Global constraint on the jet transport coefficient from single hadron, dihadron and γ -hadron spectra in high-energy heavy-ion collisions

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Collaborate with Wei-Yao Ke, Han-Zhong Zhang and Xin-Nian Wang [arXiv: 2206.01340]





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- Motivation
- NLO pQCD parton model and JQ-mFFs
- Bayesian inference of $\hat{q}(T)$ with information field method
 - 1. Prior of unknown function in an IFT method;
 - 2. The posterior distribution.
- Constraining the T dependence of $\hat{q}(T)$
 - 1. Combined analysis using both R_{AA} and I_{AA} ;
 - 2. Progressive constraining power from peripheral to central collisions.
- Validation and predictions
- Summary

Motivation



- Quark-gluon plasma (QGP) has been created in high-energy HIC.
- Jet quenching is an extremely useful tool to explore the properties of QGP.
 [X.-N. Wang and M. Gyulassy, PRL 68, 1480 (1992)]



- The energetic jet losses a large amount of its energy via radiating gluon induced by multiple scatterings, leading to the suppression of the yield of jets and high- $p_{\rm T}$ hadrons.
- Jet energy loss in QGP medium: $\Delta E \propto \hat{q}$.
- Jet transport parameter: hard parton's transverse momentum broadening squared per unit length.

$$\hat{q} = \rho \int dq_{\rm T}^2 \frac{d\sigma}{dq_{\rm T}^2} q_{\rm T}^2$$
 [BDMPS, N

[BDMPS, NPB 483 (1997) 291]

Motivation



[Xabier Feal, .et al., PLB 816 (2021) 136251] [JETSCAPE], PRC 104 (2021) 2, 024905]

Motivation

Aim: to constrain the T dependence of \hat{q} .

Data:

combined global analysis of R_{AA}^h , I_{AA}^{hh} , $I_{AA}^{\gamma h}$; both RHIC and LHC energies; a wide range of centralities.

Analysis method:

Bayesian inference method; $\hat{q}(T)$ prior of unknown function in an information field.



[HZ Zhang J.F. Owens, EK Wang and XN Wang, Phys. Rev. Lett. 103 (2009) 032302]

ε. (GeV/im)

pQCD parton model

In p-p collisions:

Single inclusive hadron: [J.F.Owens, Rev. Mod. Phys 59,465(1987)]

$$\frac{d\sigma_{pp}^{h}}{dyd^{2}p_{T}} = \sum_{abcd} \int dx_{a} dx_{b} f_{a/p}(x_{a},\mu^{2}) f_{b/p}(x_{b},\mu^{2}) \frac{1}{\pi} \frac{d\sigma_{ab \rightarrow cd}}{dt} \frac{D_{h/c}(z_{c},\mu^{2})}{z_{c}} + \mathcal{O}(\alpha_{s}^{3})$$

$$di-hadron: \frac{d\sigma_{pp}^{hh}}{dy_{h}^{c}d^{2}p_{T}^{h_{c}}dy_{h}^{d}d^{2}p_{T}^{h_{d}}} = \sum_{abcd} \int dz_{c} dz_{d} f_{a/p}(x_{a},\mu^{2}) f_{b/p}(x_{b},\mu^{2}) \frac{x_{a}x_{b}}{\pi z_{c}^{2} z_{d}^{2}} \frac{d\sigma_{ab \rightarrow cd}}{dt}$$

$$\times D_{h/c}(z_{c},\mu^{2}) D_{h/d}(z_{d},\mu^{2}) \delta^{2}(\overrightarrow{p}_{T}^{c}+\overrightarrow{p}_{T}^{d}) + \mathcal{O}(\alpha_{s}^{3})$$

$$\varphi-hadron: \frac{d\sigma_{pp}^{ph}}{dy_{\gamma}d^{2}p_{T}^{\gamma}dy_{h}d^{2}p_{T}^{h}} = \sum_{abd} \int dz_{d} f_{a/p}(x_{a},\mu^{2}) f_{b/p}(x_{b},\mu^{2}) \frac{x_{a}x_{b}}{\pi z_{d}^{2}} \frac{d\sigma_{ab \rightarrow \gamma d}}{dt}$$

$$\varphi-hadron: \frac{d\sigma_{pp}^{ph}}{dy_{\gamma}d^{2}p_{T}^{\gamma}dy_{h}d^{2}p_{T}^{h}} = \sum_{abd} \int dz_{d} f_{a/p}(x_{a},\mu^{2}) f_{b/p}(x_{b},\mu^{2}) \frac{x_{a}x_{b}}{\pi z_{d}^{2}} \frac{d\sigma_{ab \rightarrow \gamma d}}{dt}$$

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$$D_{pp}^{\text{trig}}(z_{\text{T}}) = p_{\text{T}}^{\text{trig}} \frac{d\sigma_{pp}/dy^{\text{trig}} dp_{\text{T}}^{\text{trig}} dy^{\text{assoc}} dp_{\text{T}}^{\text{assoc}}}{d\sigma_{pp}/dy^{\text{trig}} dp_{\text{T}}^{\text{trig}}}, z_{\text{T}} = p_{\text{T}}^{\text{assoc}}/p_{\text{T}}^{\text{trig}}$$



 $f_{a/p}(x_a, \mu^2)$: CT14 PDF

CT14, Phys. Rev. D 95, 034003 (2017)]

$$D_{h/d}(z_d, \mu^2)$$
 : KKP FFs

[KKP, Nucl. Phys. B 582,514(2000)]

p-p baselines



Good agreement with data.

Data from

[PHENIX, Phys. Rev. Lett. 101, 232301 (2008)] [CMS, Eur. Phys. J. C 72, 1945 (2012), JHEP 04, 039] [ALICE, JHEP 11, 013]

p-p baselines



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 $t_A(\vec{r})$: nuclear thickness functions, integrating the Woods – Saxon nuclear density distribution; $f_{a/A}(x_a, \mu^2, \vec{r})$: EPPS16 nPDF [EPPS 16, Eur. Phys. J. C 77, 163 (2017)]

 $\tilde{D}_{h/d}(z_d, \mu^2, \Delta E_d)$: medium – modifed FFs

Medium-modified FFs

$$\tilde{D}_{h/d}(z_d, \mu^2, \Delta E_d) = (1 - e^{-\langle N_g \rangle}) \left[\frac{z_d'}{z_d} D_{h/d}(z_d', \mu^2) + \langle N_g \rangle \frac{z_g'}{z_d} D_{h/g}(z_g', \mu^2) \right] + e^{-\langle N_g \rangle} D_{h/d}(z_d, \mu^2)$$

[X.-N. Wang, PRC70 (2004) 031901], [H. Z. Zhang, J.F. Owens, Enke Wang, X.-N. Wang, PRL 98.212301 (2007);103, 032302 (2009)]

$$\frac{\Delta E_d}{E} = \frac{2C_A \alpha_s}{\pi} \int d\tau \int \frac{dl_T^2}{l_T^4} \int dz \left[1 + (1-z)^2 \right] \hat{q}_d \left(\tau, \vec{r} + \left(\tau - \tau_0 \right) \vec{n} \right) \sin^2 \left(\frac{l_T^2 (\tau - \tau_0)}{4z(1-z)E} \right) \quad \text{High-Twist approach}$$

[W.T. Deng and X.-N. Wang, PRC 81,024902(2010] [E. Wang and X.-N. Wang, PRL 87, 142301 (2001); 89, 162301 (2002)]

$$\left\langle N_g^d \right\rangle = \frac{2C_A \alpha_s}{\pi} \int_{\tau_0}^{\infty} d\tau \int \frac{dl_{\rm T}^2}{l_{\rm T}^4} \int \frac{dz}{z} \left[1 + (1-z)^2 \right] \hat{q}_d \left(\tau, \vec{r} + \left(\tau - \tau_0 \right) \vec{n} \right) \sin^2 \left[\frac{l_{\rm T}^2 \left(\tau - \tau_0 \right)}{4z(1-z)E} \right]$$

[N.B. Chang, W.T. Deng and X.-N. Wang, Phys. Rev. C 89, 03491 (2014)1

Observables: nuclear modification factor

$$R_{AB} = \frac{dN_{AB}/dyd^2p_{\rm T}}{T_{AB}(\vec{b})d\sigma_{pp}/dyd^2p_{\rm T}}; \qquad I_{AB}\left(z_{\rm T}\right) = \frac{D_{AB}\left(z_{\rm T}\right)}{D_{pp}\left(z_{\rm T}\right)}$$

Bayesian inference of $\hat{q}(T)$ with parametric form.



• Strong prior assumption of parametrization form will result in strong correlation of \hat{q} at different T, e.g. $\hat{q}/T^3 = AT + B$.

- The performance of the emulator can be impaired by non-linear response between model prediction and the input parameter, $\hat{q}/T^3 = (1 + (aT/T_c)^p)^{-1}$. [W. Ke, Ph.D. dissertation, arXiv:2001.02766]
- The number of parameters and complexity increases exponential with the number of control variables (e.g. T, E, Q). [JETSCAPE, PRC 104 (2021) 2, 024905]

Bayesian inference of $\hat{q}(T)$ with information field method



- Parametrization from will result in strong correlation of \hat{q} at different T.
- The performance of the emulator can be impaired by non-linear response between model prediction and the input parameter. [W. Ke, Ph.D. dissertation, arXiv:2001.02766]
- The number of parameters and complexity increases exponential with the number of control variables (e.g. T, E, Q). [JETSCAPE, PRC 104 (2021) 2,024905]

Construction of the functional prior $\hat{q}(T)$

true distribution functional form:

$$\langle F(x) \rangle = \mu(x) \qquad F(x) = \ln(\hat{q}/T^3), x = \ln(T/\text{GeV}) \quad \text{[Y.Y. He, X.-N. Wang, etal, PRC 91,054908(2015)]} \\ \langle [F(x) - \mu(x)] [F(x') - \mu(x')] \rangle = C(x, x') \qquad \mu(x) = C; \quad C(x, x') = \sigma^2 e^{-\frac{(x-x')^2}{2L^2}}.$$



 $T_c = 0.165 \text{ GeV}$



The hydrodynamic evolution of the QGP medium provided by the CLVisc (3+1) D hydrodynamic model.

[L. G. Pang, Q. Wang, X.-N. Wang, Phys.Rev.C 86 (2012) 024911], [L. G. Pang, H. Petersen, X.-N. Wang, Phys.Rev.C 97 (2018) 6, 064918]

- $R_{AA}^{\pi^0}$ in 0-5%, 0-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-80%, 80-90% Au-Au collisions at 0.2 TeV;
- $R_{AA}^{h^{\pm}}$ in 0-5%, 5-10%, 10-20%, 20-30%, 30-40%, 40-50%, 50-60%, 60-80%, 70-90% Pb-Pb collisions at 2.76 TeV;
- $R_{AA}^{h^{\pm}}$ in 0-5%, 5-10%, 10-20%, 10-30%, 20-30%, 30-50%, 50-70% Pb-Pb collisions at 5.02 TeV;
- $I_{AA}^{\gamma h^{\pm}}$ in 0-10% Au-Au collisions at 0.2 TeV, (2 trigger ranges);
- $I_{AA}^{\pi^0 h^{\pm}}$ in 0-10% Au-Au collisions at 0.2 TeV, (2 trigger ranges);
- $I_{AA}^{h^{\pm}h^{\pm}}$ in 0-5%, 0-10% Pb-Pb collisions at 2.76 TeV, (6 trigger ranges).

Model calculations with 100 prior $\hat{q}(T)$



The posterior distribution

• Prior distribution of the random function: [Jorsten A. Enßlin Annalen Phys. 531 (2019) 3, 1800127] $P_0[F(x)] = e^{-\frac{1}{2}\int dx dx' \delta F(x) C^{-1}(x, x') \delta F(x')}$

/

$$\delta F(x) = F(x) - \mu(x); \ C(x, x') = \sigma^2 e^{-\frac{(x-x')^2}{2L^2}}$$

 Posterior distribution : [python library emcee: multi-dimensional Gaussian] $P[F(x)] = P_0[F(x)] \times$ Likelihood

$$= \exp\{-\frac{1}{2}\int dx dx' \delta F(x) C^{-1}(x, x') \,\delta F(x') \\ -\frac{1}{2}\left(M'[F] - y_{\exp}\right)^T \Sigma_{\text{error}}^{-1}\left(M'[F] - y_{\exp}\right)\}.$$

- MCMC sampling
- To marginalise the values of F* at a fixed input x* $p(F^*) = \left[\mathscr{D}F \right] \delta \left(F(x^*) - F^* \right) P[F(x)]$



Progressive constraining power from peripheral to central collisions

From low-T —> high-T region; From peripheral —> central collisions; From RHIC —> LHC energies.



The combined analysis compromises between the relatively large \hat{q}/T^3 at low-T as favored by the Au+Au data at the RHIC energy and the small \hat{q}/T^3 at high-T as favored by the Pb+Pb data at the LHC energies.

Constrain the T dependence of $\hat{q}(T)$

ET Collab.

JETSCAPE

0.5

lido

The 95% credible interval around the median of the ensemble prediction of the emulator.

12

10

8

б

4

2

0

0.2

â/T³



[JET Collaboration: Phys. Rev. C 90, 014909 (2014); JETSCAPE: Phys. Rev. C 104, 024905 (2021); LIDO, W. Ke, X.-N. Wang, JHEP 05041.]

0.4

T[GeV]

0.3







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Prediction O-O collisions at 7 TeV



Summary

- A first global Bayesian constraint of $\hat{q}(T)$ using combined experimental data of R_{AA} and I_{AA} in HIC at both RHIC and LHC energies with a wide range of centralities.
- The Bayesian inference method combined with the IFT for the prior unknown functions.
- Random field prior: avoid any intrinsic long-range correlations between prior q/T³ values at different T regions that are usual present in many explicit forms of parameterizations.
 q/T³ decreases with T from 6±2 near T_c to 1.1±0.3 at 3 T_c.
- The extracted $\hat{q}/T^3(T)$ describe for single hadron v_2 at large p_T .
- We also predict the R_{AA} and v_2 in O-O collisions at 7 TeV.



Thank you for your attention!

Single hadron



1 + 2Np representative parameter sets: Np=4; 1 median, 8 sets to get uncertainty. [W. Ke, X.-N. Wang, JHEP 05041.]

Sensitivity of the observables to the T dependence of jet transport coefficient





- At RHIC, observables are more sensitive to \hat{q} in low-T.
- In central collisions and at higher beam energy, observables are more sensitive to \hat{q} in the high-T region.
- \hat{q} are more sensitive to di-h, gam-h.



Di-hadron at LHC with 100 prior $\hat{q}(T)$



- I_{AA} with high trigger suggest a larger \hat{q} .
- Explore $p_{\rm T}$ dependence in the future.

Test transverse momentum sensitivity



- R_{AA} are almost P_{T} independence
 - I_{AA} with high trigger p_{T} suggest a larger \hat{q} .
 - Explore $p_{\rm T}$ -dependence in the future.



Training model emulators with random function realization

- Training data $(\hat{q}_{ij}, \mathbf{y}_{ik}), i = 1 100, j = 1,20;$
 - k = each observable points, including R_{AA} and I_{AA} in each centralities an at each $p_T(z_T)$ point.
- Reduce dimensionality: $N_{\text{feature}} \ll N_{\text{observables}}$.

Principal Component Analysis (PCA):

transform the high-dimensional observables into the "feature" space.

[Scikit-Learn: scikit-learn: Machine learning in Python, <u>http://scikit-learn.org</u>.] [M. E. Tipping and C. M. Bishop, "Mixtures of Probabilistic Principal Component Analyzers", Neural Computation **11**, 443–482 (1999).]

- Training the mapping from \hat{q} to each one of the $N_{feature}$ principal components using an Gaussian emulators. [C. E. Rasmussen and C. K. I. Williams, Gaussian Processes for Machine Learning (MIT Press, Cambridge, MA, 2006), http://gaussianprocess.org/gpml.]
- To predict observables at new input \hat{q} , one transforms the "interpolated" principal components back to the observables space using the inverse PCA transformation.

The posterior distribution

• prior distribution of the random function: $P_0[F(x)] = e^{-\frac{1}{2}\int dx dx' \delta F(x) C^{-1}(x, x') \delta F(x')}$ [Jorsten A. Enßlin Annalen Phys. 531 (2019) 3, 1800127] $\delta F(x) = F(x) - \mu(x) \quad C(x, x') = \sigma^2 e^{-\frac{(x-x')^2}{2L^2}}.$

 $P[F(x)] = P_0[F(x)] \times \text{Likelihood} \qquad [python library emcee: multi-dimensional Gaussian]} \\ = \exp\left\{-\frac{1}{2}\int dx dx' \delta F(x) C^{-1}(x, x') \,\delta F(x') - \frac{1}{2}\left(M'[F] - y_{exp}\right)^T \Sigma_{error}^{-1}\left(M'[F] - y_{exp}\right)\right\}.$

M'[F] : model result y_{exp} : experimental data

 $\Sigma_{\text{error}}^{-1}$: the uncertainty covariance matrix, $\Sigma_{\text{error}} = \text{diag}[\sigma_1^2, \sigma_2^2, \dots]$ combining experimental, theoretical, and emulator uncertainties,

- Markov-Chain-Monte-Carlo (MCMC) sampling
 - To marginalize the values of F* at a fixed input x*, one in principle have to perform a path integral $p(F^*) = \int [\mathscr{D}F] \delta \left(F(x^*) F^* \right) P[F(x)] \qquad (P(x_1 | \mathbf{y}) = \int dx_2 \cdots dx_n P(\mathbf{x} | \mathbf{y}))$





Back-Up



Back-Up



Back-Up

