

# $p_T$ dispersion of inclusive jets in high-energy nuclear collisions

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**Shi-Yong Chen, Jan Yan, Wei Dai, Ben-Wei Zhang and En-Ke Wang** arXiv:2204.01211

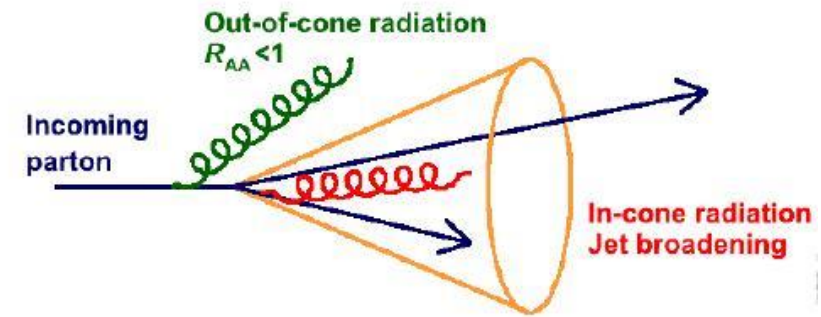
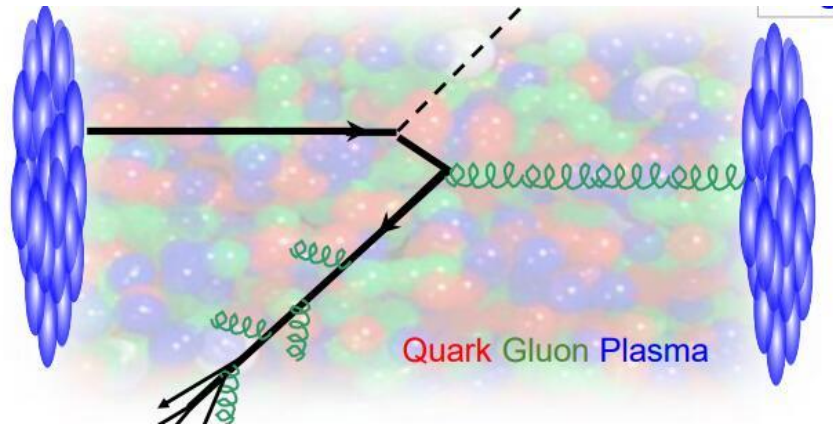
# Outline

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- Motivation
- Jet momentum dispersion ( $p_T D$ ) in pp and AA collisions
- Results and discussion
- Summary

# Motivation

Heavy-ion collisions: **Quark** **Gluon** Plasma



- Jet quenching is one of the most powerful hard probe to investigate QGP.
- High  $p_T$  hadron and full jet observables: productions and correlations.
- Jet substructures: jet shape, jet splitting functions, jet fragmentation functions, jet charge...

Xin-Nian Wang, M.Gyulassy, PRL68(1992)1480

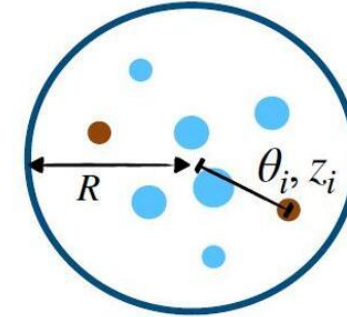
# Motivation: jet angularity

Generalized jet angularities defined as,

$$\lambda_{\alpha}^{\kappa} = \sum_{i \in \text{jet}} z_i^{\kappa} \theta_i^{\alpha}, \quad \left( z_i \equiv \frac{p_{Ti}}{\sum_{i \in \text{jet}} p_{Ti}}, \theta_i \equiv \frac{\Delta R_i}{R} \right)$$

( the transverse  
momentum of jet  
constituent  $i$  )

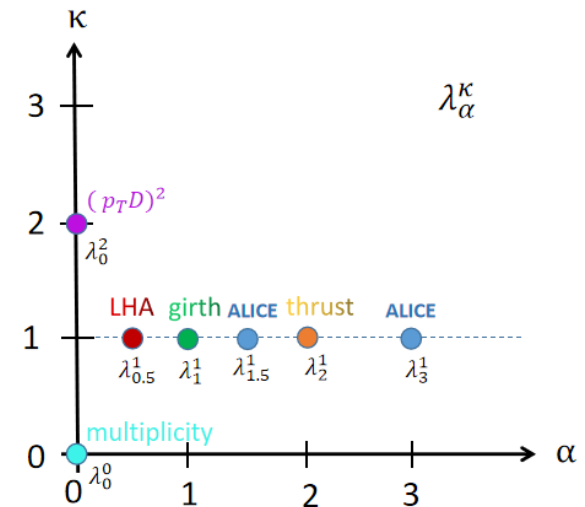
( the angle of the  $i$ th  
constituent relative  
to jet axis )



The exponents  $\kappa$  and  $\alpha$  probe different aspects of the jet fragmentation,

	( 1 , 1 )	$\Rightarrow$	girth
	( 2 , 0 )	$\Rightarrow$	$(p_T D)^2$
( $\kappa, \alpha$ )	( 0 , 0 )	$\Rightarrow$	hadron multiplicity
	( 1 , 2 )	$\Rightarrow$	jet-mass-squared divided by energy (thrust)
	( 1 , 0.5 )	$\Rightarrow$	Les Houche Angularity(LHA)

- How  $p_T D$  is modified by jet quenching?



[Larkoski, JDT, Waalewijn, 1408.3122], [For a more complete catalog, see Gallicchio, Schwartz, 1106.3076, 1211.7038]  
 [based on Berger, Kucs, Sterman, hep-ph/0303051]; [Ellis, Vermilion, Walsh, Hornig, Lee, 1001.0014],  
 [see also Larkoski, Salam, JDT, 1305.0007; Larkoski, Neill, JDT.1401.2158]

# $p_T$ dispersion in pp collisions

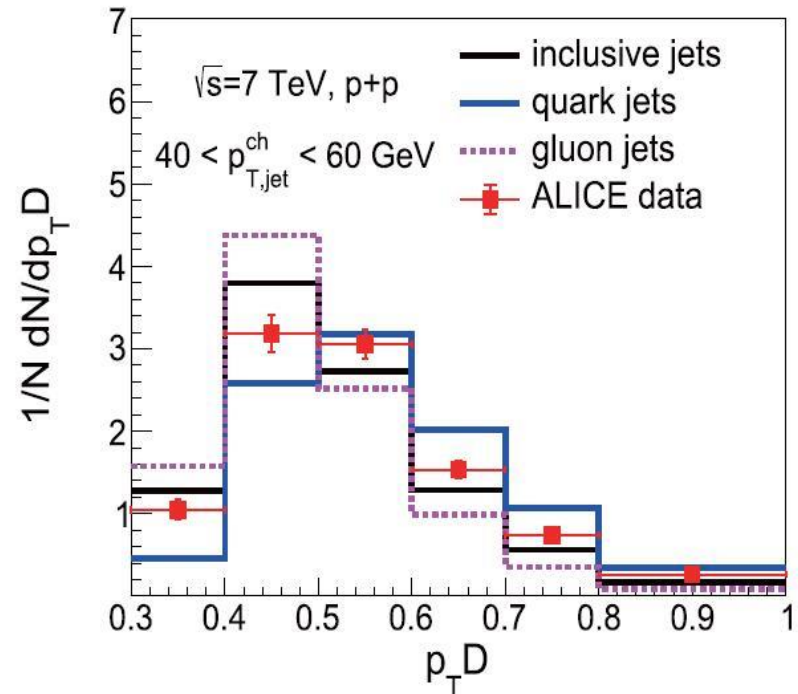
- The momentum dispersion  $p_T D$  is defined as, 
$$p_T D = \frac{\sqrt{\sum_{i \in \text{jet}} p_{T,i}^2}}{\sum_{i \in \text{jet}} p_{T,i}},$$
- Connect to how hard or soft of jet fragmentation.

e.g. in the extreme case of few constituents carrying a large fraction of the jet momentum,  $p_T D$  will be close to 1, while in the case of jets with a large number of constituents and softer momentum,  $p_T D$  would end up closer to 0.

- In pp collisions: POWHEG+PYTHIA

- Well consistent with ALICE data, provide solid pp baseline.

-  $p_T D$  distribution for gluon jets located in smaller  $p_T D$  region.



ALICE Collaboration, JHEP 1810,139(2018) [arXiv:1807.06854[nucl-ex]]  
S.Y. Chen, J.Yan, Wei Dai, Ben-Wei Zhang and En-Ke Wang. arXiv: 2204.01211.

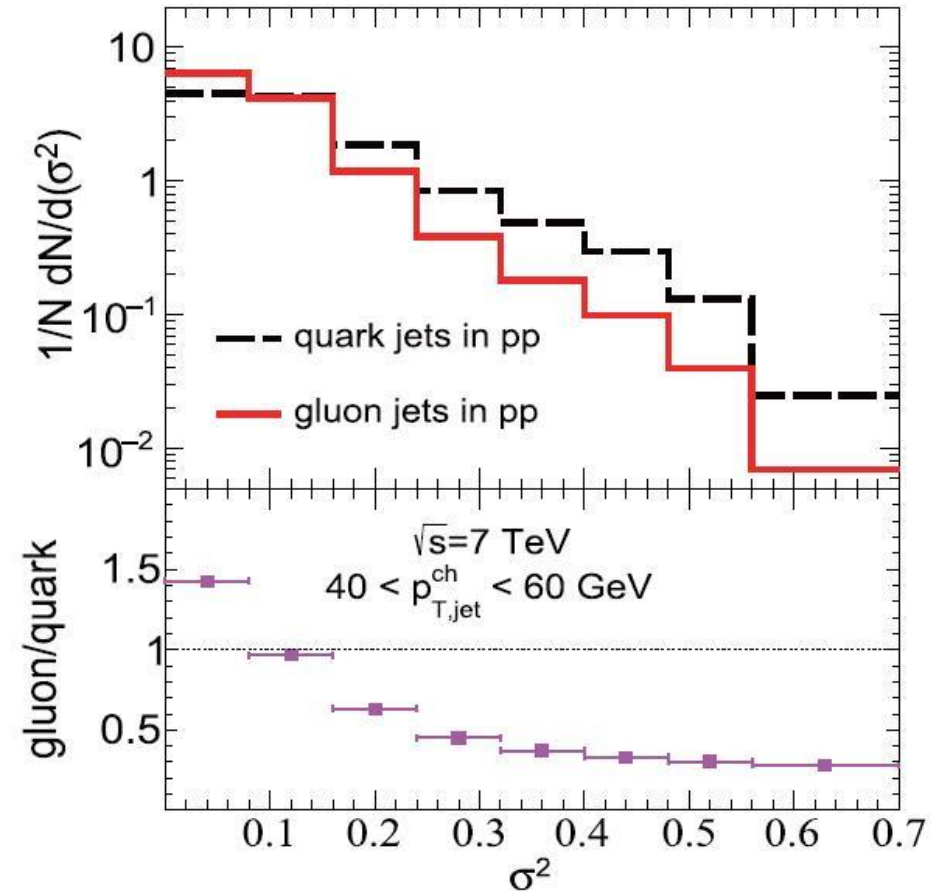
# $p_T$ dispersion in pp collisions

**Standard deviation**  $\delta = \frac{\sqrt{\sum(p_{Ti} - \langle p_{Ti} \rangle)^2}}{n \langle p_{Ti} \rangle}$

- Analytical connected with  $(p_T D)^2$  and  $1/n$ .

$$\begin{aligned} \delta^2 &= \frac{\sum(p_{Ti} - \langle p_{Ti} \rangle)^2}{n^2 \langle p_{Ti} \rangle^2} \\ &= \frac{\sum(p_{Ti}^2 - 2p_{Ti}\langle p_{Ti} \rangle + \langle p_{Ti} \rangle^2)}{n^2 \langle p_{Ti} \rangle^2} \\ &= (p_T D)^2 - \frac{1}{n} \end{aligned}$$

- Higher  $\delta$  means more  $p_{Ti}$  are generally far from the mean value  $\langle p_{Ti} \rangle$ , lower  $\delta$  indicates that more  $p_{Ti}$  are clustered close to  $\langle p_{Ti} \rangle$ .
- At the same  $p_T$ ,  $\delta$  of gluon jets are smaller than quark jets because of containing more fragment constituents.



# Jet quenching model

1. POWHEG+PYTHIA generate showered partonic event
2. parton initial position generated by Glauber model ( $r_0, T$ )
3. the parton suffer radiative energy loss during  $t_1, t_2$  by probability:

$$\langle N_g(t, \Delta t) \rangle = \Delta t \int dx d^2 k_\perp \frac{dN}{dx d^2 k_\perp} \quad P_{rad}(t, \Delta t) = 1 - e^{-\langle N_g \rangle}$$

$$\frac{dN}{dx d^2 k_\perp dt} = \frac{2\alpha_s P(x) \hat{q}}{\pi k_\perp^4} \sin^2\left(\frac{t-t_i}{2\tau_f}\right) \left(\frac{k_\perp^2}{k_\perp^2 + x^2 M^2}\right)^4$$

QGP transport coefficient:  $\hat{q}(\tau, r) = q_0 \frac{\rho^{QGP}(\tau, r)}{\rho^{QGP}(\tau_0, 0)} \frac{p^\mu u_\mu}{p^0}$

the spectrum is given by Higher-Twist,  $P(x)$  is splitting function

$$P_{q \rightarrow qg} = \frac{(1-x)(2-2x+x^2)}{x}$$

$$P_{g \rightarrow gg} = \frac{2(1-x+x^2)^3}{x(1-x)}$$

4. the number of radiated gluon is given by Poisson distribution

$$P(n) = \frac{\langle N_g \rangle^n}{n!} e^{-\langle N_g \rangle}$$

5. the collisional energy loss: Hard Thermal Loop calculation

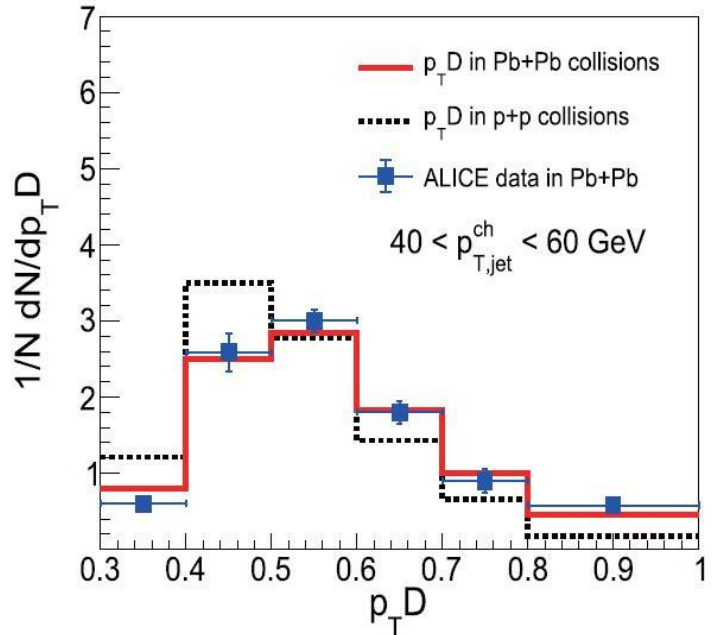
$$\frac{dE}{dz} = \frac{\alpha_s C_f m_D^2}{2} \ln \frac{\sqrt{ET}}{m_D}$$

6. the temperature is read from 2+1 D viscos hydro if  $T_i < T_C$ , escape QGP

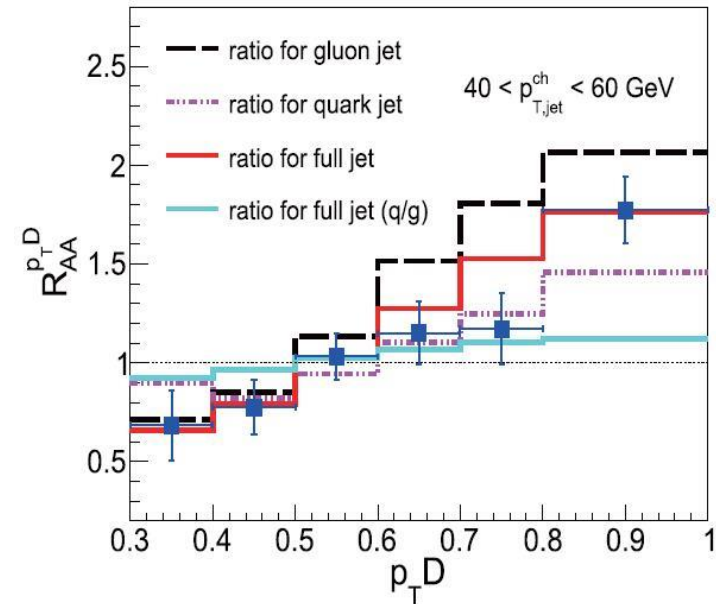
7. Perform hadronization with pythia

Xiao-feng Guo , Xin-Nian Wang Phys. Rev. Lett. 85 (2000) 3591-3594  
 Ben-Wei Zhang , Xin-Nian Wang Phys. Rev. Lett. 93 (2004) 072301  
 A. Majumder, Phys.Rev. D85(2012)014023  
 W.T. Deng and X.N Wang, Phys.Rev.C 81(2010)024902

# $p_T$ dispersion in PbPb collisions



$$R_{AA}^{p_T D} = \frac{1}{N_{AA}} \frac{dN_{AA}}{dp_T D} / \frac{1}{N_{pp}} \frac{dN_{pp}}{dp_T D}$$



- In Pb+Pb collisions: well consistent with ALICE data. Distribution of  $p_T D$  shifted to higher value.
- $R_{AA}^{p_T D} < 1$  in lower  $p_T D$  region and  $R_{AA}^{p_T D} > 1$  in higher  $p_T D$  region.  $R_{AA}^{p_T D}$  for gluon jets is much stronger than quark jets.
- What causes this?
  - Parton energy loss
  - q/g fraction alteration

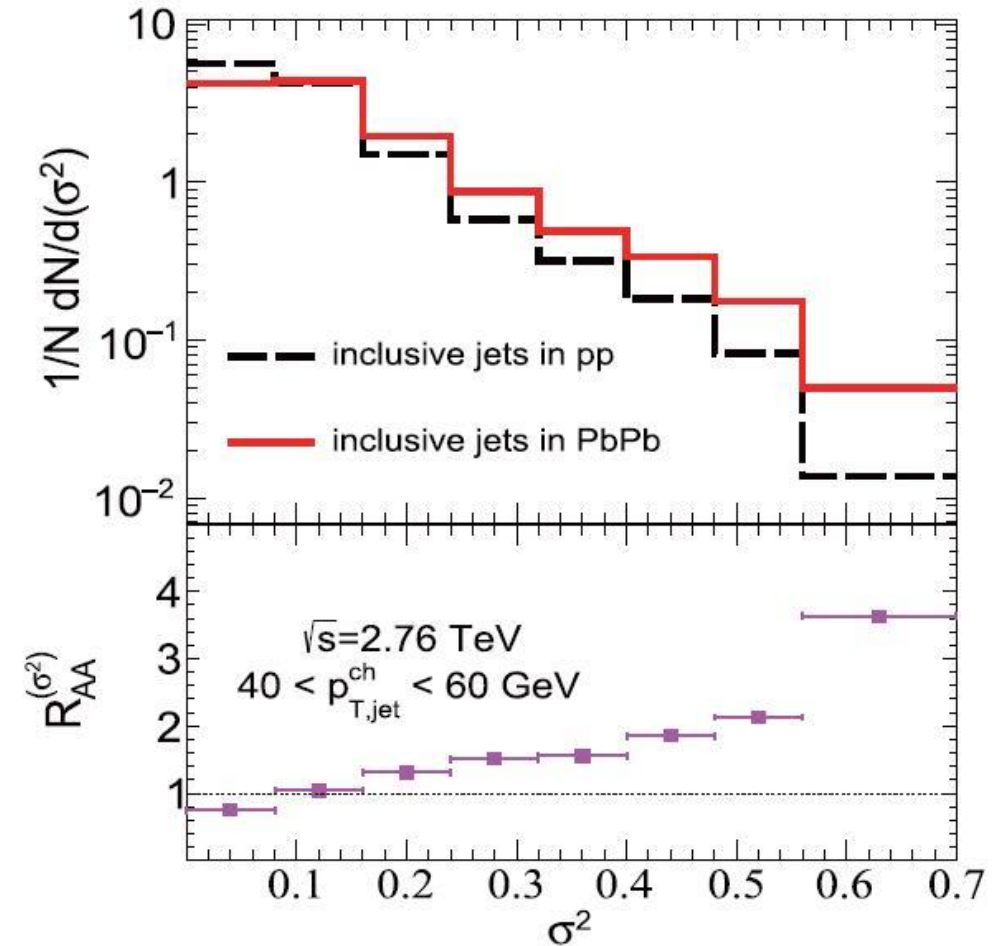


# $p_T$ dispersion in PbPb collisions

$$(p_T D)^2 = \delta^2 + \frac{1}{n}$$

- smaller  $\langle n \rangle$  larger  $1/n$ . ( $\overline{n_{pp}} = 6.74$ ,  $\overline{n_{PbPb}} = 6.52$ )
- $\sigma^2$  shift to larger value region, means more  $p_T$  of jet constituents stay further away from the mean value.

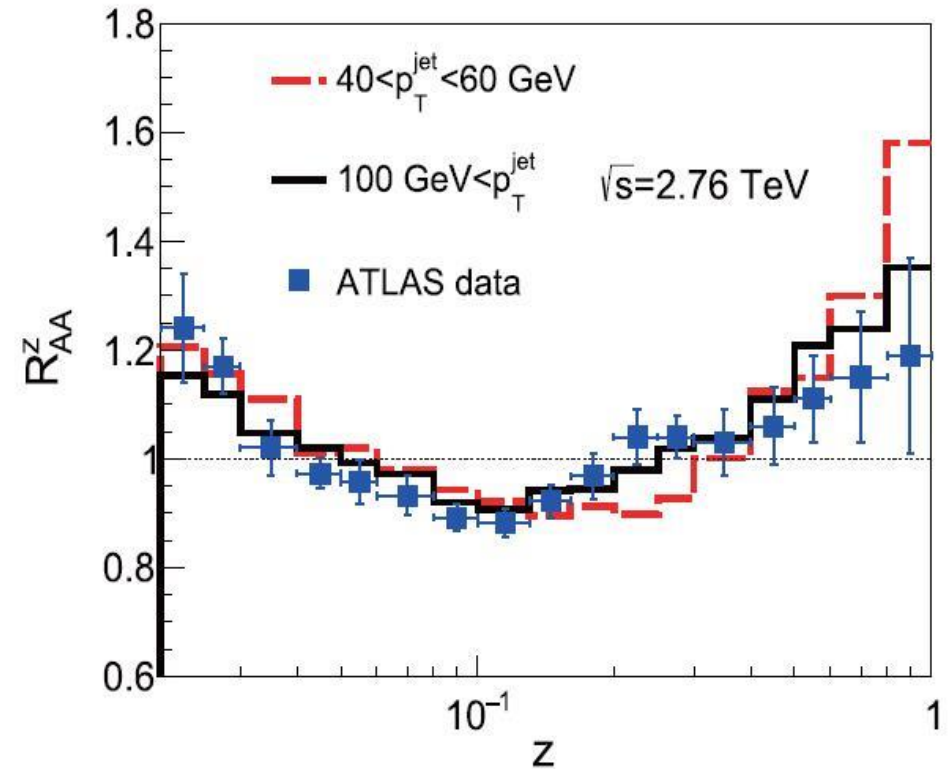
$$\sigma^2 \uparrow \quad 1/n \uparrow \quad \longrightarrow \quad (p_T D)^2 \uparrow$$



# $p_T$ dispersion in PbPb collisions

- Momentum fraction  $z$  : fragmentation function, related with  $p_{T,i}$  only.
- $R_{AA}^z > 1$  when  $0.02 < z < 0.05$  and  $0.3 < z < 1$ ;  
 $R_{AA}^z > 1$  when  $0.05 < z < 0.3$ .

means more constituents of  $p_{T,i}$  stay further away from the mean value.



# $p_T$ dispersion in PbPb collisions

## Soft-drop:

- First reclustered using the Cambridge-Aachen(C/A) algorithm.
- Then declustered in the reverse order by dropping the softer branch until two hard branches are found to satisfy the following condition,

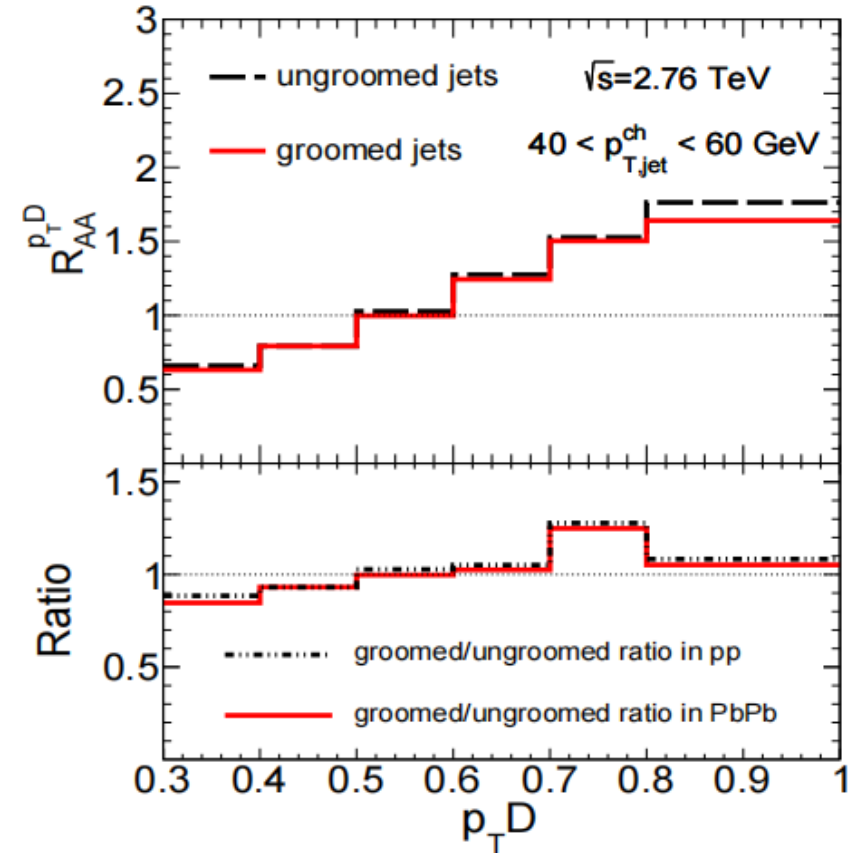
$$\frac{\min(p_{T1}, p_{T2})}{p_{T1} + p_{T2}} \equiv z_g > z_{cut} \left(\frac{\Delta R}{R}\right)^\beta$$

$$z_{cut}=0.1, \quad \beta=0$$

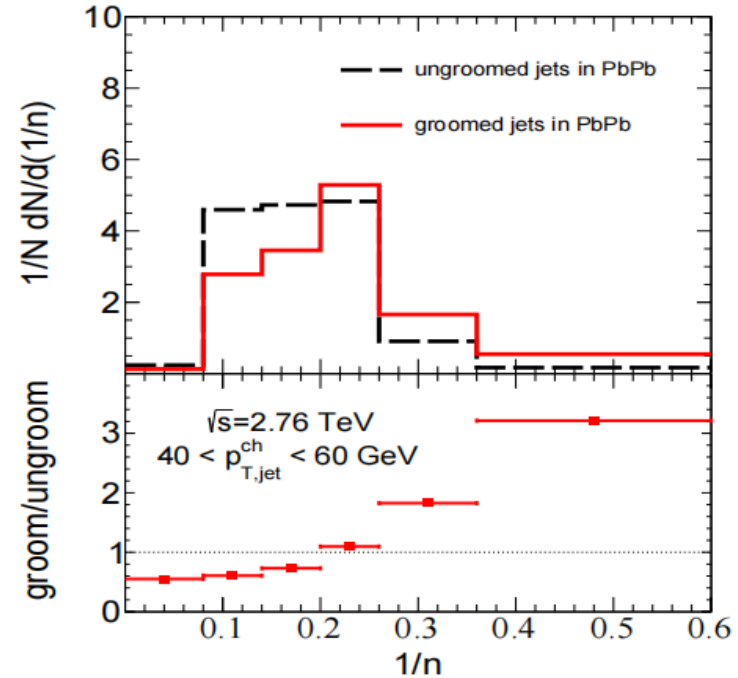
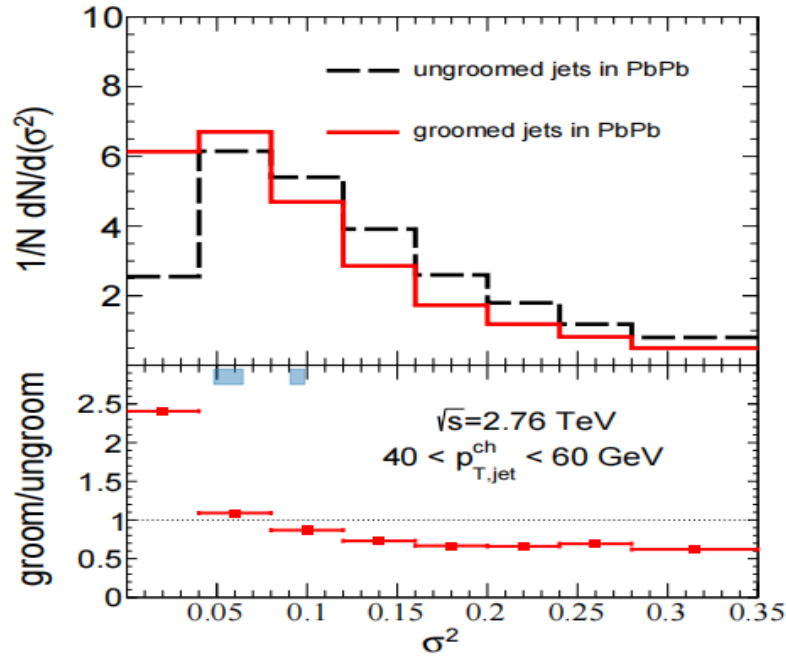
## Groomed vs ungroomed:

- medium modification **reduced**.

How does the grooming procedure modify  $p_T D$  distribution?



# $p_T$ dispersion in PbPb collisions



$$(p_T D)^2 = \delta^2 + \frac{1}{n}$$

- Grooming process will enhance the value of  $1/n$  and meanwhile lead to lower  $\delta$ .
- The correction of  $1/n$  are more pronounced.

# Summary

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- $p_T D$  distribution shifted to higher  $p_T D$  value after jet quenching.
- Medium modification of  $p_T D$  is caused by both parton redistribution (both  $\delta^2$  and  $1/n$  enhanced) and alteration of overall quark/gluon fraction.
- The trend of groomed  $R_{AA}^{p_T D}$  is consistent with ungroomed, grooming procedure would weaken  $p_T D$  nuclear modification.

Thank you for your attention !