



中国科学院高能物理研究所

Institute of High Energy Physics, Chinese Academy of Sciences



Lithium vapour

Wakefield  
acceleration

# Recent Progress on CEPC Plasma Injector

Ion channel

Pulse electrons

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on behalf of THU-IHEP AAC group



# Outlines



- **PWFA error analysis and hosing instability**
  - ✓ **Flashback: tolerance studies last year**
  - ✓ **Shorter drive beam and lower transformer ratio**
  - ✓ **General analysis on hosing instability**
- **“Perfect” beam loading for a two-bunch PWFA**
- **Preliminary results on PWFA experiment @ SXFEL**
- **PWFA test facility consideration**



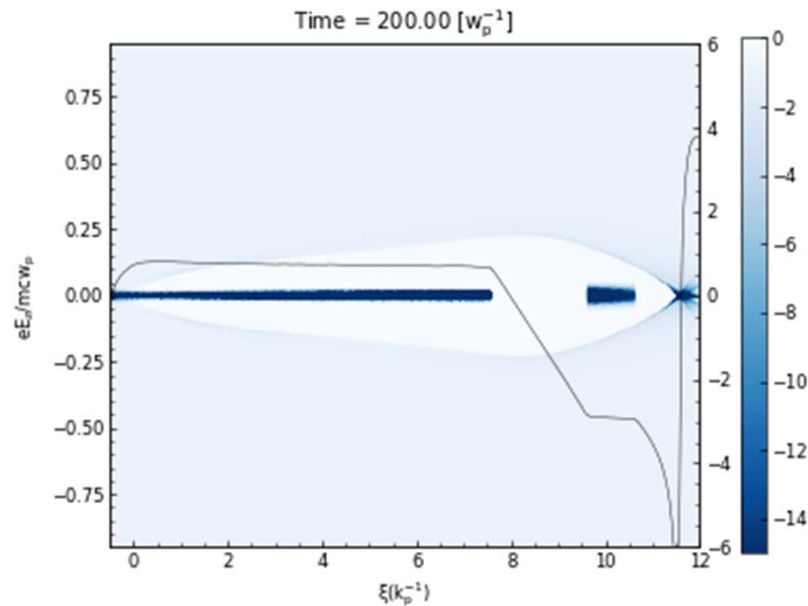
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# HTR e- acceleration without error



|   |          |
|---|----------|
| Accelerating distance (m)                     | 10.65    |
| Driver energy $E(GeV)$                        | 1.30     |
| Trailer energy $E(GeV)$                       | 45.5     |
| Normalized emittance $\epsilon_n(mm\ mrad)$   | 98.44    |
| Charge(nc)                                    | 0.84     |
| Energy spread $\delta_E(\%)$                  | 0.56     |
| TR  | $\sim 4$ |
| Efficiency (%) (driver $\rightarrow$ trailer) | 59.1     |

- 10 GeV  $\rightarrow$  45.5 GeV e- acceleration,  $R \sim 4$
- $n_e = 5 \times 10^{15} \text{ cm}^{-3}$ , the driver is about 2 ps (600  $\mu\text{m}$ ,  $\xi \sim 8$ )
- Hosing instability occurs at  $\sim 130000 \omega_p^{-1}$  and start to lose particles at  $\sim 150000 \omega_p^{-1}$
- **Assuming fully symmetric drive and witness bunches !**



# Error analysis → fully symmetry



| Perturbation          |         | Limitation      | limiting factor     |
|-----------------------|---------|-----------------|---------------------|
| beam charge           | Driver  | [-1%, 0.8%]     | $E_t$<br>$\delta_E$ |
|                       | Trailer | [-0.24%, 2%]    | $E_t$               |
| beam length           | Driver  | $\pm 1\%$       | $E_t$               |
|                       | Trailer | $\pm 5\%$       | $E_t$               |
| initial energy        | driver  | [-1%, 0.38%]    | $E_t$               |
|                       | trailer | [-1.75%, 0.37%] | $E_t$               |
| beam distance         |         | [-1um, 0.25um]  | $E_t$               |
| initial energy spread |         | 3.9%            | $E_t$<br>$\delta_E$ |
| Spot size             | driver  | [-40%, 2%]      | $E_t$               |
|                       | trailer | [8%, 8%]        | $E_t$               |



# Error analysis → not fully symmetry

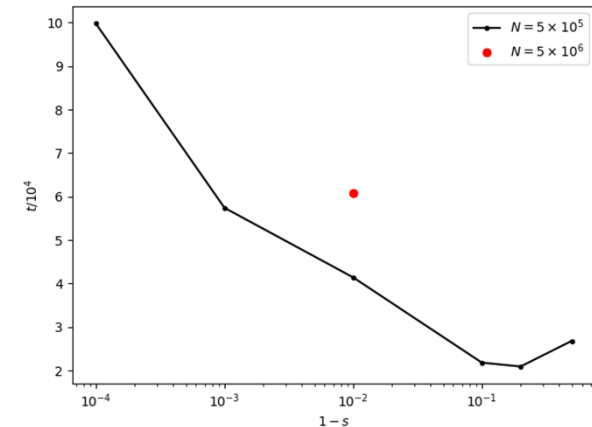
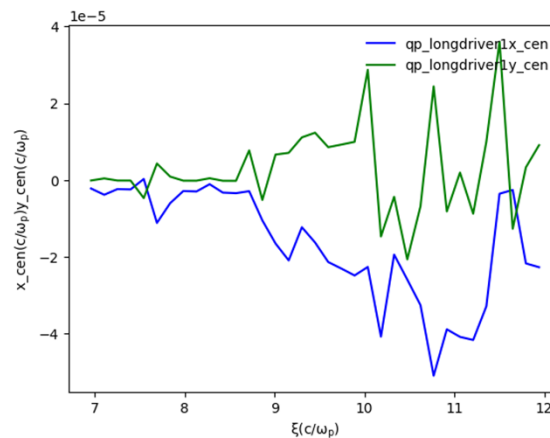
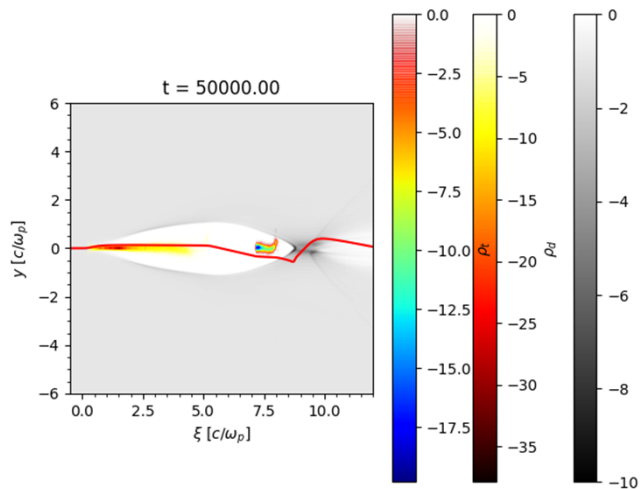


|              |                     |         |                      |
|--------------|---------------------|---------|----------------------|
| Slice jitter | Transverse position | Driver  | $\pm 0.025\text{nm}$ |
|              |                     | Trailer | $\pm 3.7\mu\text{m}$ |
|              | Transverse velocity | Driver  | $< 0.1\text{nrad}$   |
|              |                     | Trailer | $< 5\mu\text{rad}$   |

metry, even let  $\langle x_d \rangle = 0$ , the example, adding only **0.025nm** Actually, the resolution of the d noise. **Is it physical or not?**

We did different studies and found that:

- Increase particle number → hosing improved
- Increase the jitter (noise) to dx level or larger → hosing became more serious
- Partial particles asymmetry → hosing improved



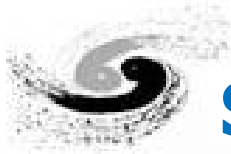
$5 \times 10^5$  particles 99.99% symmetry  $\sigma_z \sim 5$  lose 50% particles at  $100000 \omega_p^{-1}$



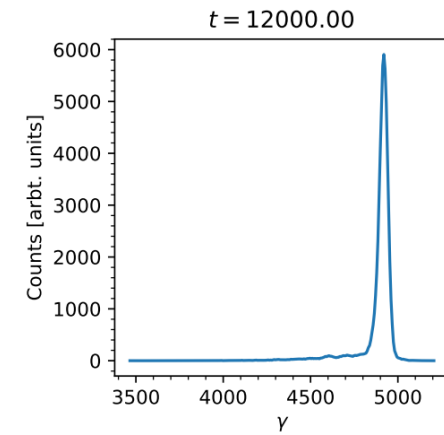
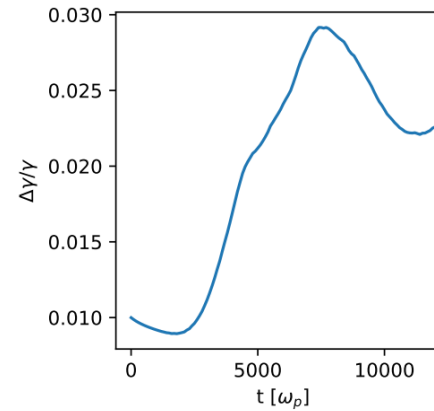
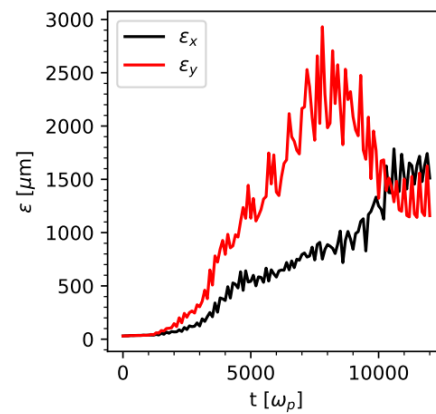
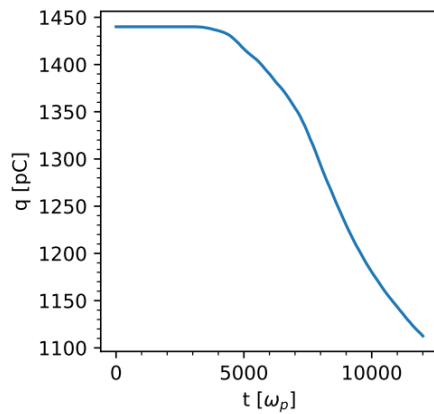
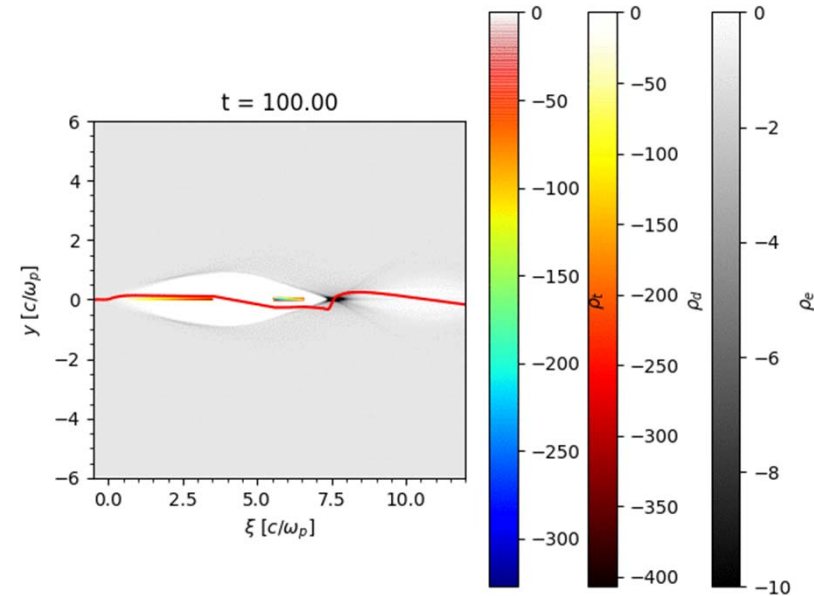
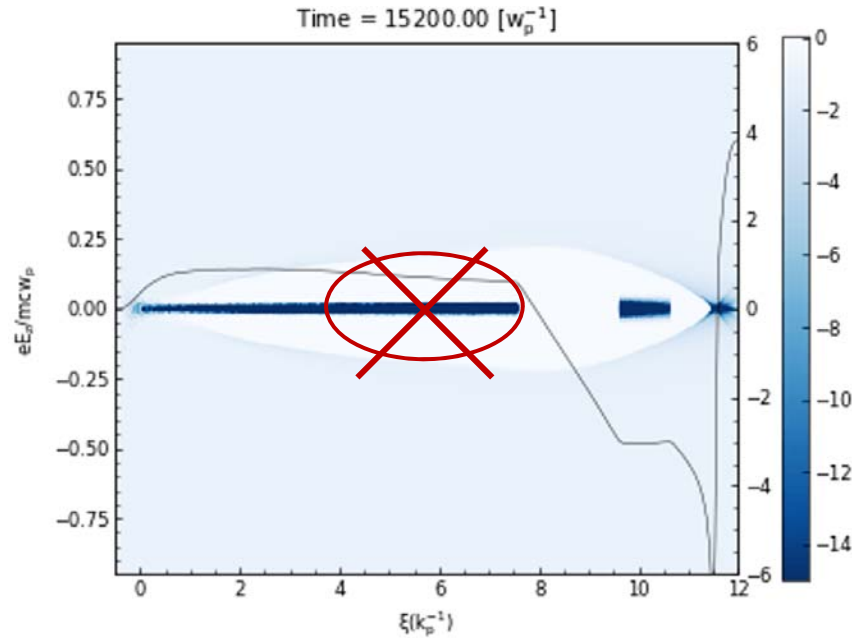
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# Short driver for more stable acc.







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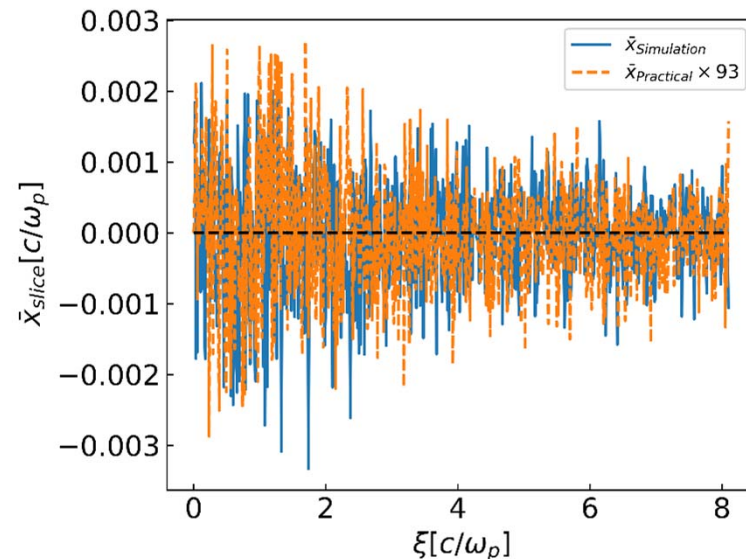
# Initial noise macro vs. practical



- An important question is “How do the beams evolve from their initial statistical noise?”
- Another question is “Does the hosing instability set any limit on the transformer ratio of PWFA?”

## Initial noise of a collimated beam

- Particle number is  $N$ , transverse profile is Gaussian with r.m.s. size  $\sigma_r \rightarrow$  the jitter of bunch center obeys a Gaussian distribution  $N(0, \sigma_r/\sqrt{N})$
- For PIC simulation, number of macro particle is much less than practical particle number, so the initial noise level is different in magnitudes.
- For a 5.8nC driver, the particle number in QuickPIC is  $128 \times 128 \times 256$ , which is  $1/93^2$  of the practical particle number.





# Hosing instability in bubble regime



➤ A straightforward way to calculate the asymptotic solution.

➤ For the most basic equations

$$\frac{\partial^2 x_b}{\partial s^2} + x_b = k_\beta^2 x_c$$

$$\frac{\partial^2 x_c}{\partial \xi^2} + \omega_0^2 x_c = \omega_0^2 x_b$$

$$\partial_\xi^2 \partial_s \bar{x}_b = \frac{\omega_0^2 k_\beta^2}{2ik_\beta} \bar{x}_b$$

➤ With the short pulse, long range limit, we can assume

$$x_b = \bar{x}_b e^{ik_\beta s}$$

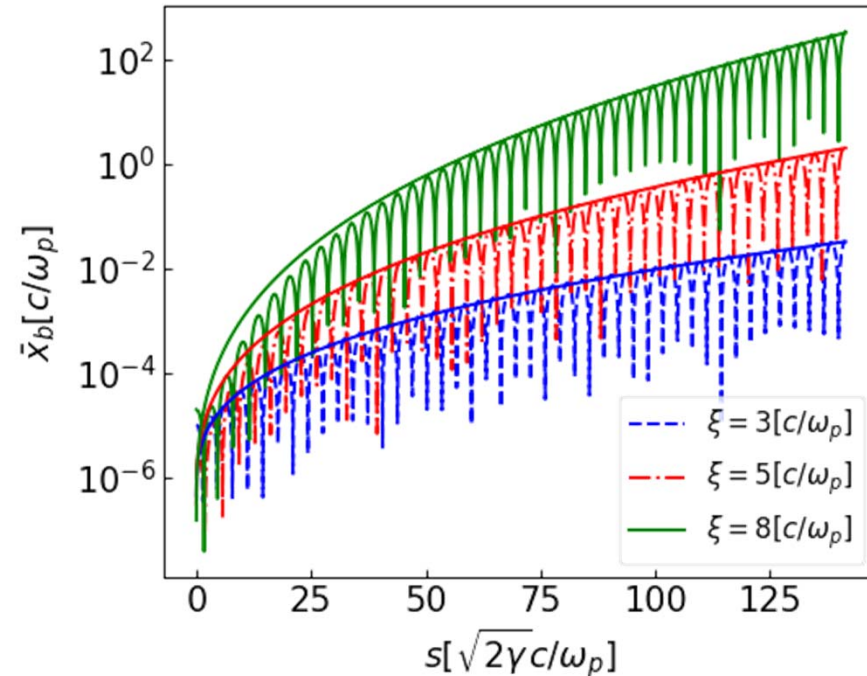
$$x_c = \bar{x}_c e^{ik_\beta s}$$

➤ Under this limit,  $\partial_s \ll k_\beta, \partial_\xi \gg \omega_0$ , and we have

$$2ik_\beta \partial_s \bar{x}_b = k_\beta^2 \bar{x}_c$$

$$\partial_\xi^2 \bar{x}_c = \omega_0^2 \bar{x}_b$$

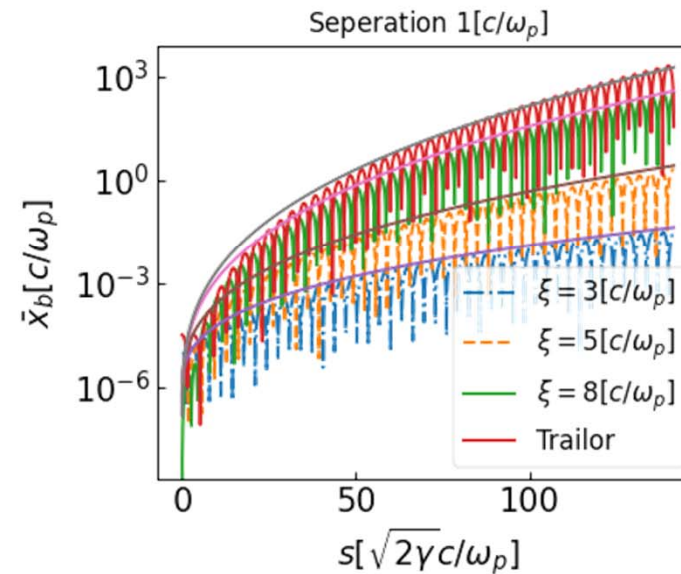
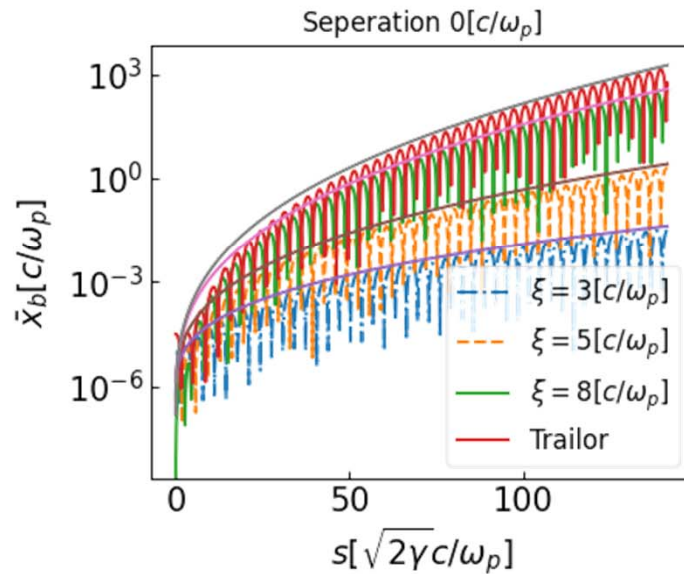
➤ Let  $\bar{x} = A e^{\gamma_0 (k_\beta s)^m (\omega_0 \xi)^n}$



C. Huang, W. Lu et al., PRL **99**, 255001 (2007)



# Witness beam's hosing instability



Different separation has little effects on hosing growth. Which means bunch train may not effective for damping hosing instability



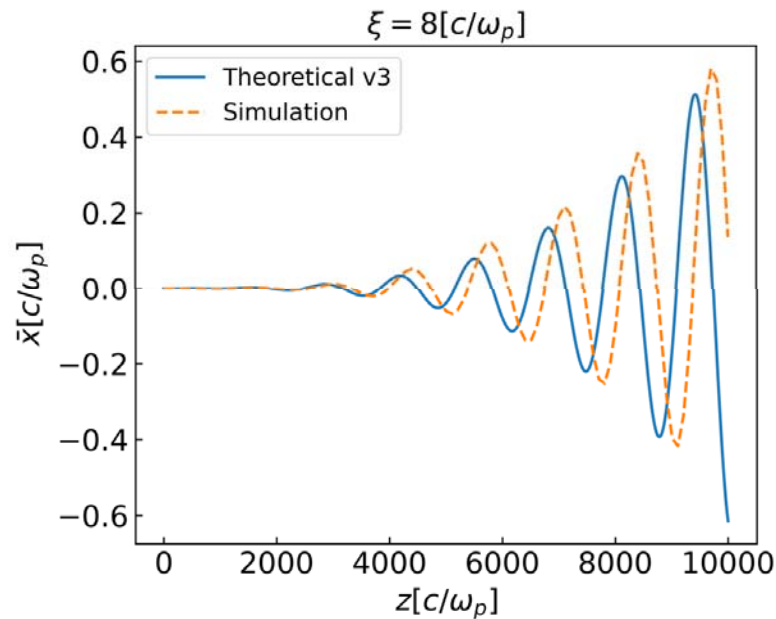
# PIC results Vs. Numerical solution



- Take the  $c_r, c_\psi$  into consideration
- Other damping regime, such as the energy spread, nonlinear focusing force can be quantified by the damping of  $x_b$

$$\text{➤ } \frac{\partial^2 x_c}{\partial \xi^2} + c_r c_\psi \omega_0^2 x_c = c_r c_\psi \omega_0^2 c_b x_b$$

$c_r, c_\psi$  from  
simulation  
 $c_b = 0.8$



**The asymptotic solution agrees well with the PIC simulation result**



# Transformer Ratio limitation

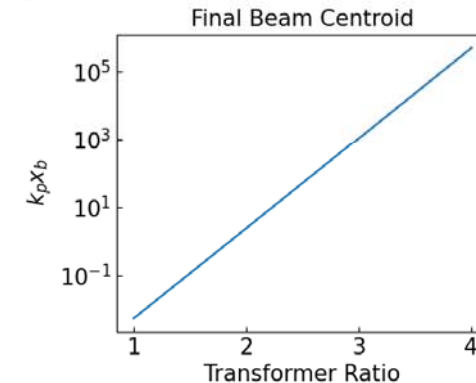


- Transformer ratio  $R$ , Energy transfer efficiency 60%
- $Q_w = 1nC$ ,  $Q_d = 1.67RnC$ , Beam size  $\sigma_r$
- Initial noise level  $\sim \frac{\sigma_r}{\sqrt{N}} = \frac{1.27\sigma_r}{\sqrt{1+1.67R}} \times 10^{-5}$
- Drive beam length  $k_p L_d \sim 2R$
- Witness beam length  $k_p L_w \sim 1$
- Initial energy  $\gamma_0$
- Accelerating distance  $k_p s \sim \gamma_0 R$

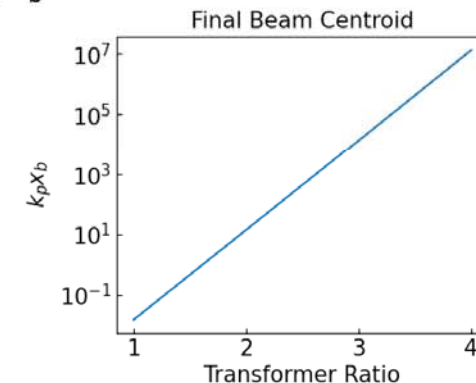
➤ We can obtain the final beam centroid of the witness beam at the end of the acceleration

$$\text{➤ } x_b \sim \frac{1.27\sigma_r}{\sqrt{1+1.67R}} \times 10^{-5} \times e^{1.3\left(\frac{\gamma_0}{2}\right)^{\frac{1}{6}} c^{\frac{1}{3}} c_b^{\frac{1}{3}} R^{\frac{1}{3}} \left(\sqrt{2R+\frac{1}{\sqrt{2}}}\right)^{\frac{2}{3}}}$$

➤ For a 10GeV driver, beam size  $k_p \sigma_r = 0.2$ ,  $c=0.7$ ,  $c_b = 0.8$



➤ For a 20GeV driver, beam size  $k_p \sigma_r = 0.2$ ,  $c=0.7$ ,  $c_b = 0.8$



**Transformer ratio 1-1.5 is acceptable without extra damping regime**

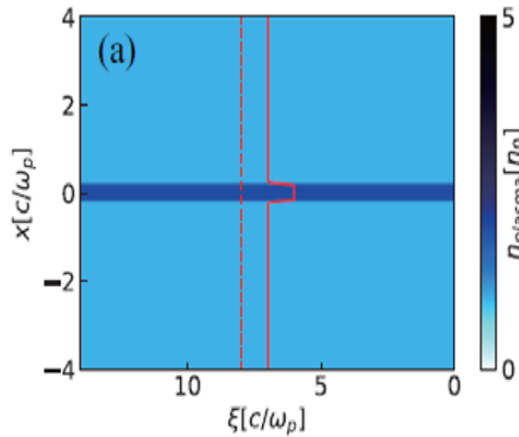




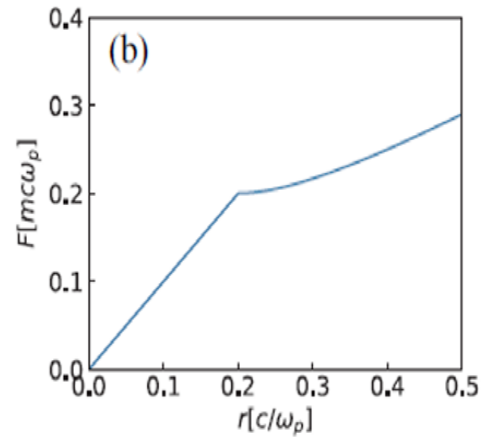
# One powerful damping method



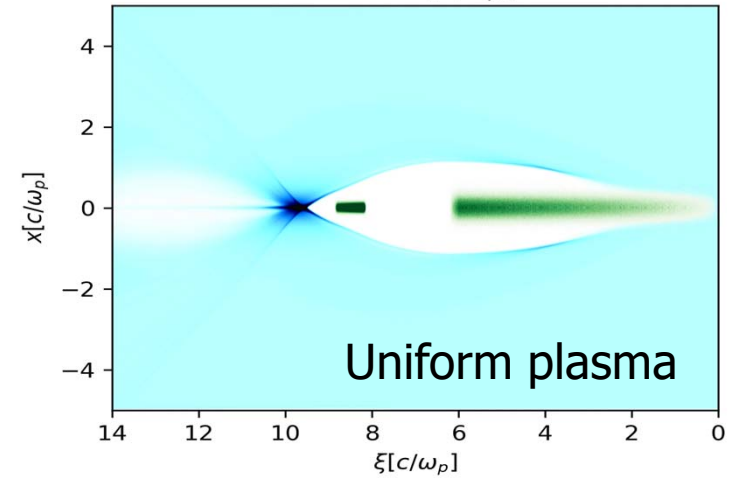
Plasma density profile



Transverse force

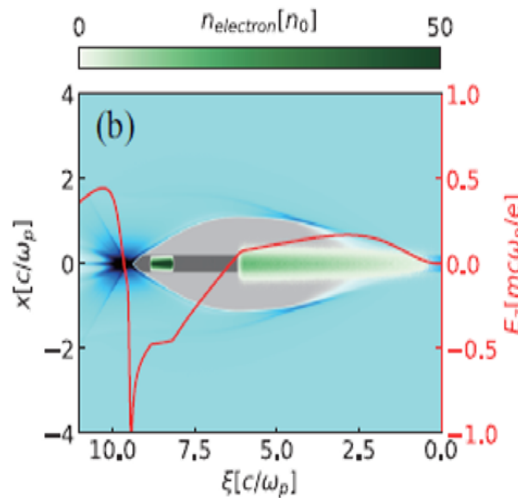
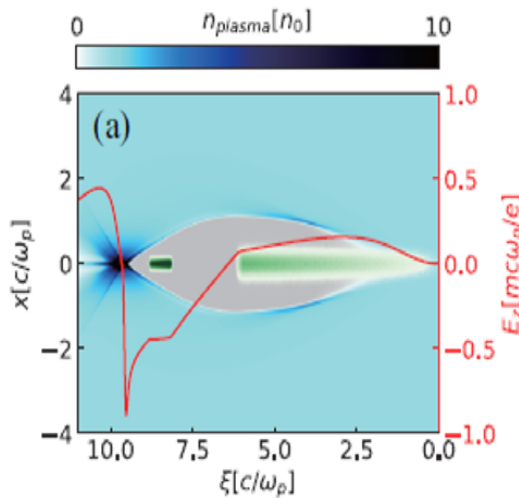


charge\_slice\_xz  
T = 4.0 [1/omega\_p]

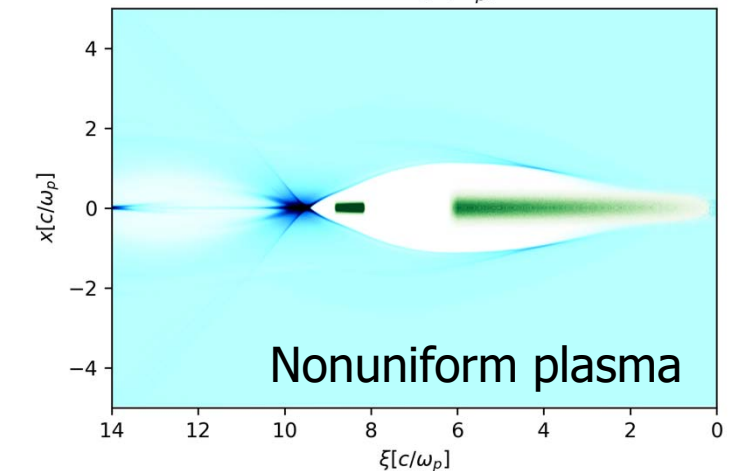


Uniform plasma

Little effects on Ez field



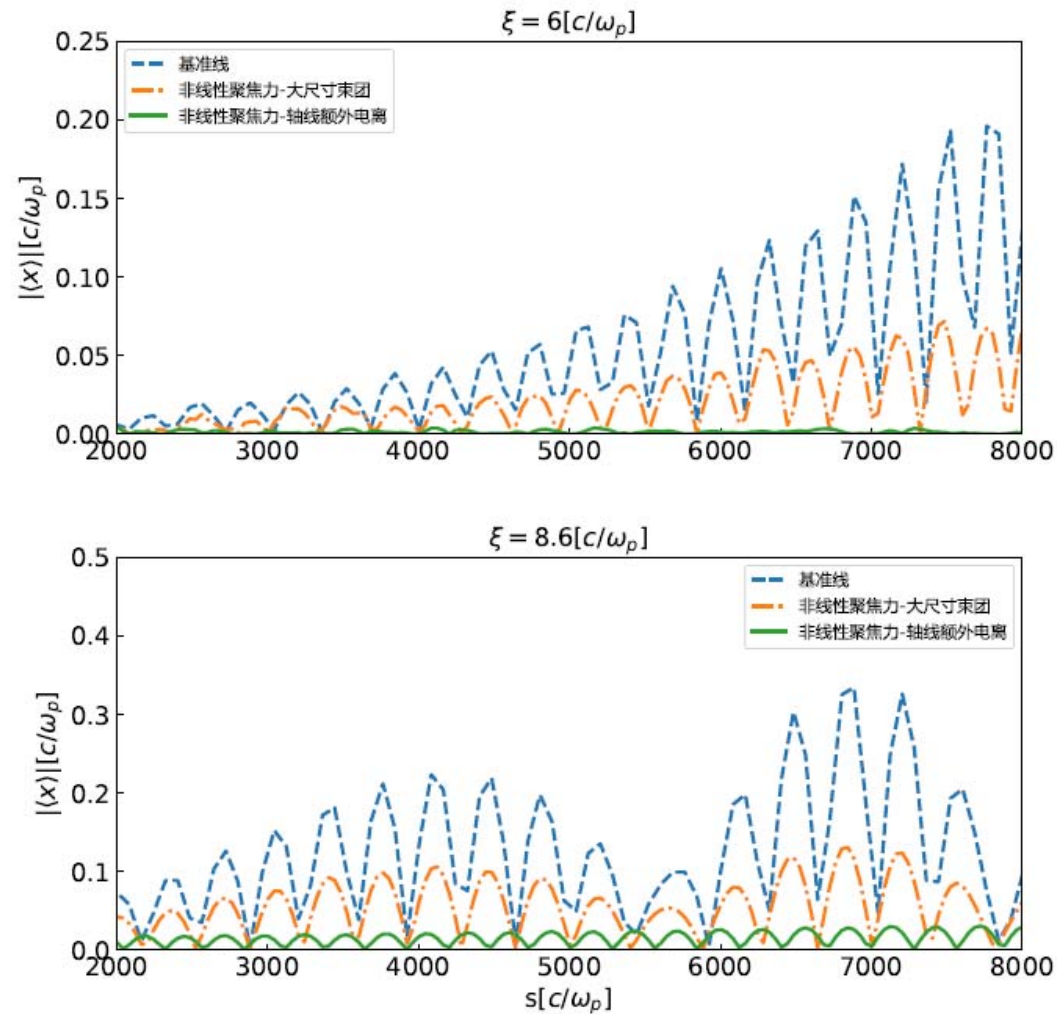
charge\_slice\_xz  
T = 4.0 [1/omega\_p]



Nonuniform plasma



# One powerful damping method







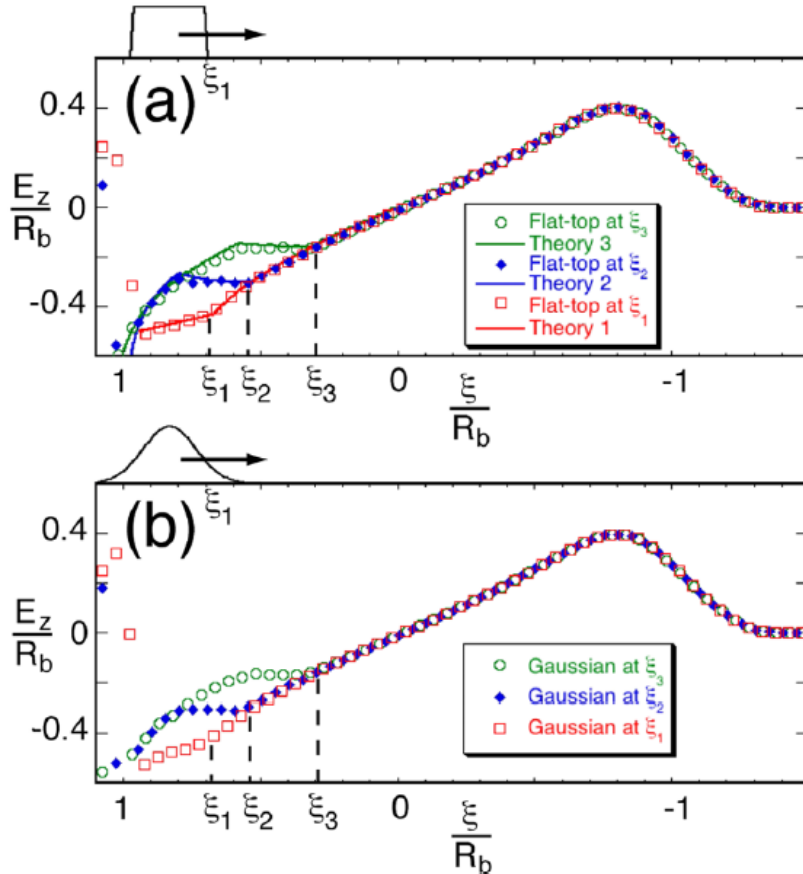
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# Motivation: find a matched condition



$$Q_s E_s = \frac{\pi R_b^4}{16}$$

$R_b$ : the maximum radius of the ion channel

$Q_s$ : the total charge of trailer

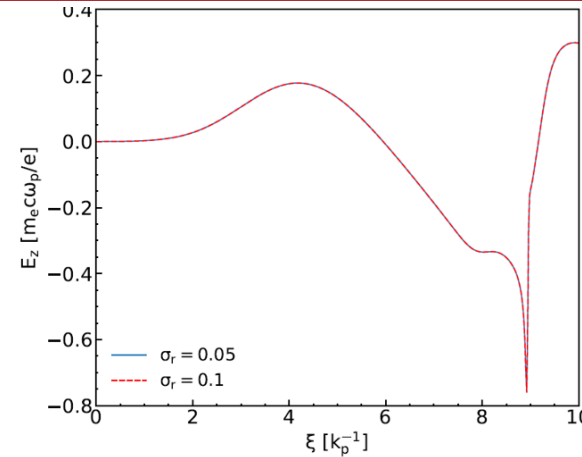
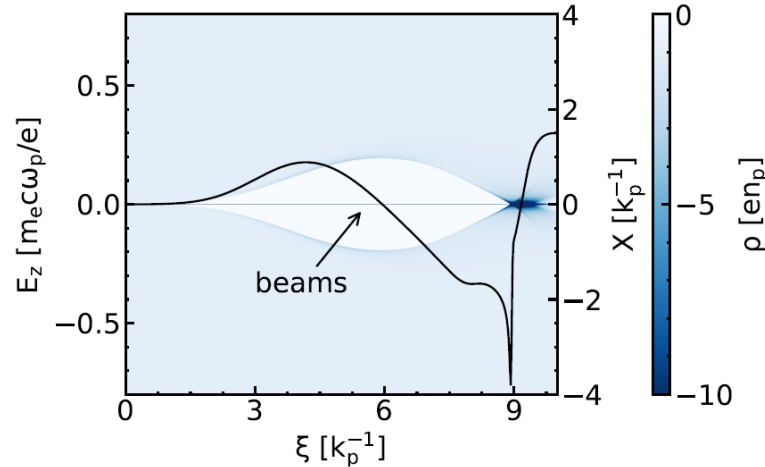
$E_s$ : the longitudinal wakefield at  $\xi_s$

- Not related to driver parameters
- Based on the assumption  $R_b \gg 1$
- Our goal: find proper bunch parameters of  $(Q_d, Q_t, \sigma_{zd}, \sigma_{zt}, \sigma_{rd}, \sigma_{rt}, d_{dt}, n_p)$

M. Tzoufras, W. Lu, et al., Phys Rev Lett 101, 145002 (2008)

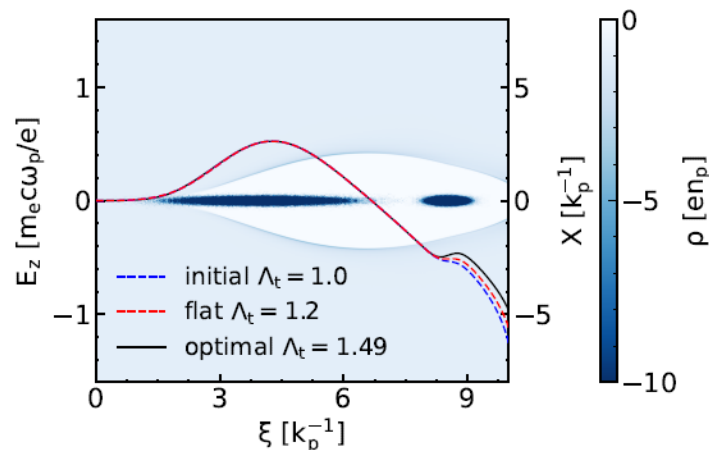


# Ignore $\sigma_r$ when $\sigma_r \ll R_b$



The acceleration structure is determined by the normalized charge per unit length  $\Lambda = n_b \sigma_r^2$  (not related to  $\sigma_r$ )

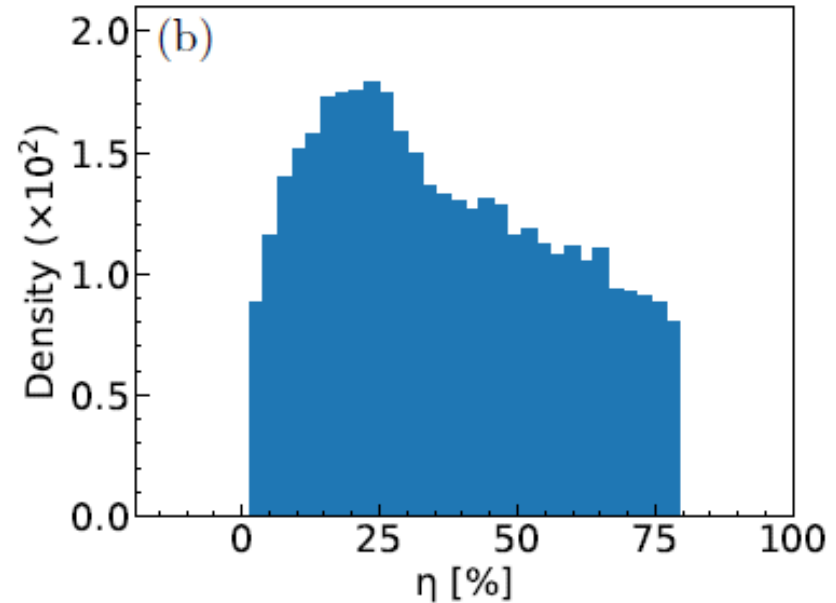
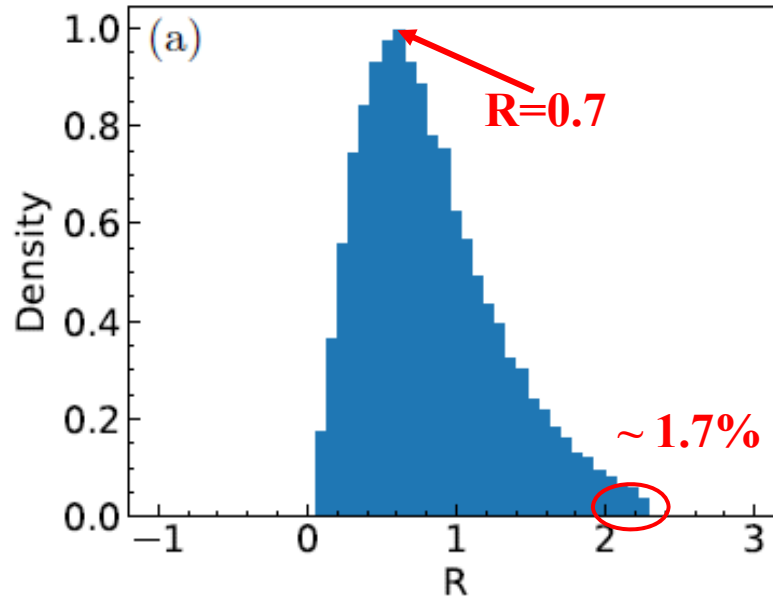
For given  $\Lambda_d, \sigma_{zd}, \sigma_{zt}, d_{dt}$ , we introduce BFGS (one of the most effective algorithms of quasi-Newton group) to find optimal  $\Lambda_t$  for smallest energy spread. Then we can get transformer ratio R directly in such condition.



- $\delta_E = 1.69\%$  at optimal  $\Lambda_t = 1.49$
- $\delta_E = 2.35\%$  at  $\Lambda_t = 1.2$
- Optimization time: 7min



# Statistics of the optimization



- Optimization average time: 7.6min
- Scanned a wide range bunch parameters (referenced FACET-II, FLASHForward, CLIC...)  
 $\Lambda_d$ : [0.0885,7.70]     $\sigma_{zd}$ : [0.0952,1.90]     $\Lambda_t$ : [0.0627,3.14]     $\sigma_{zt}$ : [0.0952,0.857]



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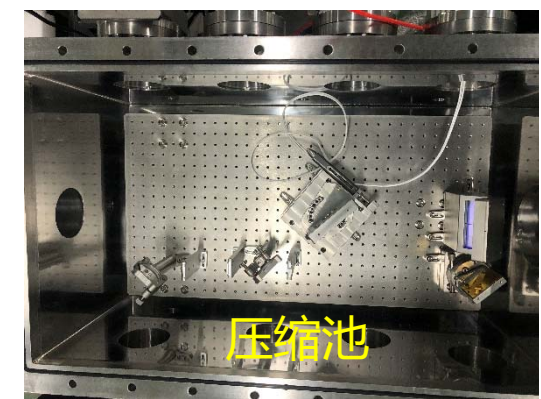
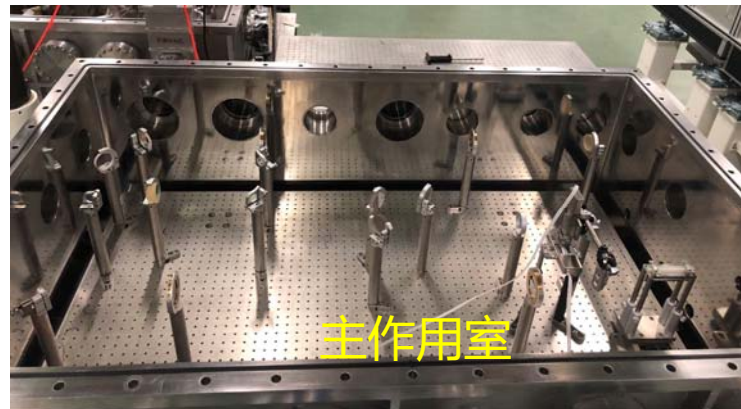
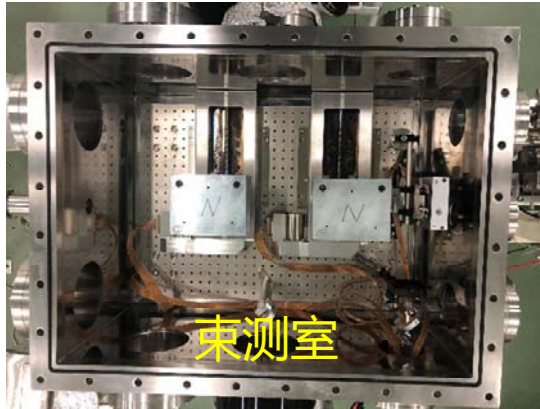


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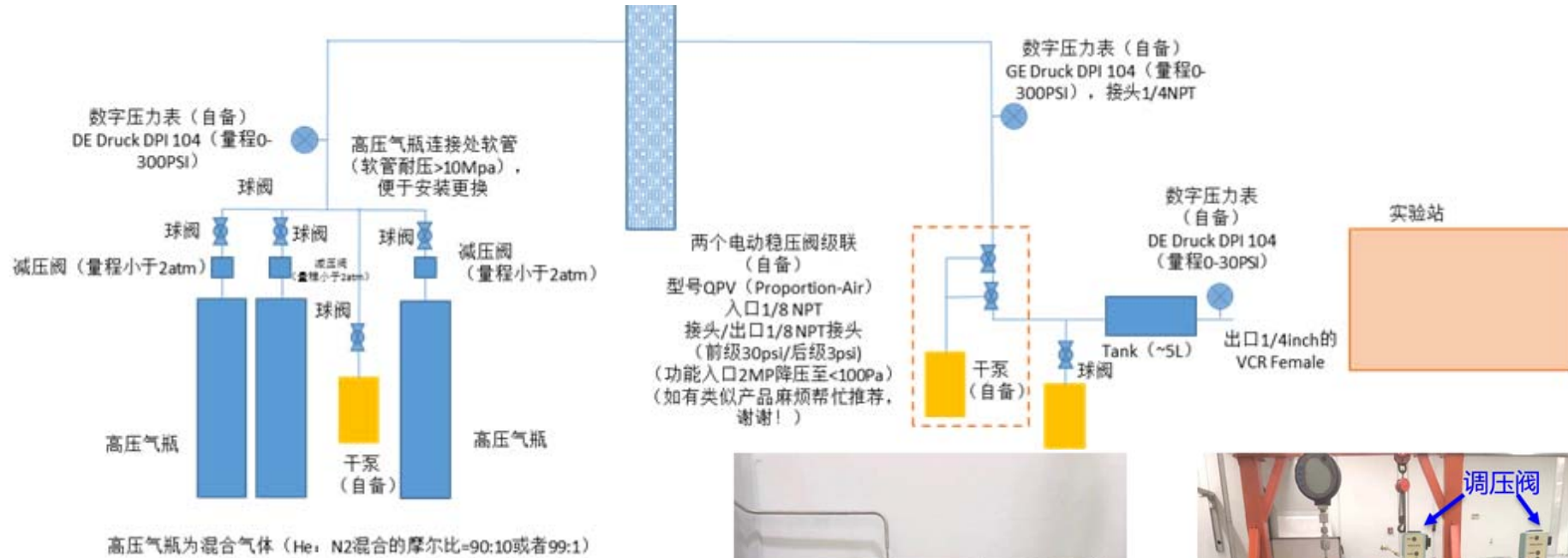
# Experiment preparation @ SXFEL



Slides from Dr. Bo Peng (2020)



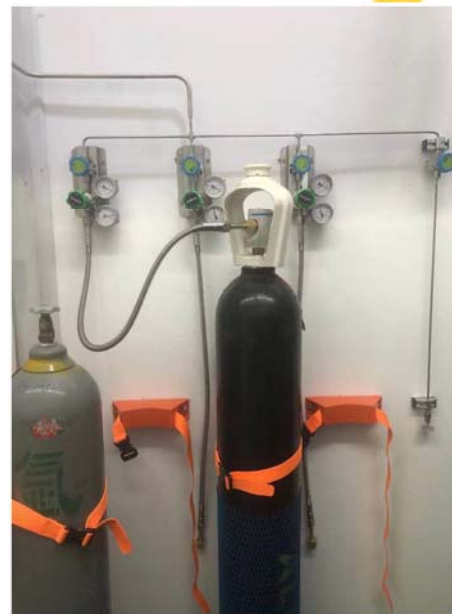
# Experiment preparation → gas loop



高压气瓶为混合气体 (He, N<sub>2</sub>混合的摩尔比=90:10或者99:1)

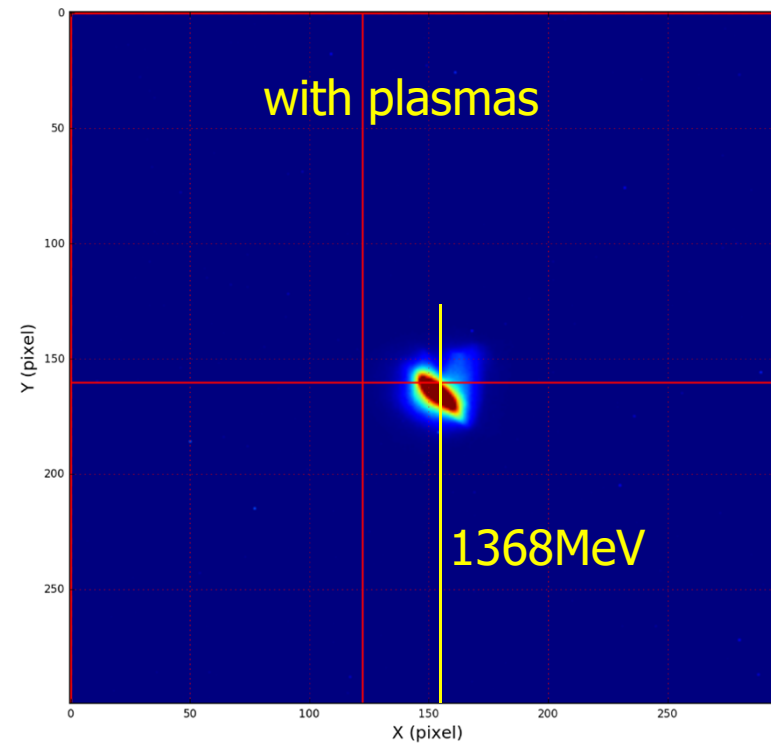
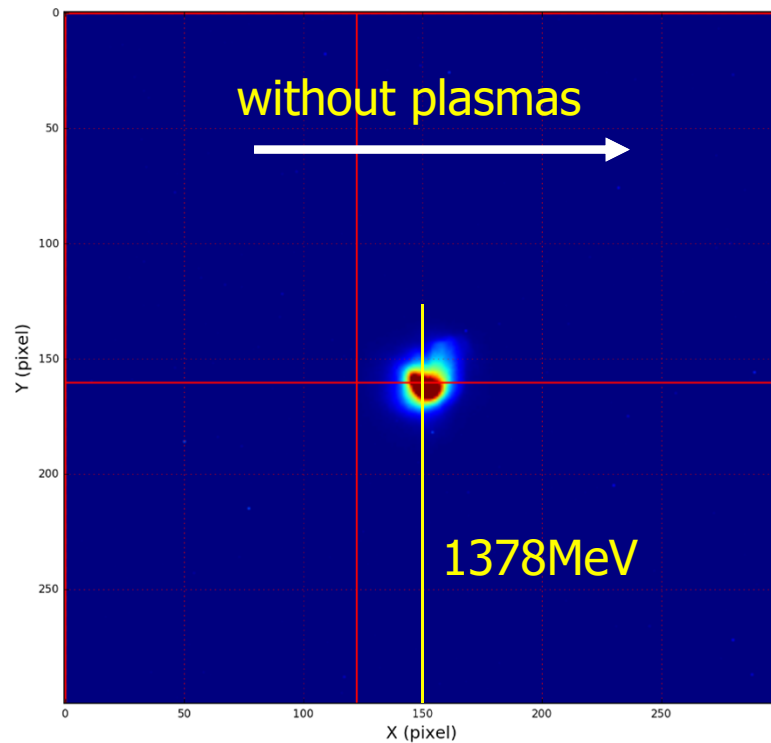
Requirement:

200 ~ 10<sup>5</sup> pa (Negative pressure)





# Preliminary experimental results



- ✓ Upgrade laser system, energy  $\sim 130\text{mJ}$ , pulse duration  $\sim 30\text{ fs}$  done
- ✓ Installation of light path, gas loop and diagnostic system done
- ✓ Laser and electron beam synchronization done
- ✓ Plasma dechirper experiment results, electron deceleration in plasmas ( $\sim 10\text{ MeV}$ )





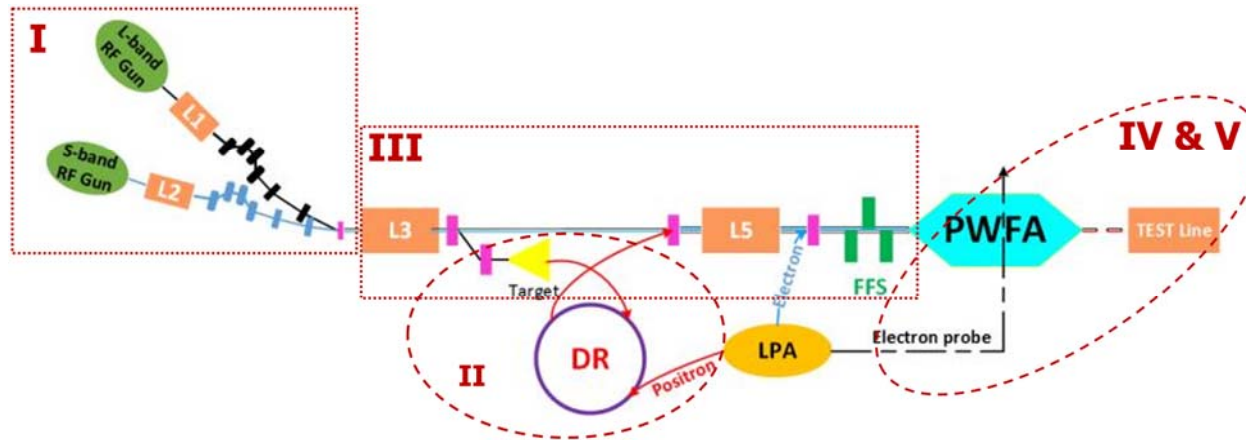
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# Test facility for plasma-based acc.



## Key requirements of the test facility:

- High charge L-band e- gun  $\rightarrow > 6$  nC / bunch
- Longitudinal shaped bunch  $\rightarrow$  laser shaping and/or EE
- Longitudinal modulation at transport line
- Two e- bunches “perfect” merging  $\rightarrow$  Essentially solved, with  $\sim 1\%$  energy difference
- e- Bunch compressor design  $\rightarrow$  optimized (2 bunches compressed in one structure)
- FFS to achieve very small beam size  $\rightarrow \sim 40\mu\text{m}$  @ 1 GeV/ 30 mm·mrad
- Cascaded with plasma accelerator  $\rightarrow$  need plasma matching section
- High current, low emittance  $e^+$  beam  $\rightarrow$  low energy damping/stacking ring under consideration
- Very precise beam instrumentation and control  $\rightarrow$  better than 10 fs /  $1\mu\text{m}$



# Summary and prospects



## ■ Hosing instability and error analysis

- The asymptotic solution of hosing equations agrees well with the numerical solution, and the numerical solution can agree well with the PIC simulation results.
- Without extra damping mechanism, the growth of hosing instability from statistical noise is acceptable when transformer ratio is 1-1.5
- There are other powerful damping mechanisms. HTR is still possible

## ■ Experiment at SXFEL

- Finally the experiment started. So far the beam time is still limited
- A dedicated test facility is absolutely necessary

## ■ PWFA Test facility consideration

- Try to optimized linac design to meet the requirement of low beam energy and high charge
- Positron beamline and damping ring are under design
- For worst condition, high efficiency and reasonable linac requirement could be ensured, with the transformer ration around 1.5



A photograph of a large, modern building with a prominent glass facade and a classical architectural style, surrounded by snow-covered evergreen trees. The word "Thanks!" is overlaid in the center.

Thanks!