

强子物理中谱学阈值结构问题

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2021年国科大物理科学学院青年委员会研讨会

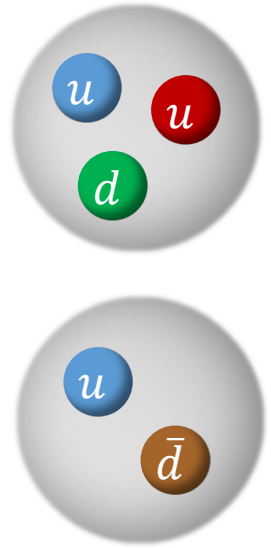
2021年11月15日

Elementary particles in the Standard Model

QUARKS

up $2.3_{-0.5}^{+0.7}$ MeV	charm 1275 ± 25 MeV	top ≈ 173 GeV	gluon 0
down $4.8_{-0.3}^{+0.5}$ MeV	strange 95 ± 5 MeV	bottom 4180 ± 30 MeV	photon 0

Strong interaction:
Quantum Chromodynamics

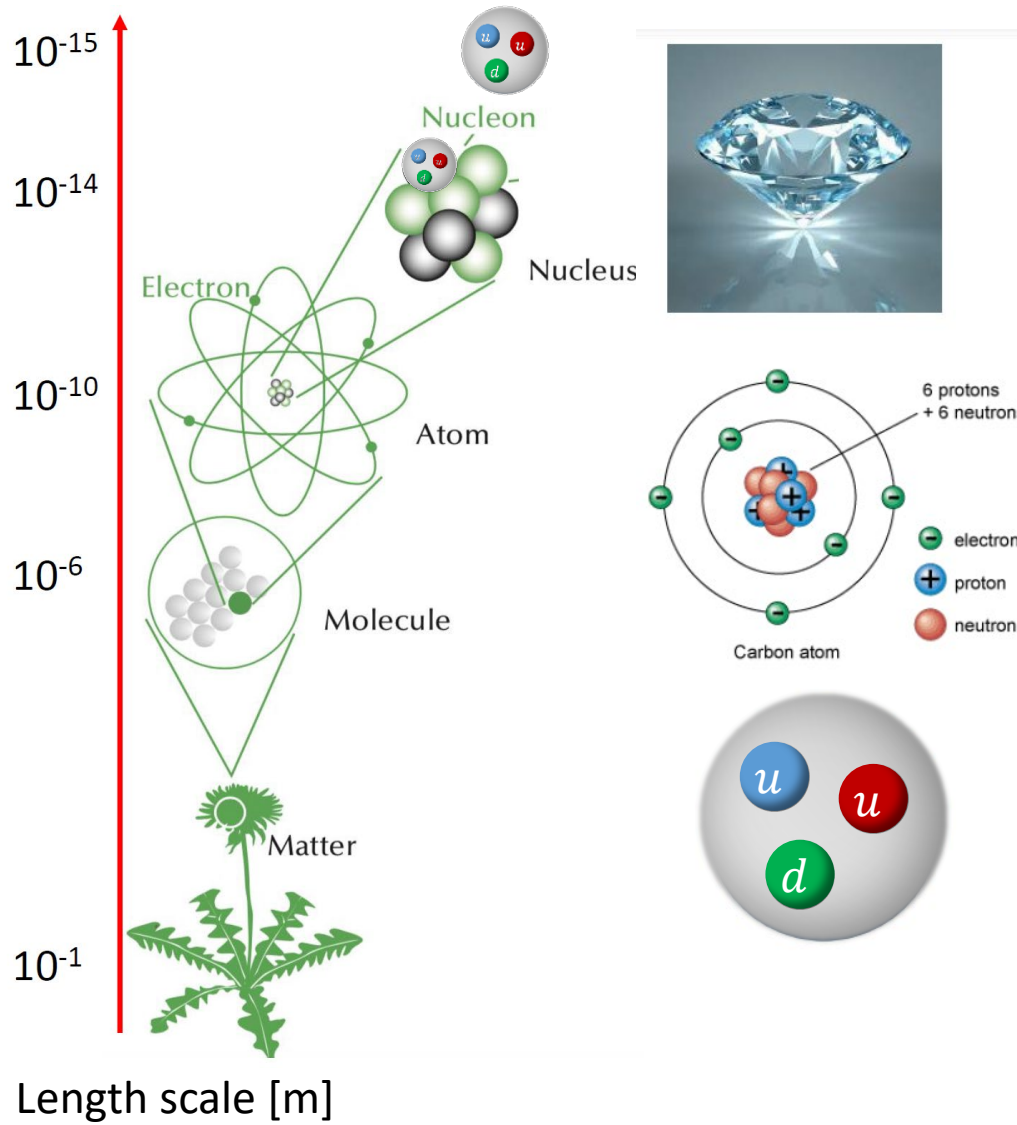


LEPTONS

electron 0.51 MeV	muon 105.7 MeV	tau 1776.8 ± 0.2 MeV	Z boson ≈ 91.2 GeV
electron neutrino < 2.2 MeV	muon neutrino < 0.17 MeV	tau neutrino < 15.5 MeV	W boson ≈ 80.4 GeV
			Higgs boson ≈ 125 GeV

GAUGE BOSONS

Origin of matter mass: Strong interaction



$$M_{\text{diamond}} \simeq \sum M_{C\text{atom}}$$

$$M_{C\text{atom}} \simeq 6(M_{\text{proton}} + M_{\text{neutron}} + M_{\text{electron}})$$

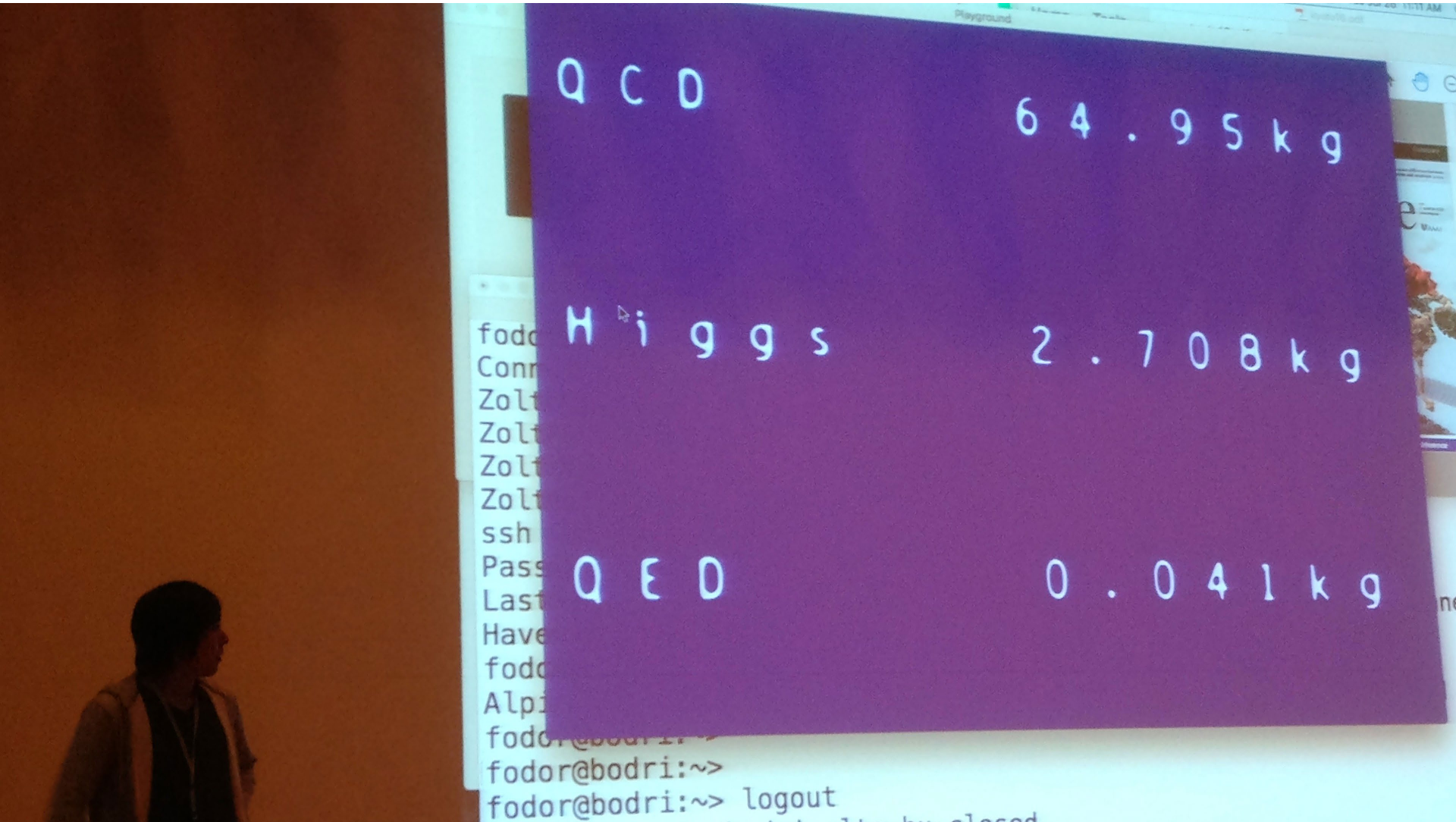
$$\underbrace{M_{\text{proton}}}_{938 \text{ MeV}} \stackrel{?}{=} 2m_u + m_d$$

Decomposition of the proton mass



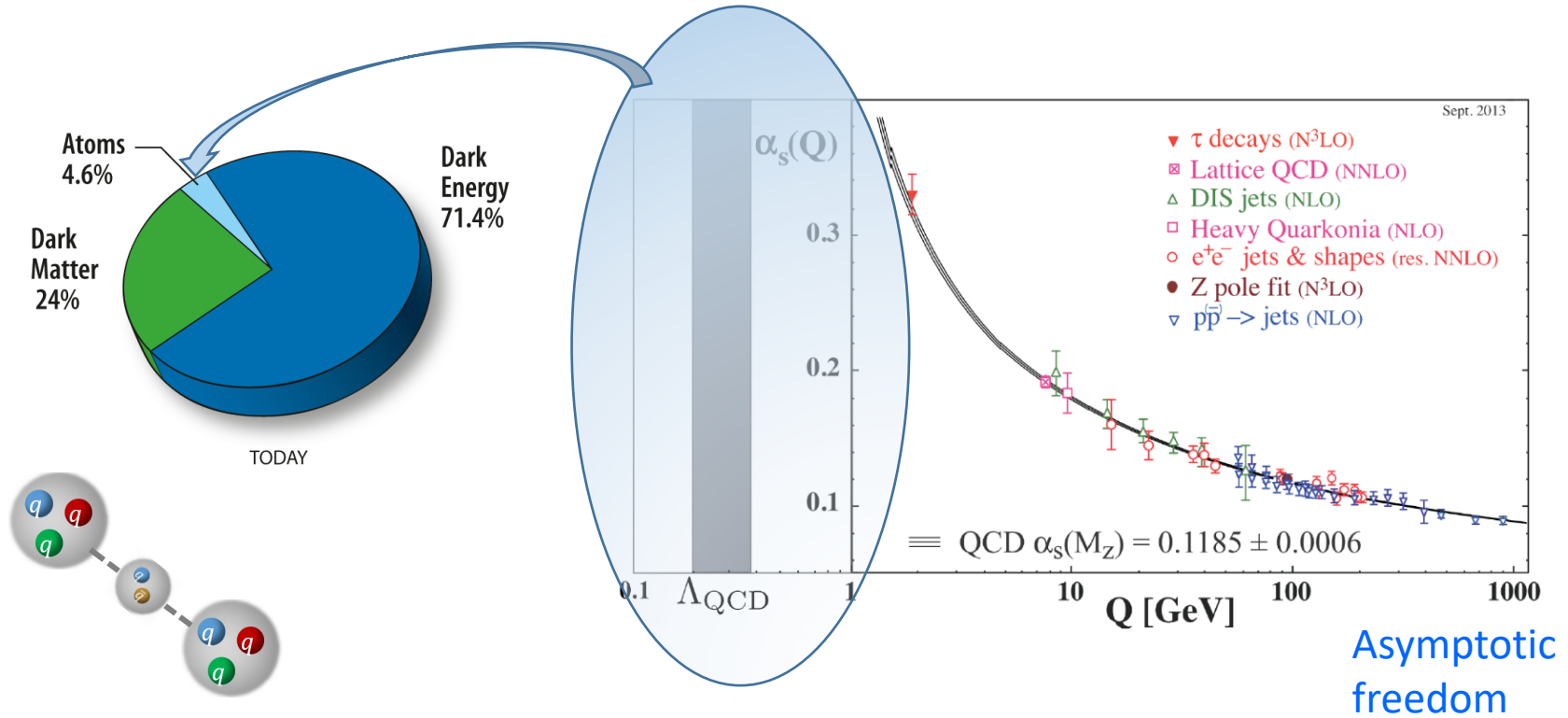
$$\underbrace{M_{\text{proton}}}_{938 \text{ MeV}} \simeq 100(2m_u + m_d) \simeq \sum_q \sigma_q m_q + 856 \text{ MeV}$$

Decomposition of a physicist's weight



Taken at the talk by Fodor at MENU2016

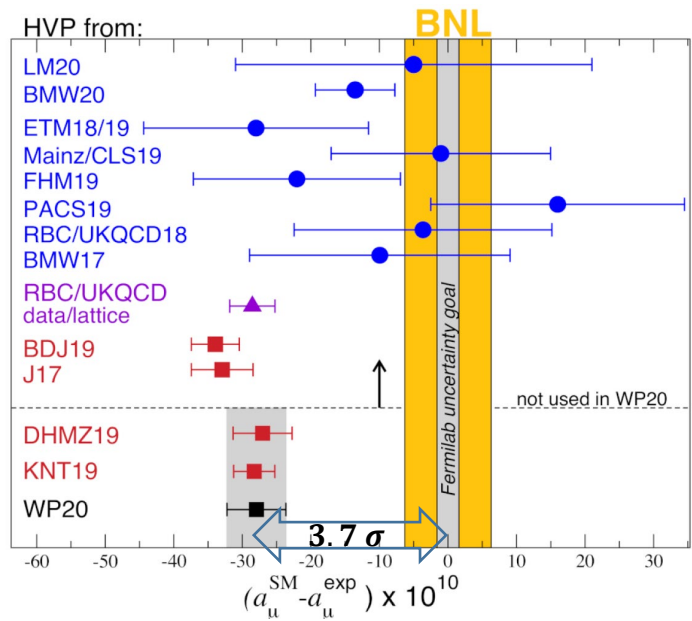
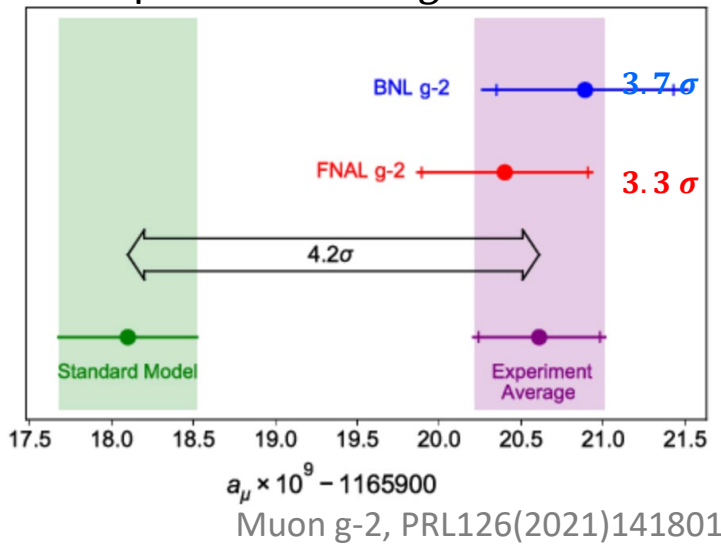
Nonperturbative dynamics



- **Nonperturbative:** extremely challenging!
- **Color confinement:** quarks and gluons are confined in hadrons; **unsolved problem**

Nonperturbative dynamics

Example: the muon $g - 2$



From talk by Luchang Jin

Contributions from known particles: The Standard Model

$$a_{\mu}(\text{SM}) = a_{\mu}(\text{QED}) + a_{\mu}(\text{Weak}) + a_{\mu}(\text{Hadronic})$$

<p>QED</p>	+ ...	116 584 718.9 (1) $\times 10^{-11}$	0.001 ppm
<p>Weak</p>	+ ...	153.6 (1.0) $\times 10^{-11}$	0.01 ppm

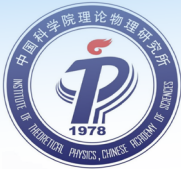
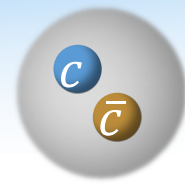
Hadronic...			
<p>...Vacuum Polarization (HVP)</p> <p>α^2</p>	+ ...	6845 (40) $\times 10^{-11}$ [0.6%]	0.37 ppm
<p>...Light-by-Light (HLbL)</p> <p>α^3</p>	+ ...	92 (18) $\times 10^{-11}$ [20%]	0.15 ppm

Numbers from Theory Initiative Whitepaper

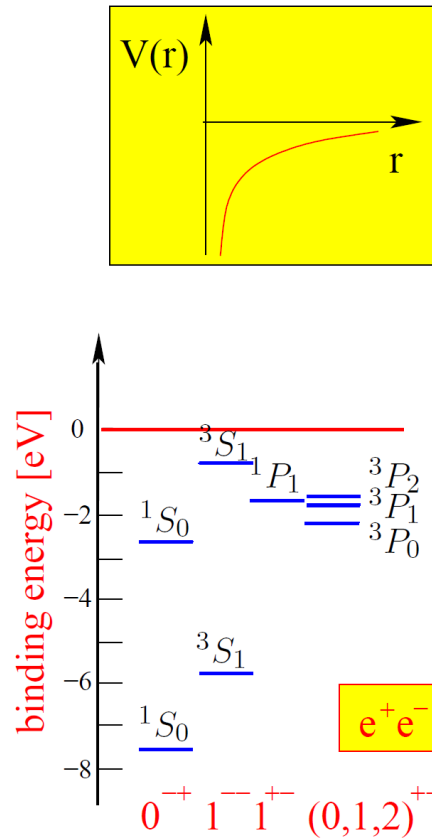
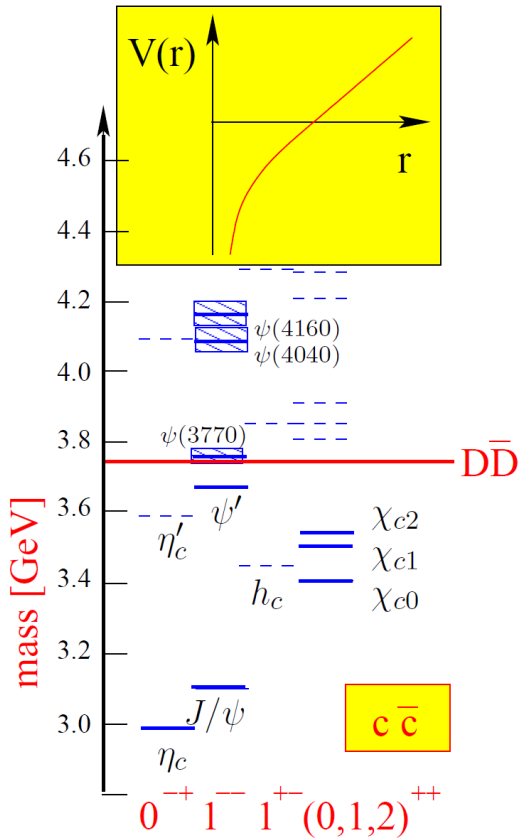
Uncertainty dominated by hadronic contributions

From talk by C. Lehner

Charmonium

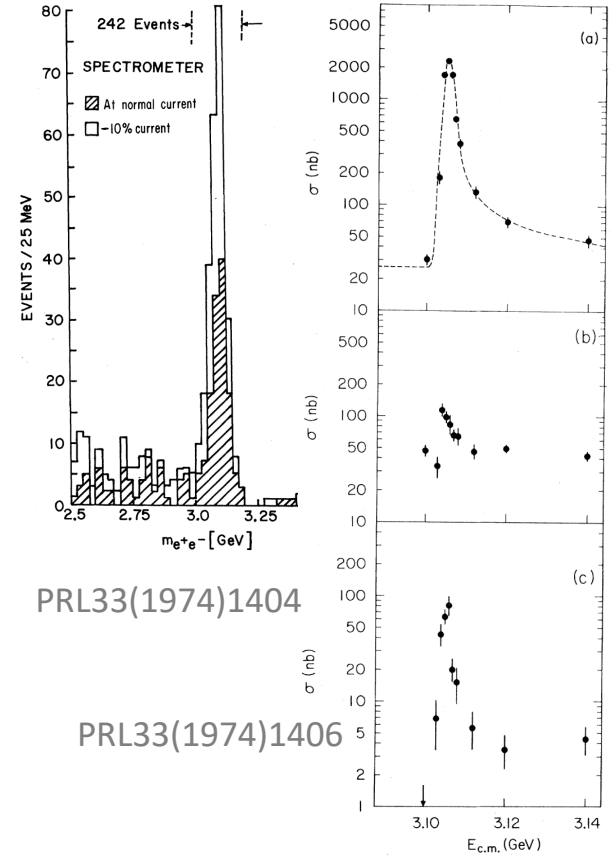


- Meson consisting of a charm quark and an anticharm quark
 - The first charmonium: J/ψ
 - Probing both perturbative and nonperturbative QCD

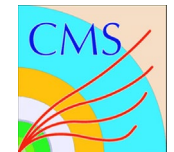
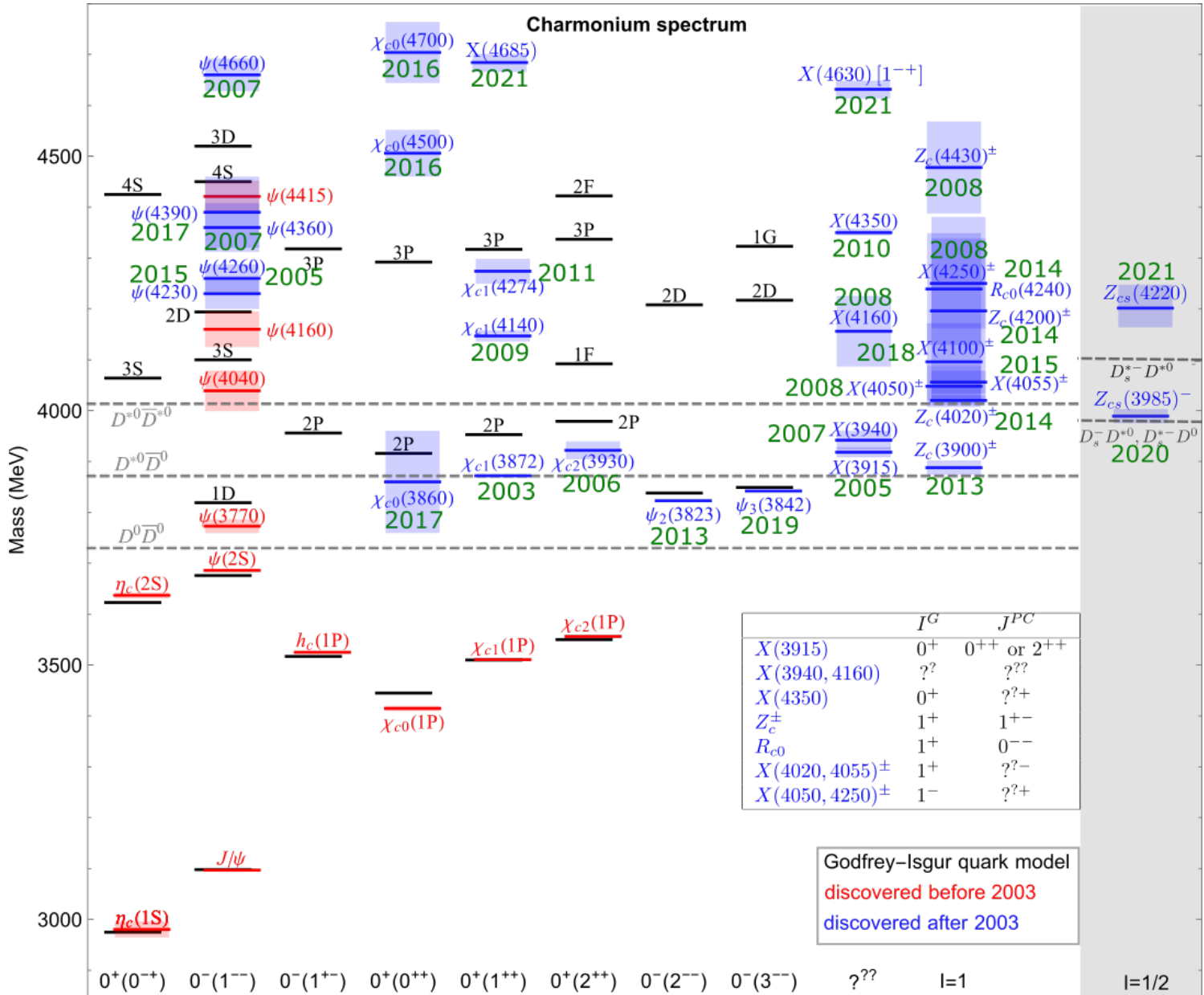


From talk by Hanhart at APS2018

Cornell potential model:
Eichten et al., PRD17(1978)3090



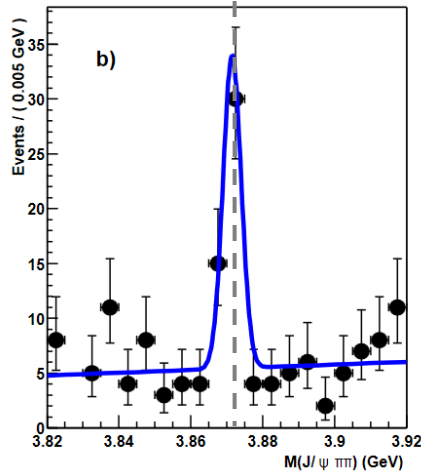
Charmonium(-like) structures: XYZ states



Charmonium-like structures

● $X(3872)$ $D^0\bar{D}^{*0}$ thr.

Belle, PRL91(2003)262001



Observation of a narrow charmonium-like state in exclusive $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$ decays #2

Belle Collaboration • [S.K. Choi](#) (Gyeongsang Natl. U.) et al. (Sep, 2003)

Published in: *Phys.Rev.Lett.* 91 (2003) 262001 • e-Print: [hep-ex/0309032](#) [hep-ex]

[pdf](#) [links](#) [DOI](#) [cite](#)

[↻](#) 2,029 citations

Observation of a Charged Charmoniumlike Structure in $e^+e^- \rightarrow \pi^+\pi^- J/\psi$ at $\sqrt{s} = 4.26$ GeV #1

BESIII Collaboration • M. Ablikim (Beijing, Inst. High Energy Phys.) et al. (Mar 24, 2013)

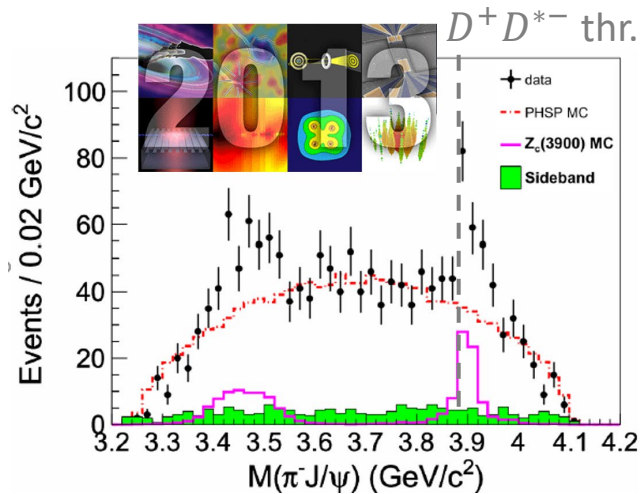
Published in: *Phys.Rev.Lett.* 110 (2013) 252001 • e-Print: [1303.5949](#) [hep-ex]

[pdf](#) [links](#) [DOI](#) [cite](#)

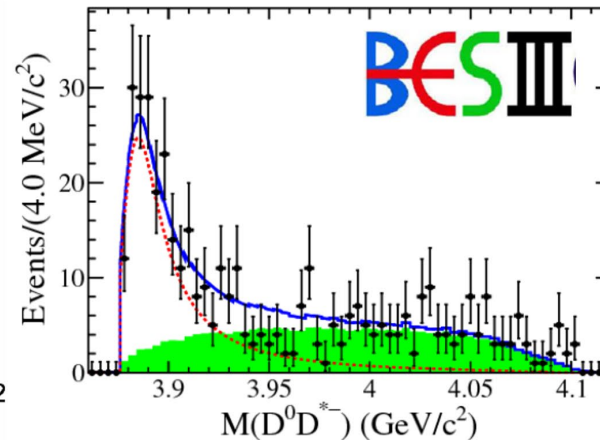
[↻](#) 898 citations

● $Z_c(3900)^\pm$

BESIII, PRL110(2013)252001; Belle, PRL110(2013)252002



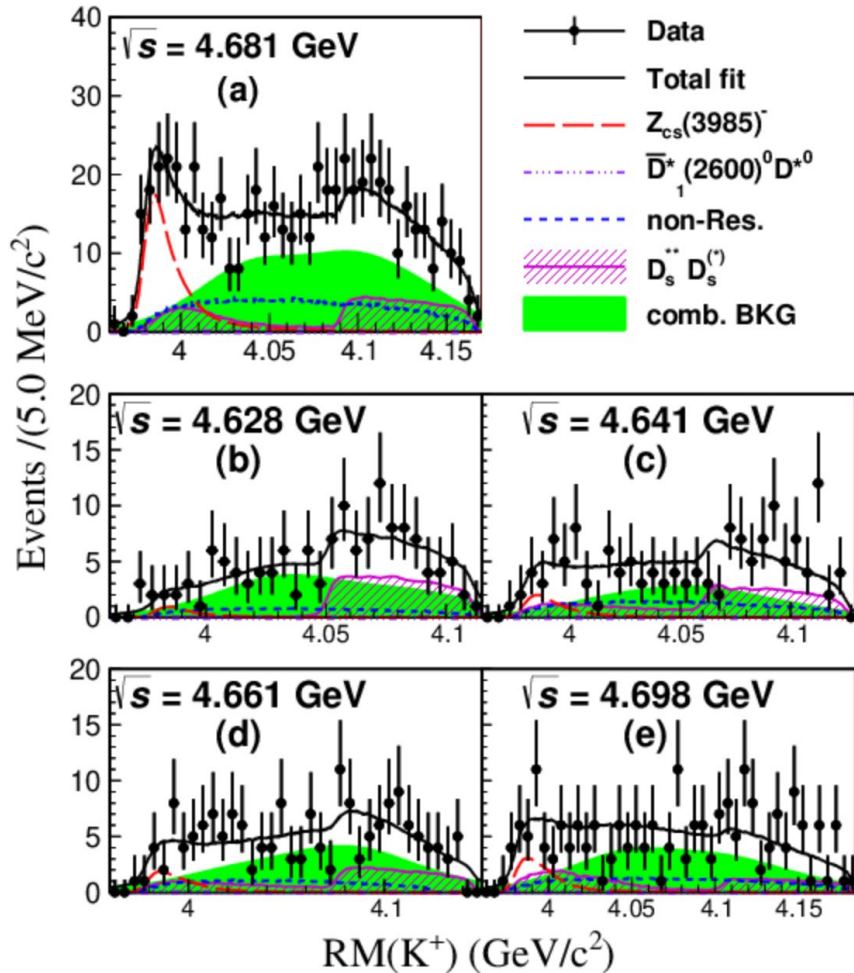
D^+D^{*-} thr.



Charmonium-like structures

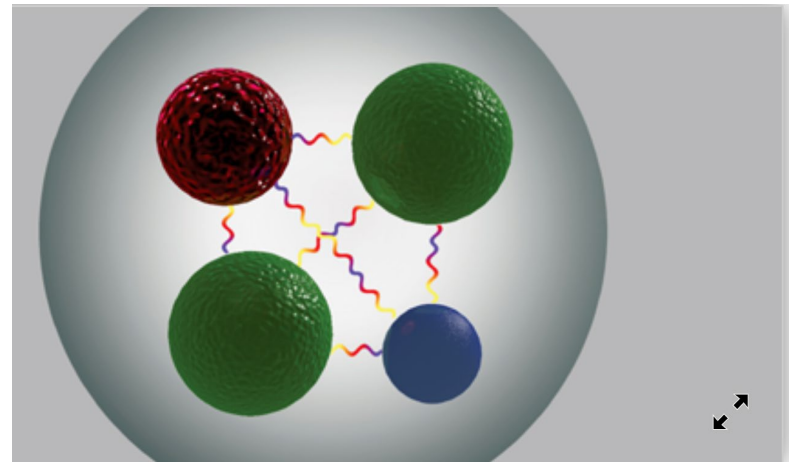
- $Z_{cs}(3985)^-$

BESIII, PRL126(2021)102001



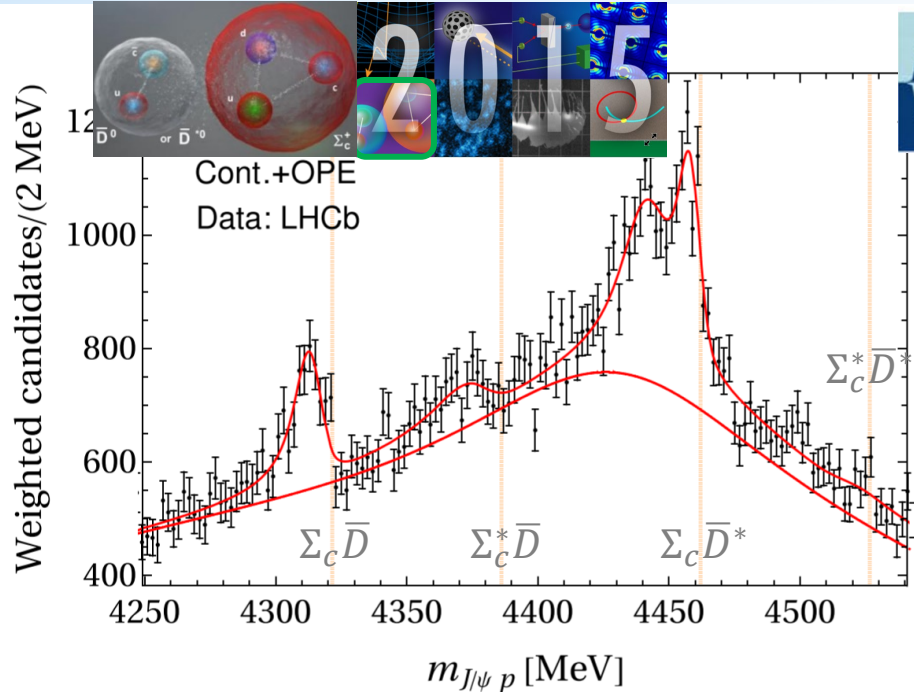
New Tetraquark Spotted in Electron-Positron Collisions

March 11, 2021 • Physics 14, s33

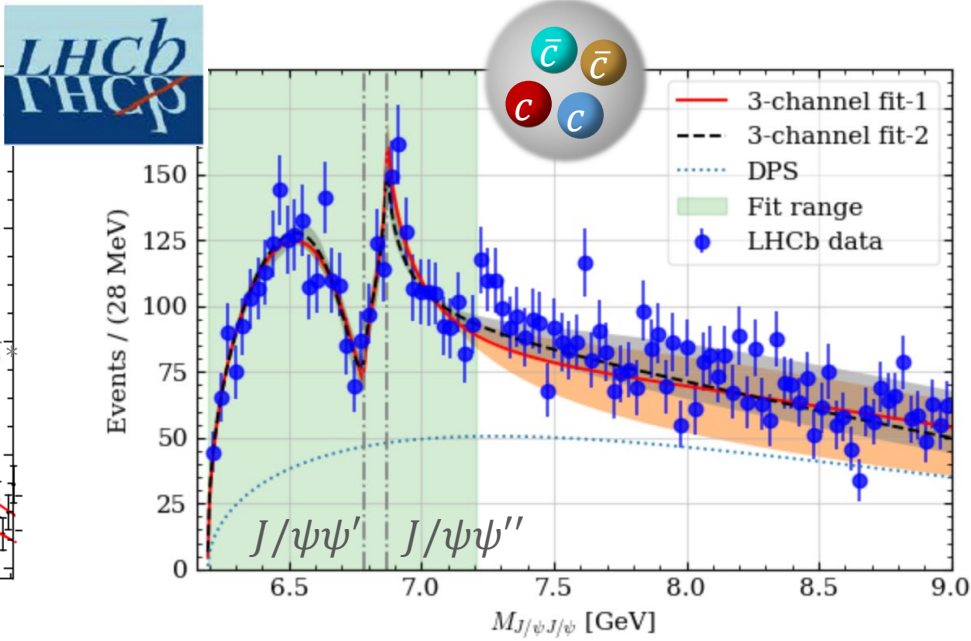


Xiao-Rui Lyu/University of Chinese Academy of Sciences

P_c and double- J/ψ structures



data from LHCb, PRL122 (2019) 222001;
 fit from
 M.-L. Du, V. Baru, FKG et al., PRL124 (2020) 072001



data from LHCb, Sci.Bull.65 (2020) 1983;
 fit from
 X.-K. Dong, V. Baru, FKG et al., PRL126 (2021) 132001

Most new hidden-charm structures are near thresholds of a pair of charm hadrons

Why are there so many (near-)threshold structures in heavy-hadron spectrum?

Is there any rule?

What are XYZ?



Einstein:

If A is success in life, I should say the formula is $A=X+Y+Z$. X is work, Y is play, and Z is keeping your mouth shut.



Some recent reviews

Lots of new hadron structures were found since 2003, a new era:

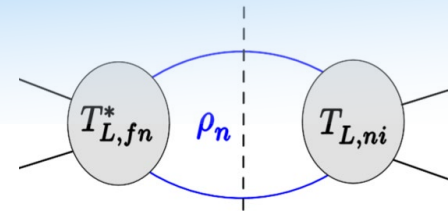
- H.-X. Chen et al., *The hidden-charm pentaquark and tetraquark states*, Phys. Rept. 639 (2016) 1
- R. F. Lebed, R. E. Mitchell, E. Swanson, *Heavy-quark QCD exotica*, Prog. Part. Nucl. Phys. 93 (2017)143
- A. Esposito, A. Pilloni, A. D. Polosa, *Multiquark resonances*, Phys. Rept. 668 (2017) 1.
- FKG, C. Hanhart, U.-G. Meißner, Q. Wang, Q. Zhao, B.-S. Zou, *Hadronic molecules*, Rev. Mod. Phys. 90 (2018) 015004
- S. L. Olsen, T. Skwarnicki, *Nonstandard heavy mesons and baryons: Experimental evidence*, Rev. Mod. Phys. 90 (2018) 015003
- Y.-R. Liu, H.-X. Chen, W. Chen, X. Liu, S.-L. Zhu, *Pentaquark and tetraquark states*, Prog. Part. Nucl. Phys. 107 (2019) 237
- N. Brambilla et al., *The XYZ states: experimental and theoretical status and perspectives*, Phys. Rept. 873 (2020) 154
- FKG, X.-H. Liu, S. Sakai, *Threshold cusps and triangle singularities in hadronic reactions*, Prog. Part. Nucl. Phys. 112 (2020) 103757



Threshold structures

X.-K. Dong, FKG, B.-S. Zou, Phys.Rev.Lett.126 (2021) 152001

(Near-)threshold behavior



- Unitarity: there is always a cusp at an S-wave threshold

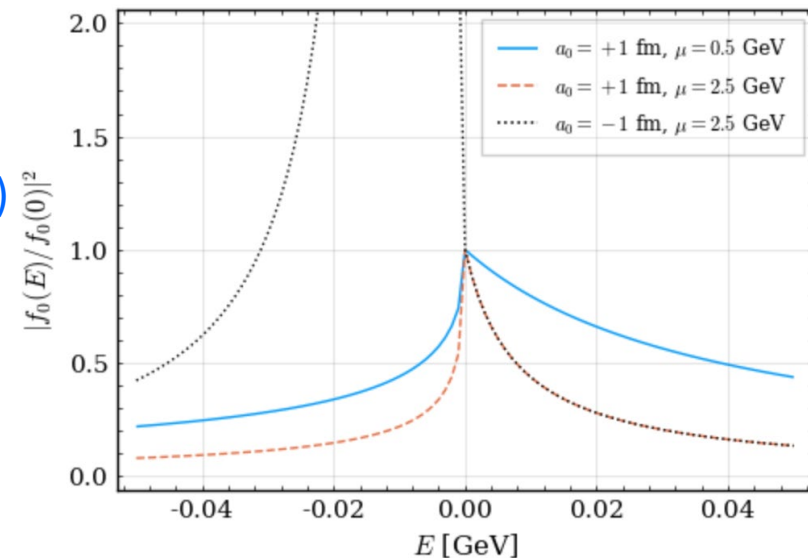
- Consider effective-range expansion: $f_0^{-1}(k) = \frac{1}{a_0} + \frac{1}{2}r_0k^2 - ik + \mathcal{O}\left(\frac{k^4}{\beta^4}\right)$

a_0 : S-wave scattering length; negative for repulsion or attraction w/ a bound state
positive for attraction w/o bound state

Very close to threshold, then scattering length approximation: $f_0^{-1}(E) = \frac{1}{a_0} - i\sqrt{2\mu E}$.

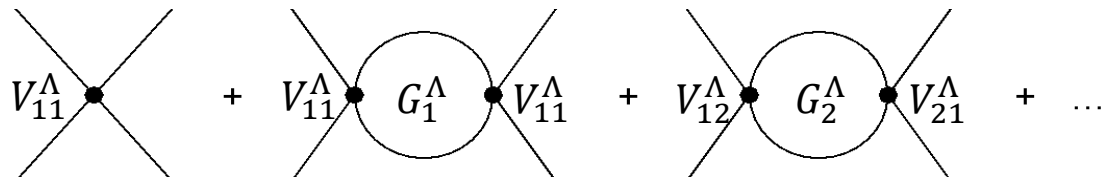
$$|f_0(E)|^2 = \begin{cases} \frac{1}{1/a_0^2 + 2\mu E} & \text{for } E \geq 0 \\ \frac{1}{(1/a_0 + \sqrt{-2\mu E})^2} & \text{for } E < 0 \end{cases}$$

- Cusp at threshold ($E=0$)
- Maximal at threshold for positive a_0 (attraction)
- Half-maximum width: $\frac{2}{\mu a_0^2}$;
virtual state pole at $E_{\text{virtual}} = -1/(2\mu a_0^2)$
- Strong interaction, a_0 becomes negative, pole below threshold, peak below threshold



Coupled channels

- Full threshold structure needs to be measured in a lower channel \Rightarrow coupled channels
- Consider a two-channel system, construct a nonrelativistic effective field theory (NREFT)
 - Energy region around the higher threshold, Σ_2
 - Expansion in powers of $E = \sqrt{s} - \Sigma_2$
 - Momentum in the lower channel can also be expanded



- NREFT at leading order

$$T(E) = 8\pi\Sigma_2 \begin{pmatrix} -\frac{1}{a_{11}} + ik_1 & \frac{1}{a_{12}} \\ \frac{1}{a_{12}} & -\frac{1}{a_{22}} - \frac{1}{\sqrt{-2\mu_2 E - i\epsilon}} \end{pmatrix}^{-1}$$

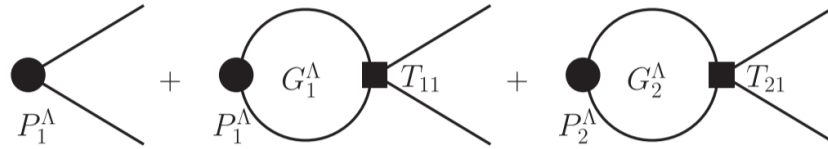
Nonanalyticity only from here

Effective scattering length with open-channel effects becomes complex, $\text{Im} \frac{1}{a_{22,\text{eff}}} \leq 0$

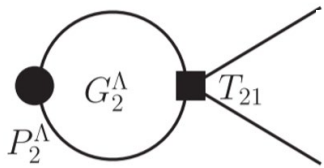
$$T_{22}(E) = -\frac{8\pi}{\Sigma_2} \left[\frac{1}{a_{22,\text{eff}}} - i\sqrt{2\mu_2 E} + \mathcal{O}(E) \right]^{-1}$$

NREFT at LO

- Consider a production process, **must** go through final-state interaction (**unitarity**)



- All nontrivial energy dependence are contained in $T_{11}(E)$ and $T_{21}(E)$
- Case-1: dominated by $T_{21}(E)$,

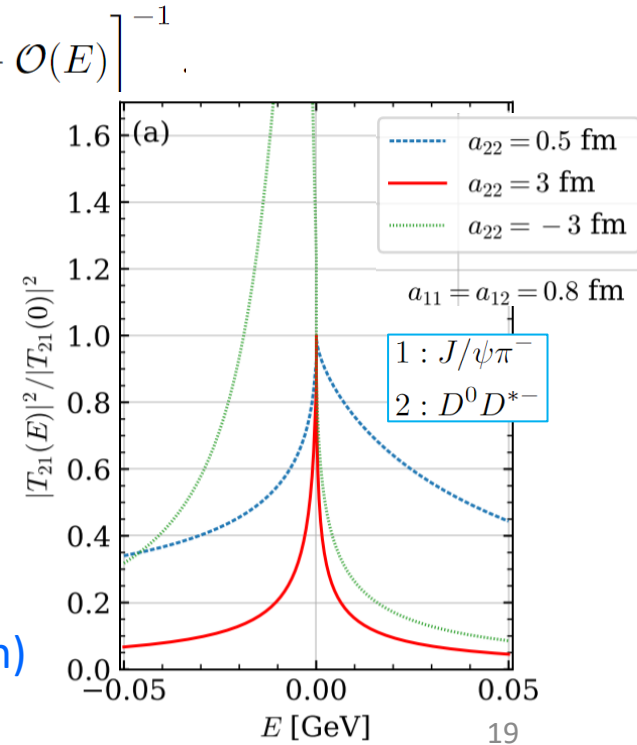


$$T_{21}(E) = \frac{-8\pi\Sigma_2}{a_{12}(1/a_{11} - ik_1)} \left[\frac{1}{a_{22,\text{eff}}} - i\sqrt{2\mu_2 E} + \mathcal{O}(E) \right]^{-1}$$

$$|T_{21}(E)|^2 \propto |T_{22}(E)|^2 \propto$$

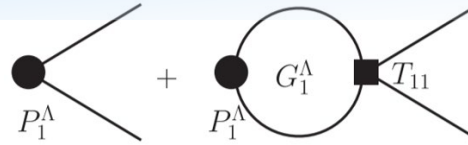
$$\begin{cases} \left[\left(\text{Re} \frac{1}{a_{22,\text{eff}}} \right)^2 + \left(\text{Im} \frac{1}{a_{22,\text{eff}}} - \sqrt{2\mu E} \right)^2 \right]^{-1} & \text{for } E \geq 0 \\ \left[\left(\text{Im} \frac{1}{a_{22,\text{eff}}} \right)^2 + \left(\text{Re} \frac{1}{a_{22,\text{eff}}} + \sqrt{-2\mu E} \right)^2 \right]^{-1} & \text{for } E < 0 \end{cases}$$

- Cusp at threshold ($E=0$)
- Maximal at threshold for **positive $\text{Re}(a_{22,\text{eff}})$ (attraction)**
- Peaking at pole for negative $\text{Re}(a_{22,\text{eff}})$



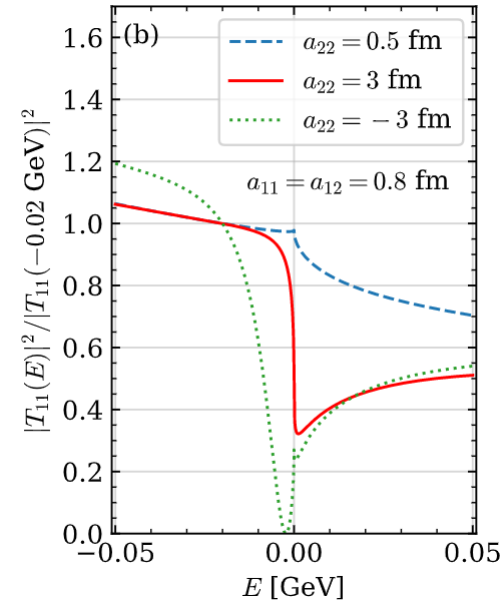
NREFT at LO

- Case-2: dominated by $T_{11}(E)$



$$T_{11}(E) = \frac{-8\pi\Sigma_2 \left(\frac{1}{a_{22}} - i\sqrt{2\mu_2 E} \right)}{\left(\frac{1}{a_{11}} - i k_1 \right) \left[\frac{1}{a_{22,\text{eff}}} - i\sqrt{2\mu_2 E} + \mathcal{O}(E) \right]}$$

- Cusp at threshold ($E=0$)
- One pole and one zero
- For strongly interacting channel-2 (large a_{22}), there must be a dip around threshold
- Abrupt drop if there is a nearby pole



Poles in complex momentum plane:

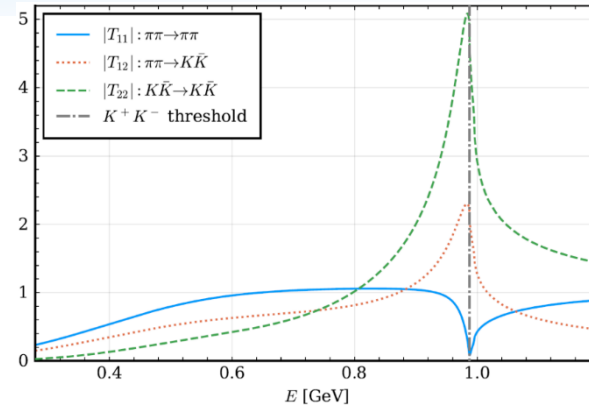
- $(0.37 - i0.08)\text{GeV}$
- $(0.04 - i0.08)\text{GeV}$
- $(-0.09 - i0.08)\text{GeV}$

- More complicated line shape if both channels are important for the production

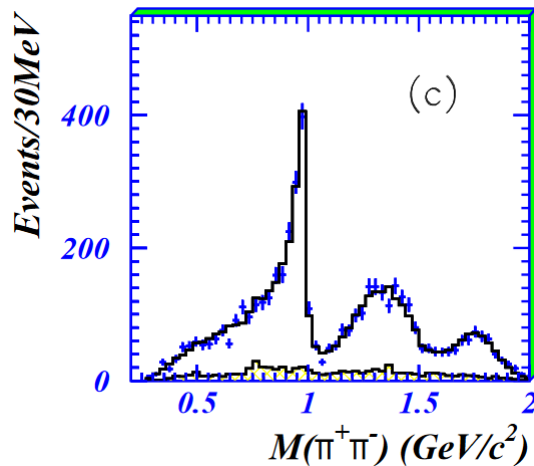
Phenomenology

- T -matrix for $\pi\pi$ and $K\bar{K}$ coupled channels

with the T-matrix from
L.-Y. Dai, M. R. Pennington, PRD90(2014)036004



- $f_0(980)$ in $J/\psi \rightarrow \phi\pi^+\pi^-$ and

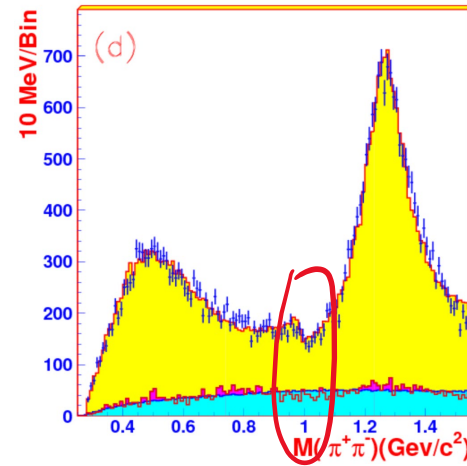


BES,
PLB607(2005)243

Driving channel: $K\bar{K}$

$$J/\psi \rightarrow \phi K\bar{K} \rightarrow \phi\pi^+\pi^-$$

- $J/\psi \rightarrow \omega\pi^+\pi^-$ Channels: $\pi\pi$ and $K\bar{K}$



BES,
PLB598(2004)149

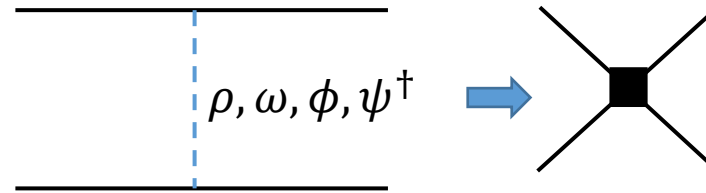
Driving channel: $\pi\pi$

$$J/\psi \rightarrow \omega\pi\pi \rightarrow \omega\pi^+\pi^-$$

Model estimate of near-th. interactions

- Constant contact terms saturated by light-vector-meson exchange, similar to [VMD in the resonance saturation](#) of the low-energy constants in CHPT

Ecker, Gasser, Pich, de Rafael, NPB321(1989)311

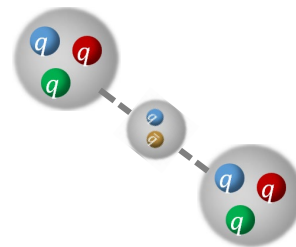


- List of attractive pairs

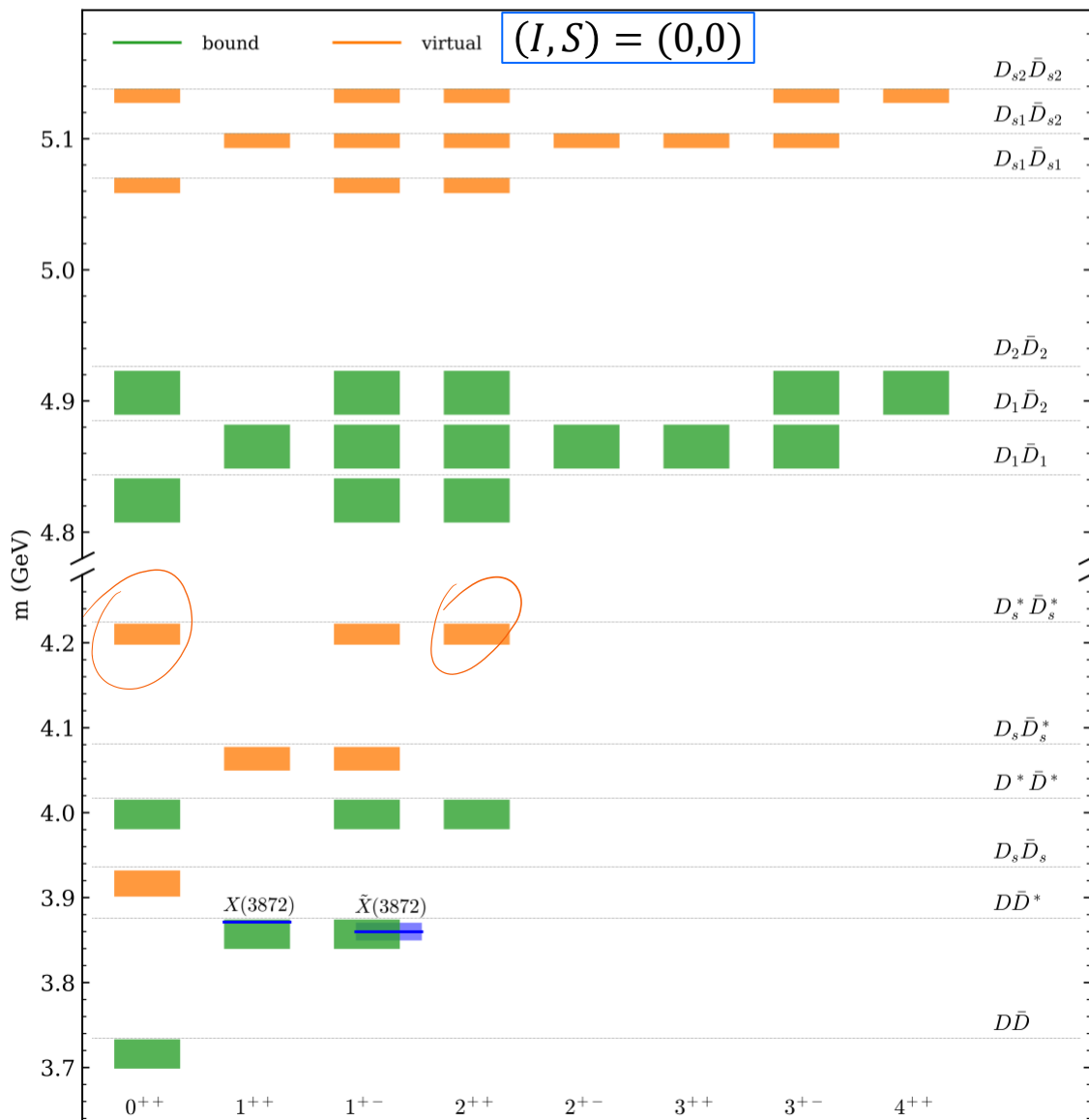
$H\bar{H}$	$D^{(*)}\bar{D}^{(*)}[0, 1^\dagger];$ $X(3872), Z_c(3900, 4020)$ $Z_b(10610, 10650)$	$D_s^{(*)}\bar{D}^{(*)}[\frac{1}{2}^\dagger];$ $Z_{cs}(3985)$	$D_s^{(*)}\bar{D}_s^{(*)}[0]$ $X(4140)$
$\bar{H}T$	$\bar{D}^{(*)}\Xi_c[0];$ $P_{cs}(4459)$	$\bar{D}_s^{(*)}\Lambda_c[0^\dagger]$	
$\bar{H}S$	$\bar{D}^{(*)}\Sigma_c^{(*)}[\frac{1}{2}];$ $P_c(4312, 4440, 4457)$ $\bar{D}^{(*)}\Omega_c^{(*)}[\frac{1}{2}^\dagger]$	$\bar{D}_s^{(*)}\Sigma_c^{(*)}[1^\dagger];$	$\bar{D}^{(*)}\Xi_c^{\prime(*)}[0];$
$T\bar{T}$	$\Lambda_c\bar{\Lambda}_c[0];$	$\Lambda_c\bar{\Xi}_c[\frac{1}{2}];$	$\Xi_c\bar{\Xi}_c[0, 1]$
$T\bar{S}$	$\Lambda_c\bar{\Sigma}_c^{(*)}[1];$ $\Xi_c\bar{\Sigma}_c^{(*)}[\frac{3}{2}^\dagger, \frac{1}{2}];$	$\Lambda_c\bar{\Xi}_c^{\prime(*)}[\frac{1}{2}];$ $\Xi_c\bar{\Xi}_c^{\prime(*)}[1, 0];$	$\Lambda_c\bar{\Omega}_c^{(*)}[0^\dagger];$ $\Xi_c\bar{\Omega}_c^{(*)}[\frac{1}{2}];$
$S\bar{S}$	$\Sigma_c^{(*)}\bar{\Sigma}_c^{(*)}[2^\dagger, 1, 0];$ $\Xi_c^{\prime(*)}\bar{\Xi}_c^{\prime(*)}[1, 0];$	$\Sigma_c^{(*)}\bar{\Xi}_c^{\prime(*)}[\frac{3}{2}^\dagger, \frac{1}{2}];$ $\Xi_c^{\prime(*)}\bar{\Omega}_c^{(*)}[\frac{1}{2}];$	$\Sigma_c^{(*)}\bar{\Omega}_c^{(*)}[0^\dagger];$ $\Omega_c^{(*)}\bar{\Omega}_c^{(*)}[0]$

Hadronic molecules

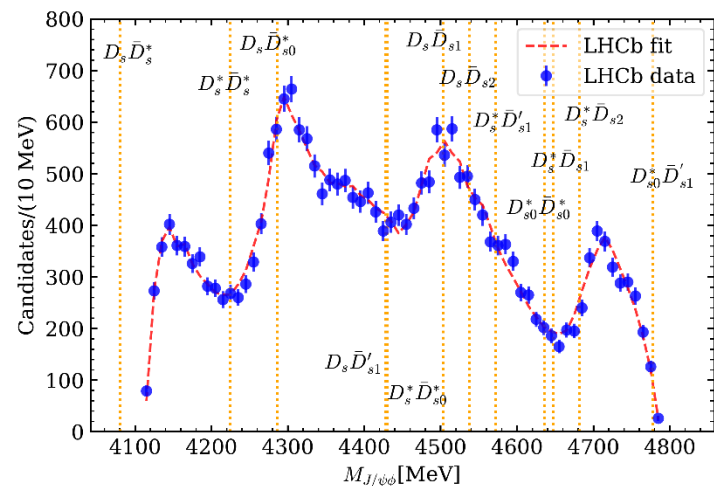
X.-K. Dong, FKG, B.-S. Zou, 《物理学进展》 41 (2021) 65 [arXiv:2101.01021]



X(3872) and related states

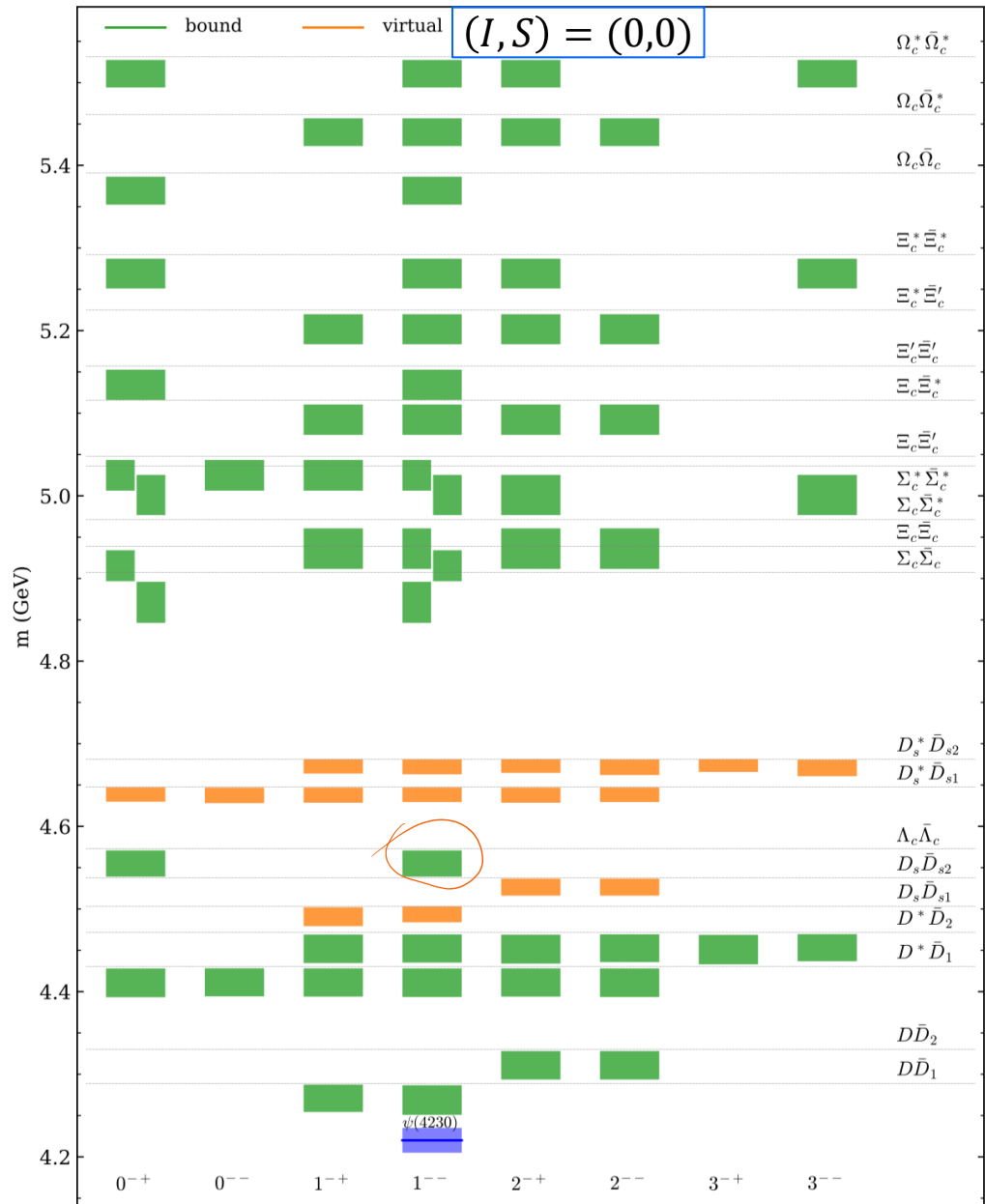


- ✓ $X(3872)$ as a $\bar{D}D^*$ bound state
- ✓ Negative-C parity partner observed by COMPASS PLB783(2018)334
- ✓ $\bar{D}D$ bound state predicted with lattice Prelovsek et al., 2011.02542
- ✓ Evidence for a $D_s^*\bar{D}_s^*$ virtual state in LHCb data?

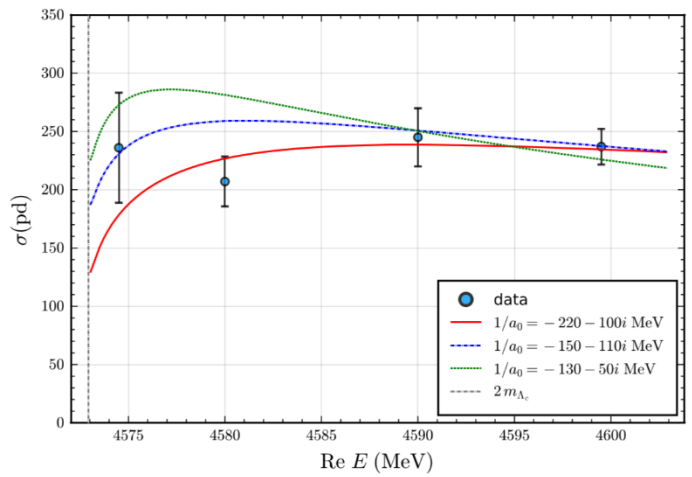


LHCb data, arXiv:2103.01803

Isoscalar vectors and related states



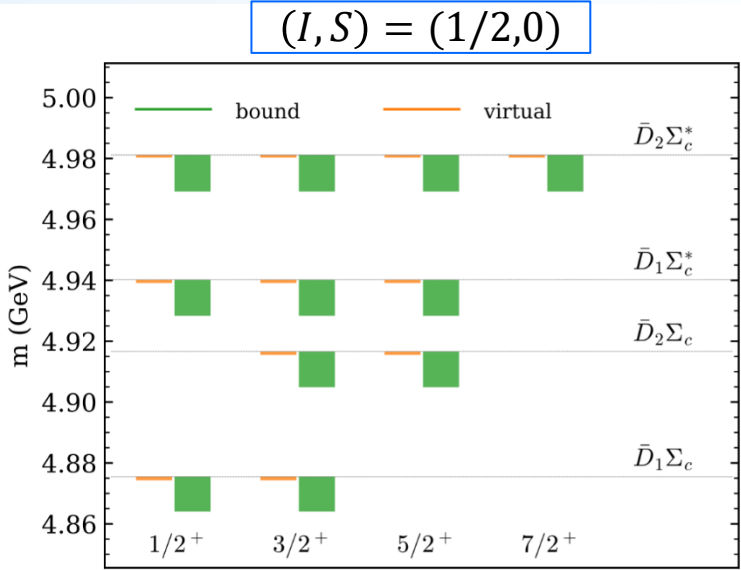
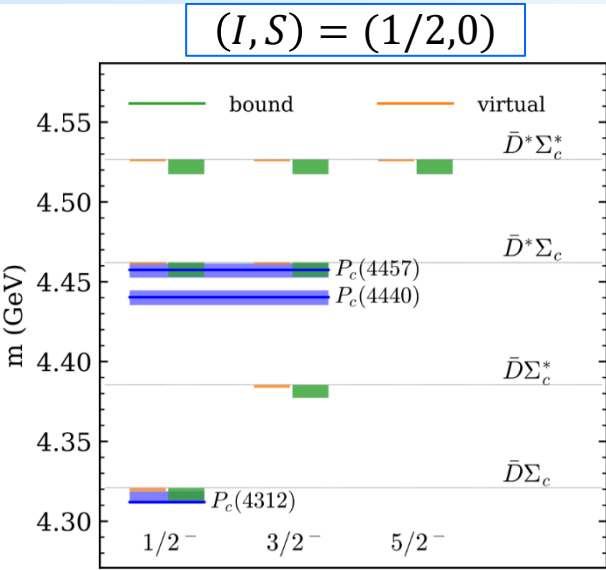
- ✓ Evidence for $1^{--} \Lambda_c \bar{\Lambda}_c$ bound state in BESIII data
 - Sommerfeld factor
 - Near-threshold pole
 - Different from $Y(4630/4660)$



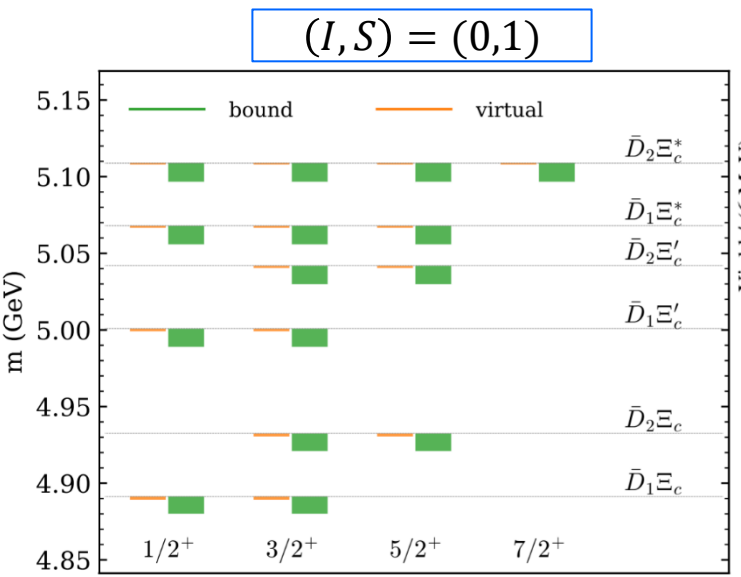
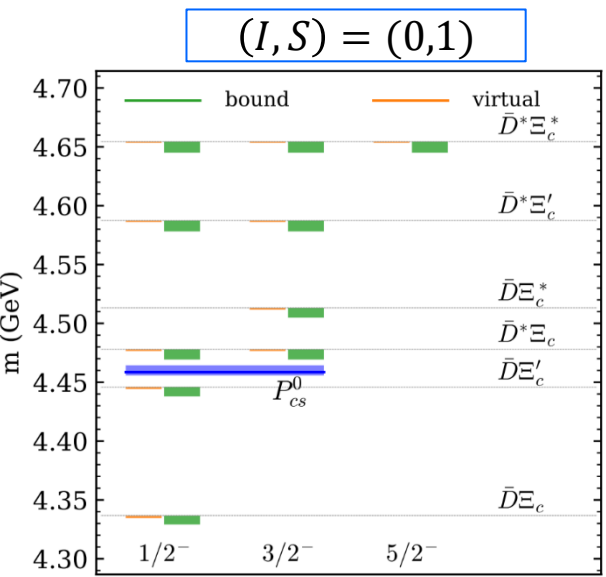
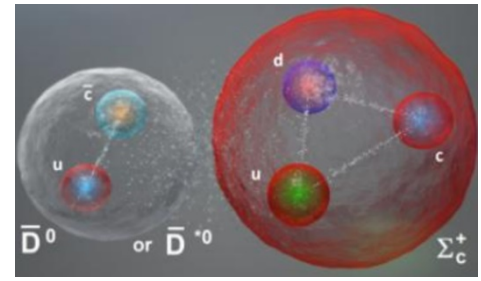
Data taken from BESIII, PRL120(2018)132001

- ✓ Many 1^{--} states in [4.8, 5.6] GeV
- ✓ Opportunities for Super Tau-Charm Factory (STCF)

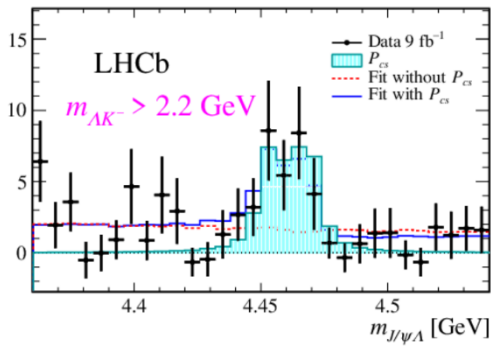
Hidden-charm pentaquarks



✓ The LHCb P_c states as $\bar{D}^{(*)}\Sigma_c$ molecules



✓ The $P_{cs}(4459)$ could be two $\bar{D}^*\Xi_c$ molecules



LHCb, 2012.10380

✓ Many more molecular states above 4.7 GeV, beyond the current exp. reach

Summary

- Threshold structures (threshold cusp or near-threshold peak) are generally expected for a **pair of heavy hadrons with attractive interaction**; strong attraction, then hadronic molecules below threshold, otherwise threshold cusps (poles are virtual states)
- **Threshold structure: general phenomenon beyond hadron physics for any short-range attractive interaction**

Experiments

Lattice

EFT, models

Thank you for your attention!