



遼寧師範大學
Liaoning Normal University

heavy flavor molecules

Kan Chen

Peking University

Collaborators: Rui Chen (Hunan Normal U.), Lu Meng (Ruhr U.), Bo Wang (Hebei U.), and Shi-Lin Zhu (Peking U.)

Eur.Phys.J.C 82 (2022) 7, 581

Outline

- Motivation
- Theoretical framework
- Numerical results
- Summary

Motivation

Discovery of the P_c states

State	Mass (MeV)	Width (MeV)
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	$9.8 \pm 2.7^{+3.7}_{-4.5}$
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	$20.6 \pm 4.9^{+8.7}_{-10.1}$
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	$6.4 \pm 2.0^{+5.7}_{-1.9}$

Experiment

Phys. Rev. Lett. 122, 222001 (2019)

Phys. Rev. Lett. 115, 072001 (2015)

Phys. Rev. Lett. 117, 082002 (2016)

Theoretical interpretation

R. Chen, et al., Phys. Rev. D 100, 011502 (2019)

M. Z. Liu, et.al., Phys. Rev. Lett. 122, 242001 (2019)

J. He, Eur. Phys. J. C 79, 393 (2019)

C. W. Xiao, J. Nieves and E. Oset, Phys. Rev. D 100, no.1, 014021 (2019)

L. Meng, B. Wang, G. J. Wang and S. L. Zhu, Phys. Rev. D 100, 014031 (2019)

M. Pavon Valderrama, Phys. Rev. D 100, 094028 (2019)

H. X. Chen, W. Chen and S. L. Zhu, Phys. Rev. D 100, 051501 (2019)

T. J. Burns and E. S. Swanson, Phys. Rev. D 100, 114033 (2019)

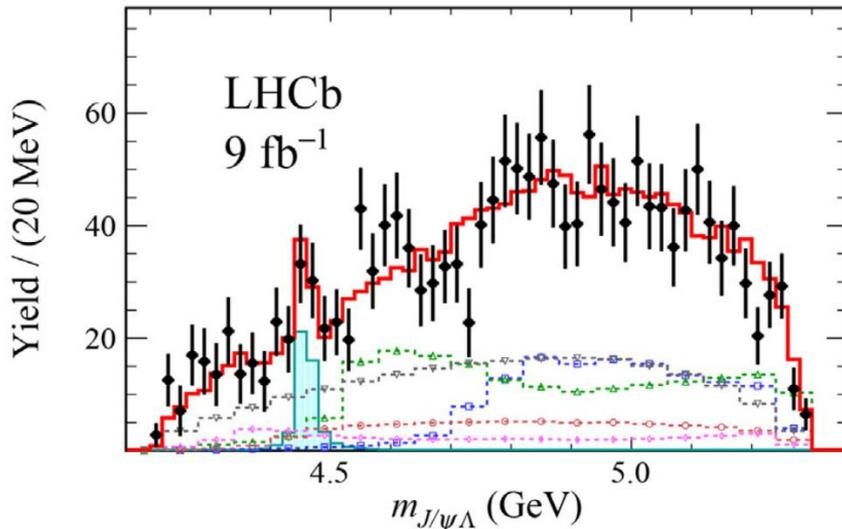
M. L. Du, et. Al., Phys. Rev. Lett. 124, 072001 (2020)

B. Wang, L. Meng and S. L. Zhu, JHEP 11, 108 (2019)

Y. Yamaguchi, et. Al., Phys. Rev. D 101, no.9, 091502 (2020)

Motivation

Discovery of the P_{cs} states



Sci. Bull. 66, 1278-1287 (2021)

$M: 4458.8 \pm 2.9 \text{ MeV}, \Gamma: 17.3 \pm 6.5 \text{ MeV}$

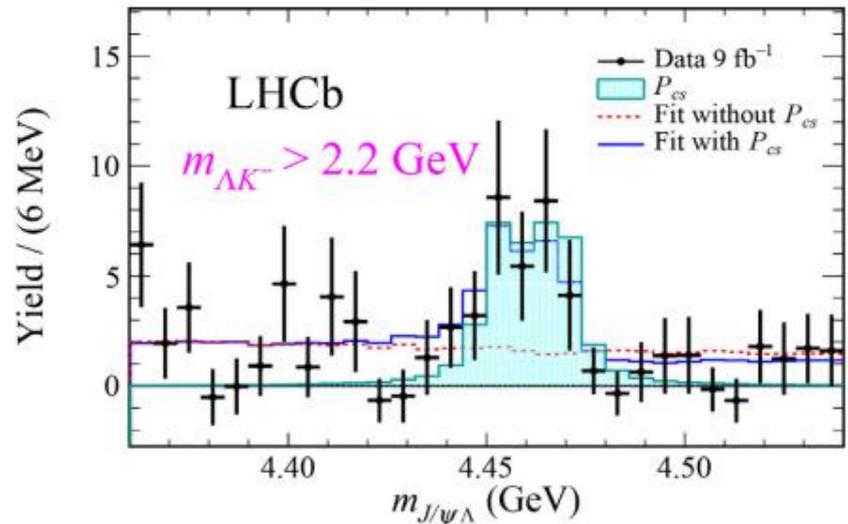
Wu J-J, Molina R, Oset E, et al. Phys Rev Lett 2010;105:232001.

Chen R, He J, Liu X. Chin Phys C 2017;41:103105.

Santopinto E, Giachino A, Phys Rev D 2017;96:014014.

Shen C-W, Wu J-J, Zou B-S. Phys Rev D

2019;100:056006.



A **two peak** hypothesis is also tested:

$M=4454.9 \pm 2.7 \text{ MeV}, \Gamma=7.5 \pm 9.7 \text{ MeV}$

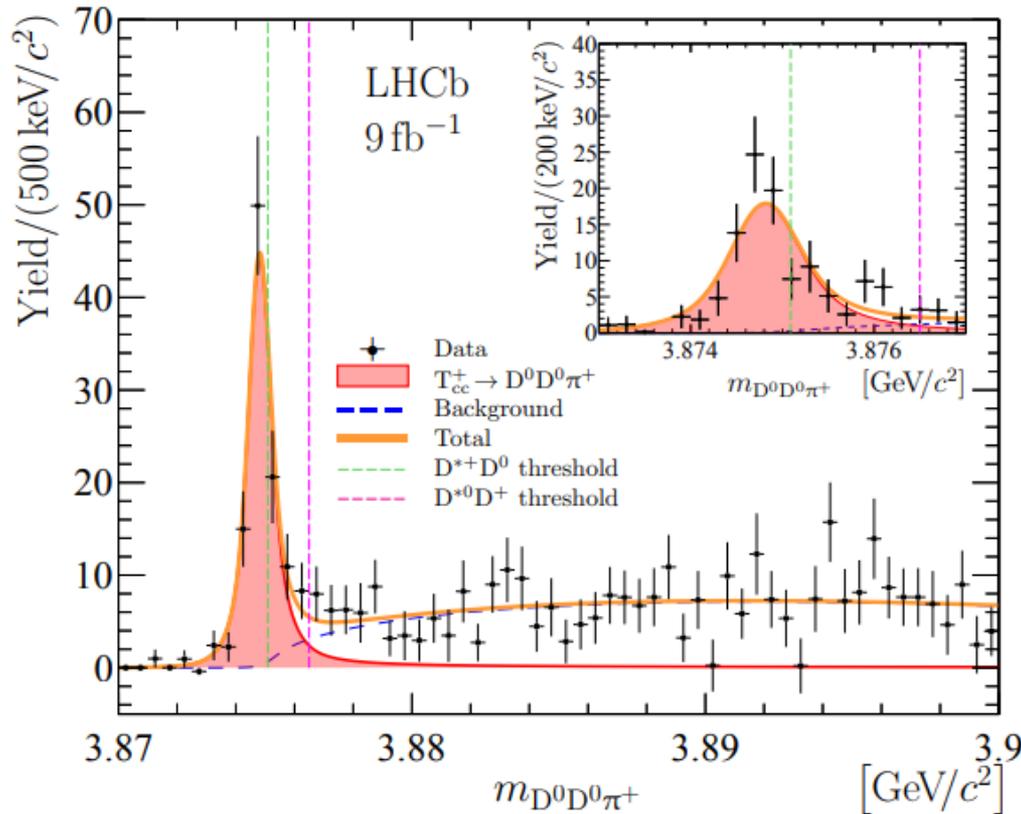
$M=4467.8 \pm 3.7 \text{ MeV}, \Gamma=5.2 \pm 5.3 \text{ MeV}$

Xiao C-W, Nieves J, Oset E. Phys Lett B 2019;799:135051.

Wang B, Meng L, Zhu S-L. Phys Rev D 2020;101:034018

Chen H-X, Geng L-S, Liang W-H, et al.. Phys Rev C 2016;93:065203.

Discovery of the T_{cc} state



Mass: 3874.8 MeV

N. Li, Z. F. Sun, X. Liu and S. L. Zhu, Chin. Phys. Lett. 38, 092001 (2021)
L. Meng, G. J. Wang, B. Wang and S. L. Zhu, Phys. Rev. D 104, 051502 (2021)
X. K. Dong, F. K. Guo and B. S. Zou, Commun. Theor. Phys. 73, 125201 (2021)
M. J. Yan and M. P. Valderrama, Phys.Rev.D 105 (2022) 1, 014007.
L. Y. Dai, X. Sun, X. W. Kang, A. P. Szczepaniak and J. S. Yu, Phys.Rev.D 105 (2022) 5, L051507.
V. Baru, X. K. Dong, M. L. Du, et. al, Phys.Lett.B 833 (2022) 137290.
M. L. Du, V. Baru, X. K. Dong, et. al, Phys.Rev.D 105 (2022) 1, 014024
L. R. Dai, R. Molina and E. Oset, Phys.Rev.D 105 (2022) 1, 016029...

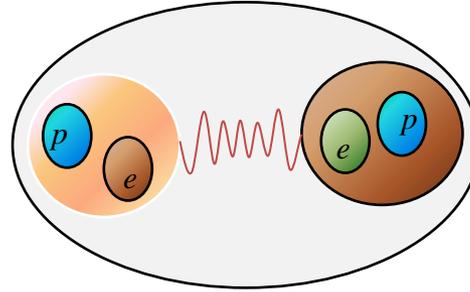
Nature Phys. 18 (2022) 7, 751-754

Nature Commun. 13 (2022) 1, 3351

Motivation

Hydrogen molecule

QED

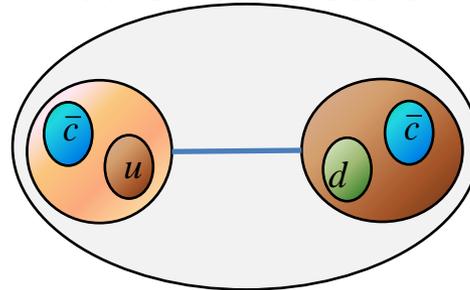


Coulomb potential

Hadronic Molecule

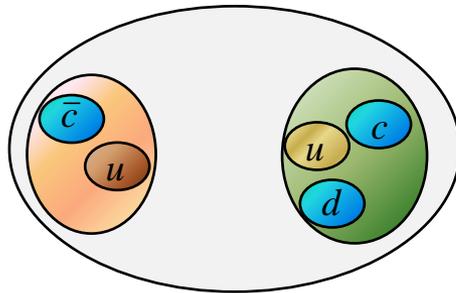
QCD

T_{cc}

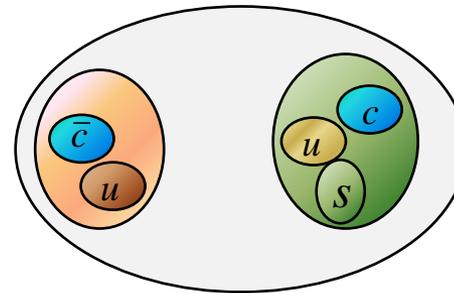


Boson exchange potential

P_c



P_{cs}

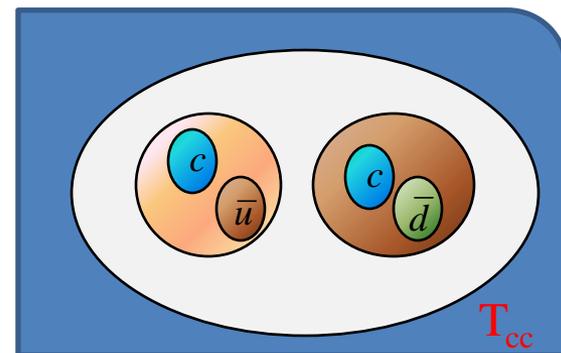
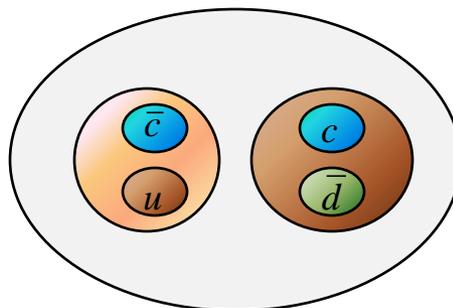


Motivation

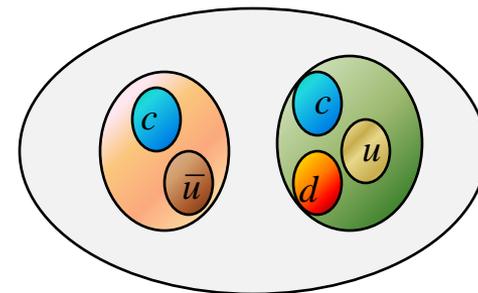
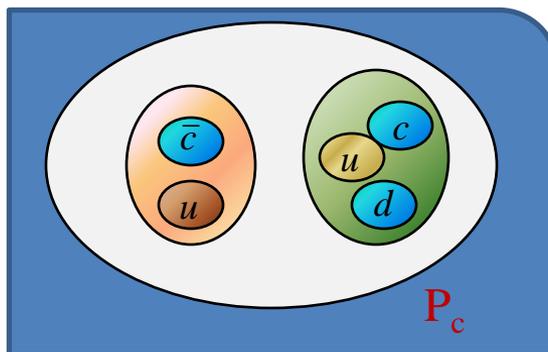
Hidden charm

Open charm

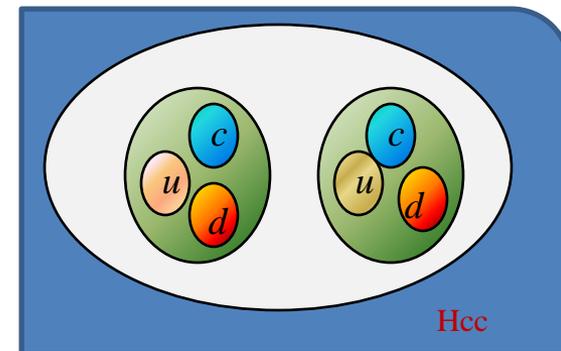
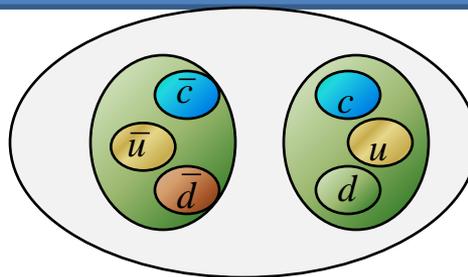
Meson-meson molecular states:



Meson-baryon molecular states:



Baryon-baryon molecular states:



Considered systems

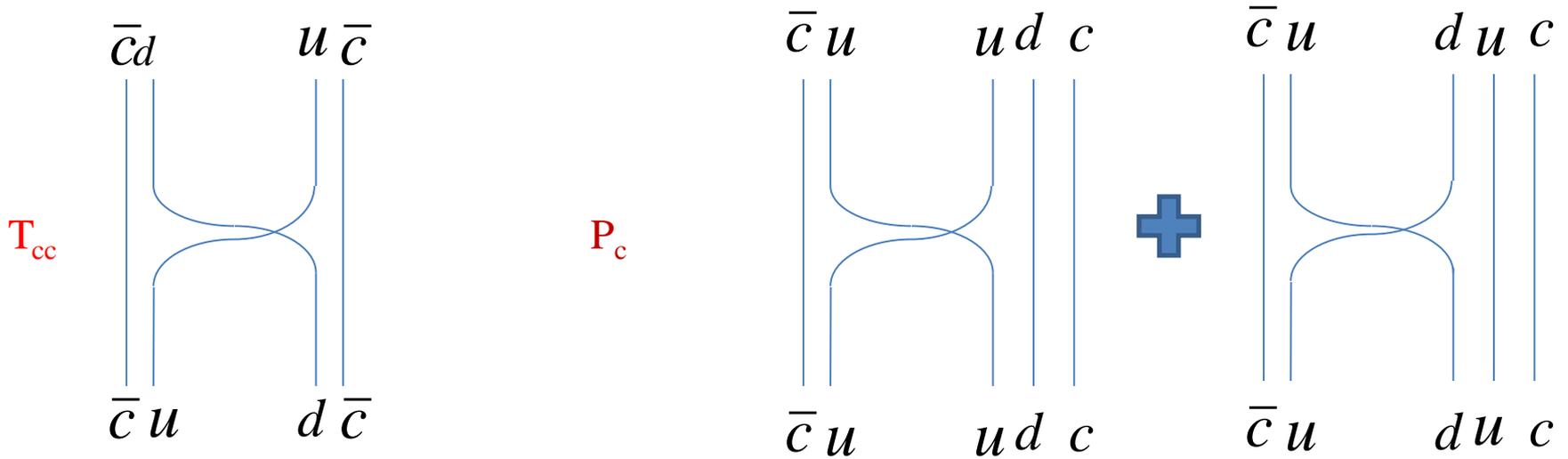
Meson-meson	$[\bar{D}\bar{D}]_0^1$	$[\bar{D}\bar{D}^*]_1^{0,1}$	$[\bar{D}^*\bar{D}^*]_{0,2}^1$
	$[\bar{D}^*\bar{D}^*]_1^0$		
Baryon-meson	$[\Lambda_c\bar{D}]_{\frac{1}{2}}^{\frac{1}{2}}$	$[\Lambda_c\bar{D}^*]_{\frac{1}{2},\frac{3}{2}}^{\frac{1}{2}}$	$[\Sigma_c\bar{D}]_{\frac{1}{2}}^{\frac{1}{2},\frac{3}{2}}$
	$[\Sigma_c\bar{D}^*]_{\frac{1}{2},\frac{3}{2}}^{\frac{1}{2},\frac{3}{2}}$	$[\Sigma_c^*\bar{D}]_{\frac{1}{2},\frac{3}{2}}^{\frac{1}{2},\frac{3}{2}}$	$[\Sigma_c^*\bar{D}^*]_{\frac{1}{2},\frac{3}{2},\frac{5}{2}}^{\frac{1}{2},\frac{3}{2}}$
	$[\Xi_c\bar{D}]_{\frac{1}{2}}^{0,1}$	$[\Xi_c\bar{D}^*]_{\frac{1}{2},\frac{3}{2}}^{0,1}$	$[\Xi_c'\bar{D}]_{\frac{1}{2}}^{0,1}$
	$[\Xi_c'\bar{D}^*]_{\frac{1}{2},\frac{3}{2}}^{0,1}$	$[\Xi_c^*\bar{D}]_{\frac{3}{2}}^{0,1}$	$[\Xi_c^*\bar{D}^*]_{\frac{1}{2},\frac{3}{2},\frac{5}{2}}^{0,1}$
	$[\Lambda_c\Lambda_c]_0^0$	$[\Lambda_c\Sigma_c]_{0,1}^1$	$[\Sigma_c\Sigma_c]_0^{0,2}$
	$[\Sigma_c\Sigma_c]_1^1$	$[\Lambda_c\Sigma_c^*]_{1,2}^1$	$[\Sigma_c\Sigma_c^*]_{1,2}^{0,1,2}$
Baryon-baryon	$[\Sigma_c^*\Sigma_c^*]_{1,3}^1$	$[\Sigma_c^*\Sigma_c^*]_{0,2}^{0,2}$	$[\Xi_c\Xi_c]_0^1$
	$[\Xi_c\Xi_c]_1^0$	$[\Xi_c\Xi_c']_{0,1}^{0,1}$	$[\Xi_c\Xi_c^*]_{1,2}^{0,1}$
	$[\Xi_c'\Xi_c']_0^1$	$[\Xi_c'\Xi_c']_1^0$	$[\Xi_c'\Xi_c^*]_{1,2}^{0,1}$
	$[\Xi_c^*\Xi_c^*]_{1,3}^0$	$[\Xi_c^*\Xi_c^*]_{0,2}^1$	

For identical particles
(fermion or boson):

$$L+S_{\text{tot}}+I_{\text{tot}}+2i=\text{Even number}$$

Have vanish
contributions from
strang light mesons!

Theoretical framework



S-wave
interaction:

$$\mathcal{L} = g_s \bar{q} \mathcal{S} q + g_a \bar{q} \gamma_\mu \gamma^5 \mathcal{A}^\mu q, \quad \mathcal{S} = \mathcal{S}_3 \lambda^i + \mathcal{S}_1 \lambda^8,$$

$$q = (u, d, s) \quad \mathcal{A}^\mu = \mathcal{A}_3^\mu \lambda^i + \mathcal{A}_1^\mu \lambda^8,$$

$$V_{qq} = \tilde{g}_s (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) + \tilde{g}_a (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2.$$

$$V_{[H_1 H_2]_J^I} = \langle [H_1 H_2]_J^I | V_{qq} | [H_1 H_2]_J^I \rangle$$

Solvable Lippmann-Schwinger equation (LSE)

$$V(p, p') = V_{[H_1 H_2]_J^I} \Theta(\Lambda - p) \Theta(\Lambda - p')$$

$$T(p', p) = V(p', p) + \int \frac{d^3 q}{(2\pi)^3} \frac{V(p', q) T(q, p)}{E - q^2 / 2m_\mu + i\varepsilon}$$

$$T(p', p) = \beta(E) \Theta(\Lambda - p') \Theta(\Lambda - p)$$

$$\beta(E) = \frac{V_{[H_1 H_2]_J^I}}{1 - V_{[H_1 H_2]_J^I} G}$$

$$G = \frac{m_\mu}{\pi^2} \left[-\Lambda + k \tan^{-1} \left(\frac{\Lambda}{k} \right) \right] \quad k = \sqrt{-2m_\mu E}$$

Theoretical framework

$$V_{qq} = \tilde{g}_s (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) + \tilde{g}_a (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$

Potentials:

$$V_{P_c}(4312) = -\frac{10}{3} \tilde{g}_s$$

$$V_{P_c}(4440) = -\frac{10}{3} \tilde{g}_s + \frac{40}{9} \tilde{g}_a$$

$$V_{P_c}(4457) = -\frac{10}{3} \tilde{g}_s - \frac{20}{9} \tilde{g}_a$$

Assignments:

$$[\Sigma_c \bar{D}]_{1/2}^{1/2}$$

$$[\Sigma_c \bar{D}^*]_{1/2}^{1/2}$$

$$[\Sigma_c \bar{D}^*]_{3/2}^{1/2}$$

Three solved
parameters:

$$\tilde{g}_s = 11.739 \text{ GeV}^{-2}$$

$$\tilde{g}_a = -2.860 \text{ GeV}^{-2}$$

$$\Lambda = 0.409 \text{ GeV}$$

Reproduce the experimental masses

	Mass (Expt.)	BE (Expt.)	Mass (Our)	BE (Our)
$T_{cc}(3875)^+$	3874.8	-1.0	3874.5	-1.8
$P_c(4312)^+$	$4311.9 \pm 0.7^{+6.8}_{-0.6}$	-8.9 (input)	4311.9	-8.9
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	-6.2	4376.2	-9.1
$P_c(4440)^+$	$4440.3 \pm 1.3^{+4.1}_{-4.7}$	-21.8 (input)	4440.2	-21.8
$P_c(4457)^+$	$4457.3 \pm 0.6^{+4.1}_{-1.7}$	-4.8 (input)	4457.3	-4.8
$P_{cs}(4459)^0$	$4458.8 \pm 2.9^{+4.7}_{-1.1}$	-19.7	4468.1	-10.0

Give a **good** description to the masses of the observed states.

Neglect the corrections from the heavy degrees of freedom:
fairly good approximation.

Interchange the assignments of $P_c(4440)$ and $P_c(4457)$ **can not** reproduce the masses of T_{cc} and P_{cs} .

Other predictions

System	$[\bar{D}^* \bar{D}^*]_1^0$	$[\Sigma_c^* \bar{D}^*]_{\frac{1}{2}}^{\frac{1}{2}}$	$[\Sigma_c^* \bar{D}^*]_{\frac{3}{2}}^{\frac{1}{2}}$	$[\Sigma_c^* \bar{D}^*]_{\frac{5}{2}}^{\frac{1}{2}}$	$[\Xi_c \bar{D}]_{\frac{1}{2}}^0$	$[\Xi_c \bar{D}^*]_{\frac{3}{2}}^0$	$[\Xi_c' \bar{D}]_{\frac{1}{2}}^0$	$[\Xi_c' \bar{D}^*]_{\frac{1}{2}}^0$
Mass	$4009.7^{+5.9}_{-2.6}$	$4501.3^{+15.7}_{-5.9}$	$4510.1^{+10.6}_{-4.2}$	$4523.8^{+2.7}_{-1.4}$	$4327.7^{+6.8}_{-2.8}$	$4468.1^{+7.3}_{-3.0}$	$4436.7^{+7.0}_{-2.9}$	$4564.9^{+14.1}_{-5.3}$
BE	$-7.4^{+5.9}_{-2.6}$	$-25.4^{+15.7}_{-5.9}$	$-15.9^{+10.6}_{-4.2}$	$-2.9^{+2.7}_{-1.4}$	$-8.9^{+6.8}_{-2.8}$	$-10.0^{+7.3}_{-3.0}$	$-9.4^{+7.0}_{-2.9}$	$-22.5^{+14.1}_{-5.3}$
System	$[\Xi_c' \bar{D}^*]_{\frac{3}{2}}^0$	$[\Xi_c^* \bar{D}]_{\frac{3}{2}}^0$	$[\Xi_c^* \bar{D}^*]_{\frac{1}{2}}^0$	$[\Xi_c^* \bar{D}^*]_{\frac{3}{2}}^0$	$[\Xi_c^* \bar{D}^*]_{\frac{5}{2}}^0$	$[\Sigma_c \Sigma_c]_0^0$	$[\Sigma_c \Sigma_c]_1^1$	$[\Sigma_c \Sigma_c^*]_1^0$
Mass	$4582.1^{+4.4}_{-1.9}$	$4503.6^{+7.1}_{-3.0}$	$4628.5^{+16.0}_{-6.0}$	$4638.0^{+11.0}_{-4.2}$	$4651.3^{+2.9}_{-1.4}$	$4825.4^{+43.1}_{-15.2}$	$4903.9^{+2.9}_{-1.5}$	$4894.3^{+41.0}_{-14.5}$
BE	$-5.2^{+4.4}_{-1.9}$	$-9.6^{+7.1}_{-3.0}$	$-26.0^{+16.0}_{-6.0}$	$-16.5^{+11.0}_{-4.2}$	$-3.2^{+2.9}_{-1.4}$	$-81.7^{+43.1}_{-15.2}$	$-3.2^{+2.9}_{-1.5}$	$-77.4^{+41.0}_{-14.5}$
System	$[\Sigma_c \Sigma_c^*]_2^0$	$[\Sigma_c \Sigma_c^*]_1^1$	$[\Sigma_c \Sigma_c^*]_2^1$	$[\Sigma_c^* \Sigma_c^*]_1^1$	$[\Sigma_c^* \Sigma_c^*]_3^1$	$[\Sigma_c^* \Sigma_c^*]_0^0$	$[\Sigma_c^* \Sigma_c^*]_2^0$	$[\Xi_c \Xi_c]_1^0$
Mass	$4931.9^{+22.6}_{-8.2}$	$4958.4^{+9.0}_{-3.5}$	$4969.3^{+2.2}_{-1.2}$	$5021.9^{+9.6}_{-3.8}$	$5035.1^{+*}_{-0.8}$	$4946.5^{+46.9}_{-16.5}$	$4996.1^{+22.8}_{-8.3}$	$4933.1^{+4.6}_{-2.1}$
BE	$-39.8^{+22.6}_{-8.2}$	$-13.3^{+9.0}_{-3.5}$	$-2.4^{+2.2}_{-1.2}$	$-14.4^{+9.6}_{-3.8}$	$-1.2^{+*}_{-0.8}$	$-89.8^{+46.9}_{-16.5}$	$-40.1^{+22.8}_{-8.3}$	$-5.8^{+4.6}_{-2.1}$
System	$[\Xi_c \Xi_c']_{0,1}^0$	$[\Xi_c \Xi_c^*]_{1,2}^0$	$[\Xi_c' \Xi_c']_1^0$	$[\Xi_c' \Xi_c^*]_1^0$	$[\Xi_c' \Xi_c^*]_2^0$	$[\Xi_c^* \Xi_c^*]_1^0$	$[\Xi_c^* \Xi_c^*]_3^0$	
Mass	$5042.1^{+4.9}_{-2.1}$	$5109.0^{+5.0}_{-2.1}$	$5153.6^{+3.4}_{-1.6}$	$5210.3^{+9.6}_{-3.7}$	$5221.7^{+2.8}_{-1.3}$	$5276.4^{+10.1}_{-3.9}$	$5290.3^{+0.0}_{-1.0}$	
BE	$-6.2^{+4.9}_{-2.1}$	$-6.4^{+5.0}_{-2.1}$	$-4.0^{+3.4}_{-1.6}$	$-14.4^{+9.6}_{-3.7}$	$-3.0^{+2.8}_{-1.3}$	$-15.6^{+10.1}_{-3.9}$	$-1.7^{+0.0}_{-1.0}$	

$$V_{qq} = \tilde{g}_s (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) + \tilde{g}_a (\lambda_1^8 \lambda_2^8 + \lambda_1^i \lambda_2^i) \boldsymbol{\sigma}_1 \cdot \boldsymbol{\sigma}_2$$

Isospin criterion: $\boldsymbol{\tau}_1 \cdot \boldsymbol{\tau}_2 = 2 [I(I + 1) - I_1(I_1 + 1) - I_2(I_2 + 1)]$

Other predictions

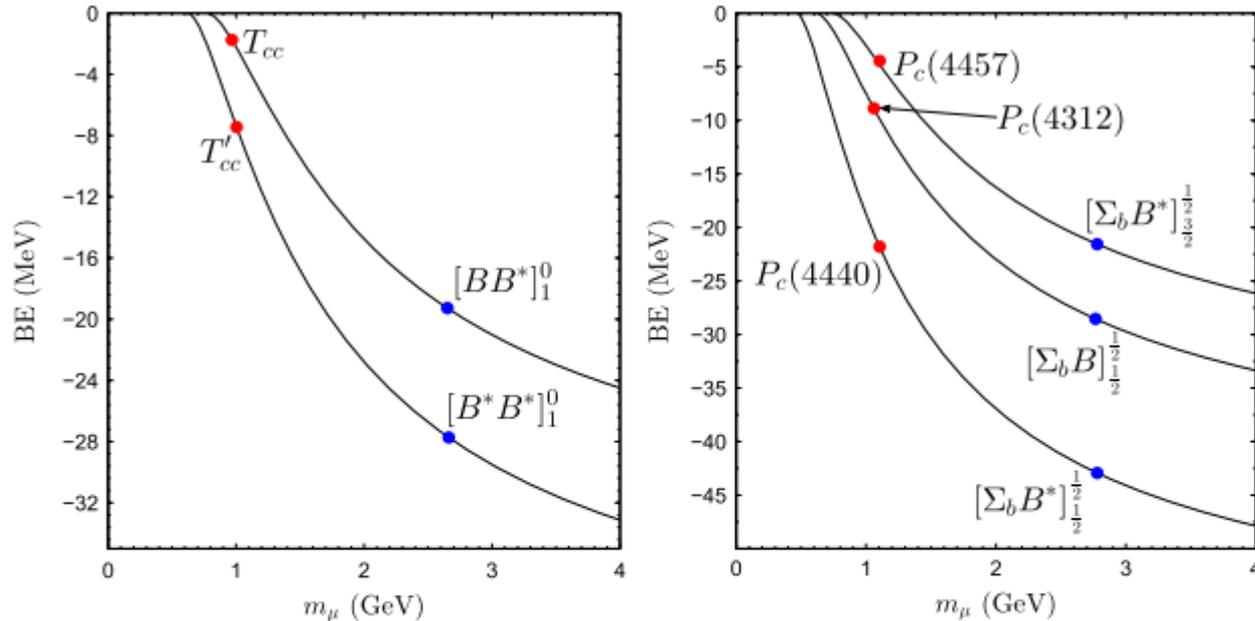


Fig. 1 The variation of binding energies for the T_{cc}^+ , $T'_{cc}+$, $P_c(4312)$, $P_c(4440)$, and $P_c(4457)$ states as their reduced masses increase. At $m_Q = m_b$, we have their bottom partners T_{bb}^- , T'_{bb}^- , $[\Sigma_b B]_{1/2}^{1/2}$, $[\Sigma_b B^*]_{1/2}^{1/2}$, and $[\Sigma_b B^*]_{3/2}^{1/2}$, respectively

Summary

- 1. Propose a toy model to understand the interactions of the P_c , P_{cs} , and T_{cc} states.
- 2. Reproduce the experimental masses of the observed molecular candidates.
- 3. **Predict** some molecules in M-M, M-B, and B-B systems.
- 4. Our model suggests an **isospin criterion** to the heavy flavor molecular states.

A scenic landscape featuring a calm lake in the foreground that perfectly reflects the sky and the surrounding environment. The middle ground is filled with a variety of trees, some with vibrant yellow and orange autumn foliage, and others that are dark green. In the background, a range of rugged mountains is visible, with several peaks covered in snow. The sky is a clear, bright blue, dotted with soft, white clouds. The overall atmosphere is peaceful and picturesque.

Thanks for your attention!