



# Studies of $\gamma \gamma \rightarrow \gamma \psi(2S)$ and $e^+e^- \rightarrow \eta \phi$ via ISR at Belle

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中国物理学会高能物理分会 第十一届全国会员代表大会暨学术年会 2022.08.10,大连



## 1 Study of $\gamma\gamma \rightarrow \gamma\psi(2S)$

Phys. Rev. D 105, 112011 (2022)

#### **Motivation**

- More than two dozen new resonances that are dubbed as X, Y or Z states have been found above the DD threshold since Belle observed the X(3872) in B → Kπ<sup>+</sup>π<sup>-</sup>J/ψ [Phys. Rev. Lett. 91, 262001(2003)].
- Many puzzles arise from these XYZ states, and one of them concerns the candidates for P-wave triplet states near 3.9 GeV/c<sup>2</sup>.
- The Z(3930) was discovered by Belle in the process  $\gamma\gamma \rightarrow D\overline{D}$ , and the angular distribution was used to identify it as the  $\chi_{c2}(2P)$  state. [PRL 96, 082003 (2006)] The X(3915) was discovered by both Belle and BABAR favored the  $J^{PC} = 0^{++}$ .[PRL 104, 092001 (2010)]
- Both 0<sup>++</sup> and 2<sup>++</sup> states can be produced in two-photon collisions and can decay to  $\gamma\psi(2S)$  via  $E_1$  transition. The partial widths are expected to be  $\Gamma(\chi_{c0}(2P) \rightarrow \gamma\psi(2S)) \approx 135 \text{ keV}$  and  $\Gamma(\chi_{c2} \rightarrow \gamma\psi(2S)) \approx 207 \text{keV}$ .



#### $J/\psi$ and $\psi(2S)$ reconstructions

- Fitting functions: A Gaussian function for  $J/\psi(\psi(2S))$  signals, 1<sup>st</sup>-order polynominal for background
- Mass resolution:  $\sigma_{J/\psi} = 11.0 \pm 0.6 \text{ MeV}/c^2$ ,  $\sigma_{\psi(2S)} = 2.80 \pm 0.21 \text{MeV}/c^2$ M $(\pi^+\pi^-J/\psi) = M(\pi^+\pi^-l^+l^-) - M(l^+l^-) + m_{J/\psi}$  to improve  $\psi(2S)$  mass resolution



□ Signal regions :  $|M_{l^+l^-} - m_{J/\psi}| < 4\sigma_{J/\psi}(\sigma_{J/\psi} \equiv 11.0 \text{ MeV}/c^2)$ 

$$\begin{split} \left| M_{\pi^{+}\pi^{-}J/\psi} - m_{\psi(2S)} \right| < 2.5\sigma_{\psi(2S)}(\sigma_{\psi(2S)} \equiv 2.8 \text{MeV}/c^{2}) \\ \blacksquare \text{ Sideband region} : \left| M_{\pi^{+}\pi^{-}J/\psi} - m_{\psi(2S)} \pm 9\sigma_{\psi(2S)} \right| < 3.75\sigma_{\psi(2S)} \end{split}$$

#### **Optimization of selection criteria**

• The background is dominated by  $e^+e^- \rightarrow \psi(2S)$  via ISR



- For two-photon collision events,  $M^2_{rec}(\gamma\psi(2S))$  would be large.
- For ISR events,  $M^2_{rec}(\gamma\psi(2S))$  is around zero.
- $M^2_{rec}(\gamma \psi(2S)) > 10 (GeV/c^2)^2$  to remove most ISR events



- Optimize the selections of  $P_t^*(\psi(2S))$  and  $P_t^*(\gamma\psi(2S))$  based on the Punzi figure of
  - merit(FOM), defined as FOM  $\equiv \frac{\varepsilon(t)}{\frac{a}{2} + \sqrt{N_{bkg(t)}}}$

 $P_t^*(\psi(2S))$ >0.1GeV/c,  $P_t^*(\gamma\psi(2S))$  <0.2 GeV/c

#### Mass distribution of $\gamma\psi(2S)$ and two structures



Two excesses around 3.92 and 4.02 GeV/ $c^2$ 

• Fit function:  $f_{sum} = f_{R1} + f_{R2} + f_{ISR} + f_{bkg} + f_{SB}$ 

 $f_{R1}$ ,  $f_{R2}$ : Breit-Wigner  $\otimes$  Crystall Ball function (solid red line)  $f_{ISR}$ : for ISR events (green blank histogram)

 $f_{bkg}$ : possible addition backgrounds(pink dashed line)

 $f_{SB}$  : the background in  $\psi(2S)$  reconstruction (blue shaded histogram)

Resonant parameters	J = 0	J = 2		
$M_{R_1}$	$3922.4 \pm 6.5 \pm 2.0$			
$\Gamma_{R_1}$	$22\pm17\pm4$			
$\Gamma_{\gamma\gamma}\mathcal{B}(R_1 \to \gamma \psi(2S))$	$9.8\pm3.6\pm1.3$	$2.0\pm0.7\pm0.2$		
$M_{R_2}$	$4014.3 \pm 4.0 \pm 1.5$			
$\Gamma_{R_2}$	$4 \pm 11 \pm 6$			
$\Gamma_{\gamma\gamma}\mathcal{B}(R_2 \to \gamma\psi(2S))$	$6.2\pm2.2\pm0.8$	$1.2\pm0.4\pm0.2$		

- *R*<sub>1</sub> near 3.92 GeV/*c*<sup>2</sup>:
   3.1σ including systematic uncertainties
- R<sub>2</sub> near 4.01 GeV/c<sup>2</sup>: study on look-elsewhere effect show a global significance of 2.8σ.

#### **Discussion on the two structures**

- $R_1$  may be X(3915),  $\chi_{c2}(3930)$ , or mix of them. Assuming  $R_1$  is the  $\chi_{c2}(3930)$ , a rough estimation shows  $\Gamma(\chi_{c2}(3930) \rightarrow \gamma \psi(2S)) = 200 \sim 300$  keV. [207 keV calculated by GI model in PRD 72, 054026 (2005)]
- R<sub>2</sub> has the same mass and width with 2<sup>++</sup> partner of X(3872) predicted in PRD 88, 054007(2013), Eur. Phys. J. C 75, 547 (2015)



- The newly reported X(4014) state still needs to be studied, and the study on the  $D^*\overline{D}^*$  interaction is crucial to explore possible internal structure.
- The possibility of the X(4014) as the  $D^*\overline{D}^*$ molecular state and its favored quantum numbers.[arXiv:2207.03930]



#### **Motivation**



• Aspects of  $\phi(2170)$  are still not fully understood.

- Published experimental information
  - ✓ Limited decay modes
  - ✓ Inconsistence on mass & width
- Theorists explain  $\phi(2170)$  as
  - ✓  $s\bar{s}g$  hybrid
  - ✓  $2^3 D_1$  or  $3^3 S_1 s \bar{s}$
  - ✓ Tetraquark
  - ✓ Molecular state  $\Lambda\overline{\Lambda}$
  - ✓  $\phi f_0(980)$  resonance with FSI
  - ✓ Three body system  $\phi KK$
  - Estimated or ruled out: not yet



#### $\phi$ and $\eta$ signals and sidebands

 $\square \eta \to \pi^+ \pi^- \pi^0 / \gamma \gamma, \phi \to K^+ K^-$ 



♦  $|M_{K^+K^-} - m(\phi)| < 12 \text{MeV}/c^2$  as signal region, 0.990< $M_{K^+K^-}$ <1.002GeV/ $c^2$ , 1.036< $M_{K^+K^-}$ <1.048 GeV/ $c^2$  as sideband region.

- $\begin{aligned} & \left| M_{\pi^{+}\pi^{-}\pi^{0}/\gamma\gamma} m_{\eta} \right| < 3\sigma_{\pi^{+}\pi^{-}\pi^{0}/\gamma\gamma} \text{ as signal region,} \\ & \left| M_{\pi^{+}\pi^{-}\pi^{0}/\gamma\gamma} m_{\eta} \pm 9\sigma_{\pi^{+}\pi^{-}\pi^{0}/\gamma\gamma} \right| < 3\sigma_{\pi^{+}\pi^{-}\pi^{0}/\gamma\gamma} \text{ as sideband} \\ & \text{region}(\sigma_{\pi^{+}\pi^{-}\pi^{0}} = 4.2 \text{MeV}/c^{2}, \sigma_{\gamma\gamma} = 11.3 \text{ MeV}/c^{2}) \end{aligned}$
- S1, S2 and S3 represent the sum of the events in the horizontal two, vertical two nearest sideband boxes and the four diagonal sideband boxes to the signal box

The normalized factor :  $S = a \cdot S_1 + b \cdot S_2 - ab \cdot S_3$ 



#### **ISR characters of the final states**



- The photon with the highest energy is identified to be  $\gamma_{ISR}$ .
- The missing component after  $\eta$ ,  $\phi$  and  $\gamma_{ISR}$  being reconstructed is nothing or another ISR photon with lower energy
- $\left|M_{miss}^2(\gamma_{ISR}\eta\phi)\right| < 0.1 (GeV/c^2)^2$ , the efficiency is about 97~98%
- The good agreements between data and signal MC simulations on visible energy  $(E_{vis})$  and the polar angle of the  $\eta\phi$  system in the  $e^+e^-$  CM frame  $(\cos\theta(\eta\phi))$ .

#### Invariant mass spectrum of $\eta\phi$



• Clear  $J/\psi$  signals in both  $\pi^+\pi^-\pi^0$  and  $\gamma\gamma$  mode

• The branching fraction of  $J/\psi \rightarrow \eta \phi$ 

$$\mathcal{B}(J/\psi \to \eta \phi) = \frac{N_{sig}^{fit}}{\sigma_{ISR}^{prod} \times \mathcal{L} \times \varepsilon \times \mathcal{B}(\phi \to K^+K^-) \times \mathcal{B}(\eta \to \gamma \gamma/\pi^+\pi^-\pi^0)}$$

- $\mathcal{B}(J/\psi \rightarrow \eta \phi) = (0.71 \pm 0.10 \pm 0.05) \times 10^{-3}$ , which agrees well with the world average value,  $(0.74 \pm 0.08) \times 10^{-3}$ .
- There is no obvious signal of  $\phi(2170)$ , but the resonant parameters of  $\phi(1680)$  could be measured more precisely.

### Fitting the $M(\eta\phi)$

An unbinned maximum likelihood fit is perform to the  $M_{\eta\phi}$  mass spectra  $\in$ [1.55, 2.85] GeV/ $c^2$  using signal candidate events and 2D sideband events simultaneously.







### Fitting the $M(\eta\phi)$

• Fit results with  $\phi(1680)$  and  $\phi(2170)$  both included, and also excluding  $\phi(2170)$ . The mass and width of  $\phi(2170)$  are fixed from prior BESIII measurement.

Parameters	with $\phi(2170)$			without $\phi(2170)$		
	Solution I	Solution II	Solution III	Solution IV	Solution I	Solution II
$\chi^2/ndf$	77/56		85/60			
$a_0$	$-4.1\pm0.5$	$5.0\pm0.7$	$-5.0\pm0.5$	$-4.8\pm0.2$	$-3.2 \pm 0.7$	$5.0\pm0.1$
$a_1$	$2.7\pm0.1$	$2.6\pm0.1$	$2.7\pm0.1$	$2.6\pm0.1$	$2.9\pm0.1$	$2.6\pm0.1$
$\mathcal{B}_{\eta\phi}^{\phi(1680)}\Gamma_{e^+e^-}^{\phi(1680)}(eV)$	$122\pm6$	$219\pm15$	$163\pm11$	$203\pm12$	$75\pm10$	$207\pm16$
$M_{\phi(1680)}({ m MeV}/c^2)$	$1683\pm7$		$1696\pm 8$			
$\Gamma_{\phi(1680)}({ m MeV})$	$149 \pm 12$			$175\pm13$		
$\mathcal{B}^{\phi(1680)}_{\eta\phi}$	$0.18\pm0.02$	$0.19\pm0.04$	$0.21\pm0.02$	$0.17\pm0.04$	$0.25\pm0.12$	$0.23\pm0.10$
$\mathcal{B}_{\eta\phi}^{\phi(2170)}\Gamma_{e^+e^-}^{\phi(2170)}(\text{eV})$	$0.09 \pm 0.05$	$0.06\pm0.02$	$16.7\pm1.2$	$17.0\pm1.2$	_	
$M_{\phi(2170)}({ m MeV}/c^2)$	2163.5 (fixed)					
$\Gamma_{\phi(2170)}({ m MeV})$	31.1(fixed)					
$ heta_{\phi(1680)}(^{\circ})$	$-89\pm2$	$96\pm 6$	$-92\pm1$	$-86\pm7$	$-87 \pm 15$	$108\pm22$
$ heta_{\phi(2170)}(^{\circ})$	$37 \pm 14$	$-102\pm11$	$-167\pm6$	$-155\pm5$		_

• The statistical significance of  $\phi(2170)$  is  $1.7\sigma$ , the upper limit of  $\phi(2170)$  at 90% *C.L* is determined to be 0.17 eV or 18.6 eV.

#### Cross sections of $e^+e^- \rightarrow \eta \phi$

• The  $M_{\eta\phi}$  distributions are combined and the cross section of  $e^+e^- \rightarrow \eta\phi$  for each  $M_{\eta\phi}$  bin is calculated according to

$$\sigma_i = \frac{n_i^{obs} - n_i^{bkg}}{\mathcal{L}_i \times \sum_j \varepsilon_{ij} \mathcal{B}_j}$$



#### Summary

- → With the full data sample taken by Belle, the ISR process  $e^+e^- \rightarrow \eta \phi$  has been scanned from threshold to 3.95 GeV/ $c^2$ .
- $\succ$  The branching fraction of J/ψ → ηφ is measured , which is in good agreement with the world average value from PDG.

> No significant  $\phi(2170)$  in this work; the upper limit of  $\phi(2170)$  at 90% *C.L* is calculated and  $\phi(1680)$  resonant parameters are measured in this work.

## Thank you for your attentions!

#### Back up

#### **Systematic Uncertainties**

Relative error (%) Source J=2J=0. . . Particle identification 2.8 Tracking efficiency 1.4 2.0Photon reconstruction  $\psi(2S)$  mass window 0.6  $P_t^*(\psi(2S))$  and  $P_t^*(\gamma\psi(2S))$ 1.0  $M_{\rm rec}^2(\gamma\psi(2S))$ 0.5 Integrated luminosity 1.4 4.3 Helicity . . . Luminosity function 2.5 Branching fractions 1.3 Statistics of MC samples 0.7 6.6 Sum in quadrature 5.1

#### **Data and MC samples**

• Data: HadronB(J) and tauskimB (980  $fb^{-1}$ , exp7-73)

• MC:

- ♦ J/ψ → ηφ, η → π<sup>+</sup>π<sup>-</sup>π<sup>0</sup>/γγ, φ → K<sup>+</sup>K<sup>-</sup> (10<sup>5</sup> events)
   Y(2175) → ηφ,η → π<sup>+</sup>π<sup>-</sup>π<sup>0</sup>/γγ, φ → K<sup>+</sup>K<sup>-</sup> (10<sup>5</sup> events)
   φ(1680) → ηφ,η → π<sup>+</sup>π<sup>-</sup>π<sup>0</sup>/γγ, φ → K<sup>+</sup>K<sup>-</sup> (3×10<sup>5</sup> events)
- \$VD2a(Exp.31-55):SVD2b(Exp.61-69):SVD1(Exp.7-27):5S(Exp71-73)=8:5:3:4, PHOKHARA

#### **Selection Criteria**

	$\pi^+\pi^-\pi^0$ mode	γγ mode		
The number of charged tracks	$3 \le N_{trk} \le 4$	$N_{trk} = 2$		
PID	for $K^{\pm}$ , $\frac{\mathcal{L}K}{\mathcal{L}K + \mathcal{L}\pi} > 0.6$ for $\pi^{\pm}$ , $\frac{\mathcal{L}K}{\mathcal{L}K + \mathcal{L}\pi} < 0.4$	For $K^{\pm}$ , $\frac{\mathcal{L}K}{\mathcal{L}K + \mathcal{L}\pi} > 0.6$		
Photon energies	$E(\gamma)>25MeV$ in the barrel $E(\gamma)>50MeV$ in the endcap	$E_l(\gamma)$ >120MeV $E_h(\gamma)$ >350MeV		
$\phi$ mass cut	$ M(K^+K^-) - m(\phi)  < 3\sigma(\sigma = 4MeV/c^2)$			
$\pi^0$ mass cut	120MeV/ $c^2$ <m(<math>\gamma\gamma)&lt;150MeV/<math>c^2</math> <math>\chi^2(\pi^0) &lt; 25</math></m(<math>	_		
$\eta$ mass cut	$ M(\pi^{+}\pi^{-}\pi^{0}) - m(\eta)  < 3\sigma$ $(\sigma = 4.2 MeV/c^{2})$	$\begin{split}  M(\gamma\gamma)-m(\eta)  < 3\sigma \\ (\sigma = 11.3 MeV/c^2) \end{split}$		
Recoil mass cut	$\left M_{miss}^{2}(\gamma_{ISR}\eta\phi)\right  < 0.1 (GeV/c^{2})^{2}$			

#### Fitting the M( $\eta\phi$ )

• The parametrization for the cross section of  $e^+e^- \rightarrow \eta \phi$ 

$$\sigma_{\eta\phi}(\sqrt{s}) = 12\pi \mathcal{P}_{\eta\phi}(\sqrt{s}) \left| A_{\eta\phi}^{n.r.}(\sqrt{s}) + A_{\eta\phi}^{\phi(1680)}(\sqrt{s}) + A_{\eta\phi}^{\phi(2170)}(\sqrt{s}) \right|^2$$

 $A_{\eta\phi}^{n.r.}(\sqrt{s}) = a_0/s^{a_1}$  is used to describe the non-resonant contribution

$$A_{\eta\phi}^{\phi(1680)}(\sqrt{s}) = \sqrt{\mathcal{B}_{\phi(1680)}^{\eta\phi}\Gamma_{\phi(1680)}^{e^+e^-}} \frac{\sqrt{\Gamma_{\phi(1680)}/\mathcal{P}_{\eta\phi}(M_{\phi(1680)}^2)} e^{i\theta_{\phi(1680)}}}{M_{\phi(1680)}^2 - s - i\sqrt{s}\Gamma_{\phi(1680)}(\sqrt{s})}$$

$$\Gamma_{\phi(1680)}(\sqrt{s}) = \Gamma_{\phi(1680)}[\frac{\mathcal{P}_{KK^*(892)}(\sqrt{s})}{\mathcal{P}_{KK^*(892)}(M_{\phi(1680)})}\mathcal{B}_{\phi(1680)}^{KK^*(892)} + \frac{\mathcal{P}_{\eta\phi}(\sqrt{s})}{\mathcal{P}_{\eta\phi}(M_{\phi(1680)})}\mathcal{B}_{\phi(1680)}^{\eta\phi}$$

$$+ (1 - \mathcal{B}_{\phi(1680)}^{\eta\phi} - \mathcal{B}_{\phi(1680)}^{KK^*(892)})].$$

 $\mathcal{B}_{\phi(1680)}^{KK^*(892)} \approx 2 \times \mathcal{B}_{\phi(1680)}^{\eta \phi}$  from Ref. [1] directly

$$A_{\eta\phi}^{\phi(2170)}(s) = \sqrt{\mathcal{B}_{\phi(2170)}^{\eta\phi}\Gamma_{\phi(2170)}^{e^+e^-}} \frac{\sqrt{\Gamma_{\phi(2170)}/\mathcal{P}_{\eta\phi}(M_{\phi(2170)}^2)} e^{i\theta_{\phi(2170)}}}{M_{\phi(2170)}^2 - s - i\sqrt{s}\Gamma_{\phi(2170)}} \cdot \frac{B(p)}{B(p')}$$

#### [1] Phys. Rev. D 77, 092002 (2008)

#### Systematic Uncertainty

Source	$\gamma\gamma$ mode	$\pi^+\pi^-\pi^0$ mode	common
Particle identification	2.0	4.0	2.0
Tracking	0.7	1.4	0.7
Photon reconstruction	6.0	6.0	6.0
$\phi, \eta$ masses and $M_{\rm miss}^2(\eta\phi\gamma_{\rm ISR})$	1.7	1.4	1.4
Luminosity	1.4	1.4	1.4
Generator	0.5	0.5	0.5
$\sigma^{ m prod}_{ m ISR}(J/\psi)$	1.0	1.0	1.0
Trigger	1.5	1.0	
Branching fractions	0.6	0.6	0.6
$J/\psi$ signal fitting	1.8	1.5	
MC statistics	0.1	0.1	0.1
Sum for $\sigma(e^+e^- \to \eta\phi)$	6.9	7.3	6.7
Sum for $\mathcal{B}(J/\psi \to \eta \phi)$	7.2	7.9	6.8

■ The total irrelevant uncertainties  $(\sigma_{tot})$  is calculated by  $\sqrt{\sum_i (\Delta \varepsilon_i \times B_i)^2 / \sum_i (\varepsilon_i \times B_i)}$ , where  $\Delta \varepsilon_i$  equal to  $\sigma_i \times \varepsilon_i$ , *i* is *i*-th mode of  $\eta$  decays. ■  $\sigma_{sys}$ =6.8% is calculated by  $\sqrt{\sum_j {\sigma_j}^2 + \sigma_{tot}^2}$  ( $\sigma_j$  is the each source of common uncertainties mentioned above)