

# Exploring the structure of hadronic showers and the hadronic energy reconstruction with highly granular calorimeters

Vladimir Bocharnikov (DESY)  
on behalf of the CALICE Collaboration  
8 Nov 2021



*The 2021 International Workshop on the  
High Energy Circular Electron Positron Collider*

# Highly granular calorimeters

## Motivation

### Planned experiments at lepton colliders

ILC, CLIC, CEPC, FCCee, ... detector concepts: ILD, SiD, ...

- **precision frontier:** measurements of Higgs couplings, W, Z and top properties, searches for BSM physics
- model-independent analyses possible
- clean environment

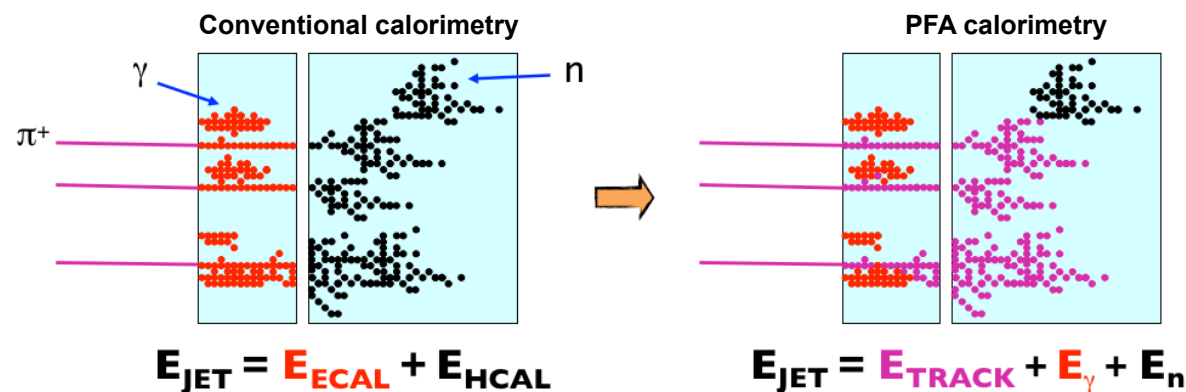
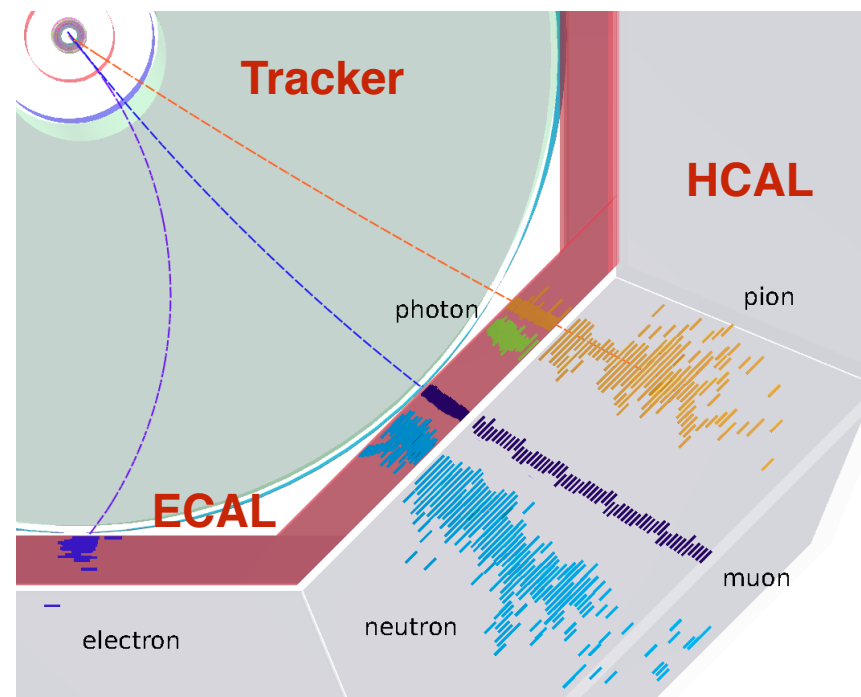
**Goal: 3-4% jet energy resolution (~50-250 GeV)**

to distinguish di-jets from W and Z hadronic decays

**Particle Flow Approach** - promising solution for jet energy reconstruction with best suited detectors depending on particle type within a jet

- Used in CMS and ATLAS
- Better performance can be achieved with
  - **High granularity** of calorimeter system

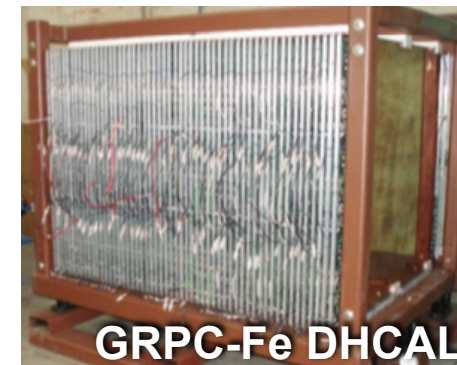
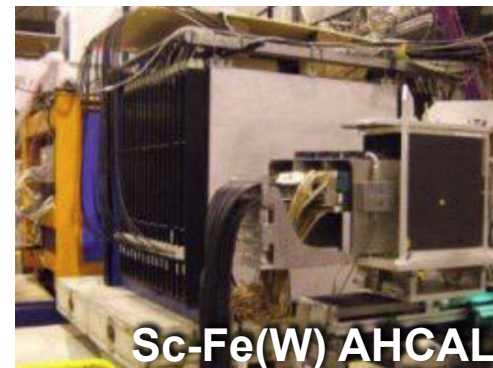
Not only lepton colliders: CMS HGCAL, DUNE ND...



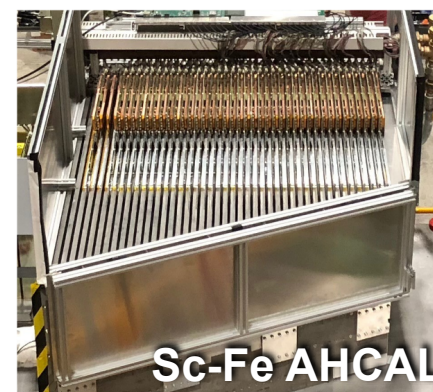
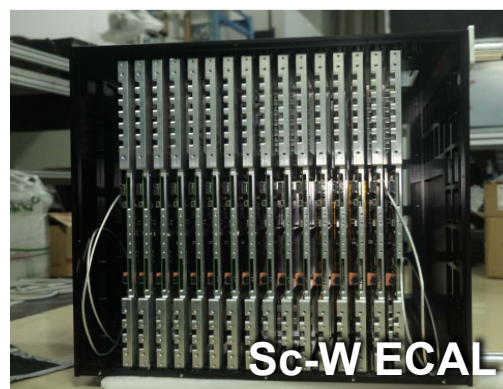
# CALICE developments of highly granular calorimeters

Since 2005. Semi-conductor, scintillator and gaseous read-outs

Proof-of-principle physics prototypes



Second generation technological prototypes



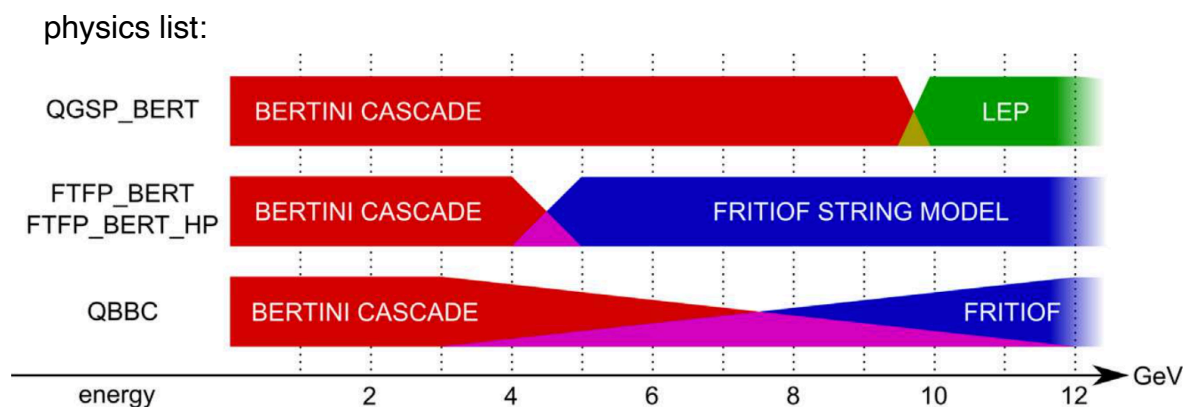
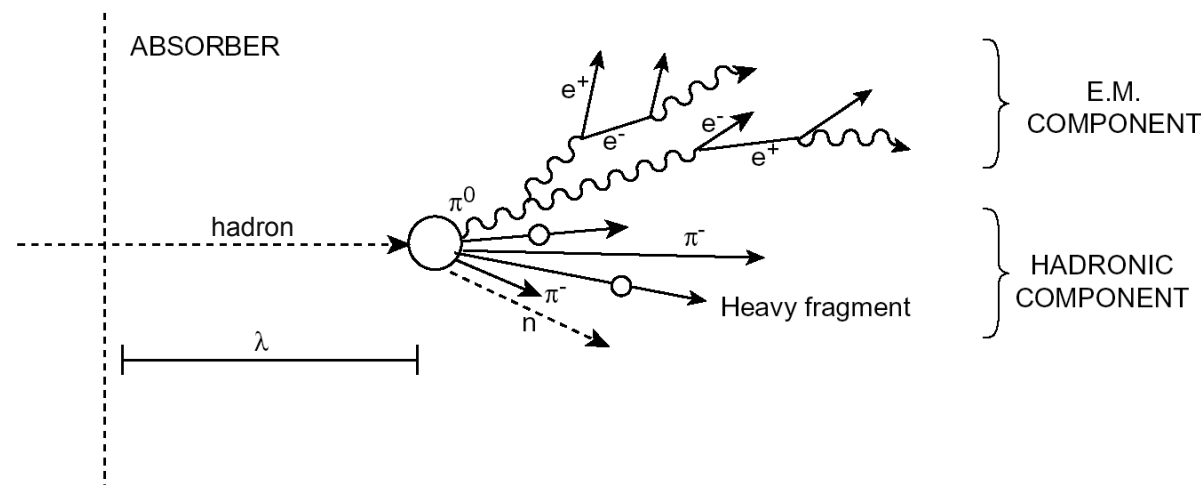
*Technical details of the CALICE prototypes will be discussed in talks by Shu and Yong*



# Hadronic showers

## General properties and Monte Carlo modelling

- Hadronic shower development is rather complex:
  - Narrow EM core component from  $\pi^0/\eta$
  - Surrounding halo dominated by charged hadrons
  - Large event-by-event fluctuation of EM/HAD ratio
  - Response to EM and HAD components is different in non-compensating calorimeters
  - Invisible energy as binding energy, nuclear recoil, neutrinos + late component
  - ➔ Limited hadronic energy resolution
- Geant4 hadronic shower modelling is not perfect
  - ➔ Strongly dependent on energy and absorber material
    - Validation of models using test beam data
- Some **results of studies on hadronic showers using test beam data with CALICE prototypes will be presented in this talk**

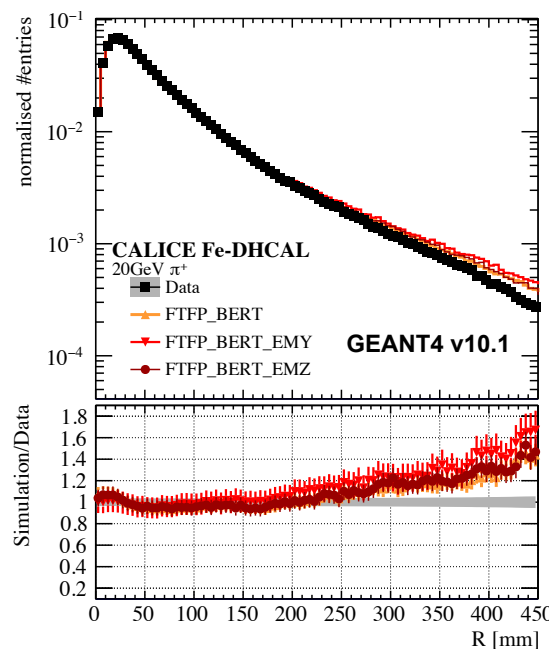




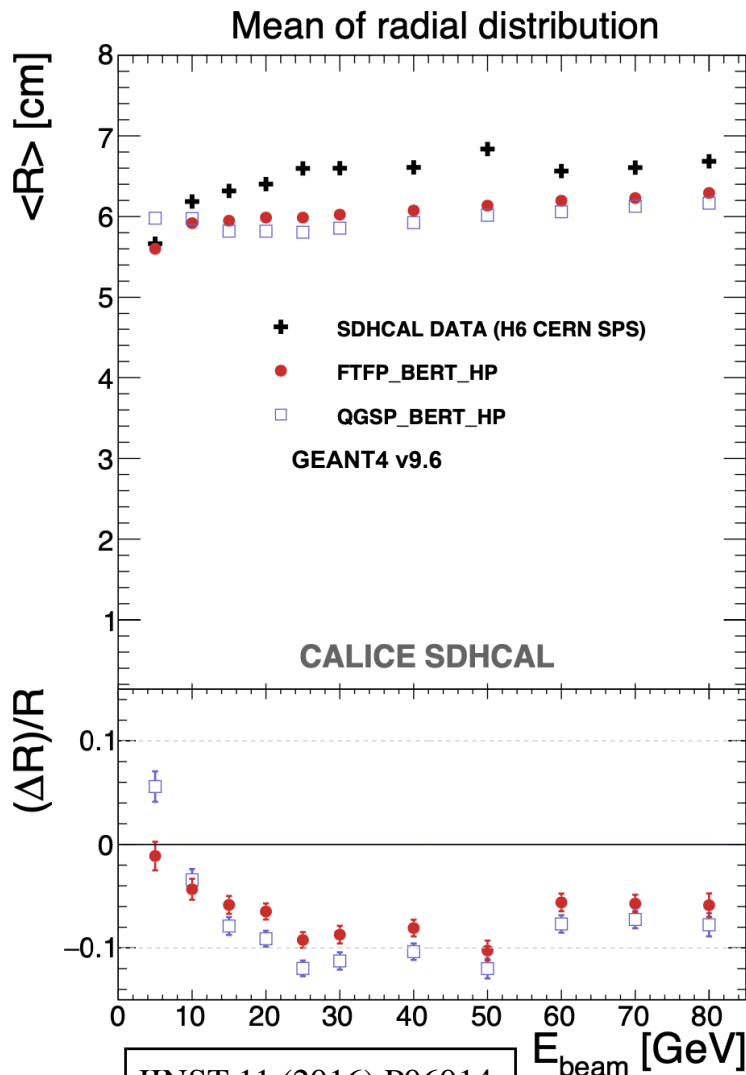
# Hadronic shower profiles

Radial development. Data-MC comparison is important for understanding of shower separation performance

- **Radial profile (S)DHCAL:**  $N_{\text{hits}}$  in 1-cm rings around shower axis
- ➔ Compare different physics lists with test beam data results

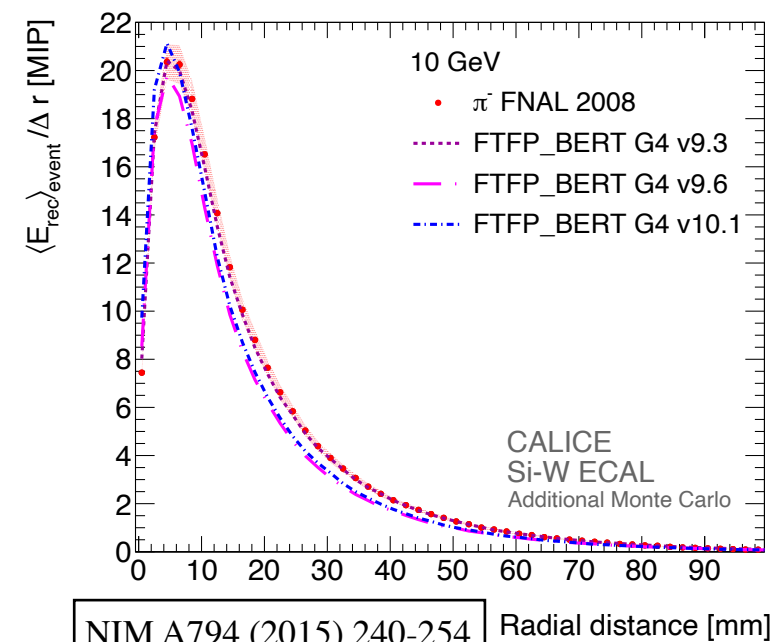


NIM A939 (2019) 89-105



JINST 11 (2016) P06014

- **Radial profile Si-W ECAL:** visible energy density in the cylinder of radius  $r$  and width  $\Delta r$  vs radial distance from shower axis
- ➔ Compare different Geant4 versions with test beam data results



NIM A794 (2015) 240-254

Radial distance [mm]

# Hadronic shower profiles

JINST 11 (2016) P06013

## Longitudinal development and decomposition of shower components

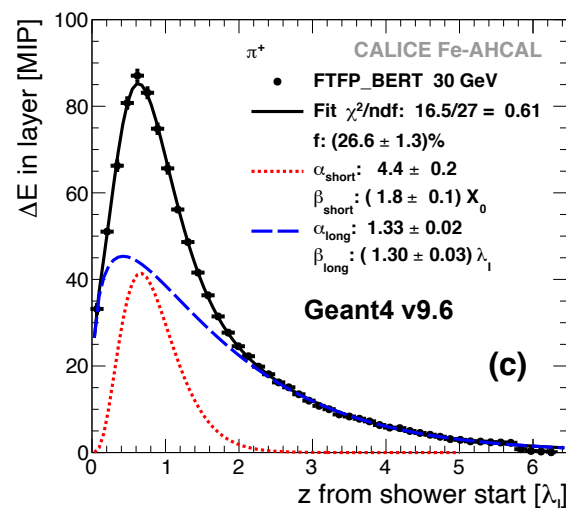
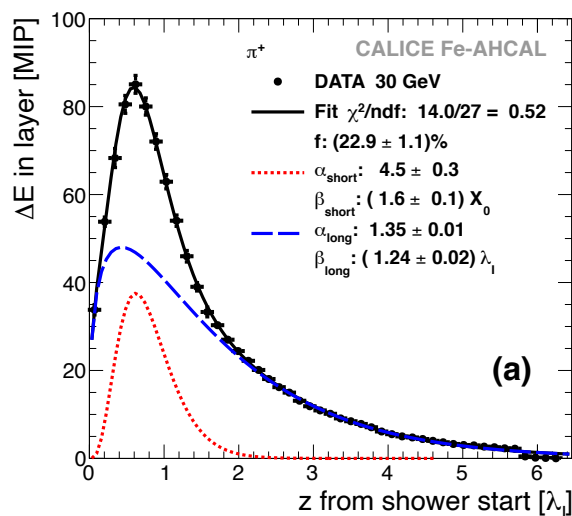
- **Longitudinal profile** (Fe-AHCAL): visible energy  $\Delta E$  per transverse layer vs. longitudinal distance from the identified shower start
- Non-compensating calorimeters: Hadronic & electromagnetic response not the same ( $h/e < 1$ )

• Parametrisation: 
$$\Delta E = A \left\{ \frac{f \cdot \exp\left(-\frac{z}{\beta_{\text{short}}}\right)}{\beta_{\text{short}} \cdot \Gamma(\alpha_{\text{short}})} \cdot \left(\frac{z}{\beta_{\text{short}}}\right)^{\alpha_{\text{short}}-1} + \frac{(1-f) \cdot \exp\left(-\frac{z}{\beta_{\text{long}}}\right)}{\beta_{\text{long}} \cdot \Gamma(\alpha_{\text{long}})} \cdot \left(\frac{z}{\beta_{\text{long}}}\right)^{\alpha_{\text{long}}-1} \right\}$$

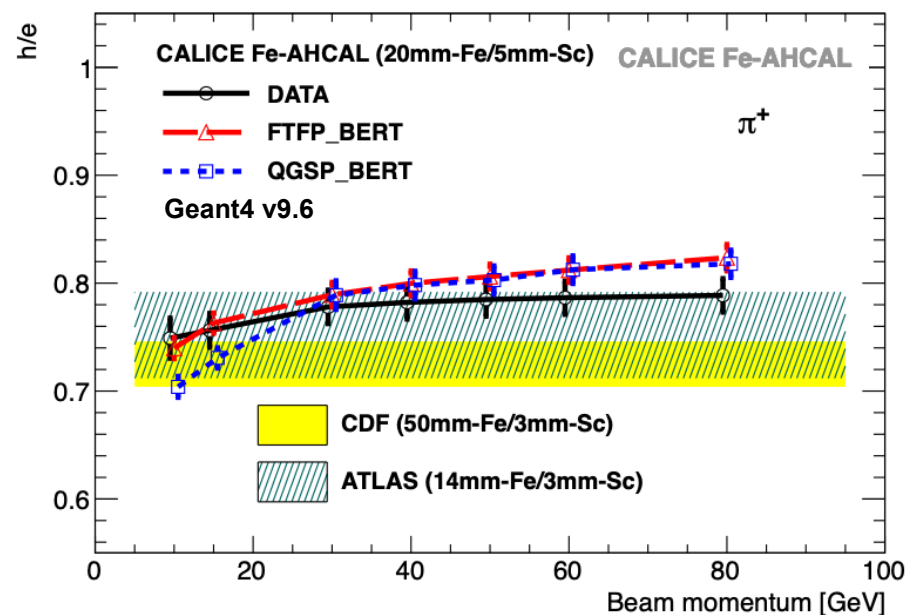
$A$  - scaling factor  
 $f$  - fraction of the "short" component  
 $\Gamma$  - gamma function

$z$  - distance from shower start  
 $\alpha_{\text{short}}$  and  $\alpha_{\text{long}}$  - shape parameters  
 $\beta_{\text{short}} < \beta_{\text{long}}$  - slope parameters

*proposed in R.K. Bock et al. NIM, 186 (1981)*



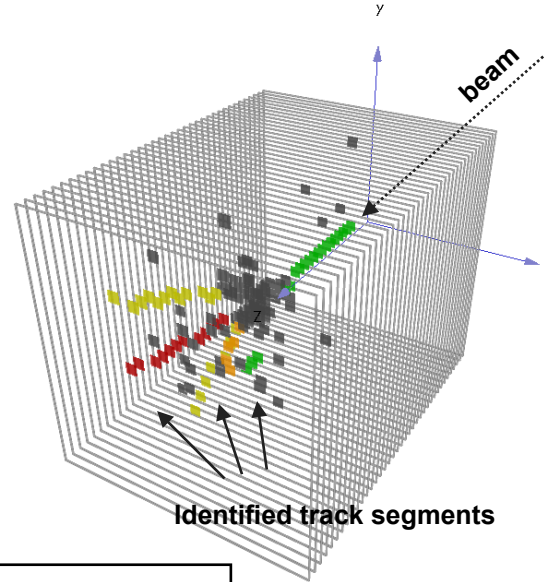
➔ Extract  $h/e$  ratio and compare to GEANT4 v9.6 simulations



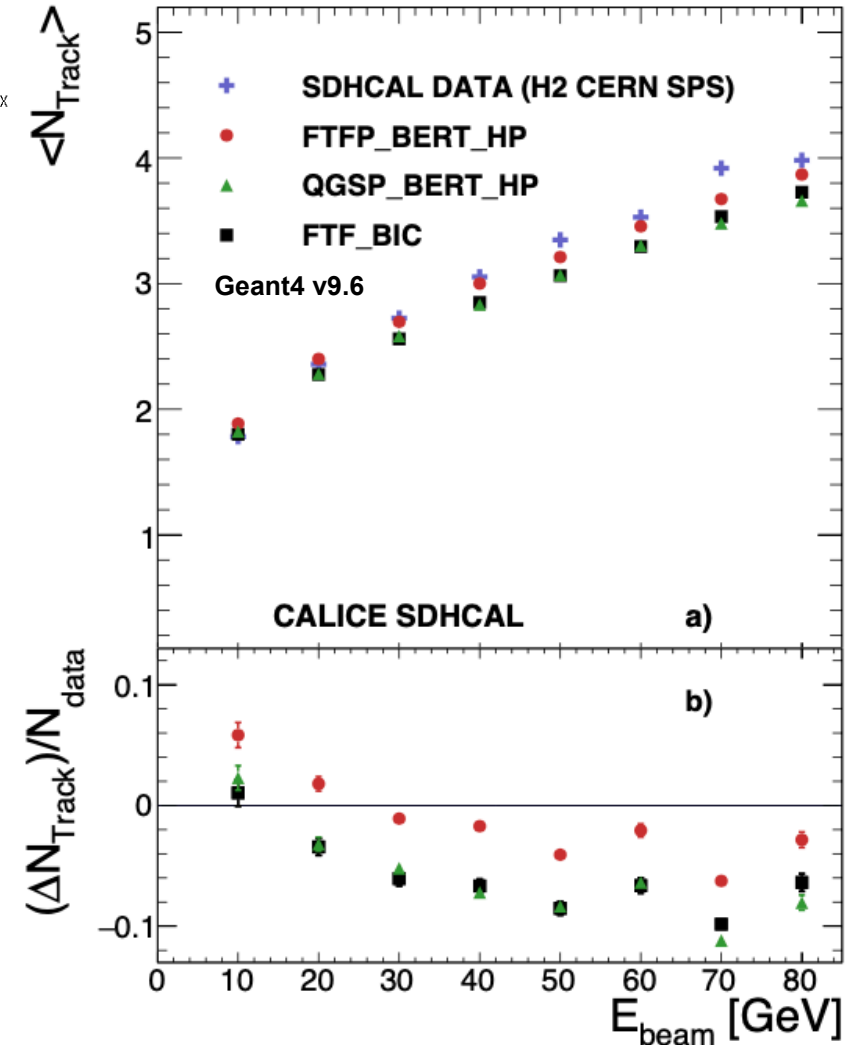
# Track segments

## In hadronic showers

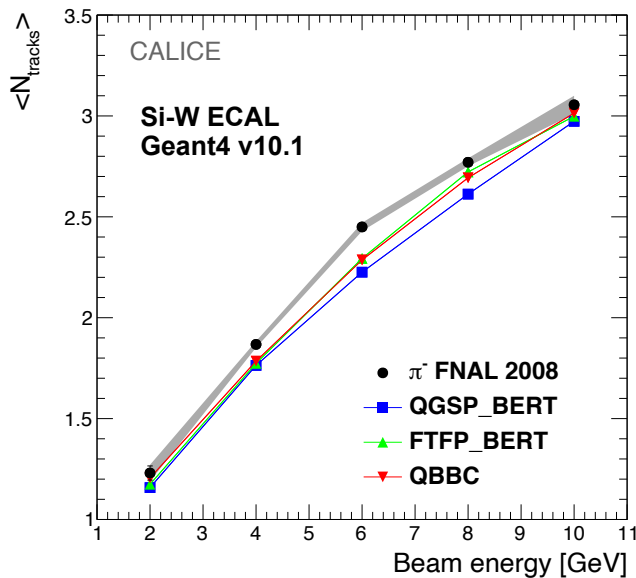
- Track finding within shower sub-structure works in all high granularity technologies
- Useful for detailed study of shower development (data vs. simulation), calibration and event characterisation



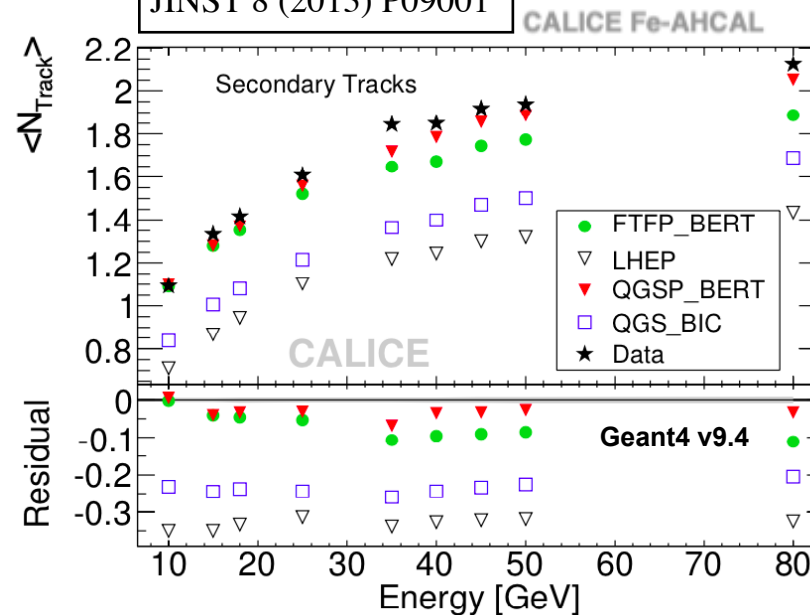
JINST 12 P05009 (2017)



NIM A937 (2019) 41-52



JINST 8 (2013) P09001





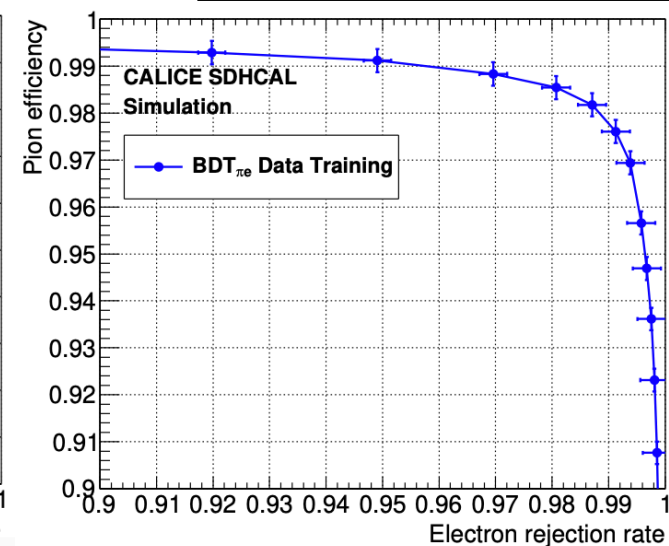
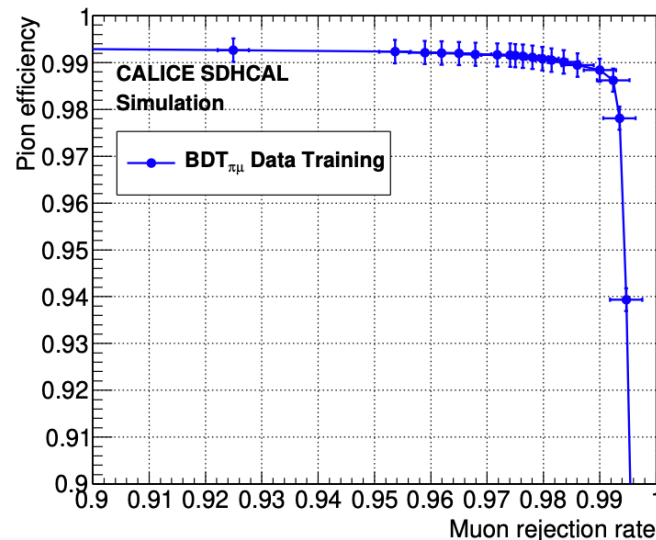
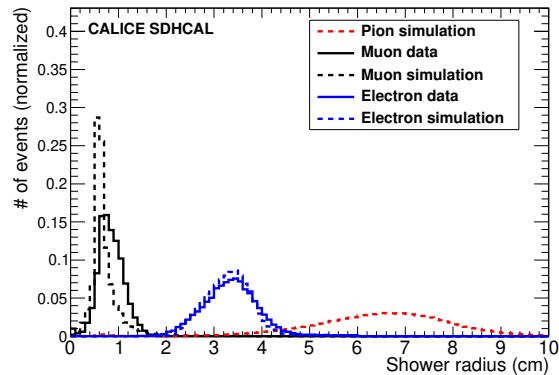
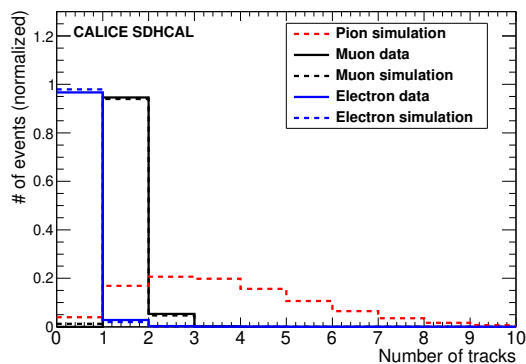
# Particle Identification

## Multi-Variate Analysis with SDHCAL and AHCAL

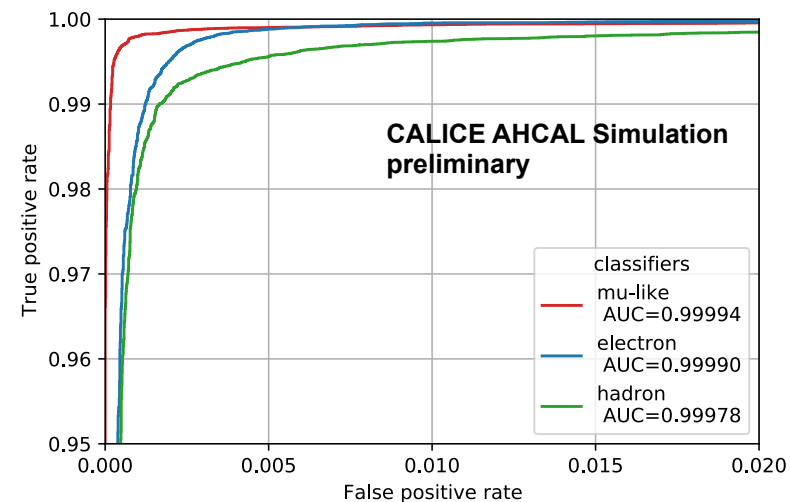
- Discriminating variables based on event topologies of **hadrons**, **electrons** and **muons** are used to train a Boosted Decision Tree (BDT) classification model

### SDHCAL:

- Shower start layer number
  - Number of track segments
  - Ratio of shower layers over total number of layers
  - Shower density
  - Shower radius
  - Shower maximum position (longitudinal coordinate)
- Training on both MC and data (SDHCAL)
- ➡ High signal purity/efficiency obtained



JINST 15 (2020) 10, P10009



$$TPR = \frac{TP}{TP + FN}$$

$$FPR = \frac{FP}{FP + TN}$$

# Particle Identification

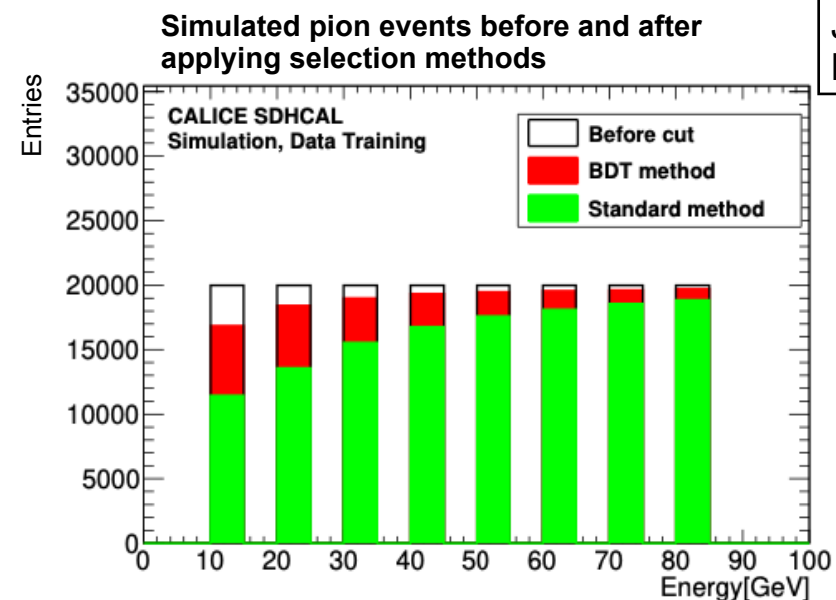
## Multi-Variate Analysis with SDHCAL and AHCAL

- Discriminating variables based on event topologies of **hadrons**, **electrons** and **muons** are used to train a Boosted Decision Tree (BDT) classification model

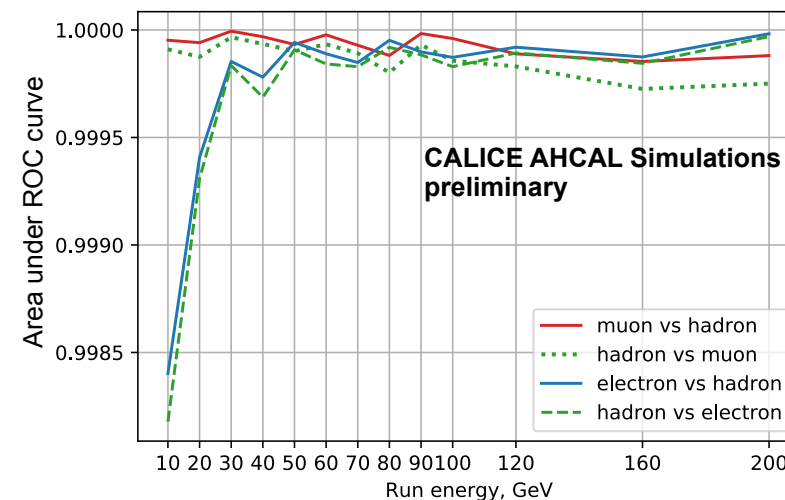
### SDHCAL:

- Shower start layer number
  - Number of track segments
  - Ratio of shower layers over total number of layers
  - Shower density
  - Shower radius
  - Shower maximum position (longitudinal coordinate)
- Training on both MC and data (SDHCAL)
  - ➔ High signal purity/efficiency obtained
  - ➔ Stable performance on wide energy range (slight decrease for low energies)

*More examples for ongoing multivariate analyses with AHCAL in backup slides*



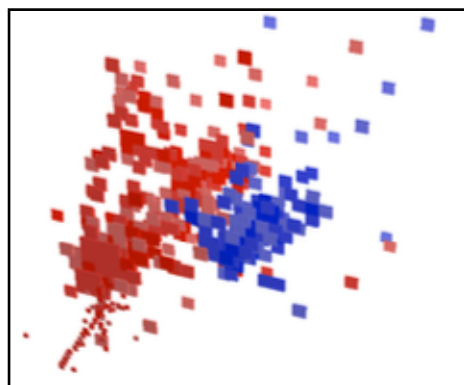
JINST 15 (2020) 10, P10009



# Particle Flow Algorithms applied to CALICE prototype data

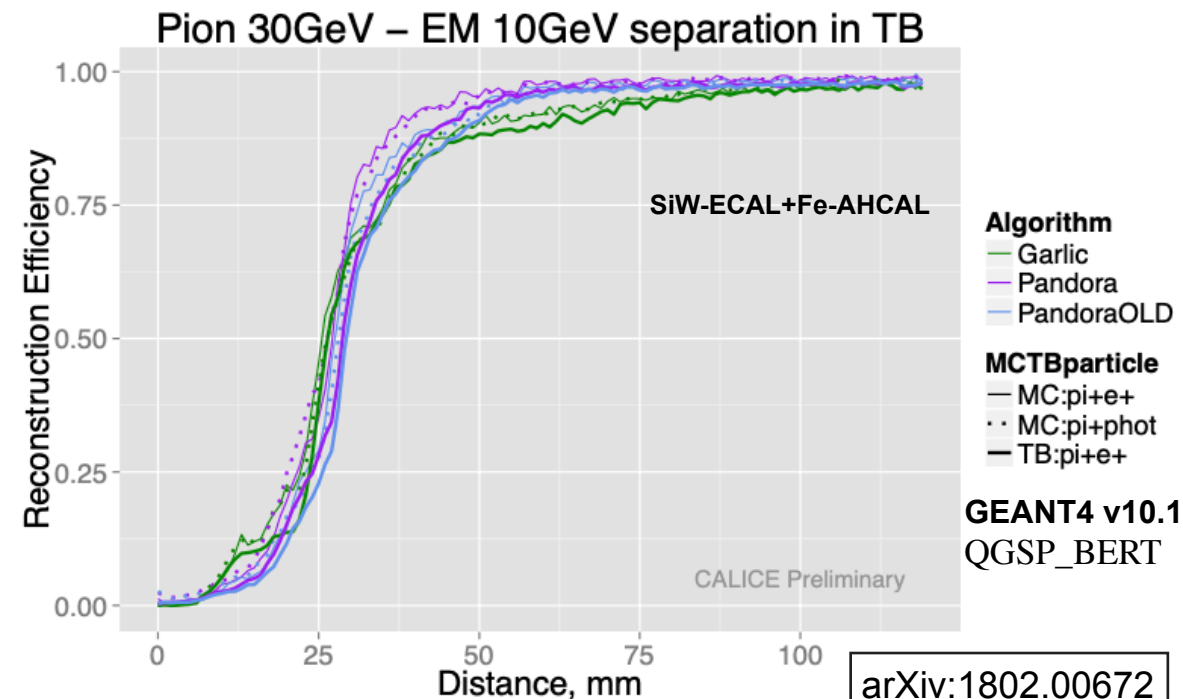
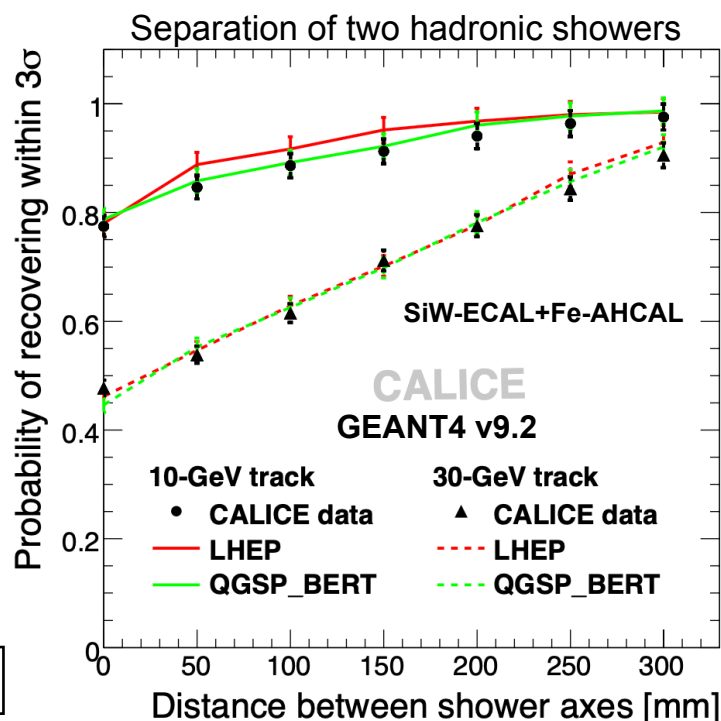
## Two particle separation performance

- Figure of merit for Particle Flow algorithms
  - Artificially overlaid test beam events in SiW ECAL + AHCAL
  - used to tune PFA parameters
  - ➔ Good agreement between data and simulations



Neutral Hadron  
Charged Hadron

JINST 6 P07005 (2011)



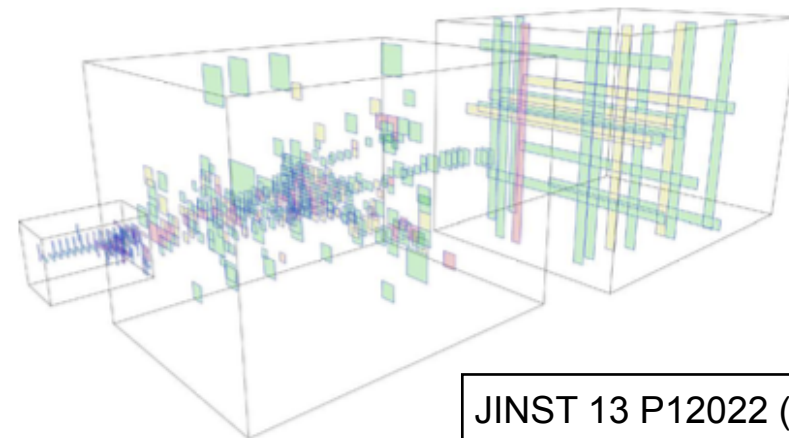


# Energy reconstruction

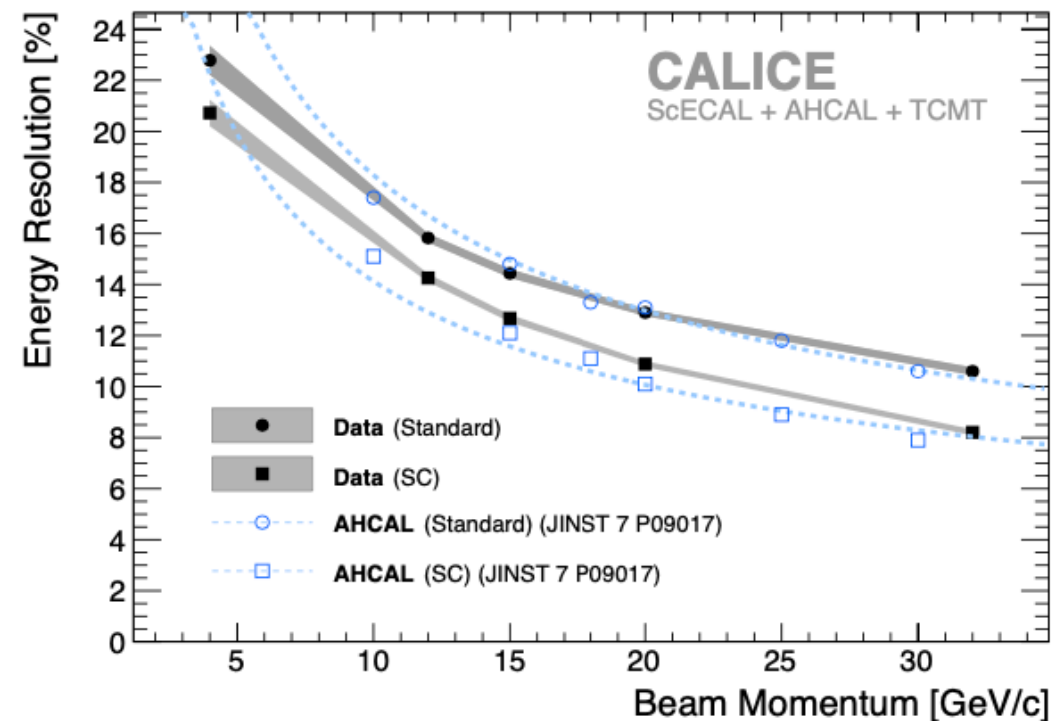
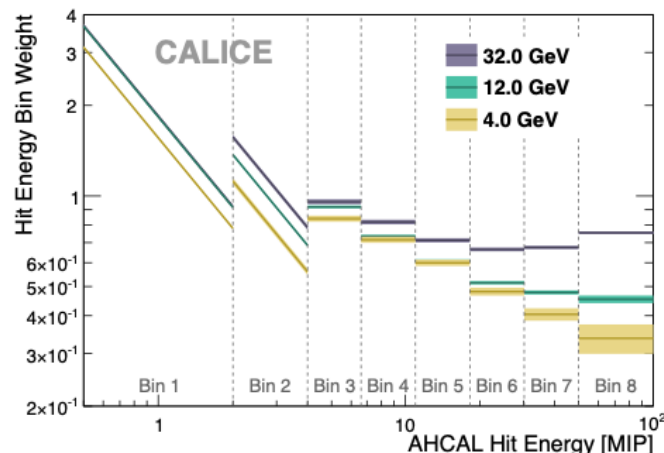
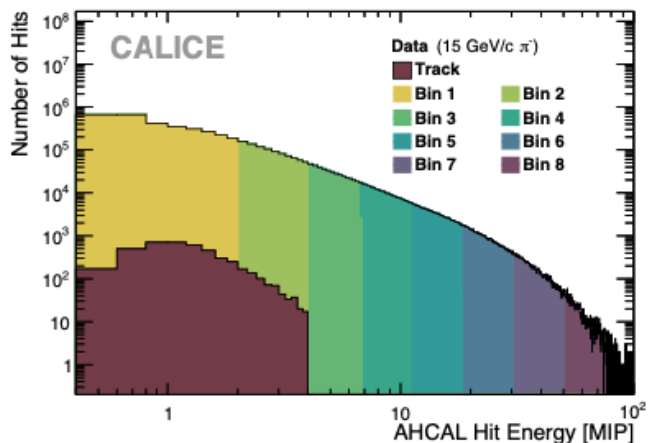
## Analog readout

### Software compensation method

- h/e response compensation by assigning energy-dependent weights to hit energies ( $\Rightarrow$  local energy density)
    - Higher weights for **low energy hits** - dominated by **HAD** component
    - Lower weights for **high energy hits** - dominated by **EM** component
- $\Rightarrow$  Significant energy resolution improvement 10-20%
- $\Rightarrow$  System performance ScECAL+AHCAL+TCMT is similar to AHCAL alone



JINST 13 P12022 (2018)



# Energy reconstruction

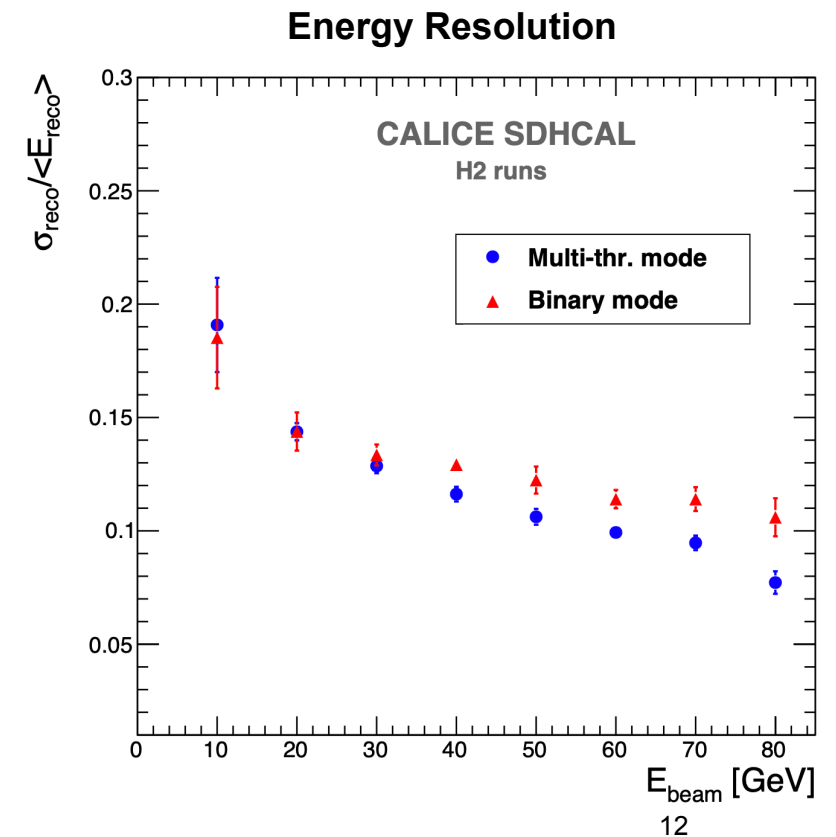
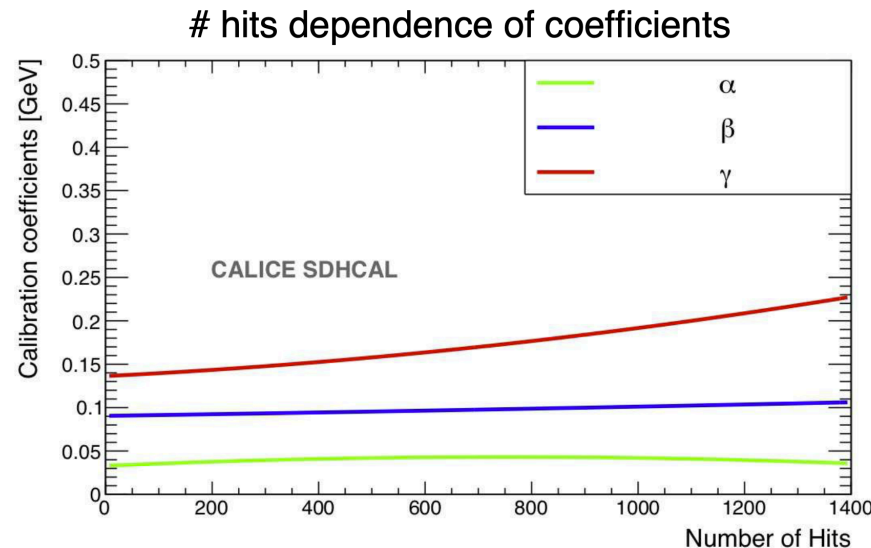
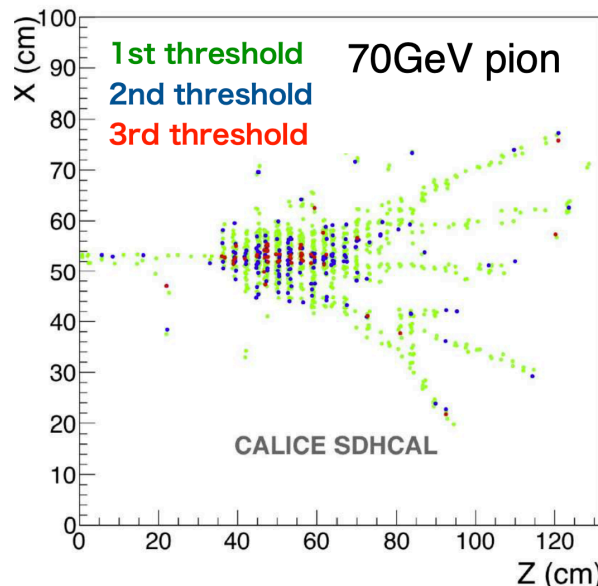
## Semi-digital readout

JINST 11 P04001 (2016)

### Multi-threshold reconstruction method:

- $N_1, N_2, N_3$ : Exclusive number of hits corresponding to 1st, 2nd and 3rd charge thresholds
  - $\alpha, \beta, \gamma$ : weights, quadratically dependent on total number of hits, parameters for each curve are extracted from test beam data @ SPS CERN
- ➔ Saturation effect at high energy region is mitigated

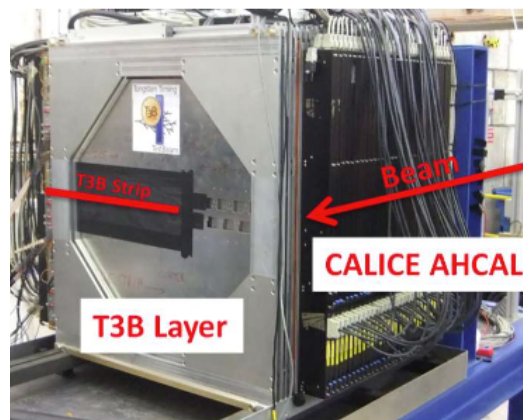
$$E_{\text{reco}} = \alpha N_1 + \beta N_2 + \gamma N_3$$



# Timing

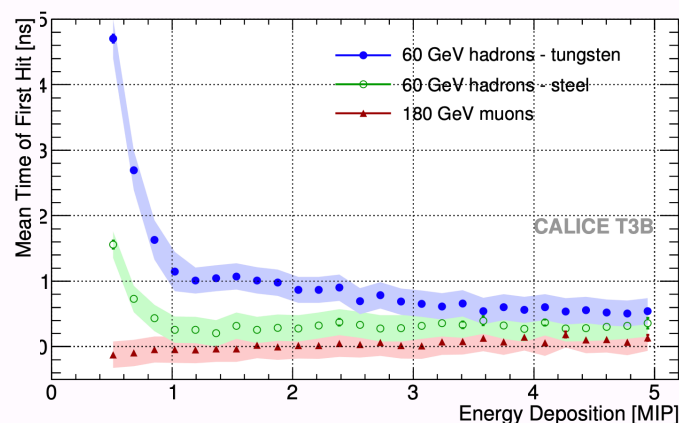
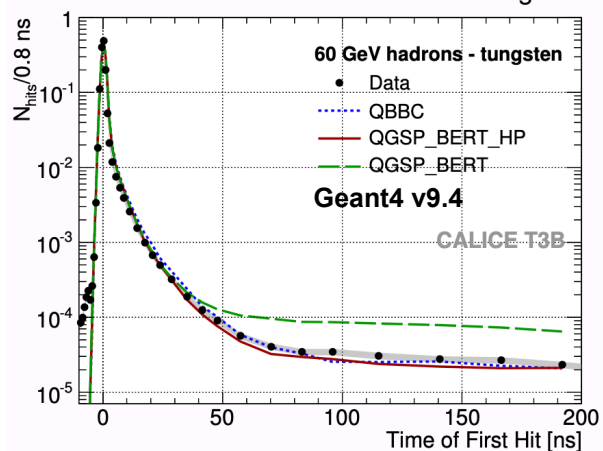
## Towards 5D calorimetry

- **CALICE T3B**: Setup of 15 scintillator-SiPM channels with **high time resolution** placed behind W-AHCAL/Fe-SDHCAL
- ➔ good agreement with GEANT4 v9.4 with emphasis on HP package for tungsten
- ➔ higher fraction of late component with tungsten specifically for low hit energies (late neutrons)
- ➔ relevant time scale  $\sim 1\text{ns}$



JINST 9 P07022 (2014)

Timing of hadronic showers

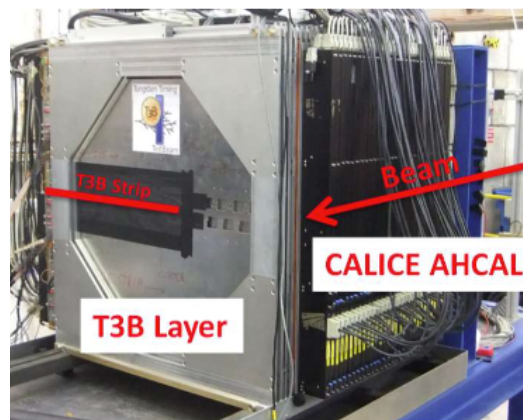




# Timing

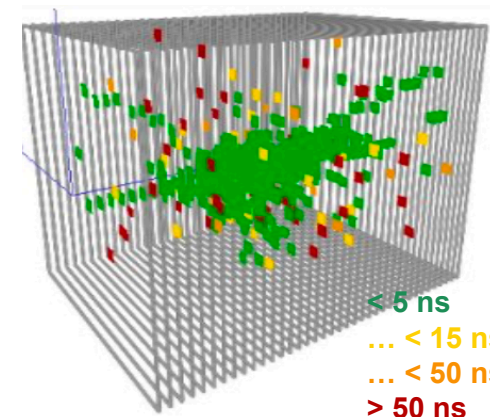
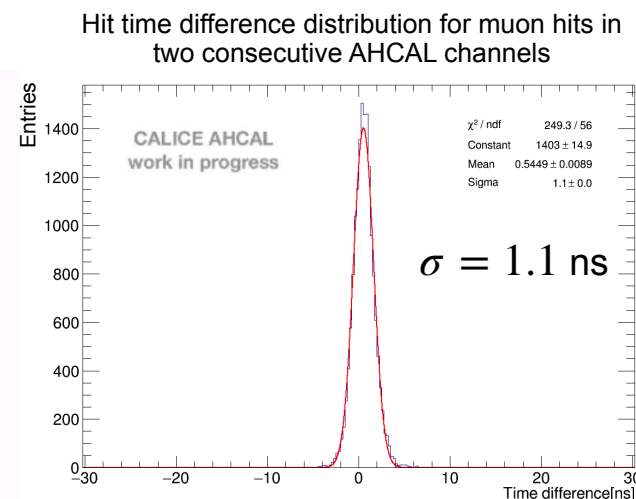
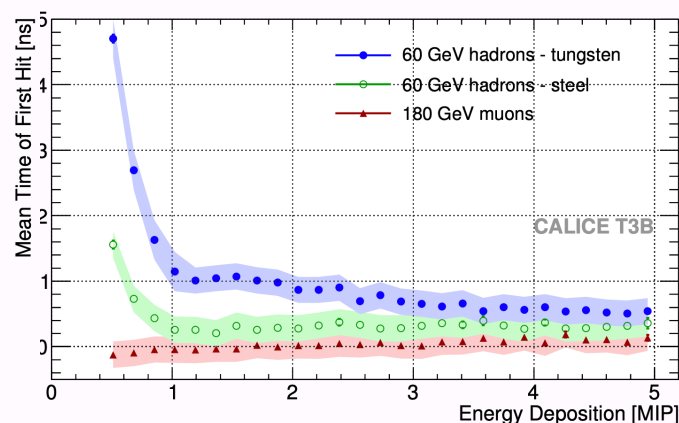
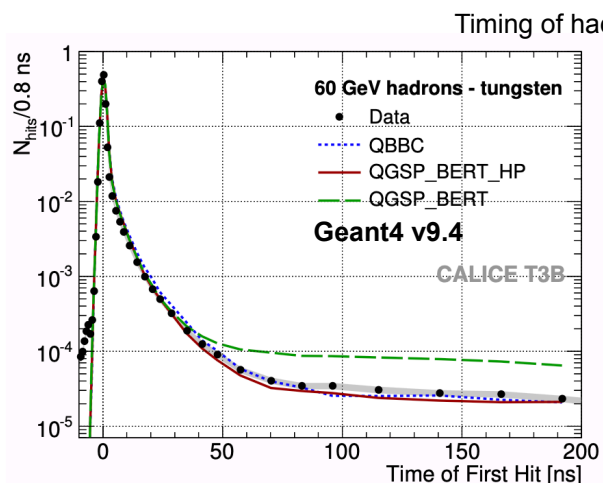
## Towards 5D calorimetry

- **CALICE T3B**: Setup of 15 scintillator-SiPM channels with **high time resolution** placed behind W-AHCAL/Fe-SDHCAL
  - ➔ good agreement with GEANT4 v9.4 with emphasis on HP package for tungsten
  - ➔ higher fraction of late component with tungsten specifically for low hit energies (late neutrons)
  - ➔ relevant time scale  $\sim 1$  ns



JINST 9 P07022 (2014)

- **AHCAL**: Hit time measurement capability with technological prototype
  - ➔ Intrinsic single channel hit time resolution of  $\sim 1$  ns for muons
  - ➔ Further optimisation and analysis on hadrons in progress
  - ➔ Envisage study of dynamical developments of showers



# Summary & Outlook

- High granularity of calorimeters is one of the key components to reach the unprecedented jet energy resolution at future lepton colliders
- Imaging capabilities of CALICE highly granular calorimeter prototypes provide excellent opportunity to study hadronic showers at beam tests
  - Detailed hadronic shower structure analysis
  - Validation of Geant4 modelling and feedback to developers
  - Calorimeter-based particle identification
  - PFA performance tests on test beam data and feedback to developers
  - Improving hadronic energy resolution using software compensation and multi-threshold reconstruction
- Timing measurements show promising results  $\Rightarrow$  next step towards 5D calorimetry
- Analyses with the CALICE technological prototypes are ongoing - stay tuned

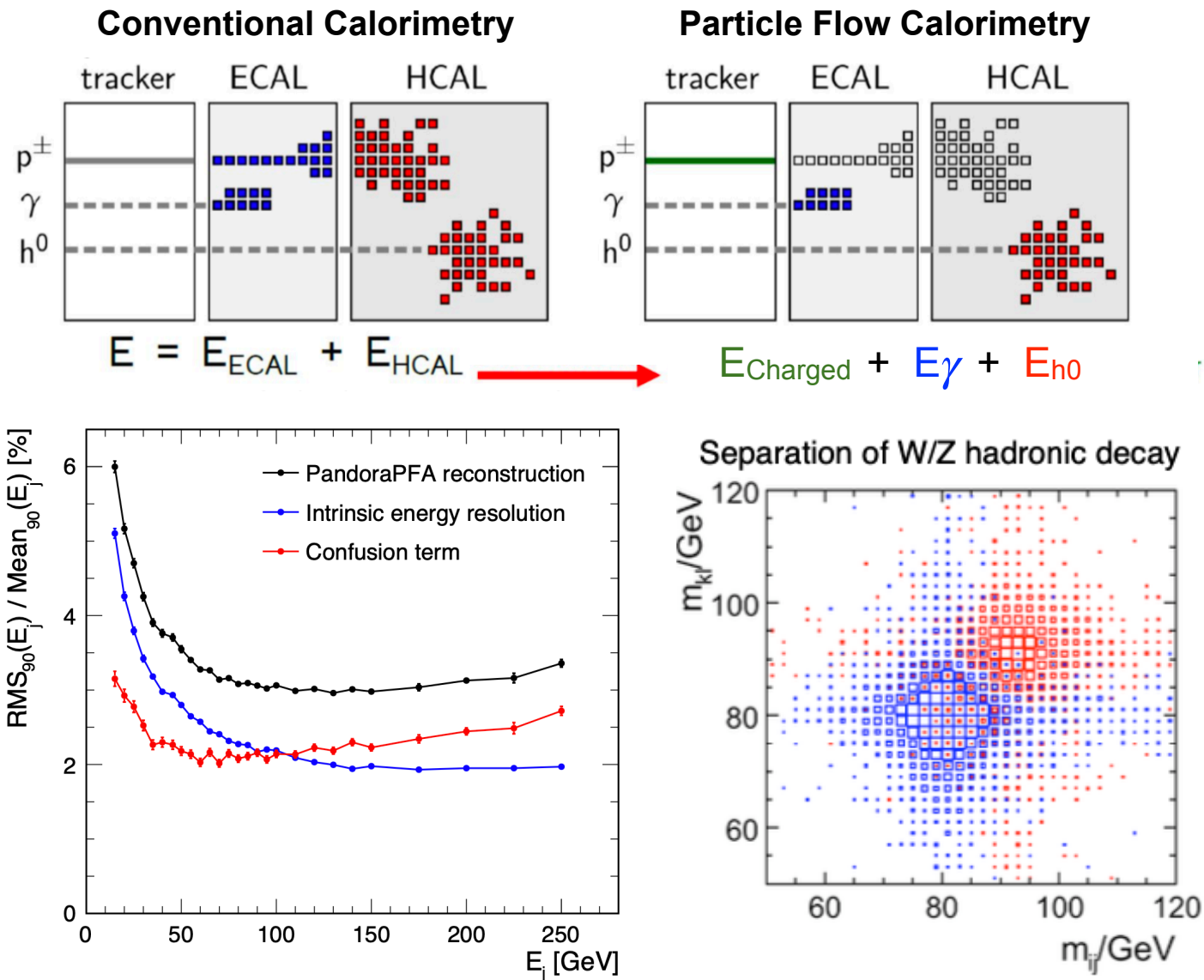
# Backup



# Particle Flow Calorimetry

## Reaching the Highest Precision

- At future  $e^+e^-$  collider experiments:  
Unprecedented jet energy resolutions for precise physics with jets required
- ➔ Use Particle Flow Algorithms (PFA)
  - Measurement of sub-detector providing the best resolution on particle-by-particle basis
    - ➔ Charged particles: Tracker
    - ➔ Photons: ECAL
    - ➔ Neutral hadrons: ECAL+HCAL
  - Requirements for PFA :
    - ➔ High precision tracker
    - ➔ **High granularity calorimeters**



**Goal: 3-4% jet energy resolutions!**

# Single Particle Energy Resolution

## Performance of CALICE Calorimeter Prototypes - Examples

- Achieved single particle (intrinsic) energy resolution of CALICE calorimeter prototypes remarkable - even if they are not explicitly optimised on this quantity alone

➔ SiW ECAL physics prototype (EM):

$$\sim 16.6\% / \sqrt{E(\text{GeV})} \oplus \sim 1.05\%$$

➔ ScECAL physics prototype (EM):

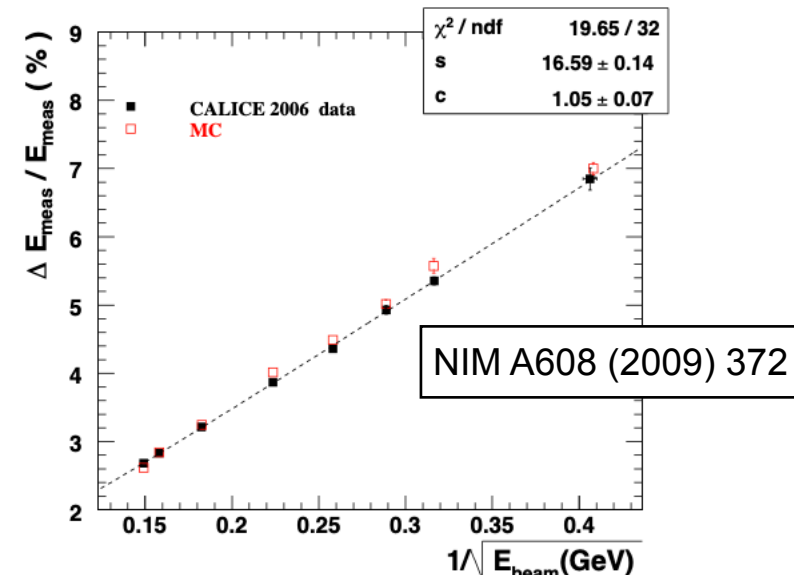
$$\sim 12.5\% / \sqrt{E(\text{GeV})} \oplus \sim 1.2\%$$

➔ AHCAL physics prototype (HAD):

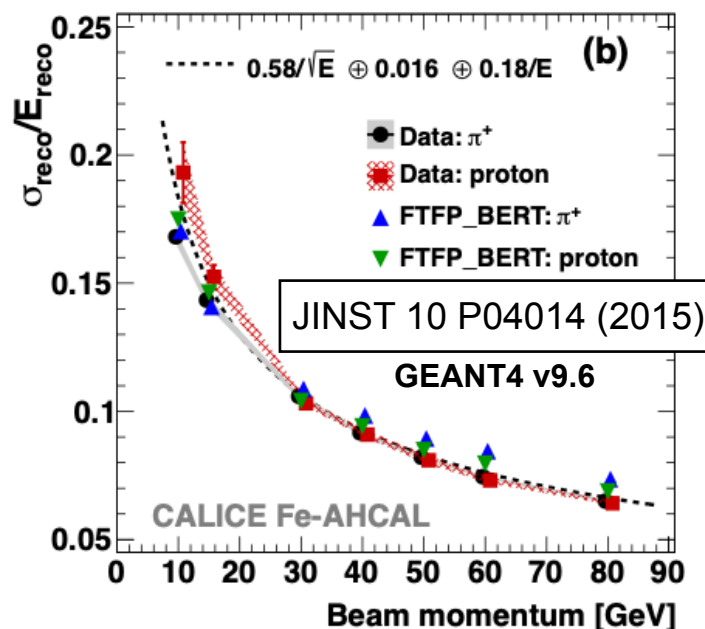
$$\sim 58\% / \sqrt{E(\text{GeV})} \oplus \sim 1.6\%$$

(before weighting)

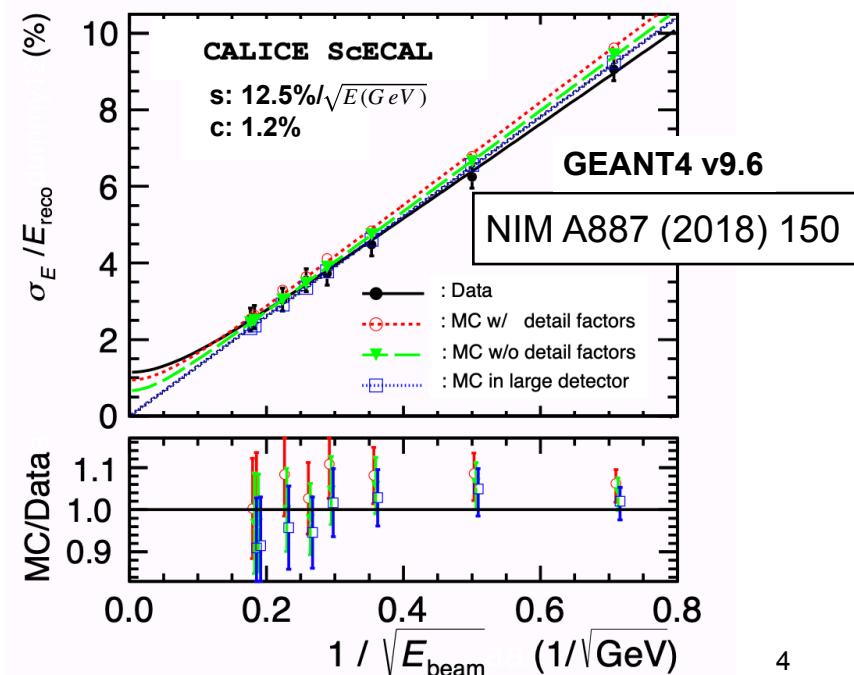
Energy Resolution SiW ECAL (e<sup>-</sup>)



Energy Resolution AHCAL (pi<sup>+</sup>/protons)

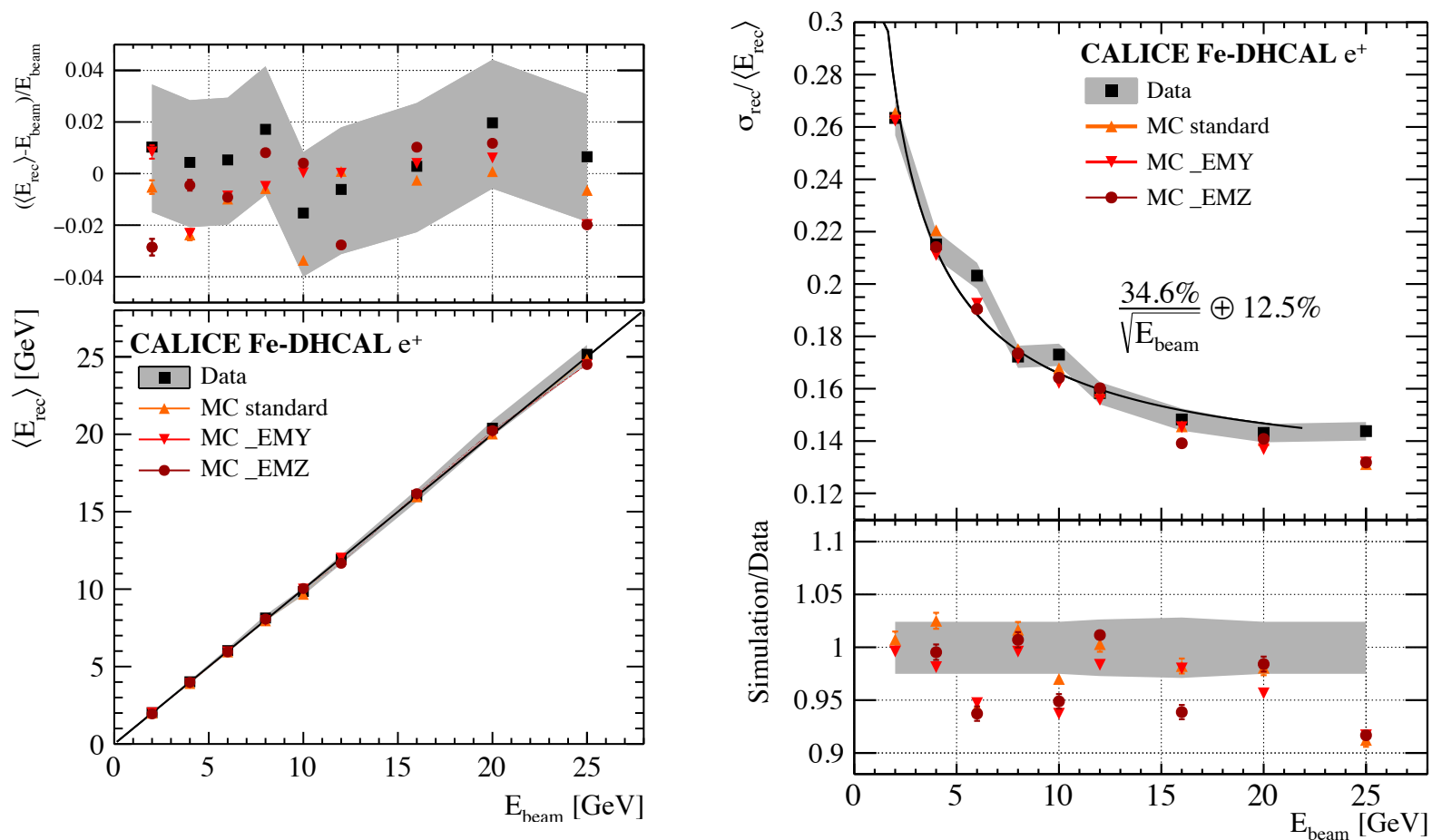


Energy Resolution ScECAL (e<sup>-</sup>)



# Digital hadronic calorimeter (DHCAL)

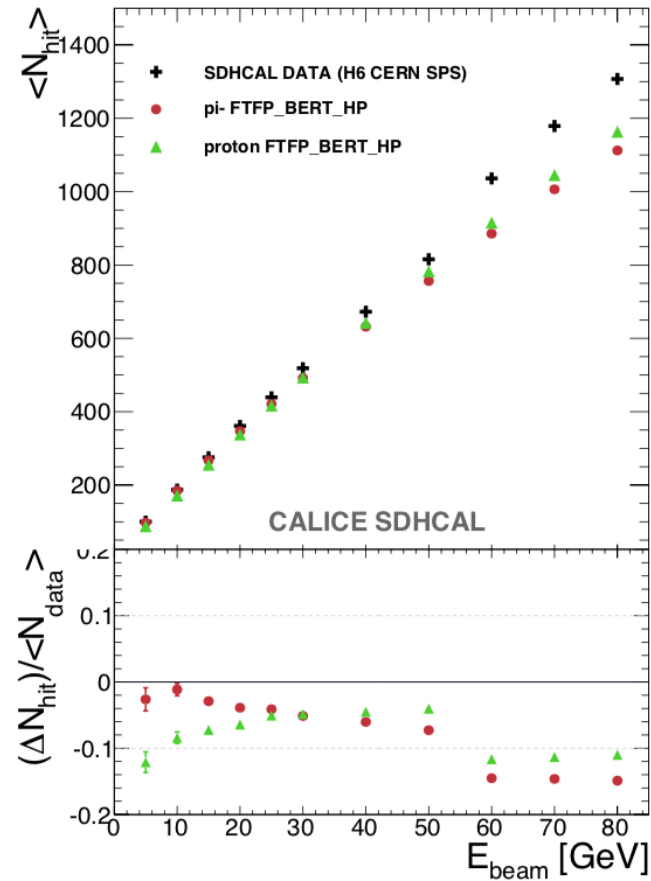
## Linearity and resolution



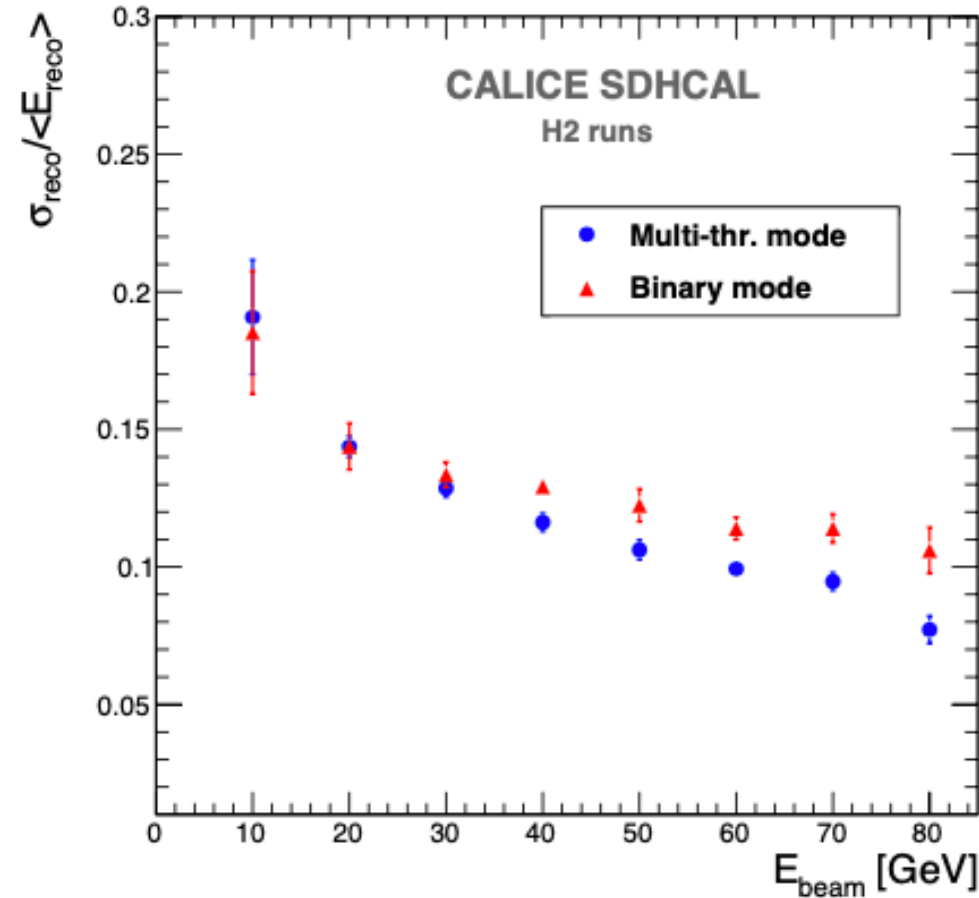
NIM A939 (2019) 89-105

# Semi-Digital Hadronic Calorimeter (SDHCAL)

## Linearity and resolution

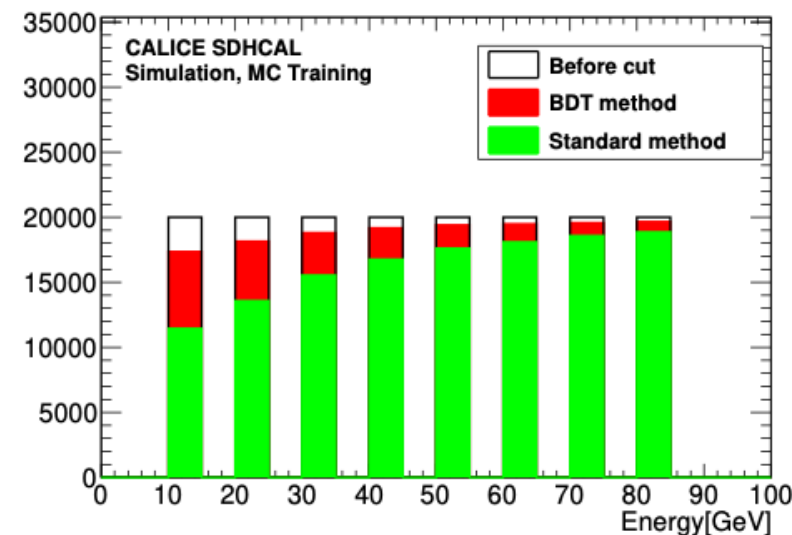
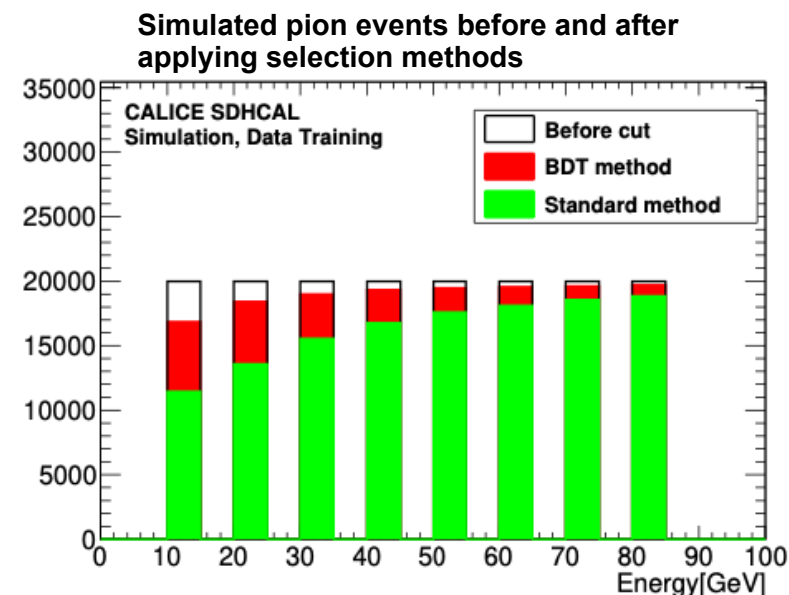


## Energy resolution

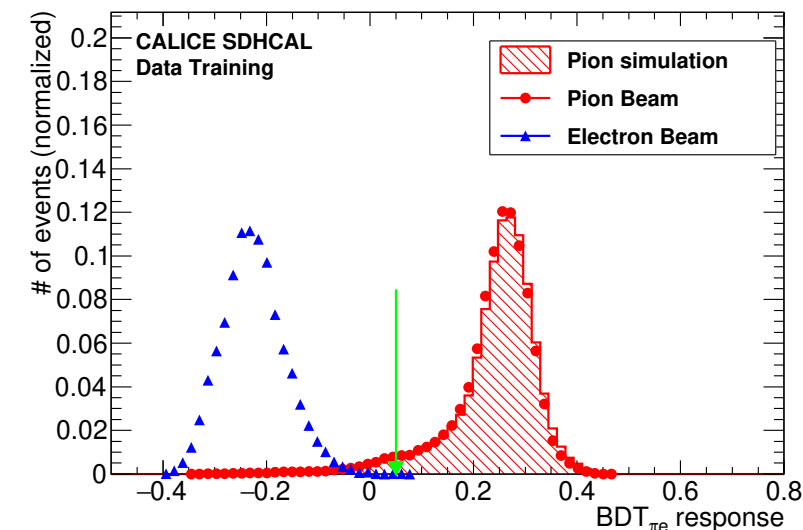
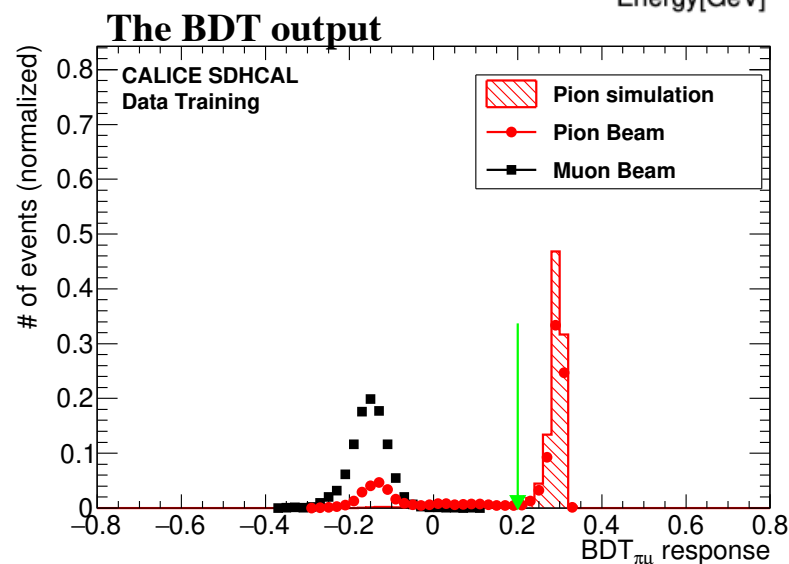


JINST 11 (2016) P06014

# BDT classification SDHCAL



JINST 15 (2020) 10,  
P10009





# BDT classification AHCAL

## Model and input.

### Software and model:

- **LightGBM** package
- Multi-class **Gradient Boosted Decision Tree**
- **Multi-log/BCE** loss function
- Output: **3 probabilistic classifiers** (electron, hadron, muon-like)

### Training and test set:

- **MC particles 10-200GeV** simulated using *Geant4 (v10.03.p02)* QGSP\_BERT\_HP physics list:
  - **pions ( $st \leq 40$ )**
  - **electrons**
  - **muons**
- Simulated data is split **50/50 - test/train**
- Simultaneous training on whole energy range

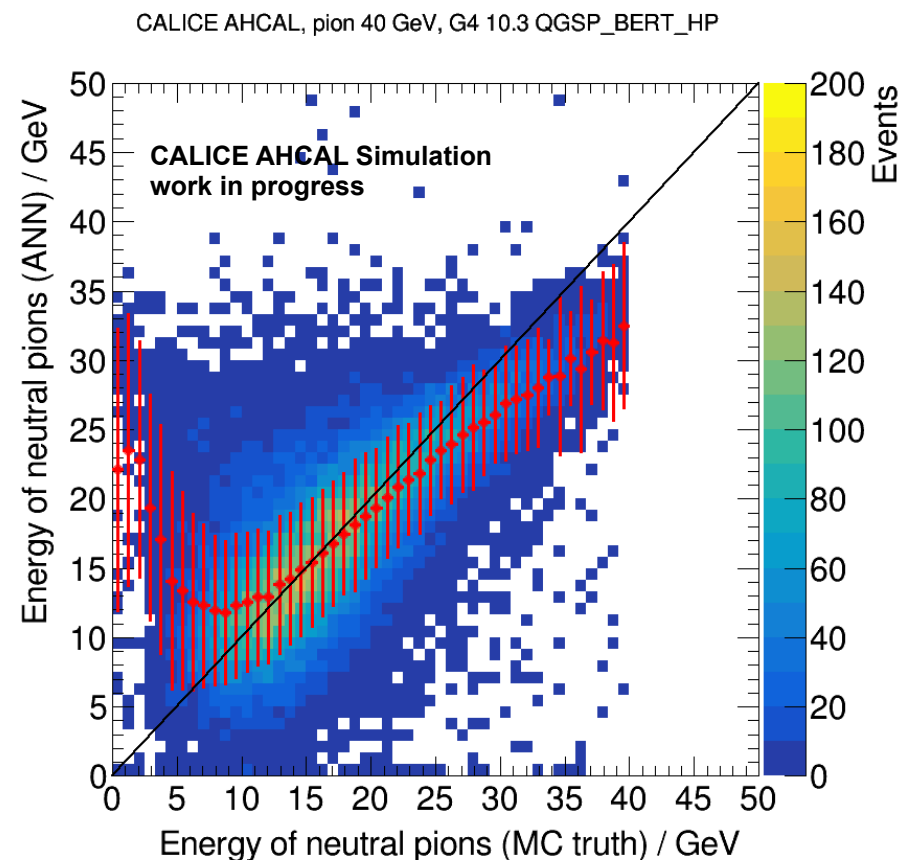
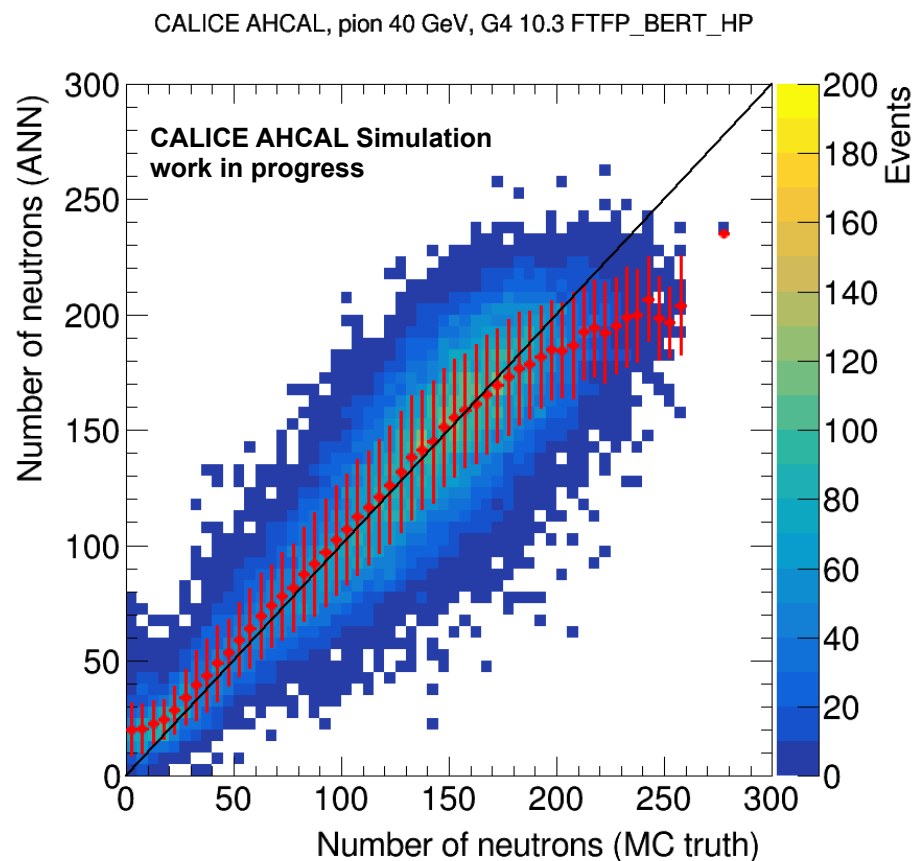
### Observables (sorted by importance):

- Event radius
- Shower start layer number
- Energy fraction in shower core
- Energy fraction in shower central region (in XY plane)
- Mean hit energy after shower start
- Energy fraction in first 22 layers
- Number of hits
- Center of gravity in z
- Number of track hits
- Number of layers with hits from last 5
- Number of hits after shower start

# Ongoing MVA examples with AHCAL

## DNN based prediction of hadronic shower properties using global observables

- Prediction vs MC truth for number of neutrons
- Prediction vs MC truth for energy of neutral pions



More details can be found in Marina's ILCX 2021 presentation

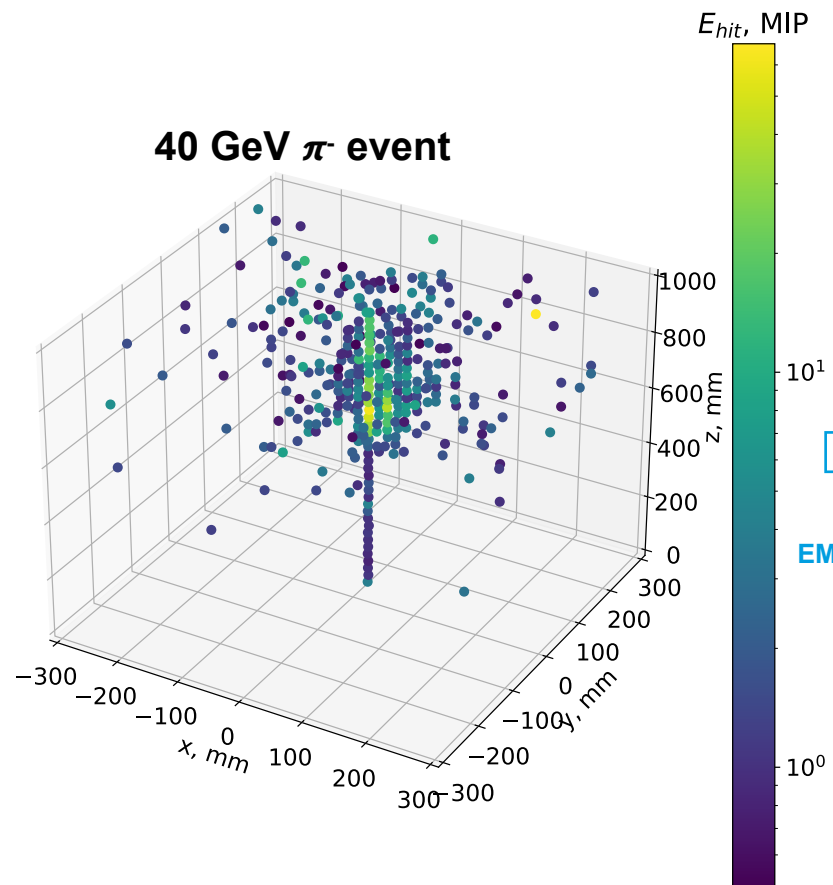
# Ongoing MVA examples with AHCAL

## GNN based reconstruction of hadronic shower components

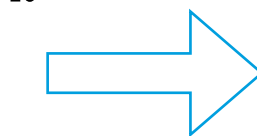
### Graph representation of calorimeter event:

- Nodes - hits
- Node features - position, energy, (time)
  - Edges - neighbours ( $R < R_{\max}$ )
  - Edge weights - 1 if pair of nodes belong to same **fundamental object** (e/m sub-shower, track), otherwise 0

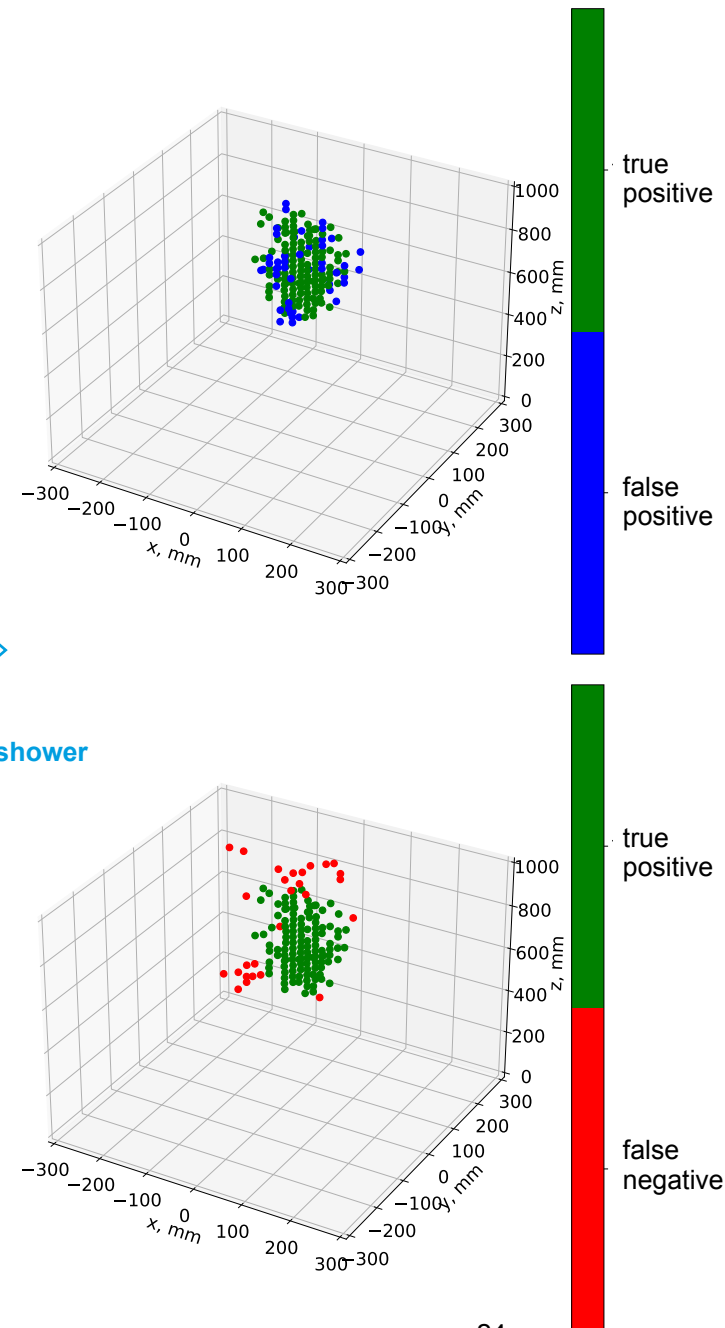
**Graph neural network** is trained to predict edge weights



**CALICE AHCAL Simulation work in progress**



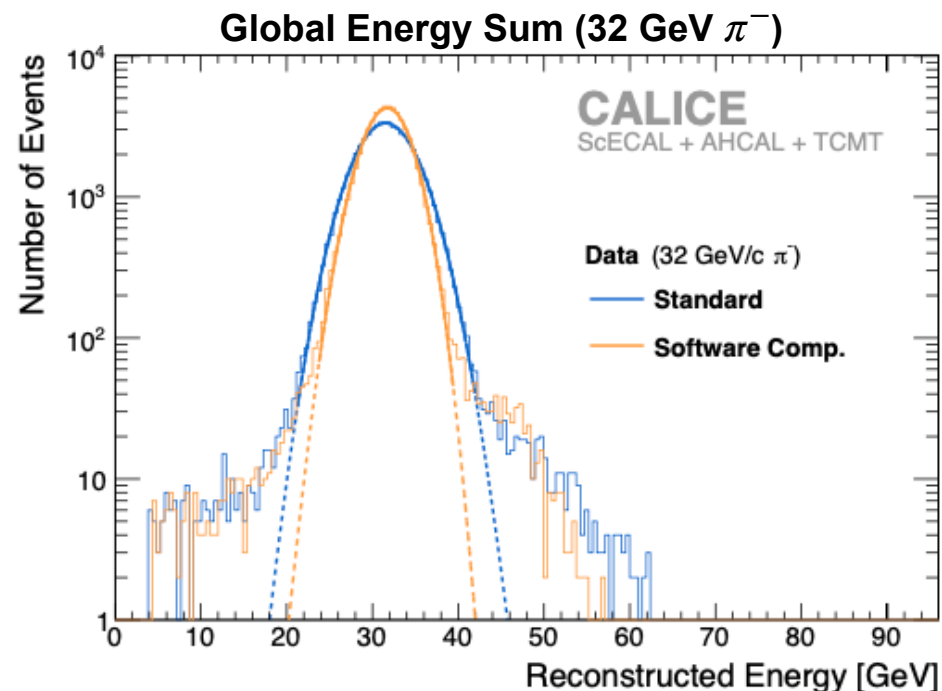
EM component of shower



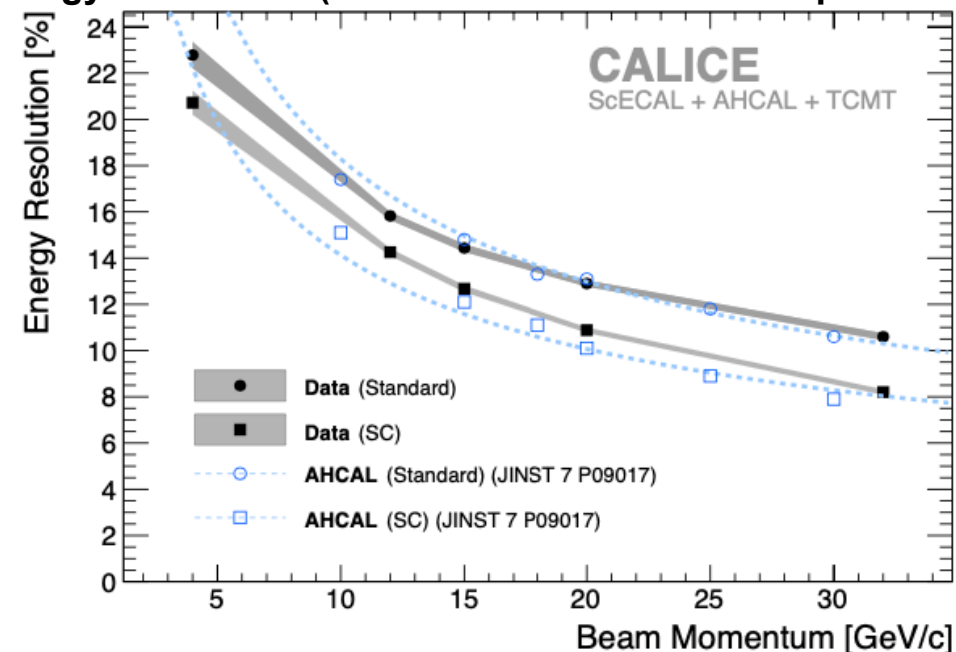
# Software Compensation - Analogue Calorimeters

## Energy Reconstruction Performance

JINST 13 P12022 (2018)  
JINST 7 P09017 (2012)



## Energy Resolution (Standard vs. Software Compensation)



- Within CALICE collaboration software compensation is studied for a variety of detector prototypes
- Here: Combined test beam of ScECAL + AHCAL + TCMT (4-32 GeV  $\pi^-$  @ FNAL)
  - ➡ Energy resolution significantly improved by 10-20% compared to standard reconstruction
  - ➡ With software compensation:  $\sim 44.3\% / \sqrt{E(\text{GeV})} \oplus \sim 1.8\%$