

# Dark magnetic dipole property in fermionic absorption

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Based on JHEP05(2022)071

arXiv: 2201.11905


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[中国物理学会高能物理分会第十一届全国会员代表大会暨学术年会](#)  
2022年8月8日至11日

# Outline

- Motivation
- The dark photon model with magnetic dipole moment
- DM absorption by nuclear targets
- DM absorption by electron targets
- Summary

# Motivation

- Existence evidences of DM: 
  - Rotation curve of spiral galaxies
  - Gravitational lensing
  - Larger and cosmological scales
  - CMB anisotropies
  - etc.

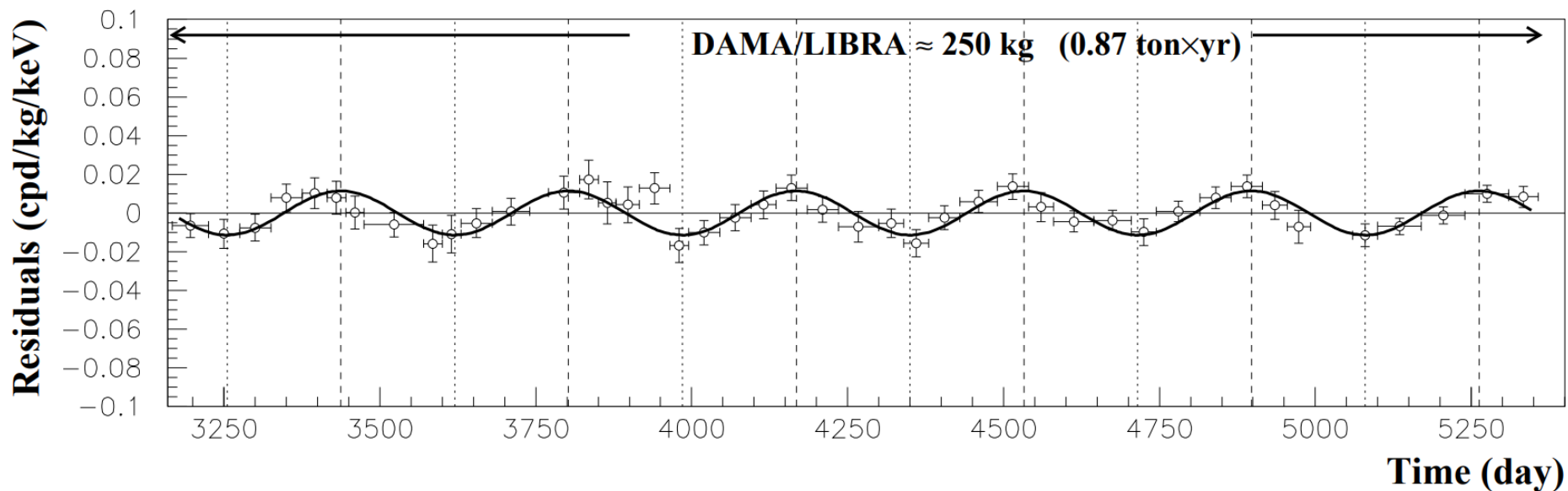
⚠ Terrestrial experiments give null results!

- **DAMA** collaboration, R. Bernabei et al. [Phys. Lett. B 480 \(2000\) 23–31](#).

**8.9**  $\sigma$  C.L. for DM annual modulation  
signature in the galactic halo [[1002.1028](#)]

# Motivation

Rotation curve of spiral galaxies  
Gravitational lensing  
2-6 keV



**8.9  $\sigma$  C.L.** for DM annual modulation  
signature in the galactic halo [[1002.1028](#)]

# Motivation

could have off-diagonal magnetic dipole [hep-ph/0003010]



- To explain the DAMA signal, the inelastic DM transition which induced by **dark magnetic dipole** is a good idea.

(dipole-charge)

[1007.4200] & [1007.4345] -- dipole-dipole NaI → Xe, Ar, W...

$\chi + N(e) \rightarrow \nu + N(e)$  A typical scattering of fermionic absorption

[1905.12635], [1908.10861]  
[2011.01940]. J. A. Dror et al.

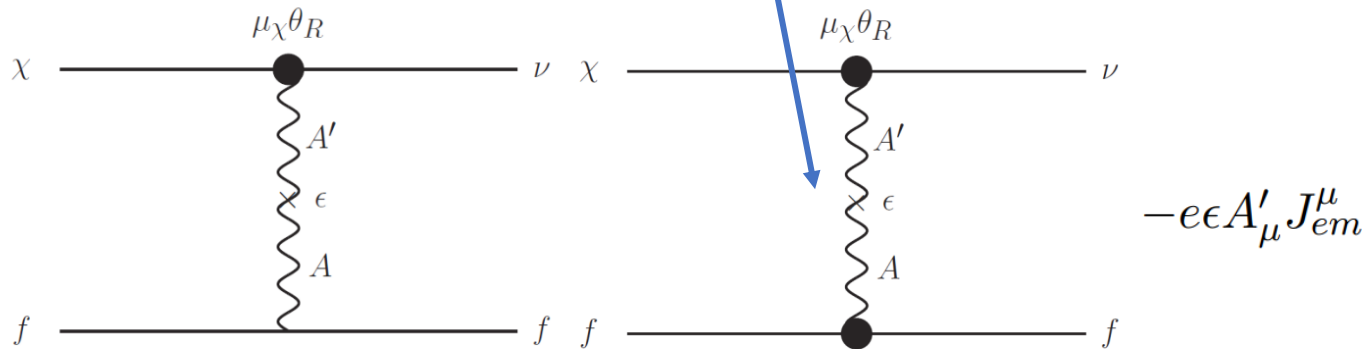
$$E_R = m_\chi^2 / 2m_{N,e}$$

The localized recoil energy of nucleus or electron which gives a peak-like signature in scattering rate.

# The dark photon model with magnetic dipole moment

- We consider a Dirac fermion DM charged under a dark gauge group  $U(1)'$  and the magnetic dipole operator.

$$\mathcal{L} \supset \frac{\mu_\chi}{2} \bar{\chi} \sigma^{\mu\nu} \chi F'_{\mu\nu} + \frac{1}{4} F'^{\mu\nu} F'_{\mu\nu} + \frac{\epsilon}{2} F^{\mu\nu} F'_{\mu\nu} + \frac{1}{2} m_{A'}^2 A'^\mu A'_\mu,$$

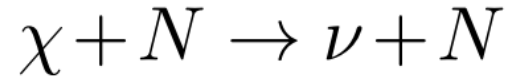


$$\mathcal{L}_{eff} \supset \frac{\epsilon e Q_f \mu_\chi \theta_R}{q^2 - m_{A'}^2} q^\mu \bar{\chi}_L \sigma_{\mu\nu} \nu_R \bar{f} \gamma^\nu f + h.c.,$$

dipole-charge

$$\frac{\epsilon \mu_\chi \mu_N \theta_R}{q^2 - m_{A'}^2} q^\mu q^\alpha g^{\nu\beta} \bar{\chi}_L \sigma_{\mu\nu} \nu_R \bar{N} \sigma_{\alpha\beta} N + h.c.$$

dipole-dipole



# DM absorption by nuclear targets

- The differential scattering cross section induced by neutral current (NC)

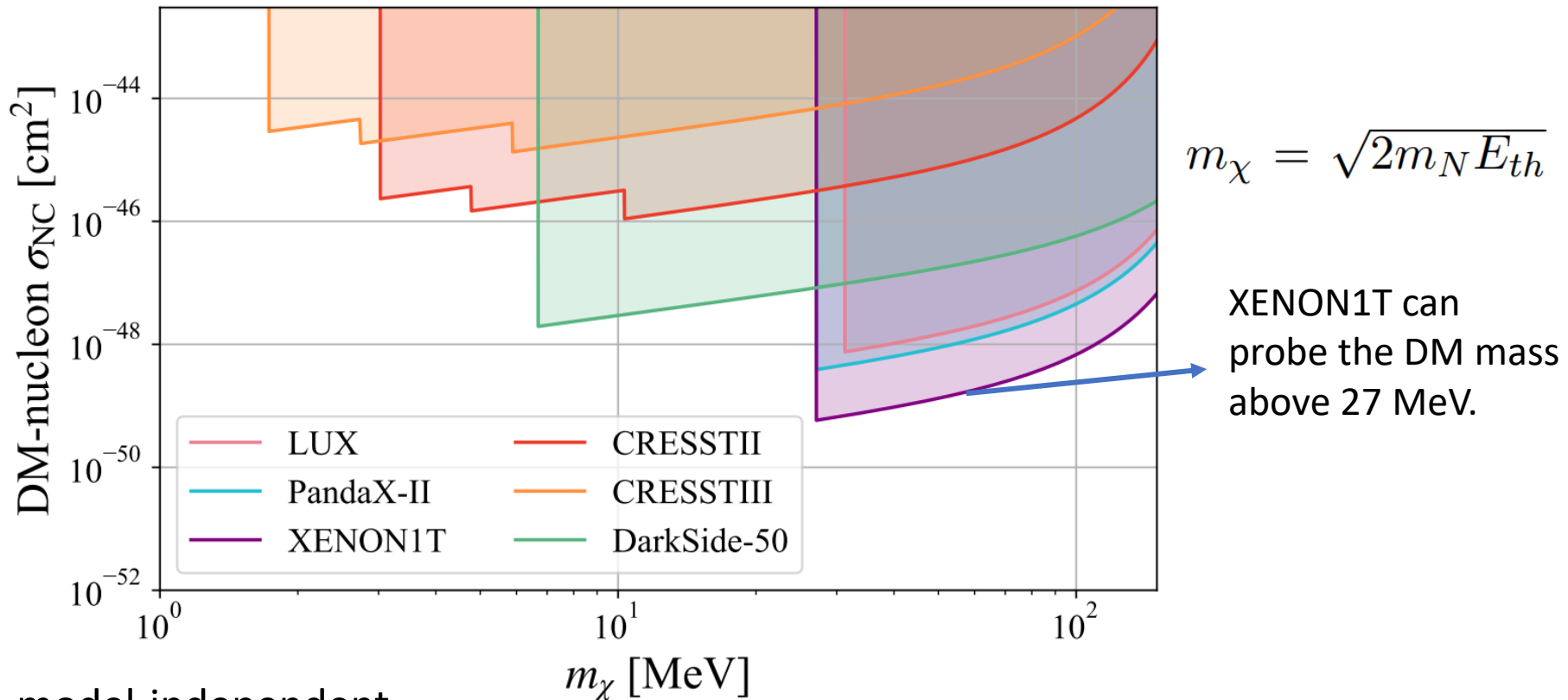
$$\begin{aligned} \frac{d\sigma_{NC}}{dE_R} &= \frac{d\sigma_{DC}}{dE_R} + \frac{d\sigma_{DD}}{dE_R} \\ &= \frac{\alpha\mu_\chi^2\theta_R^2\epsilon^2m_\chi}{vm_N(m_{A'}^2 + 2m_NE_R)^2} Z^2 F_Z^2(E_R)\delta(E_R - E_R^0) && \text{dipole-charge} \\ &\quad \left(6m_N^2m_\chi E_R - 8m_N^2E_R^2 - m_Nm_\chi^3 + 4m_Nm_\chi^2E_R - 2m_Nm_\chi E_R^2 + m_\chi^3E_R\right) \\ &+ \frac{\mu_\chi^2\mu_N^2\theta_R^2\epsilon^2m_\chi E_R}{2\pi v(m_{A'}^2 + 2m_NE_R)^2} \frac{I+1}{3I} F_D^2(E_R)\delta(E_R - E_R^0) && \text{dipole-dipole} \\ &\quad \left(-4m_N^2E_R^2 + 8m_Nm_\chi^2E_R - 8m_Nm_\chi E_R^2 + 2m_NE_R^3 + m_\chi^4 + 4m_\chi^3E_R - 3m_\chi^2E_R^2\right), \end{aligned}$$

$$R = \frac{\rho_\chi}{m_\chi} \sigma_{NC} Z^2 \sum_j N_{T,j} F_j(q)^2 \Theta(E_{R,j}^0 - E_{th}),$$

[\[1908.10861\]](#).

$$\chi + N \rightarrow \nu + N$$

# DM absorption by nuclear targets

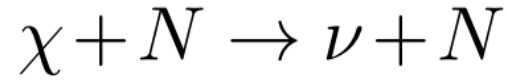


- model-independent

$$R = \frac{\rho_\chi}{m_\chi} \sigma_{NC} Z^2 \sum_j N_{T,j} F_j(q)^2 \Theta(E_{R,j}^0 - E_{th}) ,$$

[1908.10861].





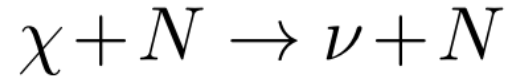
# DM absorption by nuclear targets

define  $U = \mu_\chi \epsilon \theta_R$

$$\begin{aligned} \frac{d\sigma_{NC}}{dE_R} &= \frac{d\sigma_{DC}}{dE_R} + \frac{d\sigma_{DD}}{dE_R} \longrightarrow \text{truncated Maxwell distribution } f(\mathbf{v}) \\ &= \frac{\alpha \mu_\chi^2 \theta_R^2 \epsilon^2 m_\chi}{v m_N (m_{A'}^2 + 2m_N E_R)^2} Z^2 F_Z^2(E_R) \delta(E_R - E_R^0) \\ &\quad \left( 6m_N^2 m_\chi E_R - 8m_N^2 E_R^2 - m_N m_\chi^3 + 4m_N m_\chi^2 E_R - 2m_N m_\chi E_R^2 + m_\chi^3 E_R \right) \\ &+ \frac{\mu_\chi^2 \mu_N^2 \theta_R^2 \epsilon^2 m_\chi E_R}{2\pi v (m_{A'}^2 + 2m_N E_R)^2} \frac{I+1}{3I} F_D^2(E_R) \delta(E_R - E_R^0) \\ &\quad \left( -4m_N^2 E_R^2 + 8m_N m_\chi^2 E_R - 8m_N m_\chi E_R^2 + 2m_N E_R^3 + m_\chi^4 + 4m_\chi^3 E_R - 3m_\chi^2 E_R^2 \right), \end{aligned}$$

$$\frac{dR}{dE_R} = N_T \frac{\rho_\chi}{m_\chi} \int \frac{d\sigma}{dE_R} v f(\mathbf{v}) d^3\mathbf{v}$$

$$\begin{aligned} \frac{dR_{DC}}{dE_R} &= N_T \frac{\rho_\chi}{m_\chi} \sqrt{\frac{E_R}{2m_N}} \frac{e^2 U^2 m_N}{4\pi m_\chi p_\nu (m_{A'}^2 + 2m_N E_R)^2} Z^2 F_Z^2(E_R) \int d^3\mathbf{v} \frac{f(\mathbf{v})}{v} \Theta(v - v_{\min}) \\ &\quad \times [6m_N^2 m_\chi E_R - 8m_N^2 E_R^2 - m_N m_\chi^3 + 4m_N m_\chi^2 E_R - 2m_N m_\chi E_R^2 + m_\chi^3 E_R], \quad (3.3) \end{aligned}$$



# DM absorption by nuclear targets

$$\frac{dR_{DC}}{dE_R} = N_T \frac{\rho_\chi}{m_\chi} \sqrt{\frac{E_R}{2m_N}} \frac{e^2 U^2 m_N}{4\pi m_\chi p_\nu (m_{A'}^2 + 2m_N E_R)^2} Z^2 F_Z^2(E_R) \int d^3\mathbf{v} \frac{f(\mathbf{v})}{v} \Theta(v - v_{\min})$$

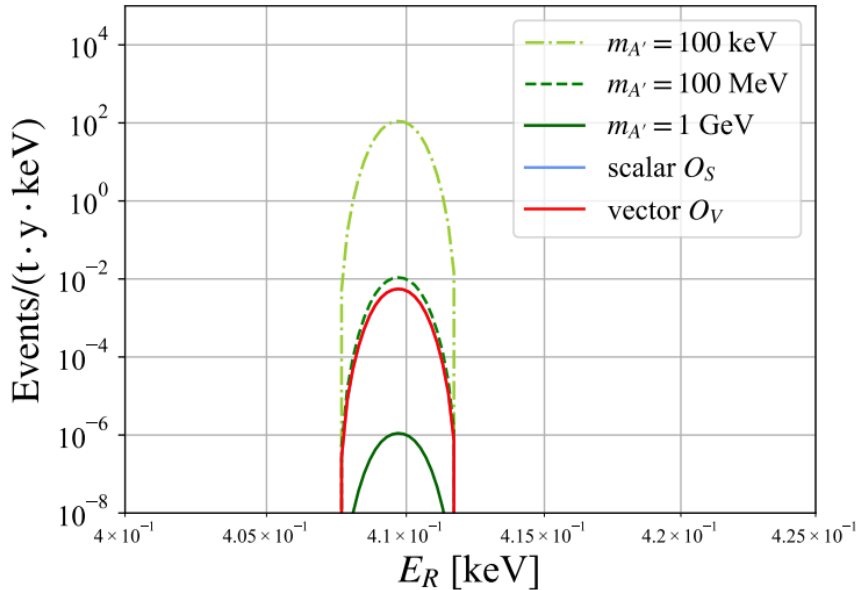
$$\times [6m_N^2 m_\chi E_R - 8m_N^2 E_R^2 - m_N m_\chi^3 + 4m_N m_\chi^2 E_R - 2m_N m_\chi E_R^2 + m_\chi^3 E_R], \quad (3.3)$$

$$e^2 U^2 = 1/\Lambda^2 = 10^{-50} \text{ cm}^2$$

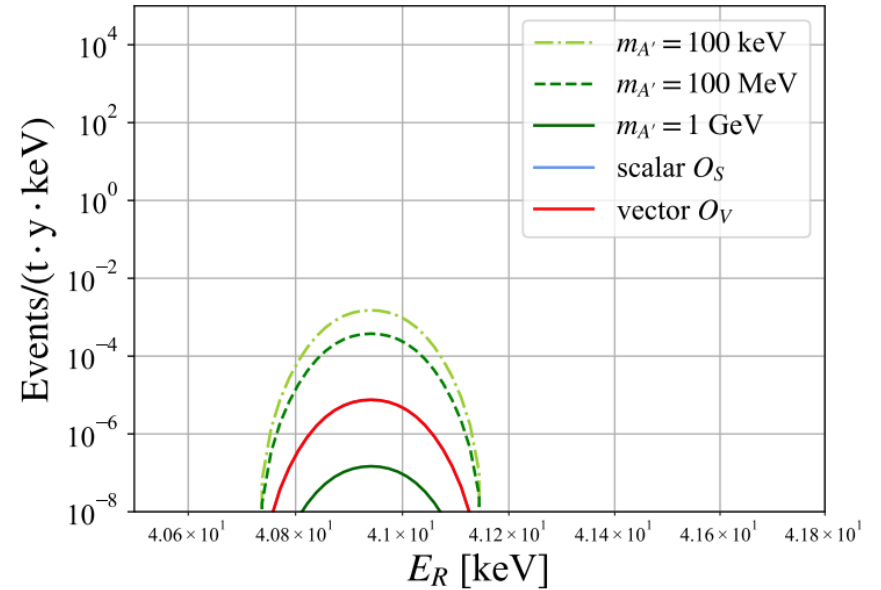
$$O_V = \frac{1}{\Lambda^2} (\bar{\chi} \gamma^\mu P_{L,R} \nu) (\bar{e} \gamma_\mu e),$$

[2011.01940]

$$O_S = \frac{1}{\Lambda^2} (\bar{\chi} P_{L,R} \nu) (\bar{e} e),$$

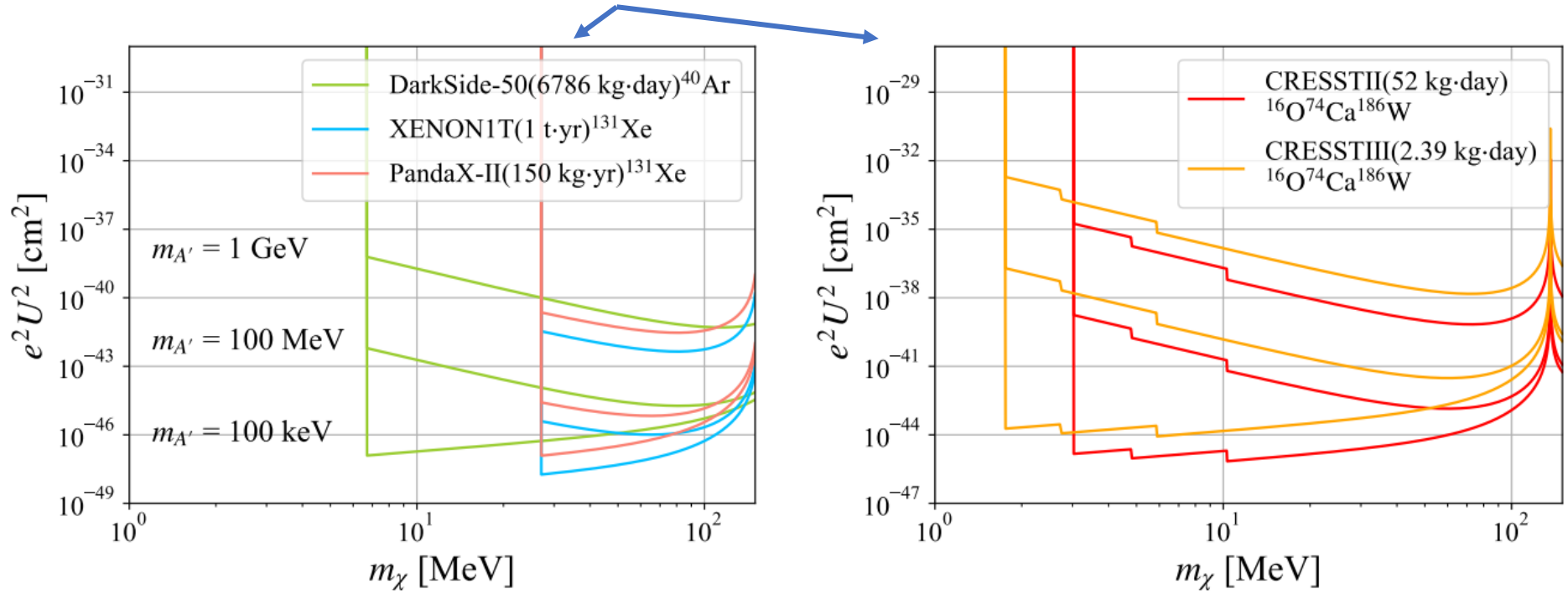


(a)  $m_\chi = 10 \text{ MeV}$



(b)  $m_\chi = 100 \text{ MeV}$

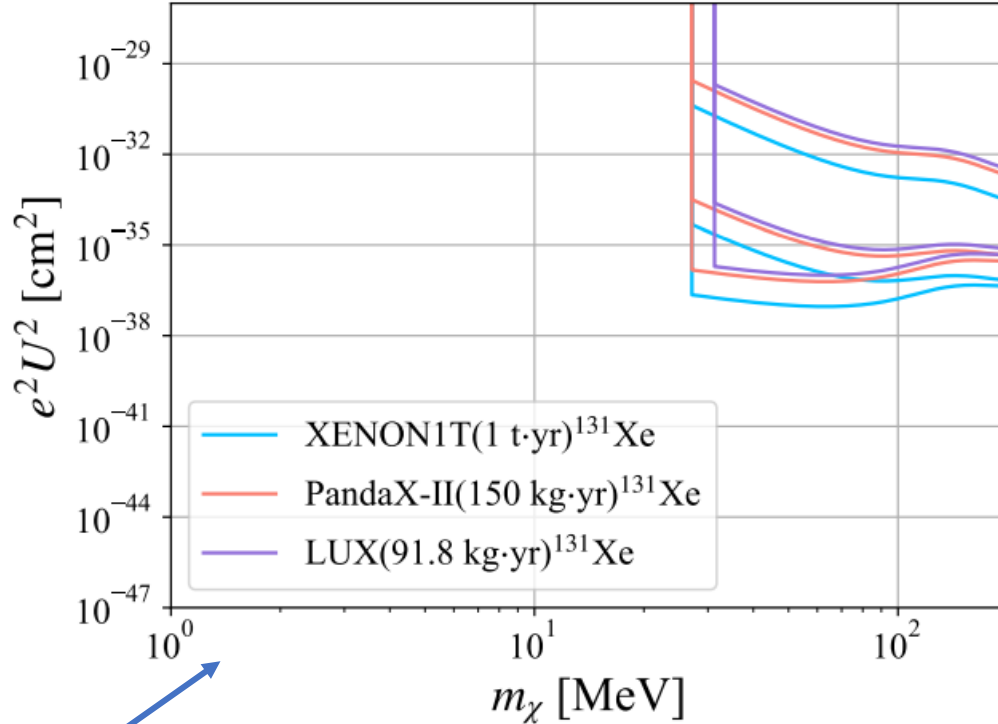
$$R_{DC} = N_T \left( \frac{\rho_\chi}{m_\chi} \right) \frac{e^2 U^2}{4\pi(m_{A'}^2 + m_\chi^2)^2} (2m_\chi^4) Z^2 F_Z^2(q) \Theta(E_R^0 - E_{th})$$



$$R_{DD} = N_T \left( \frac{\rho_\chi}{m_\chi} \right) \frac{\mu_N^2 U^2}{2\pi(m_{A'}^2 + m_\chi^2)^2} \frac{I+1}{3I} \left( \frac{m_\chi^3}{2m_N} \right) F_D^2(q) \frac{m_\chi^4}{2m_N^2} (8m_N^2 - m_\chi^2) \Theta(E_R^0 - E_{th})$$

$$F_D^2(q) = \left( 0.4 \frac{L(q)}{L(0)} + 0.6 \sqrt{\frac{S(q)}{S(0)}} \right)^2 \quad [1007.4200]$$

$$R_{DC} = N_T \left( \frac{\rho_\chi}{m_\chi} \right) \frac{e^2 U^2}{4\pi(m_{A'}^2 + m_\chi^2)^2} (2m_\chi^4) Z^2 F_Z^2(q) \Theta(E_R^0 - E_{th})$$

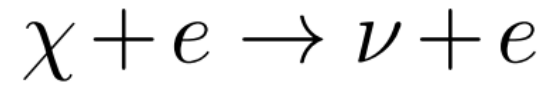


- No significant contribution from dipole-dipole interaction for the inelastic DM absorption.
- DM lifetime constraint is quite severe for the sensitive region of inelastic DM-nucleus scattering.

$$\Gamma(\chi \rightarrow \nu\gamma\gamma\gamma)$$

$$R_{DD} = N_T \left( \frac{\rho_\chi}{m_\chi} \right) \frac{\mu_N^2 U^2}{2\pi(m_{A'}^2 + m_\chi^2)^2} \frac{I+1}{3I} \left( \frac{m_\chi^3}{2m_N} \right) F_D^2(q) \frac{m_\chi^4}{2m_N^2} (8m_N^2 - m_\chi^2) \Theta(E_R^0 - E_{th})$$

$$F_D^2(q) = \left( 0.4 \frac{L(q)}{L(0)} + 0.6 \sqrt{\frac{S(q)}{S(0)}} \right)^2$$



# DM absorption by electron targets

$$\begin{aligned} \frac{d\langle\sigma_{\text{ion}}^{nl} v\rangle_{DC}}{dE_R} &= \frac{|\mathcal{M}|^2}{64\pi m_\chi m_e^2} \frac{q}{E_R} |f_{\text{ion}}^{nl}(k', q)|^2 \Theta(q) \quad \longrightarrow \text{Ionization form factor} \\ &= \frac{e^2 U^2}{16\pi(m_{A'}^2 - m_\chi(m_\chi - 2q))^2} \frac{q}{E_R} \frac{m_\chi^2}{m_e^2} |f_{\text{ion}}^{nl}(k', q)|^2 \Theta(q) \\ &\times [-4m_e m_\chi(m_e + m_\chi) - m_\chi^3 + 3(m_\chi^2 + 2m_e^2 + 4m_e m_\chi)q - 2(m_\chi + 4m_e)q^2] \end{aligned}$$

$(m_\chi \lesssim 50 \text{ keV})$

$$|f_{\text{ion}}^{nl}(k', q)|^2 = \frac{4k'^3}{(2\pi)^3} \sum_{l'l} (2l+1)(2l'+1)(2L+1) \times \begin{bmatrix} l & l' & L \\ 0 & 0 & 0 \end{bmatrix}^2 \left| \int r^2 dr R_{k'l'}(r) R_{nl}(r) j_L(qr) \right|^2$$

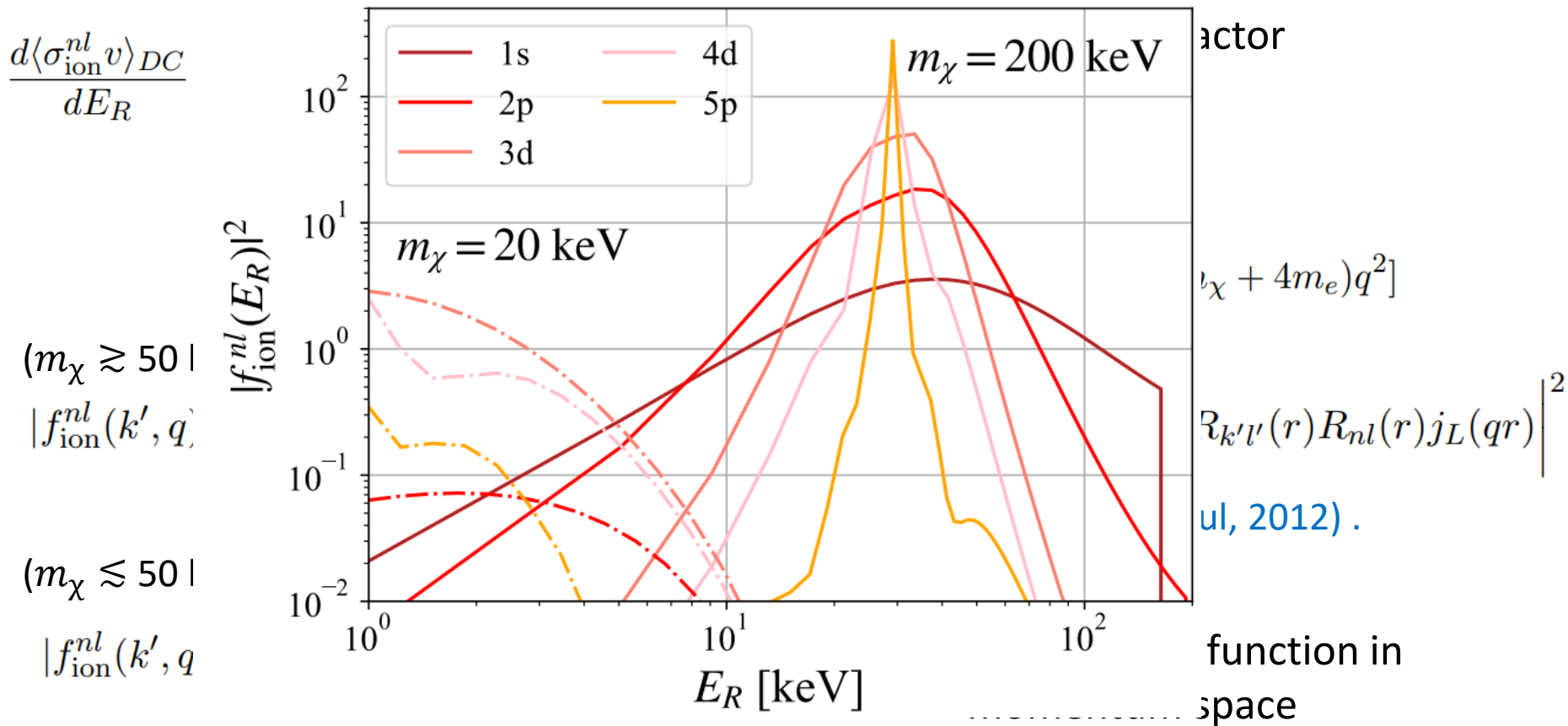
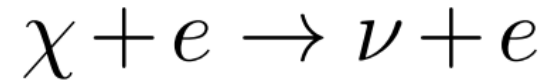
R. Essig et al. Physical Review Letters 109 (Jul, 2012) .

$(m_\chi \gtrsim 50 \text{ keV})$

$$|f_{\text{ion}}^{nl}(k', q)|^2 = \frac{(2l+1)k'^2}{4\pi^3 q} \int_{|k'-q|}^{|k'+q|} k dk |\chi_{nl}(k)|^2 \quad \longrightarrow \text{an analytical function in momentum space}$$

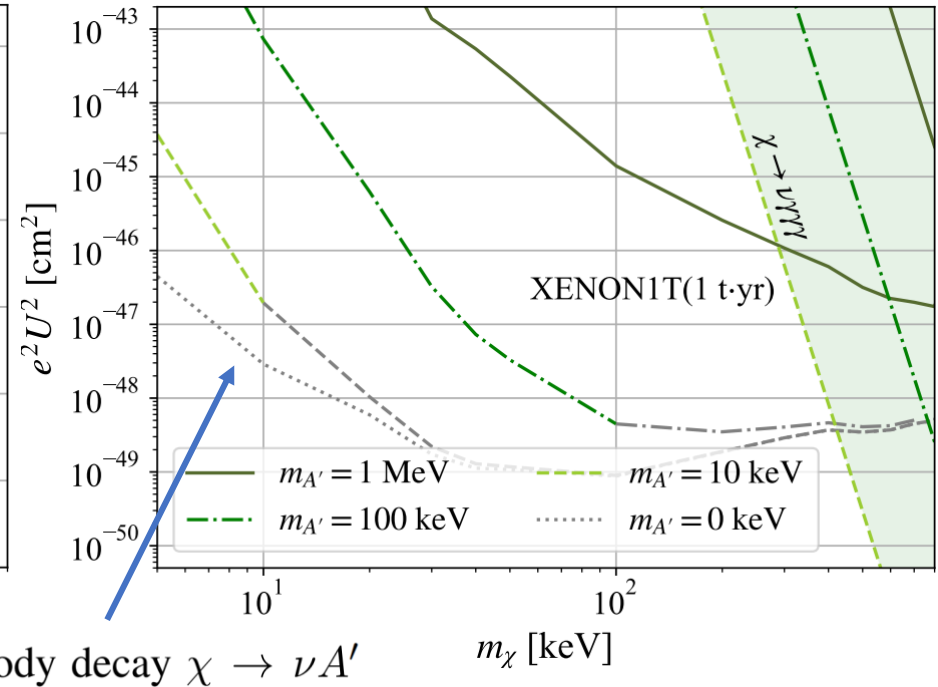
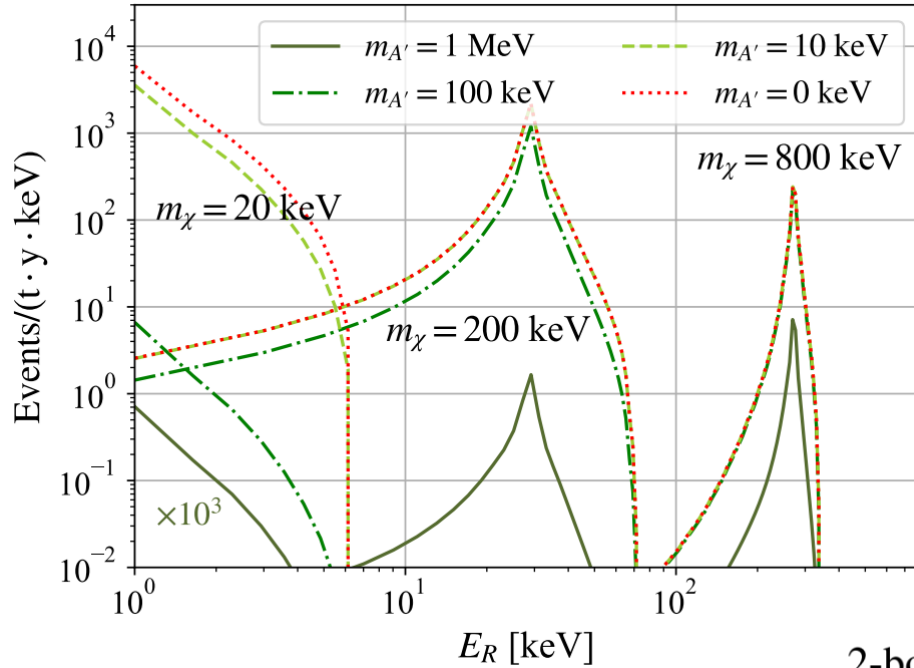
R. Essig et al. Physical Review D 85 (Apr, 2012) .

# Dark Matter Absorption by Electron Targets



R. Essig et al. Physical Review D 85 (Apr, 2012) .

The coupling  $e^2 U^2$  is fixed at  $10^{-45} \text{ cm}^2$



- energy conservation:

$$q = m_\chi + E_B^{nl} - E_R > 0$$

make the constraint more severe

- DM lifetime should be longer than

$$t_{\text{Universe}} = 4.4 \times 10^{17} \text{ sec}$$

$$\Gamma(\chi \rightarrow \nu \gamma \gamma) \simeq 10^{-32} \text{ s}^{-1} \left( \frac{m_\chi}{100 \text{ keV}} \right)^{15} \left( \text{TeV} \cdot eU \right)^2 \left( \frac{\text{GeV}}{m_{A'}} \right)^4$$

[1905.12635].

# Summary

- The fermionic DM absorption by nucleus or electron targets provides a distinctive signal to search for sub-GeV DM.
- Inelastic DM-nuclear absorption scattering is severely limited by DM lifetime.
- The absorption of DM by bound electron induces ionization signal and is sensitive to sub-MeV DM mass below 100 keV. For extremely small dark photon mass, the limit of coupling  $e^2 U^2$  can reach as small as  $10^{-49} \text{cm}^2$ .



# Summary

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Thank you!