

# Back to the Formula

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## LHC Edition

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arXiv: [2109.10414](https://arxiv.org/abs/2109.10414)



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# Content

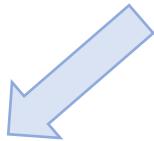
- Motivation
- Optimal observable
- CP violation in WBF
- Results

# Motivation

New techniques for improved LHC analysis



Optimal Observables

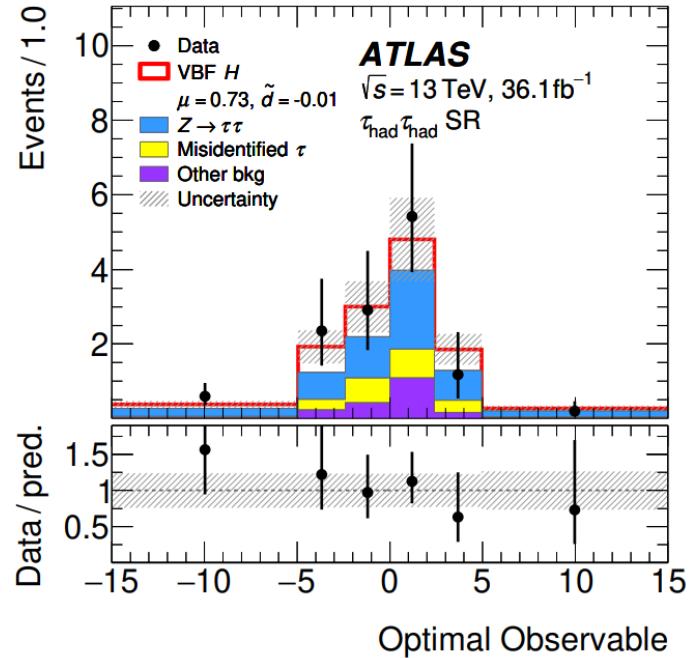


Neural networks

Symbolic Regression

# Optimal observable

- Best observable to measure a parameter
- First introduced in:
  - D. Atwood, A Soni: [Phys. Rev. D45 \(1992\) 2405](#)
  - M. Diehl, O. Nachtmann: [Z. Phys. C 62 \(1994\) 397-412](#)
  - M. Davier et al.: [Phy. Lett. B306 \(1993\) 411](#)
- Traditionally introduced for processes in e+e- colliders
- Used for instance in ATLAS analysis [arXiv 2002.05315](#)



# Optimal observable

Traditional optimal observables numerically involved

→ More general approach by Brehmer et al. [arXiv 1805.00020](https://arxiv.org/abs/1805.00020) (MadMiner)

Likelihood

$$p(z|\theta) = \frac{1}{\sigma(\theta)} \frac{d\sigma(z|\theta)}{dz}$$

Score

$$t(z|\theta) = \nabla_\theta \log p(z|\theta) = \frac{\nabla_\theta d\sigma(z|\theta)}{d\sigma(z|\theta)} - \frac{\nabla_\theta \sigma(\theta)}{\sigma(\theta)} \sim \frac{\nabla_\theta |\mathcal{M}|^2}{|\mathcal{M}|^2}$$

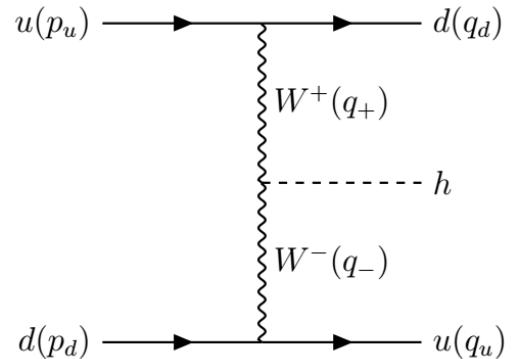
$z$  contains latent variables (parton shower, detector effects, etc.)

Marginalize over latent variables → Optimal observable

# CP violation in weak boson fusion

Hankele et al. [arXiv: hep-ph/0609075](https://arxiv.org/abs/hep-ph/0609075)

Brehmer et al. [arXiv: 1712.02350](https://arxiv.org/abs/1712.02350)



Parameter  $\theta = f_{W\widetilde{W}}$

Operator  $\mathcal{O}_{W\widetilde{W}} = -(\phi^\dagger \phi) \widetilde{W}_{\mu\nu}^k W^{\mu\nu k}$

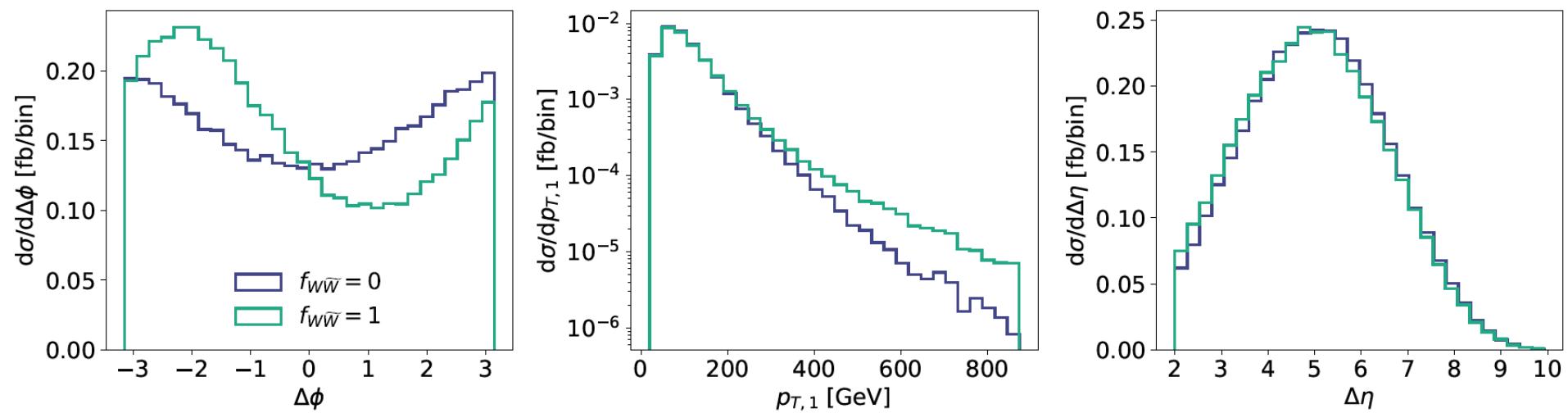
Matrix element  $|\mathcal{M}|^2 = p_0 + a\theta + b\theta^2$

Score  $t(z|\theta) \sim \frac{\nabla_\theta |\mathcal{M}|^2}{|\mathcal{M}|^2} = \frac{a + 2b\theta}{p_0 + a\theta + b\theta^2} \sim \frac{a}{p_0} + \frac{1}{p_0} \left( 2b - \frac{a^2}{p_0} \right) \theta$

CP observable  $\epsilon_{\mu\nu\rho\sigma} p_u^\mu p_d^\nu q_u^\sigma q_d^\rho \sim p_{T1} p_{T2} \sin \Delta\phi$

# Optimal observable for $f_{W\bar{W}} \widetilde{=} 0$

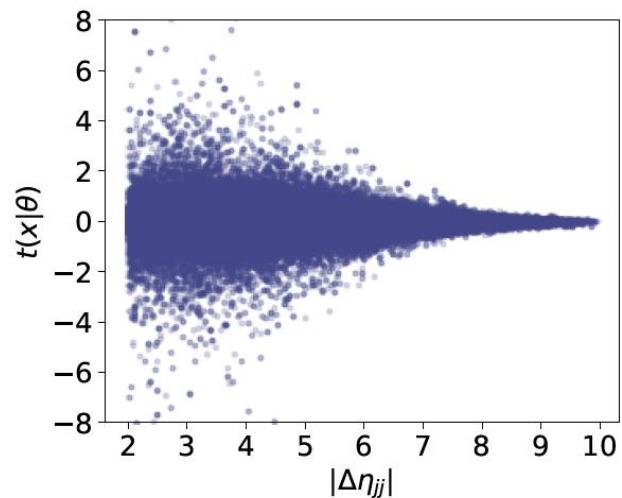
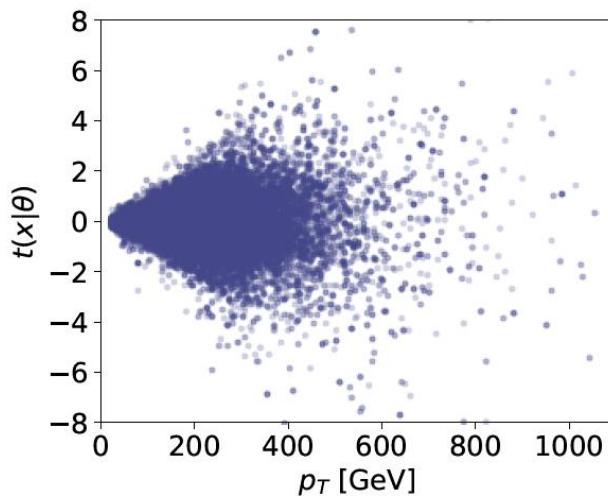
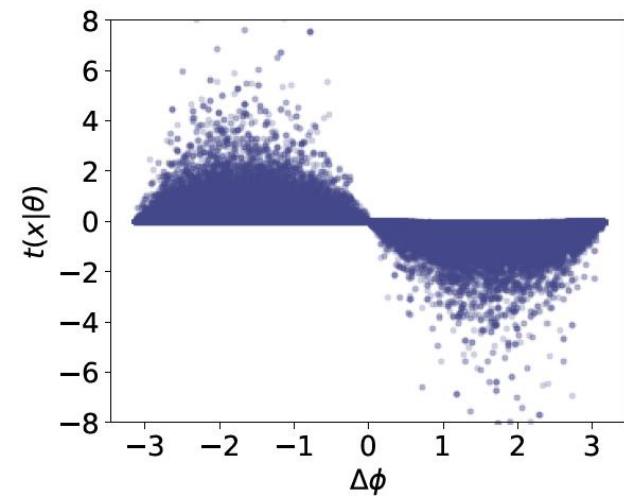
## Event distribution



Relevant observables  
 $\Delta\phi, p_{T,1}, p_{T,2}, \Delta\eta$

# Optimal observable for $f_{W\widetilde{W}} = 0$

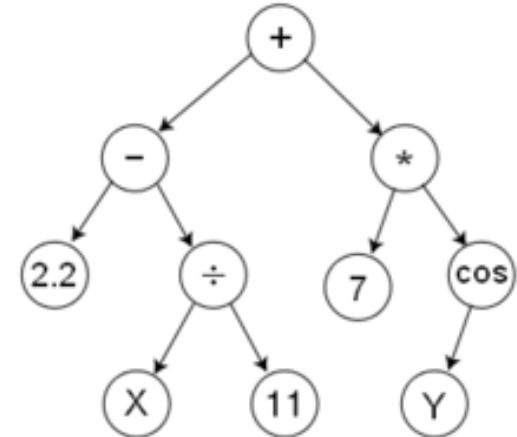
Score



Relevant observables  
 $\Delta\phi, p_{T,1}, p_{T,2}, \Delta\eta$

# Symbolic regression

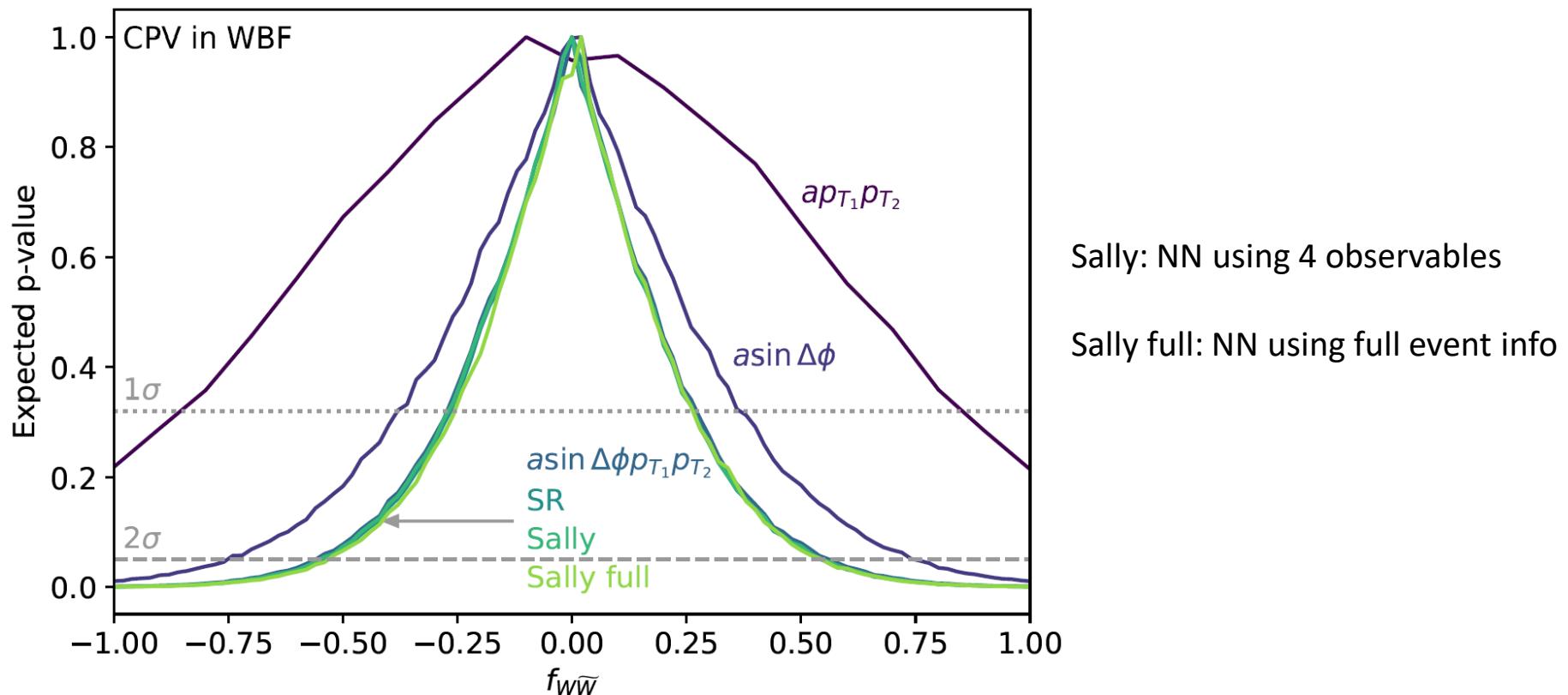
- Genetic algorithm implemented in [PySR](#)  
M. Cranmer et al. [arXiv 2006.11287](#)
- Input: operators and training data
- Output: hall of fame - best formulas for each complexity



# nodes

cmpl.	function	MSE
4	$a \sin(\Delta\phi)$	$1.03 \cdot 10^{-1}$
8	$a \sin(\Delta\phi) p_{Tj1} p_{Tj2}$	$1.49 \cdot 10^{-2}$
16	$-p_{Tj1}(a - b\Delta\eta)(p_{Tj2} + c) \sin(\Delta\phi + d)$	$8.50 \cdot 10^{-3}$
28	$(p_{Tj2} + a)(bp_{Tj1}(c - \Delta\phi) - p_{Tj1}(d\Delta\eta + ep_{Tj2} + f) \sin(\Delta\phi + g))$	$8.18 \cdot 10^{-3}$

# Results



Symbolic regression formula comparable to NN

# Summary

- Optimal observables first introduced for e+e- colliders
- OO evaluation possible numerically or analytically
- Symbolic regression provides interpretable formulas