

# *r*-process nucleosynthesis



Fission In R-process  
Elements

**Nicole Vassh**  
**TRIUMF Theory Group**

NIC School Lecture,  
Live from home wishing I could see pandas :/  
September 13, 2021

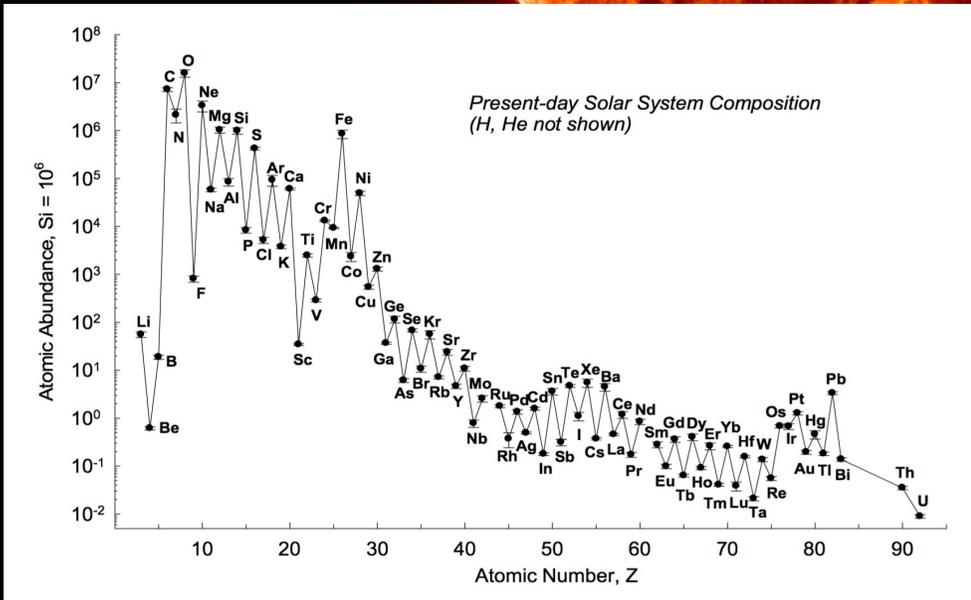
# Outline

- Observational evidence that the  $r$  process occurs [4-9]
- Discussion of astrophysical sites (history (CCSNe), candidate sites, MHD SNe, NSNS/NSBH) [11-21]
- Spotlight on GW170817 and AT2017gfo: the first multi-messenger NSNS event [23-33]
- $r$ -process calculations (intro to reaction rates and equilibrium, history (classical  $r$  process), intro to using networks and trajectories,  $r$ -process dynamics) [35-52]
- The fundamental role of nuclear physics [54-82]

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The solar composition can be decomposed into many processes  
 → multiple nucleosynthesis sites enriched the solar system



Lodders 10

### The Origin of the Solar System Elements

1 H	big bang fusion										cosmic ray fission						2 He		
3 Li	4 Be	<b>r-process</b>										5 B	6 C	7 N	8 O	9 F	10 Ne		
11 Na	12 Mg	dying low mass stars						exploding white dwarfs						13 Al	14 Si	15 P	16 S	17 Cl	18 Ar
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr		
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe		
55 Cs	56 Ba	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn			
87 Fr	88 Ra																		
57 La	58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu					
89 Ac	90 Th	91 Pa	92 U	93 Np	94 Pu	Very radioactive isotopes; nothing left from stars													

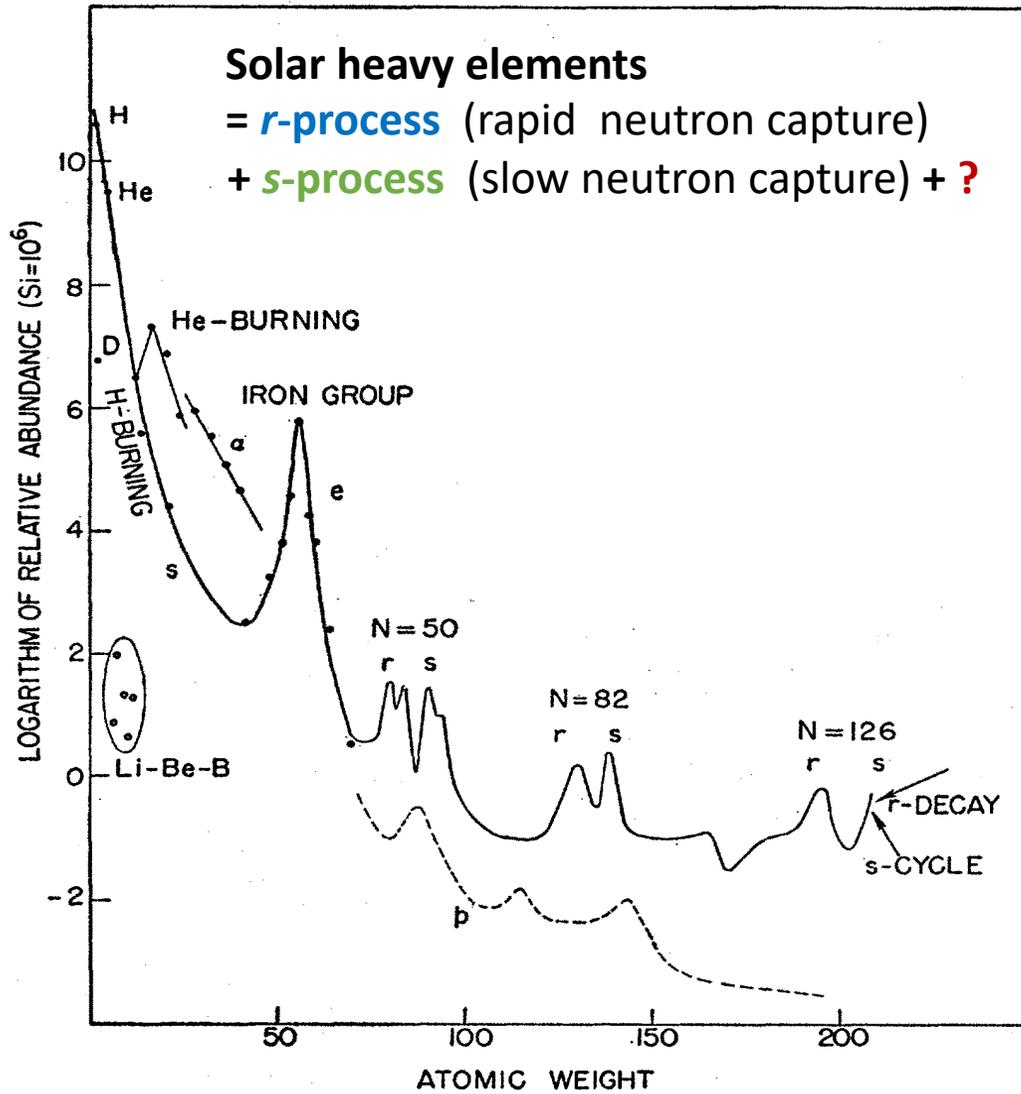
Graphic created by Jennifer Johnson  
<http://www.astronomy.ohio-state.edu/~jaj/nucleo/>

Lanthanides

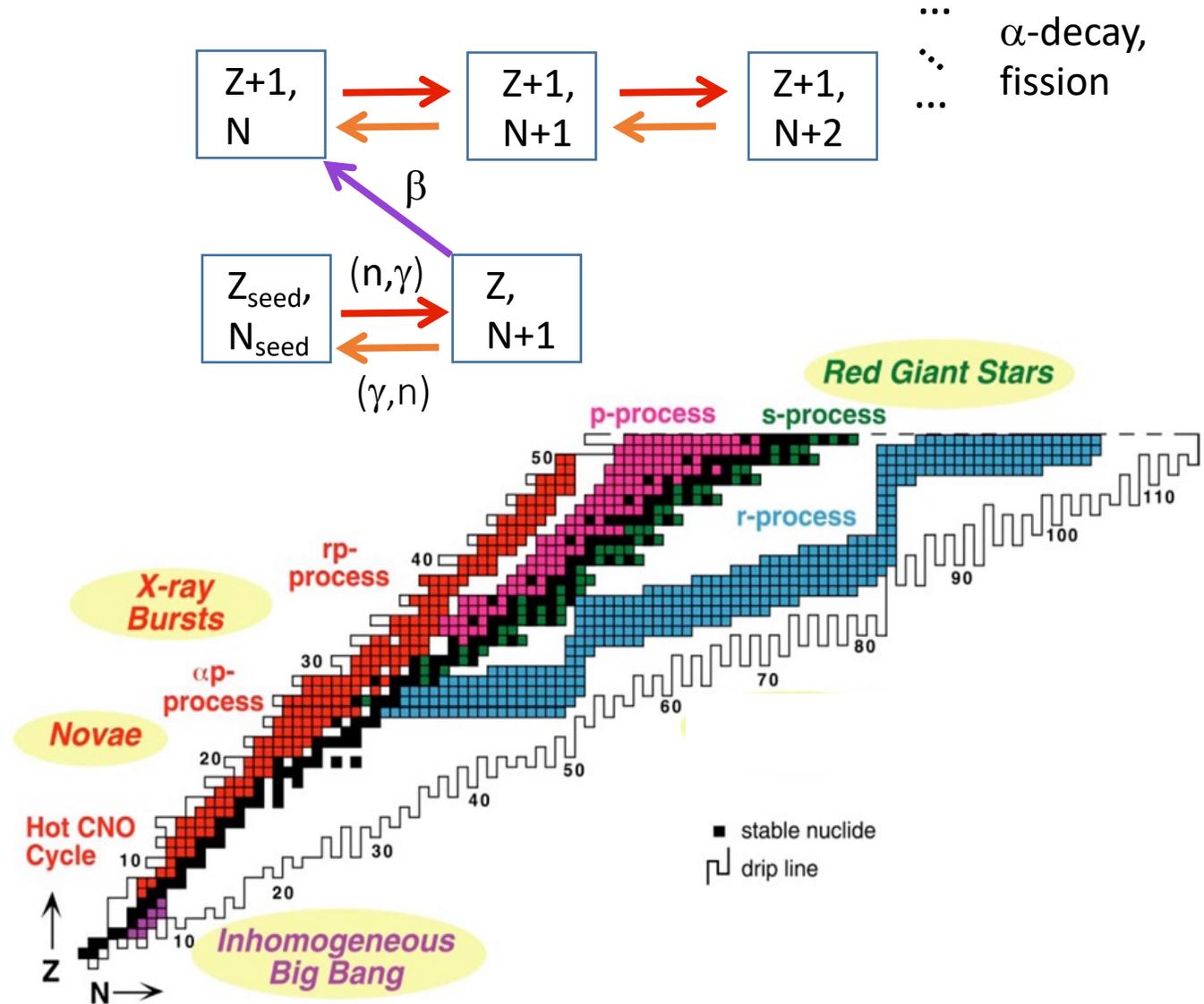
Actinides

Astronomical Image Credits:  
 ESA/NASA/AASNova

# How do we know there is an *r*-process? Solar abundance peaks

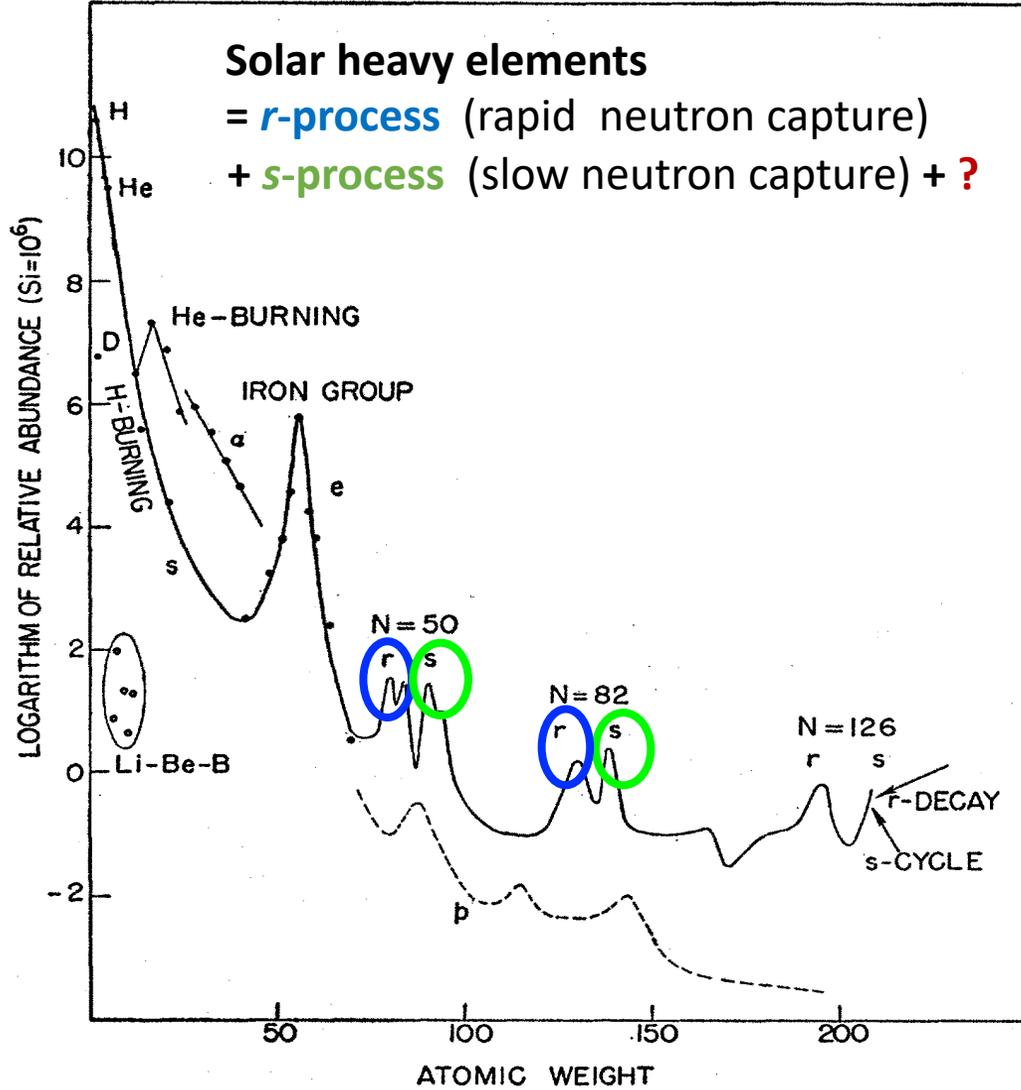


Burbidge, Burbidge, Fowler, and Hoyle (B<sup>2</sup>FH) (1957)

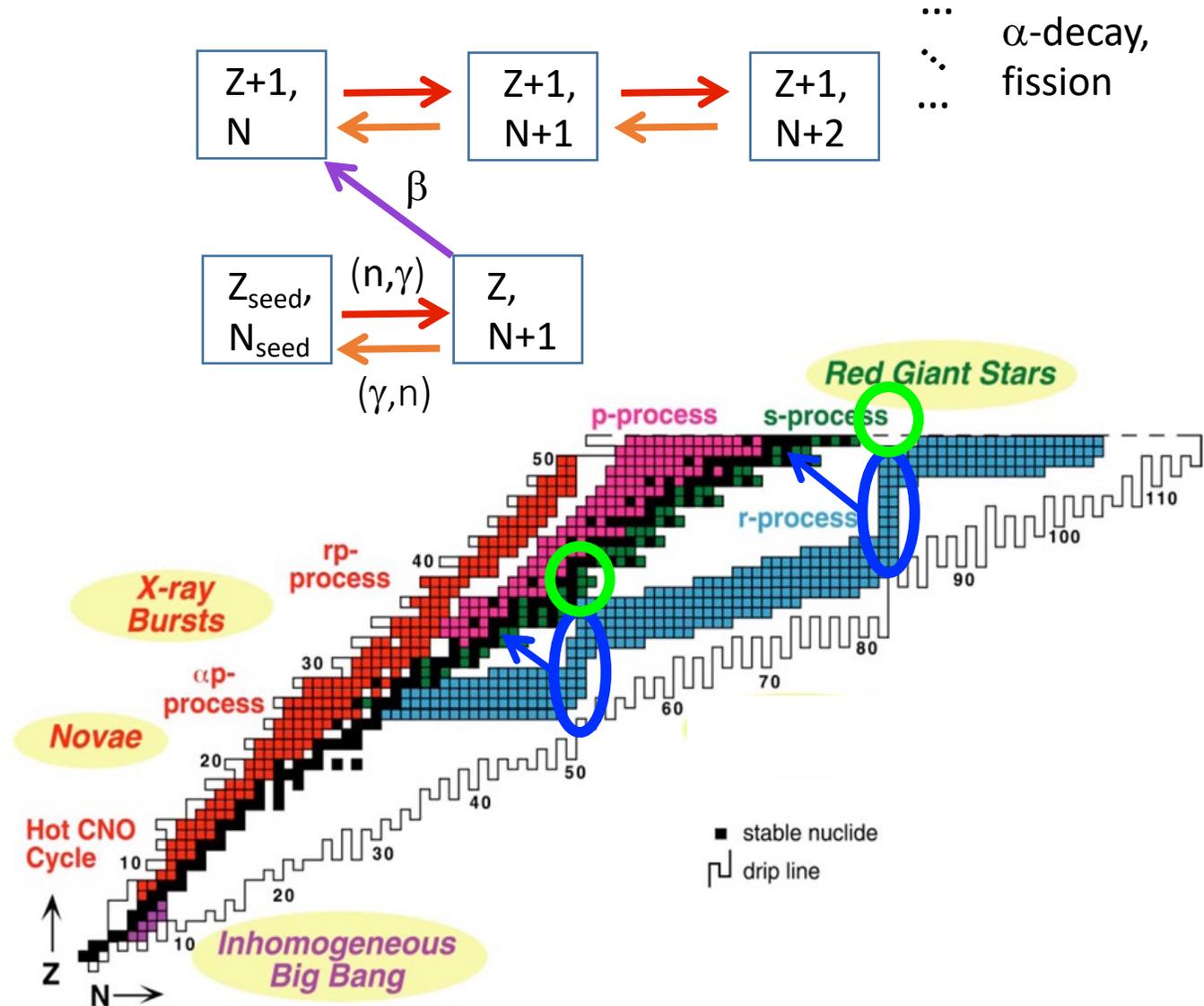


Smith&Rehm 01

# How do we know there is an *r*-process? Solar abundance peaks

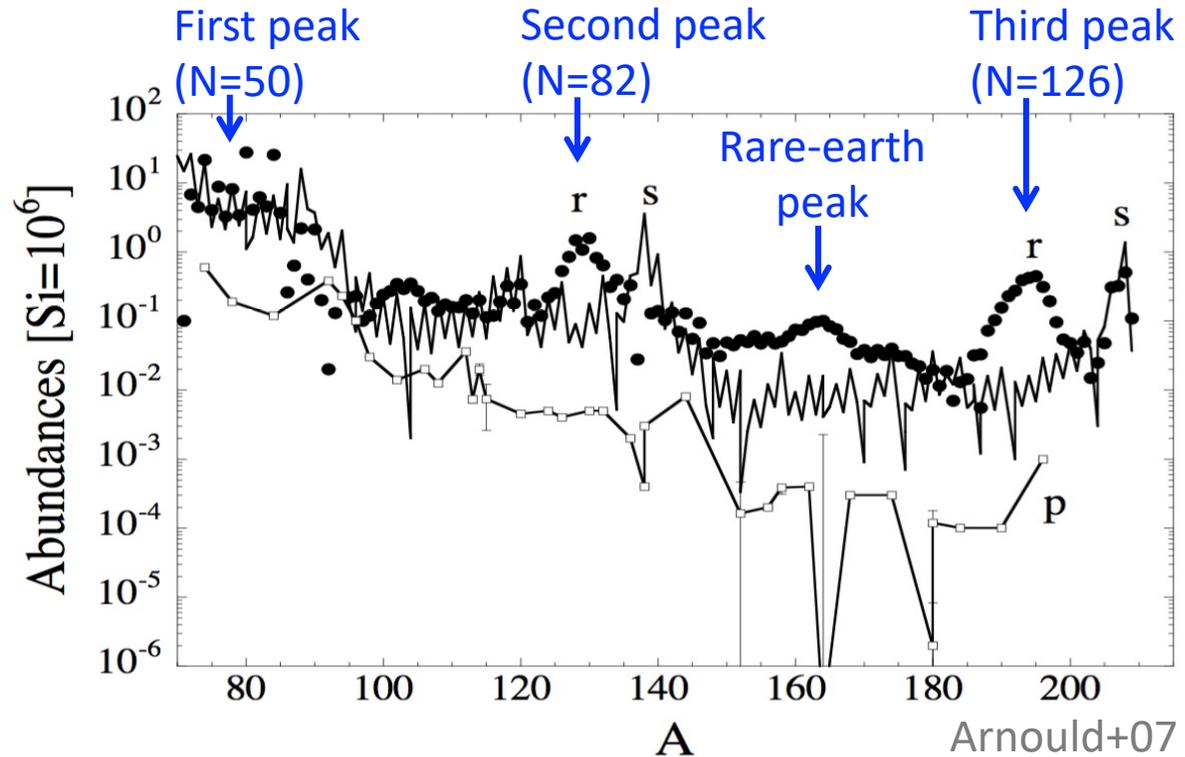
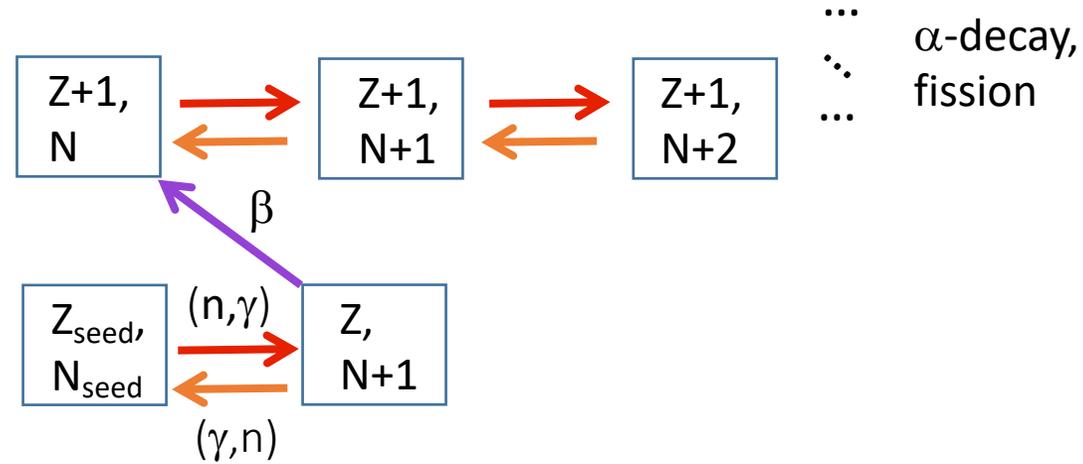
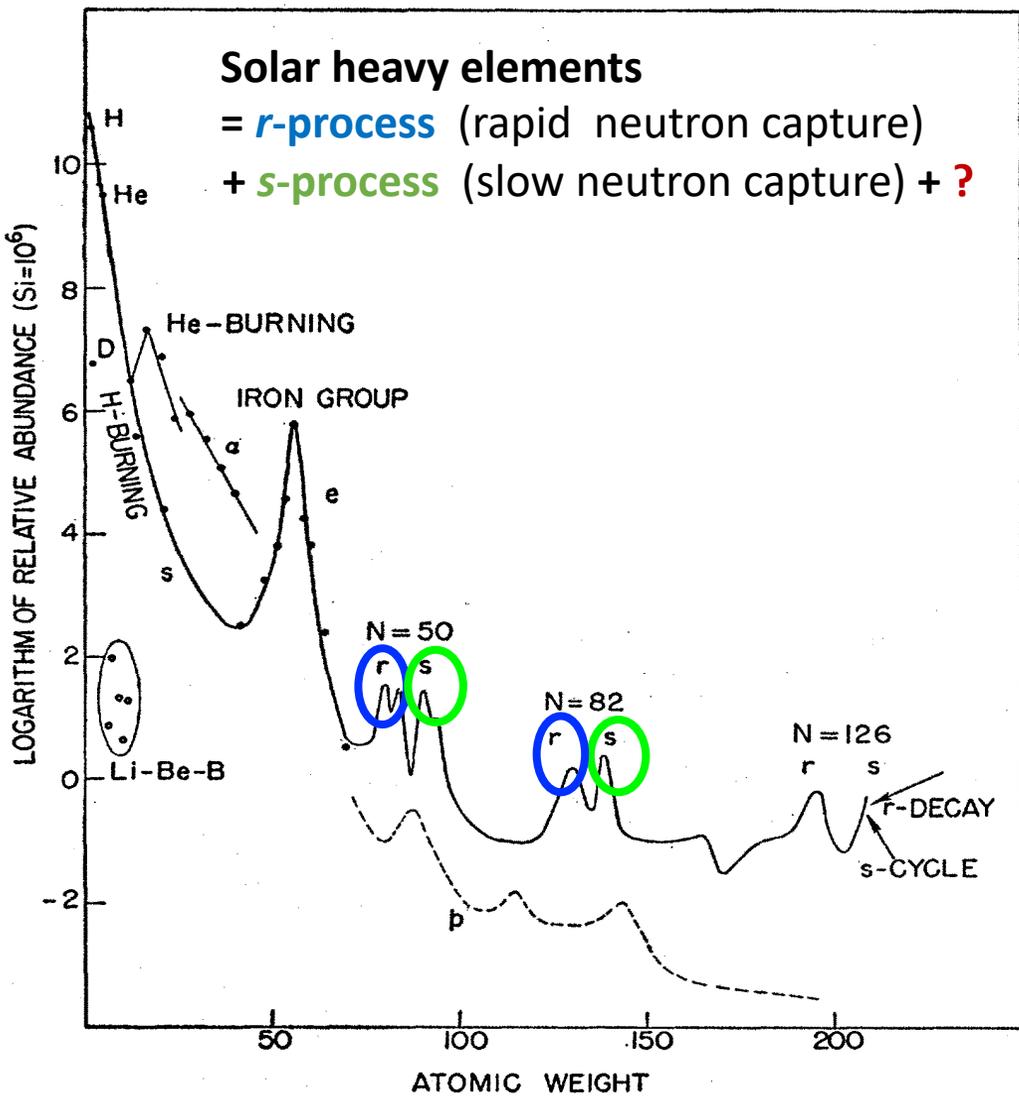


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Smith&Rehm 01

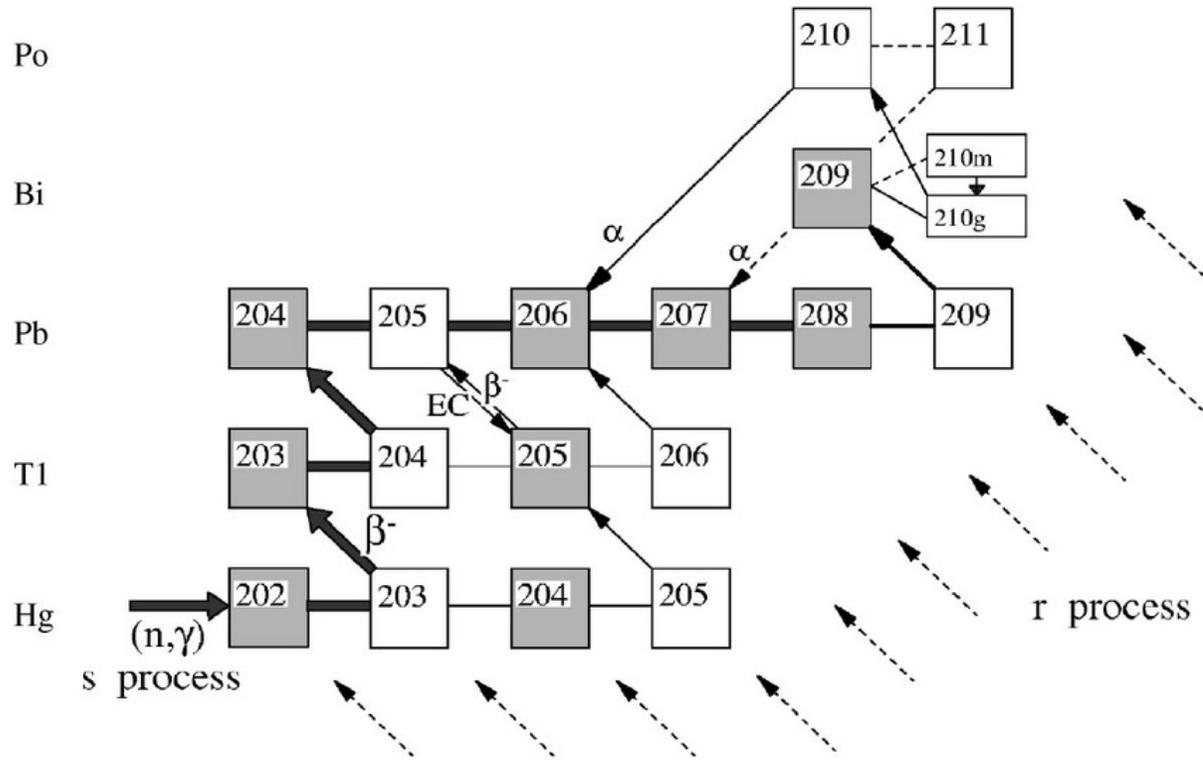
# How do we know there is an *r*-process? Solar abundance peaks



Burbidge, Burbidge, Fowler, and Hoyle (B<sup>2</sup>FH) (1957)

# How do we know there is an *r*-process? Actinides (Z=89-103)

The *s*-process terminates at Pb-208 (Z=82) but *we observe actinides* in meteorites, Earth ocean crusts, our Sun, and other stars

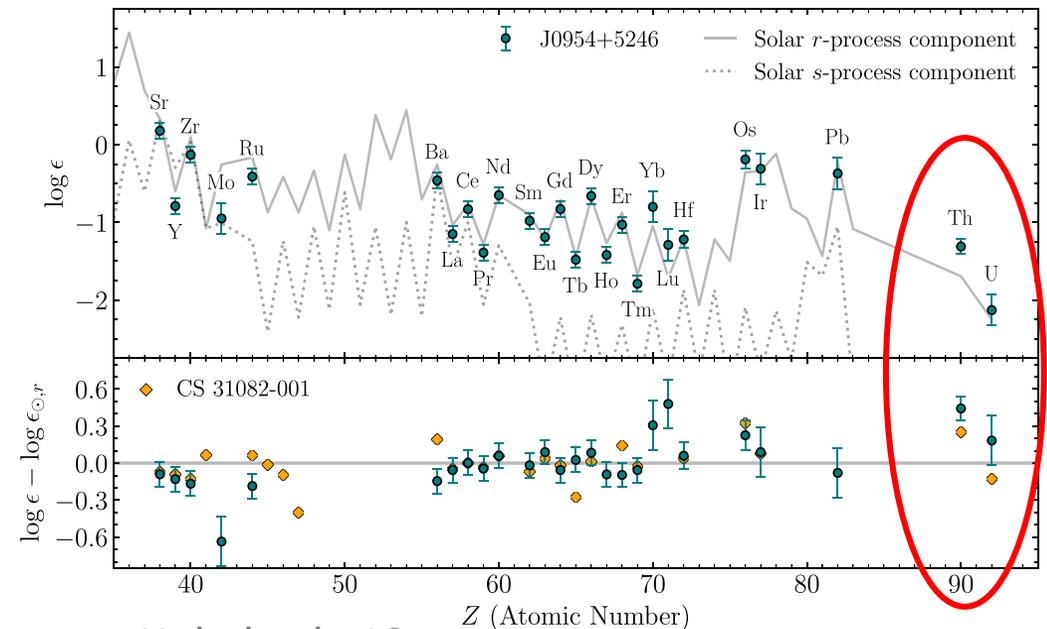


Ratzel+04

“Curious Marie” sample of Allende meteorite shows excess U-235 which is a trace of Cm-247

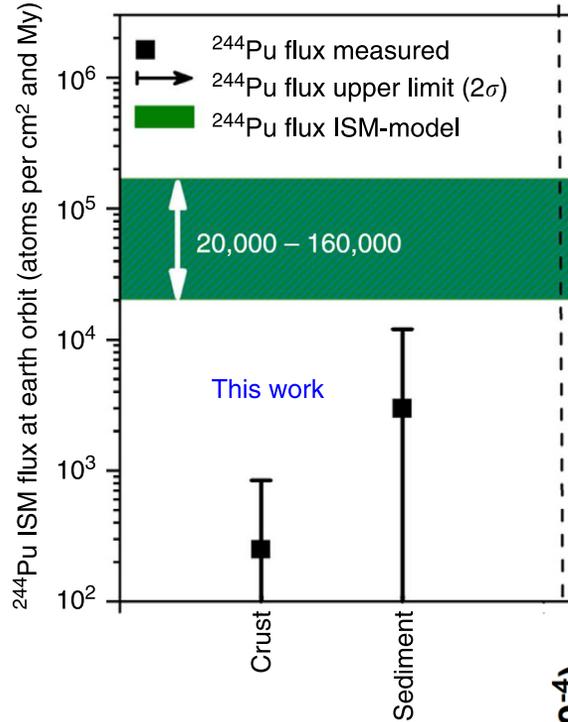


Actinide boost stars compared to solar



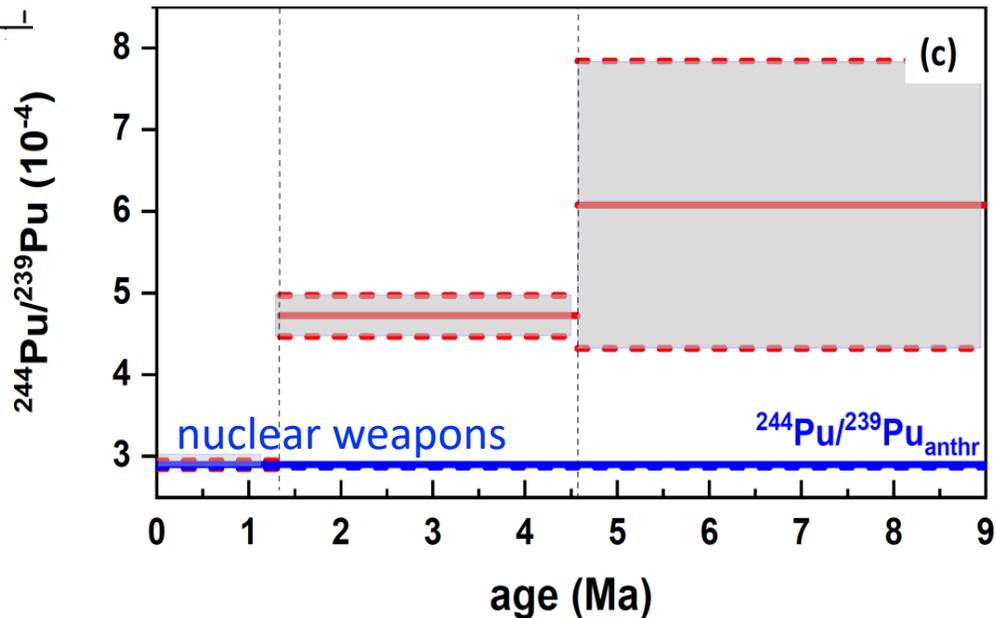
Holmbeck+18

# r-process species must be from a *rare source*



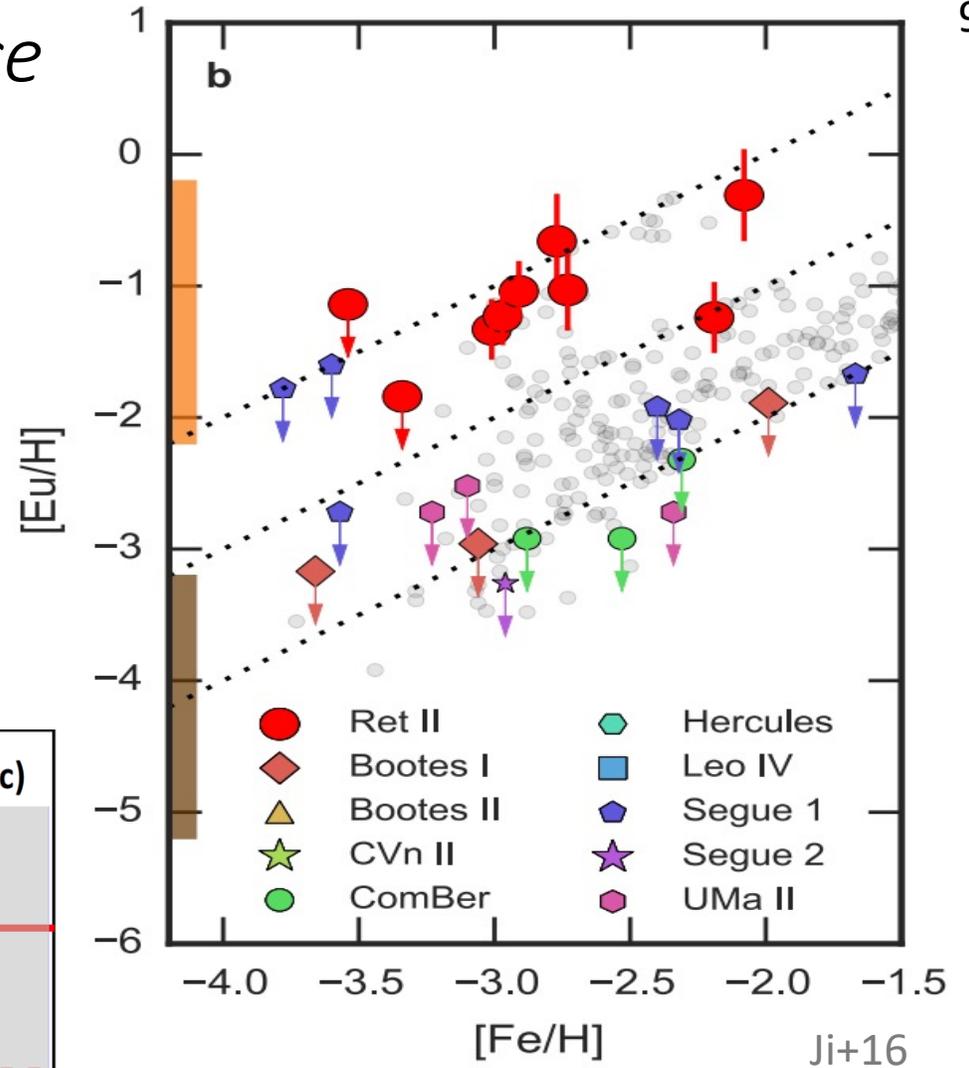
Pu-244 in deep-sea ocean crusts compared to a **model** which assumes a source as frequent as supernova

Wallner+15



Most recent measurements are still consistent with a rare extraterrestrial source for Pu-244 (long lived compared to Pu-239)

Wallner+21

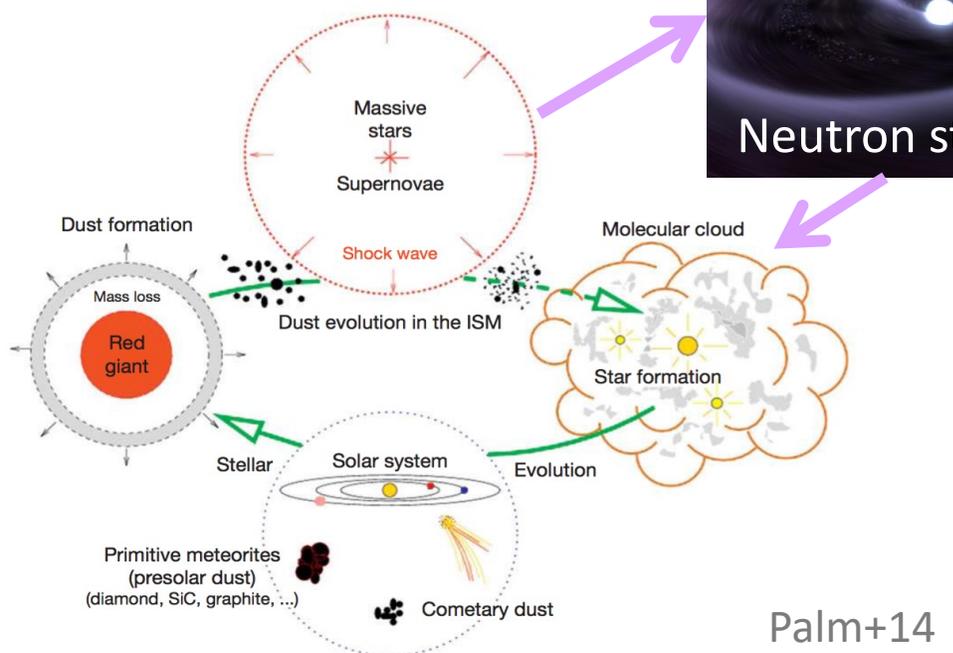


Ultra faint dwarf galaxies (formed shortly after first stars) rarely show an enhancement in *r*-process elements like in **Reticulum II** (MW in grey)

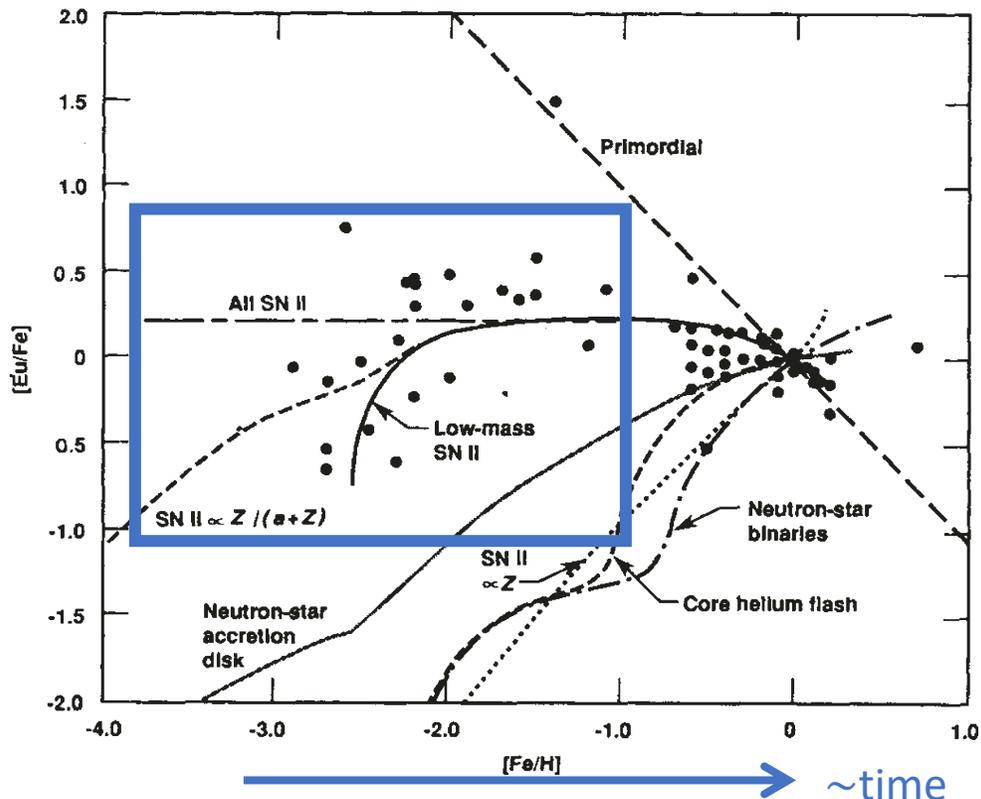
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# Which astrophysical sites enriched our solar system?



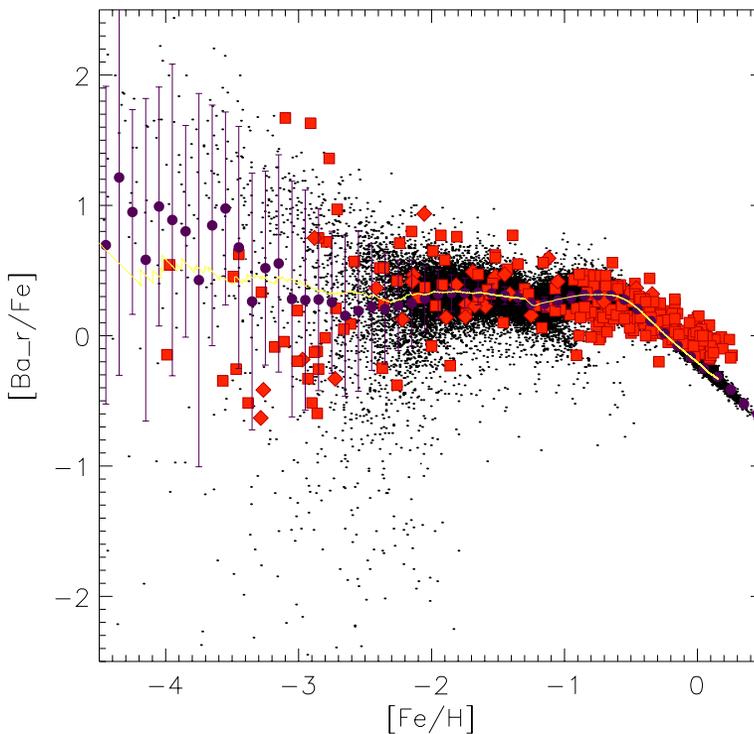
# Supernovae as the *r*-process source? Galactic chemical evolution (GCE) and low metallicity stars



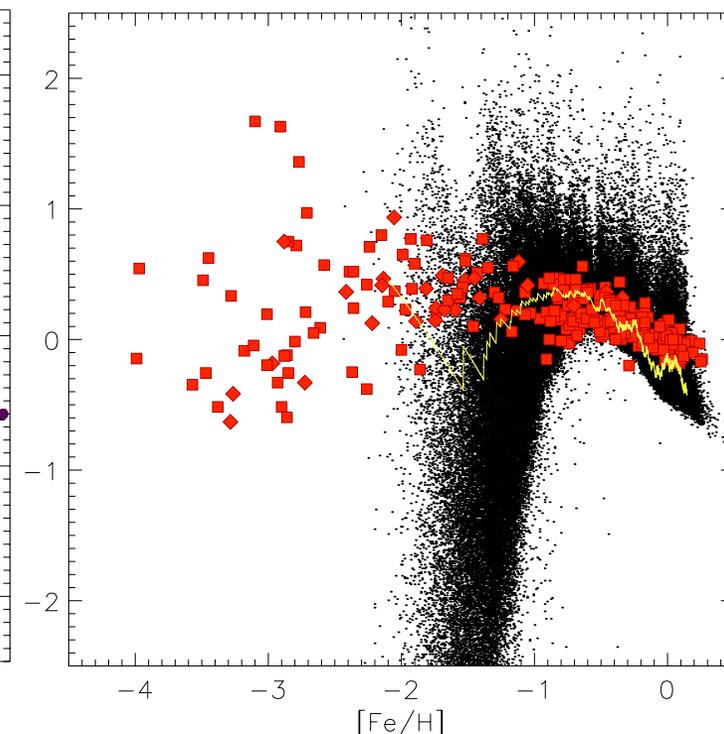
Mathews & Cowan 90

\*The stars in the box seem to be more consistent with supernovae since neutron stars take time to merge

Type II Supernova



Neutron Star Mergers

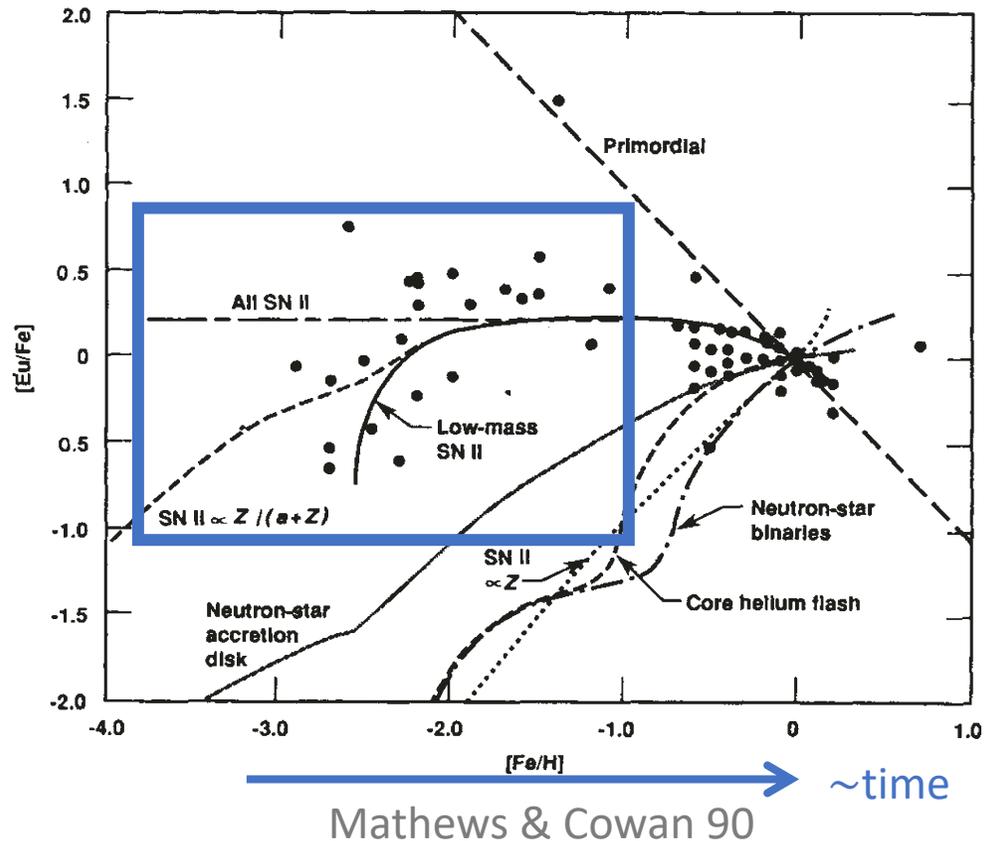


Argast+04

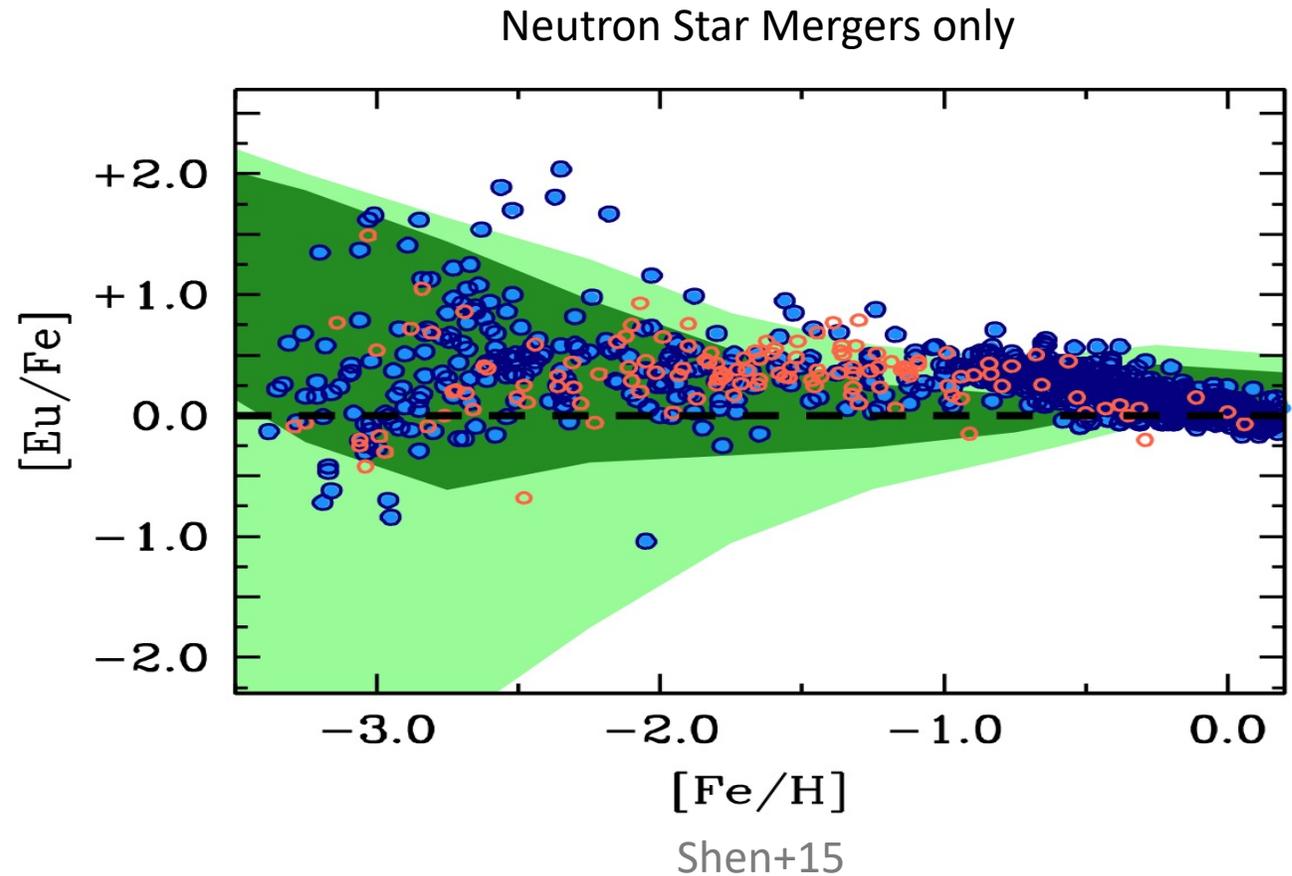
- ◆ ■ observations
- model stars
- ~ average ISM abundances

# Supernovae as the $r$ -process source?

## Galactic chemical evolution (GCE) and low metallicity stars

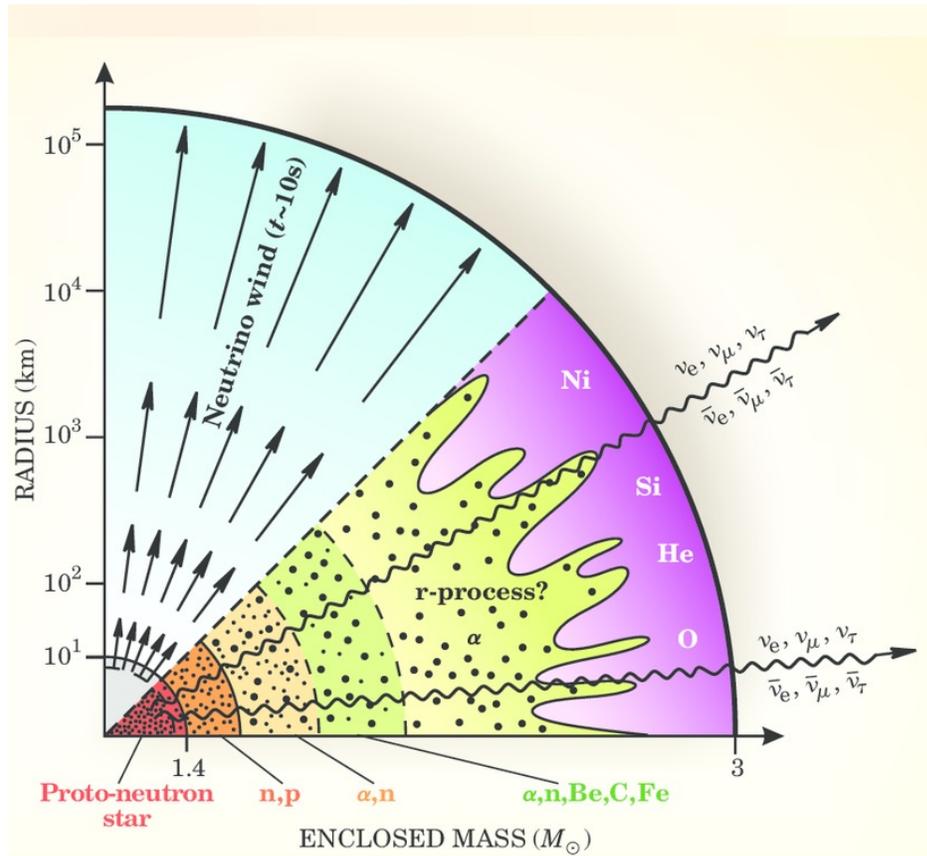


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Hydrodynamic mixing accounting for inhomogeneities in the interstellar medium could explain how  $r$ -process elements find their way to low metallicity regions

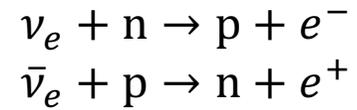
# Supernovae as the $r$ -process source? Simulations and neutrino-driven winds (NDWs)



Neutrinos set the  
neutron to proton ratio

$$Y_e = \frac{n_p}{n_p + n_n}$$

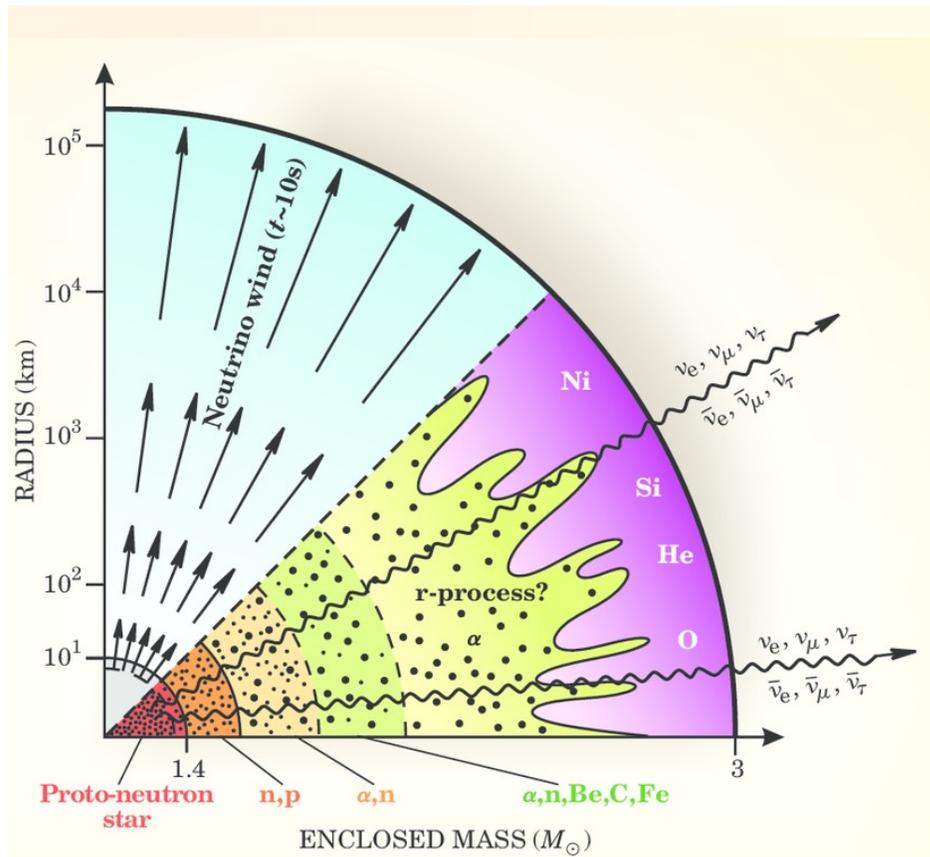
via weak interactions



and the influence of  
these reactions  
depends on the  
neutrino luminosities  
and average energies

Woosley&Janka 06; see  
also Panov&Janka 08

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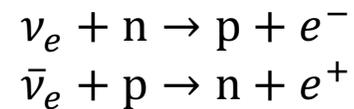


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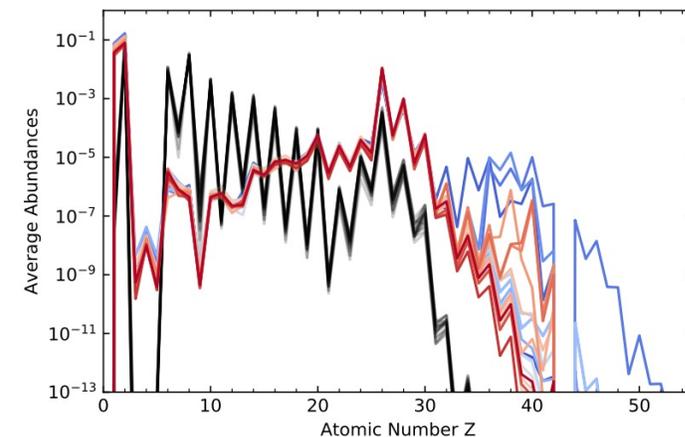


and the influence of  
these reactions  
depends on the  
neutrino luminosities  
and average energies

Conditions which synthesize  $A > 130$  are not found  
by most modern core-collapse SNe simulations  
(e.g. Arcones+07, Wanajo+09, Fischer+10,  
Hüdepohl+10)

In such events other processes such as  $(\alpha, n)$  and  
 $\nu p$  process could reach up to  $A \sim 100$   
(e.g. Pruet+06, Fröhlich+06, Bliss+18)

Recent simulations find some cases develop NDWs  
but not standard feature for successful explosions

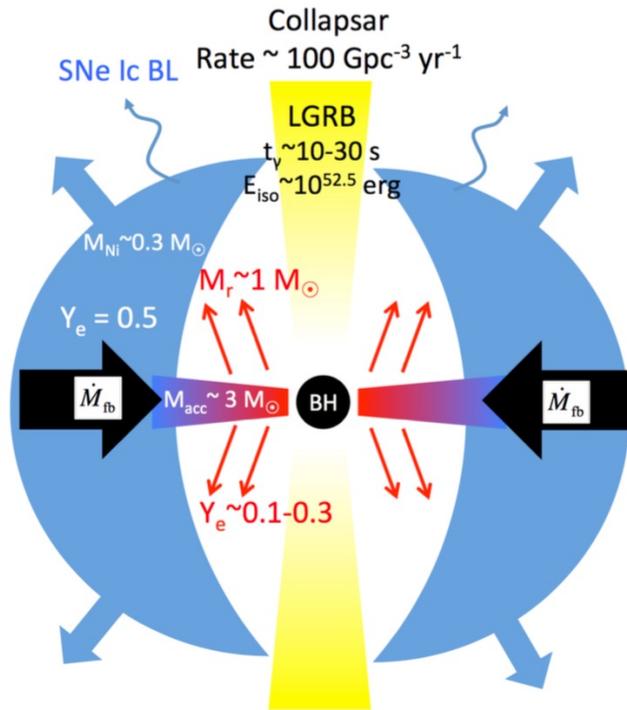


All exploding  
 $15 M_\odot$  models

Witt+21

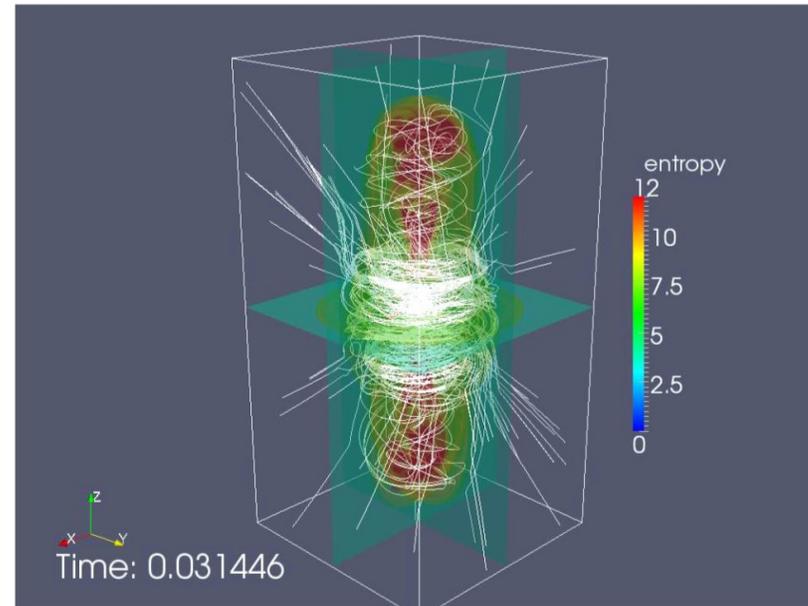
# Some candidate sites for $r$ -process element production

## Collapsar disk winds



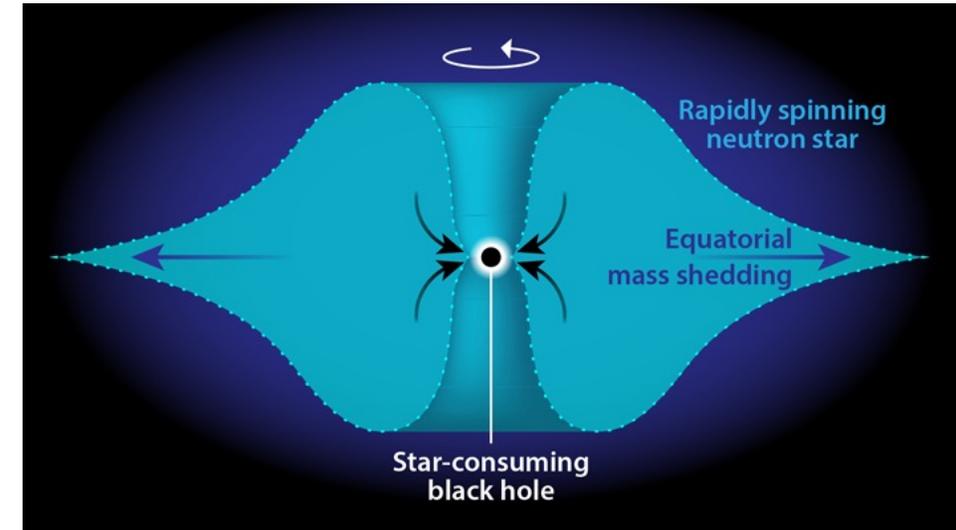
Siegel+18; see also  
McLaughlin&Surman 05,  
Miller+19

## Magneto-rotationally driven (MHD) supernovae



Winteler+12; see also Mosta+17

## Primordial black hole + neutron star

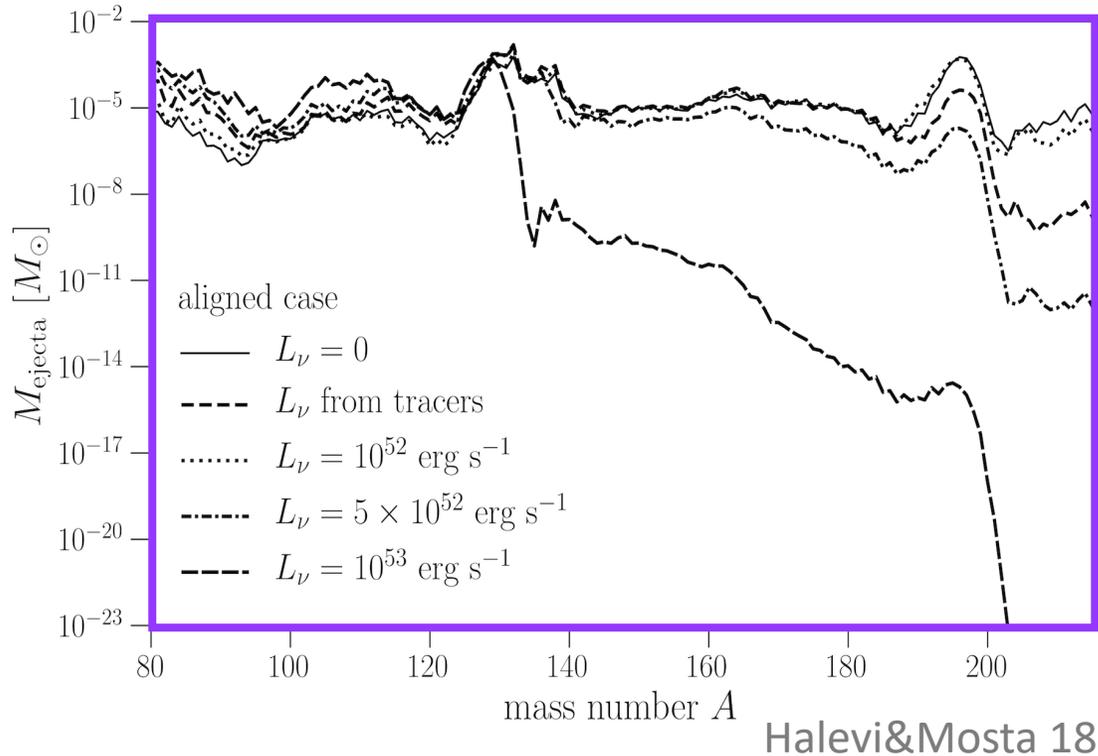


Credit: APS/Alan Stonebraker, via *Physics*

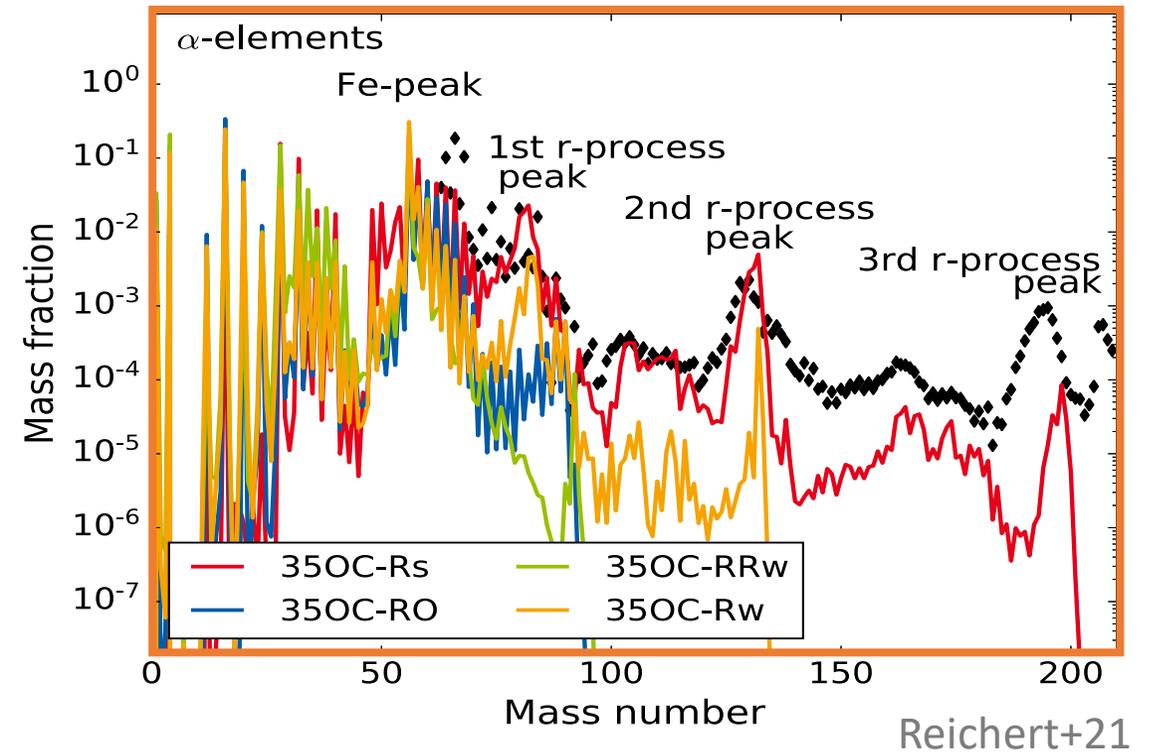
Fuller+17

# Spotlight on MHD supernovae

Whether MHDs undergo only a “weak”  $r$  process reaching the second peak rather than a “main” or “strong”  $r$  process reaching the third peak or beyond depends on the **influence of neutrinos** and the **magnetic field strength**



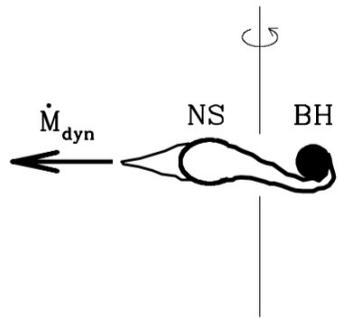
Just like in CCSNe, neutrino energies and luminosities are crucial to determine the  $r$ -process reach



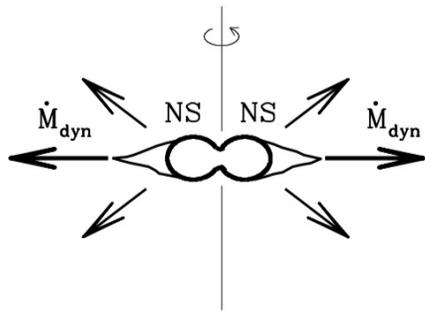
Simulations with higher magnetic field strength (ex 350C-Rs  $\rightarrow 10^{12} \text{ G}$ ) undergo a stronger  $r$  process than those with lower magnetic field strength (ex 350C-Rw  $\rightarrow 10^{10} \text{ G}$ )

# Neutron star mergers and the $r$ process: a bit of history

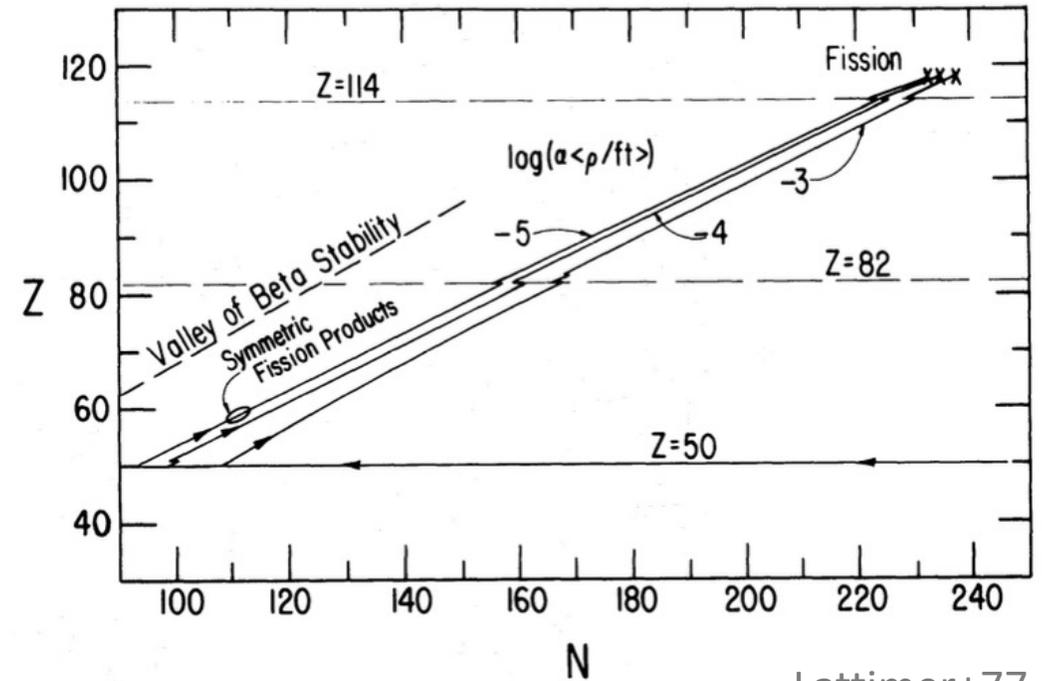
## Neutron-rich ejecta from neutron stars > 40 years ago



Lattimer&Schramm (1974): ~5% of the neutron star ejected as n-rich matter



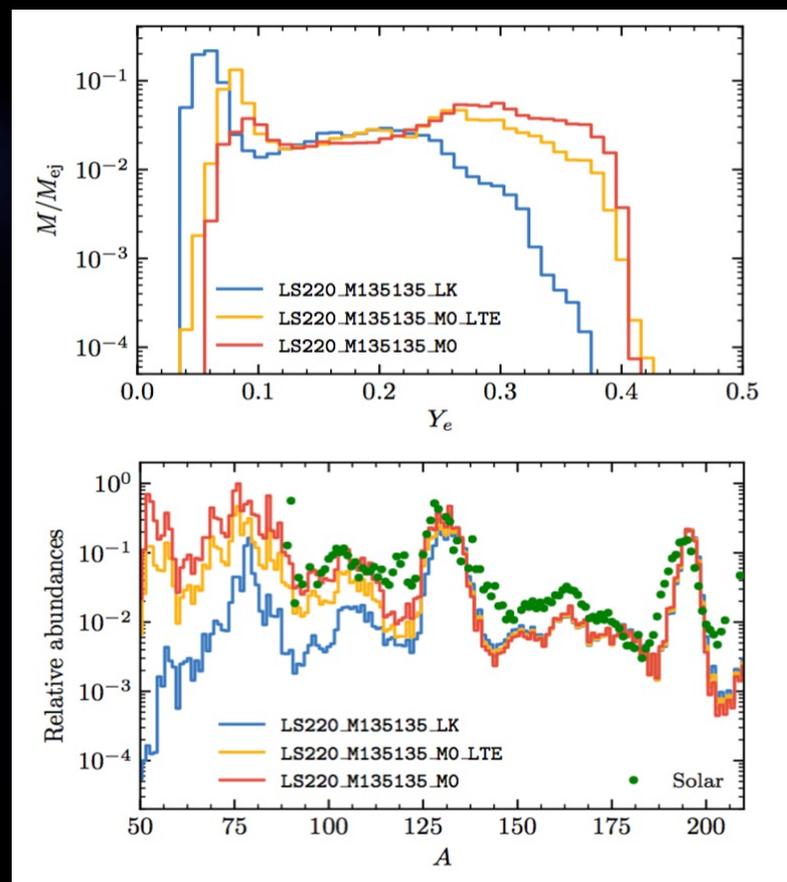
Lattimer+ (1977): initially cold, expanding neutron star matter  $\rightarrow$  fission cycling  $r$  process capable of super heavy element formation



Lattimer+77

# NSM dynamical ejecta

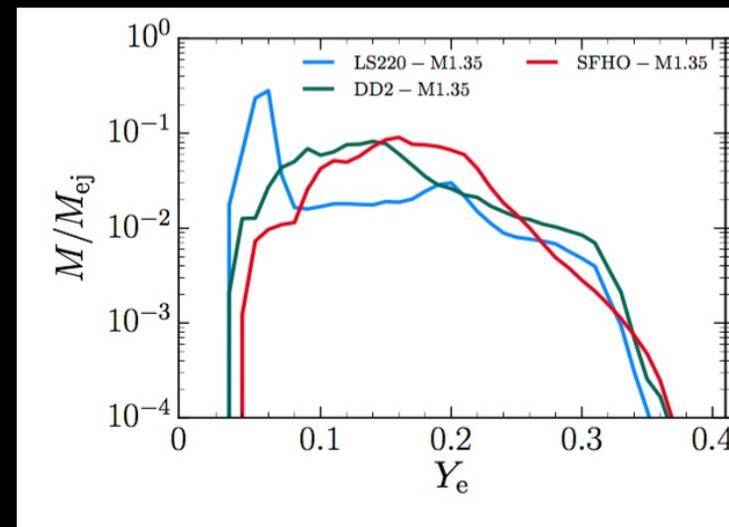
## Effect of neutrinos



Rosswog+13

Radice+19; see also Perego+19

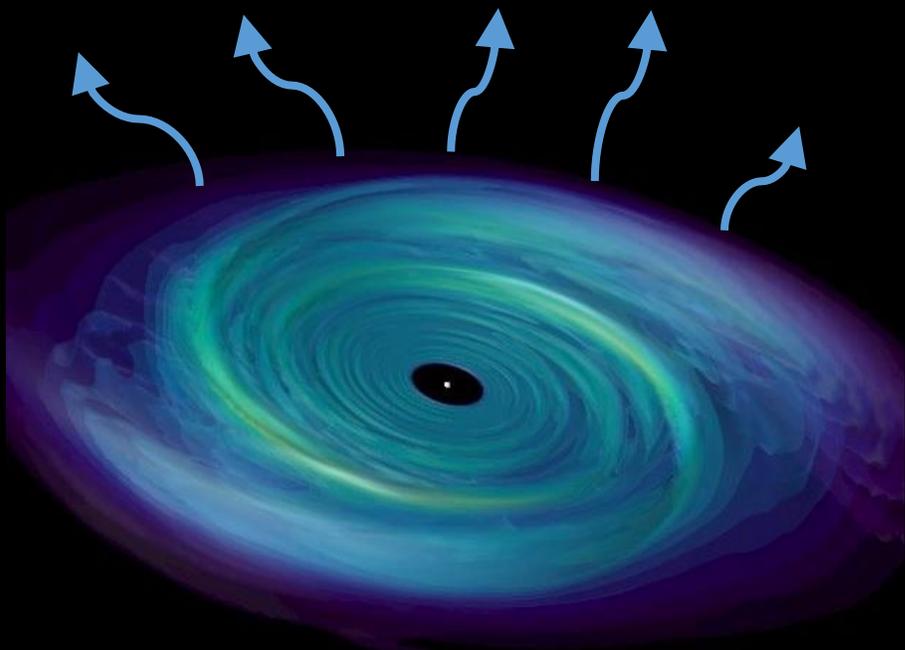
## Equation of state



Bovard+17

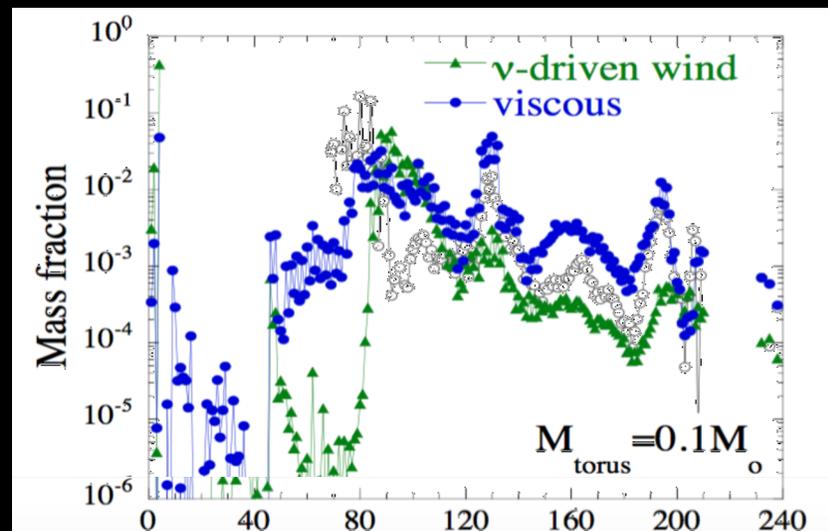
See also Wanajo+14,  
Vincent+19, Foucart+20....

# Post-merger disk ejecta

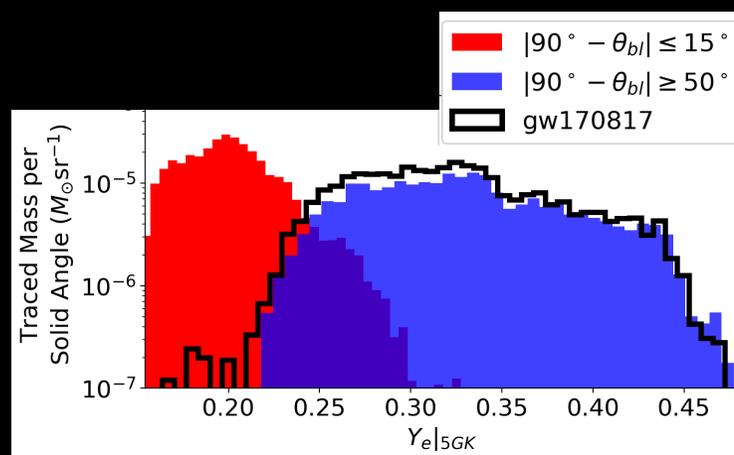


Owen&Blondin 05

# Neutrino driven vs viscous

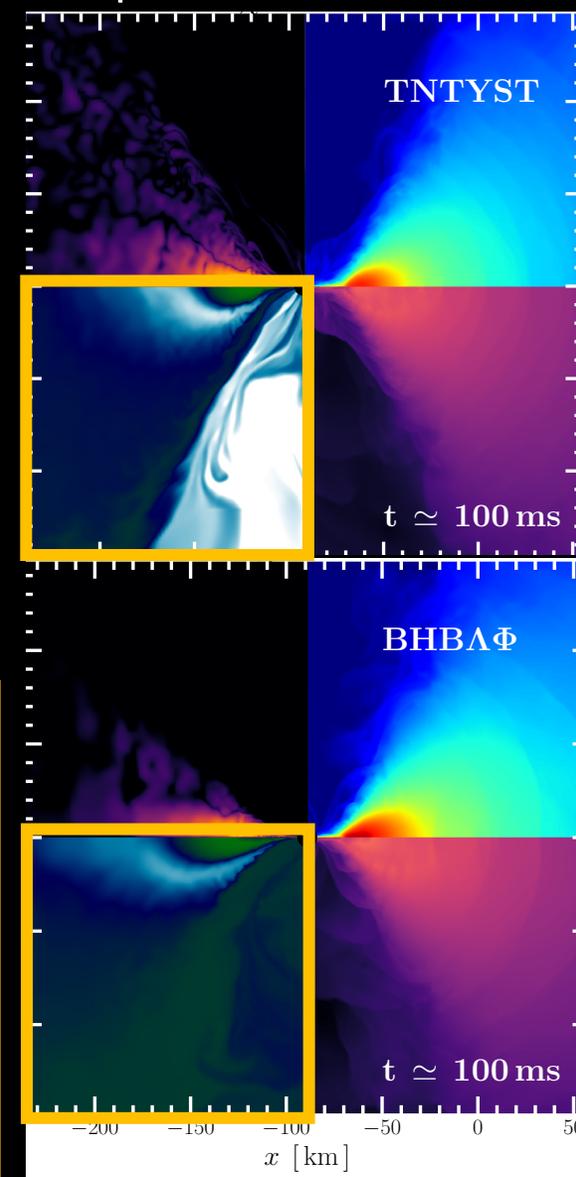


Just+16



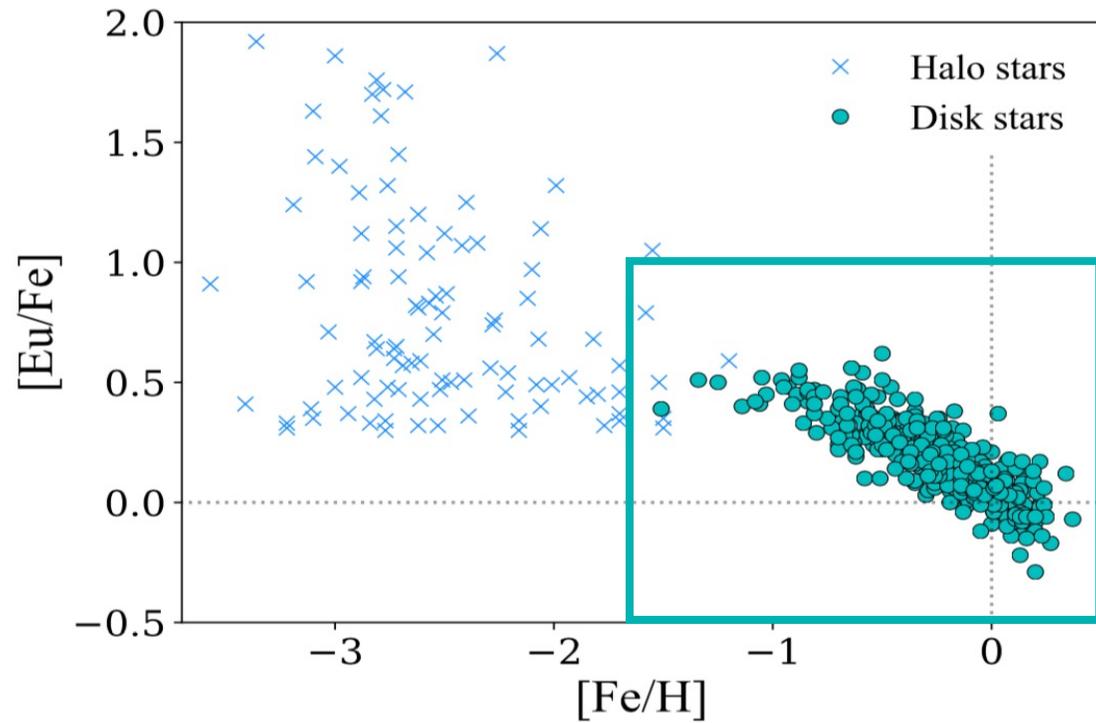
Miller+19

# Equation of state



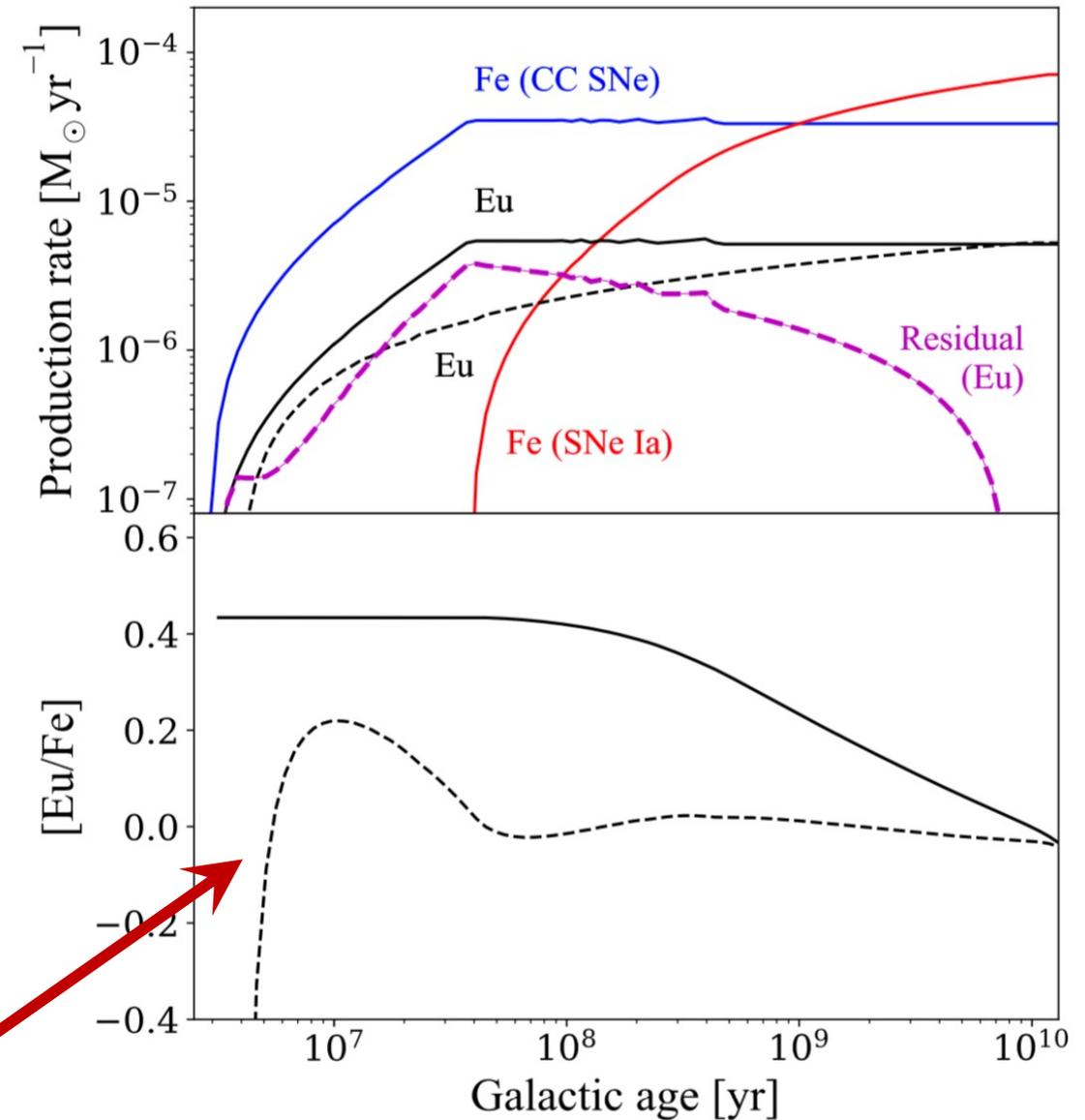
Most+21

Could NSMs be the only  $r$ -process source?  
 Back to GCE but now consider stars in the  
 Galactic disk



Eu production rate must reach equilibrium before onset  
 of SNe Ia in order to reproduce  $[\text{Eu}/\text{Fe}]$  of disk stars

NSM with delay times  $\sim t^{-1}$  don't reproduce this behavior:  
 earlier sources?



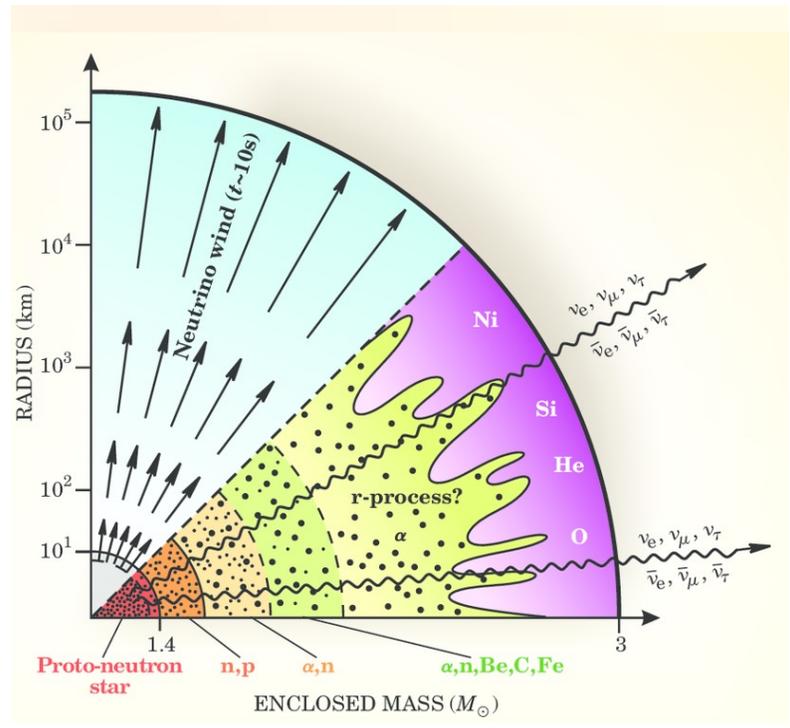
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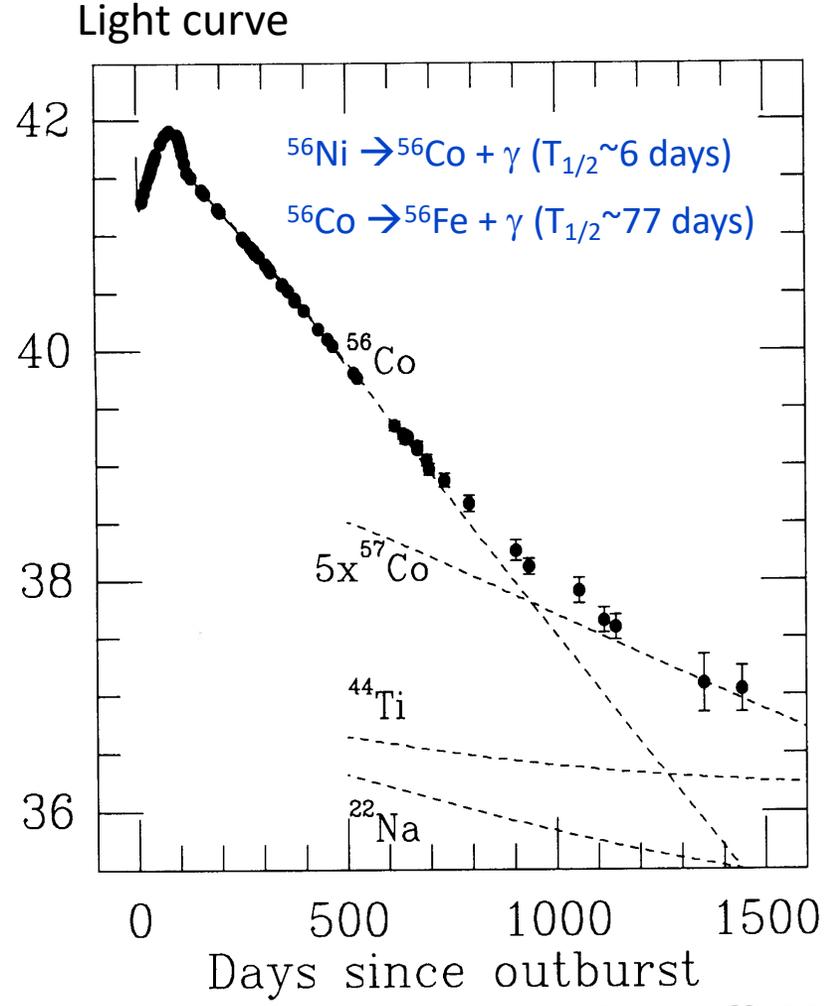
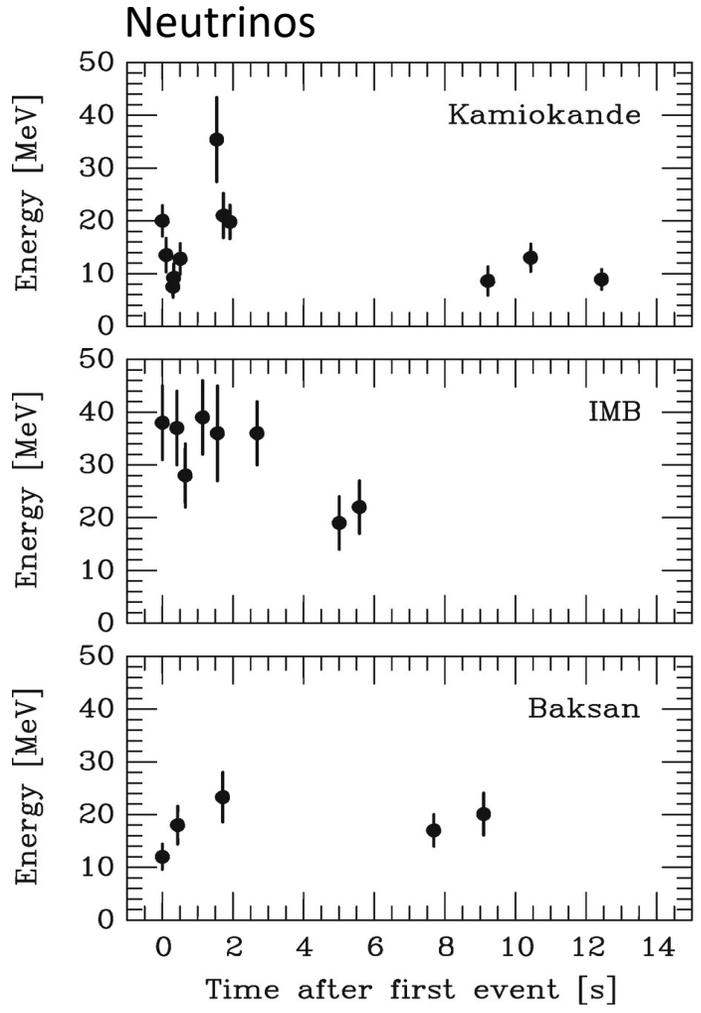
# What is a multi-messenger event?



**SN1987A:**  
A famous core-collapse supernova



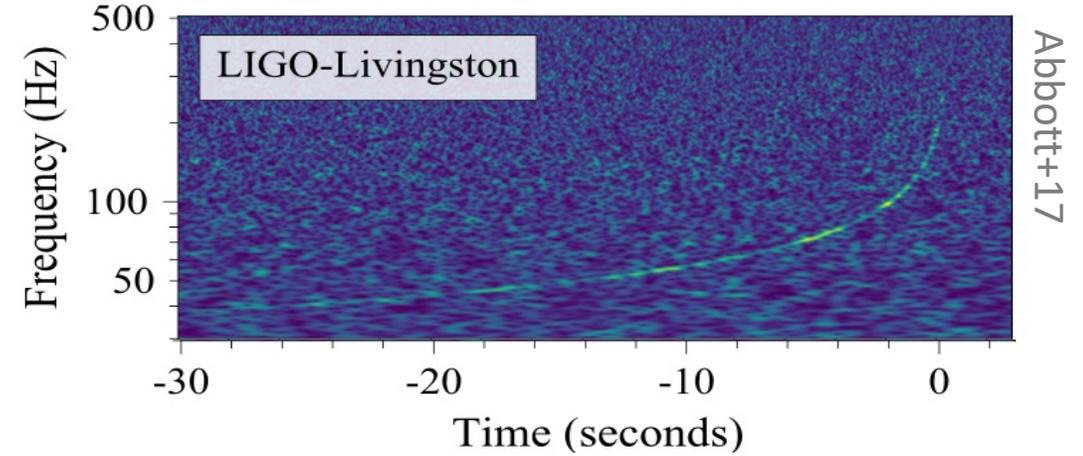
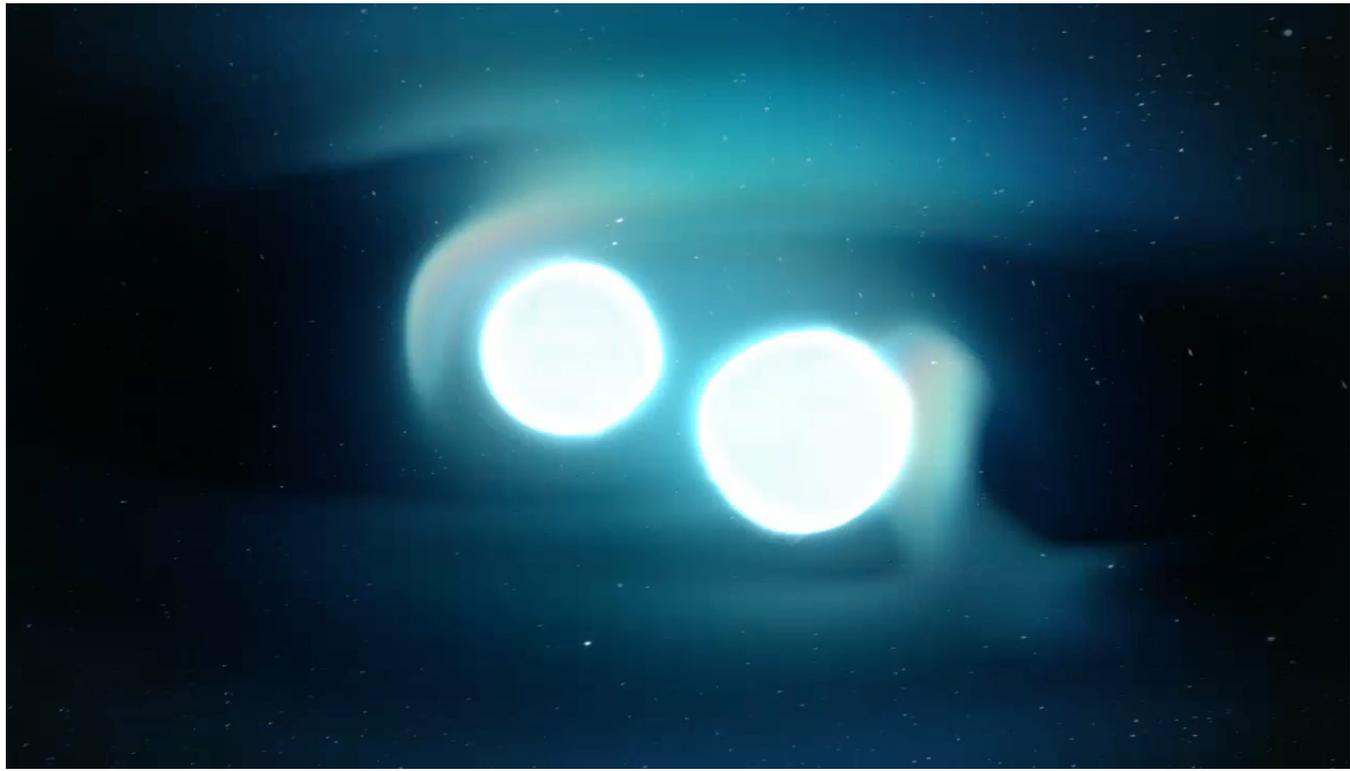
Woosley&Janka 06



Suntzeff+92

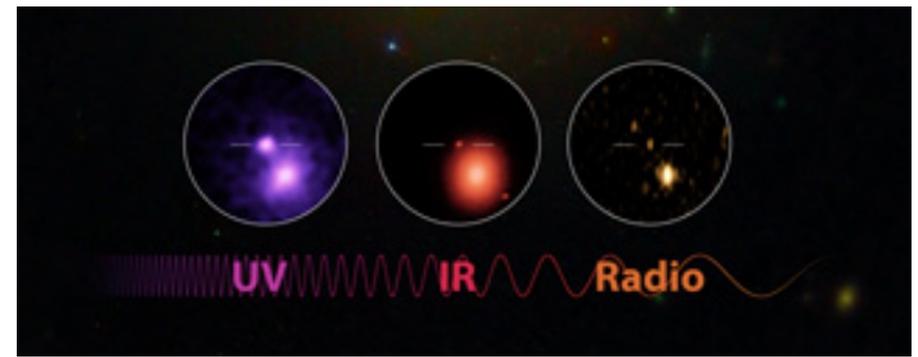
# A new kind of messenger: gravitational waves

GW170817 & AT2017gfo:  
Binary neutron star merger



Abbott+17

NASA Goddard



Hurt/Kasliwal/Hallinan, Evans,  
and the GROWTH collab.

Over ~70 observing teams (~1/3 of the worldwide astronomical community) followed up on the merger event!

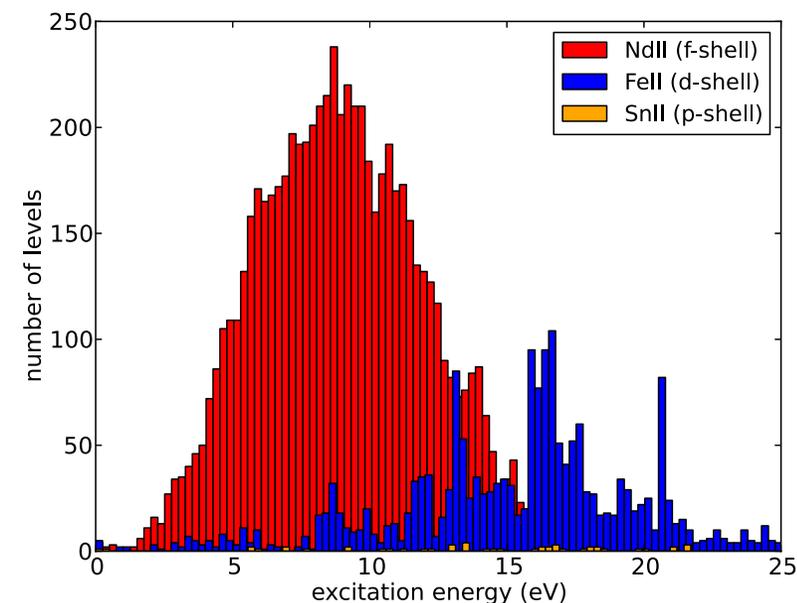
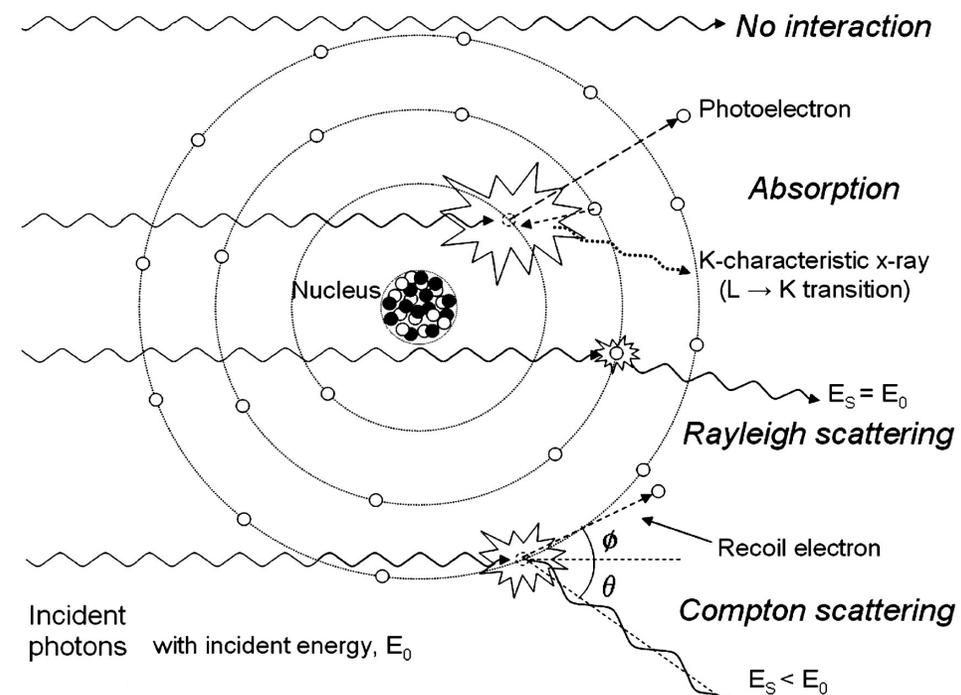
- Ultraviolet** (left, NASA Swift satellite)
- Infrared** (middle, Gemini South telescope)
- Radio** (right, Very Large Array)
- $\gamma$ -ray, X-ray, and optical** also observed

# GW170817 & AT2017gfo: photon opacity

Opacity sources include (\*most important in NSM ejecta):

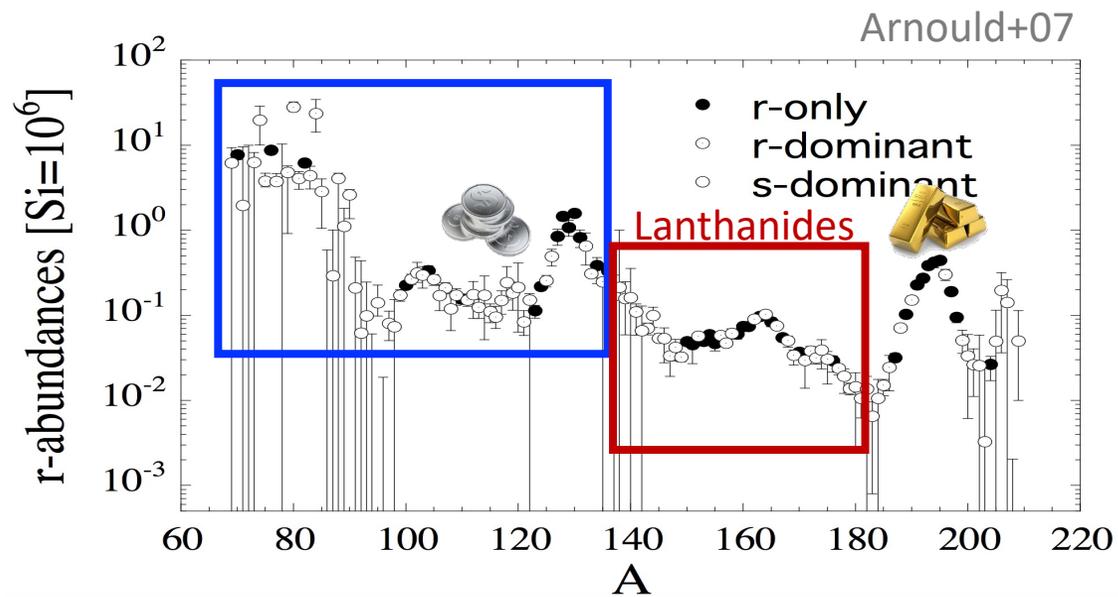
- **bound-bound transitions\*** – photoelectric absorption: photon absorbed or emitted as an electron moves between levels
- **bound-free** – photoionization: electron absorbs photon and escapes
- **free-free scattering** – bremsstrahlung: free electron passing close to ion or nucleus can emit or absorb a photon
- **electron scattering** – inelastic (Compton) scattering and elastic (Rayleigh) scattering: photons scatter off electrons

1																	2
H																	He
3	4											5	6	7	8	9	10
Li	Be											B	C	N	O	F	Ne
11	12											13	14	15	16	17	18
Na	Mg											Al	Si	P	S	Cl	Ar
19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
55	56	57-71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
Cs	Ba	Lanthanides	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
87	88	89-103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118
Fr	Ra	Actinides	Rf	Db	Sg	Bh	Hs	Mt	Ds	Rg	Cn	Nh	Fl	Mc	Lv	Ts	Og
		↓															
57	58	59	60	61	62	63	64	65	66	67	68	69	70	71			
La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu			
89	90	91	92	93	94	95	96	97	98	99	100	101	102	103			
Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr			



Kasen+13;  
see also  
Fontes+20,  
Tanaka+20

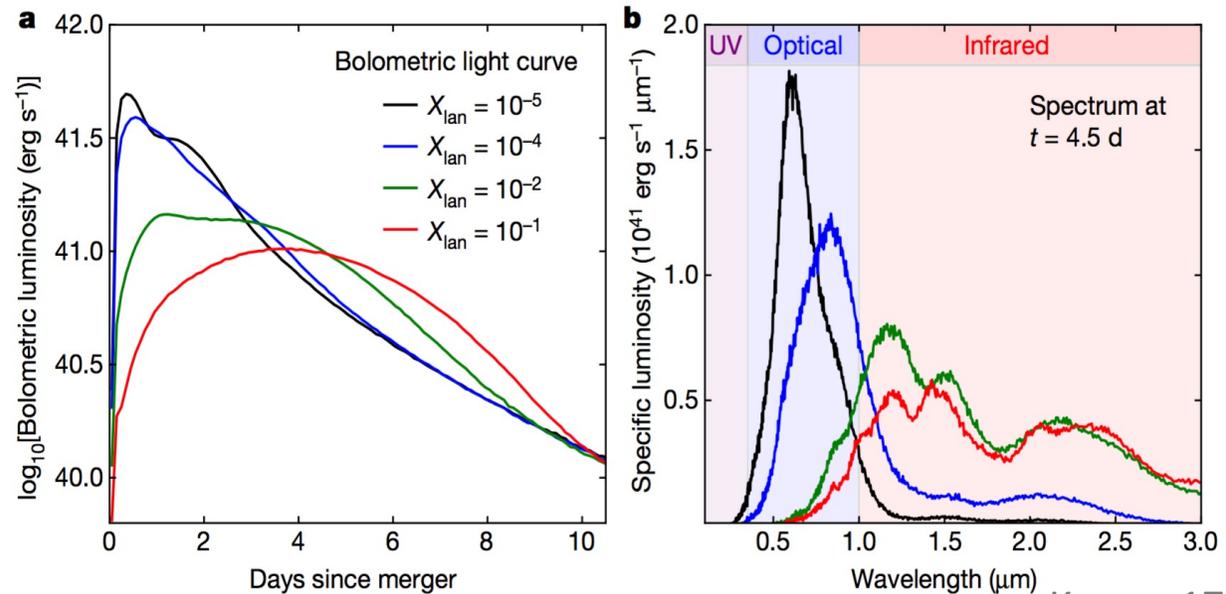
# GW170817 & AT2017gfo: “red” and “blue” kilonovae



Spectra and light curves depend on the species present;  
Lanthanide and/or actinide mass fraction  $\uparrow$ , opacity  $\uparrow$ ,  
longer duration light curve shifted toward infrared

(e.g. Metzger+10, Lippuner+15, Barnes+16,21, Wanajo+18,  
Watson+19, Hotokezaka+20, Korobkin+20, Zhu+18,21, Wang+20)

## Model

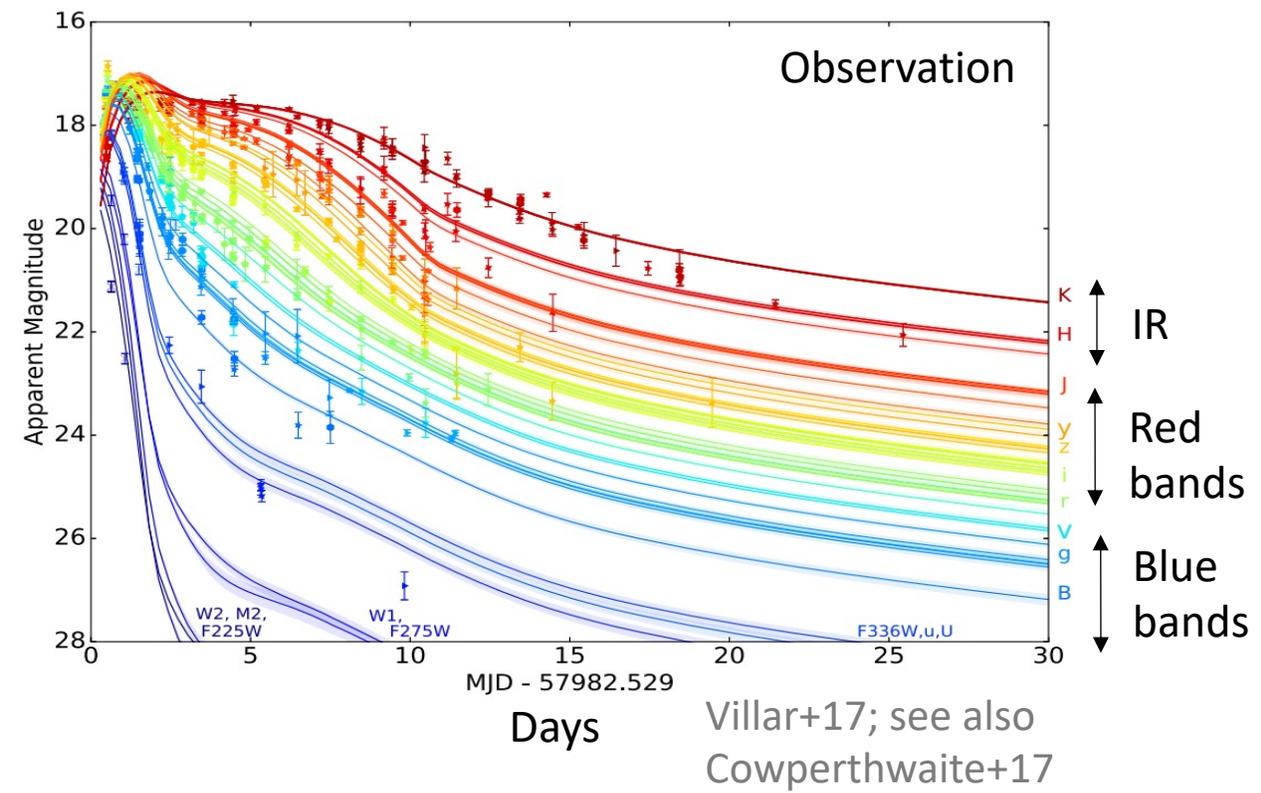
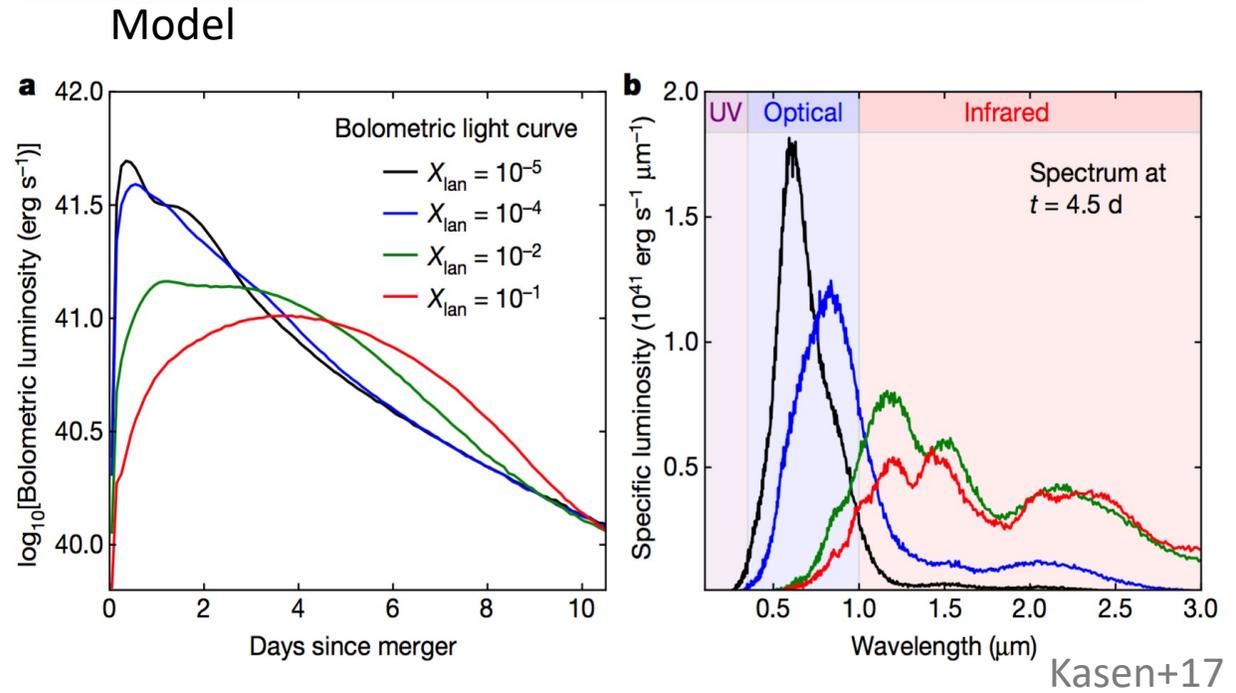
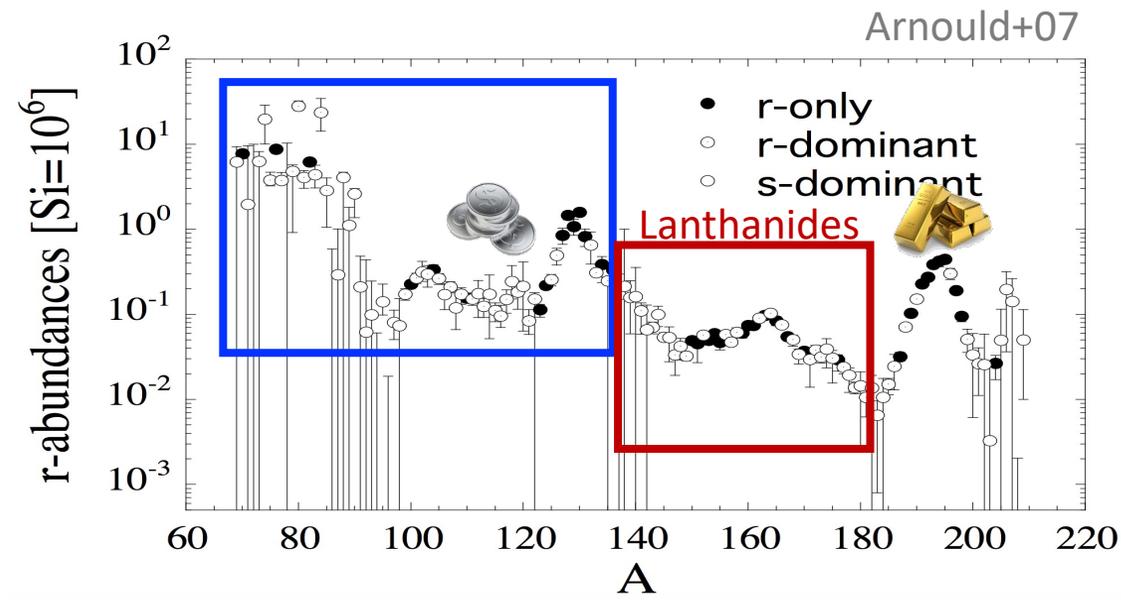


Kasen+17

# GW170817 & AT2017gfo: “red” and “blue” kilonovae

Spectra and light curves depend on the species present;  
Lanthanide and/or actinide mass fraction  $\uparrow$ , opacity  $\uparrow$ ,  
longer duration light curve shifted toward infrared

(e.g. Metzger+10, Lippuner+15, Barnes+16,21, Wanajo+18,  
Watson+19, Hotokezaka+20, Korobkin+20, Zhu+18,21, Wang+20)

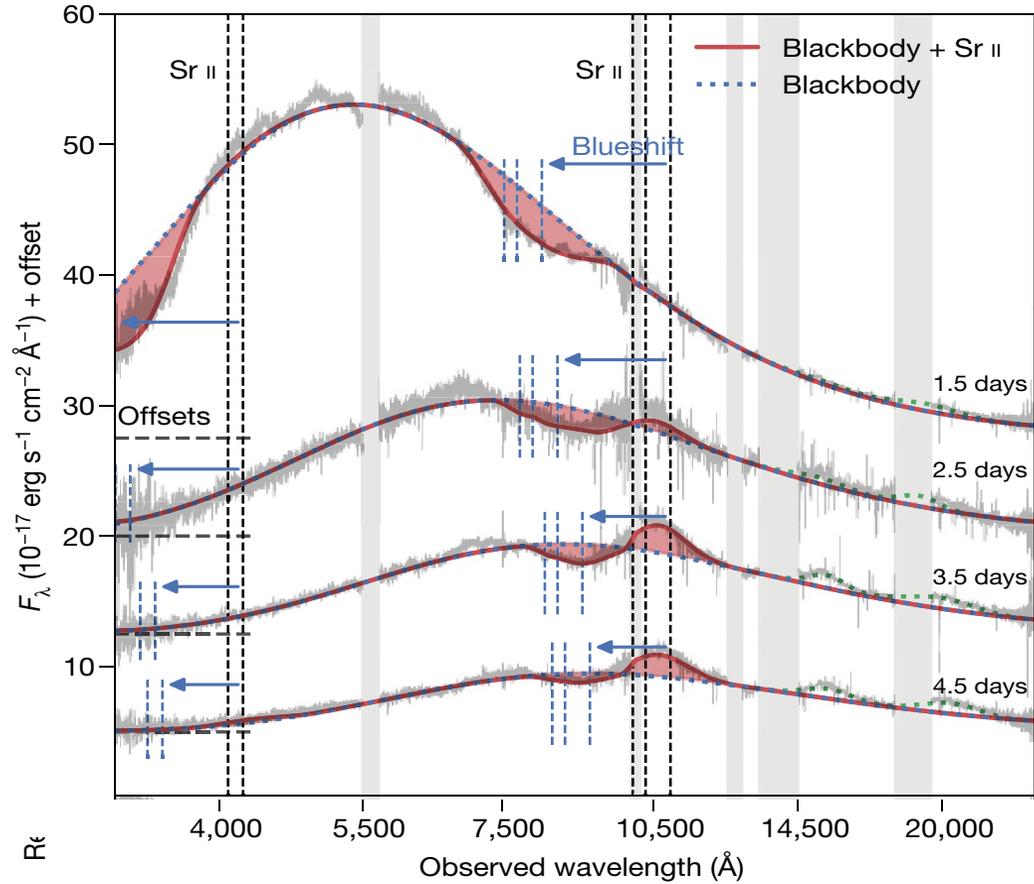


Kasen+17

Villar+17; see also  
Cowperthwaite+17

# Observing individual elements from NSMS?

AT2017gfo and individual element identification:  
Observation of strontium in reanalysis of spectra

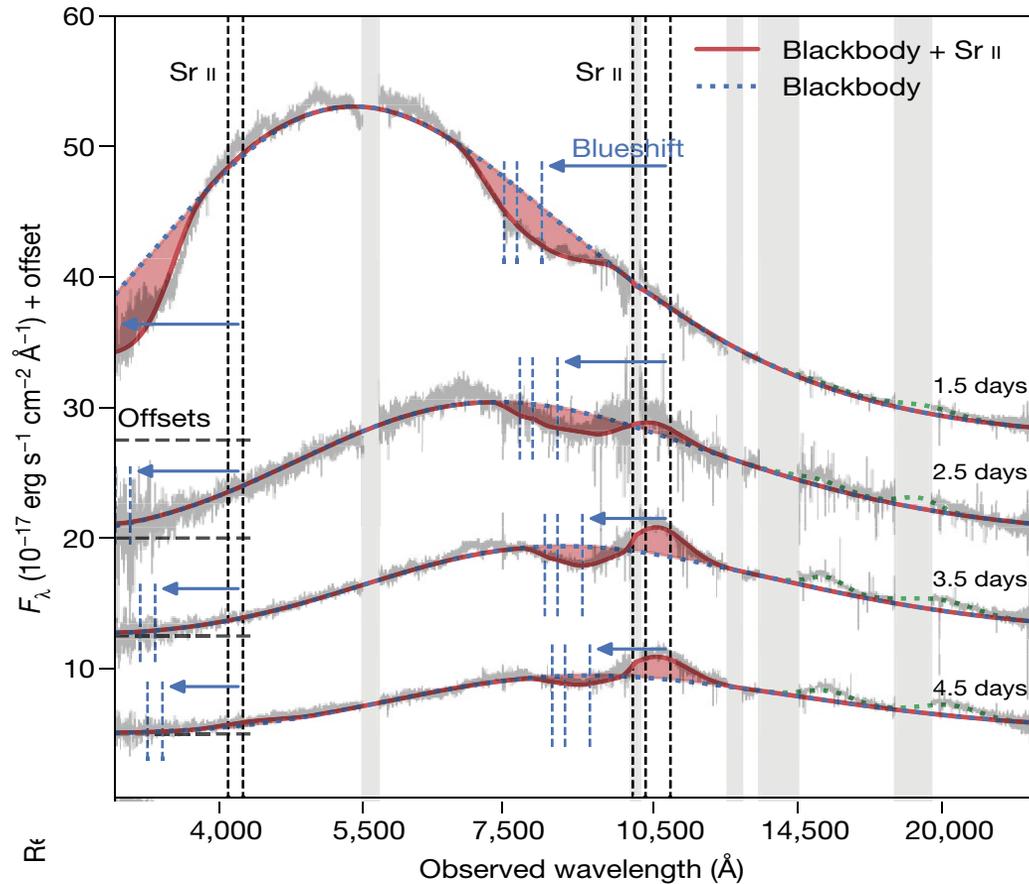


Watson+19

Sr (1<sup>st</sup> *r*-process peak) gives the observed **strong, broad absorption feature around 800 nm**

# Observing individual elements from NSMS?

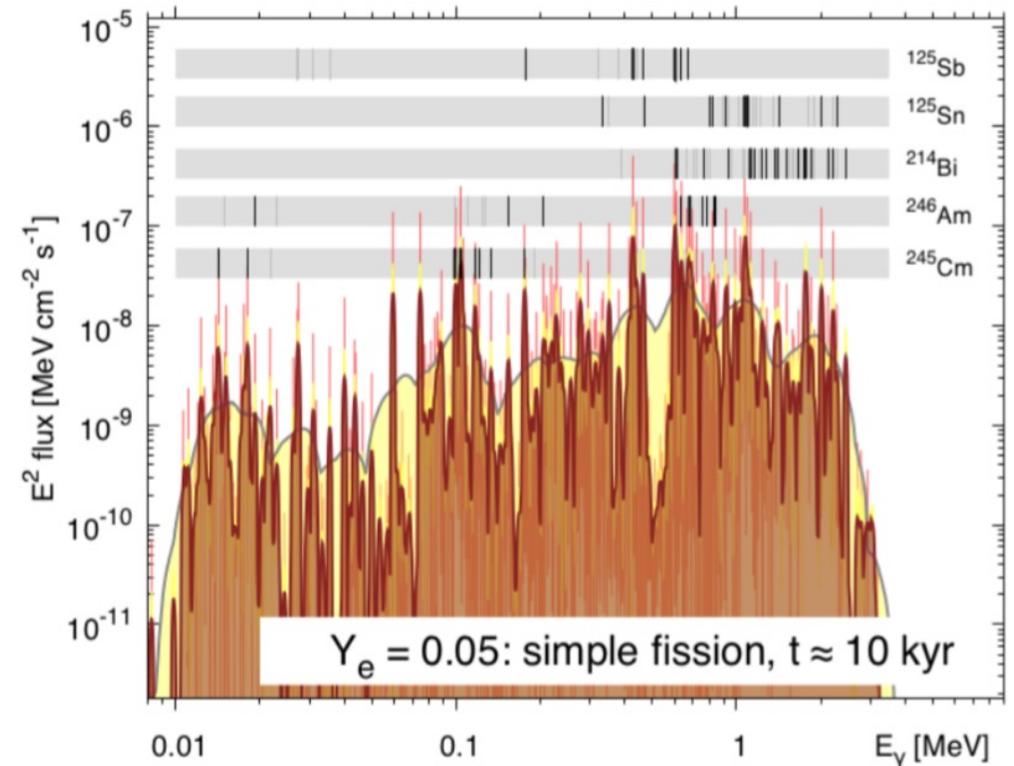
AT2017gfo and individual element identification:  
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Watson+19

Sr (1<sup>st</sup> *r*-process peak) gives the observed **strong, broad absorption feature around 800 nm**

Searching for neutron star merger *remnants*:  
modeling spectral lines from  $\beta$ -decay and  $\alpha$ -decay



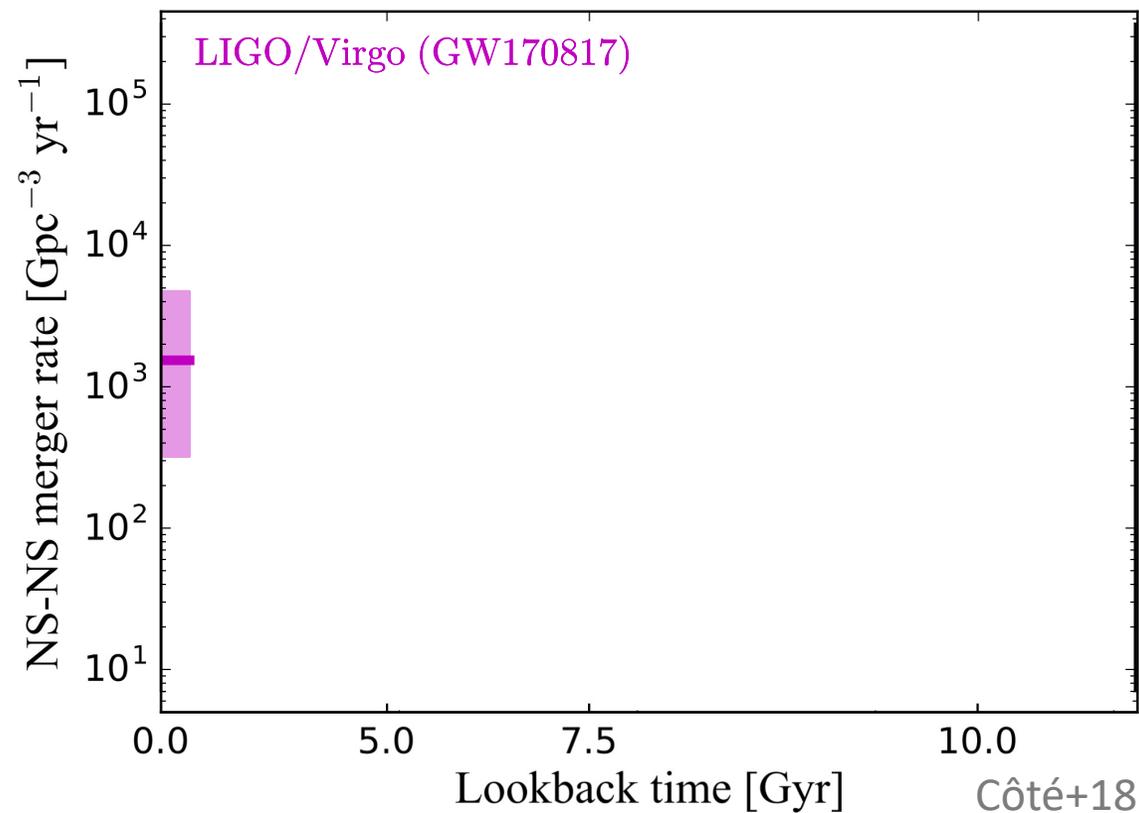
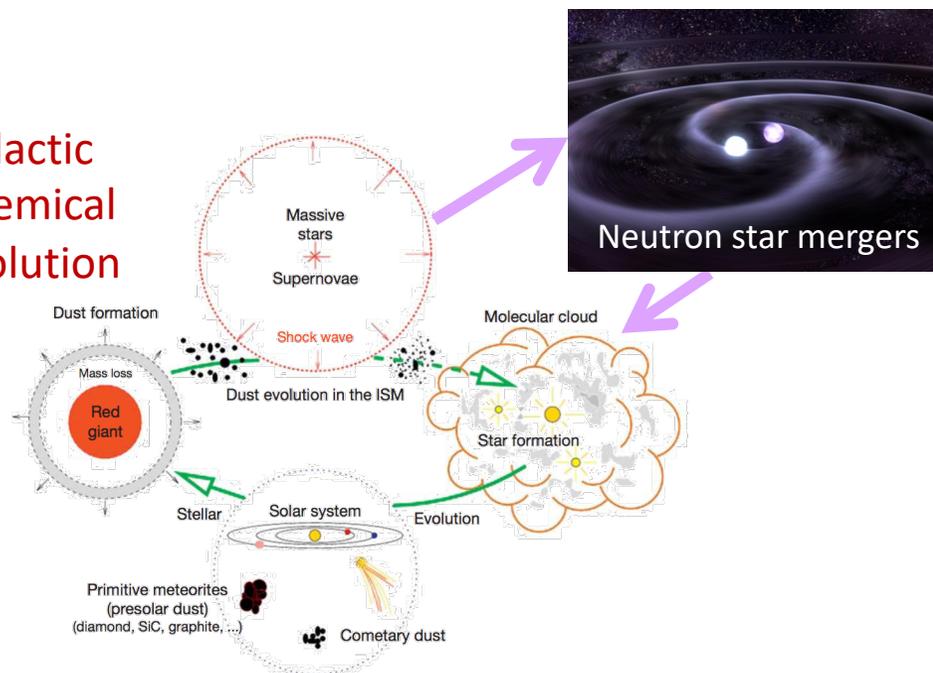
Korobkin+20; see also Wu+19

Above at 10 kpc (within Milky Way) and shows how **Doppler broadening** can wash away features; for reference AT2017gfo was at 40 Mpc

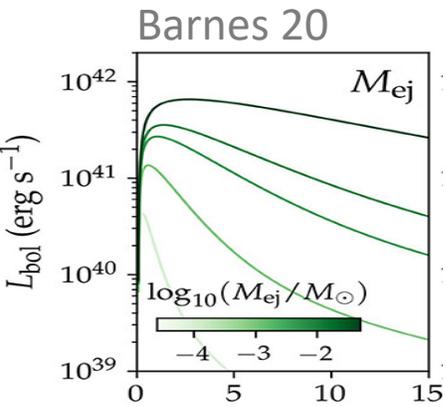
# Do binary NS mergers make enough heavy elements?

## Galactic Chemical Evolution

Palm+14



# Do binary NS mergers make enough heavy elements?

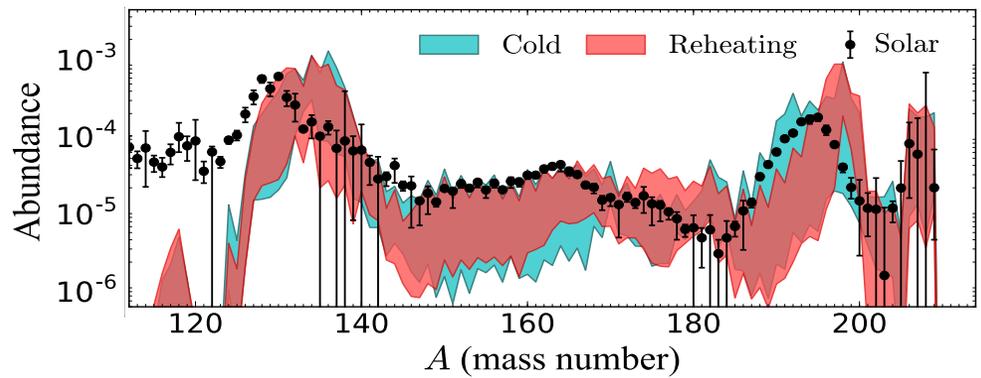
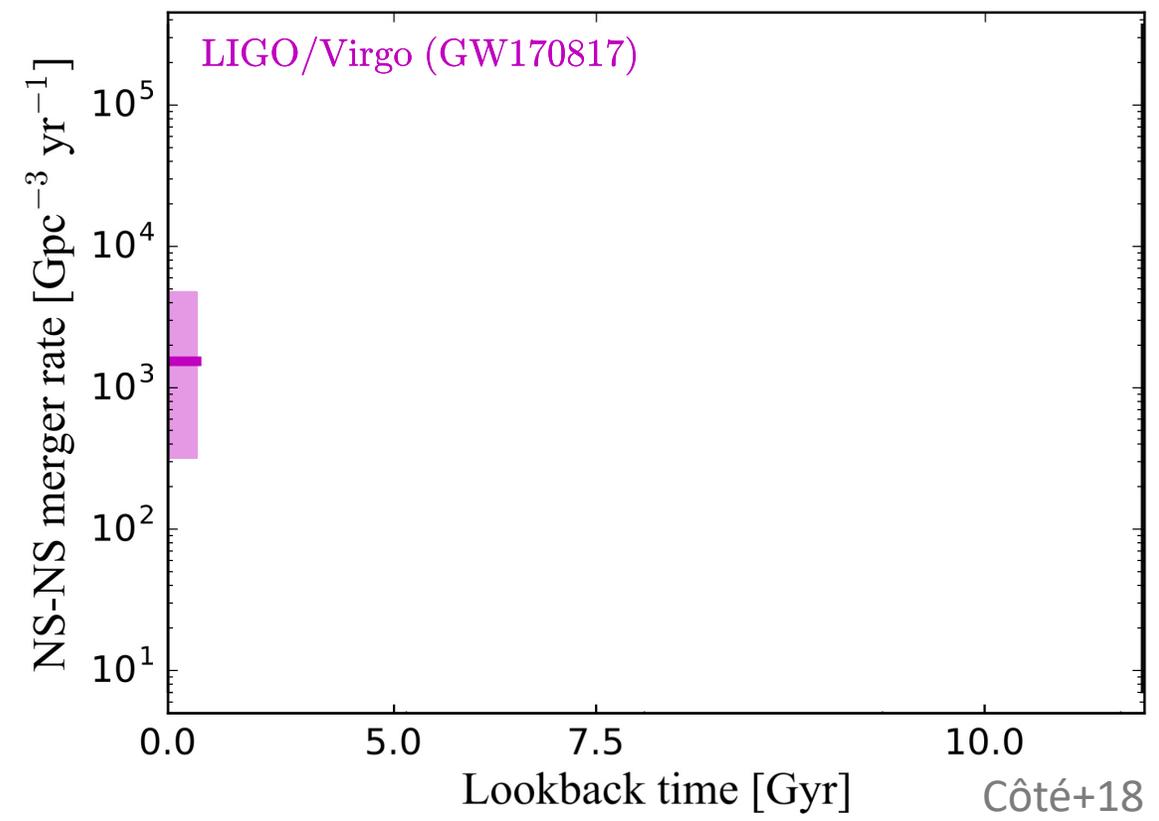
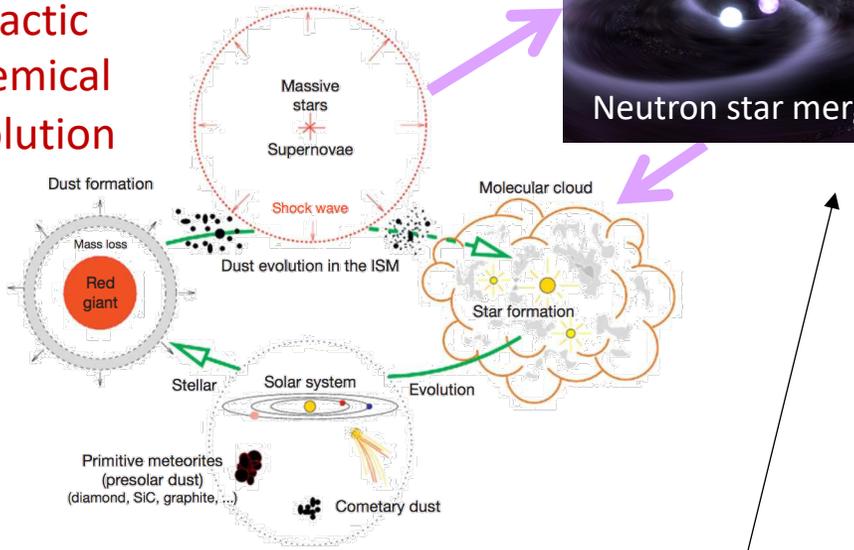


**Light Curves**  
 Take estimates for GW170817 mass ejection range from literature



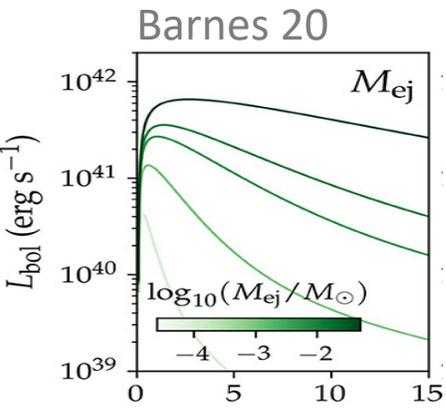
**Galactic Chemical Evolution**

Palm+14



**Nucleosynthesis Predictions**  
 Abundance range of dynamical ejecta from 10 mass models

# Do binary NS mergers make enough heavy elements?

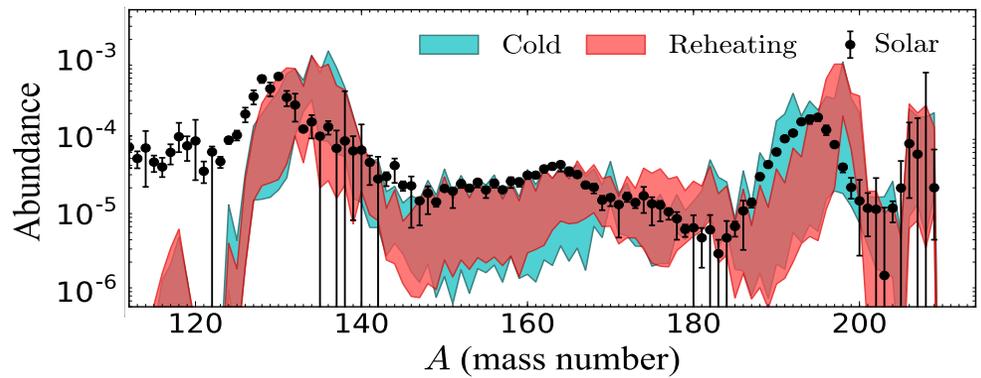
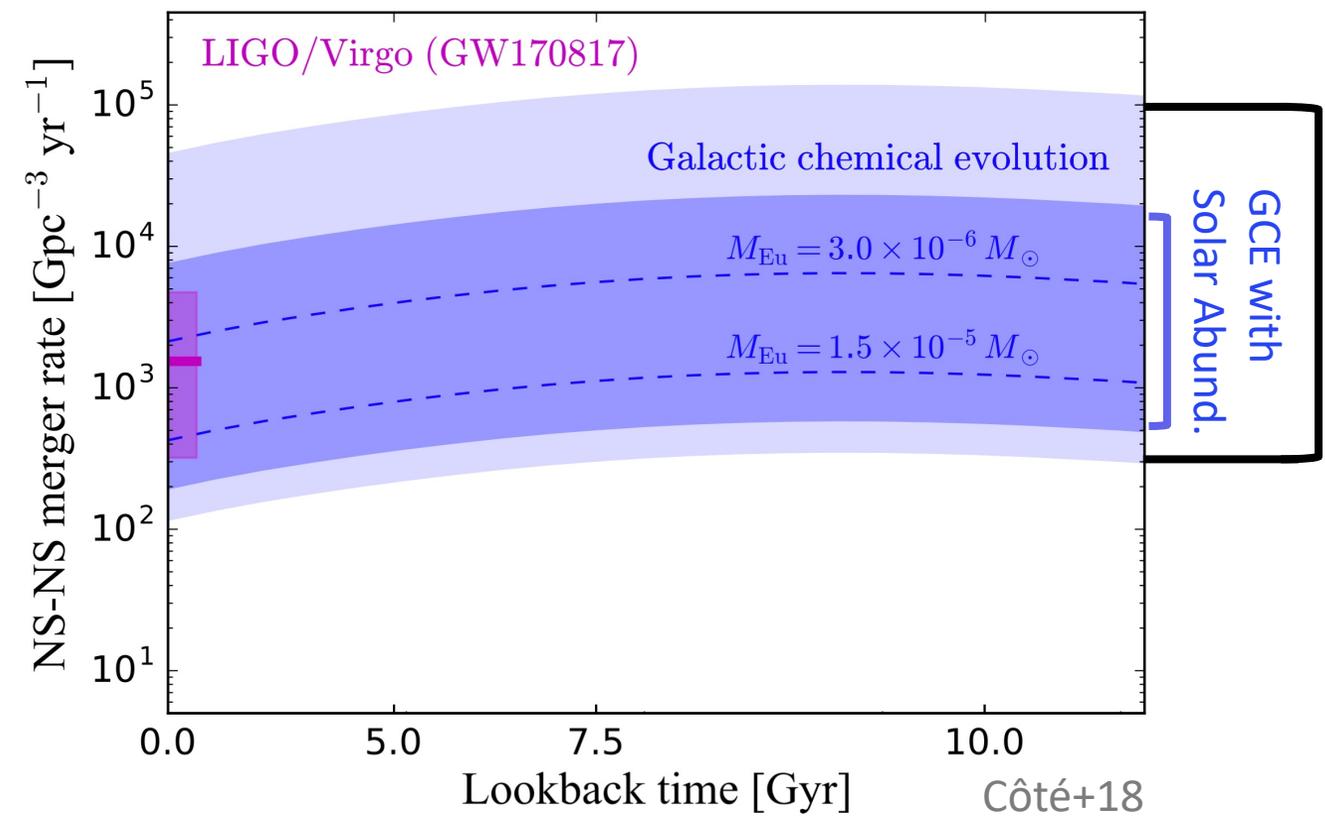
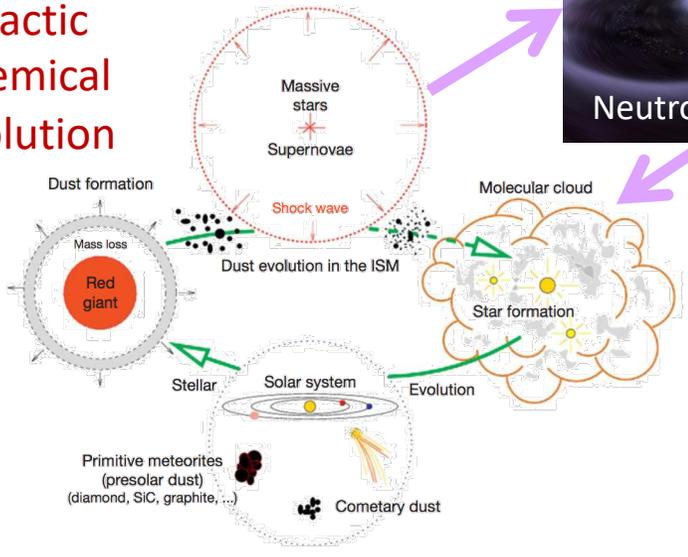


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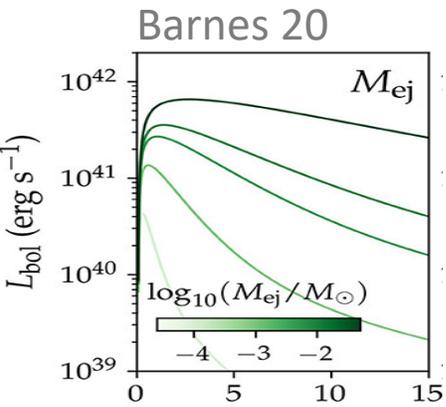
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Palm+14



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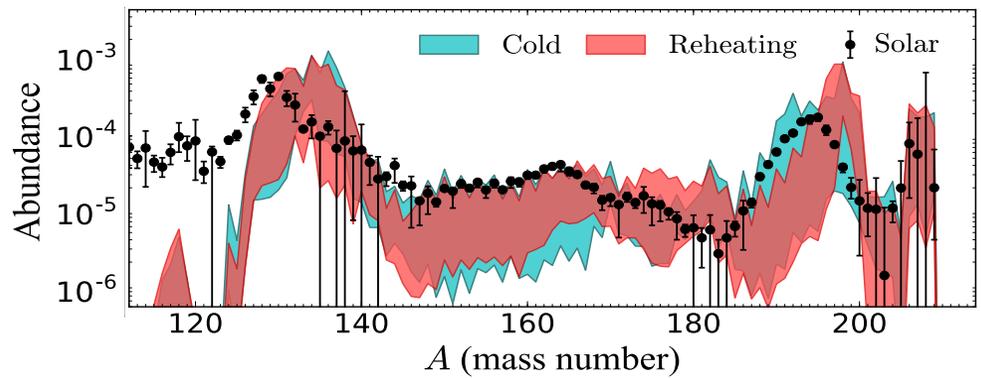
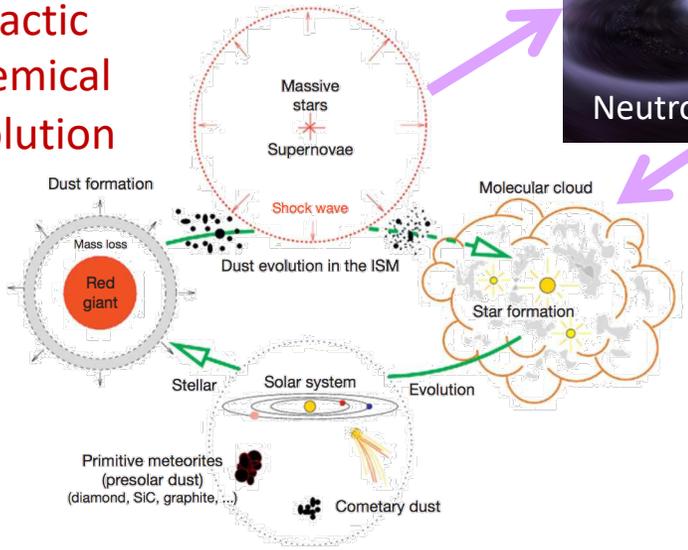


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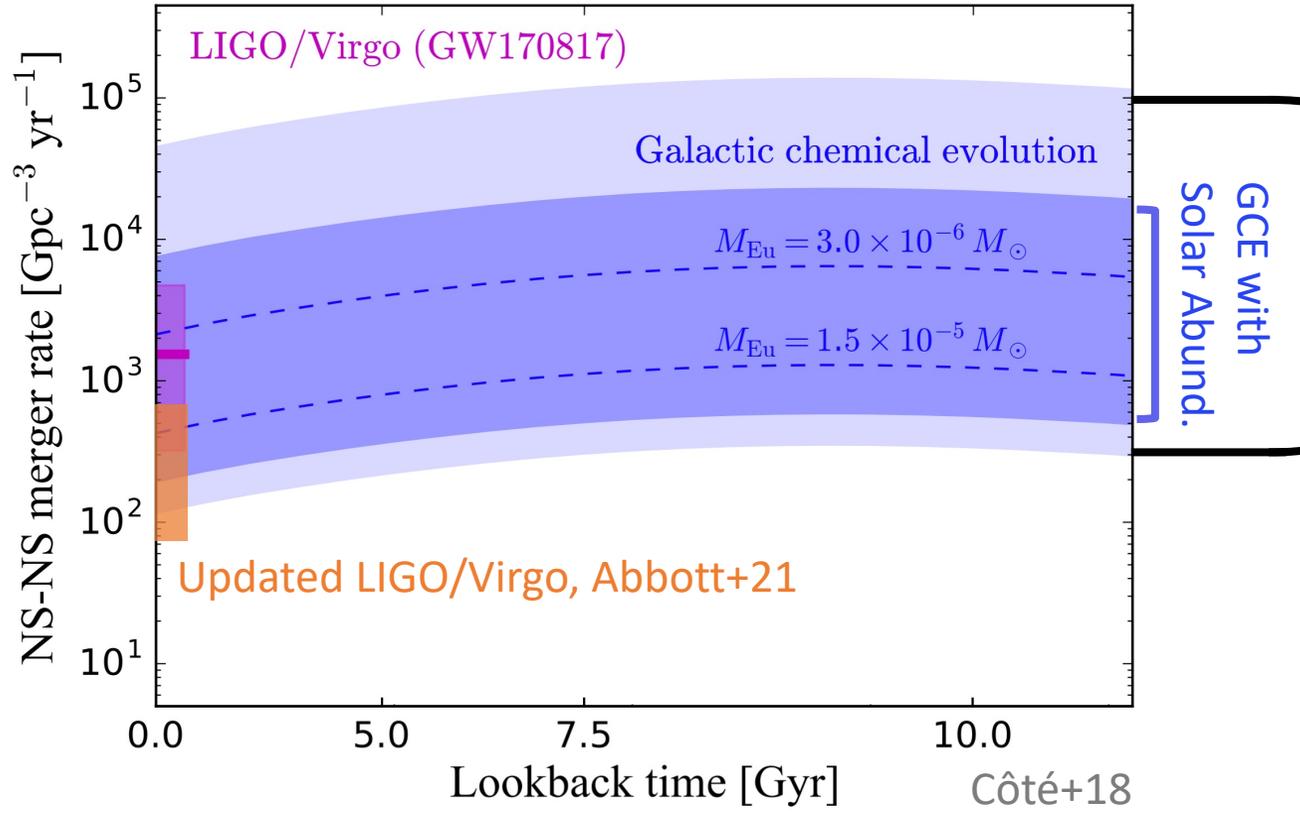


**Galactic Chemical Evolution**

Palm+14



**Nucleosynthesis Predictions**  
Abundance range of dynamical ejecta from 10 mass models



\*Now another confirmed NSNS merger GW190425 as well as a June 2021 confirmation of two NSBH mergers GW200105 and 200115!

# Outline

- Observational evidence that the  $r$  process occurs [4-9]
- Discussion of astrophysical sites (history (CCSNe), candidate sites, MHD SNe, NSNS/NSBH) [11-21]
- Spotlight on GW170817 and AT2017gfo: the first multi-messenger NSNS event [23-33]
- $r$ -process calculations (intro to reaction rates and equilibrium, history (classical  $r$  process), intro to using networks and trajectories,  $r$ -process dynamics) [35-52]
- The fundamental role of nuclear physics [54-82]

# Some definitions and intro to astrophysical rates: consider $B + x \rightarrow C + D$

$$Q = (M_B + M_x - M_C - M_D)c^2$$

$Q$  = energy released (+) or absorbed (-), aka Q-value [MeV]

$$S_n(Z, A + 1) = M_{Z,A} + M_n - M_{Z,A+1}$$

$S_n$  = one neutron separation energy [MeV]

$$n_B = \rho N_A \frac{X_B}{A_B} = \rho N_A Y_B$$

$n_B$  = number density [ $\text{cm}^{-3}$ ],  $\rho$  = density [ $\text{g} \cdot \text{cm}^{-3}$ ],  $N_A$  = Avogadro's number ( $6.022 \times 10^{23}$ ) [ $\text{g}^{-1}$ ]

$$\frac{X_B}{A_B} = \frac{\text{mass fraction } (\sum_i X_i = 1)}{\text{mass number } (\# \text{ protons} + \# \text{ neutrons})}, Y_B = \text{abundance}$$

$$Y_e = \sum_i Z_i Y_i = \frac{n_p}{n_p + n_n}$$

$Y_e$  = electron fraction (formula assumes charge neutrality); lower  $Y_e$  is more neutron rich

$$r_{Bx} = \frac{n_B n_x}{1 + \delta_{Bx}} \langle \sigma v \rangle$$

$\langle \sigma v \rangle$  = thermally averaged cross section =  $\int \sigma v f(v) dv$  where  $f(v) = \left(\frac{m}{2\pi kT}\right)^{3/2} 4\pi v^2 e^{-\frac{mv^2}{2kT}}$  is the Maxwell-Boltzmann distribution ( $\sim e^{-E/kT}$ ) and  $m = \frac{m_B m_x}{m_B + m_x}$  (the reduced mass)

$$\lambda_{Bx} = \frac{1}{1 + \delta_{Bx}} Y_x \rho N_A \langle \sigma v \rangle$$

$r$  = interaction rate or reaction rate [ $\text{cm}^{-3} \text{s}^{-1}$ ],  
 $\lambda$  = "stellar reaction rate" (per target nucleus) [ $\text{s}^{-1}$ ] (Note units of  $N_A \langle \sigma v \rangle = \text{cm}^3/\text{s/g}$ )

# Nuclear Statistical Equilibrium (NSE)

If the environment is hot enough to overcome Coulomb barriers and has high energy photons, neutron and proton captures on  $(Z,N)$  are in chemical equilibrium with reverse photodissociations:

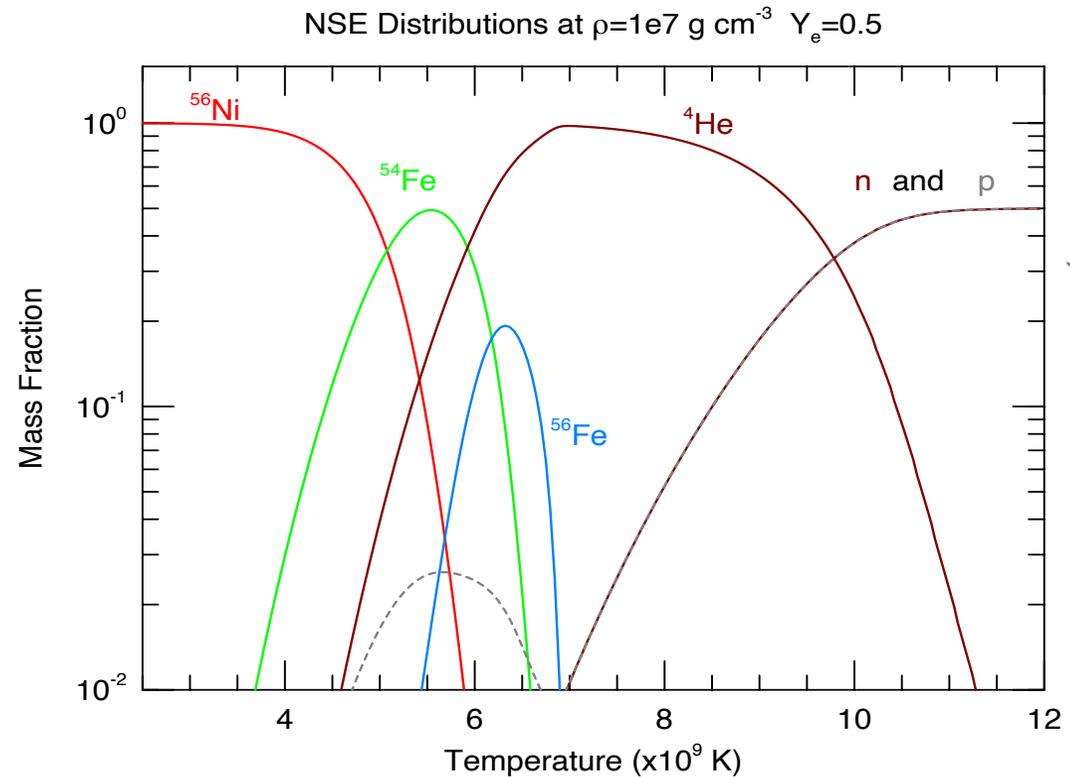


$$N\mu_n + Z\mu_Z = \mu_{Z,N}$$

where  $\mu$  is the chemical potential; nucleons and nuclei are described by Maxwell-Boltzmann distributions (note  $G_i$  is the partition function):

$$\mu_i = m_i c^2 + kT \ln \left[ \rho N_A \frac{Y_i}{G_i} \left( \frac{2\pi\hbar^2}{m_i kT} \right)^{3/2} \right]$$

\*The above equations are used along with  $\sum_i A_i Y_i = 1$  and  $\sum_i Z_i Y_i = Y_e$  to solve for abundances at a given  $\rho, T, Y_e$



For high temperatures, favors a composition of n, p, and  $\alpha$  due to photodissociation, for lower temperatures nuclei with the highest binding energy are favored ( $^{56}\text{Fe}$  for  $Y_e < 0.5$  and  $^{56}\text{Ni}$  for  $Y_e = 0.5$ )

Recall definitions for  $B + x \rightarrow C + D$ 

$$Q = (M_B + M_x - M_C - M_D)c^2 \quad r_{Bx} = \frac{n_B n_x}{1 + \delta_{Bx}} \langle \sigma v \rangle$$

$$n_B = \rho N_A \frac{X_B}{A_B} = \rho N_A Y_B \quad \lambda_{Bx} = \frac{1}{1 + \delta_{Bx}} Y_x \rho N_A \langle \sigma v \rangle$$

*Reverse rate* for  $C + D \rightarrow B + x$  from detailed balance (equilibrium): Saha Equation

If  $B \neq x$  and  $C \neq D$  with all being nuclei:

$$r_{Bx} = r_{CD} \Rightarrow \frac{n_C n_D}{n_B n_x} = \frac{\langle \sigma v \rangle_{Bx}}{\langle \sigma v \rangle_{CD}} \quad \text{along with} \quad \frac{\sigma_{Bx}}{\sigma_{CD}} = \frac{g_C g_D}{g_B g_x} \frac{A_C A_D E_{CD}}{A_B A_x E_{Bx}}$$

where  $g=2J+1$ ; can then obtain:

$$\frac{n_C n_D}{n_B n_x} = \frac{\langle \sigma v \rangle_{Bx}}{\langle \sigma v \rangle_{CD}} = \frac{g_C g_D}{g_B g_x} \left( \frac{A_C A_D}{A_B A_x} \right)^{3/2} e^{+Q/kT}$$

\*See Fowler, Caughlan, and Zimmerman (1967) for more details

Recall definitions for  $B + x \rightarrow C + D$ 

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If instead C is a photon:

$$r_{Bx} = r_{D\gamma} \Rightarrow \frac{n_D}{n_B n_x} = \frac{\langle \sigma v \rangle_{Bx}}{\lambda_\gamma}$$

Gives:

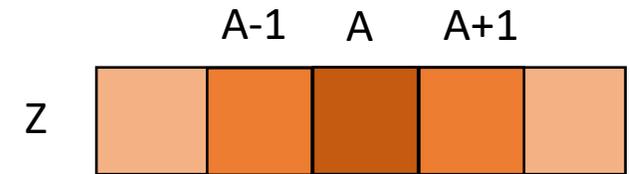
$$\frac{n_D}{n_B n_x} = \frac{\langle \sigma v \rangle_{Bx}}{\lambda_\gamma} = \frac{g_D}{g_B g_x} \left( \frac{A_D}{A_B A_x} \right)^{3/2} \left( \frac{2\pi\hbar^2}{mkT} \right)^{3/2} e^{+Q/kT}$$

\*See Fowler, Caughlan, and Zimmerman (1967) for more details

Classical approach to  $r$ -process calculations:  $(n, \gamma) \rightleftharpoons (\gamma, n) + \text{steady } \beta \text{ flow}$

Assume  $(n, \gamma) \rightleftharpoons (\gamma, n)$  equilibrium to obtain relative abundances of neighboring isotopes:

$$\frac{Y_{A+1}}{Y_A} = \frac{n_{A+1}}{n_A} \approx n_n \frac{g_{A+1}}{g_A g_n} \left(\frac{A+1}{A}\right)^{3/2} \left(\frac{2\pi\hbar^2}{Am_n m_n kT} (A+1)m_n\right)^{3/2} e^{+S_n/kT}$$



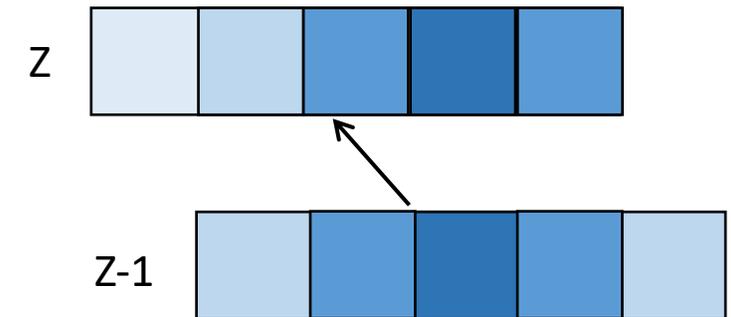
\*Sets the relative abundances along an isotopic chain

The evolution of abundances is determined from flow of  $\beta$ -decay:

$$\frac{dn(Z)}{dt} = \lambda_{Z-1}n(Z-1) - \lambda_Z n(Z) \quad \text{where} \quad \lambda_Z = \sum_A n(Z, A)\lambda_\beta(Z, A)$$

*Steady flow equilibrium* (or  $\beta$ -flow equilibrium) assumes  $\lambda_Z n(Z) \sim \text{constant}$

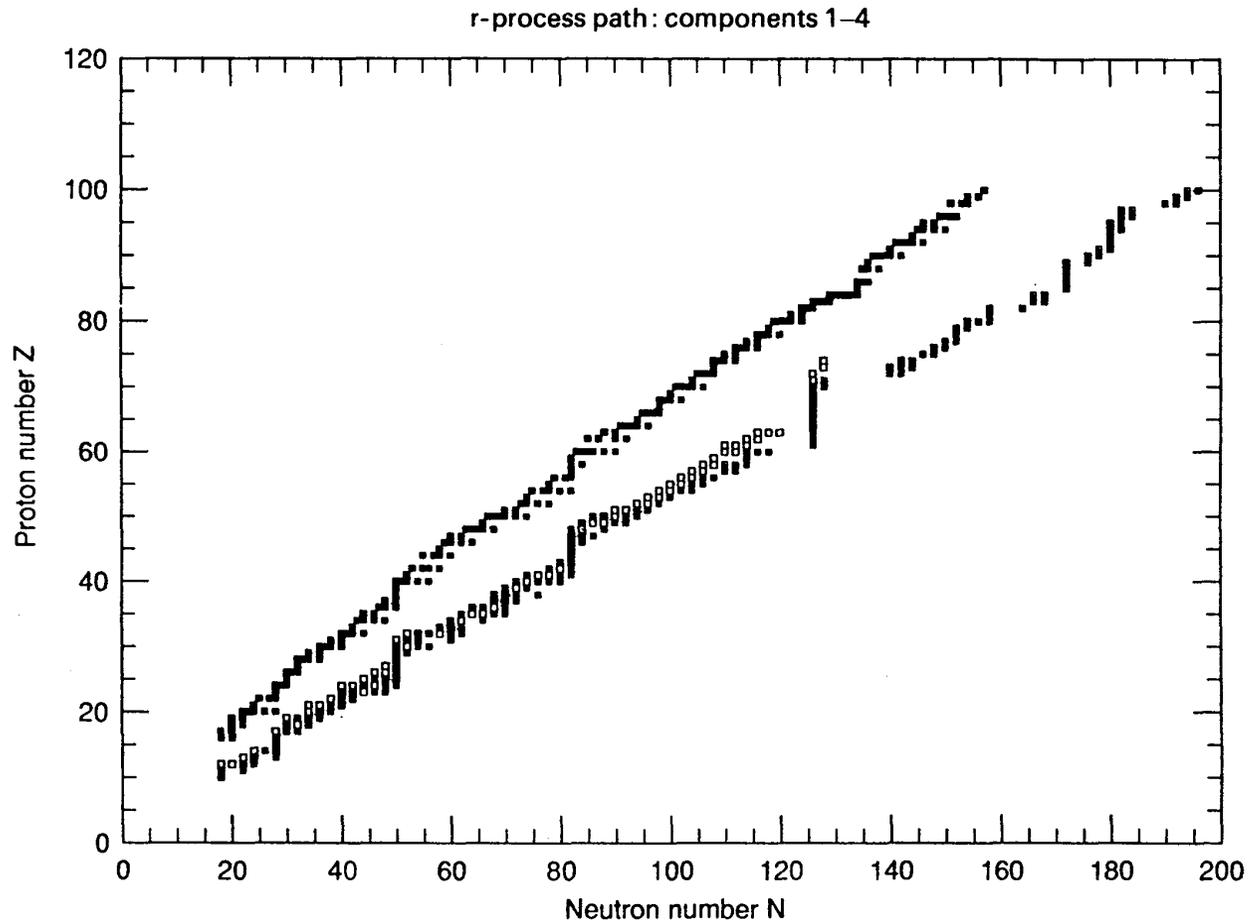
\*Note: also called “waiting point approximation” since the nucleus with the maximum abundance in each isotopic chain must wait for the longest  $\beta$ -decay



\*Allows for the chain to move to elements with higher proton numbers or in the case of steady flow sets relative Z abundances

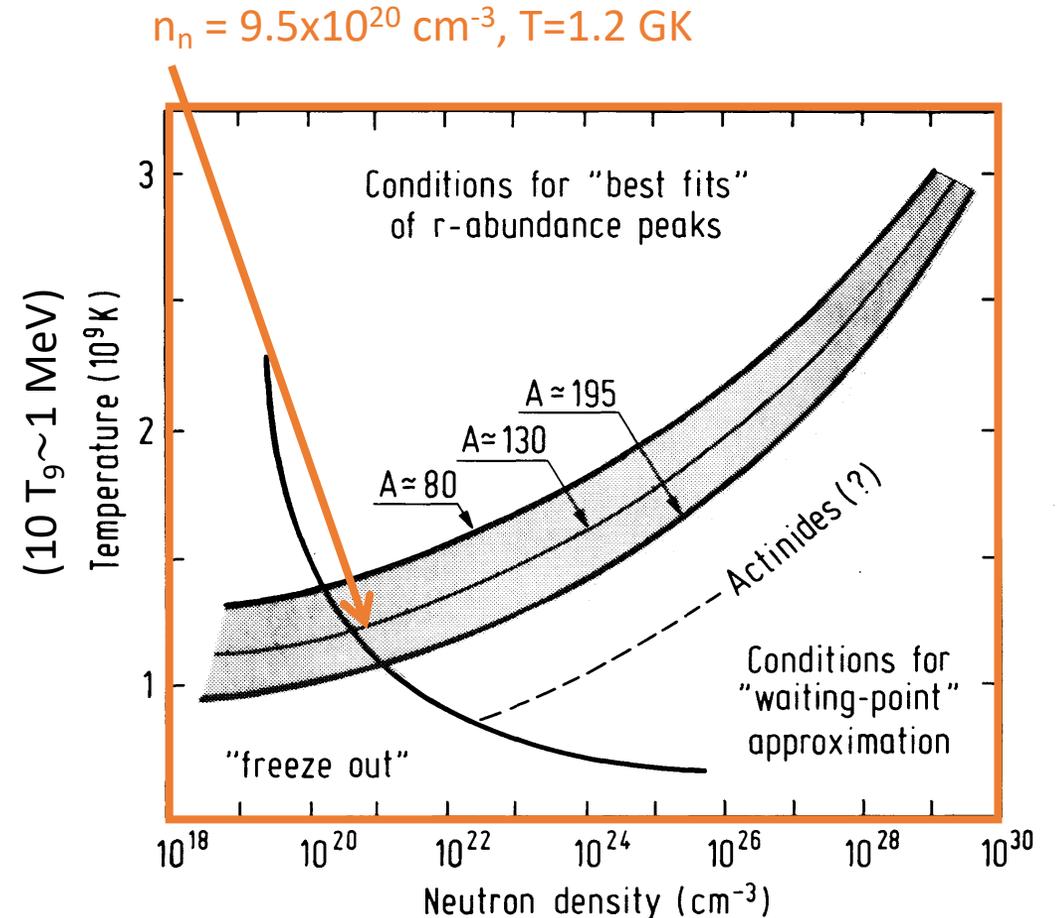
# The $r$ -process “path”

= Location of the maximum abundance for all isotopic chains  
(what  $N$  is most populated for a given  $Z$ )



Classical calculation (with steady flow equilibrium) of the different paths for **four  $n_n$ - $T$  values which reproduce solar features**

Kratz, Bitouzet, Thielemann, Möller, and Pfeiffer (1993)



\*Note “freeze-out” is when equilibrium fails, can be prompted by neutron-to-seed ratio  $\rightarrow 1$

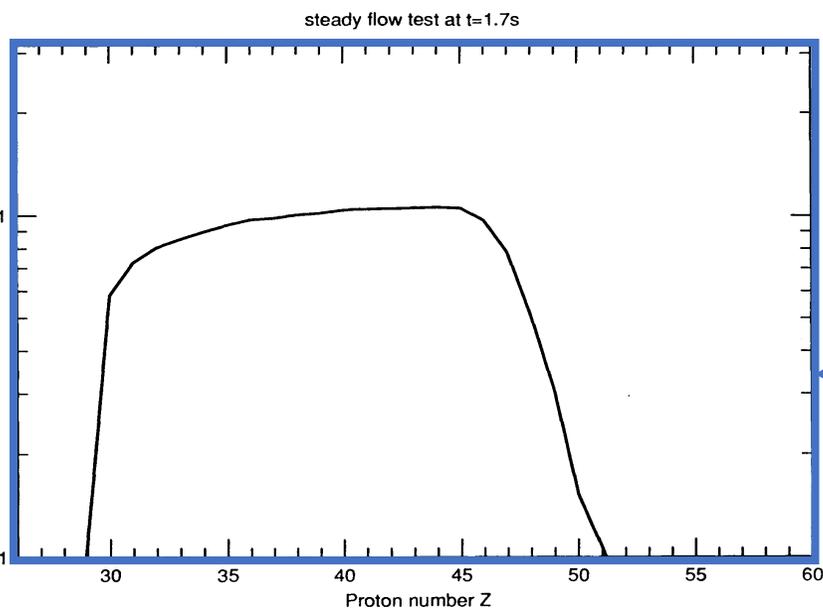
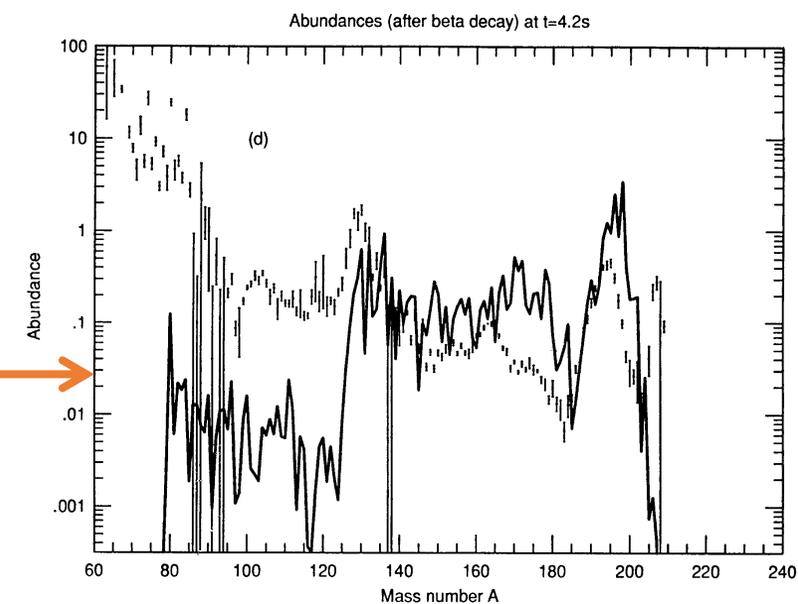
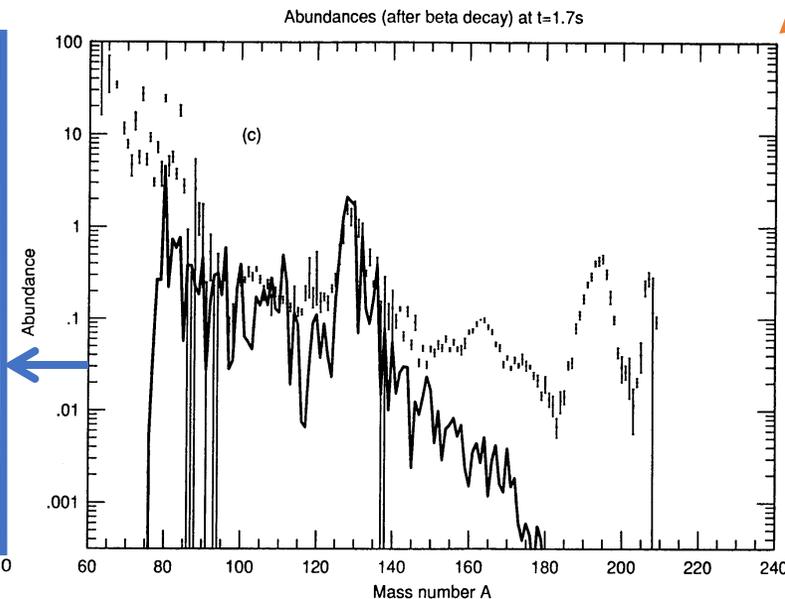
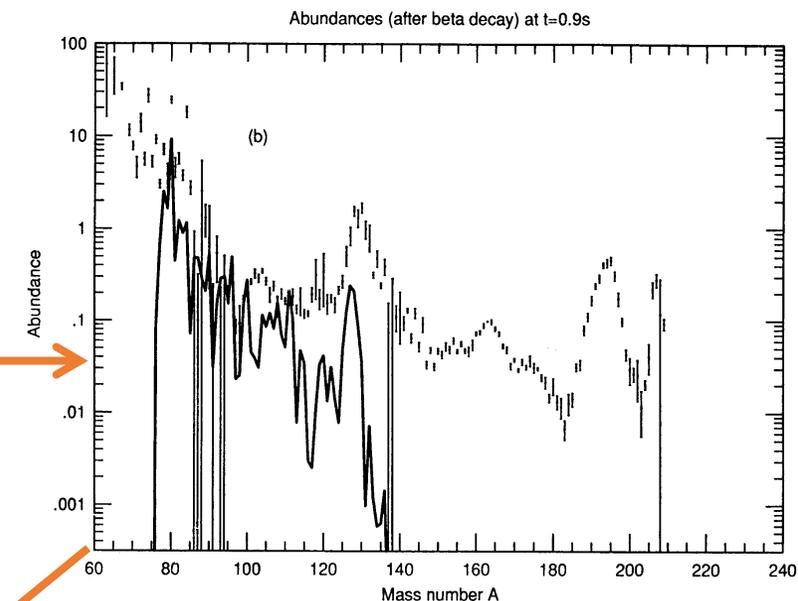
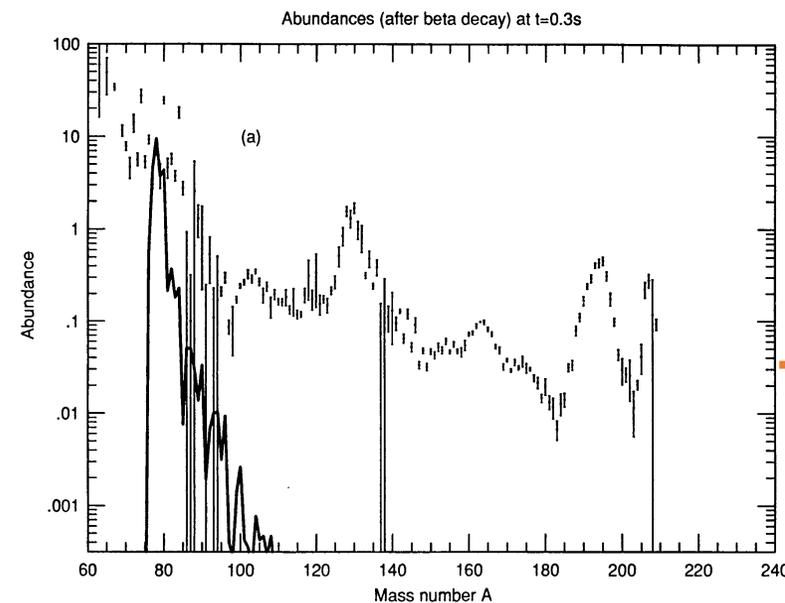
# An example of a classical $r$ -process calculation

Here abundances from detailed balance are evolved in time by

applying  $\frac{dn(Z)}{dt} \neq 0$

The steady flow condition

$\lambda_Z n(Z) \sim \text{constant}$  can then be tested for this case



## A short intro to reaction networks

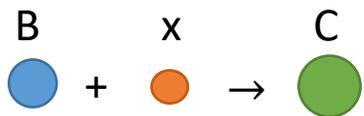
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$$\lambda_{Bx} = \frac{1}{1 + \delta_{Bx}} Y_x \rho N_A \langle \sigma v \rangle$$

For the **two-body reaction**



$$\frac{dn_B}{dt} = -n_B \lambda_{Bx} = -n_B Y_x \rho N_A \langle \sigma v \rangle$$

$$\frac{dn_C}{dt} = +n_B \lambda_{Bx}$$

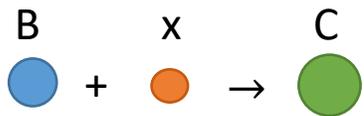
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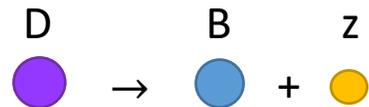
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For the **two-body reaction**



Now if a **one-body decay** produces B



$$\frac{dn_B}{dt} = -n_B \lambda_{Bx} = -n_B Y_x \rho N_A \langle \sigma v \rangle$$

$$\frac{dn_C}{dt} = +n_B \lambda_{Bx}$$

$$\frac{dn_B}{dt} = -n_B Y_x \rho N_A \langle \sigma v \rangle + n_D \lambda_D$$

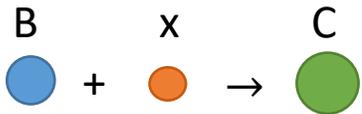
$$\frac{dn_D}{dt} = -n_D \lambda_D$$

# A short intro to reaction networks

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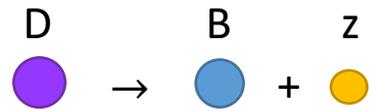
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Now if a **one-body decay** produces B



$$\frac{dn_B}{dt} = -n_B Y_x \rho N_A \langle \sigma v \rangle + n_D \lambda_D$$

$$\frac{dn_D}{dt} = -n_D \lambda_D$$

Thus network equations can be written as:

$$\dot{Y}_i = \sum_j \xi_j^i \lambda_j Y_j + \sum_{j,k} \xi_{j,k}^i \rho N_A \langle \sigma v \rangle_{j,k} Y_j Y_k + \sum_{j,k,l} \xi_{j,k,l}^i \rho^2 N_A^2 \langle \sigma v \rangle_{j,k,l} Y_j Y_k Y_l$$

Where  $\xi$  is + when i created, - when i consumed, and corrects for overcounting in a reaction involving identical particles

\*Coupled differential equations can be put into matrix form so networks use matrix solvers

# A short intro to reaction networks

$$Q = (M_B + M_x - M_C - M_D)c^2 \quad r_{Bx} = \frac{n_B n_x}{1 + \delta_{Bx}} \langle \sigma v \rangle$$

$$n_B = \rho N_A \frac{X_B}{A_B} = \rho N_A Y_B \quad \lambda_{Bx} = \frac{1}{1 + \delta_{Bx}} Y_x \rho N_A \langle \sigma v \rangle$$

Written out in a more schematic way, for the  $r$  process this means:

$$\begin{aligned} \dot{Y}_i = & \sum(\text{2body reactions into } i) - \sum(\text{2body reactions out of } i) && (\text{ex: n capture, photodissociation}) \\ & + \sum(\text{3body reactions into } i) - \sum(\text{3body reactions out of } i) && (\text{ex: } \alpha\alpha n, (n,2n)) \\ & + \sum(\text{decays into } i) - \sum(\text{decays out of } i) && (\text{ex: } \beta\text{-decay, } \beta\text{-delayed n emission, } \alpha\text{-decay}) \\ & + \sum(\text{fission into } i) \text{ OR } - \sum(\text{fission out of } i) && (\text{ex: neutron-induced, } \beta\text{-delayed, spontaneous fission}) \end{aligned}$$

Some reaction network codes used for the  $r$ -process include PRISM, SkyNet, NucNetTools, Xnet, and WINNET; See e.g. Hix&Meyer 06, Lippuner&Roberts 18 for discussions of solving network equations

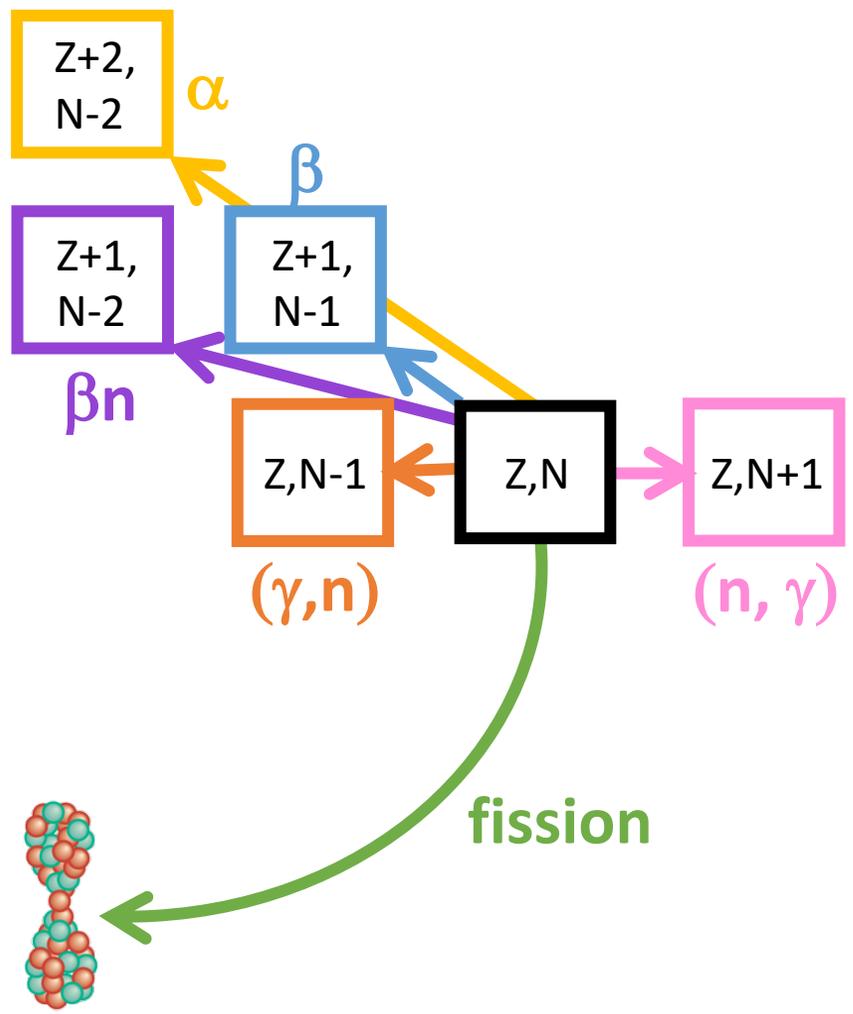
Thus network equations can be written as:

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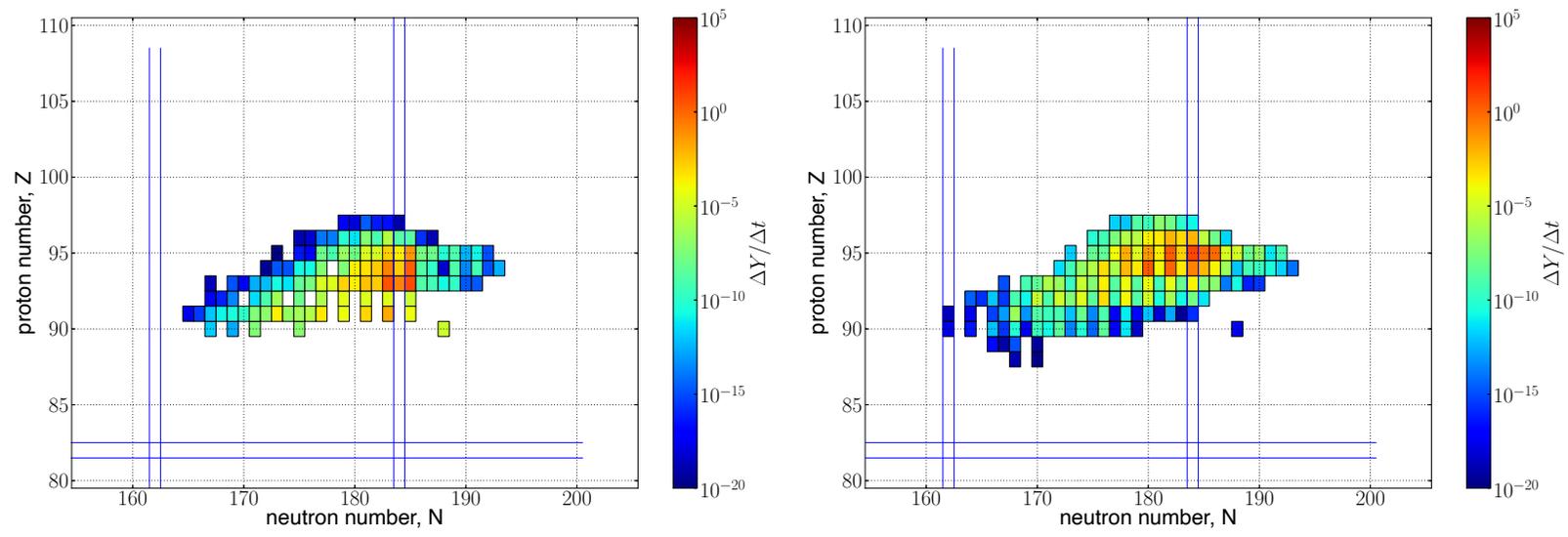
Where  $\xi$  is + when  $i$  created, - when  $i$  consumed, and corrects for overcounting in a reaction involving identical particles

\*Coupled differential equations can be put into matrix form so networks use matrix solvers

Analyzing the reactions in your network calculation:  
*Flows = rate x abundance*

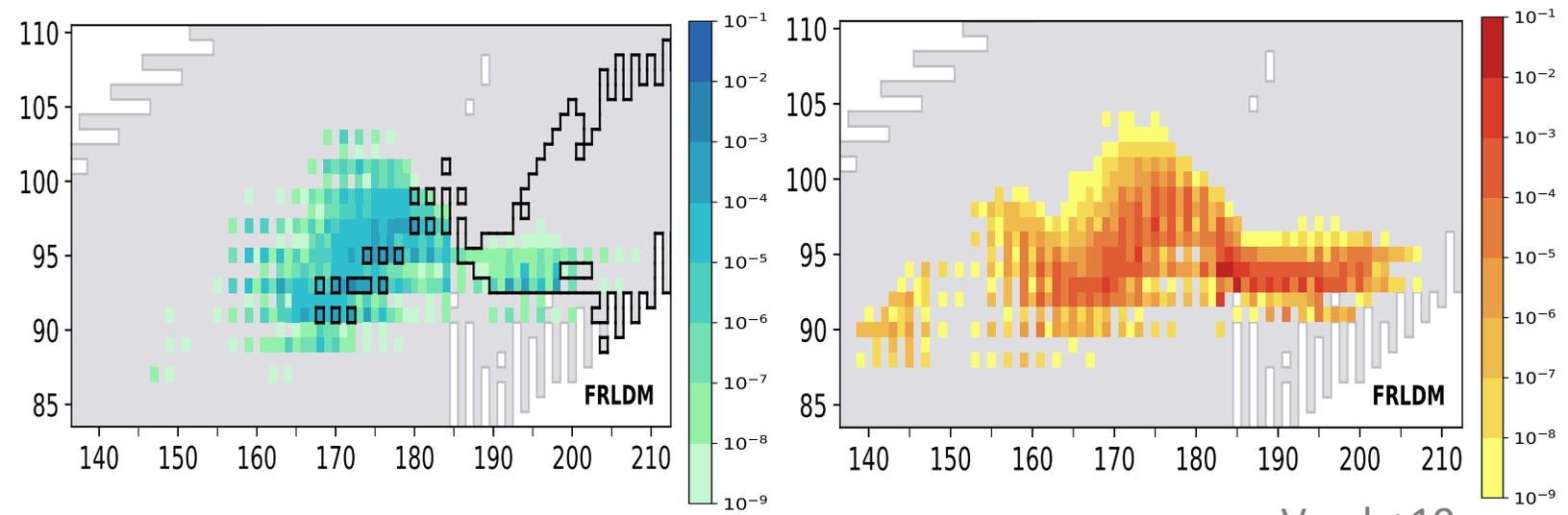


$\beta$ -delayed (left) and neutron-induced (right) fission flows *at an instance in time* (here  $t=1$  s)



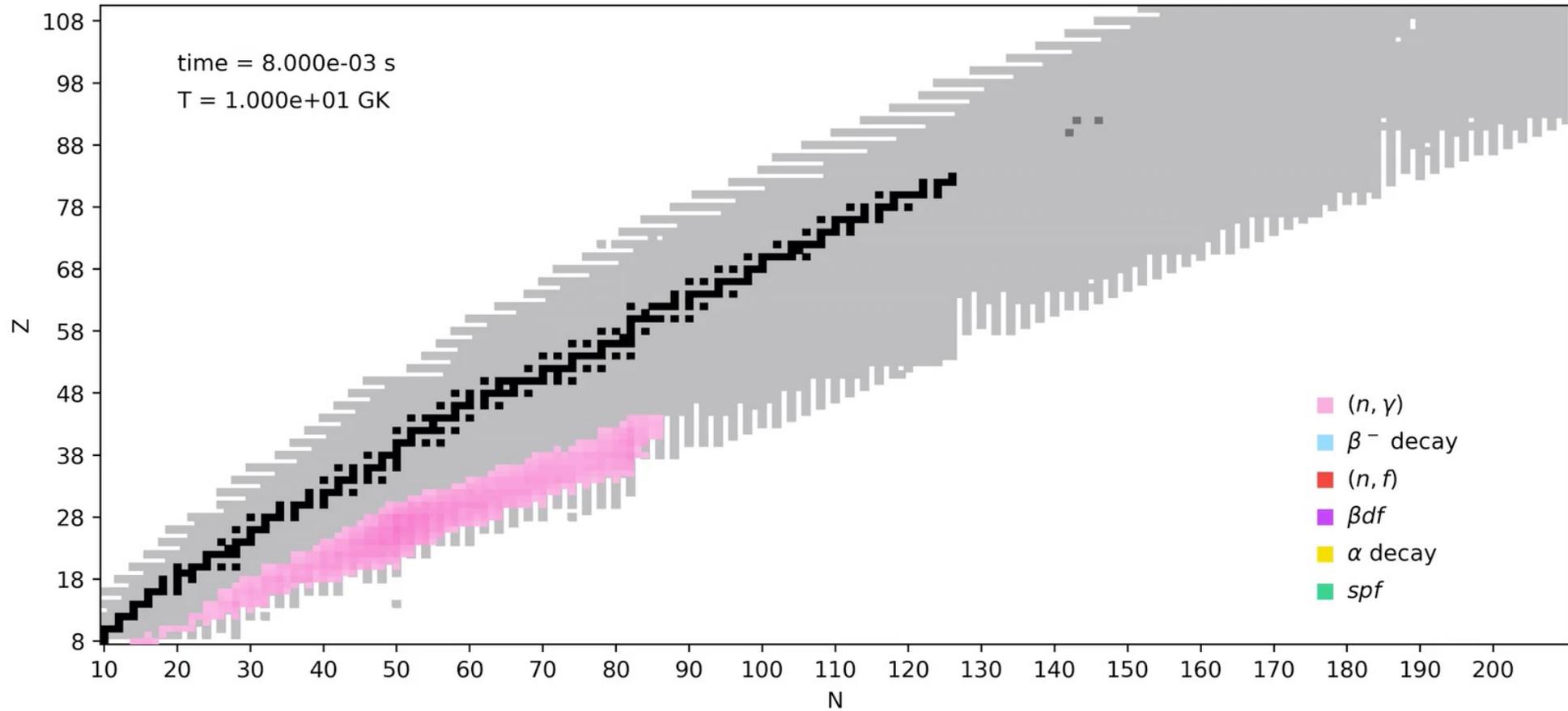
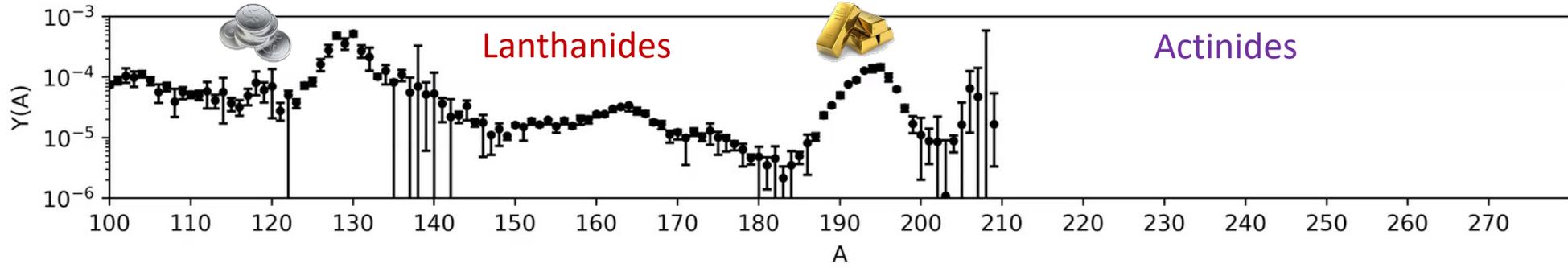
Eichler+15

$\beta$ -delayed (left) and neutron-induced (right) fission flows *integrated over time*



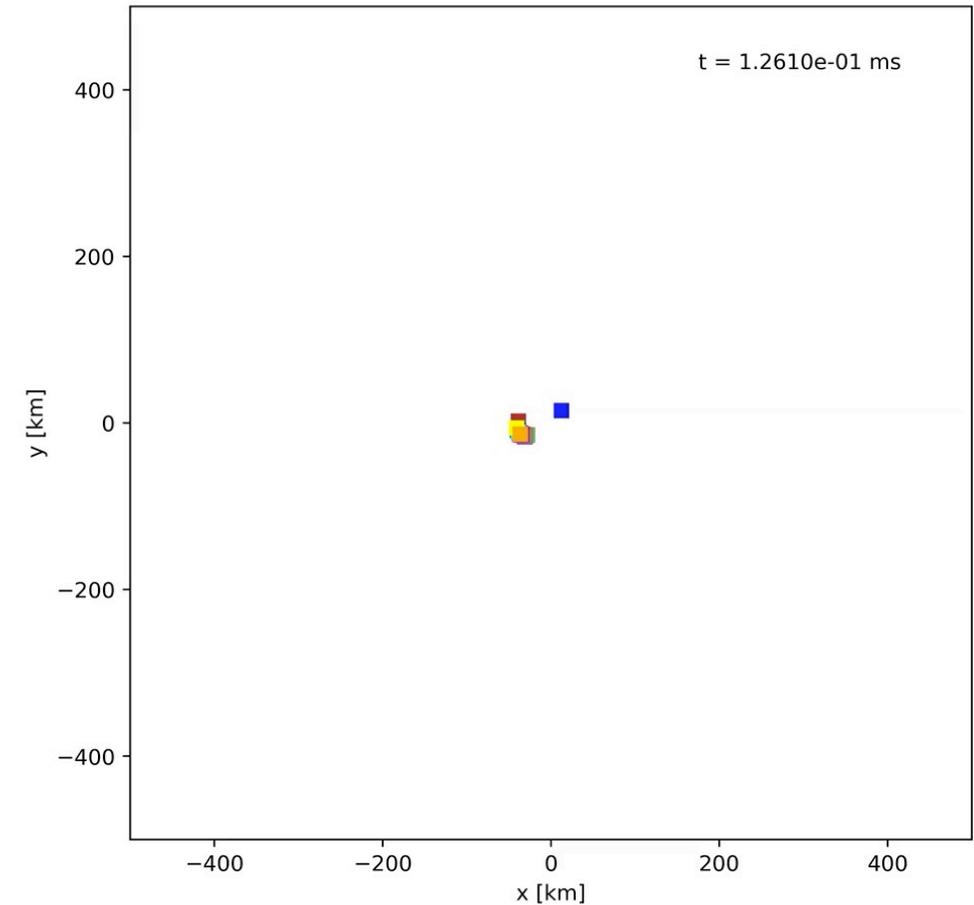
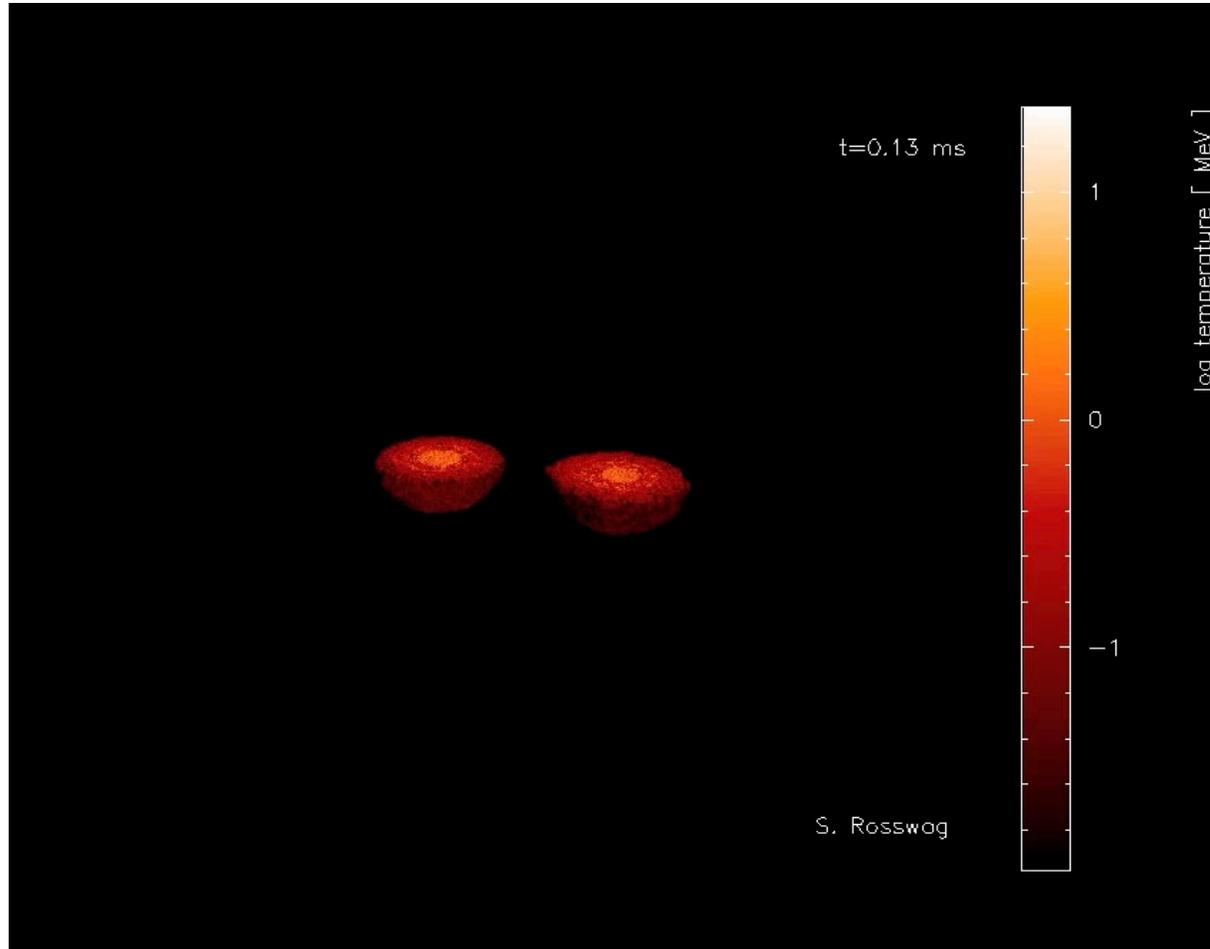
Vassh+19

# Putting it all together: evolution of abundances and dominant flows

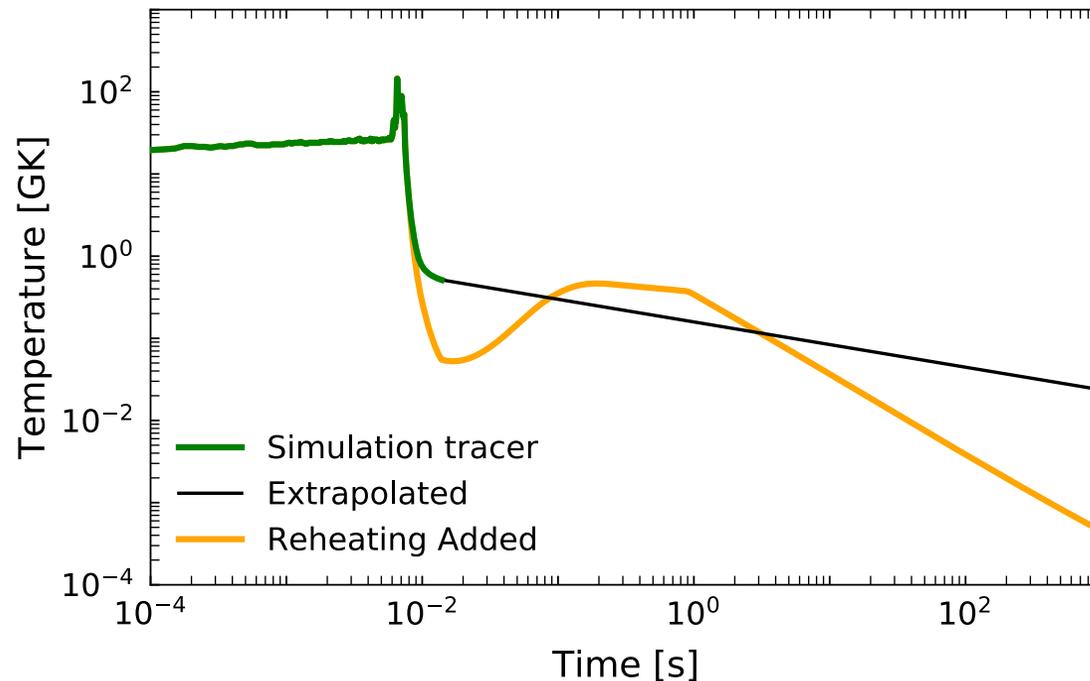
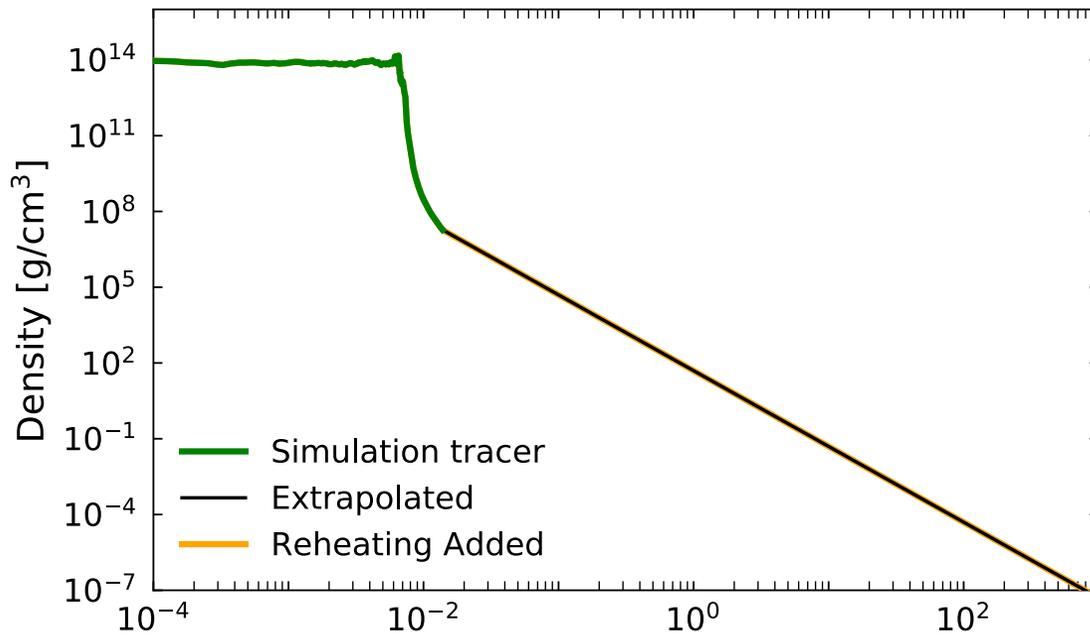


# Using simulation tracers

Networks permit *r*-process calculations to account for the *time evolution of the temperature and density of a particular mass element in an astrophysical environment (aka trajectory)*



# Using simulation tracers: Extrapolating trajectories and reheating



The density beyond the  $\sim$ ms timescale considered in hydrodynamic simulations is typically extrapolated assuming “free expansion” (homologous expansion such that  $r = vt$ ):

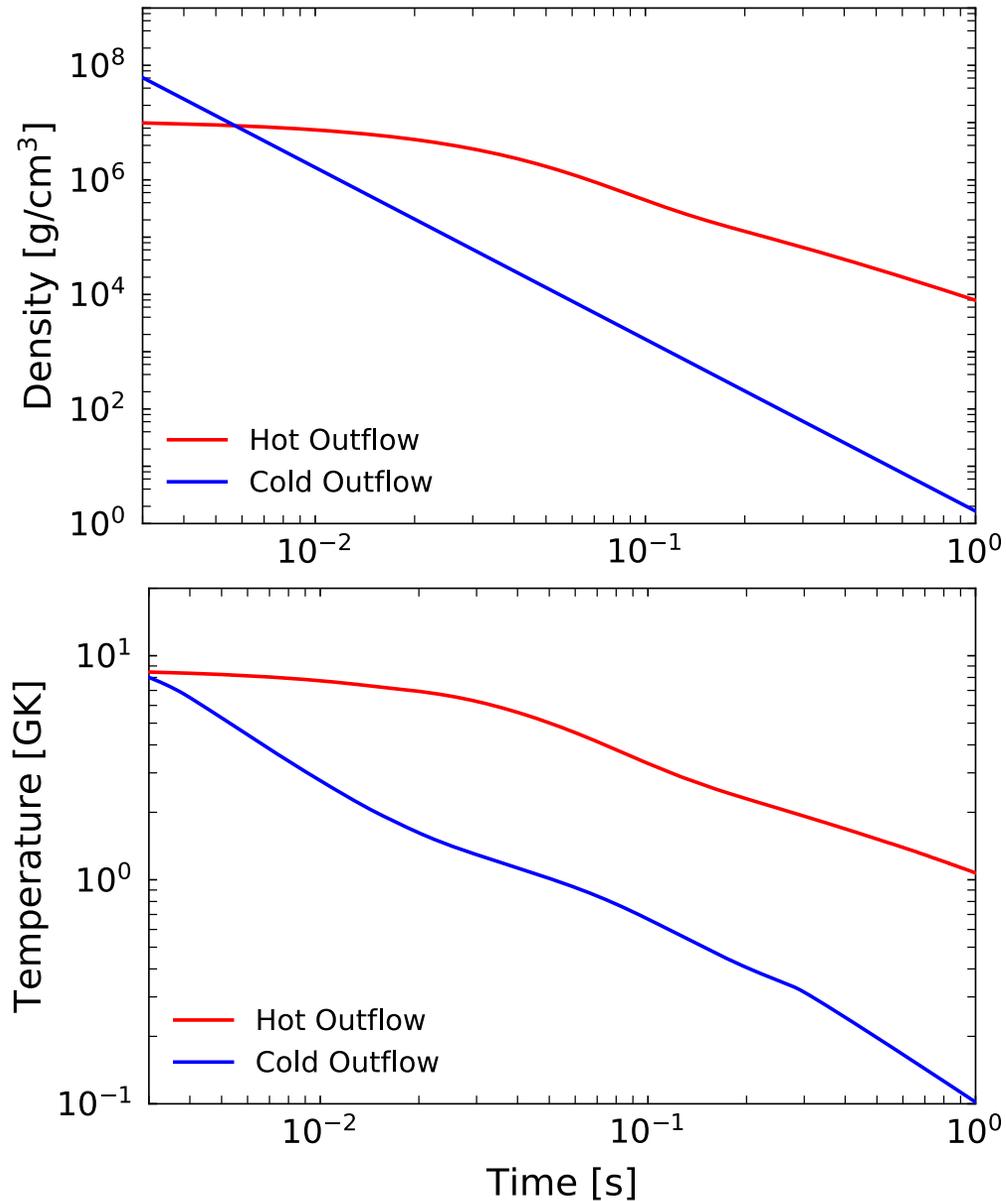
$$\rho(t) = \rho_0 \left( \frac{t}{t_0} \right)^{-3}$$

Given  $\rho(t)$ , the composition, and the entropy  $s_0$ , the change in entropy can be calculated via the nuclear equation of state (EOS) which is then linked to temperature ( $\Delta s = \frac{\Delta Q}{T}$ ) thus

$$T(t) = \text{EOS}[s_0, \rho(t), Y(t)]$$

This is called “reheating” or “self-heating” since the changes in the composition from nuclear reactions heat the system

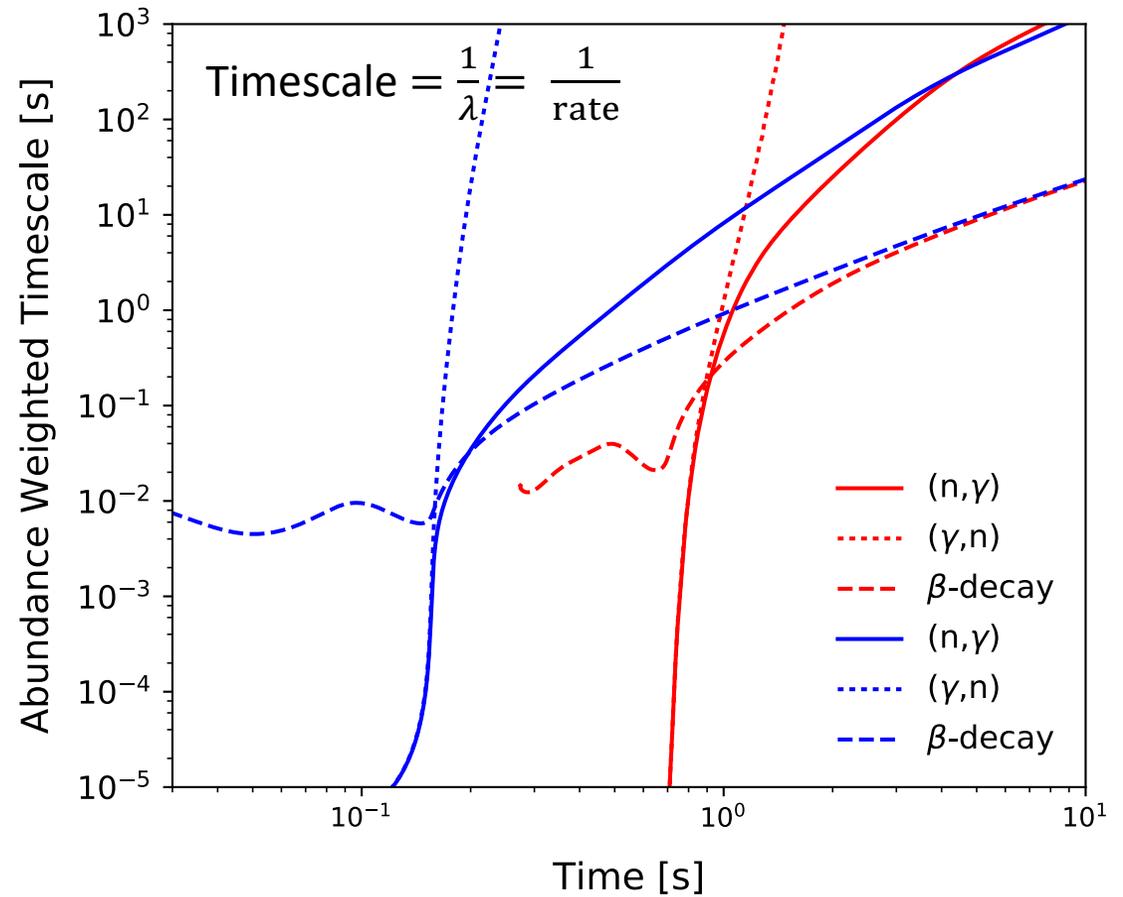
# Introduction to timescales and $r$ -process dynamics



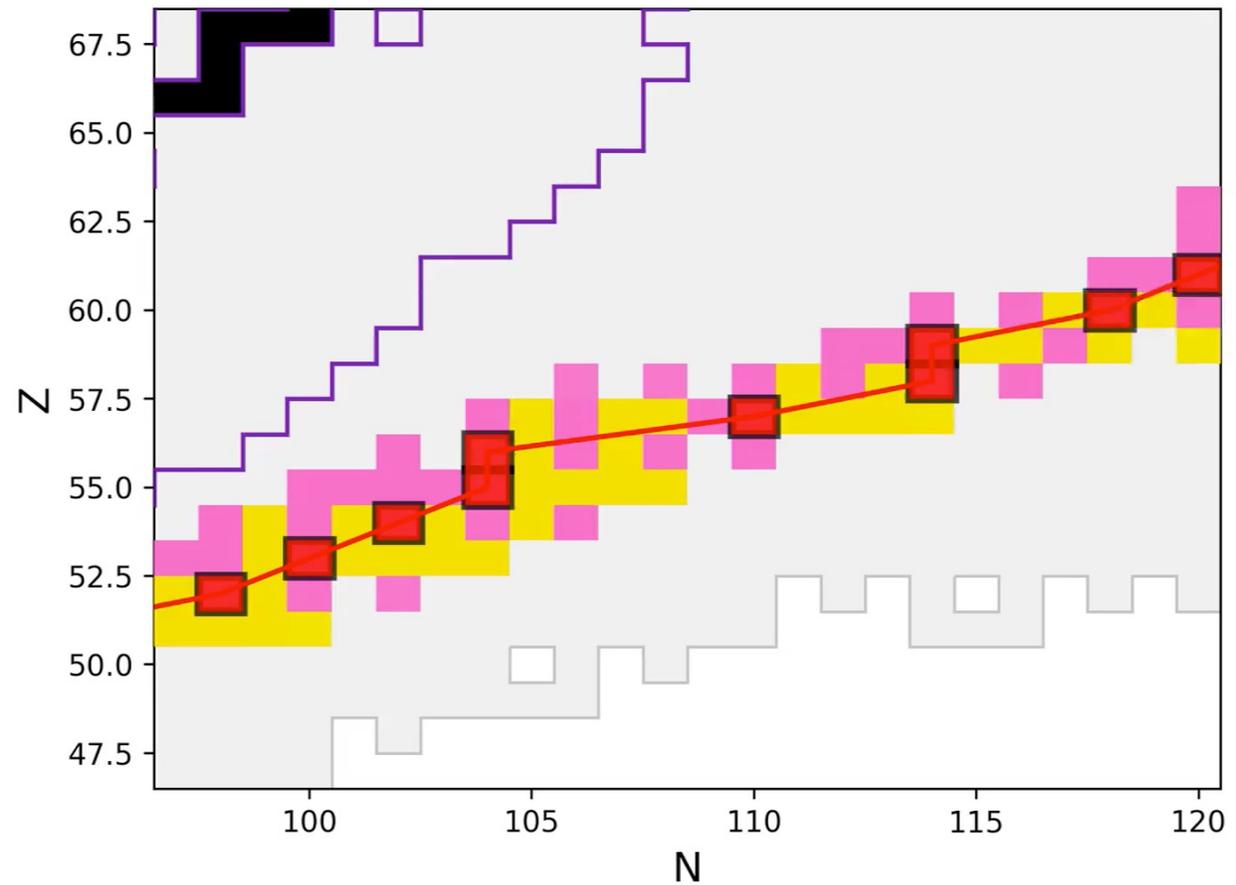
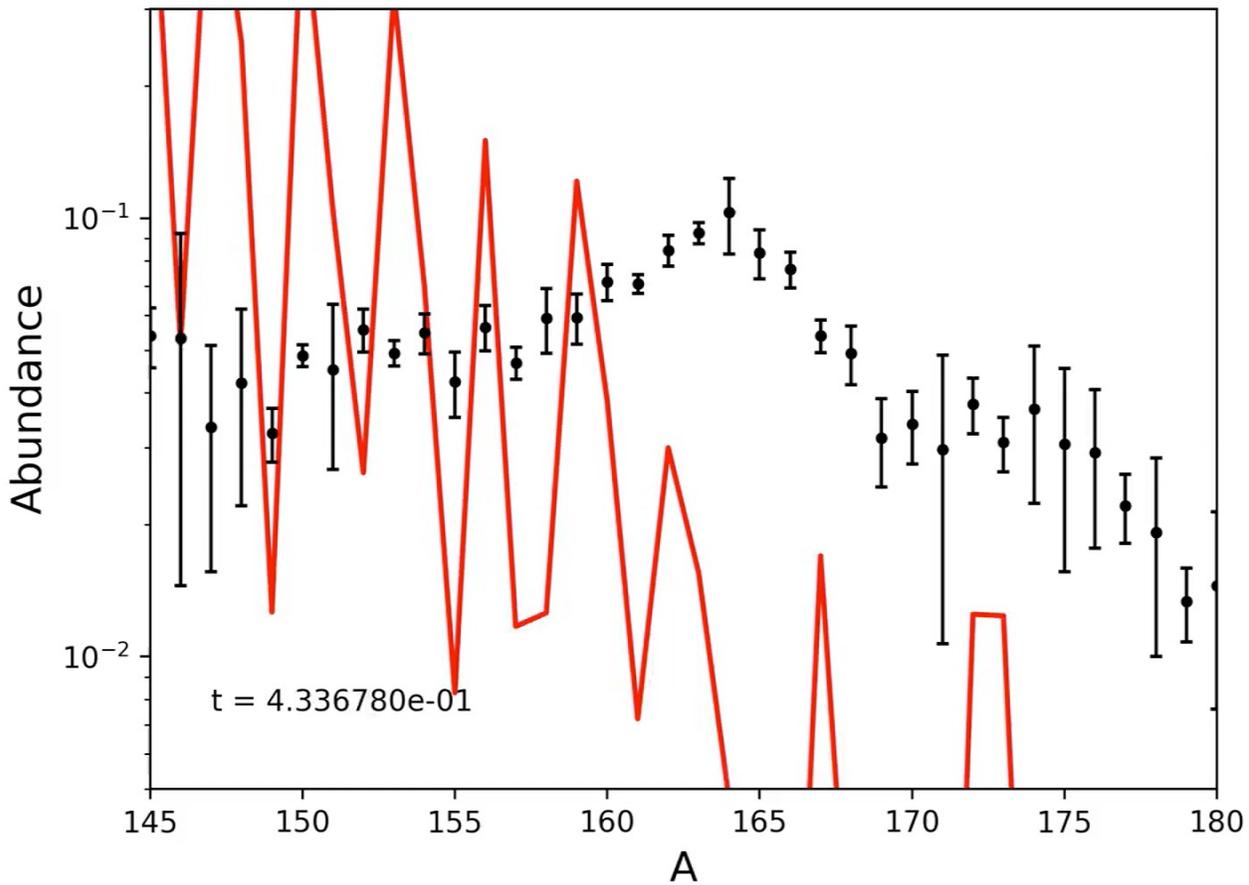
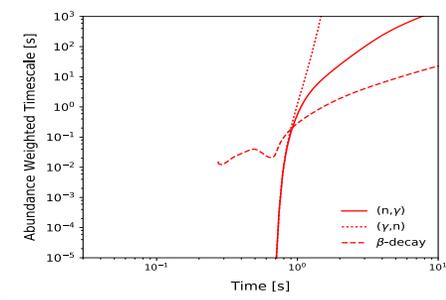
Consider two cases which both start  $n$ -rich ( $Y_e=0.2$ ) but differ in their initial entropy ( $s/k=10$  vs  $s/k=30$ ) as well as their density evolution ( $\tau=3$  ms vs  $\tau=70$  ms with  $\rho(t)\sim e^{-3t/\tau}$ )

“Hot” dynamics: extended  $(n, \gamma) \rightleftharpoons (\gamma, n)$  equilibrium

“Cold” dynamics: photodissociation falls out early

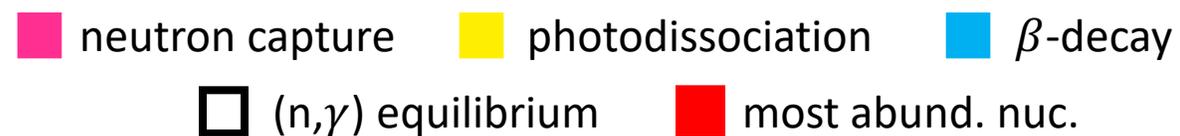
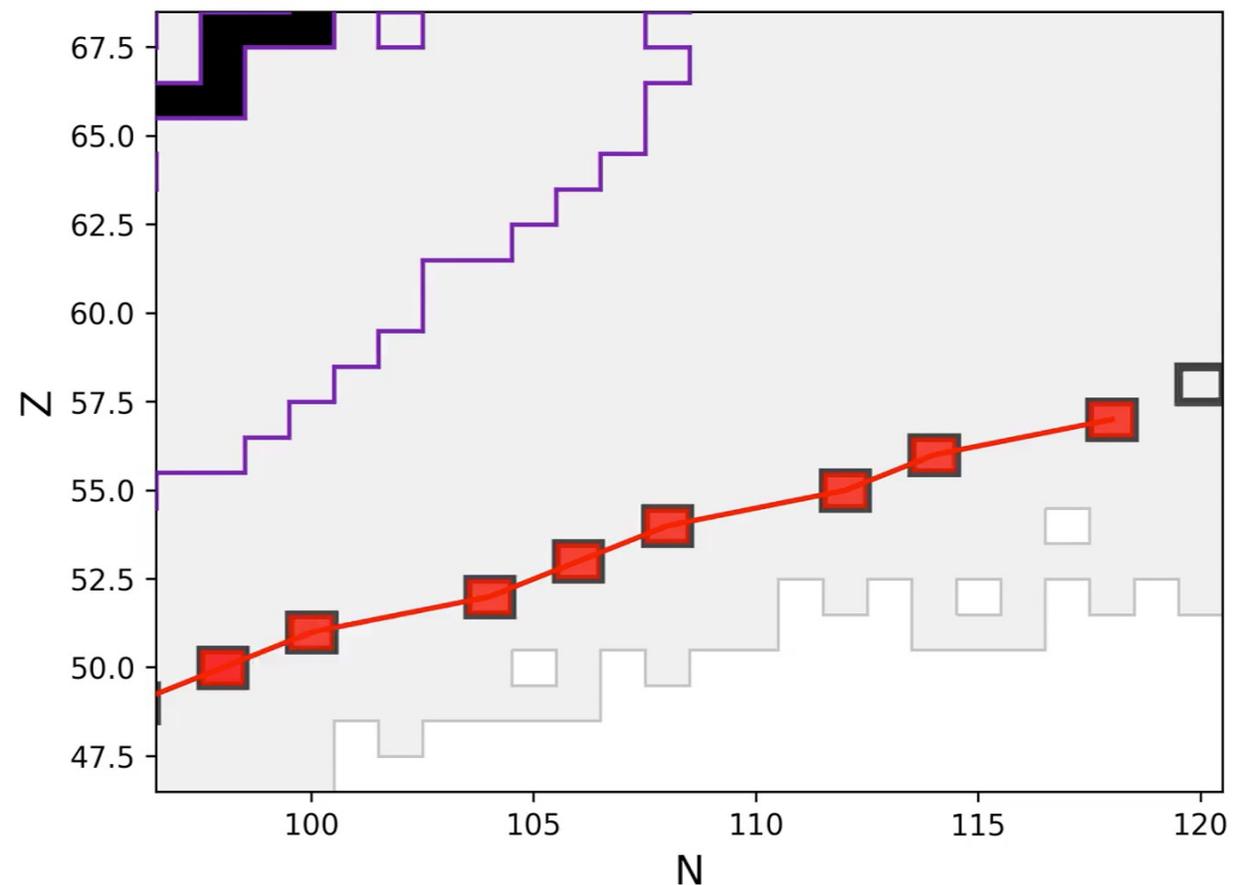
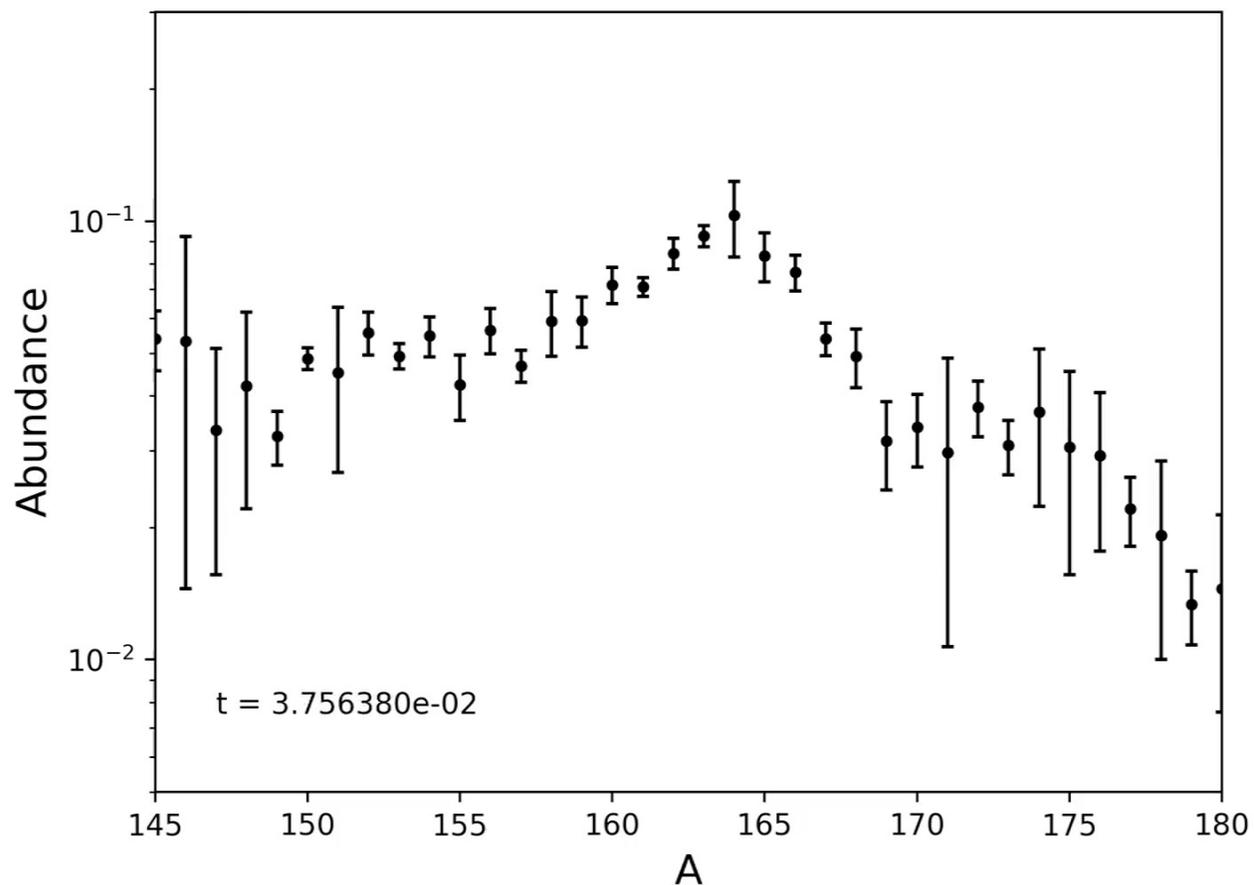
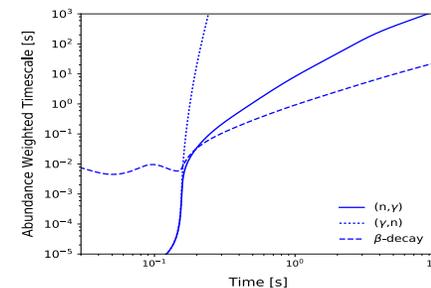


# Dynamics of a “hot” $r$ process with an extended $(n, \gamma) \rightleftharpoons (\gamma, n)$ equilibrium



- neutron capture
- photodissociation
- $\beta$ -decay
- $(n, \gamma)$  equilibrium
- most abund. nuc.

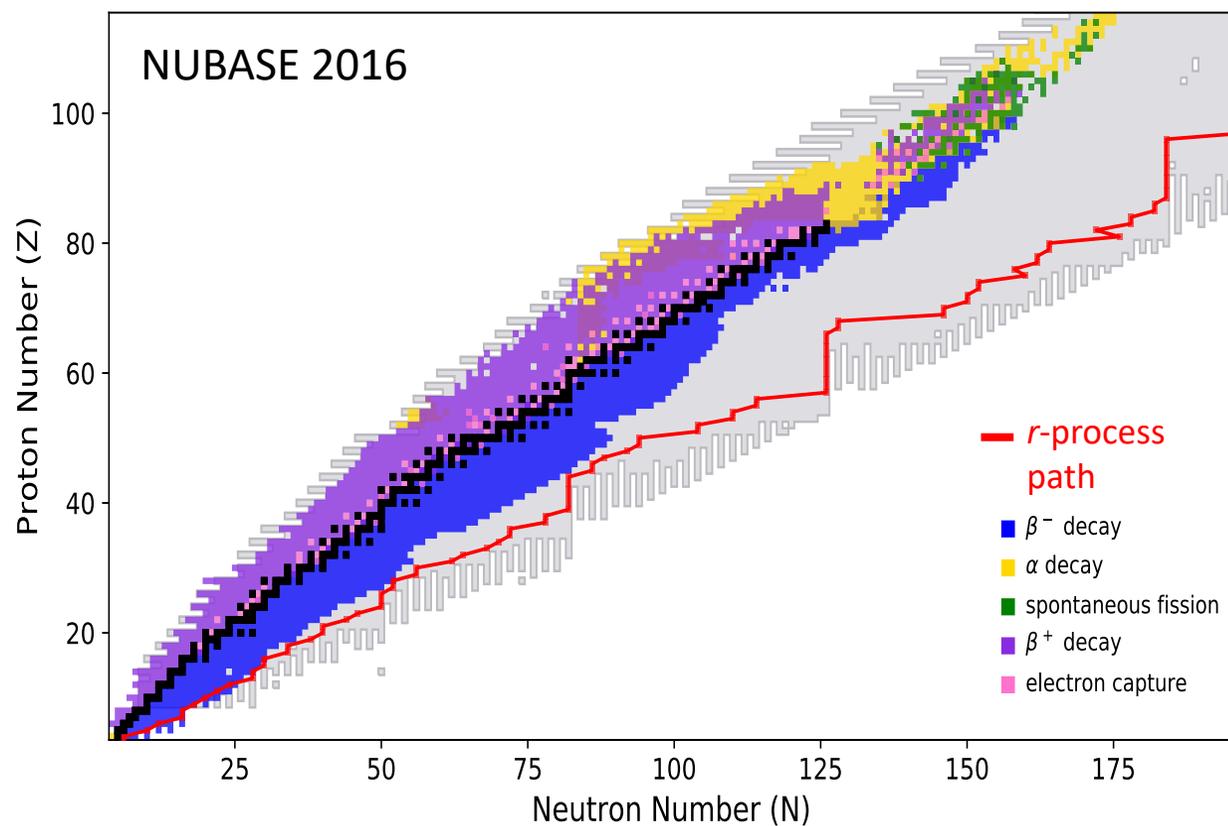
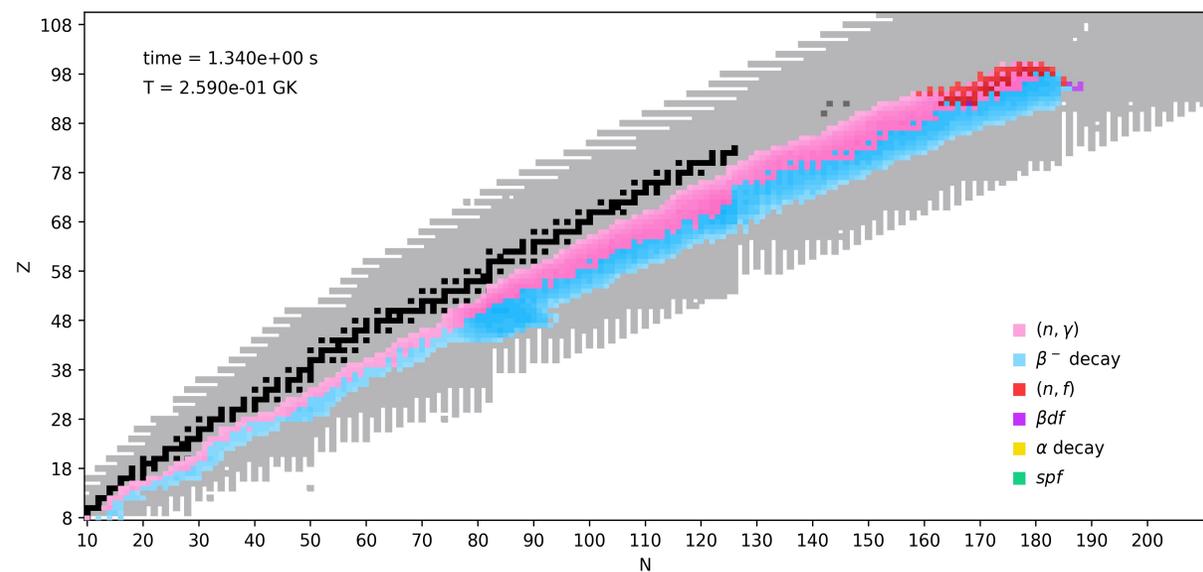
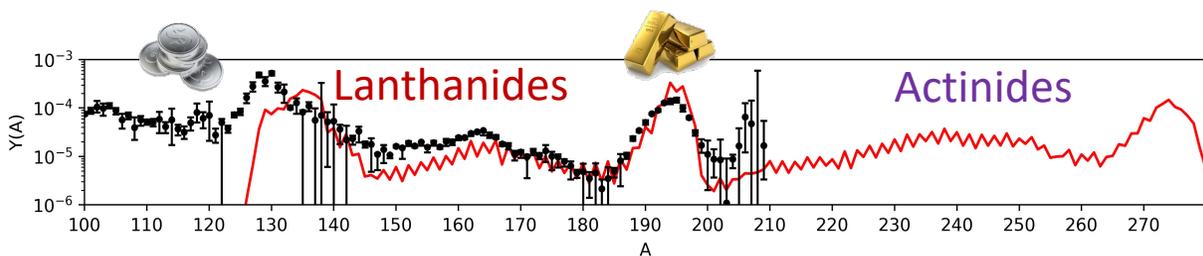
# Dynamics of a “cold” $r$ process where photodissociation falls out early



# Outline

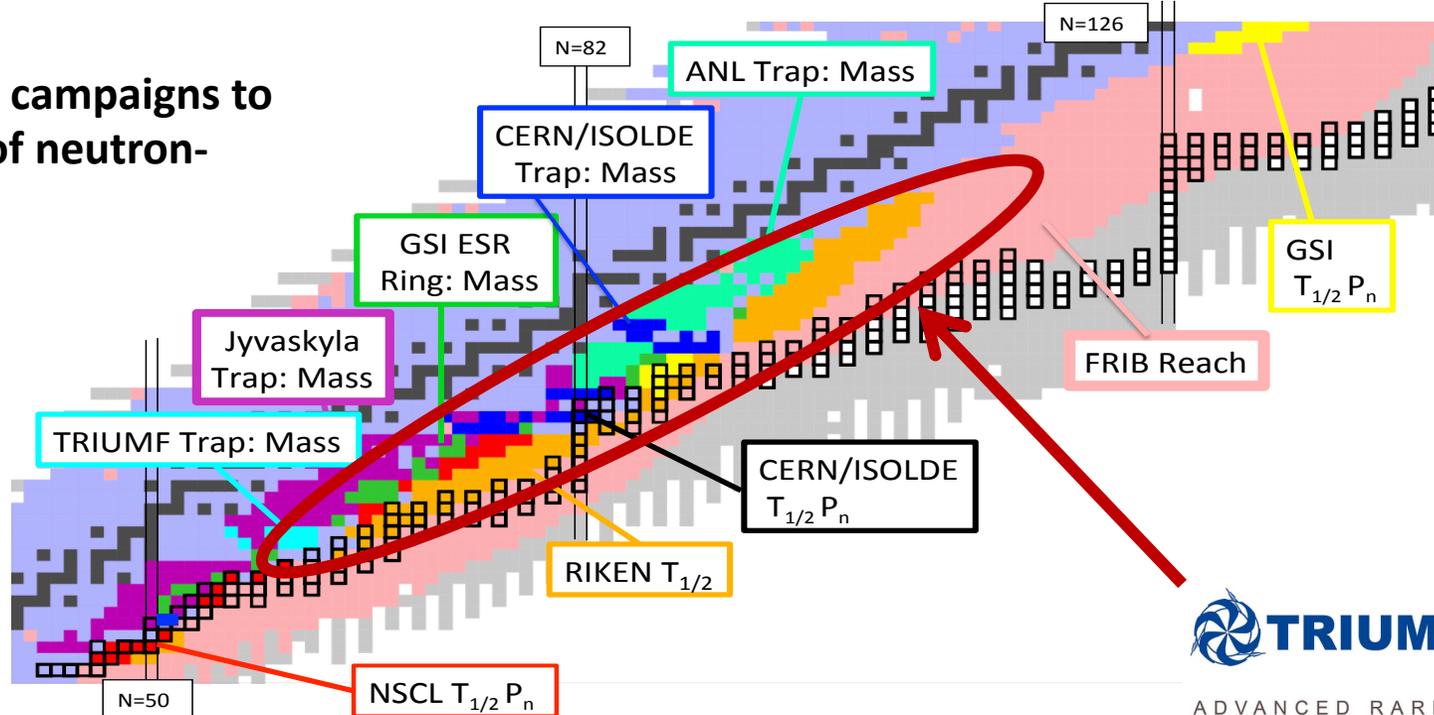
- Observational evidence that the  $r$  process occurs [4-9]
- Discussion of astrophysical sites (history (CCSNe), candidate sites, MHD SNe, NSNS/NSBH) [11-21]
- Spotlight on GW170817 and AT2017gfo: the first multi-messenger NSNS event [23-33]
- $r$ -process calculations (intro to reaction rates and equilibrium, history (classical  $r$  process), intro to using networks and trajectories,  $r$ -process dynamics) [35-52]
- The fundamental role of nuclear physics [54-82]

# Nuclei synthesized by the $r$ process compared to experimentally studied species

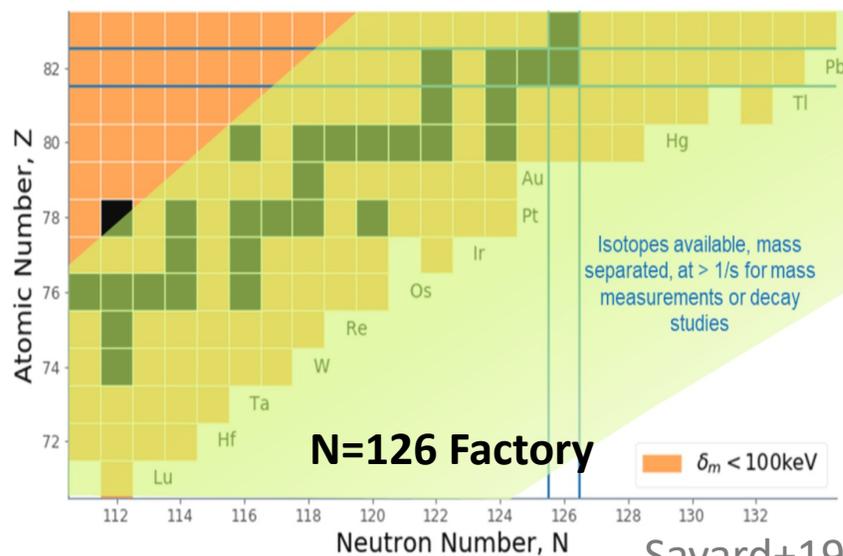


# Worldwide experimental campaigns to measure the properties of neutron-rich nuclei:

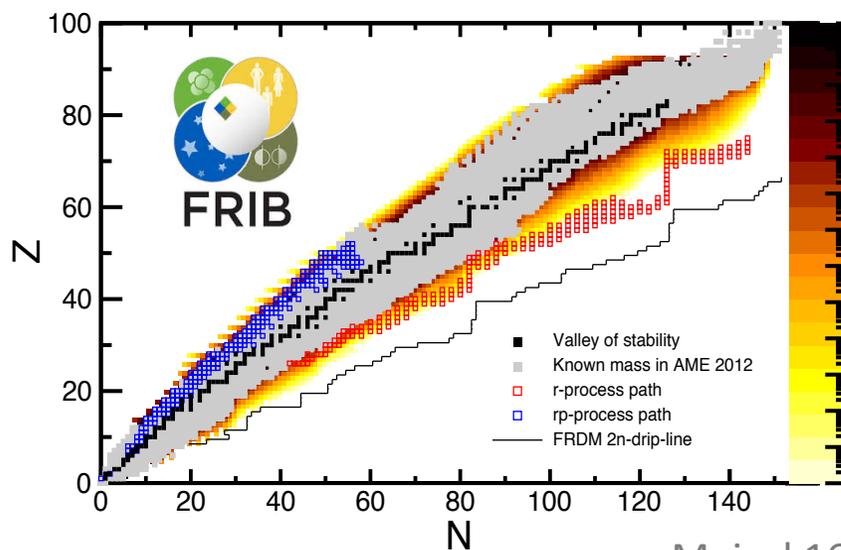
masses, half-lives, reaction rates...



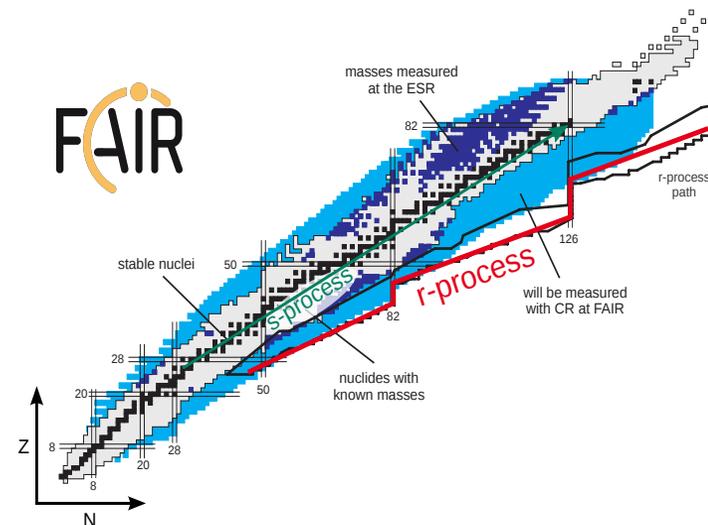
Horowitz+18



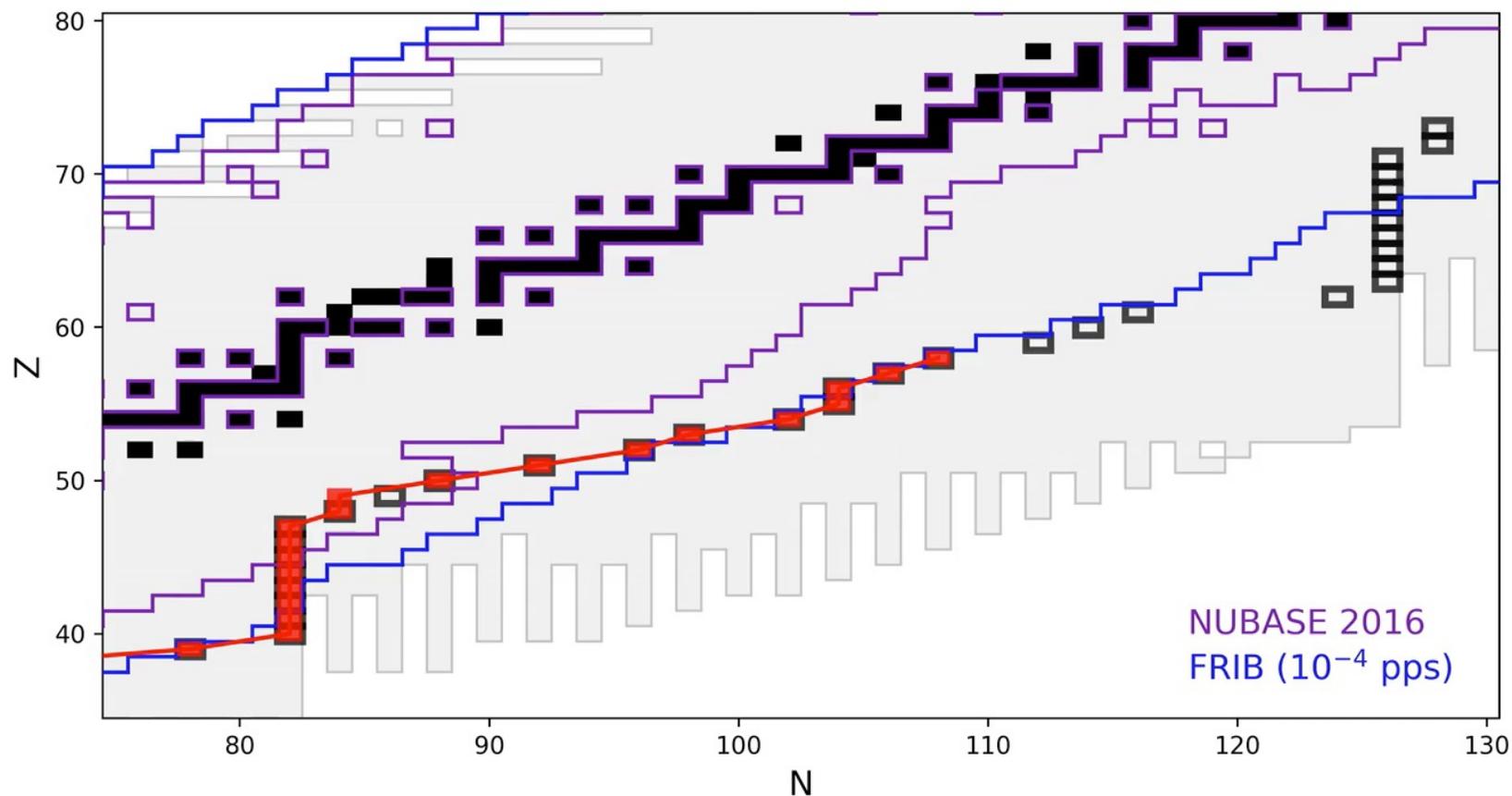
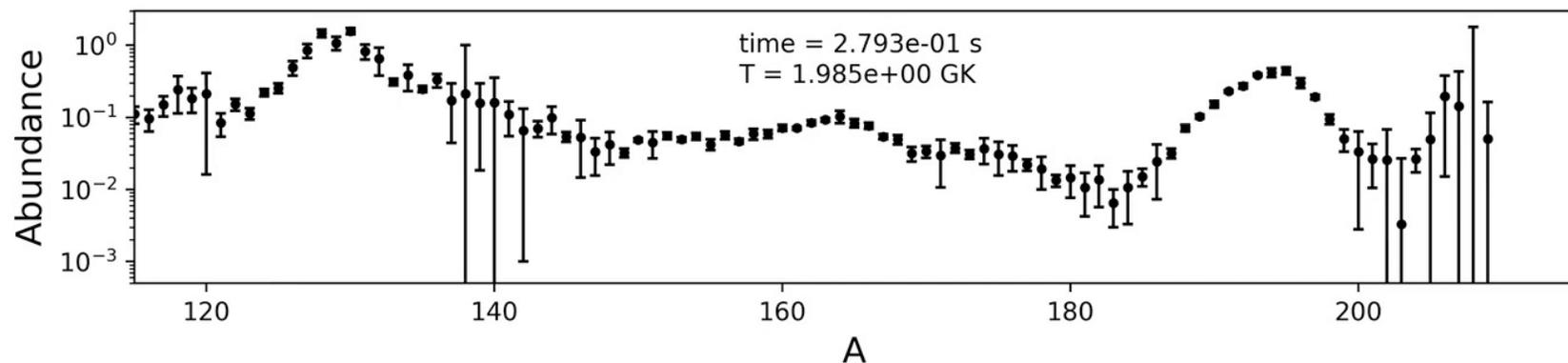
Savard+19



Meisel 16



# Future experiment meets the $r$ -process path

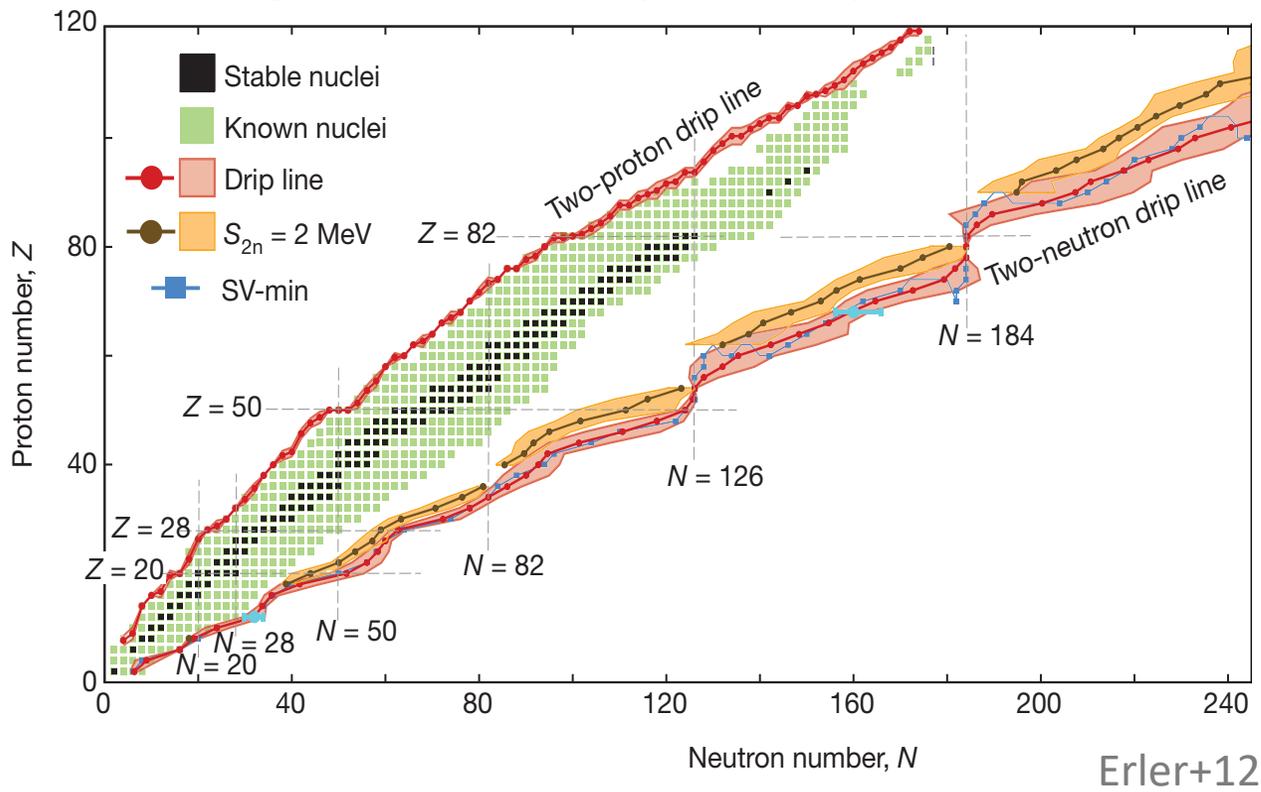


\*reach of future experiment in key regions impacting the evolution of abundances (note moderately n-rich conditions used here)

### Theory developments:

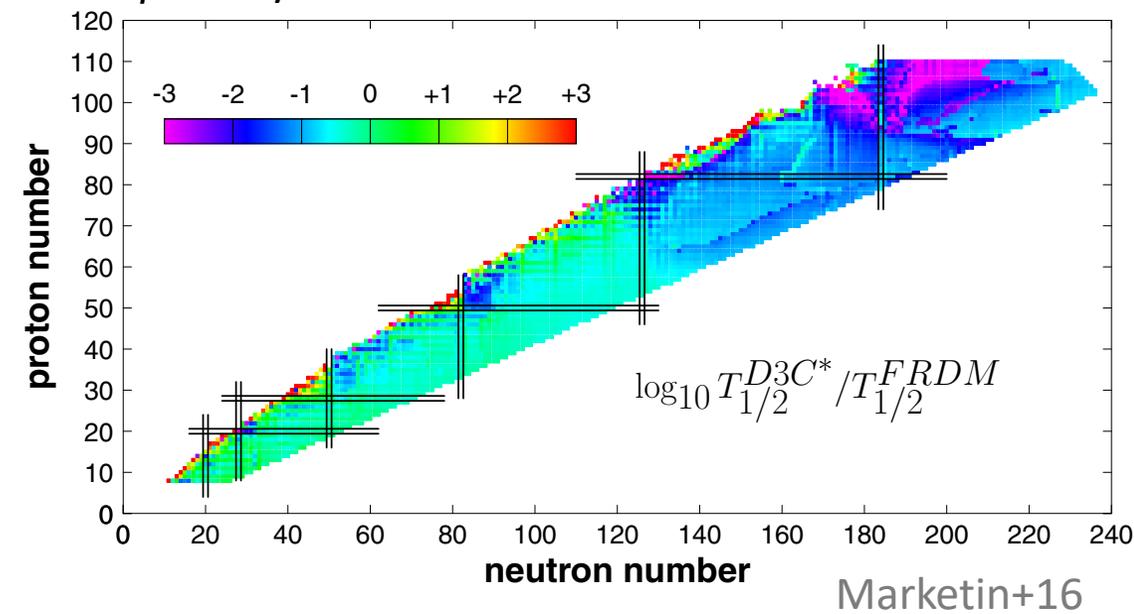
Structure theory (masses, deformation, level densities...),  
 reaction theory (capture cross sections...), fission yields  
 and rates, and  $\beta$ -decay rates....

### Modeling masses all the way to the dripline



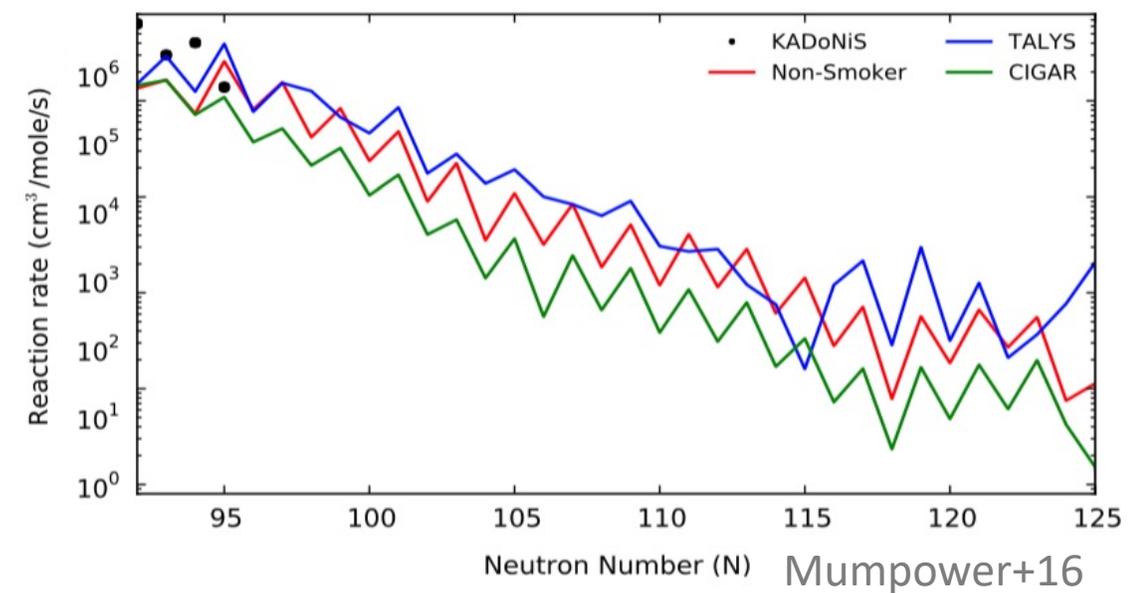
Erlar+12

### $\beta$ -decay calculations



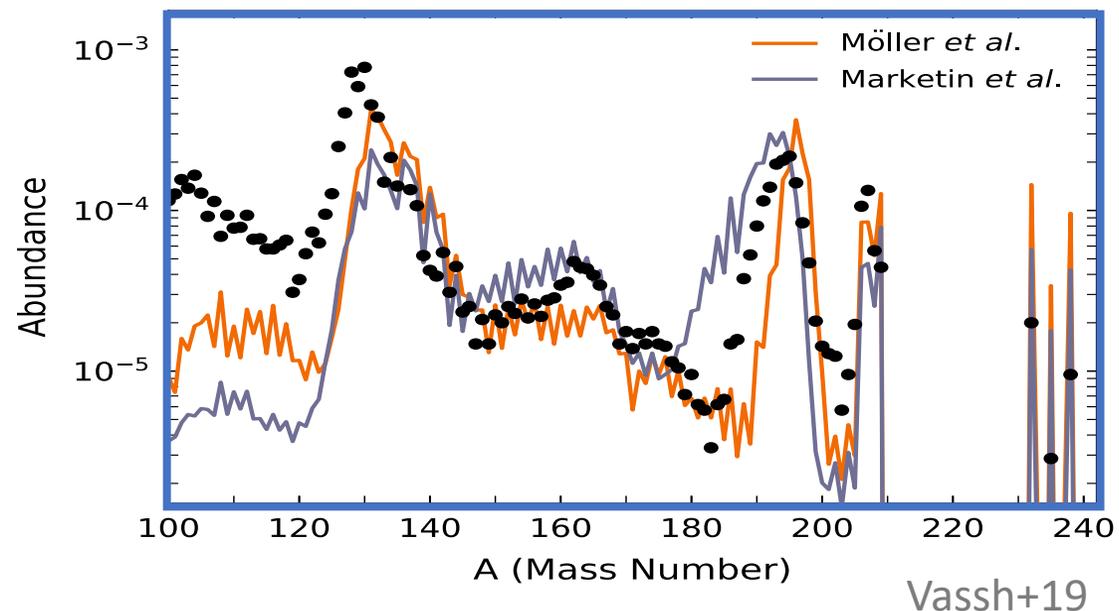
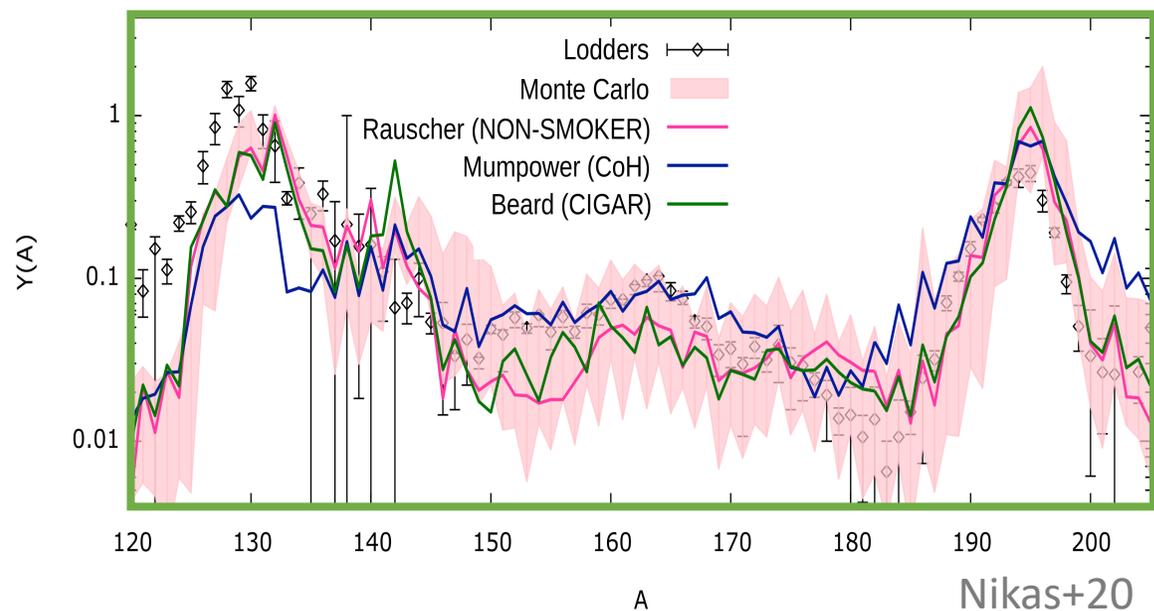
Marketin+16

### Neutron capture models

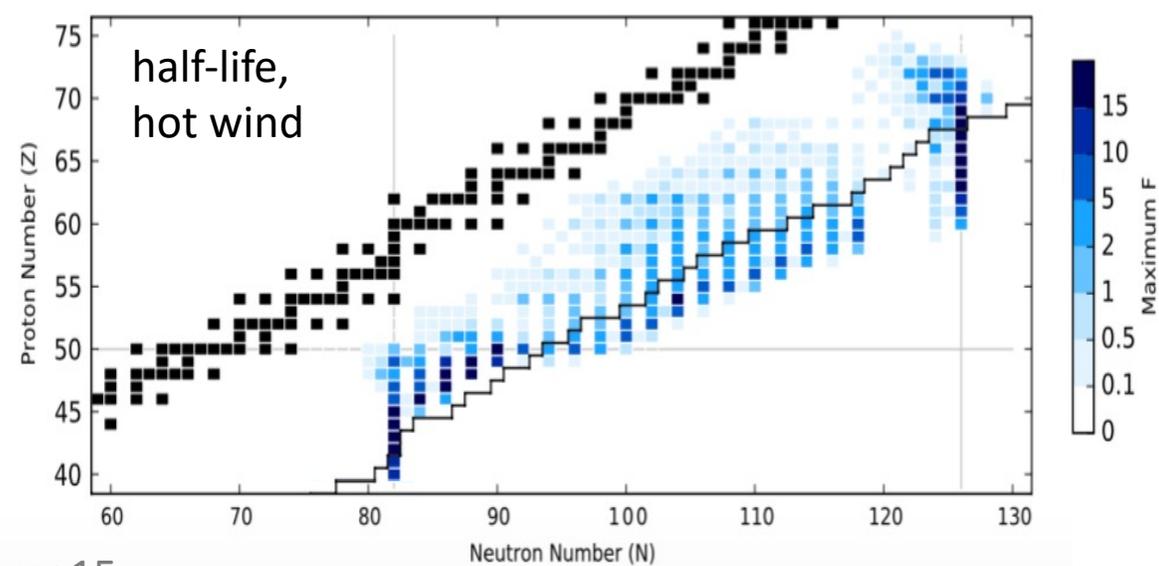
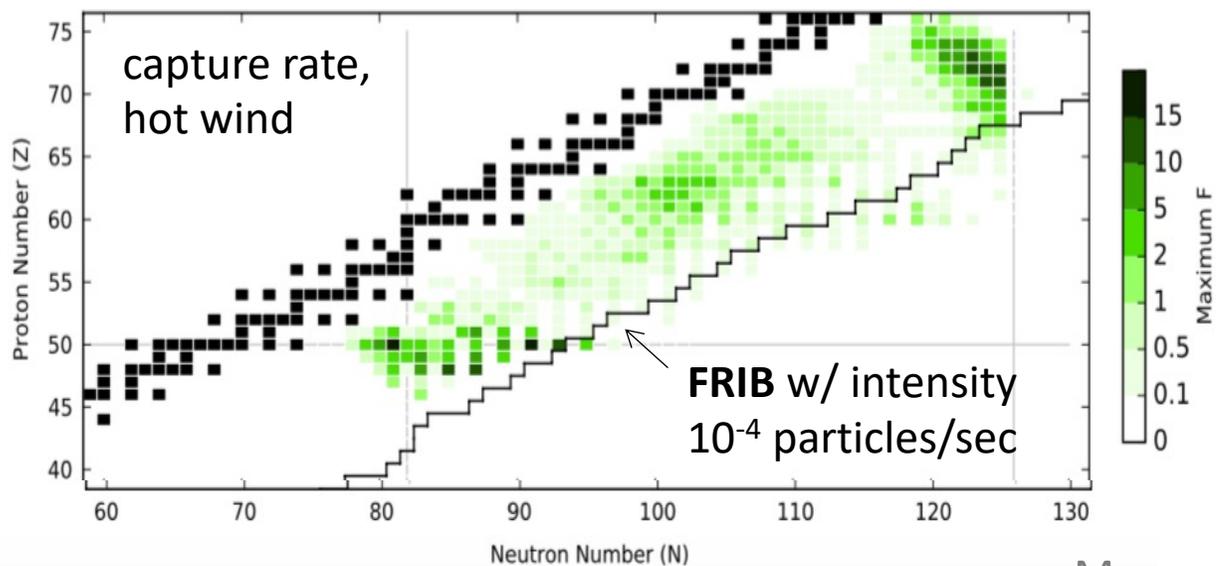
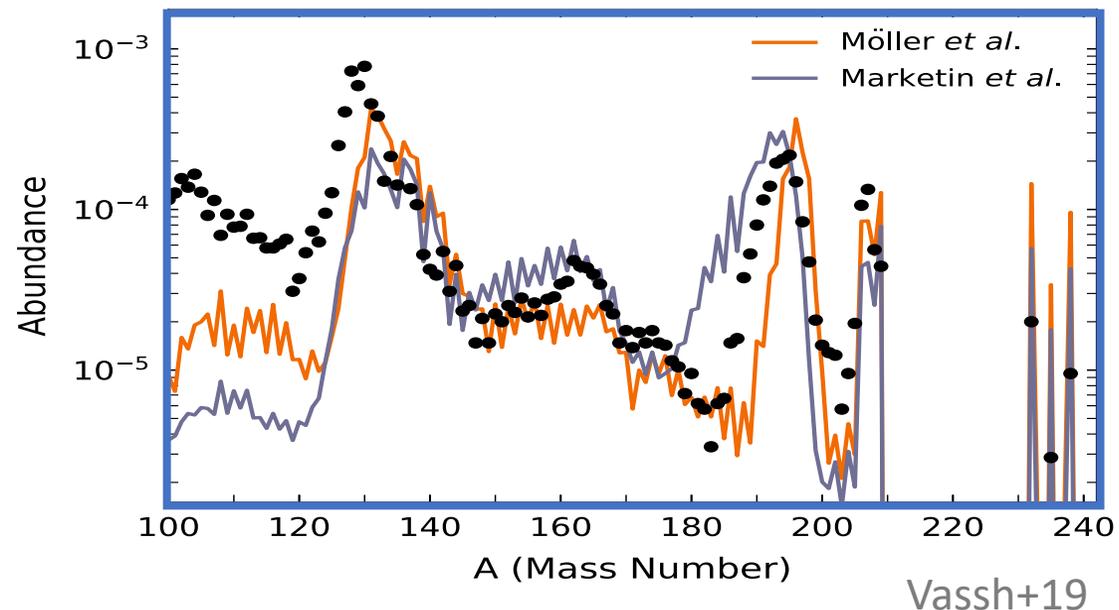
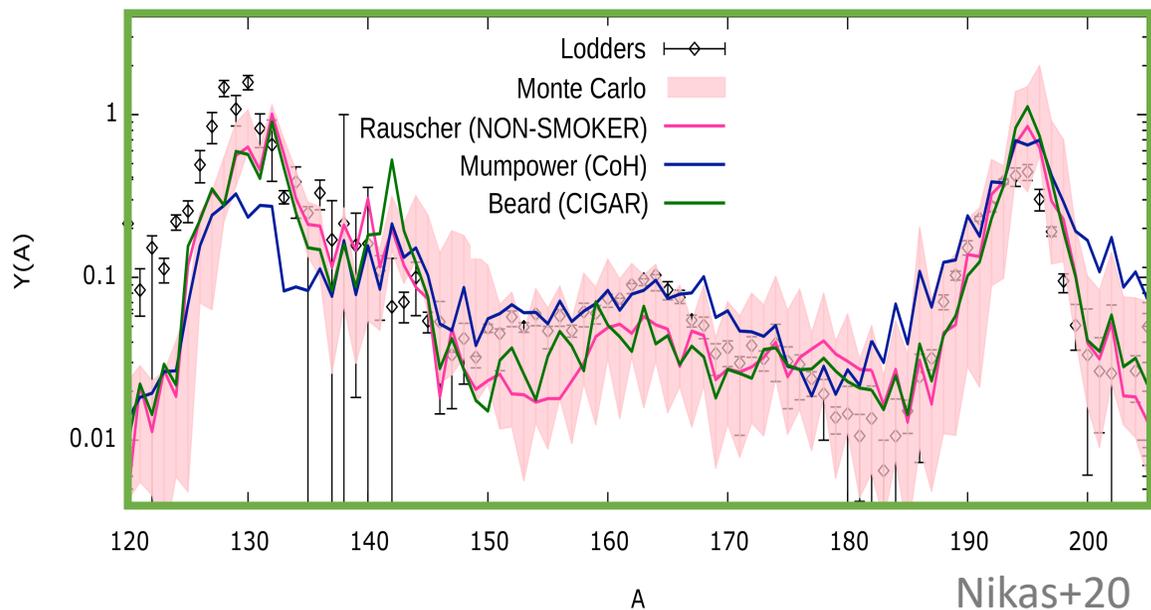


Mumpower+16

# Sensitivity of $r$ -process abundances to neutron capture and $\beta$ -decay



# Sensitivity of $r$ -process abundances to neutron capture and $\beta$ -decay



Mumpower+15

# Spotlight on the impact of nuclear masses

Masses determine key quantities that go into calculating capture and decay rates; for instance:



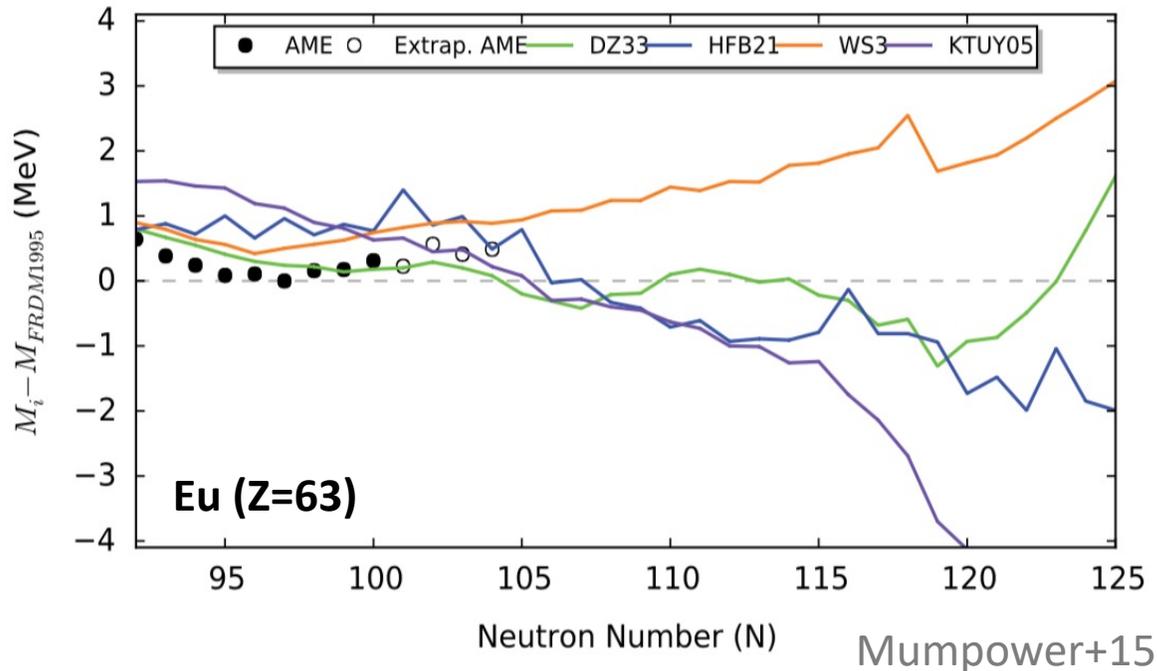
*r*-process calculations should use datasets which *self-consistently* assume the same nuclear masses, but this isn't always done since availability of theory data in the n-rich regions is limited

Neutron capture rates depend on

$$S_n(Z, A + 1) = M_{Z,A} + M_n - M_{Z,A+1}$$

$\beta^-$ -decay rates depend on

$$Q_{\beta^-} = (M_{\text{parent}} - M_{\text{daughter}})c^2$$



# Spotlight on the impact of nuclear masses

Masses determine key quantities that go into calculating capture and decay rates; for instance:



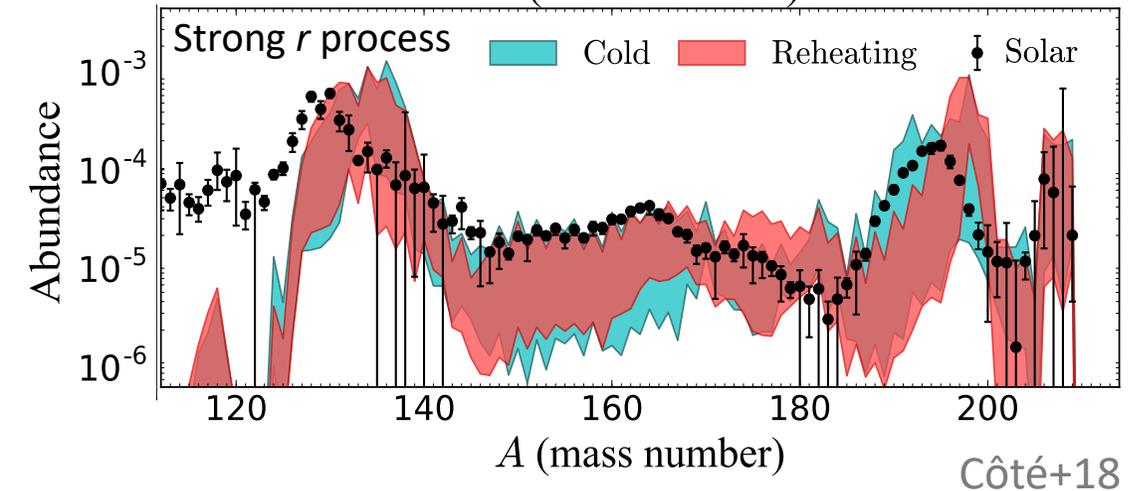
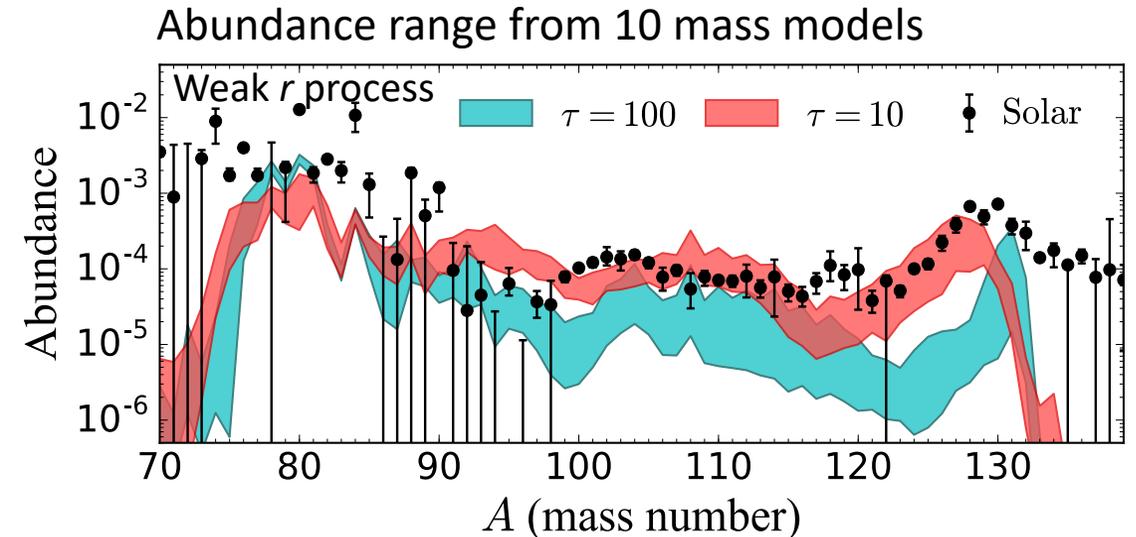
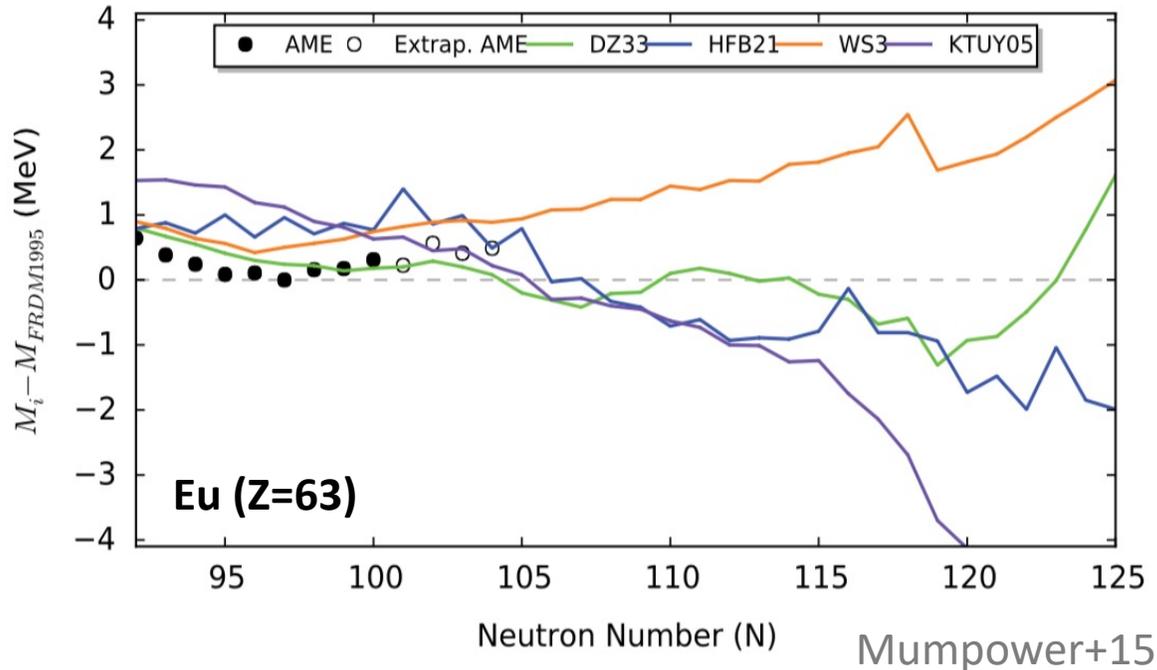
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Neutron capture rates depend on

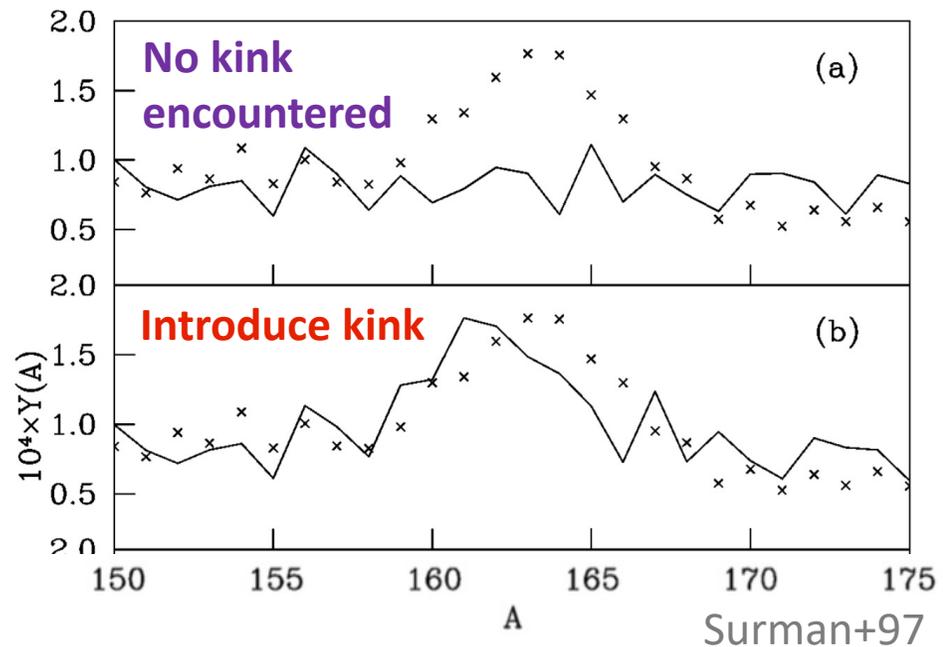
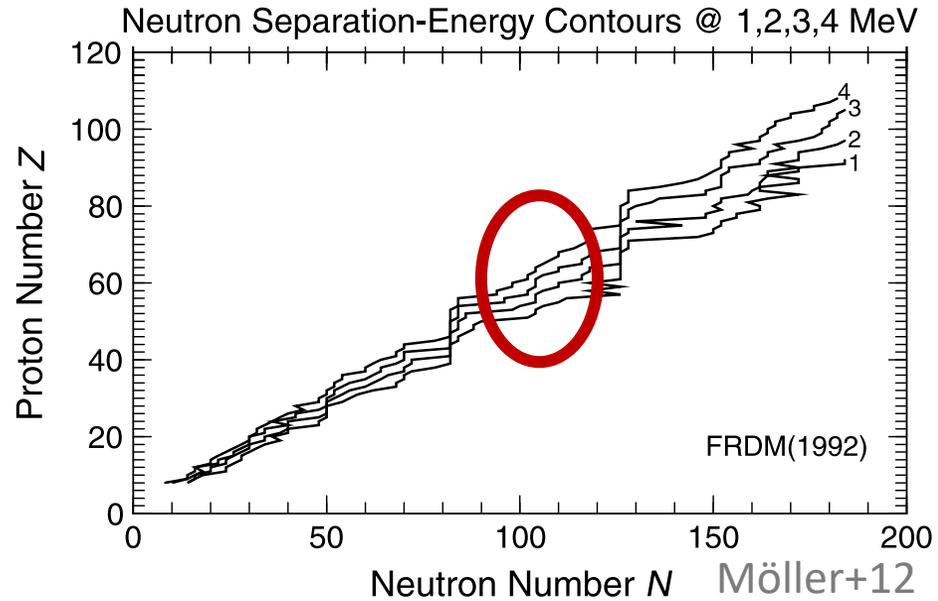
$$S_n(Z, A + 1) = M_{Z,A} + M_n - M_{Z,A+1}$$

$\beta^-$ -decay rates depend on

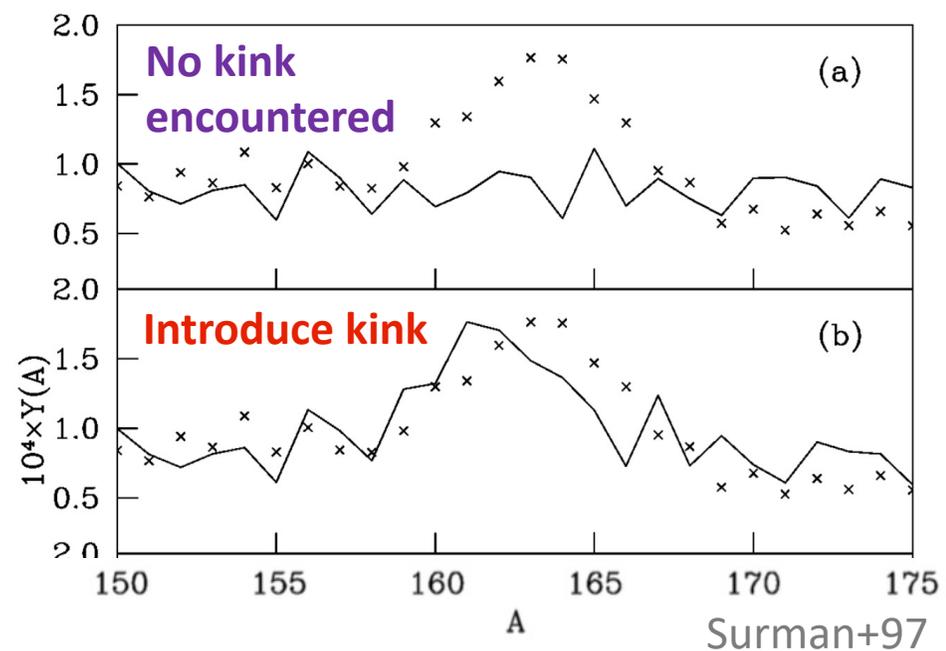
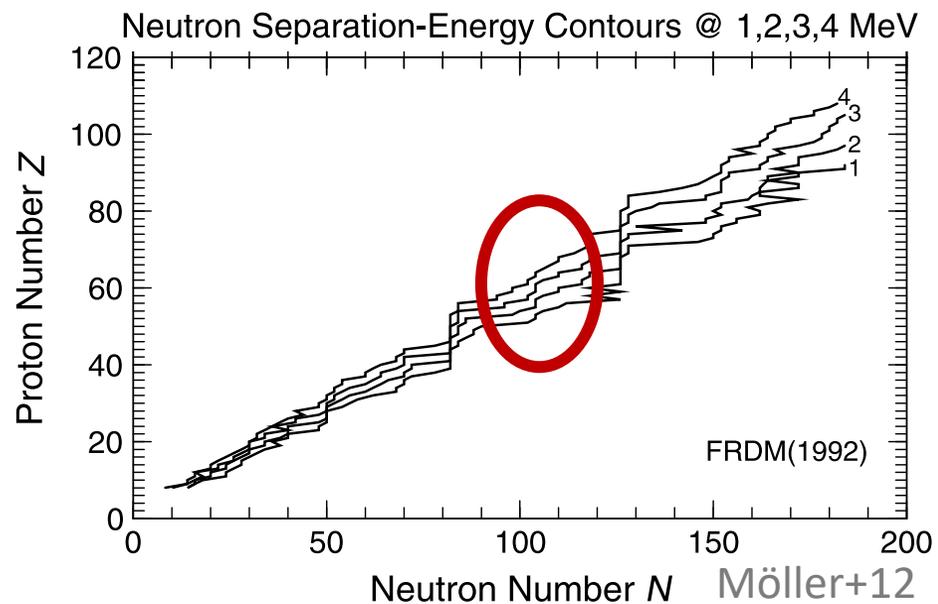
$$Q_{\beta^-} = (M_{\text{parent}} - M_{\text{daughter}})c^2$$



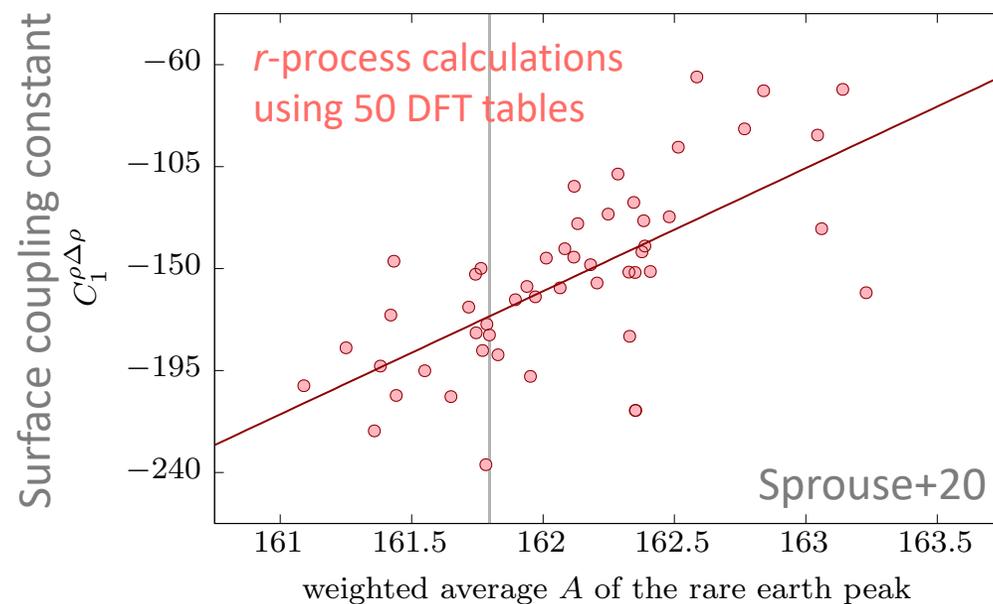
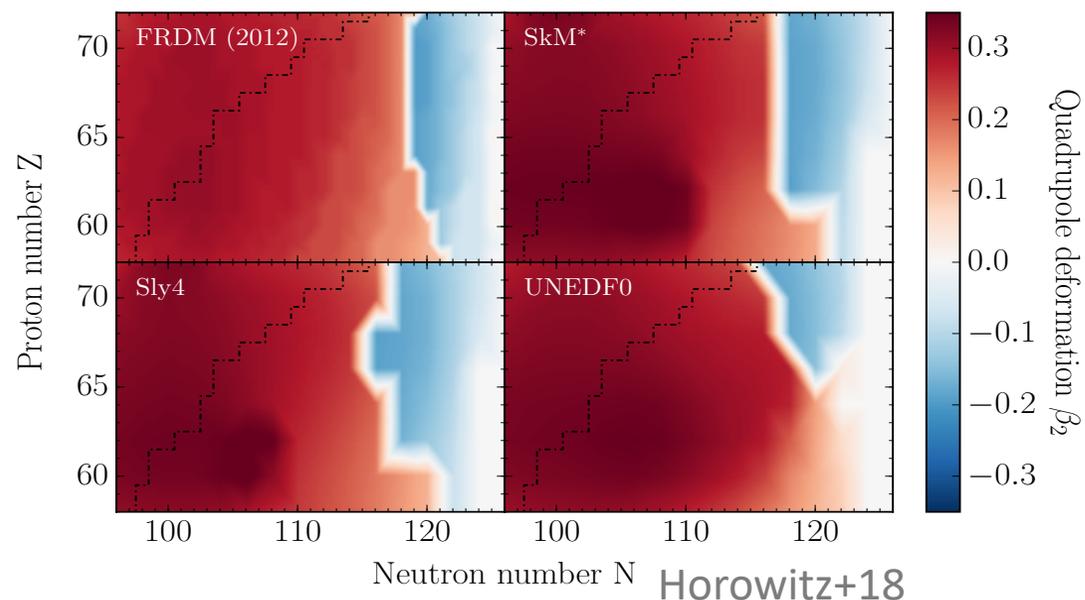
# The rare-earth peak and nuclear structure



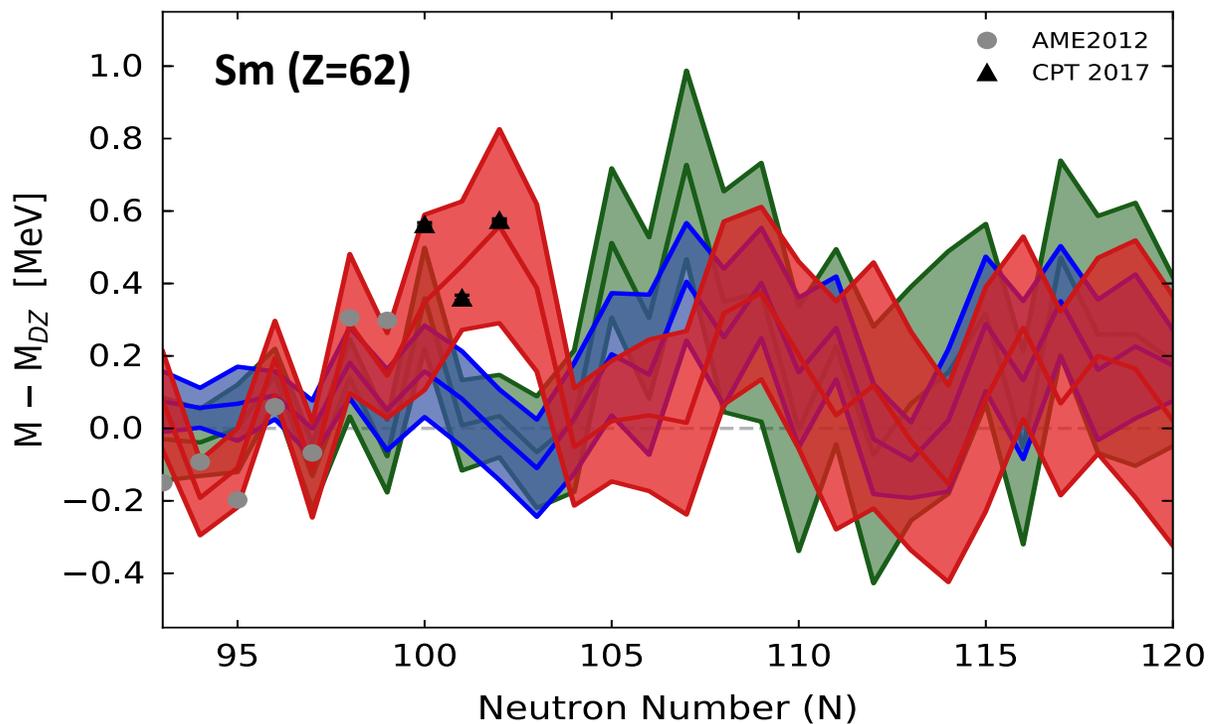
# The rare-earth peak and nuclear structure



Droplet model compared to density functional theory



# Markov Chain Monte Carlo calculations: finding the masses capable of forming the peak in *distinct* outflows

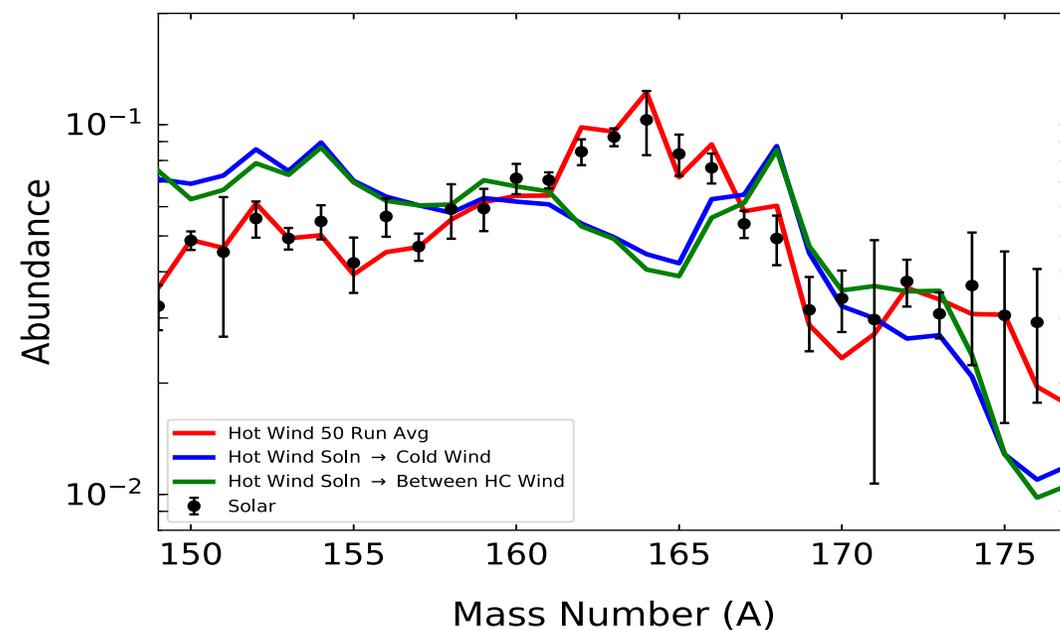
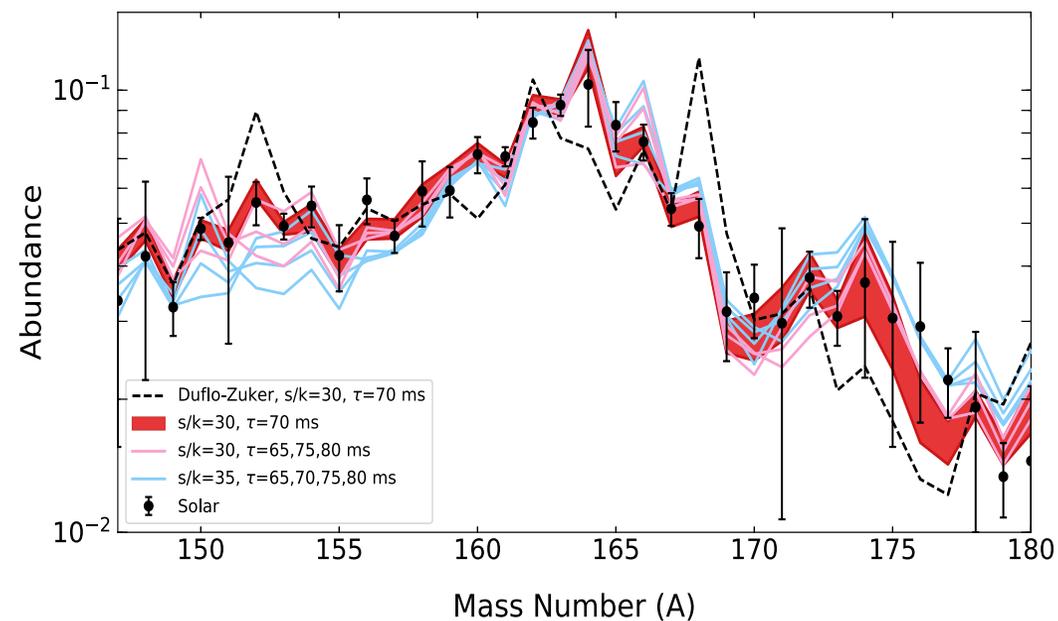


Neutron star merger accretion disk winds with:

**Hot** = extended  $(n,\gamma) \rightleftharpoons (\gamma,n)$  equilibrium

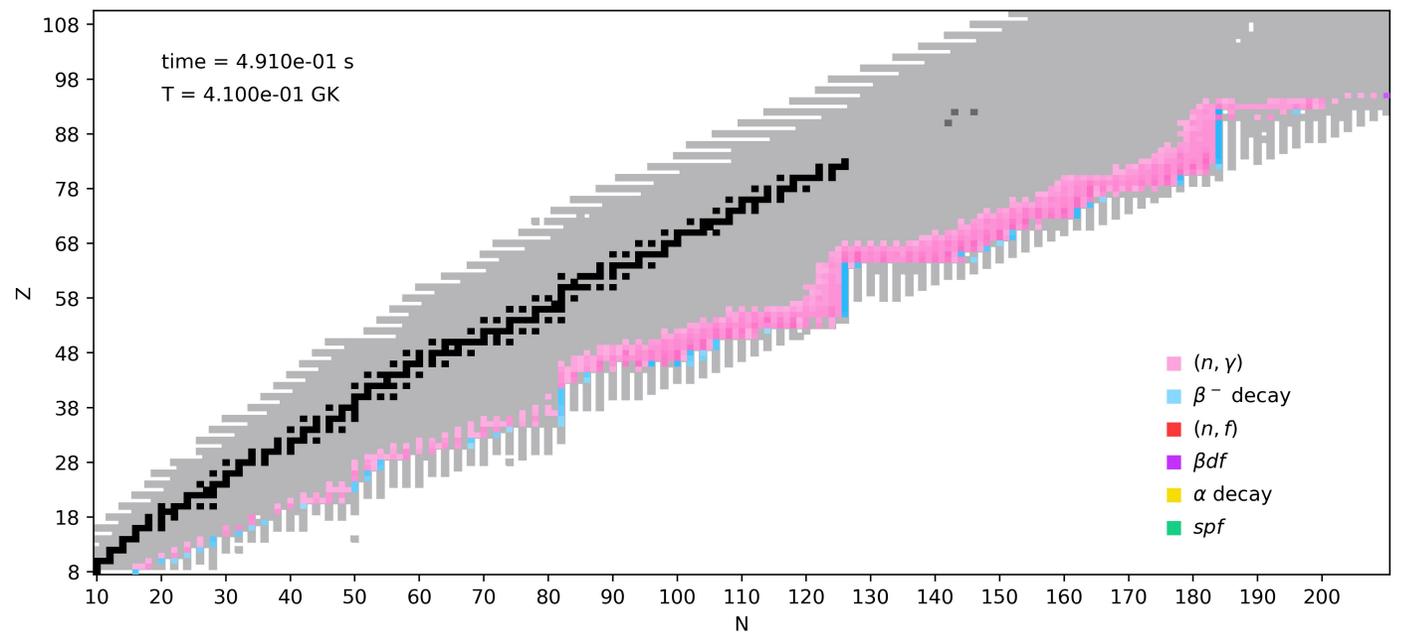
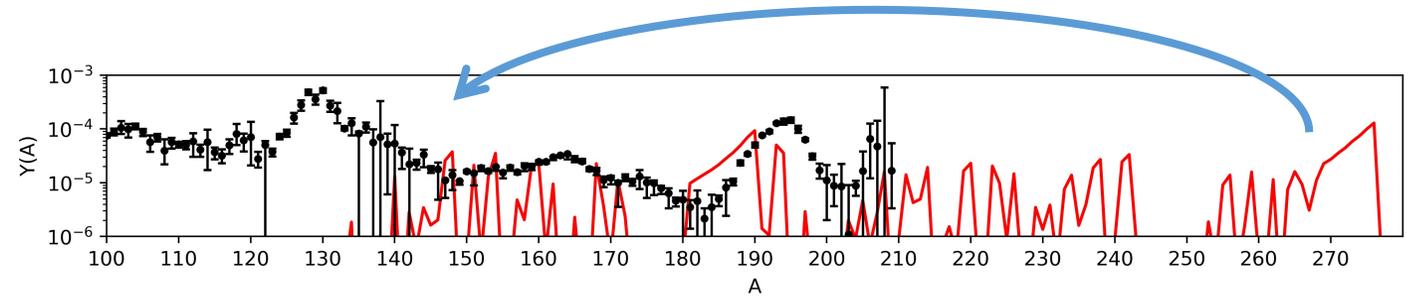
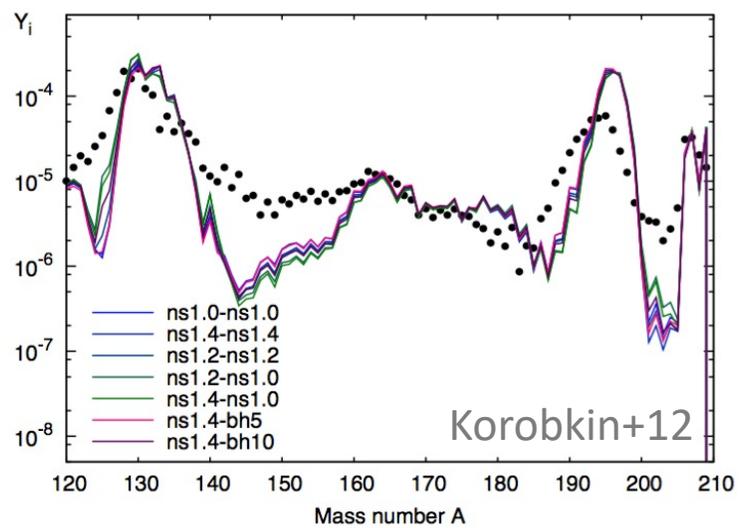
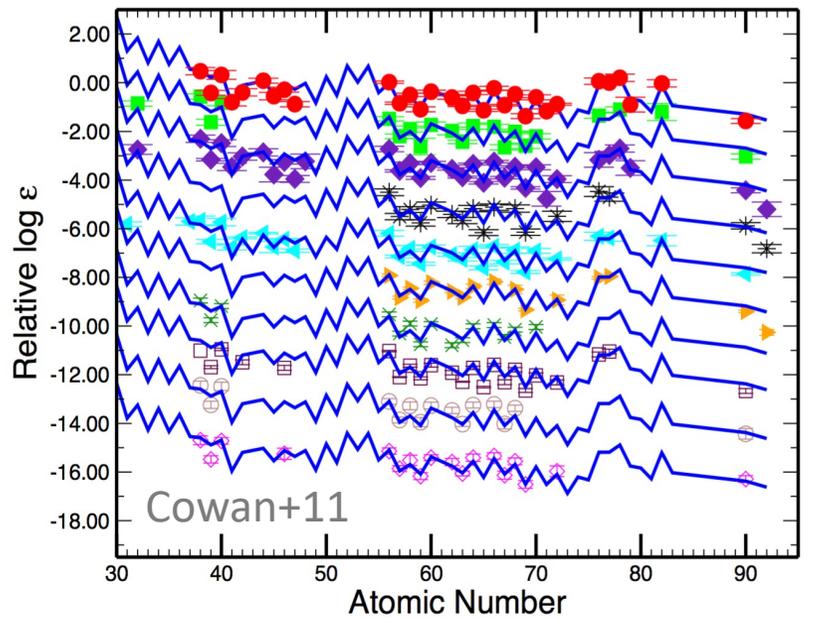
**Cold** = photodissociation falls out early

Vassh+21, Orford, Vassh+18



# Fission cycling to explain observed robustness of lanthanide abundances?

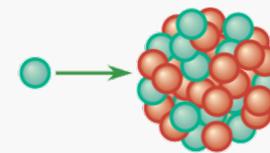
10 *r*-process rich halo stars compared to Solar



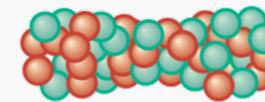
NSM dynamical ejecta using Rosswog+13 simulation conditions (very neutron-rich with robust fission)

# Nuclear Fission (in Astrophysics)

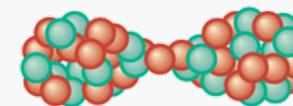
Incident neutron strikes



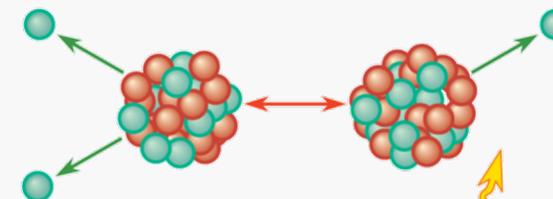
Deformation



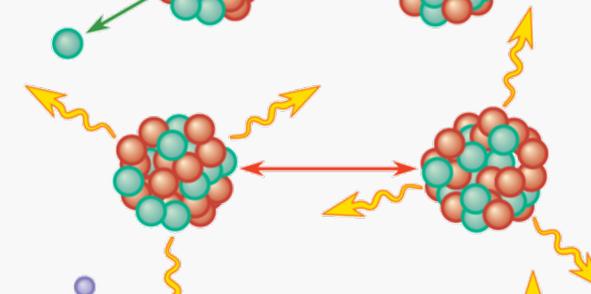
Scission



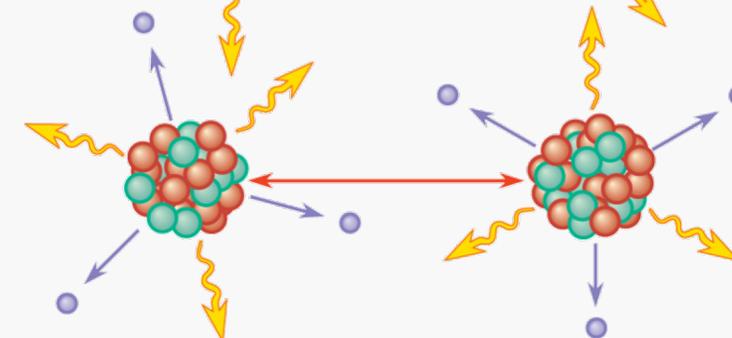
Prompt Neutron Emission from  
excited fission fragments ( $\sim 2-3$ )



Energy release  $\sim 200$  MeV with  
kinetic energy of fragments  
 $\sim 170$  MeV

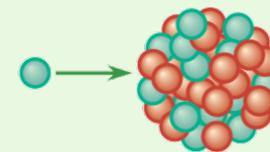


Delayed emission from  $\beta$ -decay  
of neutron-rich fission products

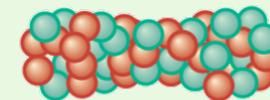


# Nuclear Fission (in Astrophysics)

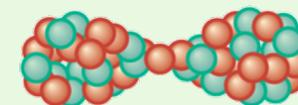
Incident neutron strikes



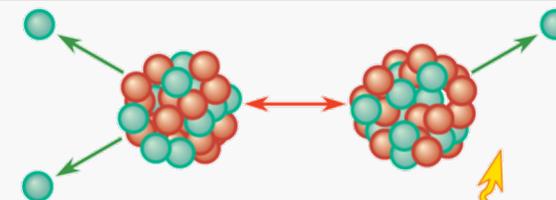
Deformation



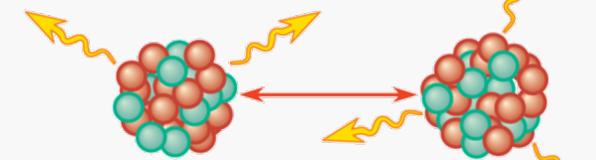
Scission



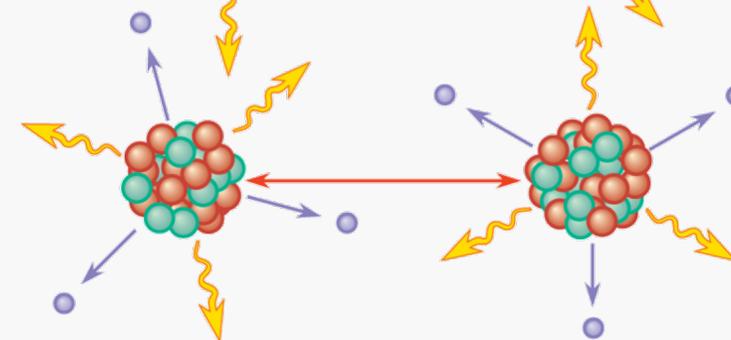
Prompt Neutron Emission from excited fission fragments (~2-3)



Energy release ~200 MeV with kinetic energy of fragments ~170 MeV

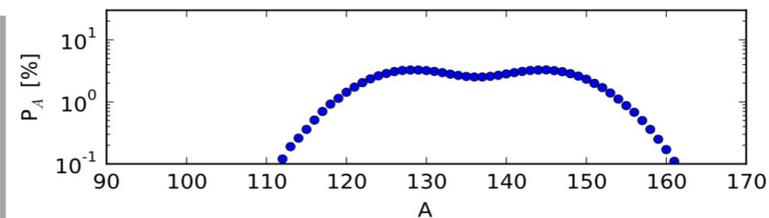
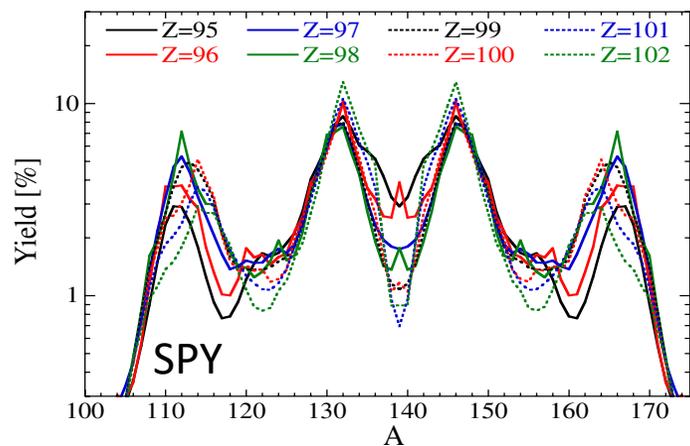
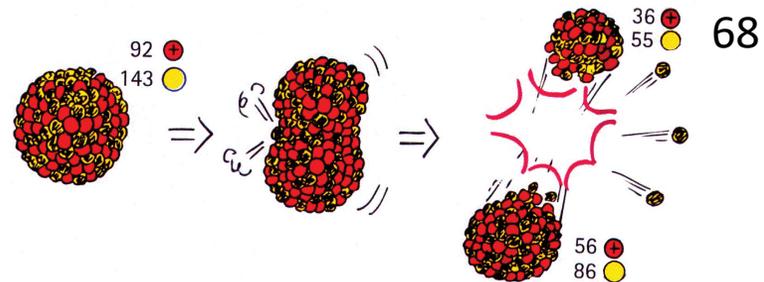


Delayed emission from  $\beta$ -decay of neutron-rich fission products

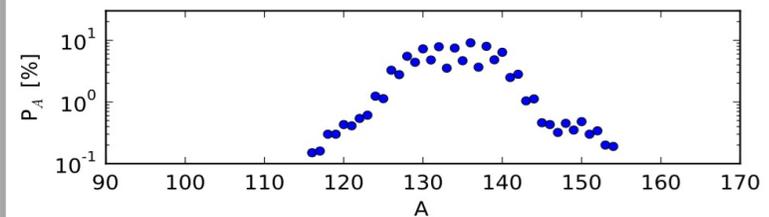


● Neutrons   ● Protons   ● Beta particles   ⚡ Gamma rays

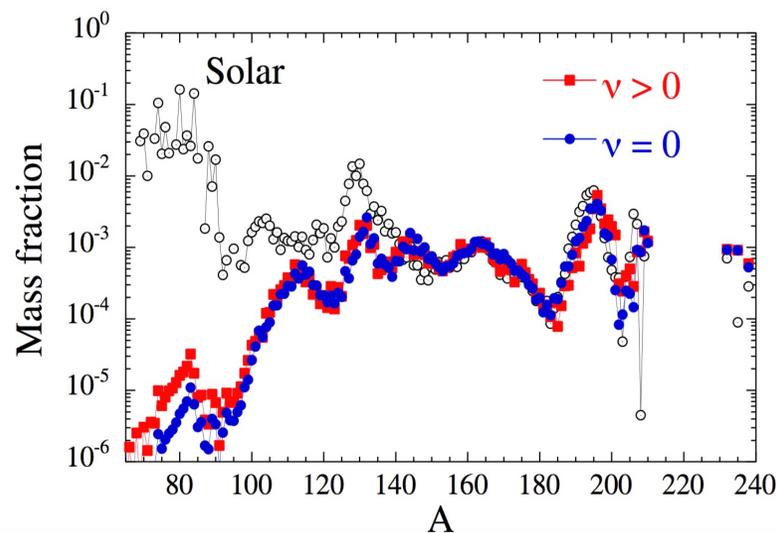
# Dependence of $r$ -process abundances on fission yields



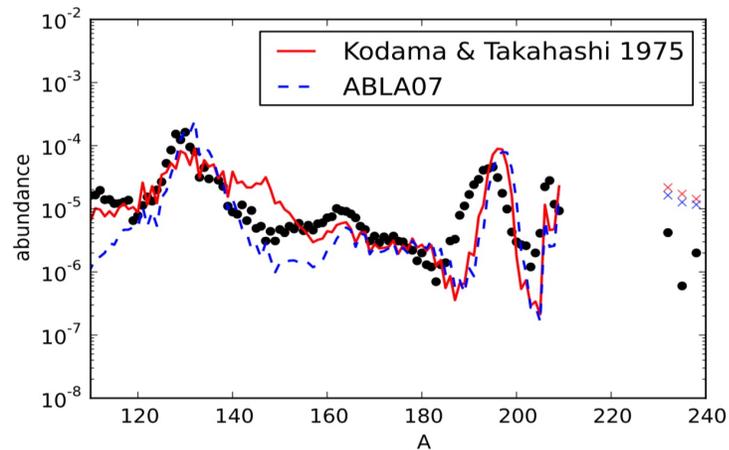
(b) Kodama & Takahashi (1975)



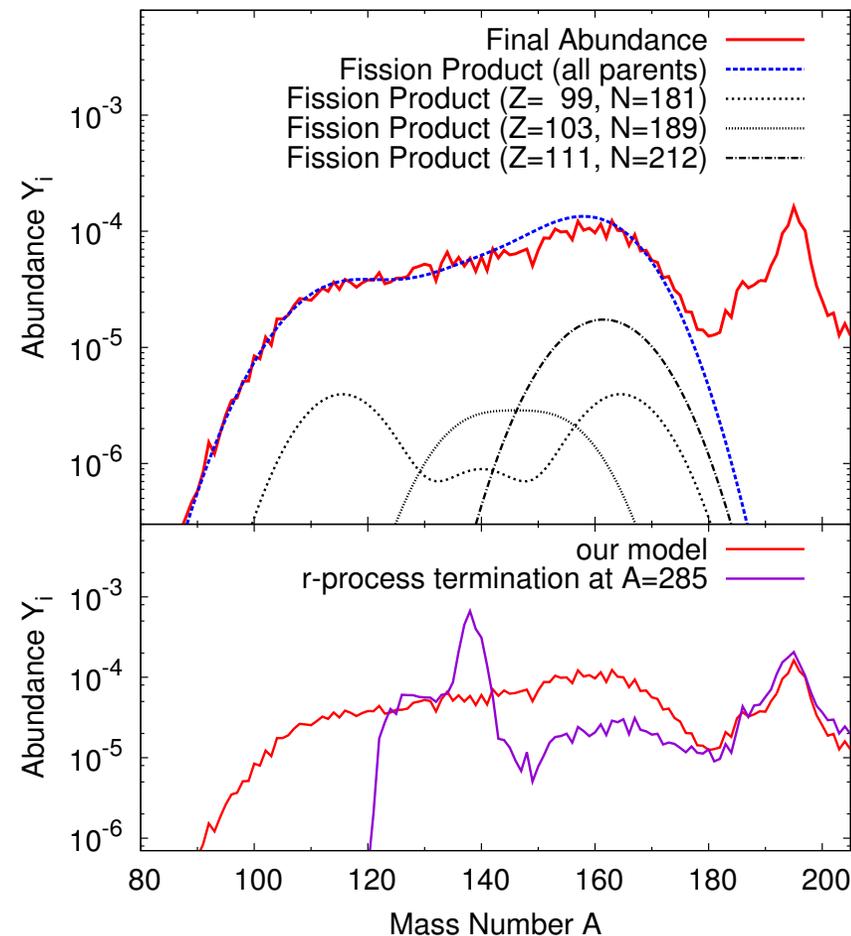
(c) ABLA07



Goriely+13,15; see also Lemaître+21

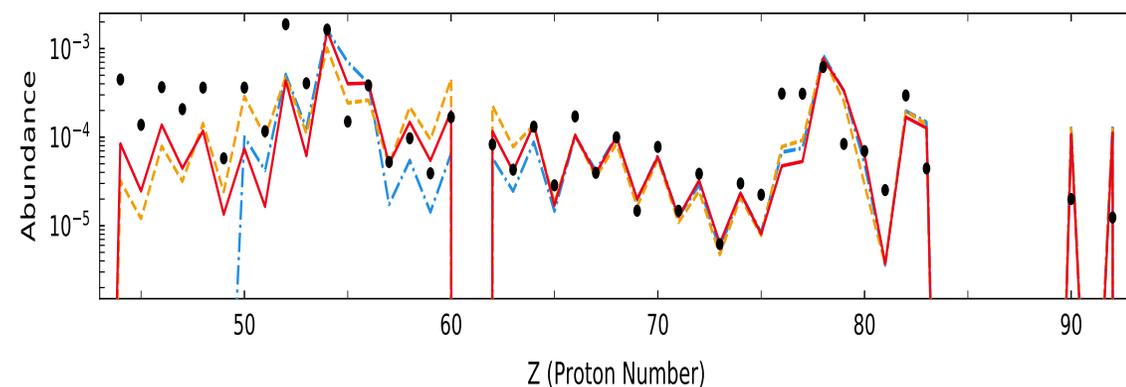
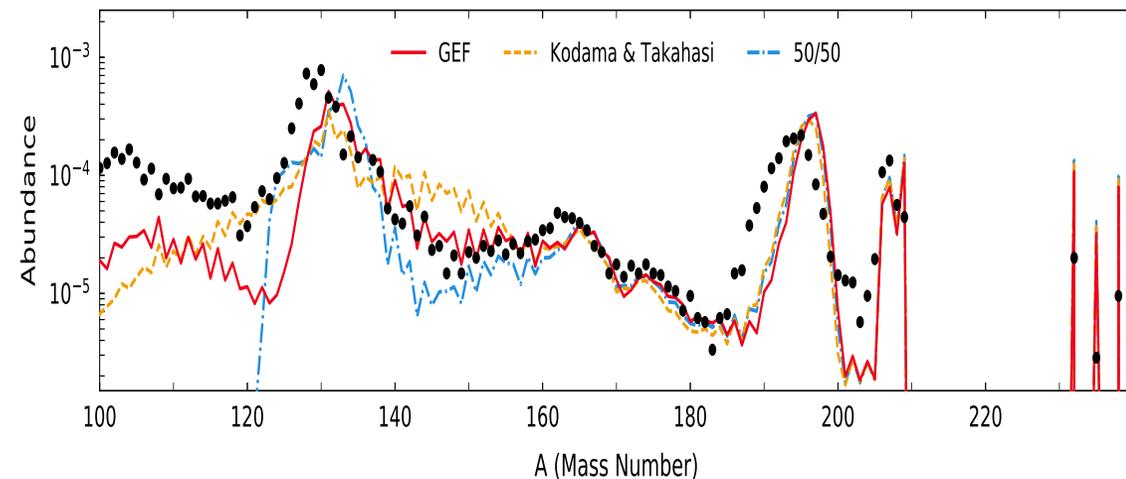
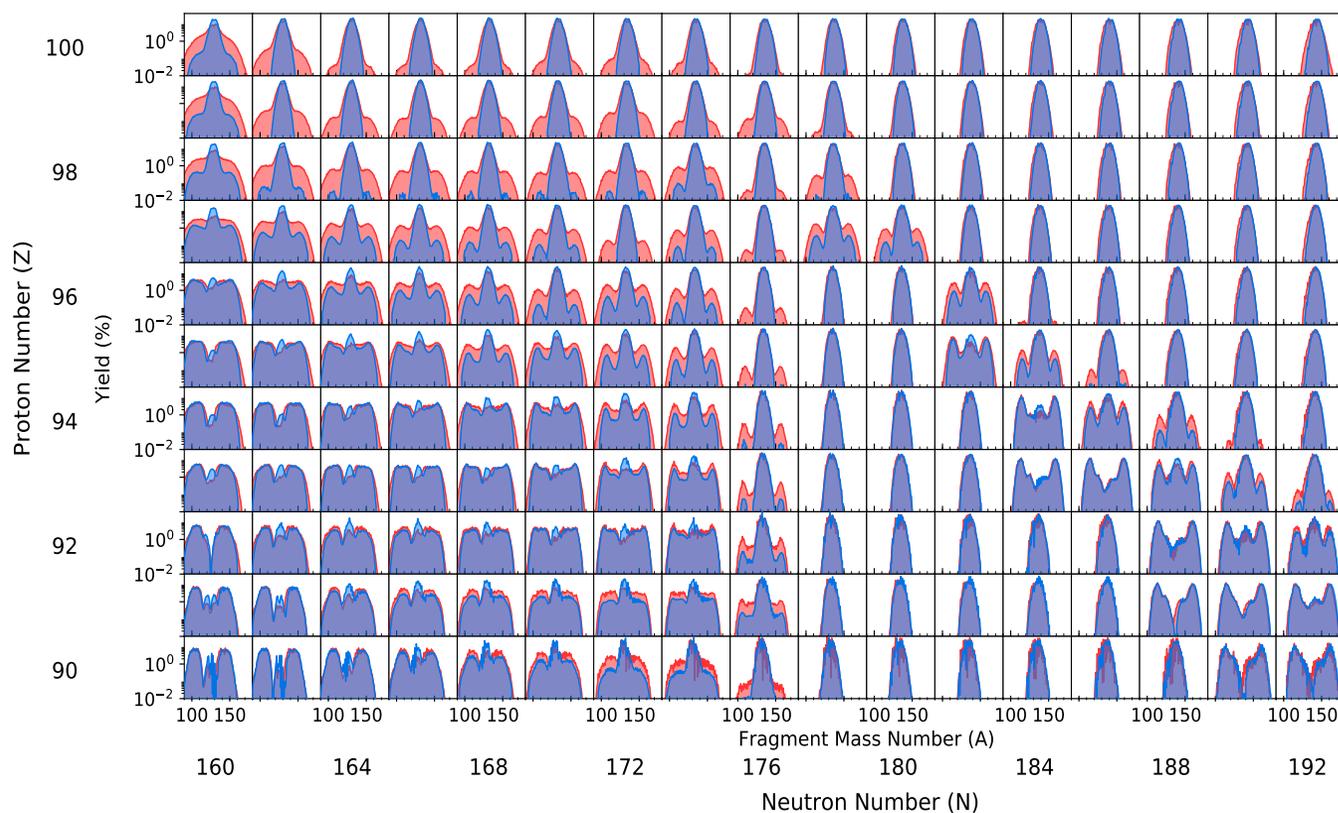


Eichler+15



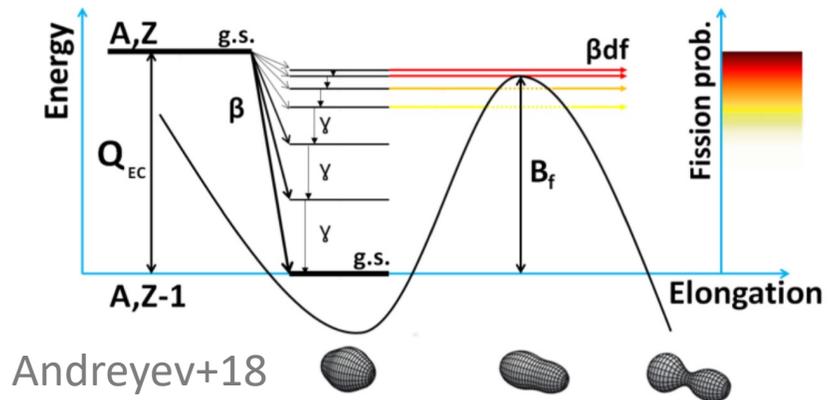
Shibagaki+16

# Excitation energy dependence: distinct fission yields for neutron-induced, $\beta$ -delayed, and spontaneous fission



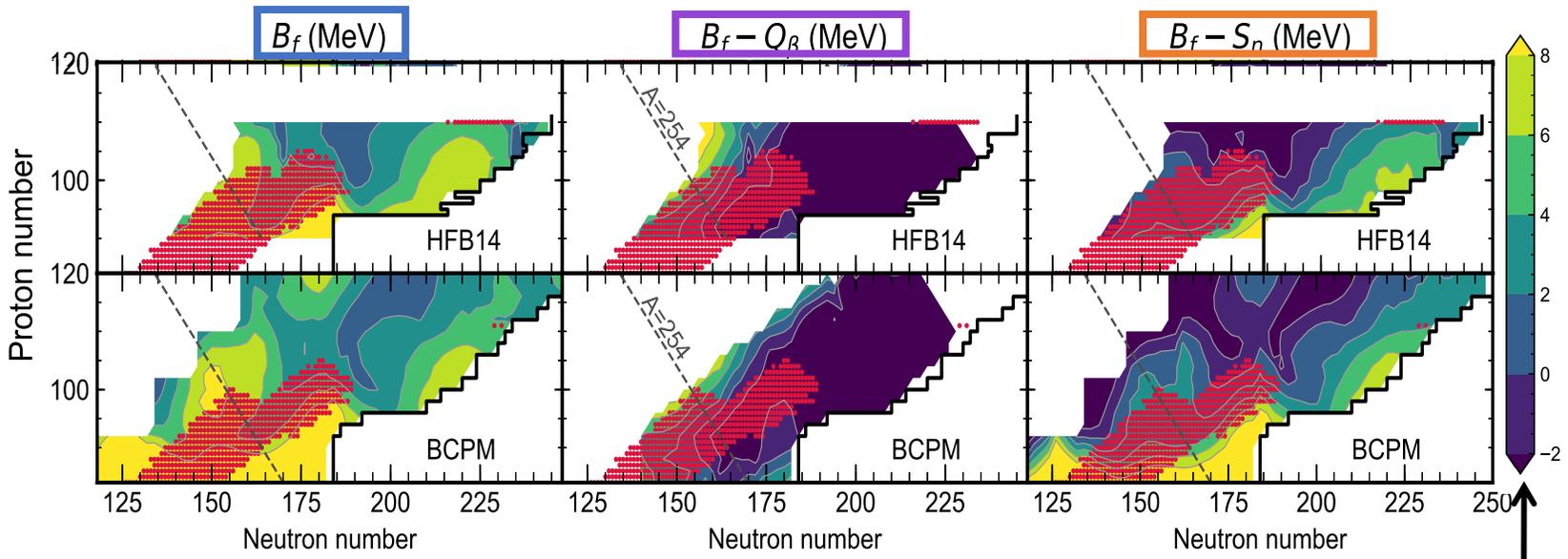
**(n,f) yields** with excitation energy  $E_i + S_n$  differ from **sf yields** which have zero excitation energy (above from GEF 2016)

# Fission and the ultimate reach of the *r* process



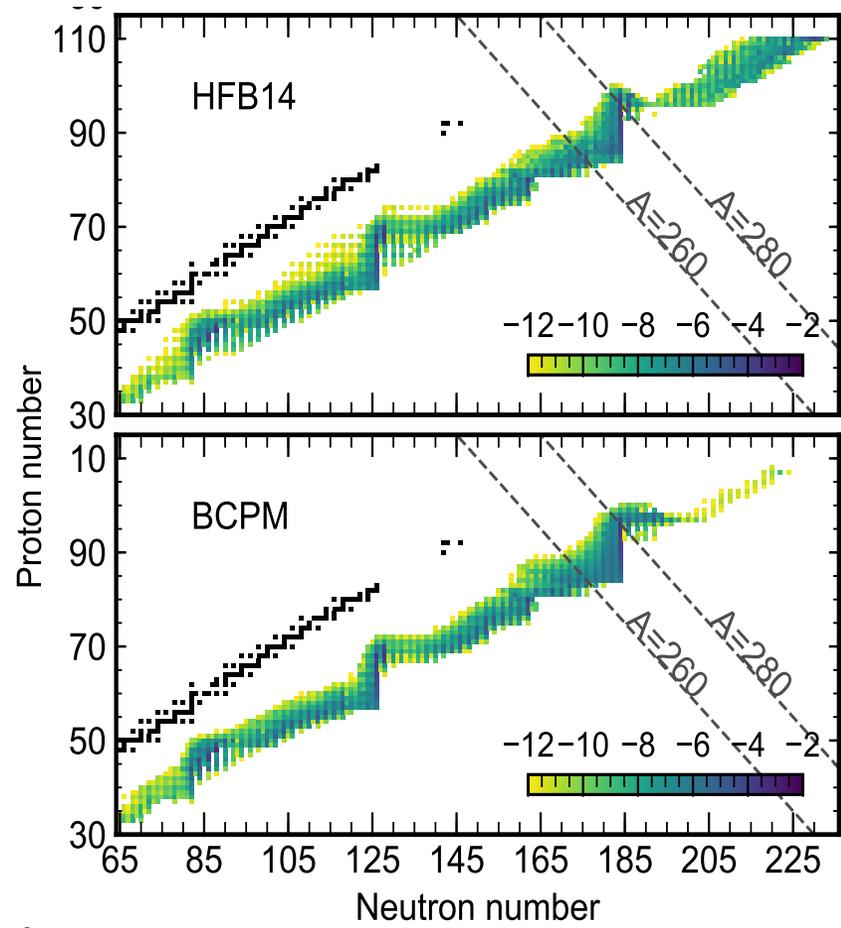
Andreyev+18

Fission barriers and masses are used to determine spontaneous,  $\beta$ -delayed, and neutron-induced fission rates



Giuliani+20

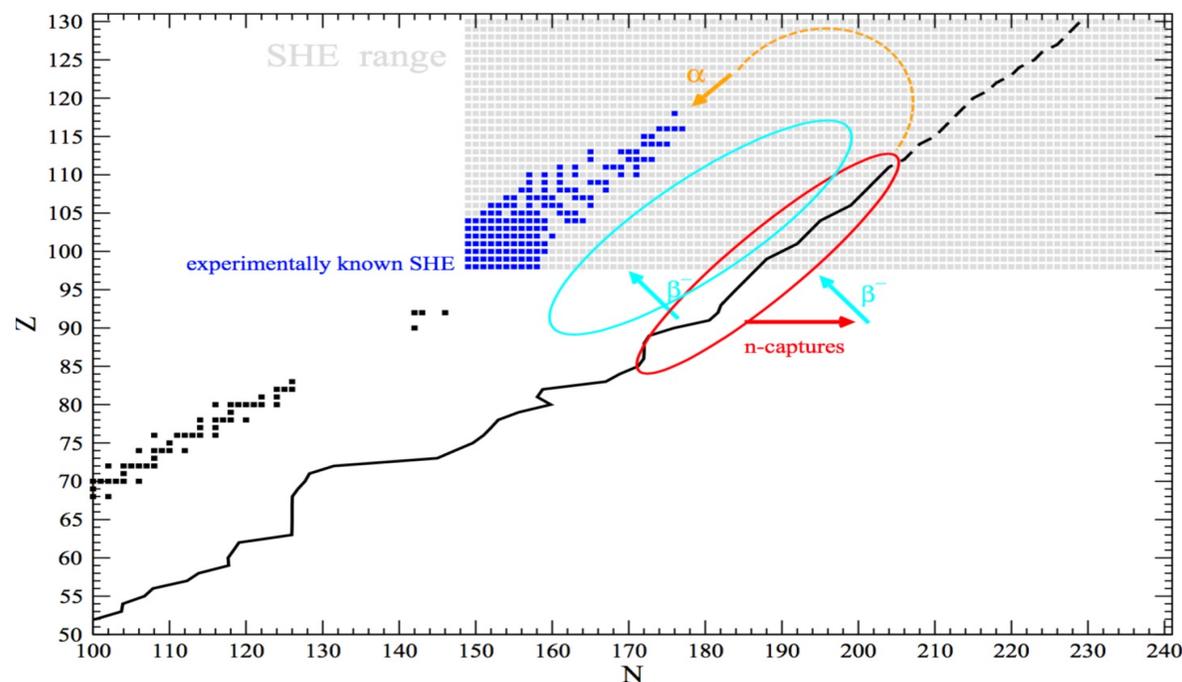
Smaller  $\Rightarrow$  larger fission probability



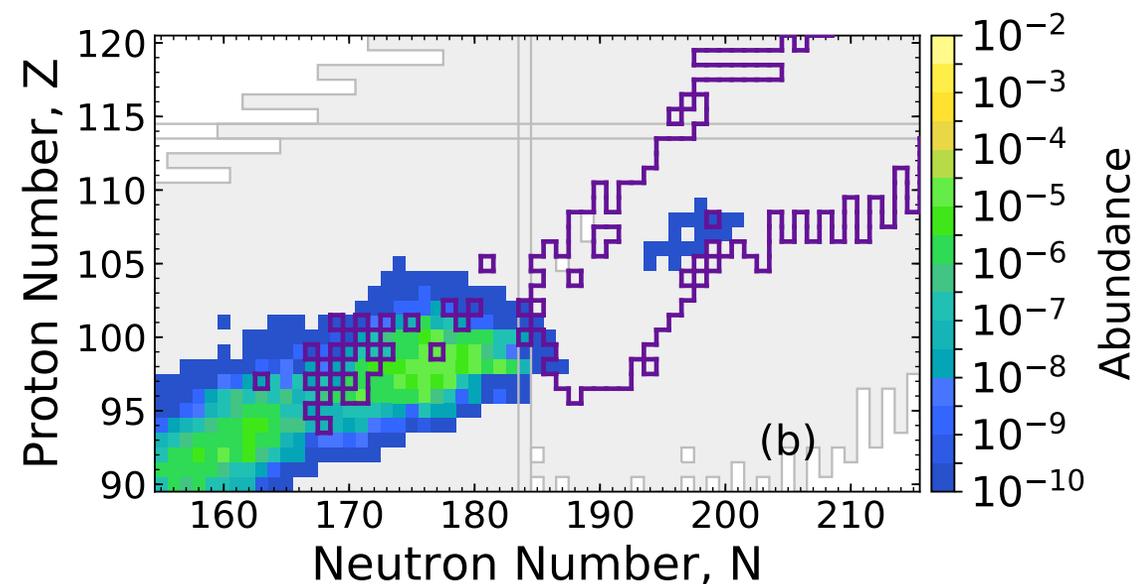
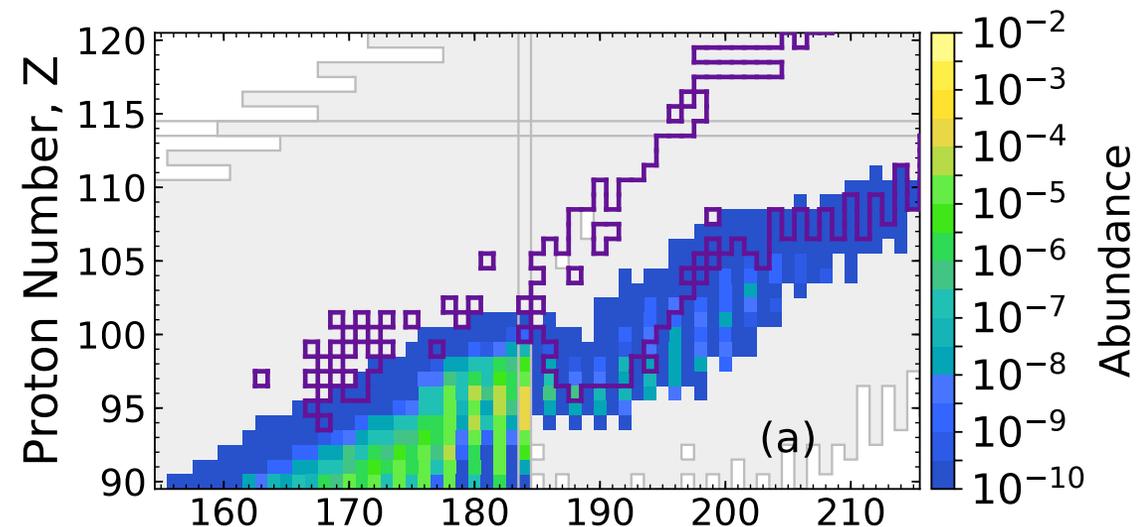
# $r$ -process production of superheavy elements?

Super heavy elements ( $Z \gtrsim 103$ ) have been produced in laboratories and models predict an “island of stability” at  $Z=114$ ,  $N=184$ , but current  $r$ -process calculations see fission prevent the population of such species

→ if observed in nature, fission barriers would have to differ from theory predictions



Petermann+12

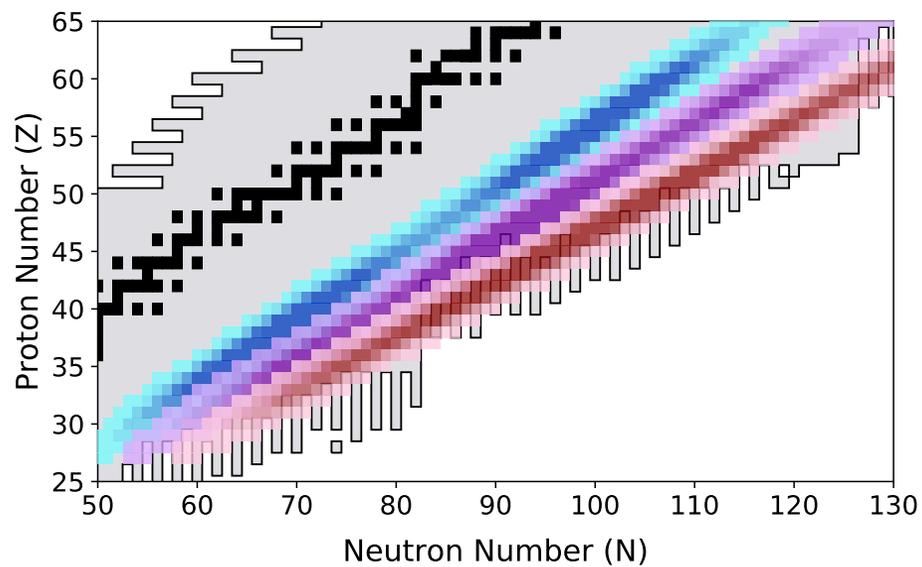
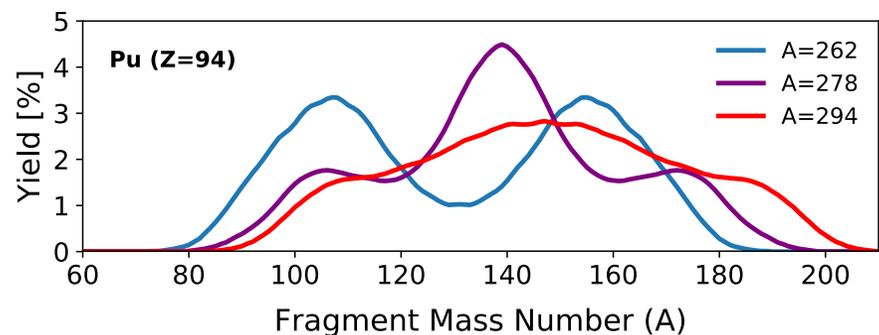


(purple outline – probability of  $\beta df \geq 90\%$ )

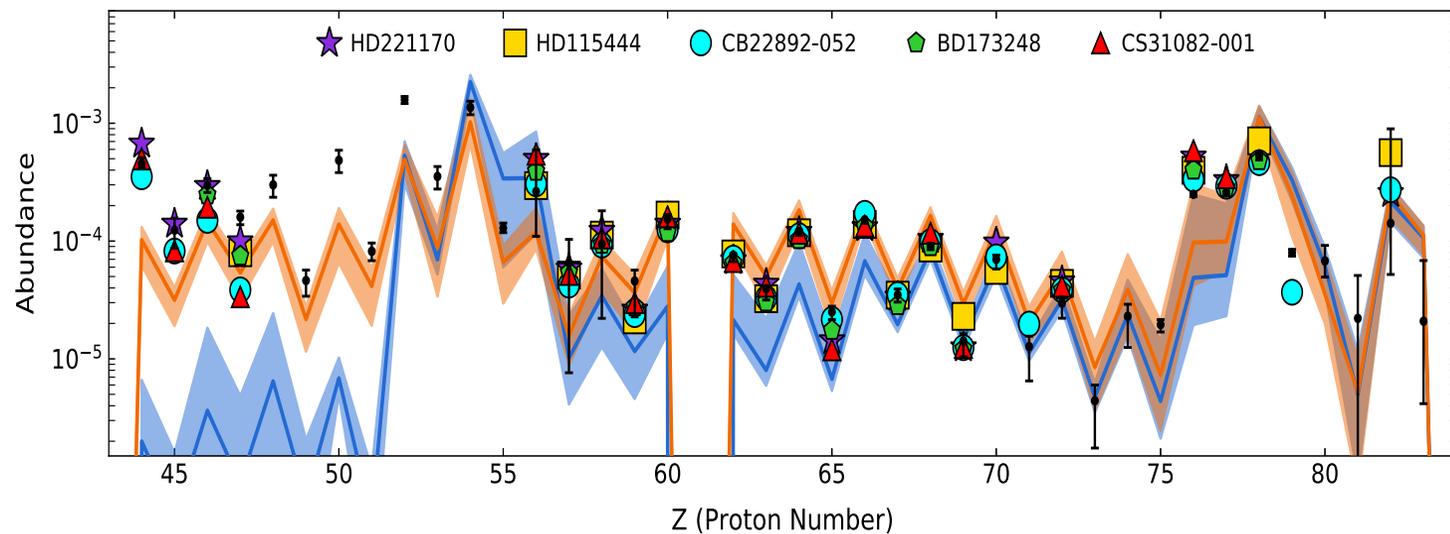
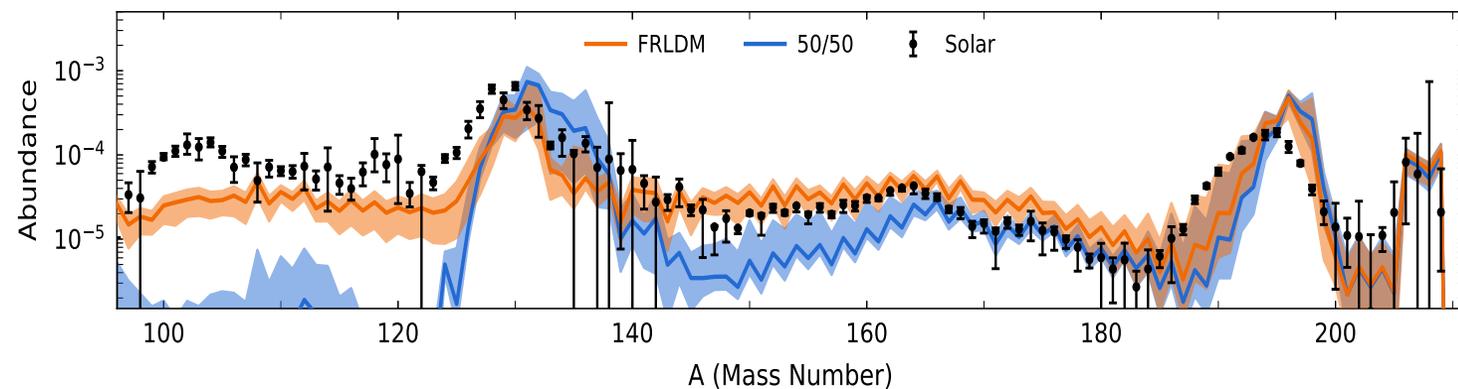
Mumpower+18

# Using fission yields and fission rates calculated with self-consistent fission barriers

## FRLDM Yields from Mumpower+20

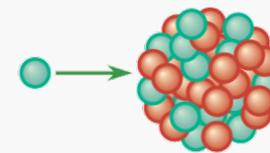


## Range from Rosswog+13 NSM dynamical ejecta ( $Y_e \sim 0.01-0.05$ )

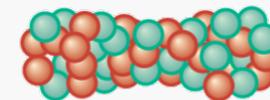


# Nuclear Fission (in Astrophysics)

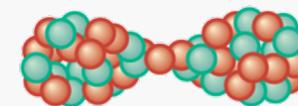
Incident neutron strikes



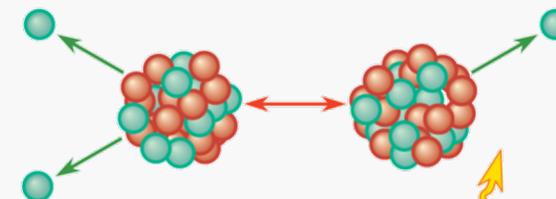
Deformation



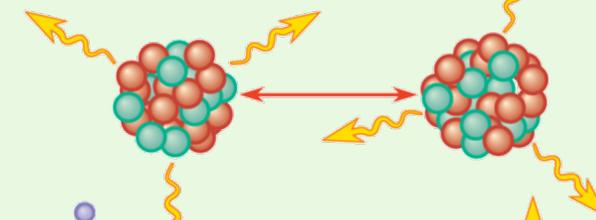
Scission



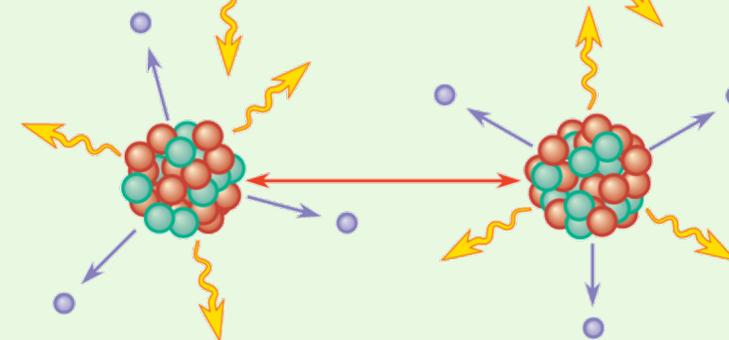
Prompt Neutron Emission from excited fission fragments (~2-3)



Energy release ~200 MeV with kinetic energy of fragments ~170 MeV

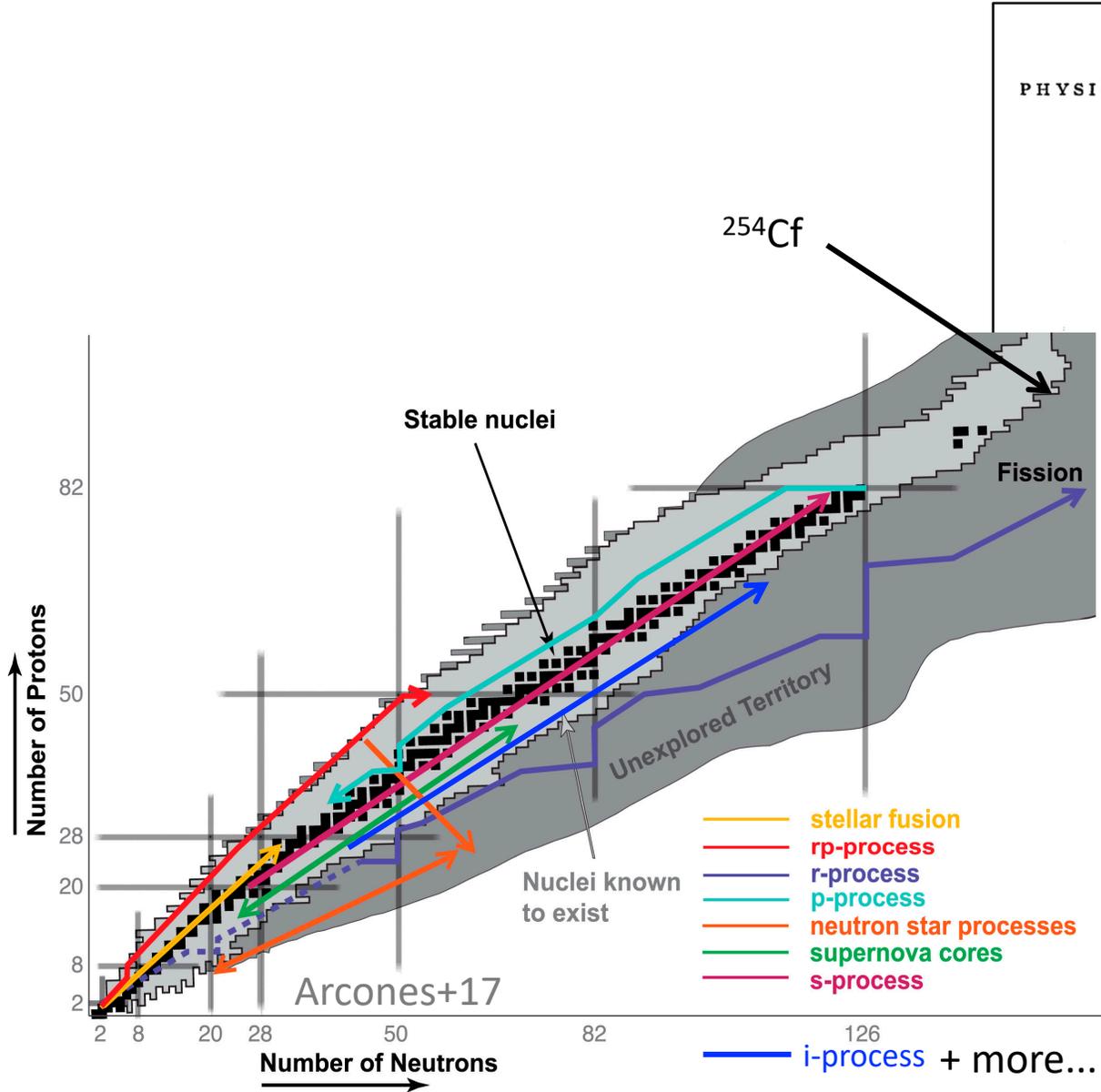


Delayed emission from  $\beta$ -decay of neutron-rich fission products



● Neutrons    ● Protons    ● Beta particles    ⚡ Gamma rays

# Late time kilonova light curves can shed light on actinide production



PHYSICAL REVIEW

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SEPTEMBER 1, 1956

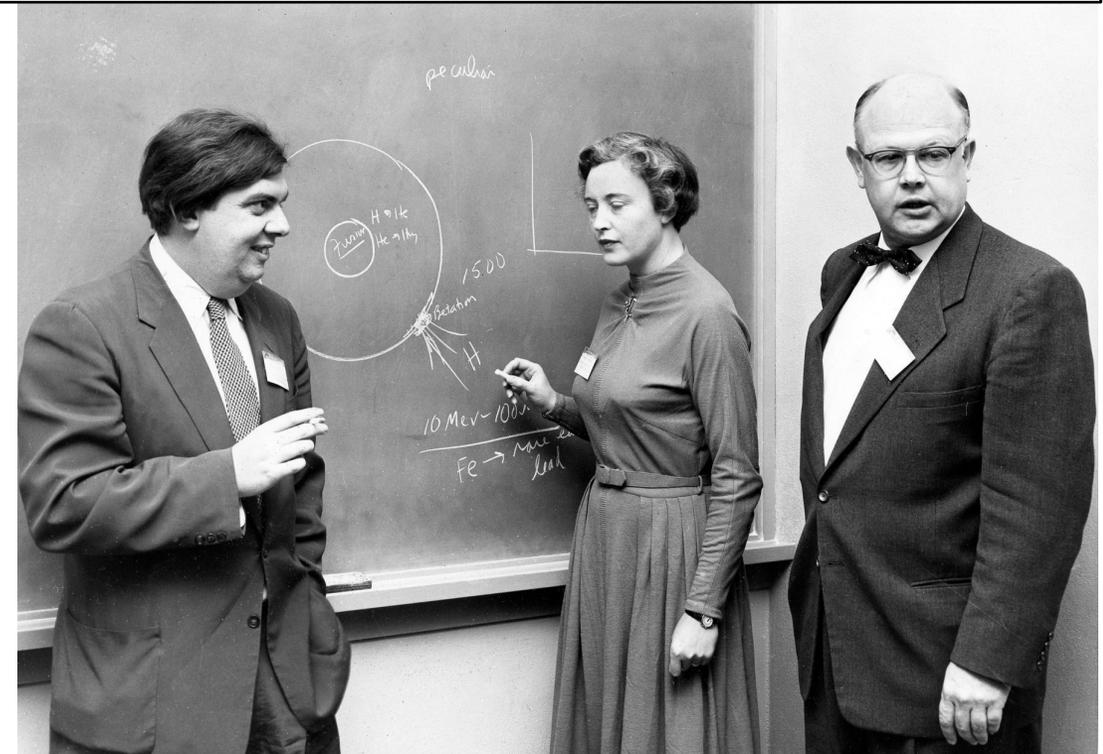
**Californium-254 and Supernovae\***

G. R. BURBIDGE AND F. HOYLE,† *Mount Wilson and Palomar Observatories, Carnegie Institution of Washington, California Institute of Technology, Pasadena, California*

AND

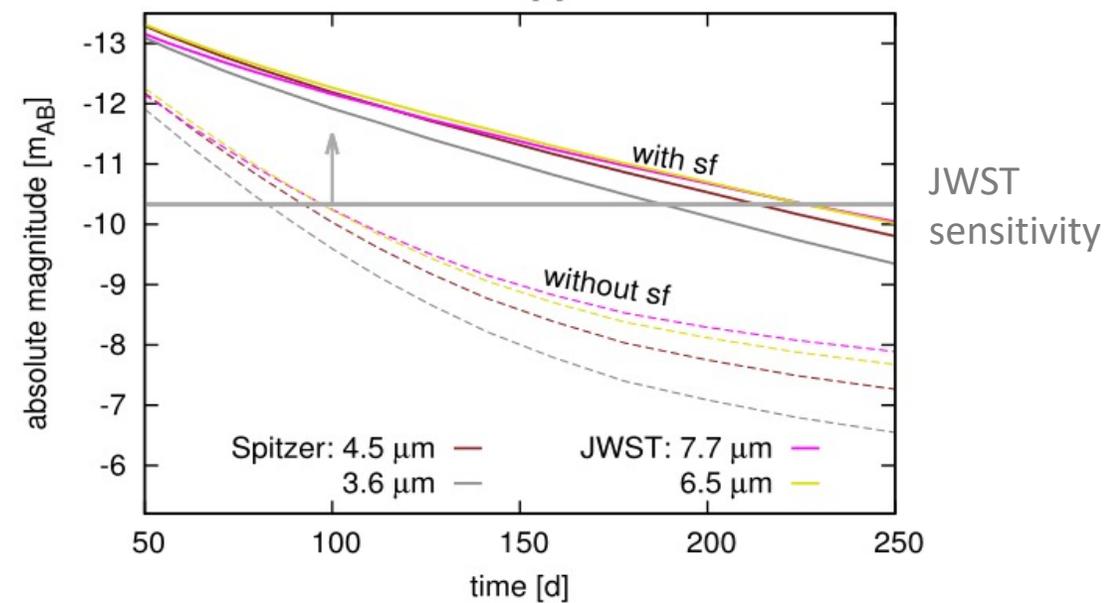
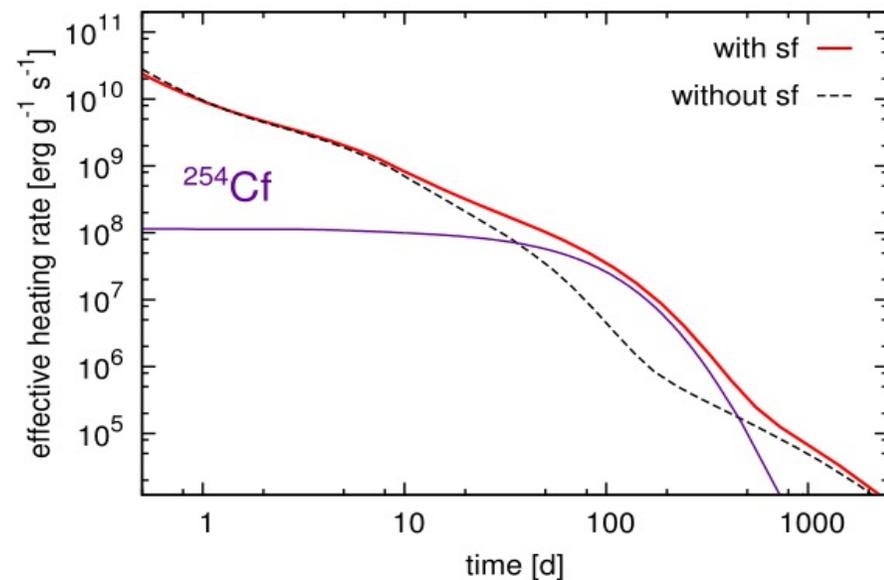
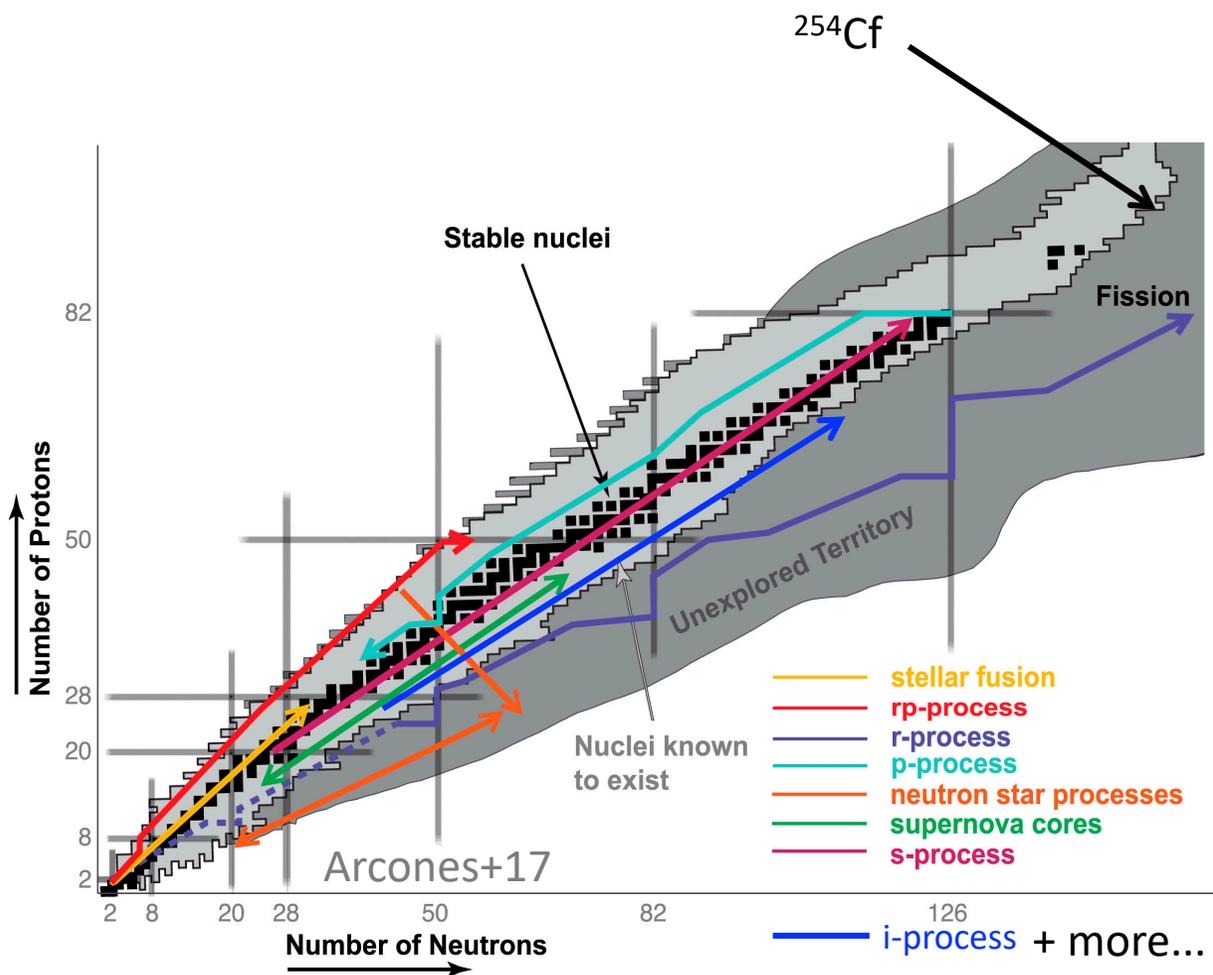
E. M. BURBIDGE, R. F. CHRISTY, AND W. A. FOWLER, *Kellogg Radiation Laboratory, California Institute of Technology, Pasadena, California*

(Received May 17, 1956)



W. W. Girdner/Caltech Archives

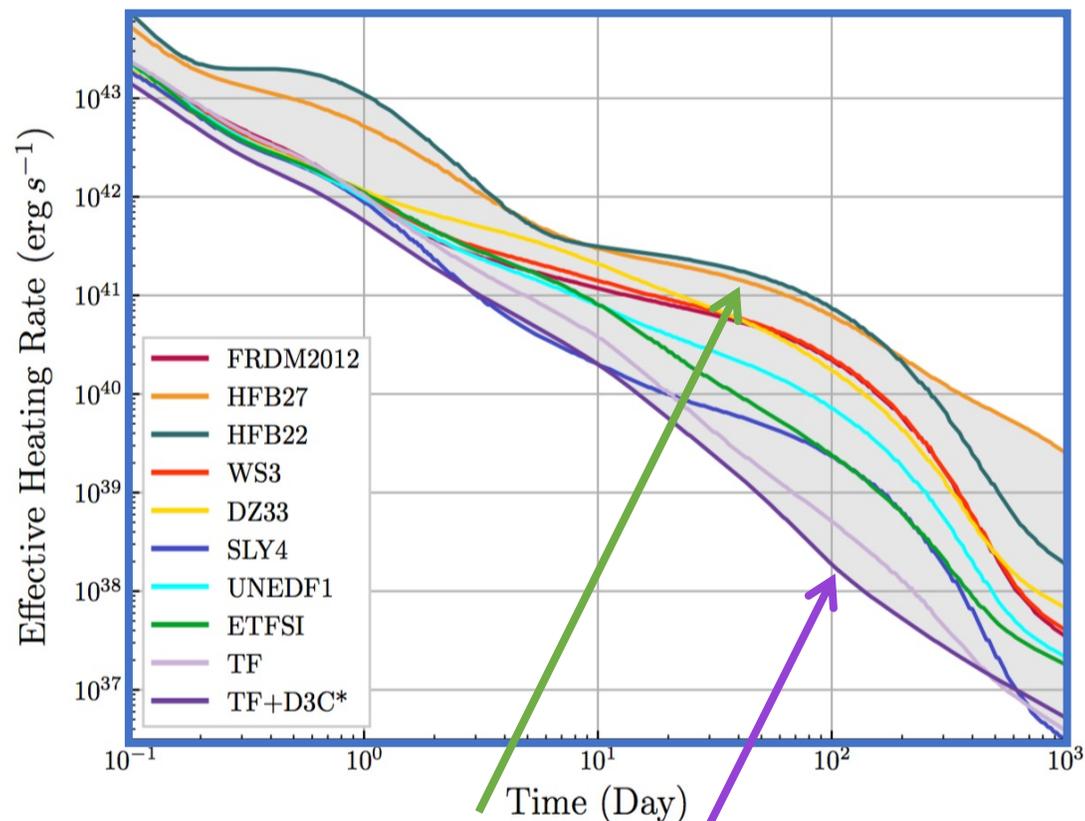
# Late time kilonova light curves can shed light on actinide production



Zhu+18; see also Wu+19

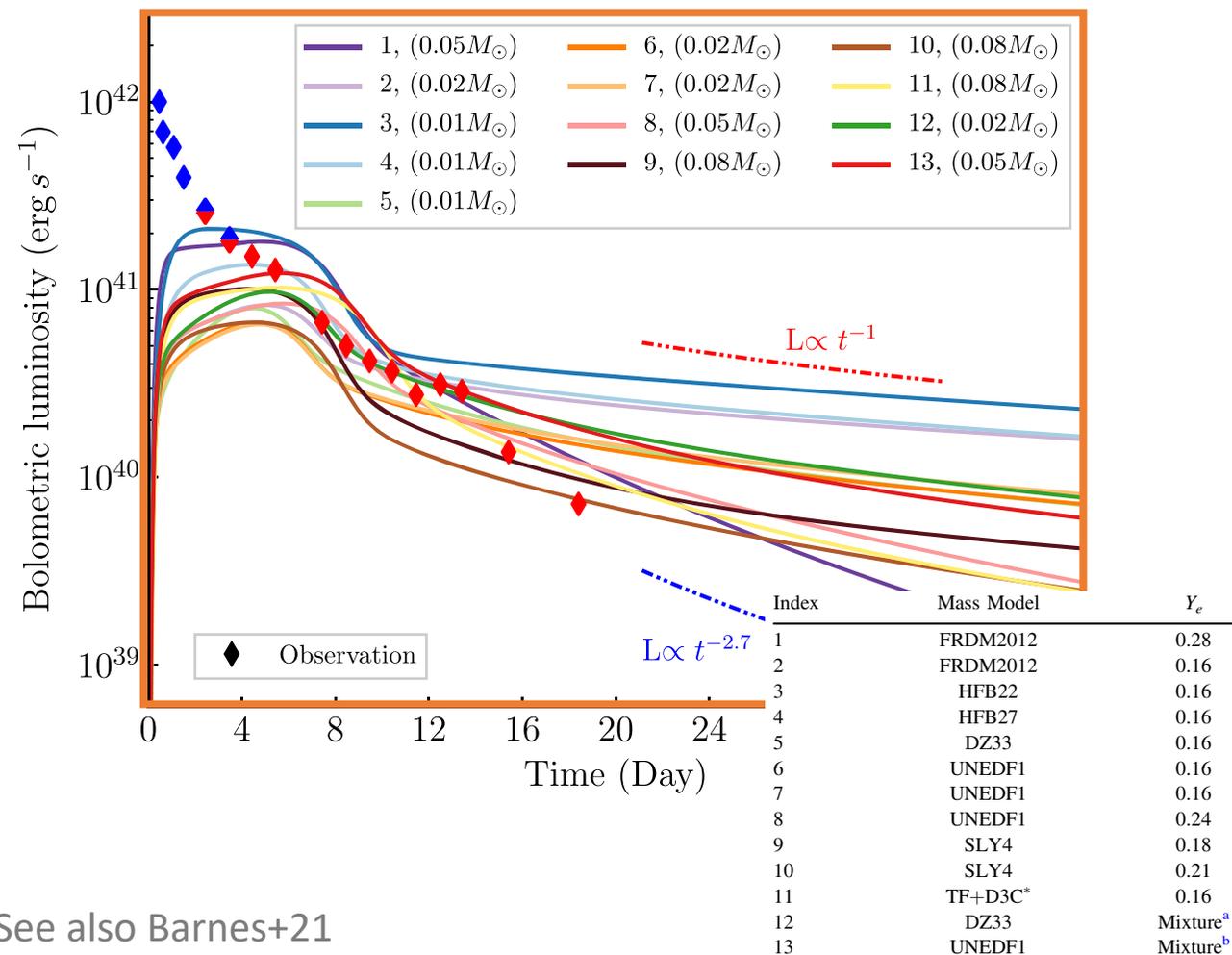
# Nuclear model influence on interpreting kilonova

Different abundance predictions affect nuclear heating, bolometric luminosity, and inferred ejecta mass by roughly an order of magnitude or more



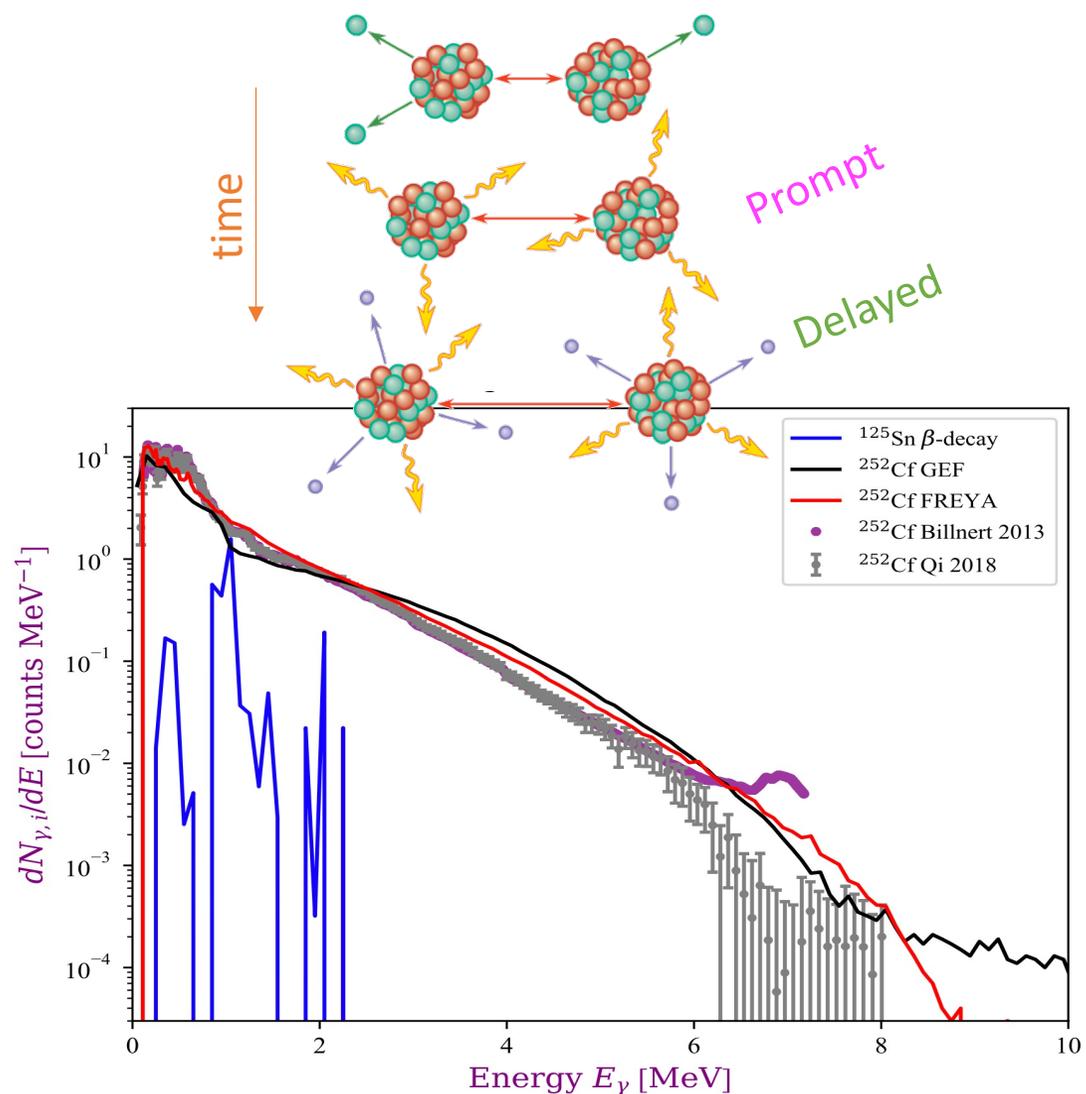
Nuclear models that strongly populate long-lived actinides

Nuclear models that don't

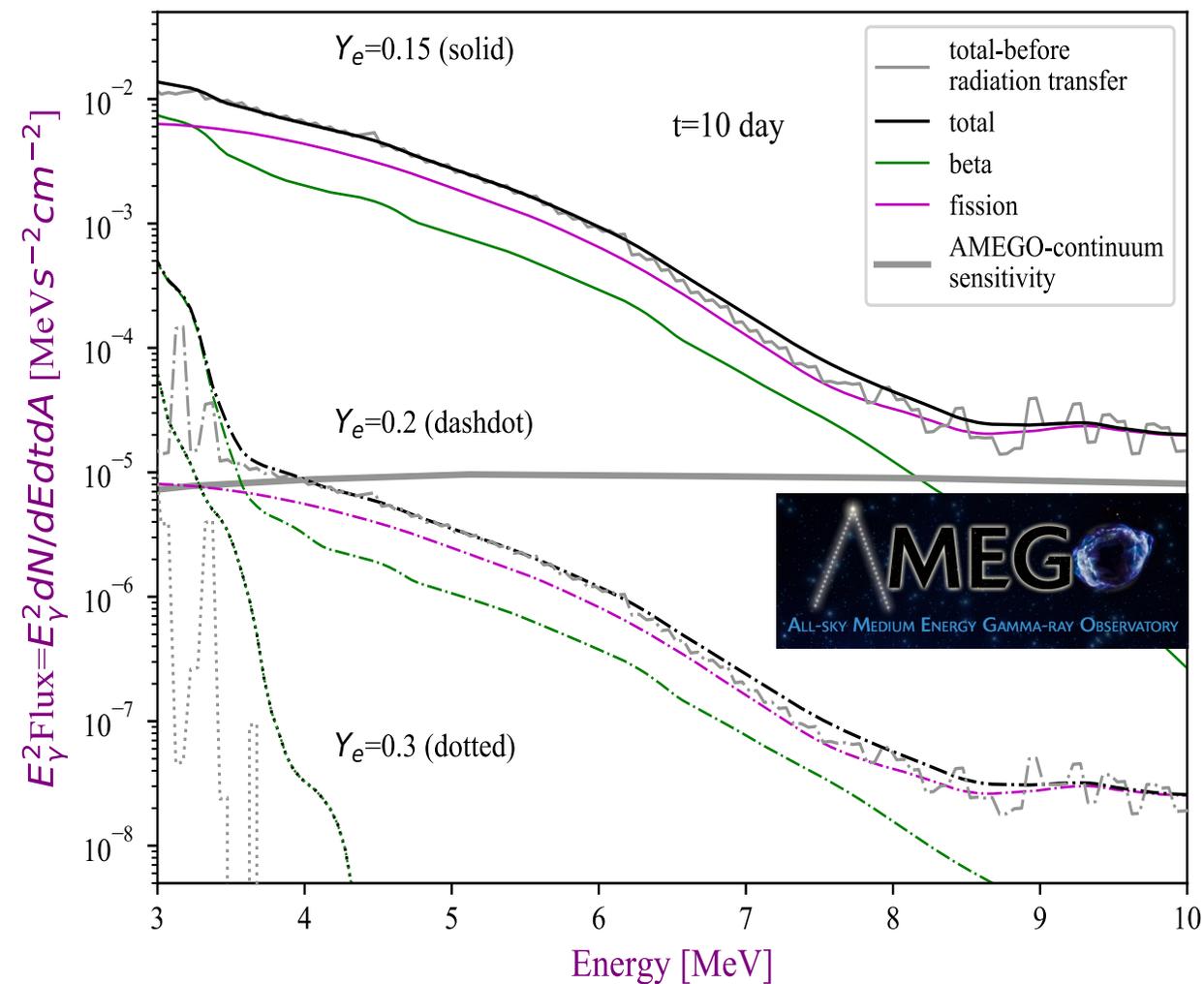


Zhu,Lund+21; See also Barnes+21

# Another possible signature of fission: MeV gamma rays



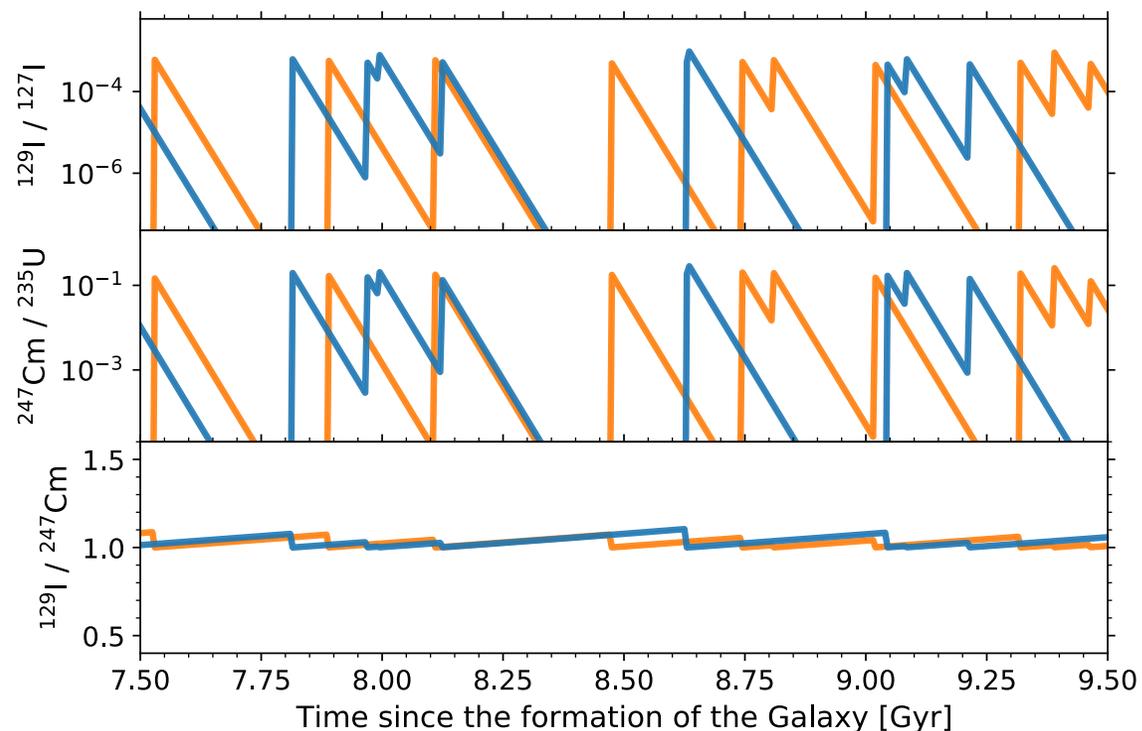
Wang,Vassh+20 using GEF inputs from Vassh+19



# A closer look at Curious Marie: the nature of the last $r$ -process event in our solar system

Only 4 radioactive isotopes in meteorites linked to  $r$  process with  $T_{1/2} < 1$  Gyr:

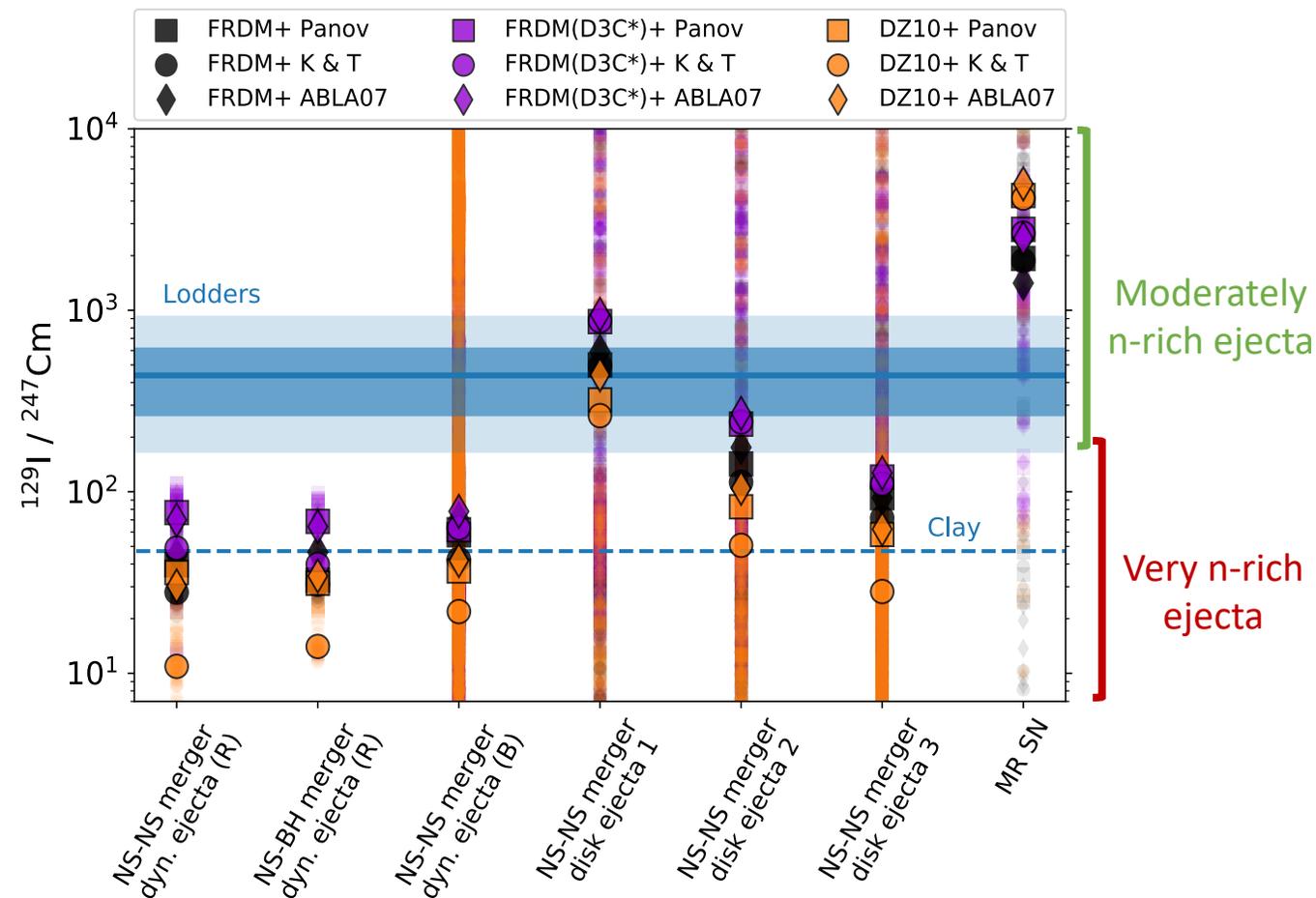
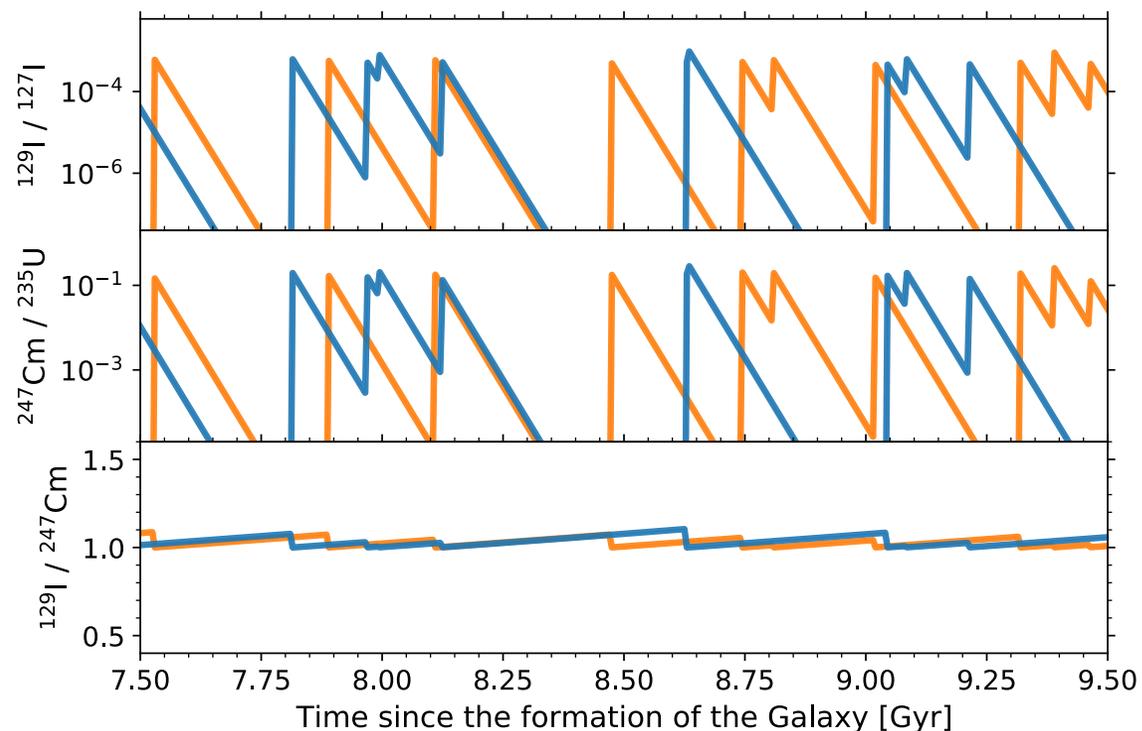
$^{129}\text{I}$	$T_{1/2} = 15.7$ Myr	$^{244}\text{Pu}$	$T_{1/2} = 80$ Myr
$^{247}\text{Cm}$	$T_{1/2} = 15.6$ Myr	$^{235}\text{U}$	$T_{1/2} = 700$ Myr



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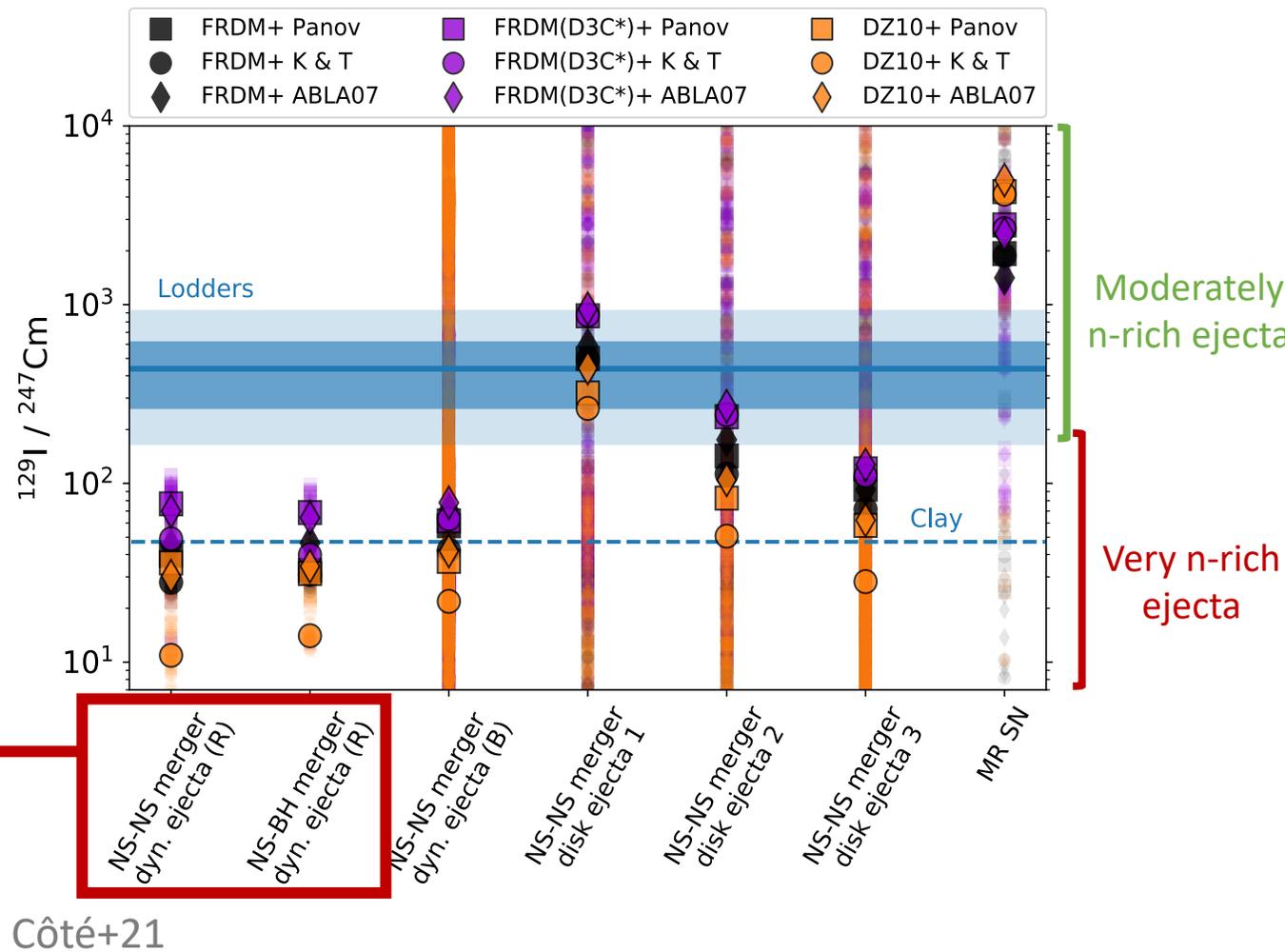
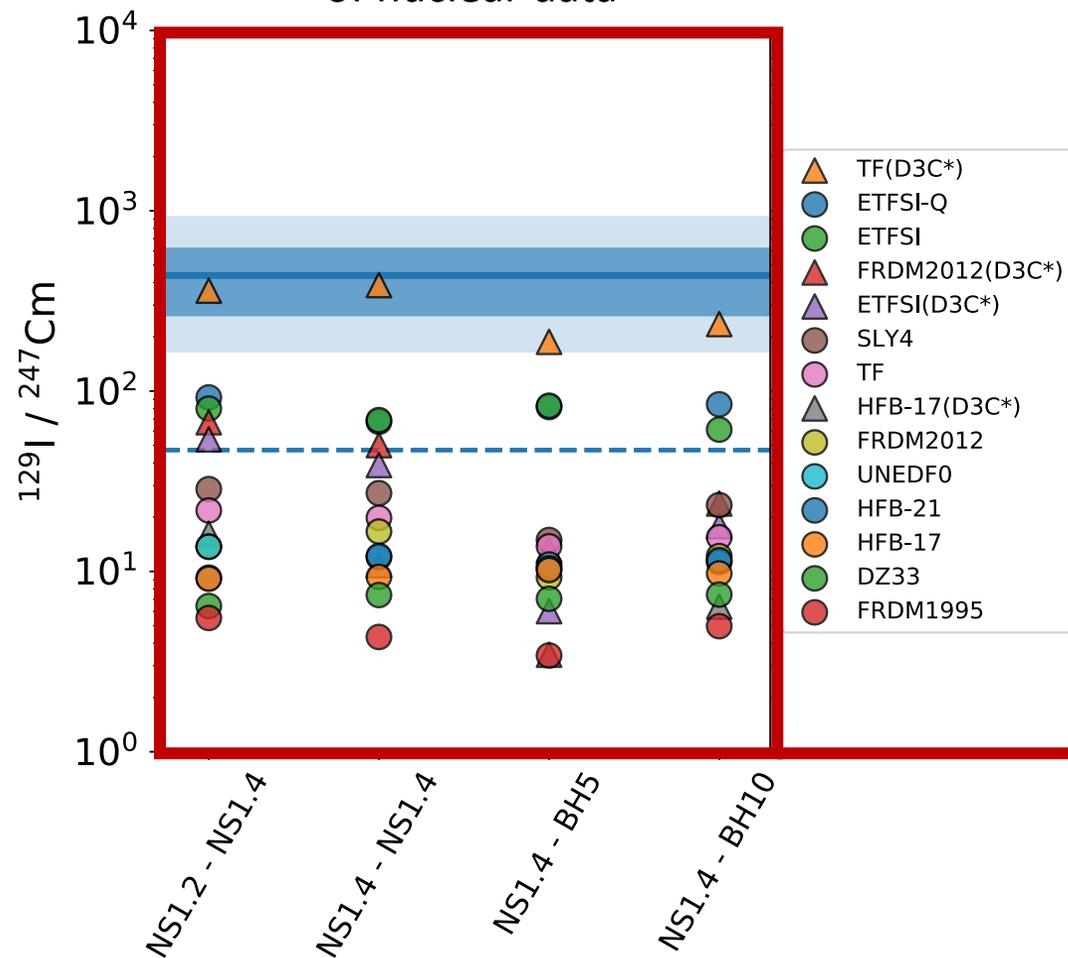
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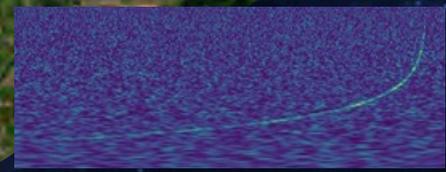
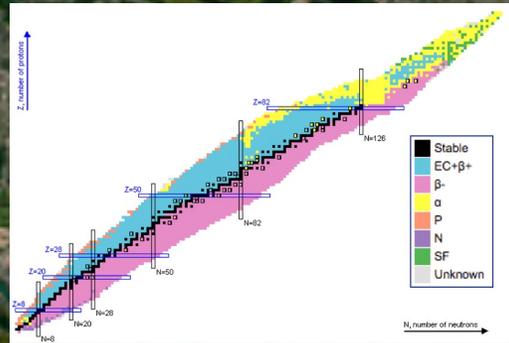
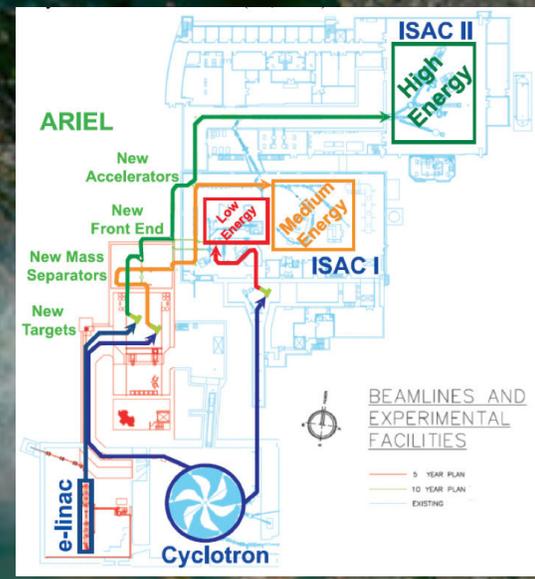
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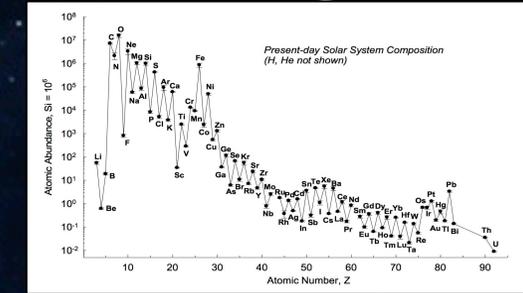
PRISM calculations with 12 sets of nuclear data



# Multi-messenger nuclear astrophysics



## Solar and Stellar Abundances



Experiment + Fundamental Theory

Nuclear Properties

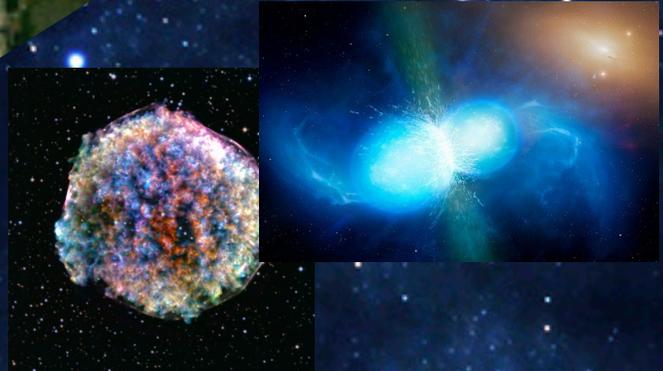
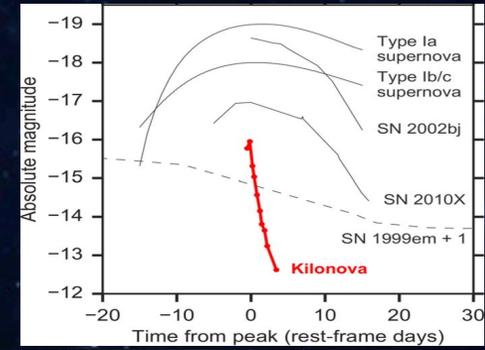
Astrophysical Observables

Astrophysical Sites

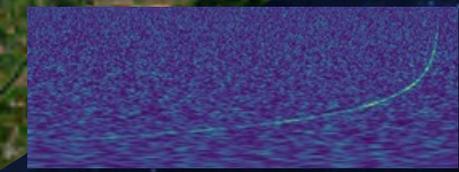
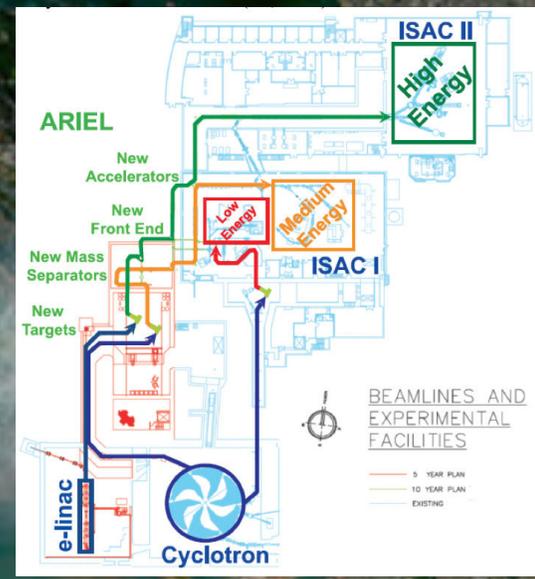
Galactic Origins

Physics of Nucleons	Degrees of Freedom	Energy (MeV)
quarks, gluons	24	940 (nucleon mass)
constituent quarks	3	140 (pion mass)
baryons, mesons	3	8 (pion separation energy in had)
quarks, gluons	24	1.32 (vibrational state in had)
nucleons, baryons and currents	3	0.043 (rotational state in nucleus)
collective coordinates	3	

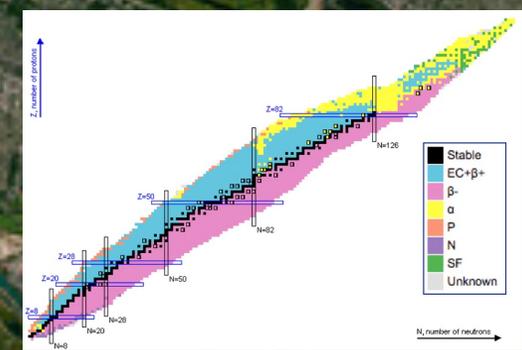
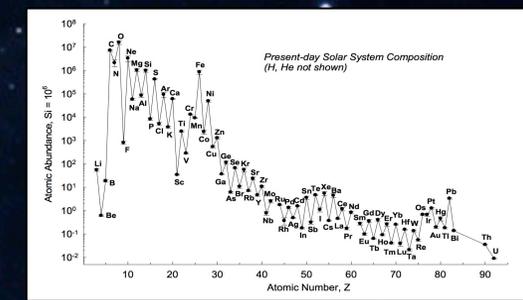
## Electromagnetic Emission



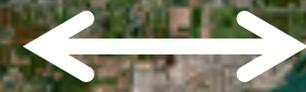
# Multi-messenger nuclear astrophysics



## Solar and Stellar Abundances



Experiment + Fundamental Theory



Nuclear Properties

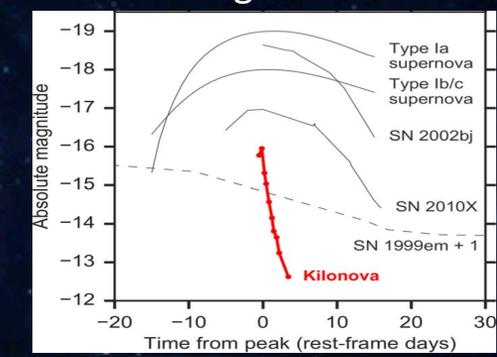
+

Astrophysical Sites



Astrophysical Observables

## Electromagnetic Emission



Galactic Origins

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	nucleonic, bosonic and currents	1.32 (vibrational state in lead)
	collective coordinates	0.043 (rotational state in uranium)

