

Search for 4 top quarks production in final states containing hadronic tau decays

Huiling Hua¹ **Fabio lemmi**¹ Duncan Leggat² Hongbo Liao¹ Hideki Okawa² Yu Zhang²

¹Institute of High Energy Physics (IHEP), Beijing

²Fudan University, Shanghai

November 24, 2021



F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

4 top quarks production



- Process yet to be observed at the LHC
 - ATLAS close to observation: 4.7 σ obs (2.6 exp.)
- BSM contributions could enhance the cross section
- Very rare SM process: $\sigma^{SM}_{t\bar{t}t\bar{t}} \simeq 12 ~{
 m fb}$
- Challenging final states: high jet multiplicity
- τ_h final states firstly explored in this analysis
- Goal: set UL on signal strength, give BSM interpretations using full Run2 data
- Following results based on 2016Legacy data and MC



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Object definitions

ELECTRONS

- $|\eta| <$ 2.5; $p_{\mathrm{T}} >$ 10 GeV
- MVA electron ID developed by SUSY group
 - Tight WP
- Multilsolation with LepAware JEC
 - Tight WP
- 2D IP requirements
 - Tight WP
- 3D IP requirements
 - Tight WP
- Same cuts of 4tops SSDL

Muon M

- Multilsolation with LepAware JEC
 Medium WP
- **2D IP** requirements • Tight WP
- **3D IP** requirements • Tight WP
- Same cuts of 4tops SSDL

MUONS

- $|\eta| < 2.4; \ p_{\mathsf{T}} > 10 \ {
 m GeV}$
- Muon ID developed by MUO POG
 Medium WP
- F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Results



Status report

Object definitions



- $|\eta| <$ 2.4; $p_{\mathrm{T}} >$ 25 GeV
- AK4 jets
- CHS jets
- B tagging through **DeepJet**
 - Medium WP
- Cross-cleaned from lepton collection TOPS
- Identified with resolved HOT
- 1% mistag rate WP

TAUS

- Reconstructed with HPS algorithm
- $|\eta| <$ 2.3; $p_{\mathrm{T}} >$ 20 GeV
- 2D IP requirements
- Identified with DeepTau
 - VVVLoose VsEle WP
 - VLoose VsMu WP
 - Medium VsJet WP
- Cross-cleaned from lepton collection



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Simulated processes

Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Results

• tītī signal

\bullet $t\bar{t}$ associated production

• Splitted in DL, SL and FH samples

• $t\bar{t}+X$ associated production

• $t\bar{t}W$, $t\bar{t}Z$, $t\bar{t}\gamma$, $t\bar{t}H$

QCD

 ${\circ}~$ Splitted in H_{T} slices for $H_{T}>200~GeV$

Single top

- ₀ tW
- ₀ īW

• tZq
$$(\nu\nu)$$

Single Higgs

• $ggH(b\bar{b})$

• $ggH(\gamma\gamma)$

• $ggH(\mu\mu)$

• $ggH(\tau\tau)$

VBF(bb̄)

• VBF(4ℓ)

• VBF($\tau\tau$)

• VBF($\gamma\gamma$)

• VBF($\mu\mu$)

• ggH(WW $\rightarrow \ell \nu qq$)

• ggH(WW $\rightarrow \ell \nu \ell \nu$)

• VBF(WW $\rightarrow \ell \nu \ell \nu$)

Corrections to simulations

- Implemented corrections and scale factors to improve MC description of the data
 - JES and JER
 - MET filters
 - Pileup
 - Prefiring
 - Trigger
 - b tagging (BTagShapeCalibration)
 - Electron SFs (ID, ISO, IP)
 - Muon SFs (ID, ISO, IP)

• To be implemented:

- DeepTau SFs
- Reosolved HOT SFs
- tt+bb corrections





Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

- - F. lemmi (IHEP)

7 / 28

• First, apply loose preselection to retain $t\bar{t}t\bar{t}(\tau_h)$ -like events

- To do so, use somehow looser object definitions than the ones
 - showed previously

Baseline selection

- Three object definitions: **loose**, fakeable and tight objects
- Previous cuts define tight objects
- Analysis baseline selection is:
 - 1 $N_{loose\tau_{k}} > 0$ 2 $N_{iets} \geq 2$ 3 $N_{\text{loose b-jets}} \ge 2$

	Loose	Fakeable	Tight
Electron	$\begin{split} \eta < 2.5; p_T > 10 \mathrm{GeV} \\ \text{Loose MVA ID} \\ \text{Loose ISO (SSDL)} \\ 2D \text{IP cut} \\ \text{ExpMissInnerHits} \leq 1 \end{split}$	$\begin{array}{l} \eta <2.5; \ \mathrm{p_T}>10 \ \mathrm{GeV}\\ \mathrm{Loose} \ \mathrm{MVA} \ \mathrm{ID}\\ \mathrm{Loose} \ \mathrm{ISO} \ (\mathrm{SSDL})\\ \mathrm{2D} \ \mathrm{IP} \ \mathrm{cut}\\ \mathrm{3D} \ \mathrm{IP} \ \mathrm{cut}\\ \mathrm{ExpMissInnerHits}=0 \end{array}$	$\begin{array}{l} \eta <2.5; \ p_T>10 \ GeV \\ Tight MVA ID \\ Tight ISO (SSDL) \\ 2D IP \ cut \\ 3D IP \ cut \\ ExpMissInnerHits = 0 \end{array}$
Muon	$\begin{array}{l} \eta <2.4; \mathbf{p}_T>10~\mathrm{GeV}\\ \text{Loose MUO POG ID}\\ \text{Loose ISO (SSDL)}\\ 2D~\mathrm{IP~cut} \end{array}$	$\begin{array}{l} \eta <2.4; \ \mathbf{p_T}>10 \ \mathrm{GeV}\\ \text{Medium MUO POG ID}\\ \text{Loose ISO (SSDL)}\\ 2D \ \text{IP cut}\\ 3D \ \text{IP cut} \end{array}$	$\begin{array}{l} \eta <2.4; \mathrm{p_T}>10~\mathrm{GeV}\\ \mathrm{Medium}~\mathrm{MUO}~\mathrm{POG}~\mathrm{ID}\\ \mathrm{Tight}~\mathrm{ISO}~(\mathrm{SSDL})\\ \mathrm{2D}~\mathrm{IP}~\mathrm{cut}\\ \mathrm{3D}~\mathrm{IP}~\mathrm{cut} \end{array}$
Tau	$ert \eta ert <$ 2.3; $\mathbf{p_T}$ $>$ 20 GeV 2D IP cut VVLooseVsJet	$\label{eq:phi} \begin{array}{l} \eta < 2.3; \ \mathbf{p_T} > 20 \ \mathrm{GeV} \\ 2D \ \mathrm{IP} \ \mathrm{cut} \\ \mathrm{Exclude} \ \mathrm{DM}{=}5,6 \\ \mathrm{VVLooseVsJet} \\ \mathrm{VLooseVsMu} \\ \mathrm{VVVLooseVsEle} \end{array}$	$\begin{split} \eta &< 2.3; \mathbf{p_T} > 20 \mathrm{GeV} \\ & 2D \mathrm{IP} \mathrm{cut} \\ & \mathrm{Exclude} \mathrm{DM}{=}5,6 \\ & \mathrm{MediumVsJet} \\ & \mathrm{VLooseVsMu} \\ & \mathrm{VVVLooseVsEle} \end{split}$

Status report F lemmi

Objects and

preselection

strategy



Trigger strategy

- Tried different trigger strategies
- **First**: try to inherit trigger setup of $t\bar{t}H$ multilepton (ML) analysis
 - Complicated combination of single-, double-, triple-lepton triggers, lepton+tau triggers, double tau triggers
- **Second**: use a simpler combination of multijet triggers
 - HLT PFHT450 SixJet40 BTagCSV p056

Decided to use the multijet triggers setup

- HLT_PFHT400_SixJet30_DoubleBTagCSV_p056
- Same choice of ttH(bb) analysis
- Tau triggers are found to be inefficient for our signal
- **Multijet triggers** provide **good signal efficiency** (more in backup) •

Objects and

Trigger strategy





Status report

Some remarks about multijet triggers

- $\,$ Well known issue with 2016 data: efficiency in data is lower than in MC by a non-negligible amount at high H_T
- The issue is understood (see, e.g., $t\bar{t}H(b\bar{b})$ AN):

²⁷⁰ Initially a drop in efficiency in data at high HT was observed, which is attributed to the last ²⁷¹ run period of the LHC in 2016 (Run H) which had very high instantaneous luminosity. The ²⁷² L1 HT triggers suffered a problem in which saturated (high p_T) jets were excluded from the ²⁷³ HT calculation [62]. A partial mitigation strategy of including an OR of a single jet trigger ²⁷⁴ HLT_PFJet450_v* has been implemented, which recovers most of the lost efficiency at high ²⁷⁵ HT.

- Include HLT_PFJet450 in the signal triggers
 - Recover some efficiency at high H_T



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

One-dimensional trigger efficiency



- ${\scriptstyle \bullet \,}$ Preselection + 1μ
- Plotted data, MC wrt reference, MC truth
- Also plotted H_T distribution for signal
- A $H_T > 400 \text{ GeV}$ cut saves enough signal and makes trigger efficient



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Two-dimensional trigger efficiency



- nJets vs H_T trigger efficiency
- Left: data/MC efficiency ratio; right: corresponding errors
- Add $H_T > 400 \text{ GeV}$ cut to analysis selection to make trigger efficient
- Use these histograms as trigger efficiency scale factors and uncertainties

Analysis categories

Category	$ au_{ m h}$	ℓ	$\rm N_{jets}$	$\mathrm{N}_{\mathrm{b-jets}}$
1tau0L	1	0	\geq 8	≥ 2
1tau1L	1	1	\geq 6	≥ 2
1tau2L	1	2	\geq 4	≥ 2
1tau3L	1	3	≥ 2	≥ 2
2tau0L	2	0	\geq 6	≥ 2
2tau1L	2	1	\geq 4	≥ 2
2tau2L	2	2	≥ 2	≥ 2

9

Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Results

Phase space splitting based on τ_h,
 ℓ, jets, b-jets multiplicities

- Two hadronic categories + six leptonic categories
- Strategy:
 - For categories with BDT, fit BDT shape (see the following)
 - For remaining categories, fit H_T shape

Multivariate analysis

- Train a **BDT** to better **separate signal from background**
- Use TMVA package
- Sufficient stats for training in
 - ₀ 1tau1L
 - 1tau2L
 - 2tauXL = 2tau1L + 2tau2L
- Input set of variables optimized by correlation-based removal
- **Goal**: achieve optimal performance while keeping the input set small

Internal

node

Leaf

node

Root

node

Leaf

node

Internal

Leaf

node

Internal

node

Leaf

node

Class

Class





Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Correlation-based variable removal

• Correlation-based variable removal:

- Start with set of 50 variables showing best separation power
- Find pair of variables with highest correlation
- **Remove** the one with lower separation power, **retrain**
- Repeat until 1 variable is left in the set
- Plot AUC as a function of number of variables
- Choose smallest number of variables before performance drops





9

Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Correlation-based variable removal (1tau1L)

- AUC shows a plateau above 11 input features
- Knee below 11 input features
- Drop below 5 input features
- We use 11 input features
 - Sum of jets b tag scores
 - 7th jet p_{T}
 - Resolved tops H_T
 - 6th jet *p*[⊤]
 - Invariant mass of b tagged jets
 - Transverse mass of jets
 - 4th non b tagged jet p_T
 - Minimum ΔR between b tagged jets
 - 3rd resolved top p_T
 - Vector sum of resolved top p_T
 - Number of loose leptons





Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Training results (1tau1L)







- Correlation-based removal keeps variables with low-medium correlation
- Results obtained with standard hyperparameters \implies room for improvement after hyperparameter tuning



Validation of input variables (1tau1L)



F. lemmi (IHEP)

QCD estimation in 1tau0L



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

- We have an hadronic category in our analysis, 1tau0L
 - 1 $au_{
 m h}$, no leptons, \geq 8 jets, \geq 2 b jets
- Dominant background in 1tau0L is QCD multijet production
- MC predictions for QCD cannot be safely used
 - Big theoretical uncertainties on cross sections and NLO corrections
 - $\, \circ \,$ Usually very low selection efficiency $\, \Longrightarrow \,$ poor statistics
- Look for a data-driven estimation of the QCD background
- Both yield and shape are estimated from data
 - Yield: from fake rate method
 - Shape: from control region in data

QCD regions

• Three regions are involved in our QCD studies:

- Signal region (SR): where analysis is performed
- Control region (CR): where fake rates and shapes are extracted
- Validation region (VR): where QCD estimation is validated

	$N_{ au_h}$	N_ℓ	N_{jets}	N_{bjets}	tītī	tī	QCD	$t\bar{t}{+}X$
SR	1	0	\geq 8	≥ 2	10	6371	7461	192
VR	1	0	\ge 8	1	1	2321	7792	79
CR	1	0	\geq 8	0	0	294	8979	8

• The large QCD simulated yield that we get in CR comes from fake taus

Status report

• Use fake rate method to estimate this yield from data



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Fake rate method

• Estimate the background completely from data by doing

$$N_{\mathsf{fake}\text{-}\tau} = \sum_{\boldsymbol{p}\mathsf{T},\eta} N_{\mathsf{fake}\text{-}\tau}(\boldsymbol{p}\mathsf{T},\eta) = \sum_{\boldsymbol{p}\mathsf{T},\eta} \left[N_{\mathsf{F},\overline{\mathsf{T}}}(\boldsymbol{p}\mathsf{T},\eta) \times \frac{\mathsf{FR}(\boldsymbol{p}\mathsf{T},\eta)}{1 - \mathsf{FR}(\boldsymbol{p}\mathsf{T},\eta)} \right]$$

- $N_{\text{F},\overline{T}}(p_{\text{T}},\eta)$, number of fakeable-non-tight taus in SR
- $FR(p_T, \eta)$, probability for a fakeable tau to be a tight tau, computed in the CR
- Parametrize as a function of $p_{\rm T}$, η of fakeable tau
- Binning in (p_T, η) : $p_T \in [20, 30, 75, 150, 300, Inf]; \eta \in [0, 1.5, 2.3]$
- Performed several sanity checks before applying FR method, see backup



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation



F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Results

- Compute FR in CR, apply the method using previous formula
- Important: take care of subtracting $t\bar{t}$ and $t\bar{t}+X$ from $N_{F,\overline{T}}(p_T,\eta)$

MC QCD FR method

Yield 7461 ± 1681 7679 ± 273

- The estimated yield from FR method is in agreement with QCD MC predictions
- But it comes with way lower uncertainty (4% vs 23%)

- Take the QCD shape from the CR in data
- Need to extrapolate from shape in CR to shape in different QCD regions
- Correct for kinematic differences between CR and region of interest using the simulation
- $\bullet\,$ Take the ratio of H_T shapes in CR and region of interest, fit it and $get\ a$ transition function
- Apply the transition function to the data distribution in CR to get the final shape

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

- To validate method, compute QCD shape in the VR
- Just compare shapes: normalize areas to 1
- Smoothen the ratio by fitting with a straight line
- This straight transition function is applied to the H_T distribution of data in the CR to obtain the final shape





F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

QCD estimation: validation





- $\, \bullet \,$ Good data/MC closure in VR $\, \Longrightarrow \,$ validates the QCD estimation
- Estimate systematic unc. on yield by the level of disagreement in ratio plot

F. lemmi (IHEP)

Status report

Expected yields



Status report

F. lemmi

Objects and preselection

Trigger strategy

categorization

MVA

Background

Results

	tītī	tī	$t\overline{t}{+}X$	QCD	Single top	Single Higgs
1tau0L	8.79	5389.6	171.0	7679	111.1	-0.29
1tau1L	6.47	1570.4	73.3	2.2	31.7	0.029
1tau2L	1.25	24.5	10.0	0	0.22	0
1tau3L	0.07	0	0.57	0	0	0
2tau0L	0.44	168.2	13.0	1.70	6.3	0.015
2tau1L	0.17	8.6	3.7	0	0.08	0
2tau2L	0.014	0.08	0.20	0	0	0

-

Preliminary results



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Results

- We wrote a first, **stat-only datacard**
- Fit simultaneously shapes in 1tau0L, 1tau1L, 1tau2L, 1tau3L, 2tau0L, 2tauXL
- Get expected upper limit on signal strength: combine -M AsymptoticLimits datacardname.root --run blind
 - Expected upper limit on $\mu_{t\bar{t}t\bar{t}}$ at 95% CL:

 $\mu_{ ext{t\bar{t}t\bar{t}}} < 2.0156$

- Get expected significance of the measurement: combine -M Significance datacardname.root -t -1 --expectSignal=1
 - Expected significance:

1.0389 σ

Summary



Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation

Prospects and publication strategy

- Looking for conveners' advice about long-term strategy
- Concerning a **possible combination**, main point is hadronic tau veto
 - Other channels currently do not apply such a veto
- Checked DeepTau documentation looking for efficiencies and mistag rates
- Found some information in AN Study of the misidentification of jets, electrons and muons as hadronically decaying tau leptons with the DeepTau ID for the full Run II data.
- Document provides mistag rate for VsJet discriminant only
 - Our working point: 70% eff., 0.2% mistag rate (tables 1 and 19)
- Numbers seem encouraging, but further studies should be carried on

Status report

F. lemmi

Introduction

Objects and preselection

Trigger strategy

Event categorization

MVA

Background estimation



F. lemmi

Backup slides

0

- ttWJets_13TeV_madgraphMLM
- ttZJets_13TeV_madgraphMLM-pythia8

• TTTT TuneCP5 PSweights 13TeV-amcatnlo-

pythia8 correctnPartonsInBorn

TTGJets TuneCUETP8M1 13TeV-amcatnloFXFX-madspin-pythia8

TTToSemiLeptonic_TuneCP5_PSweights_13TeV-powheg-pythia8

TTToHadronic TuneCP5 PSweights 13TeV-powheg-pythia8

• ttH 4f ctcvcp TuneCP5 13TeV madgraph pythia8



• tttt

• tt

Status report F. lemmi TTTo2L2Nu TuneCP5 PSweights 13TeV-powheg-pythia8



Samples

Status report

F. lemmi

QCD

QCD_HT200to300_TuneCUETP8M1_13TeV-madgraphMLM-pythia8
QCD_HT300to500_TuneCUETP8M1_13TeV-madgraphMLM-pythia8
QCD_HT500to700_TuneCUETP8M1_13TeV-madgraphMLM-pythia8
QCD_HT700to1000_TuneCUETP8M1_13TeV-madgraphMLM-pythia8
QCD_HT1000to1500_TuneCUETP8M1_13TeV-madgraphMLM-pythia8
QCD_HT1500to2000_TuneCUETP8M1_13TeV-madgraphMLM-pythia8

QCD_HT2000toInf_TuneCUETP8M1_13TeV-madgraphMLM-pythia8

Single top

- ST_tW_top_5f_inclusiveDecays_13TeV-powheg-pythia8_TuneCUETP8M2T4
- ST_tW_antitop_5f_inclusiveDecays_13TeV-powhegpythia8_TuneCUETP8M2T4
- tZq_ll_4f_ckm_NL0_TuneCP5_PSweights_13TeV-amcatnlo-pythia8
- tZq_nunu_4f_13TeV-amcatnlo-pythia8_TuneCUETP8M1

Trigger efficiency for $t\bar{t}t\bar{t}$ signal

$$\varepsilon^{i} = \frac{N_{\text{trig}}^{i}}{N^{i}},$$

 N^i = number of events falling in category *i*; N^i_{trig} = number of events also passing trigger

LtddLL
1.94 2.23

 ${\small { o } }$ With $H_T > 400$ GeV cut:

	1tau0L	1tau1L	1tau2L	1tau3L	2tau0L	2tau1L	2tau2L
N ⁱ trig	484.31 488.43	347.75 352.27	70.43 71.94	3.58 3.62	24.60 25.01	8.58 8.88	1.03 1.03
ε	0.991	0.986	0.979	0.989	0.984	0.966	1



Correlation-based variable removal (1tau2L)

Status report

- AUC shows a plateau above 15 input features
- Drop below 5 input features
- We use 15 input features • to be filled



Training results (1tau2L)



Status report



 Correlation-based removal keeps variables with low-medium correlation



Validation of input variables (1tau2L)





Status report

Correlation-based variable removal (2tauXL)

- AUC shows a plateau above 12 input features
- Drop below 5 input features
- We use 12 input features • to be filled





Status report

Training results (1tau2L)



Status report



 Correlation-based removal keeps variables with low-medium correlation



Status rep

Validation of input variables (2tau1L)



Status report

- Compute FR in CR, apply the method in the same CR
- Compare with number of events in CR you count from MC
- These numbers should close

	Value	Raw entries
Counting	7979 ± 1350	547
Fake rate method	8636 ± 2321	-

- Values are in agreement within the uncertainties, closure is not perfect (8% discrepancy)
 - **Due to approximations** in weighting and summing TEfficiency objects
 - See my discussion with ROOT developer Lorenzo Moneta here



- F. lemmi
- Compute FR in CR, **apply the method in** the **application region** (same as signal region, but use fakeable-not-tight taus)
- Compare with number of events in SR you count from MC

	Value	Raw entries
Counting	7461 ± 1681	315
Fake rate method	5887 ± 1782	_

- Values are in agreement within the uncertainties
- Uncertainties are big due to poor statistics in MC samples

- Compute FR in CR, apply the method in the same CR
- Compare with number of events in CR you count from data
- This should close (at least approximately)

	Value	Raw entries
Counting	11561 ± 108	11561
Fake rate method	11561 ± 384	_

• Values are in agreement within the uncertainties, perfect closure

No weighting of any kind of objects is needed for data



Status report

Uncertainties on the QCD shape

- QCD H_T shapes are taken from the CR in data and translated to VR or SR using the corresponding transition functions (TFs)
- TFs are the result of a fit: ROOT gives you the fitted parameters and the correlation matrix ${\cal V}$ of the fit
- In our case, we fitted with straight lines of the form

$$y = mx + q$$
,

so the correlation matrix will look like

$$\mathcal{V} = \begin{bmatrix} \sigma_q^2 & \rho_{qm} \\ \rho_{mq} & \sigma_m^2 \end{bmatrix},$$

where $\sigma_{q/m}^2$ are the variances of the parameters and $\rho_{qm} = \rho_{mq}$ are the correlation coefficients between m and q

F. lemmi (IHEP)



Status report

Uncertainties on the QCD shape

• In general, $\rho_{qm} = \rho_{mq} \neq 0$, i.e., some degree of correlation exists between the two parameters

- This means one cannot shift *m* and *q* up and down independently
- ${\cal V}$ is a real, symmetric matrix \implies it can always been diagonalized by means of an orthogonal transformation
- This means it exists some auxiliary parameter space in which *m* and *q* are fully decorrelated
 - One can shift them up/down independently in this space
- \bullet Linear algebra theorem: the orthogonal diagonalizing matrix ${\cal O}$ has the eigenvectors of ${\cal V}$ as columns

$$\mathcal{D} = \mathcal{O}^{-1} \mathcal{V} \mathcal{O} = \mathcal{O}^{\mathsf{T}} \mathcal{V} \mathcal{O}$$





Status report

Uncertainties on the QCD shape

• Idea: Starting from the "real" parameters, described by the vector $\mathbf{p}^T = (q, m)$, we first transform them to some auxiliary parameters $\tilde{\mathbf{p}}^T = (\tilde{q}, \tilde{m})$:

$$\tilde{\mathbf{p}} = \mathcal{O}\mathbf{p}$$

• In the auxiliary space, the correlation matrix is diagonal and its non-zero elements are the variances of \tilde{m}, \tilde{q}

$$\mathcal{D} = egin{bmatrix} ilde{\sigma}_{ ilde{m{q}}}^2 & 0 \ 0 & ilde{\sigma}_{ ilde{m{m}}}^2 \end{bmatrix}.$$

 Now the parameters can be shifted independently, so we define the shifted TFs in the auxiliary space to be described by

$$\begin{split} \tilde{\mathbf{p}}_{up}^{T} &= (\tilde{q} + \tilde{\sigma}_{\tilde{q}}, \tilde{m} + \tilde{\sigma}_{\tilde{m}}) \\ \tilde{\mathbf{p}}_{down}^{T} &= (\tilde{q} - \tilde{\sigma}_{\tilde{q}}, \tilde{m} - \tilde{\sigma}_{\tilde{m}}) \end{split}$$



Status report

• Finally, we perform the **inverse transformation** to go back and get the parameters describing the **TFs in the original space**

$$egin{aligned} \mathbf{p}_{up} &= \mathcal{O}^{-1} \widetilde{\mathbf{p}}_{up} \ \mathbf{p}_{down} &= \mathcal{O}^{-1} \widetilde{\mathbf{p}}_{down} \end{aligned}$$

- ${\scriptstyle \bullet }$ Now compare nominal shapes with the upwards/downwards shifted shapes
- Scale all areas to one: we are interested in the shape differences
 - The yield will be coming from FR for all of them



Status report

QCD shape uncertainty: VR



	q	т
Nominal	0.95	-0.00024
Up	1.31	-0.00064
Down	0.59	0.00016

9

Status report