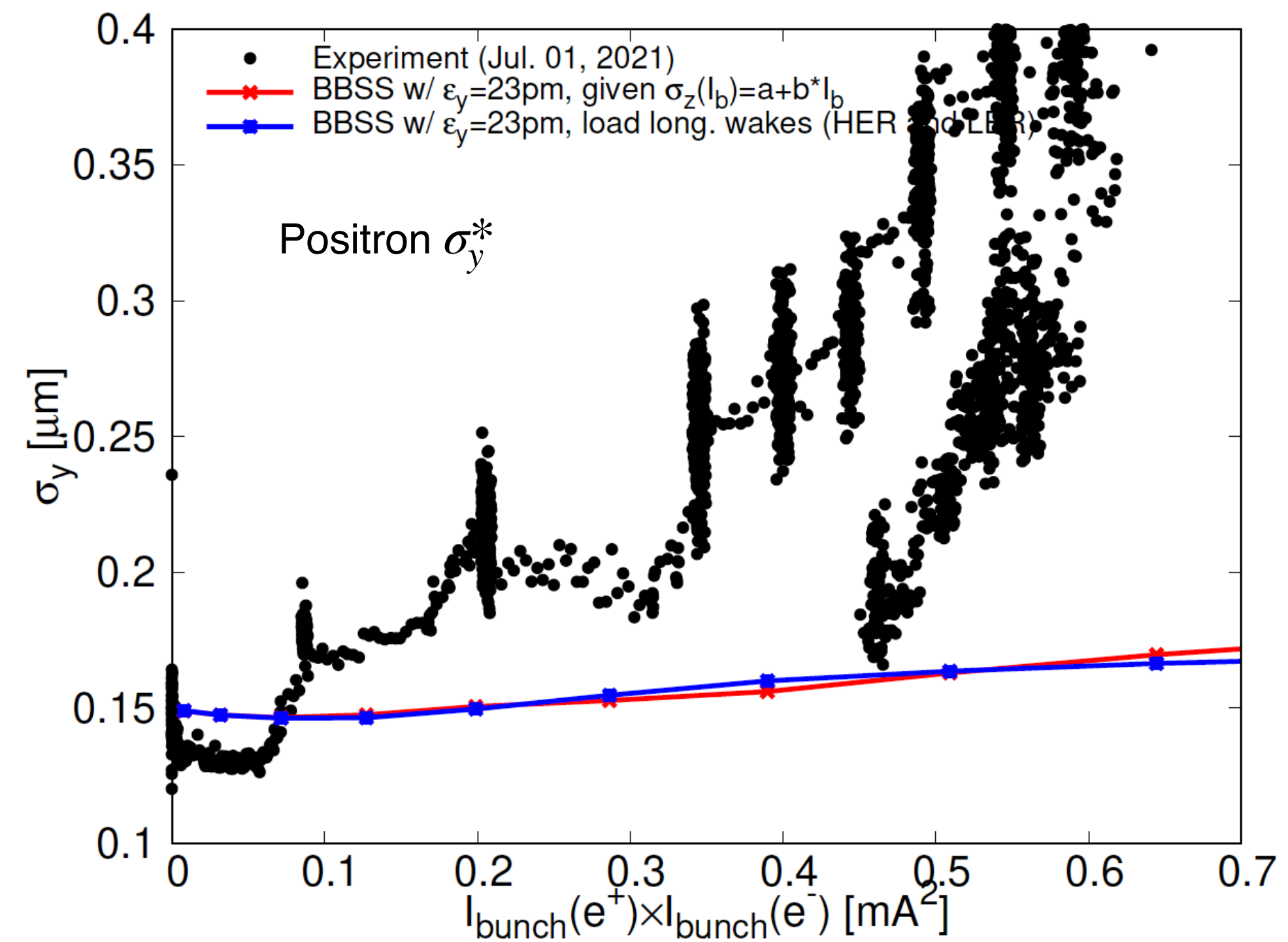
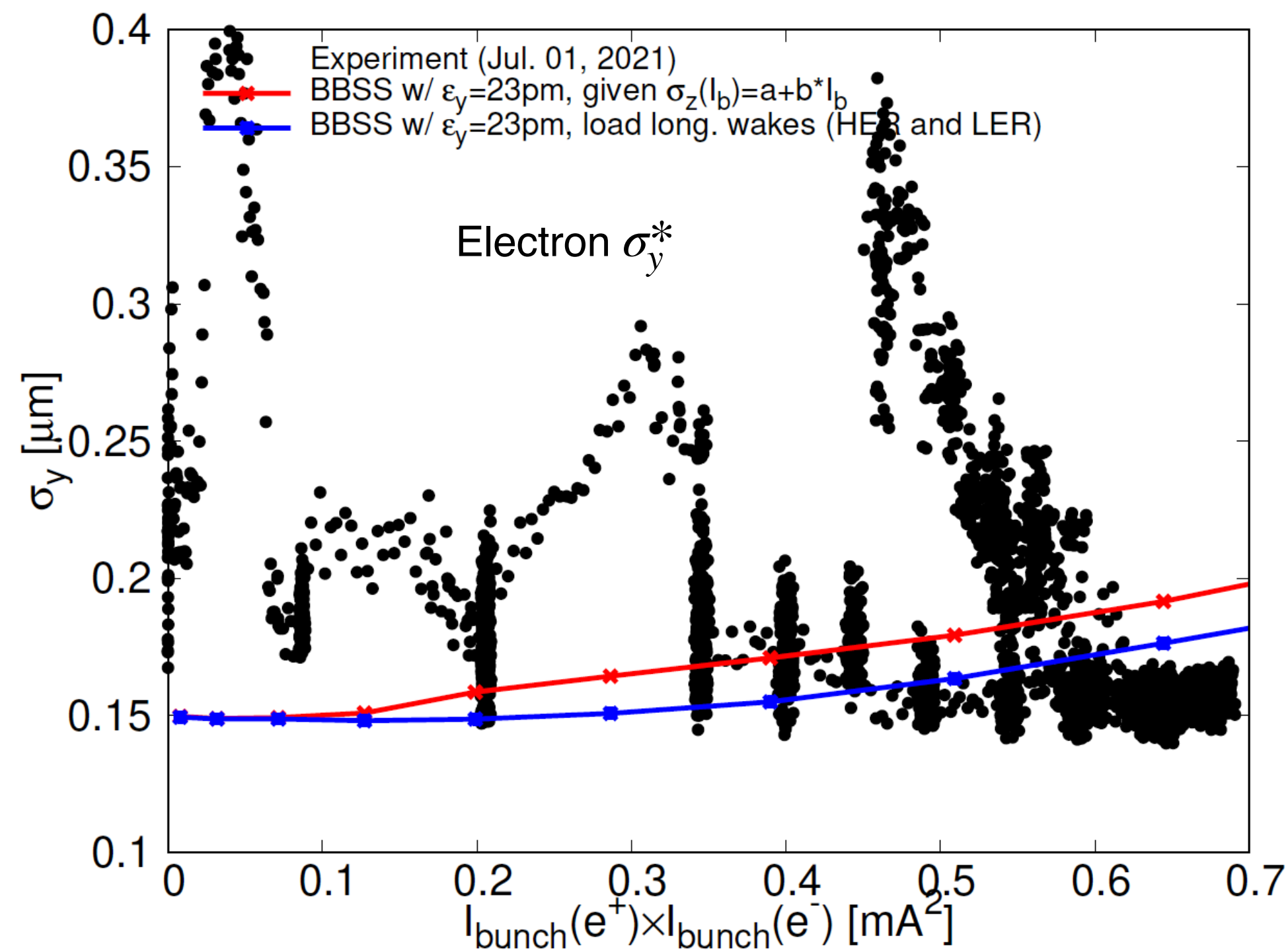
Beam-beam simulations for SuperKEKB (cont'd)

- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - Blowup of horizontal beam sizes is visible in simulations. Blowup in LER beam is stronger than that in HER beam. Somehow simulations agreed with experiment.
 - Horizontal blowup at low bunch currents was attributed to a feature of X-ray monitors.



Beam-beam simulations for SuperKEKB (cont'd)

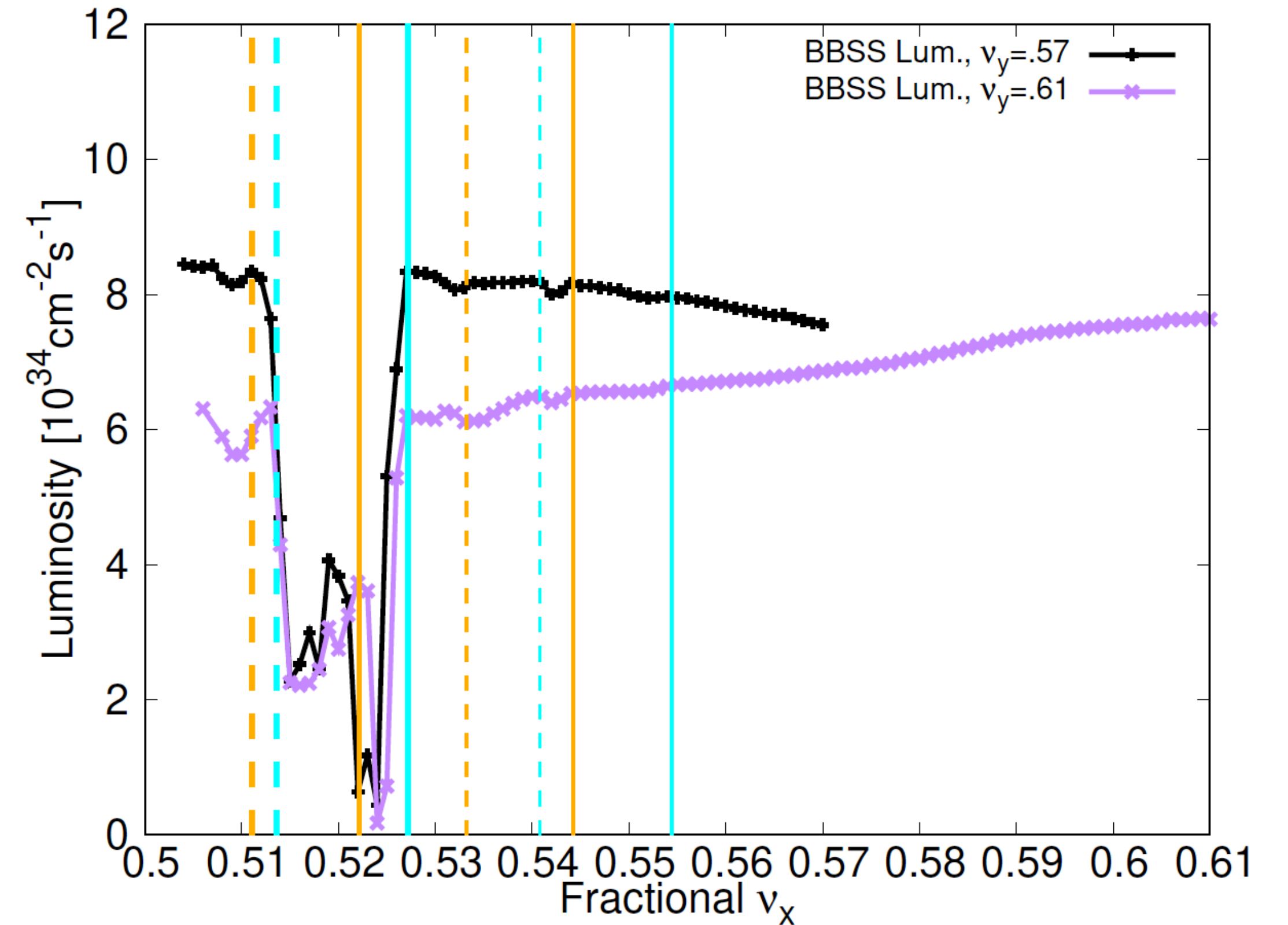
- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - Prediction of vertical blowup remains to be a challenge.
 - To predict the experiments, other sources are necessary to be included in beam-beam simulations.
 - Candidates sources: Transverse wakes, collision offset noise, IP aberrations (chromatic coupling, third-order RDTs, etc.), and others to be identified.



Beam-beam simulations for SuperKEKB (cont'd)

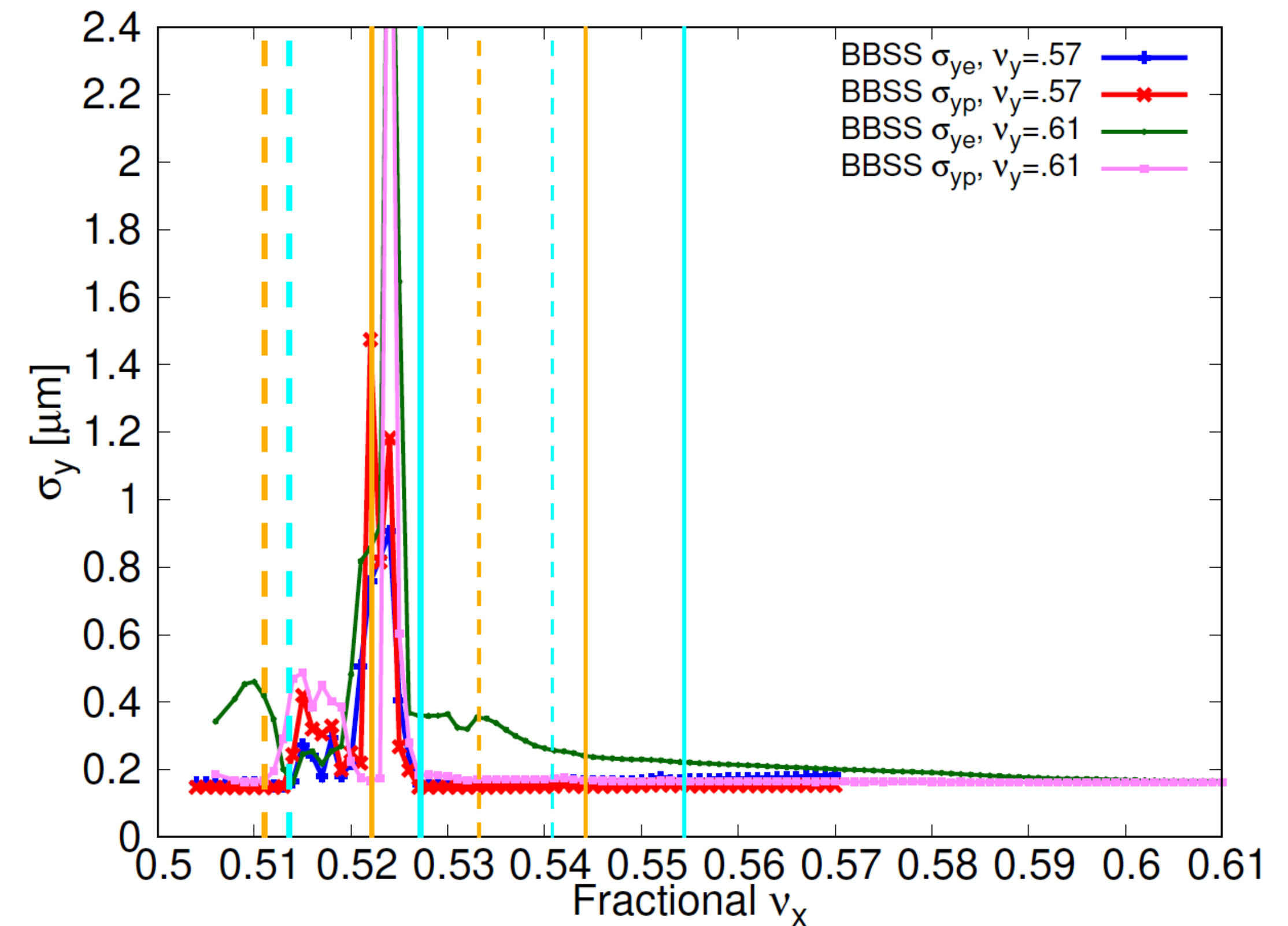
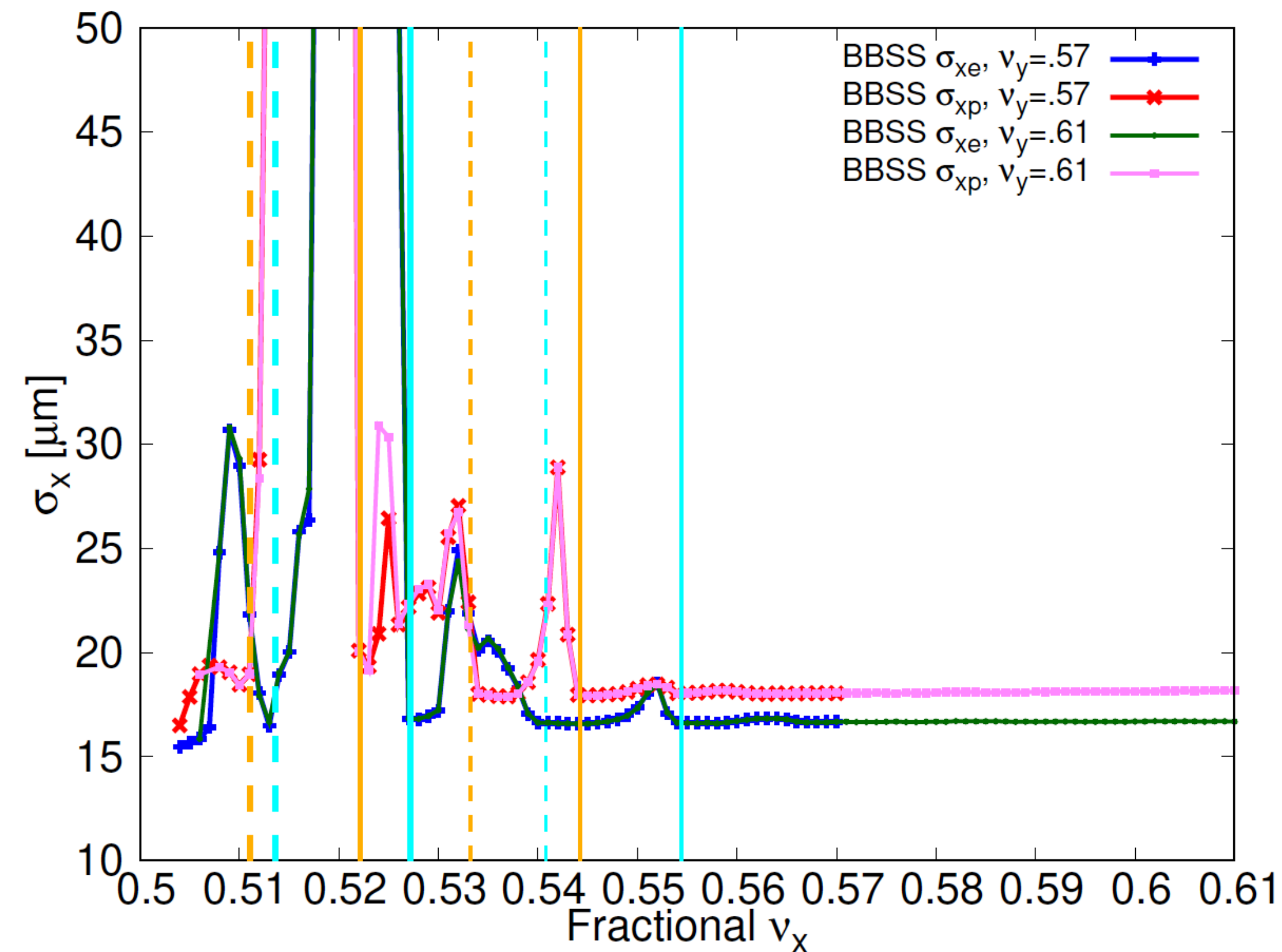
- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - The effects of beam-beam on choice of working point were investigated using BBSS simulations.
 - Beam parameters similar to observations on Jul. 1, 2021.
 - Assume equal ν_x for HER and LER. Fractional vertical tune set as $\nu_y = .57/.61$, scan ν_x . Track 2e6 macro particles to 12000 turns.

	2021.07.01		Comments
	HER	LER	
I_{bunch} (mA)	0.80	1.0	
# bunch	1174		Assumed value
ϵ_x (nm)	4.6	4.0	w/ IBS
ϵ_y (pm)	23	23	Estimated from XRM data
β_x (mm)	60	80	Calculated from lattice
β_y (mm)	1	1	Calculated from lattice
σ_{z0} (mm)	5.05	4.84	Natural bunch length (w/o MWI)
ν_x	45.532	44.525	Measured tune of pilot bunch
ν_y	43.582	46.593	Measured tune of pilot bunch
ν_s	0.0272	0.0221	Calculated from lattice
Crab waist	40%	80%	Lattice design



Beam-beam simulations for SuperKEKB (cont'd)

- Beam-beam simulations with machine parameters of Phase-3 including crab waist
 - With horizontal tune on the left of resonance line $\nu_x - 2\nu_s = N/2$, beam-beam drives horizontal blowup.
 - The X-Y emittance coupling is not included in BBSS simulations. But in realistic machine operation, there will be nonzero emittance coupling, therefore horizontal blowup will cause vertical blowup [3].
 - Avoiding horizontal blowup is a challenge to SuperKEKB.



Summary and outlook

- Beam-beam simulations with Phase-2 and Phase-3 machine parameters
 - BBSS simulations predict higher luminosity than measurement.
 - Vertical blowup observed in measurements cannot be predicted by BBSS simulations.
 - Beam-beam drives horizontal blowup. It requires careful choice of horizontal tunes.
- Outlook
 - The interplay of beam-beam and other effects (machine imperfections, longitudinal and transverse wake fields, space charge, etc.) is important and should be properly included in beam-beam simulations.

Backup

Introduction

- Weak-strong model + simple one-turn map: BBWS code [1]
 - The weak beam is represented by N macro-particles (statistical errors $\sim 1/\sqrt{N}$). The strong beam has a rigid charge distribution with its EM fields expressed by Bassetti-Erskine formula.
 - The simple one-turn map contains lattice transformation (Tunes, alpha functions, beta functions, X-Y couplings, dispersions, etc.), chromatic perturbation, synchrotron radiation damping, quantum excitation, crab waist, etc.
- Weak-strong model + full lattice: SAD code [2]
 - The BBWS code was implemented into SAD as a type of BEAMBEAM element, where beam-beam map is called in particle tracking.
 - Tracking using SAD: 1) Symplectic maps for elements of BEND, QUAD, MULT, CAVI, etc. 2) Element-by-element SR damping/excitation; 3) Distributed weak-strong space-charge; 4) MAP element for arbitrary perturbative maps (such as crab waist, wake fields, artificial SR damping/excitation, etc.); ...
- Strong-strong model + simple one-turn map: BBSS code [1]
 - Both beams are represented by N macro-particles.
 - The one-turn map is the same as weak-strong code. Beamstrahlung model is also available. Choices of numerical techniques: PIC, Gaussian fitting for each slice, ...
 - For SuperKEKB, it is hard to include a full lattice in SS simulations.

$$M = M_{rad} \circ M_{chr} \circ M_{bb} \circ M_{cw} \circ M_0$$

$$M_0 = R \cdot M_{lin} \cdot R^{-1}$$

Beam-beam element in SAD code:

```
;  
BEAMBEAM  BMBMP =(NP=3.63776D10  
           BETAX=0.06 BETAY=0.001  
           EX=0.D0 EY=0.D0  
           EMIX=4.6D-9 EMIY=40.D-12  
           SIGZ=6.D-3 DP=6.30427D-4  
           ALPHAX=0.D0 ALPHAY=0.D0  
           DX=0.E-6 DZ=0.0  
           SLICE=200.D0  
           XANGLE=41.5D-3  
           STURN=1000)  
;
```

[1] K. Ohmi, Talk presented at the 2019 SAD workshop, <https://conference-indico.kek.jp/event/75/>.

[2] <https://acc-physics.kek.jp/SAD/>.

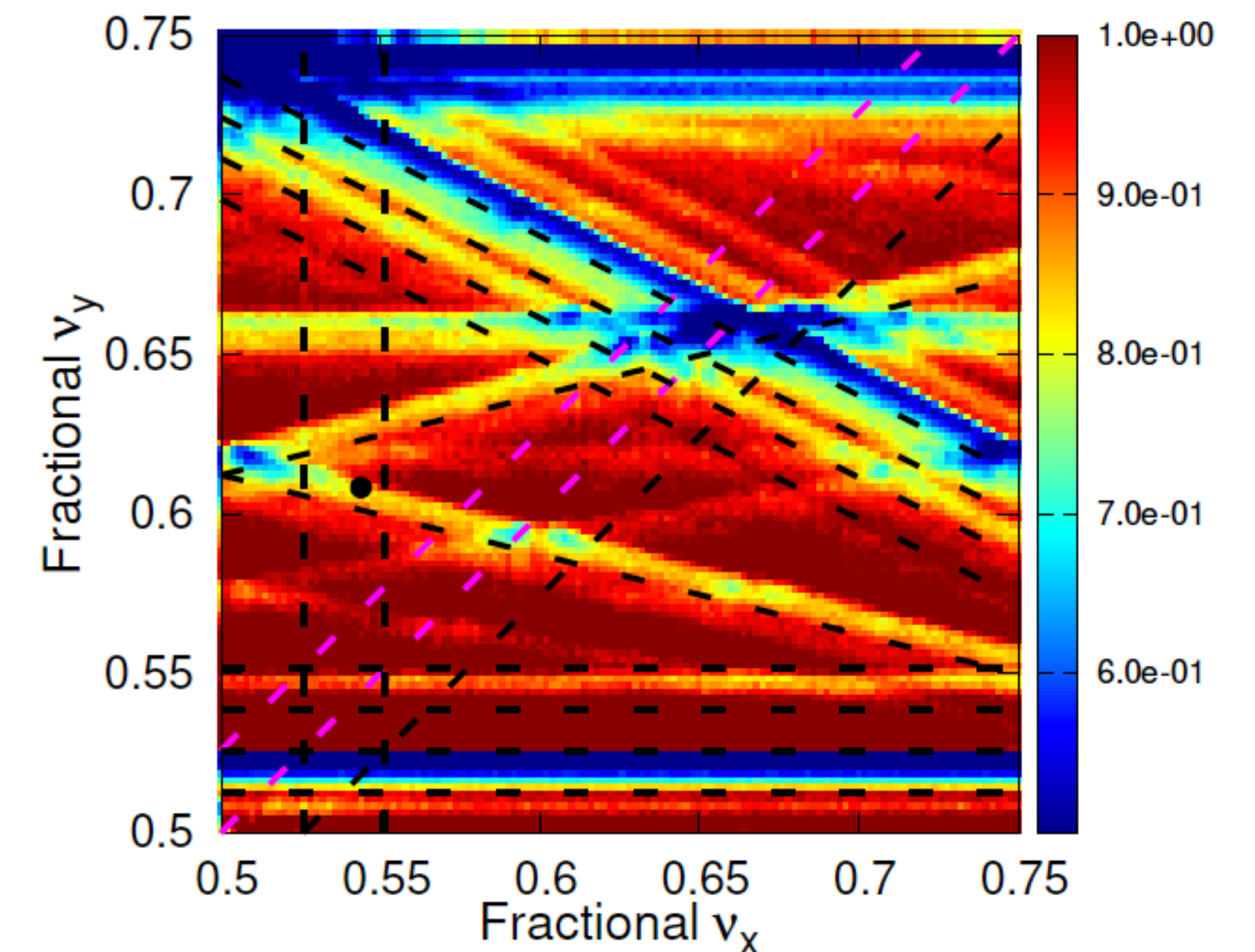
Brief overview of strategy for beam-beam simulations (cont'd)

- Weak-strong model + simple one-turn map: BBWS code
 - Pros: Fast simulation of luminosity and beam-beam effects. Not require much computing resources. Used for [tune survey](#), [fast luminosity calculation](#), etc..
 - Cons: Strong beam frozen. Not sensitive to coherent beam-beam head-tail (BBHT) instability (BBHTI).
- Weak-strong model + full lattice: SAD code
 - Pros: Relatively fast to allow tracking with lattice. [Interplay of beam-beam and lattice nonlinearity](#). Space-charge modeling possible. Localized geometric wakes possible.
 - Cons: Same as BBWS code. Tune survey possible but relatively slow.
- Strong-strong model + simple one-turn map: BBSS code
 - Pros: Allow dynamic evolution of 3D distribution of two beams. Detect [BBHTI](#).
 - Cons: PIC tracking quite slow. Not feasible for survey in tune space. No effective method of parallelization.

Beam-beam simulations for SuperKEKB (cont'd)

- Beam-beam simulations with machine parameters of Phase-2 and early Phase-3
 - Machine observations without crab waist: Peak luminosity lower than predictions of simulations; Easy blowup of one beam; Small area in tune space for good luminosity; Unexpected high Belle-2 background; No or small gain of luminosity via squeezing $\beta_{x,y}^*$; Hard to approach to the design working point (.53, .57); ...
 - Tune scan using BBWS with observed beam parameters showed that the beam-beam resonances of $\pm\nu_x + 4\nu_y + \alpha = N$ (they appear without crab waist) could be important [4].
 - Collision with small ϵ_y would be very challenging: vertical emittance blowup seemed unavoidable.

	2019.03.30		2019.04.02		2019.07.01	
	HER	LER	HER	LER	HER	LER
I_b (A)	0.21	0.26	0.17	0.22	0.8	0.8
# bunch	789		789		1576	
ϵ_x (nm)	4.728	1.731	4.537	1.641	4.49	1.93
ϵ_y (pm)	122.5	40	53.33	13.33	16.2	6.05
β_x (mm)	200	200	100	200	80	80
β_y (mm)	4	4	3	3	2	2
σ_z (mm)	6	6	6	6	5.5	5.2
ν_x	45.564	44.571	45.5439	44.5568	45.53	44.542
ν_y	43.603	46.610	43.6082	46.618	43.583	46.605
ν_s	0.0256	0.0219	0.02576	0.02205	0.02717	0.02349



Luminosity tune scan: BBWS simulations with weak e- beam using parameter set of 2019.04.02

[4] D. Zhou, Talk presented at the 1st SuperKEKB Beam Dynamics Mini-Workshop, KEK, Jul. 17, 2019 (<https://kds.kek.jp/event/31793/>).