



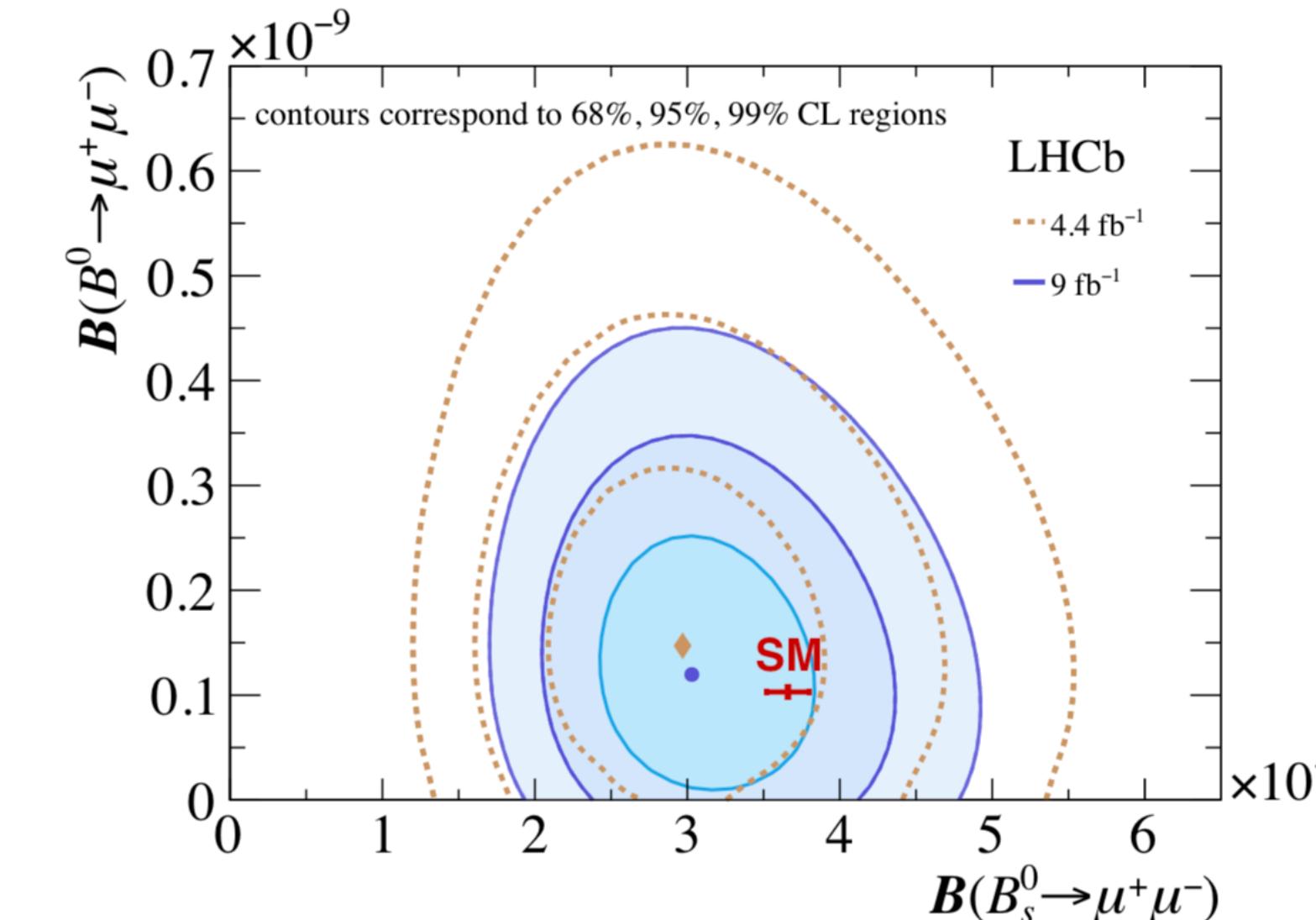
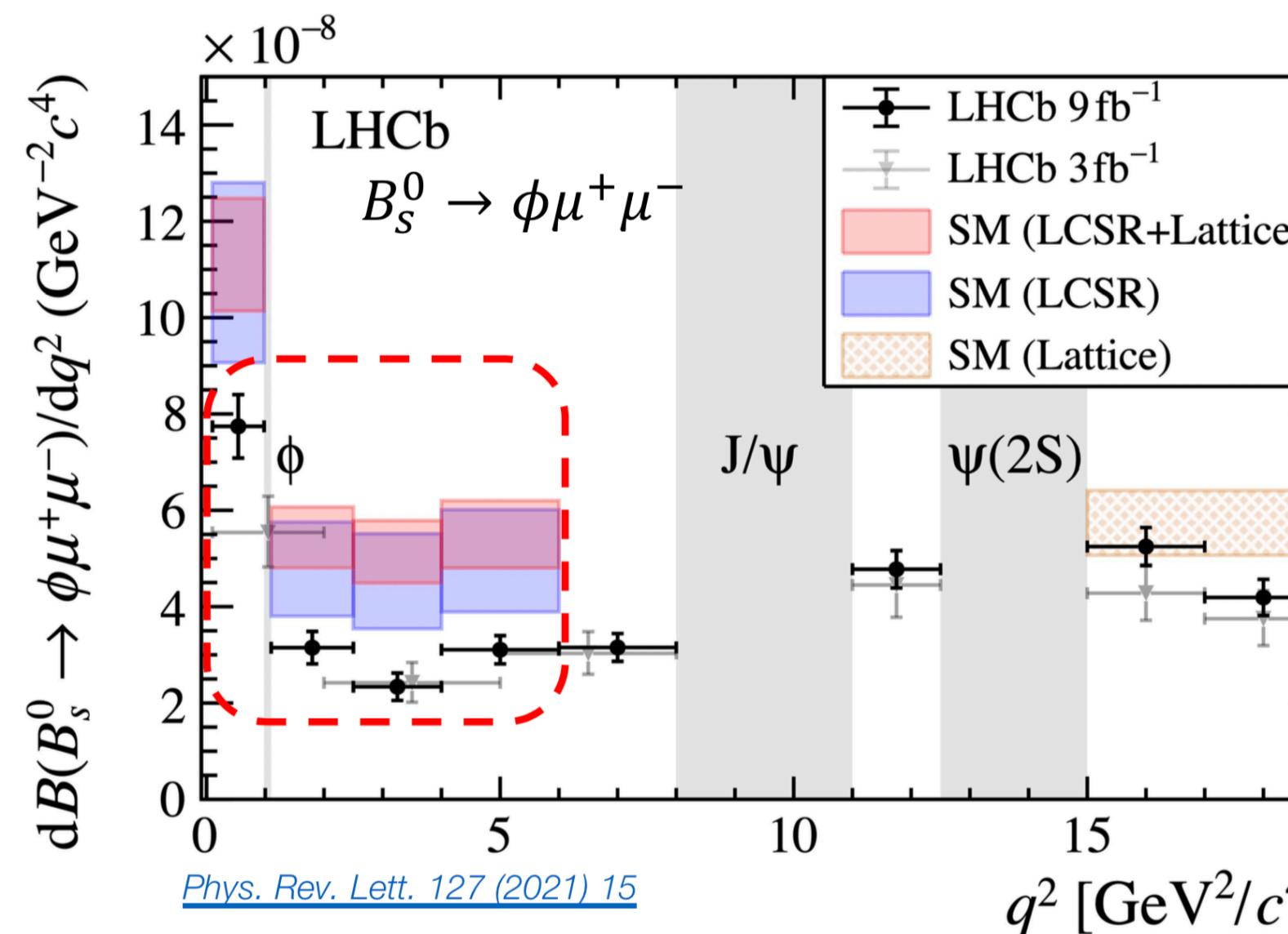
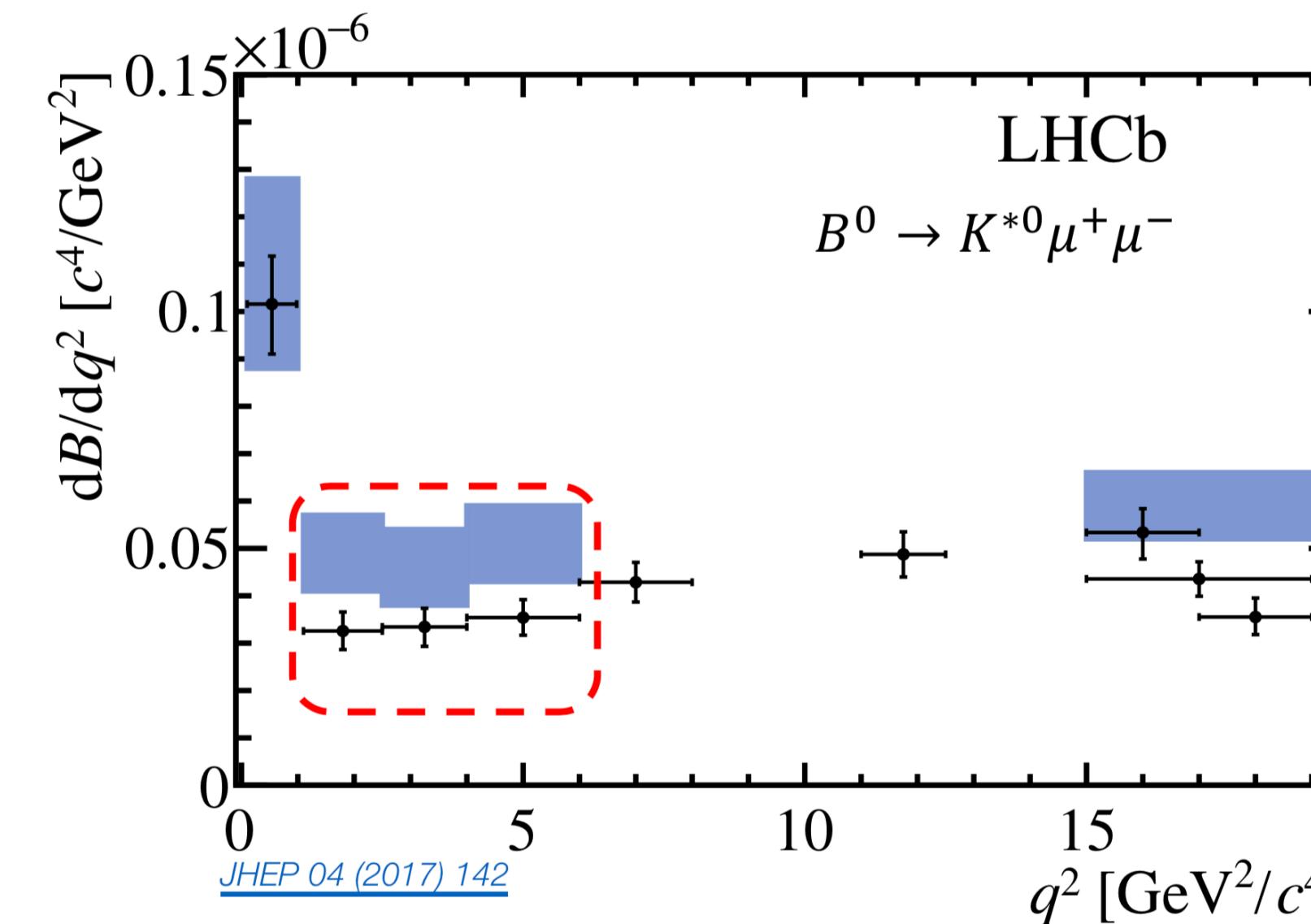
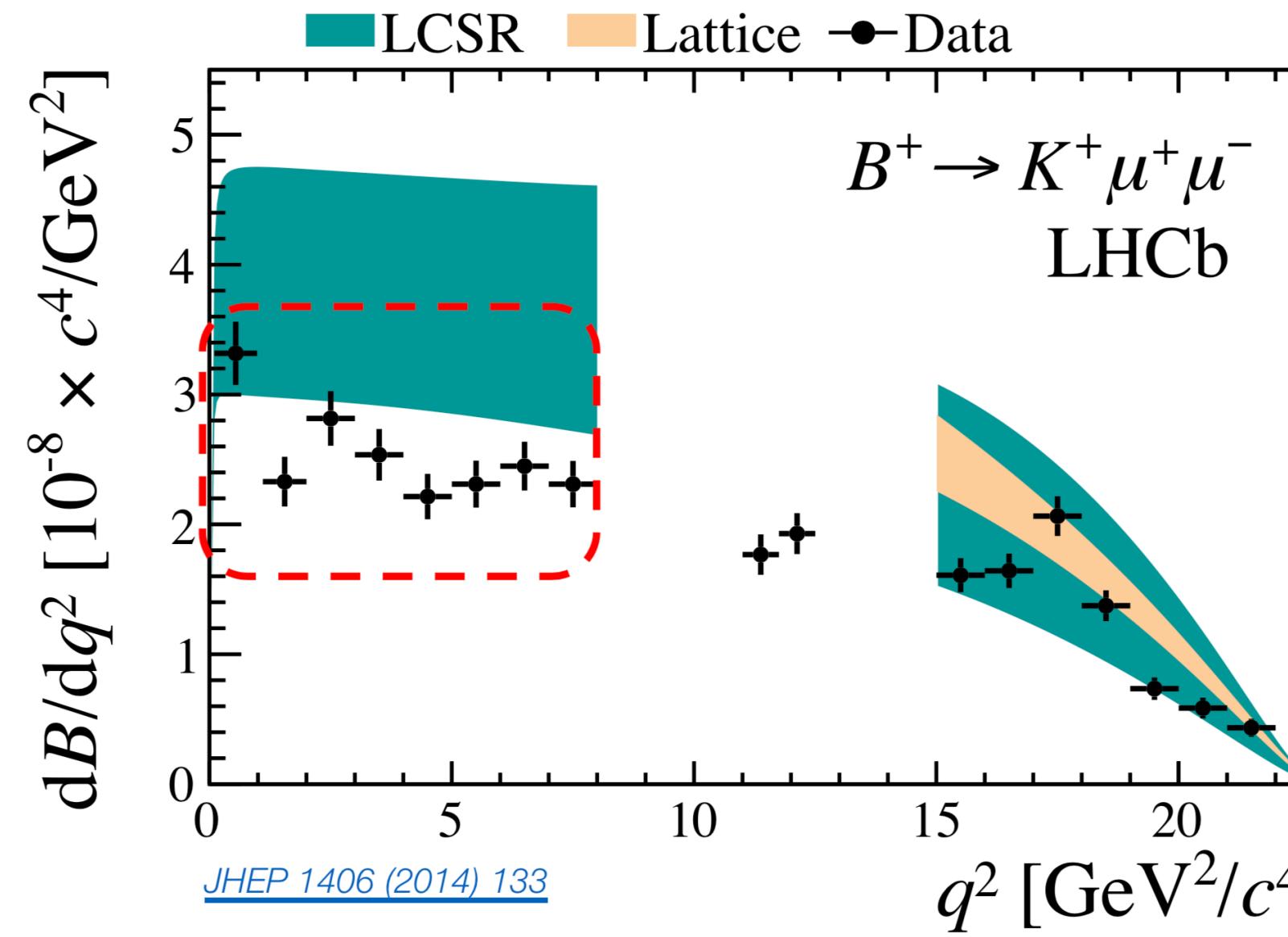
Explaining the $b \rightarrow s\ell^+\ell^-$ anomalies in Z' scenarios with top-FC/FCNC couplings and its implications for the W -boson mass shift

袁兴博
华中师范大学

[arXiv: 2112.14215](#), 李新强, 沈萌, 王东洋, 杨亚东, 袁兴博

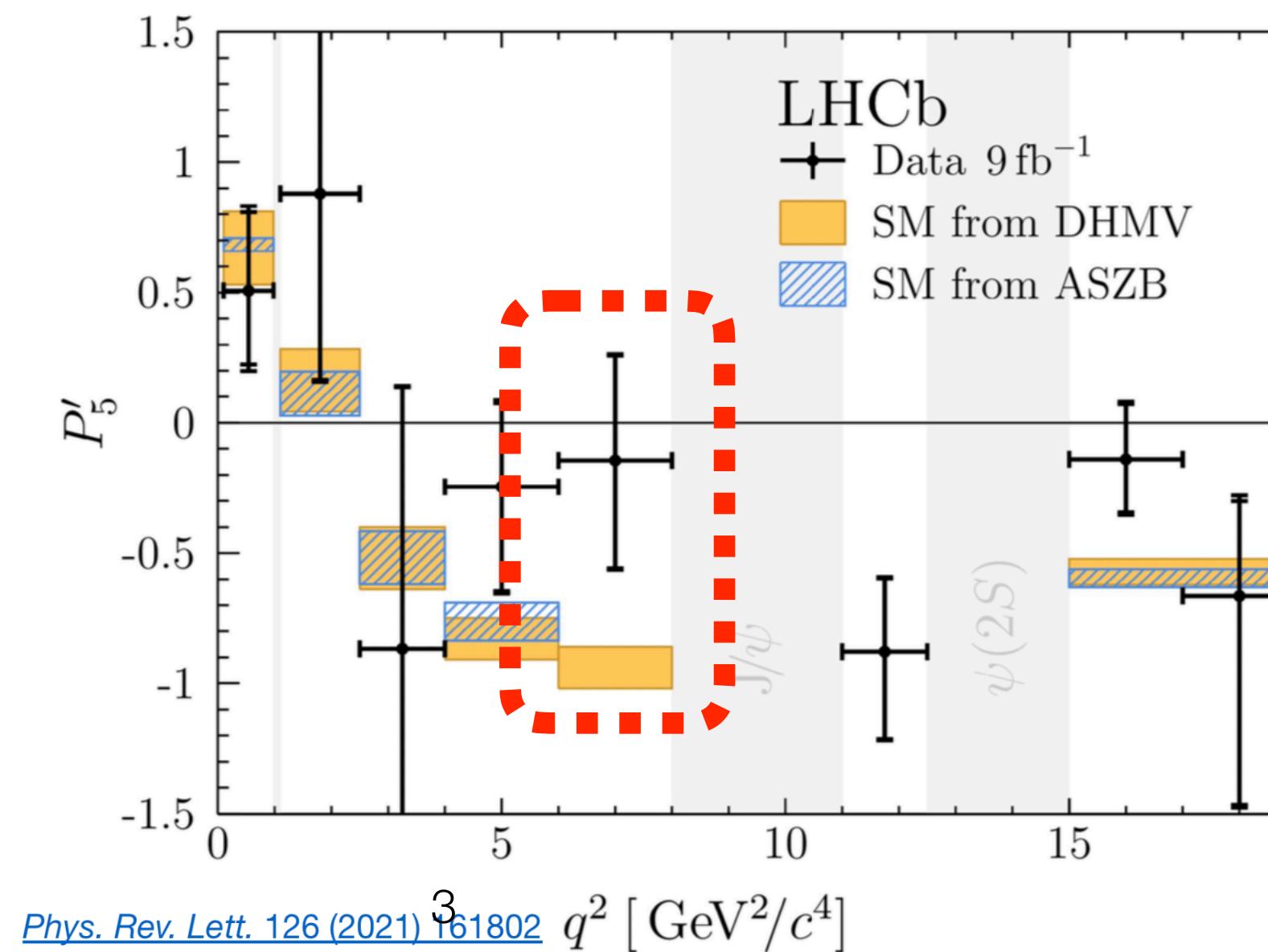
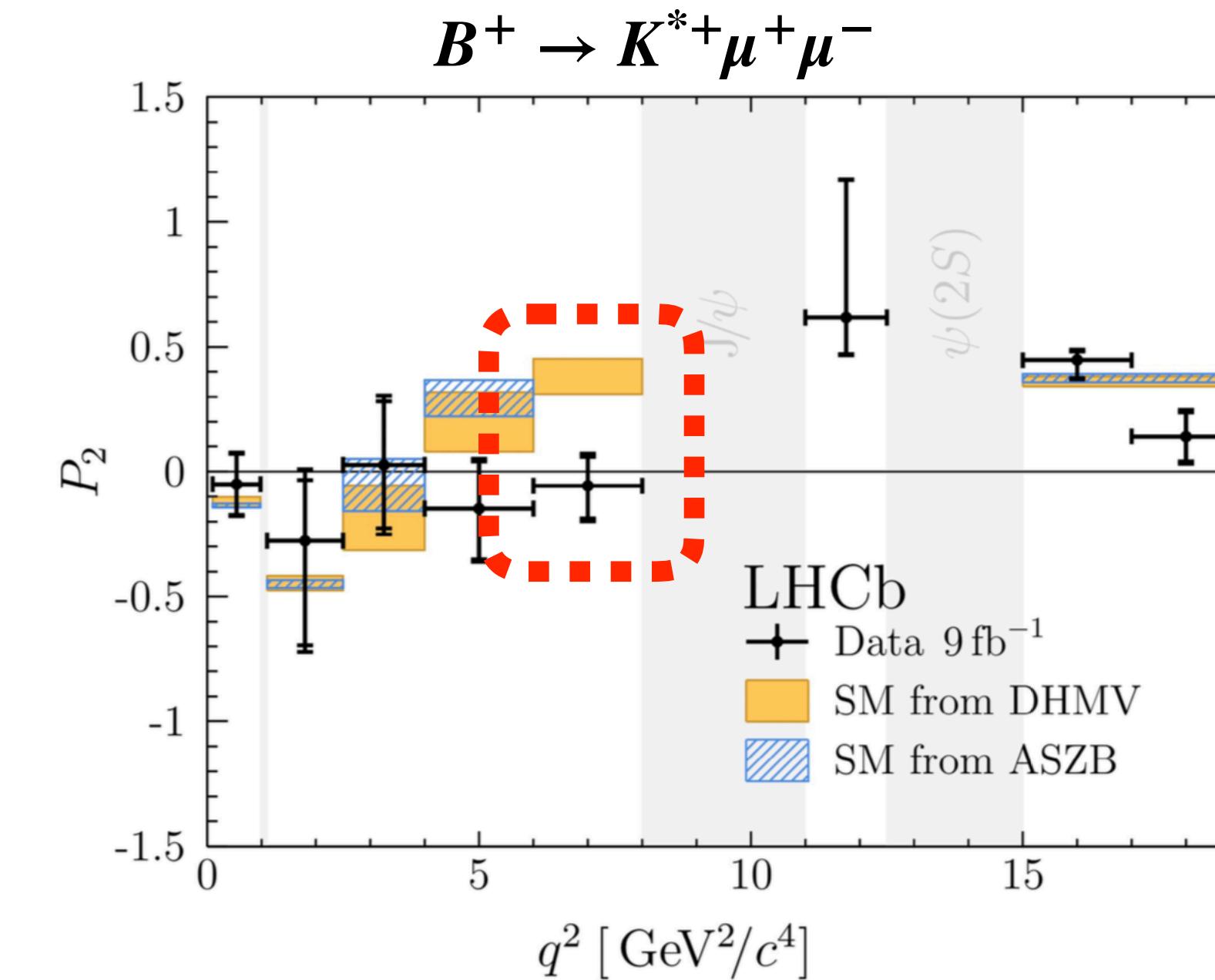
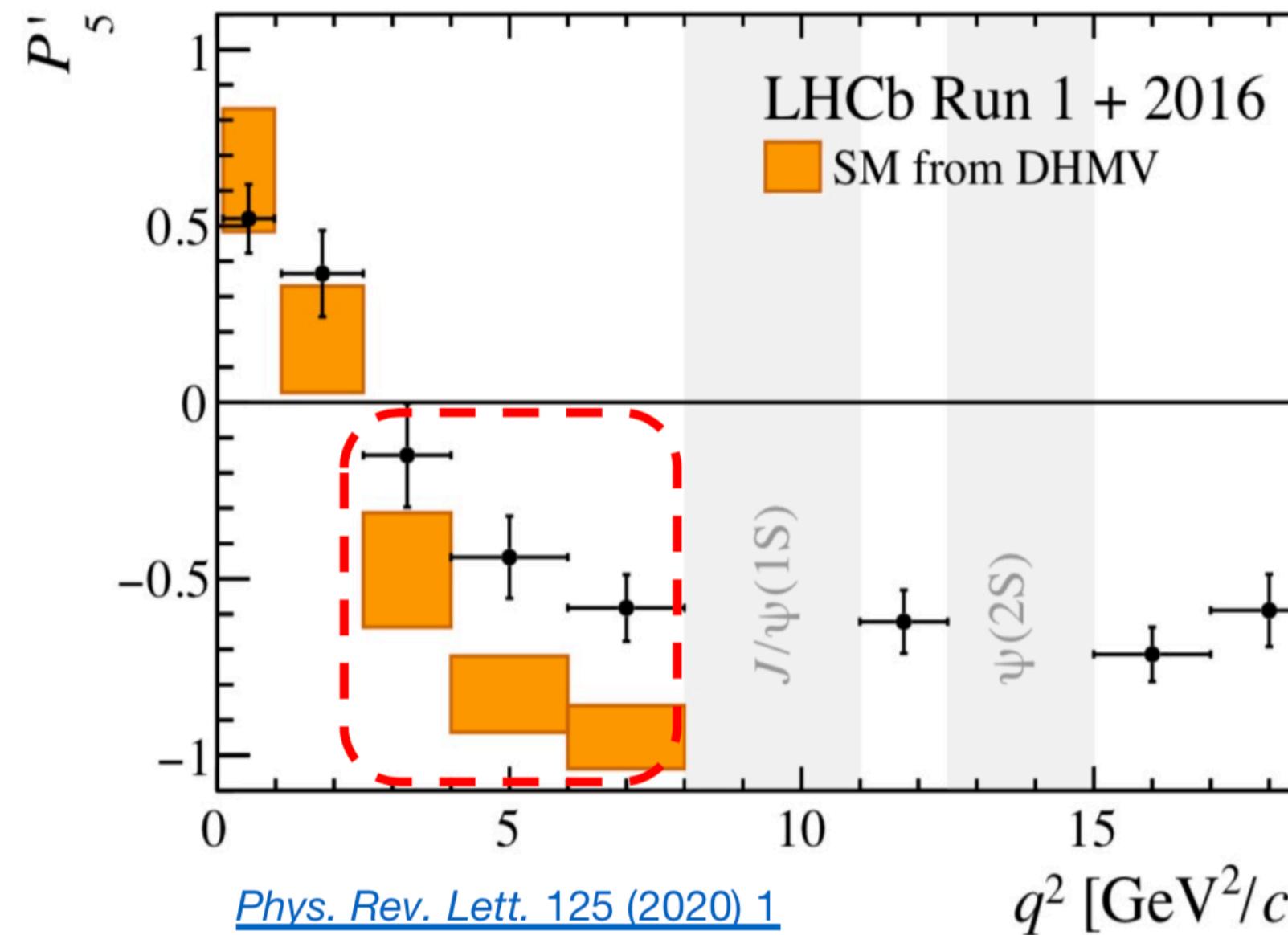
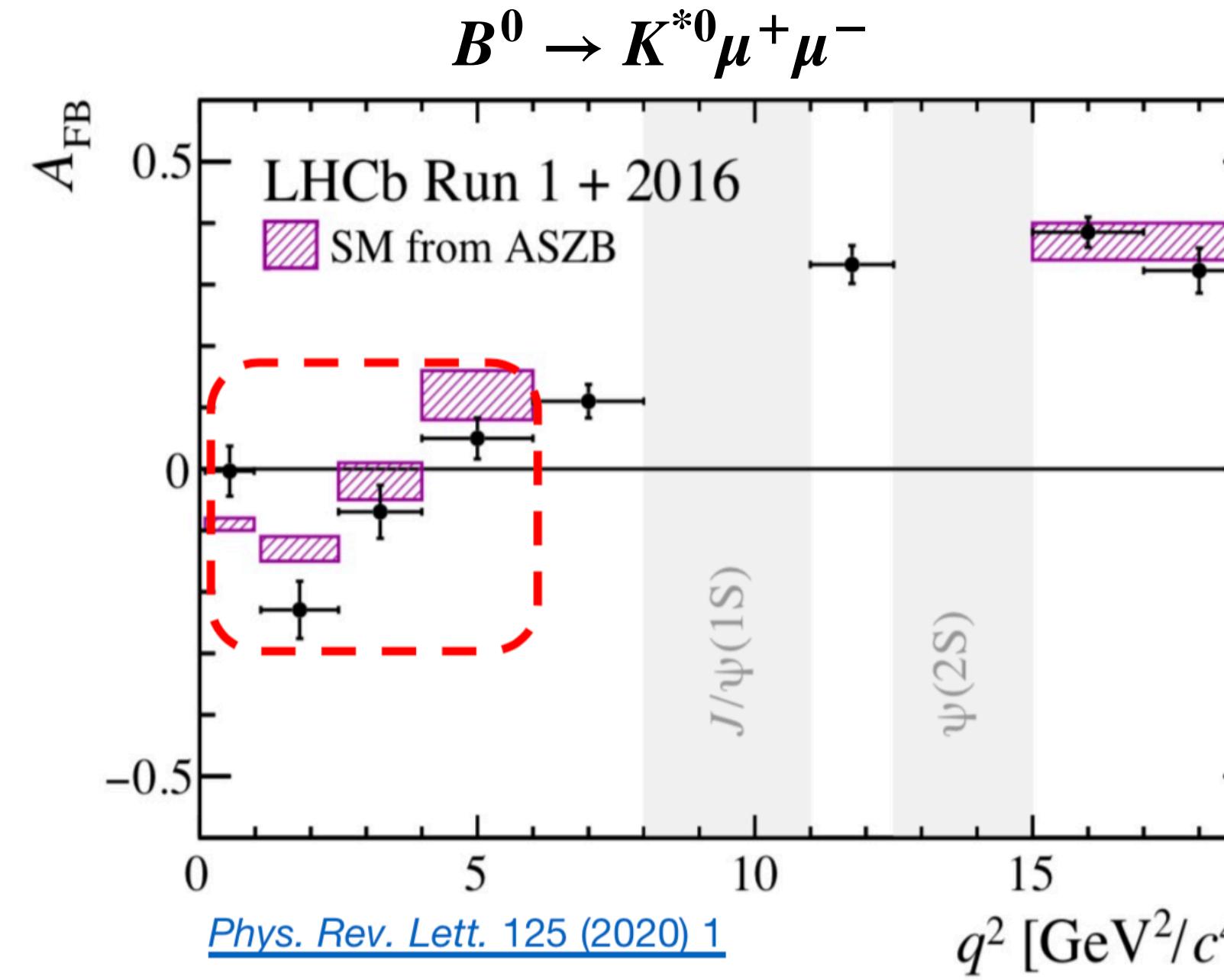
[arXiv: 2205.02205](#), 李新强, 谢泽俊, 杨亚东, 袁兴博

$b \rightarrow s\ell\ell$ anomalies: branching ratio



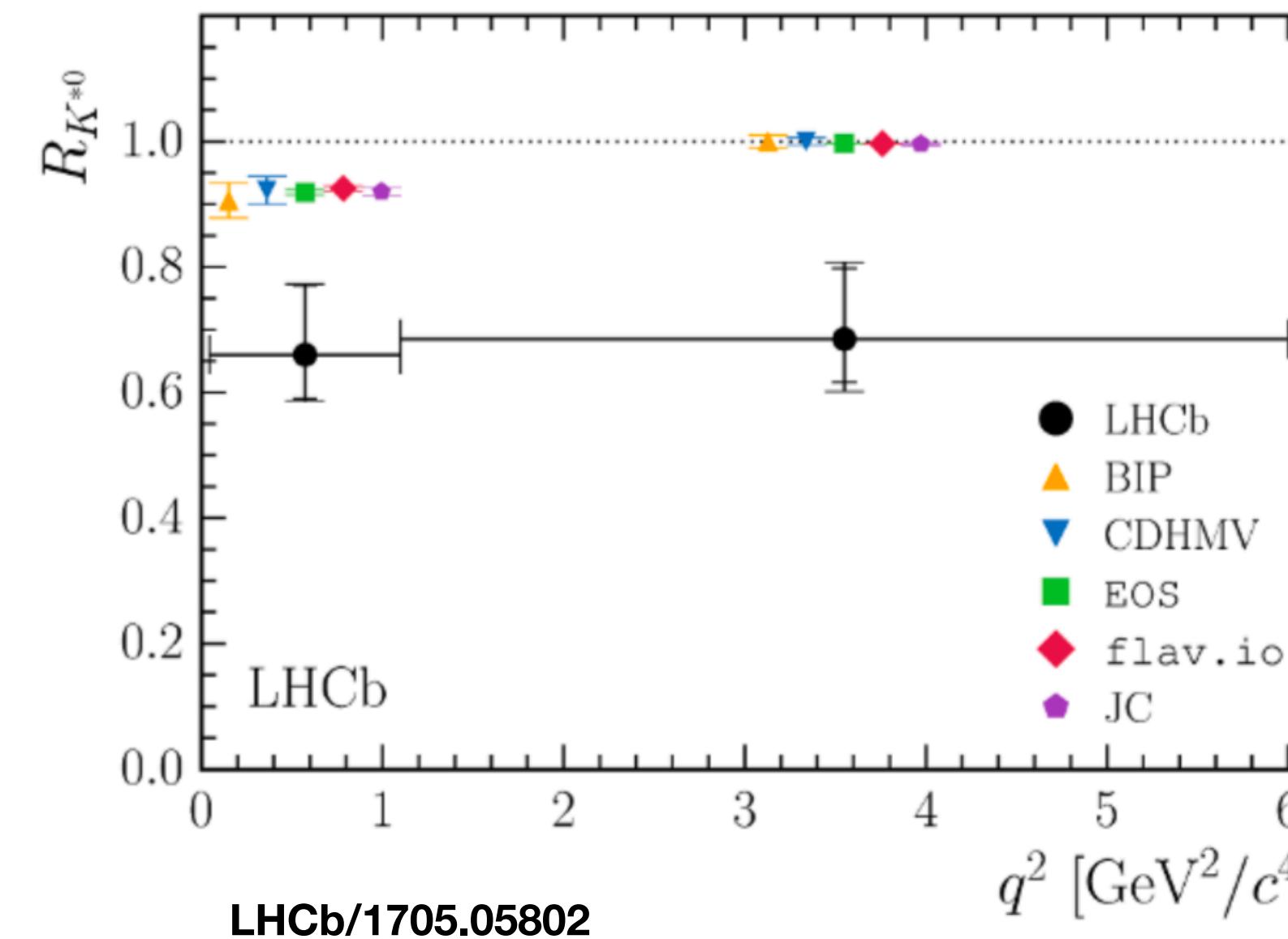
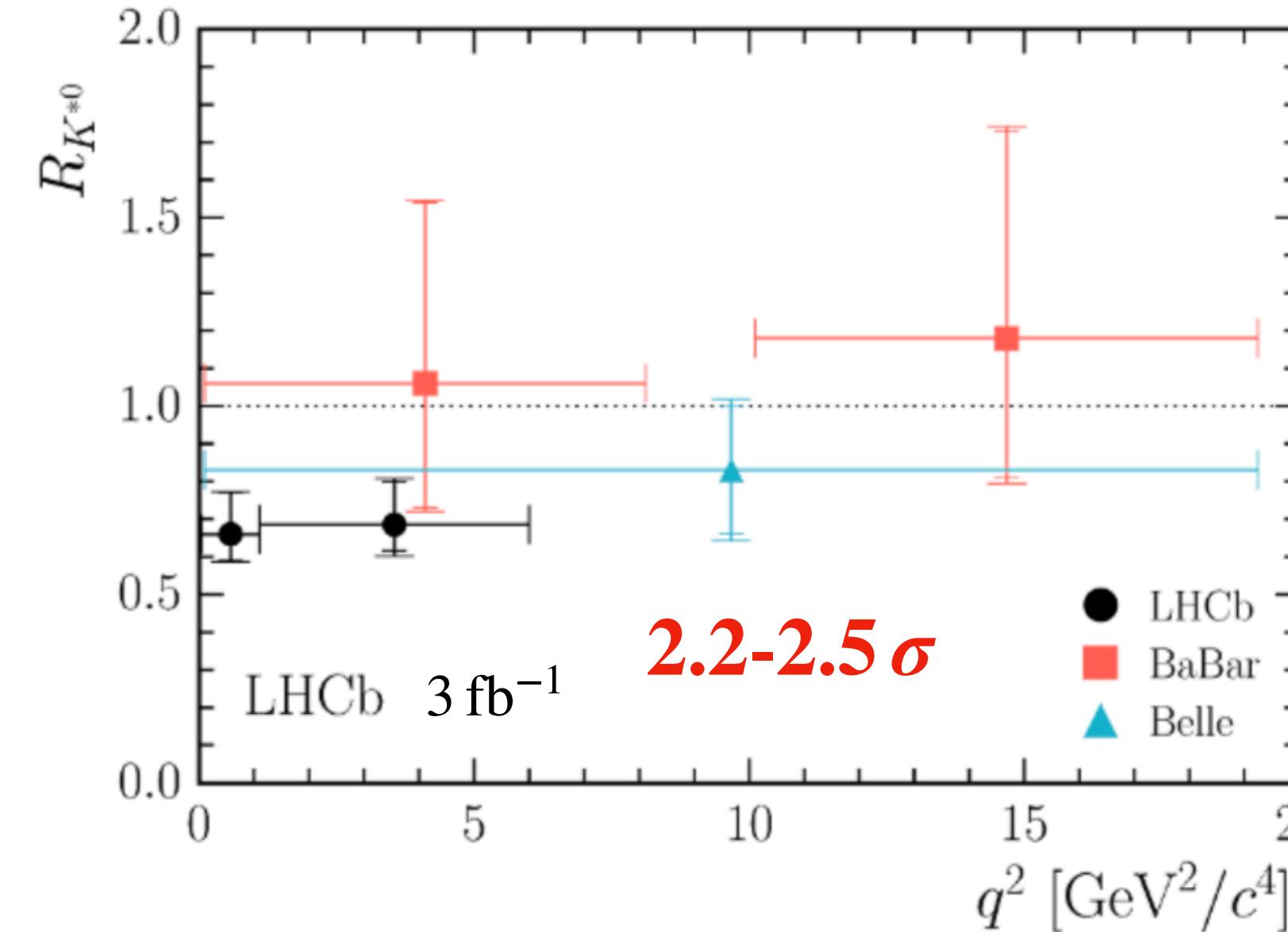
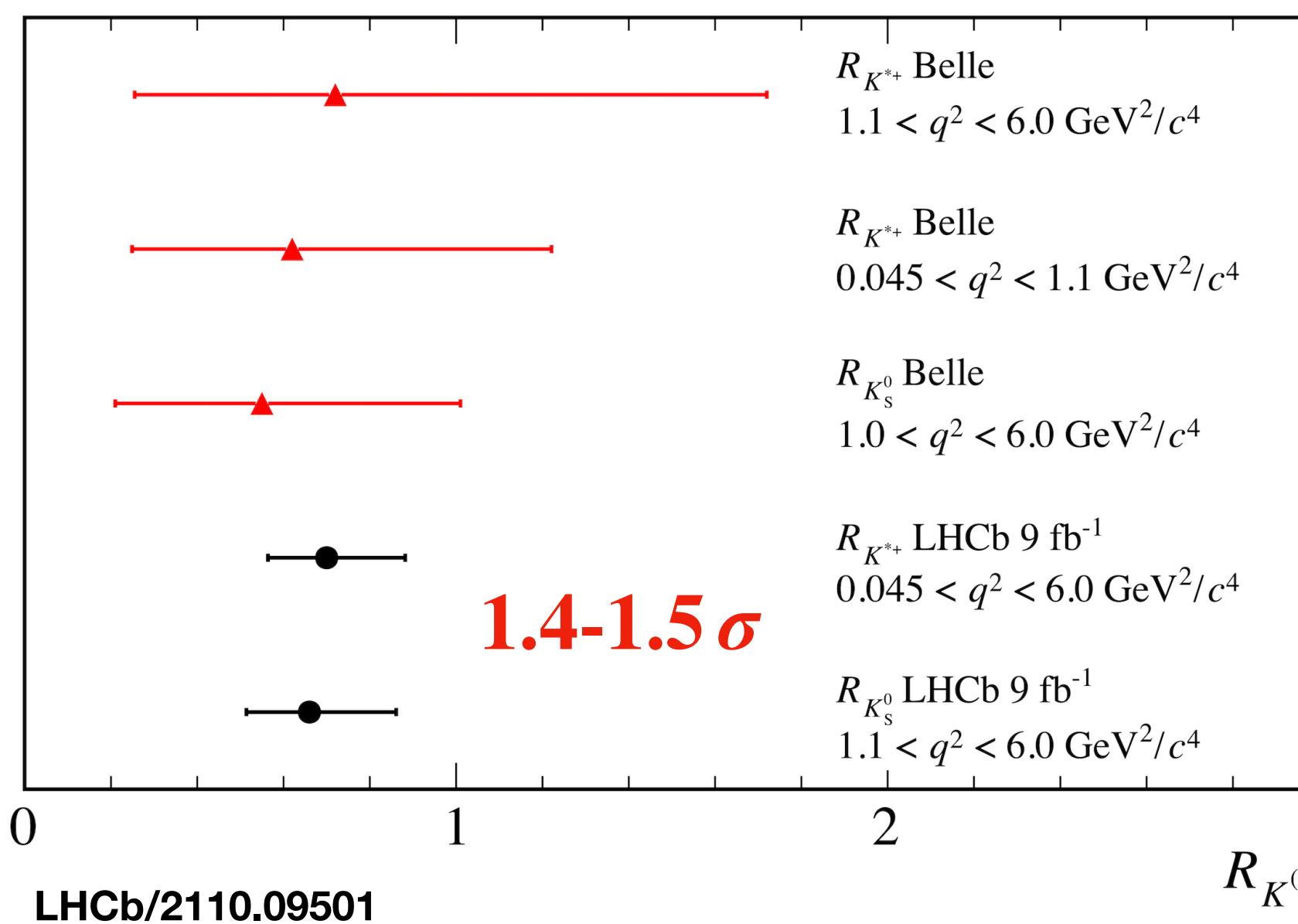
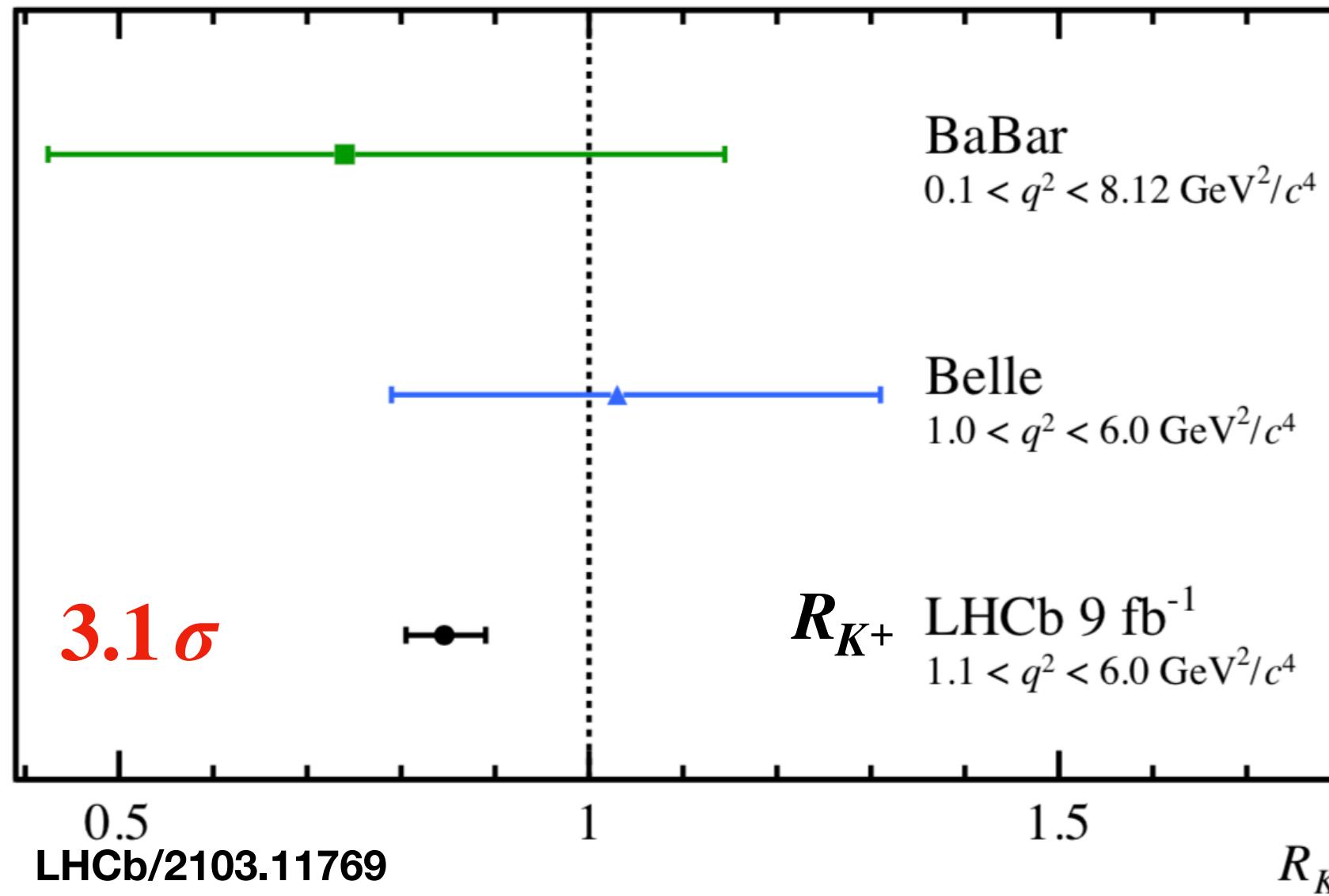
- ▶ EXP below SM
- ▶ Low q^2
- ▶ Theoretical Uncertainties: 😢

$b \rightarrow s\ell\ell$ anomalies: angular distribution



- ▶ Similar deviations in the 2 modes
- ▶ Theoretical Uncertainties:
 - branching ratio: 😭
 - angular distribution: 😢

$b \rightarrow s\ell\ell$ anomalies: lepton flavour violation ratio



$$R_{K^+} = \frac{\mathfrak{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathfrak{B}(B^+ \rightarrow K^+ e^+ e^-)}$$

- ▶ $R_H^{\text{SM}} \approx 1$
- ▶ Hadronic uncertainties cancel
- ▶ $\mathcal{O}(10^{-2})$ QED correction

Theoretical Uncertainties:

- branching ratio: 😢
- angular distribution: 😢
- LFV ratio: 😊

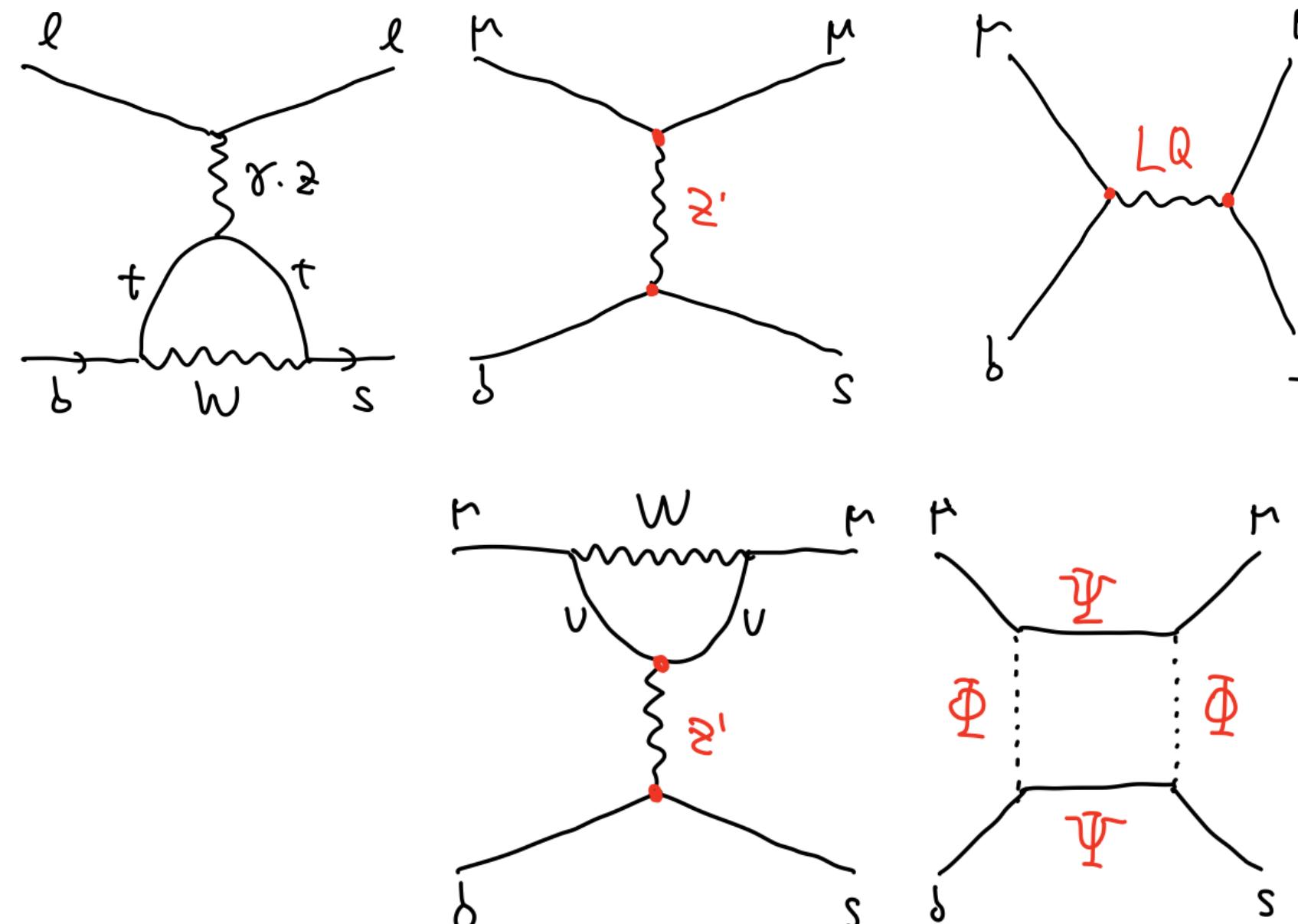


deviation from unity

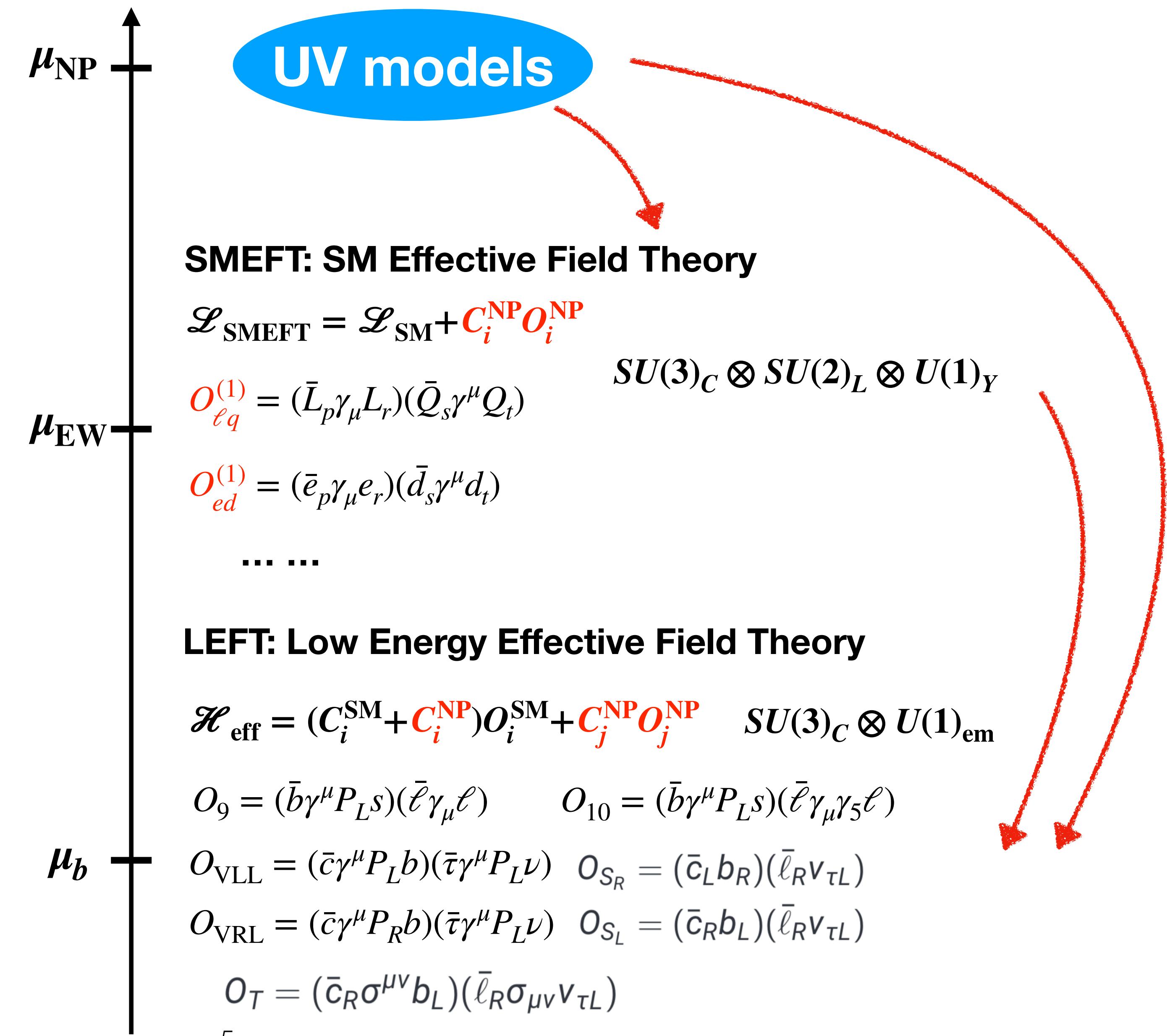
Physics beyond the SM

Flavour anomalies: theoretical interpretation

► $b \rightarrow s\ell^+\ell^-$ anomalies

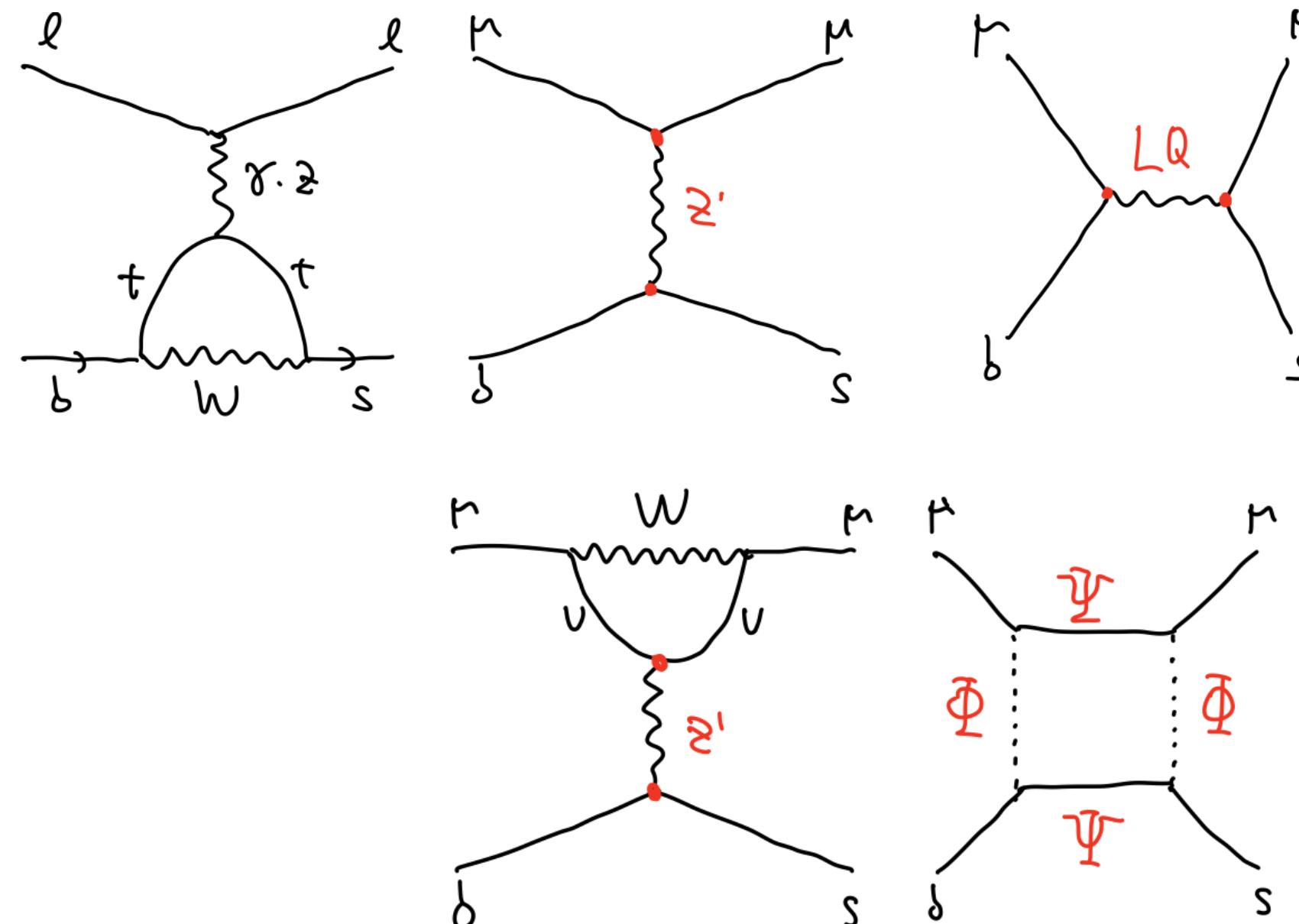


Altmannshofer, Gori, Pospelov, Yavin; 1403.1269,
 Crivellin, D'Ambrosio, Heeck; 1501.00993,
 Celis, Fuentes-Martin, Jung, Serodio; 1505.03079,
 Crivellin, Fuentes-Martin, AG, Isidori; 1611.02703,
 Alonso, Cox, Han, Yanagida; 1705.03858,
 Bonilla, Modak, Srivastava, Valle; 1705.00915,
 Ellis, Fairbairn, Tunney; 1705.03447;
 Allanach, Davighi; 1809.01158,
 Altmannshofer, Davighi, Nardecchia; 1909.02021,
 Allanach; 2009.02197,
 + many more ...

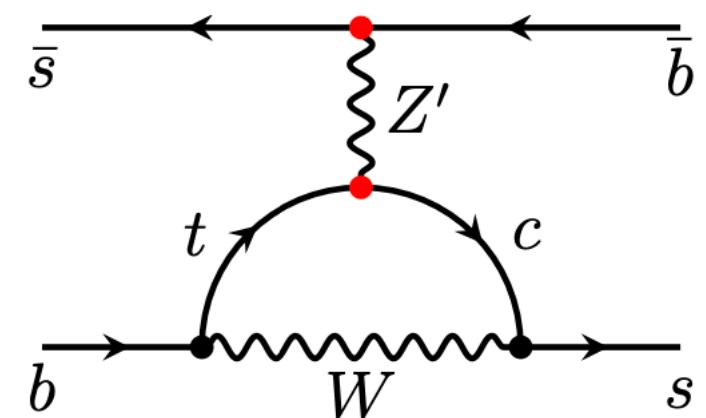


Flavour anomalies: theoretical interpretation

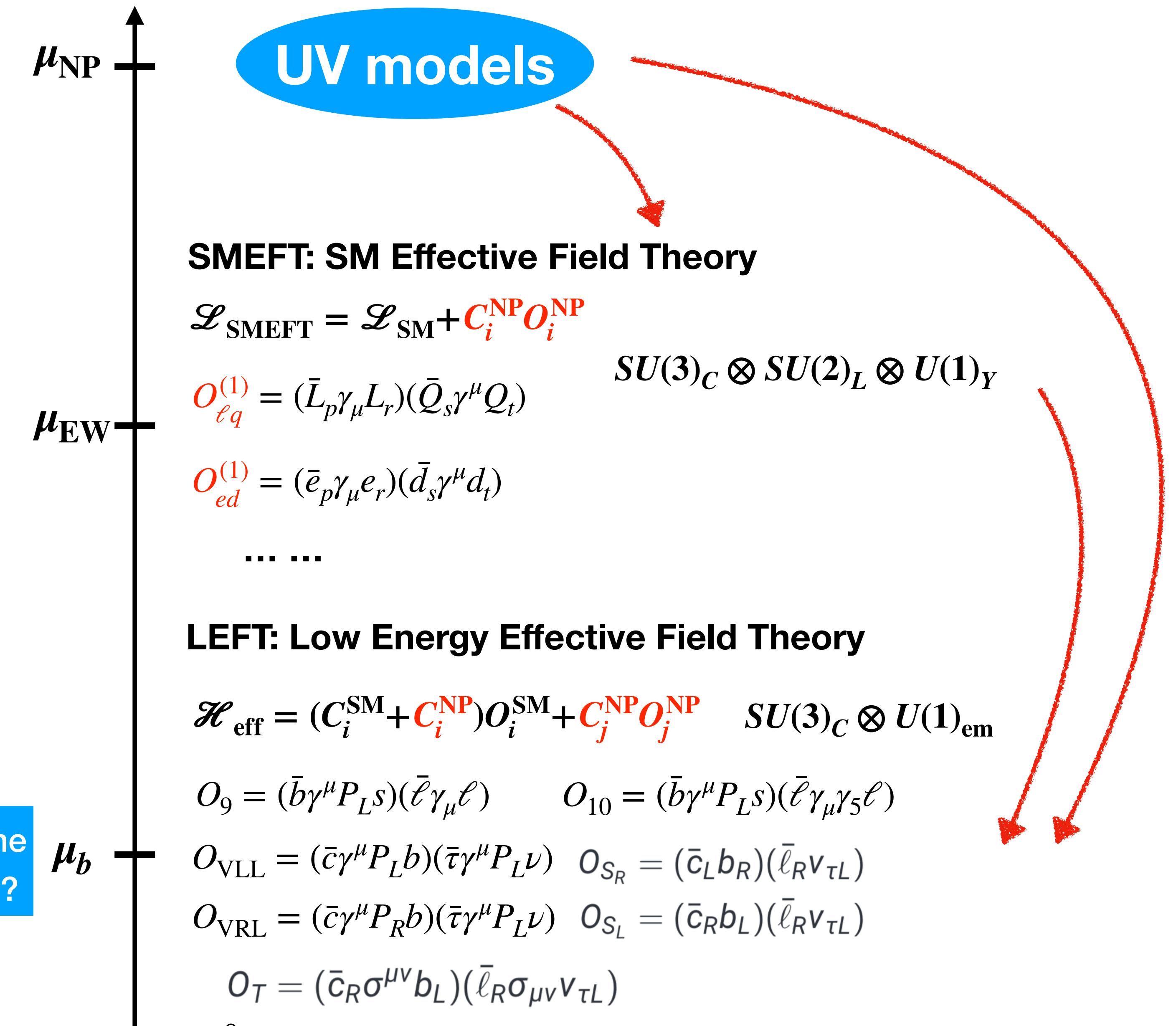
► $b \rightarrow s\ell^+\ell^-$ anomalies



► New possibility ?



Explain $b \rightarrow s\ell^+\ell^-$ by the NP with $t \rightarrow c$ transition ?



Z' scenarios with top-FCNC couplings

► Lagrangian (mass eigenstates)

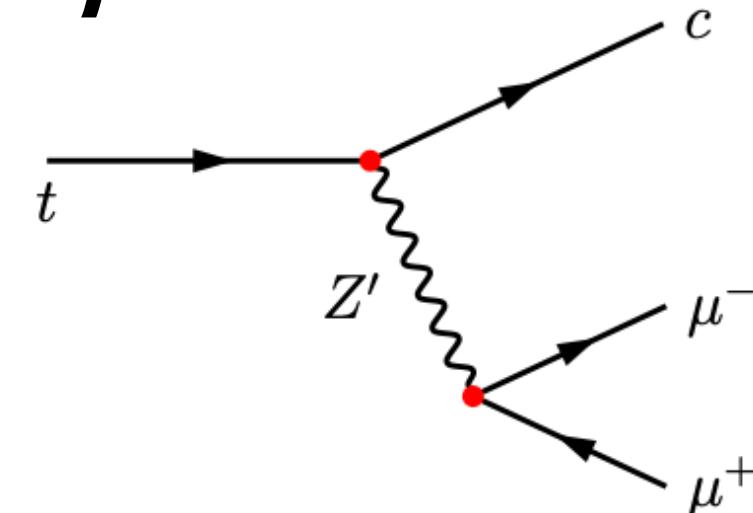
$$\mathcal{L}_{Z'}^I = \left(X_{ct}^L \bar{c} \gamma^\mu P_L t Z'_\mu + \text{h.c.} \right) + \lambda_{\mu\mu}^L \bar{\mu} \gamma^\mu P_L \mu Z'_\mu$$

► Comments

- Phenomenological scenarios (simple, but not UV complete)
- 2 parameters X_{ct}^L (complex) and $\lambda_{\mu\mu}^L$ (real)
- Right-handed $\mu^+ \mu^- Z'$ interaction can be added $\implies (g-2)_\mu$
- $e^+ e^- Z'$ instead of $\mu^+ \mu^- Z'$ is also possible \implies pheno@ $e^+ e^-$ collider
- $\bar{t} u Z'$ instead of $\bar{t} c Z'$ is also possible
- Models with right-handed $\bar{t} c Z'$ couplings

R. Coy, M. Frigerio, F. Mescia, O. Sumensari, EPJC 2020.
 H.J. He, T.M.P. Tait, C.P. Yuan, PRD 2000
 X.F. Wang, C. Du, H.J. He, PLB 2013

► $t \rightarrow c \mu^+ \mu^-$

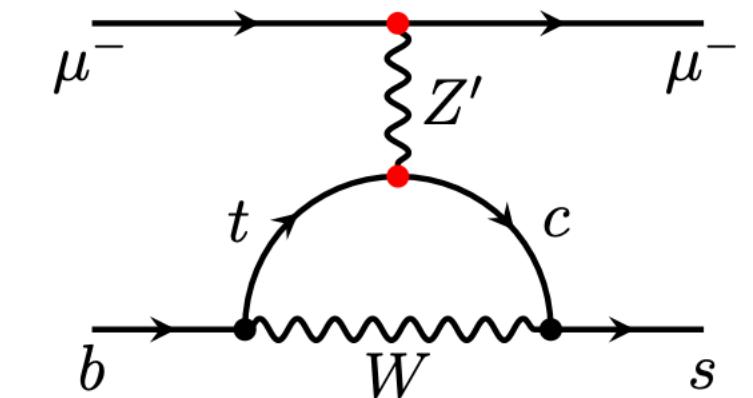
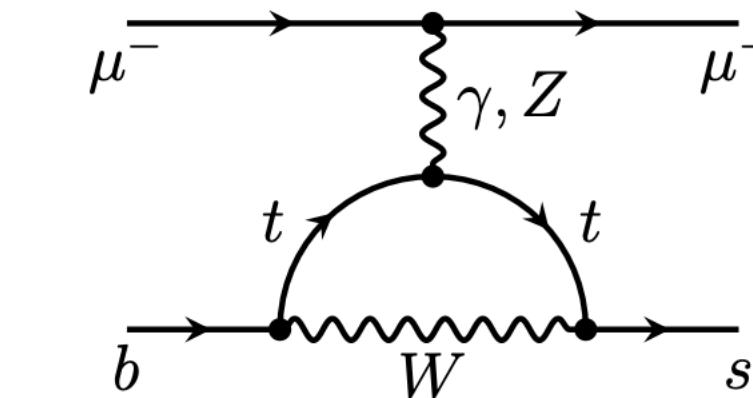


SM branching ratio $\sim \mathcal{O}(10^{-10})$

clean NP signal

► $b \rightarrow s \mu^+ \mu^-$

► Feynman diagram



► Effective Hamiltonian

$$\mathcal{H}_{\text{eff}}^{b \rightarrow s \mu^+ \mu^-} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_{i=1}^{10} \mathcal{C}_i \mathcal{O}_i$$

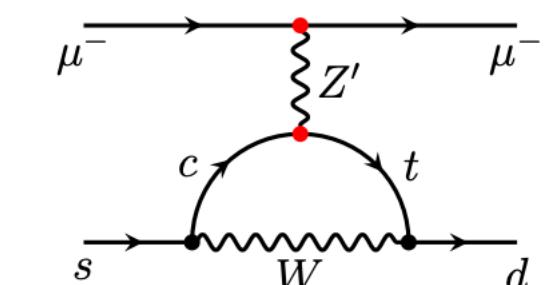
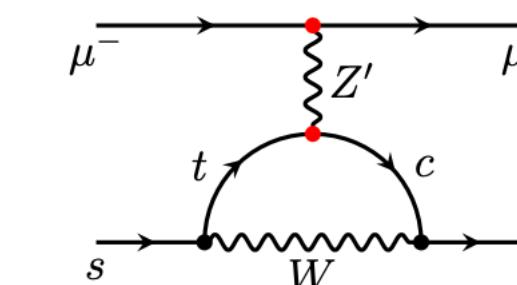
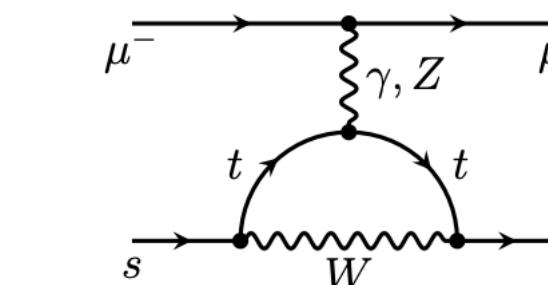
$$\mathcal{O}_{9\ell} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b)(\bar{\ell} \gamma^\mu \ell) \quad \mathcal{O}_{10\ell} = \frac{e^2}{16\pi^2} (\bar{s} \gamma_\mu P_L b)(\bar{\ell} \gamma^\mu \gamma_5 \ell)$$

► Wilson coefficient: NP effect

$$\mathcal{C}_{9\mu}^{\text{NP}, I} = -\mathcal{C}_{10\mu}^{\text{NP}, I} = \frac{1}{8\sqrt{2}G_F s_W^2} \frac{V_{cs}^*}{V_{ts}^*} \frac{X_{ct}^L \lambda_{\mu\mu}^L}{m_{Z'}^2} f(x_t)$$

- enhanced by V_{cs}/V_{ts}
- favored by $b \rightarrow s \ell^+ \ell^-$ global fits

► $s \rightarrow d \mu^+ \mu^-$



Numerical analysis: $b \rightarrow s\ell^+\ell^-$

► Global fit

► Inclusive decays

- $B \rightarrow X_s \gamma$
- $B \rightarrow X_s \ell^+ \ell^-$

► Exclusive leptonic decays

- $B_{s,d} \rightarrow \ell^+ \ell^-$

► Exclusive radiative/semileptonic decays

- $B \rightarrow K^* \gamma$

- $B^{(0,+)} \rightarrow K^{(0,+)} \ell^+ \ell^-$ e.g., LHCb, Nature Phys. 18 (2022) 3, 277 | PRL128(2022)19, 191802

- $B^{(0,+)} \rightarrow K^{*(0,+)} \ell^+ \ell^-$ e.g., LHCb PRL126(2021), 16161802

- $B_s \rightarrow \phi \mu^+ \mu^-$ e.g., LHCb, PRL127(2021)15, 151801, JHEP11(2021)043

- $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$ e.g., LHCb JHEP 09 (2018) 146

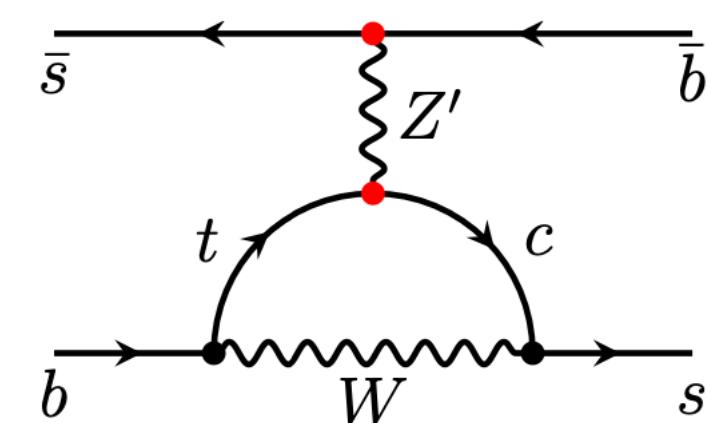
► Including about 200 observables (almost all available measurements

from BaBar, Belle, CDF, ATLAS, CMS, and LHCb)

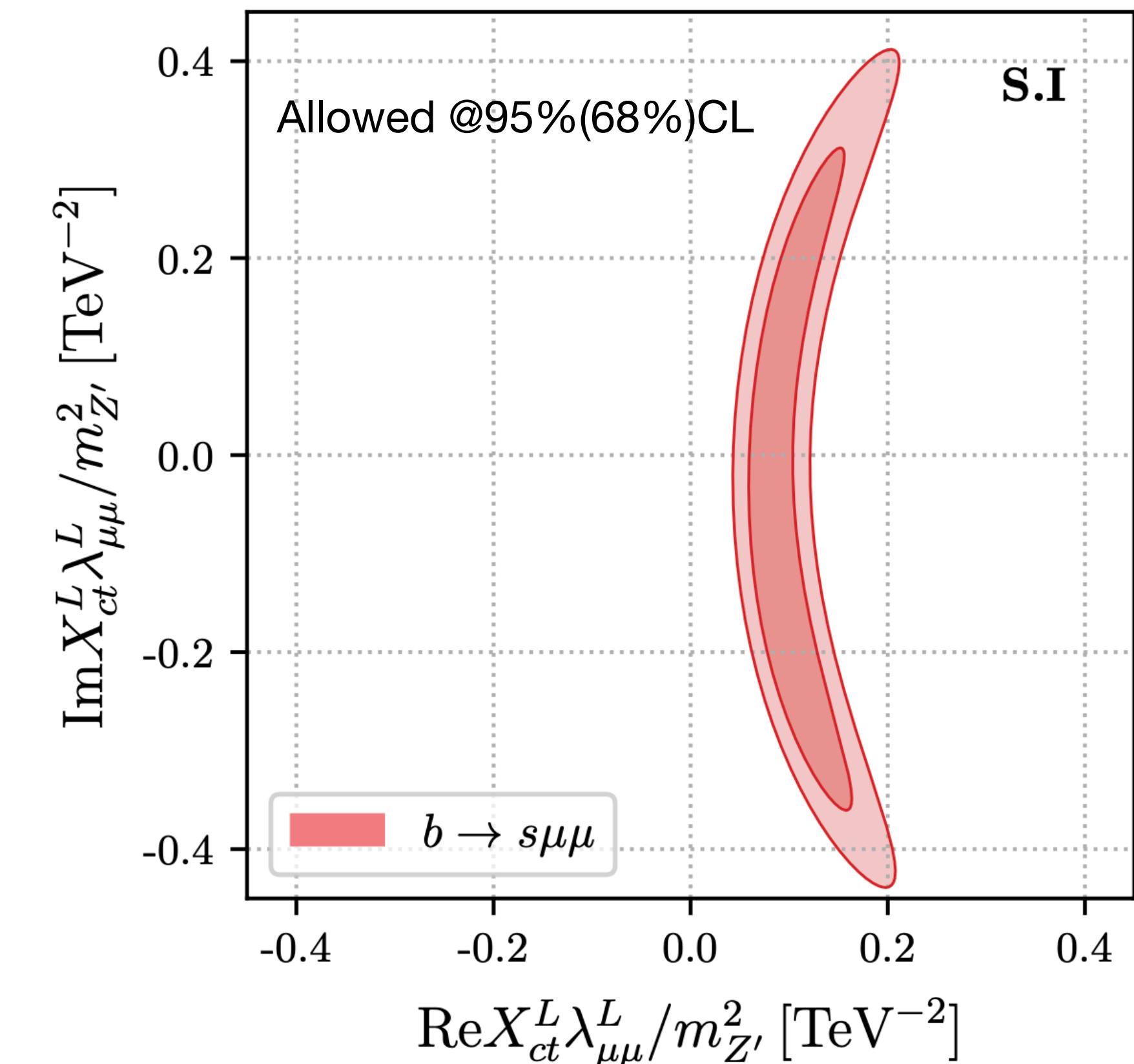
► performed using an extended version of the package **flavio**

► Parameters

$$\frac{\text{Re}X_{ct}^L \lambda_{\mu\mu}^L}{m_{Z'}^2} \quad \frac{\text{Im}X_{ct}^L \lambda_{\mu\mu}^L}{m_{Z'}^2}$$



► Fit result



- ★ can explain $b \rightarrow s\ell^+\ell^-$ anomalies at 95% CL.
- ★ for $m_{Z'} < \mathcal{O}(5)$ TeV, both X_{ct}^L and $\lambda_{\mu\mu}^L$ are in the perturbative region

Numerical analysis: $t \rightarrow c\mu^+\mu^-$

$m_{Z'} < m_t$

► $t \rightarrow c\mu^+\mu^-$

- ▶ Currently, no direct experimental bounds
- ▶ LHC searches performed at the Z peak, $|m_{\mu\mu} - m_Z| < 15$ GeV
- ▶ Detailed analysis with the signal shape could be used to derive constraints
- ▶ We concentrate on the mass region 105 GeV $< m_{Z'} < m_t$

► $t \rightarrow cZ'$

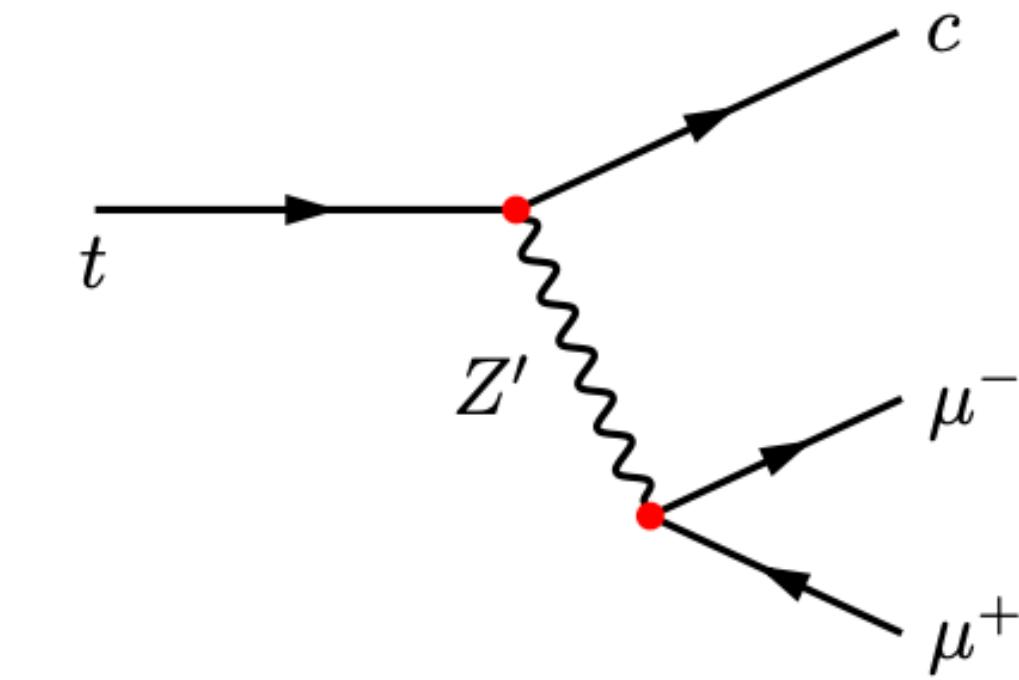
- ▶ Currently, no direct experimental bounds
- ▶ Contribute to the top-quark width
- ▶ $\Gamma_t^{\text{SM}} = 1.3$ GeV v.s. $\Gamma_t^{\text{exp}} = 1.42^{+0.19}_{-0.15}$ GeV leaves $\mathcal{O}(20\%)$ room for Z'
- ▶ ★ Top-quark provides a unique constraint on the $\bar{t}cZ'$ coupling

$m_{Z'} > m_t$

► $t \rightarrow c\mu^+\mu^-$

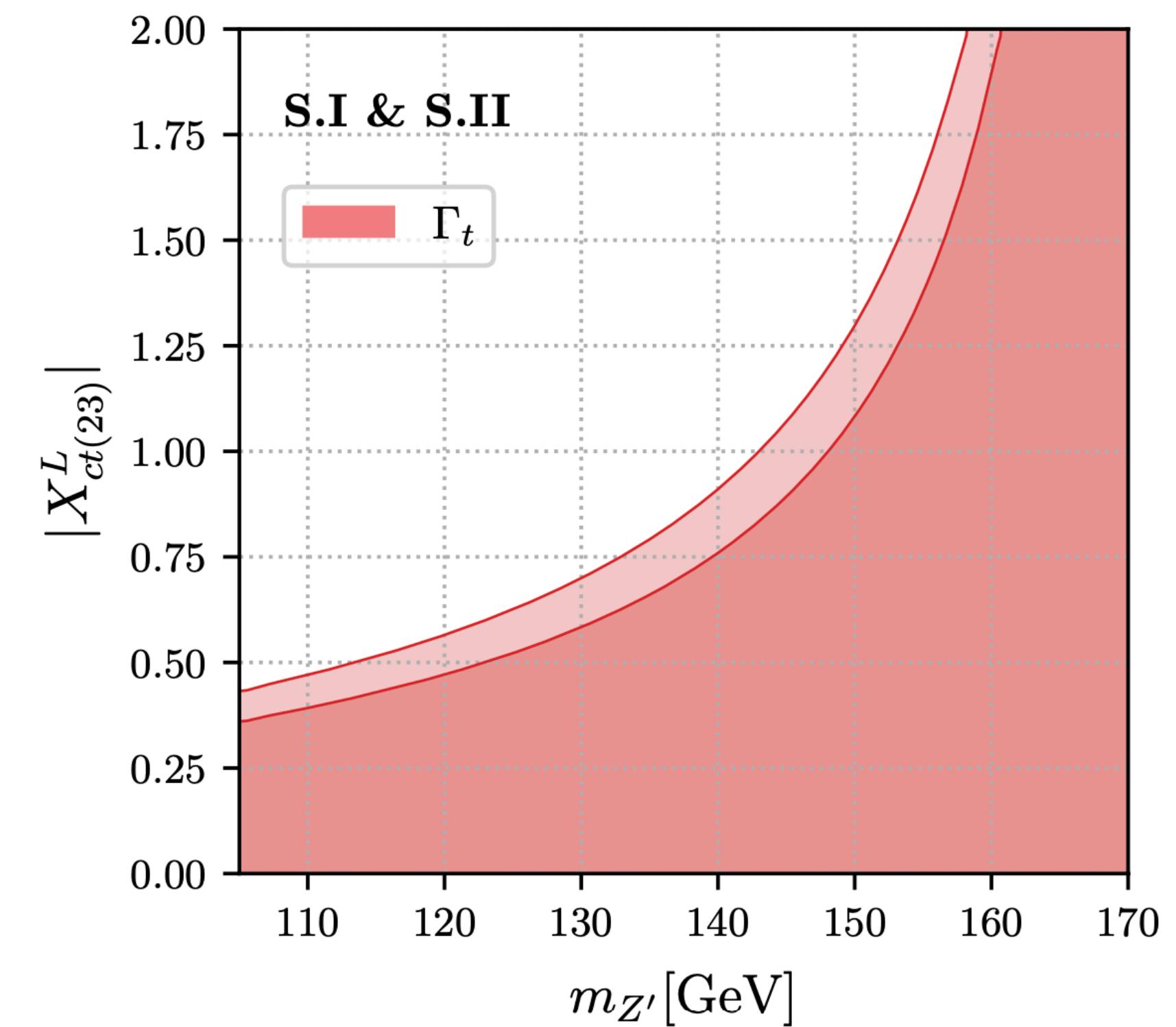
- ▶ Currently, no direct experimental bounds
- ▶ No constraints, similar as the $m_{Z'} < m_t$ case

► $pp \rightarrow tZ'$



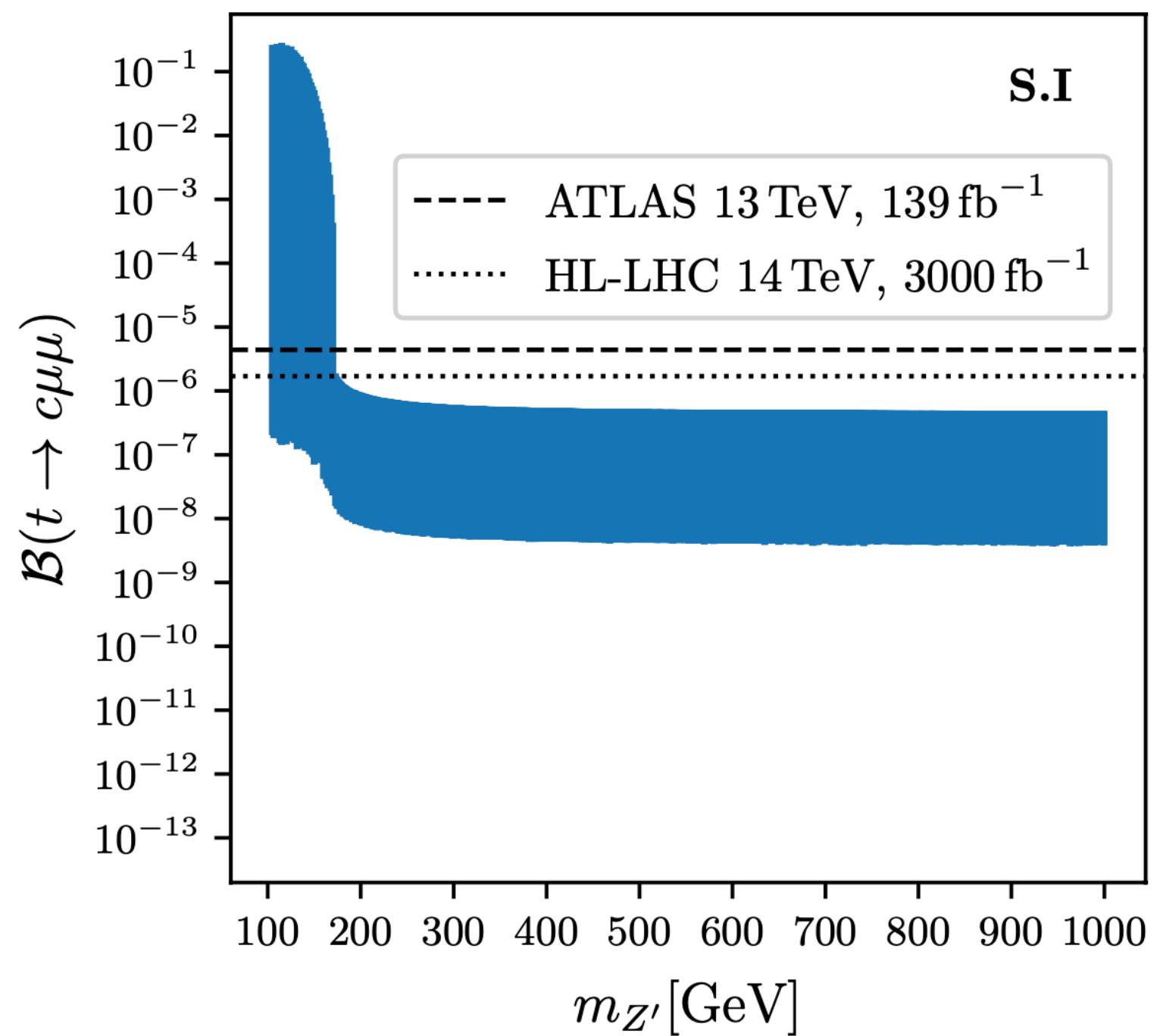
ATLAS, JHEP07(2018)176; CMS, JHEP07(2017)003

M. Chala, J. Santiago, and M. Spannowsky, JHEP04(2019)014



Numerical analysis: $t \rightarrow c\mu^+\mu^-$

► Prediction on $Br(t \rightarrow c\mu^+\mu^-)$



- Upper bound on $Br(t \rightarrow c\mu^+\mu^-)$ is estimated by the bound on $Br(t \rightarrow cZ)$ and $Br(Z \rightarrow \mu^+\mu^-) = 3.37\%$

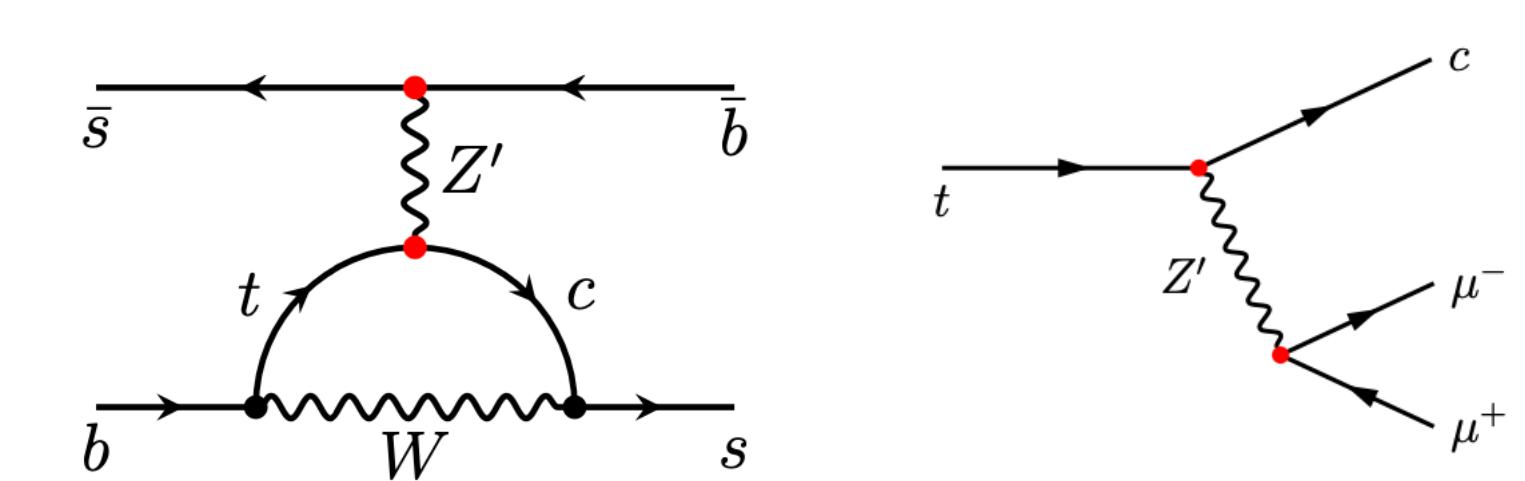
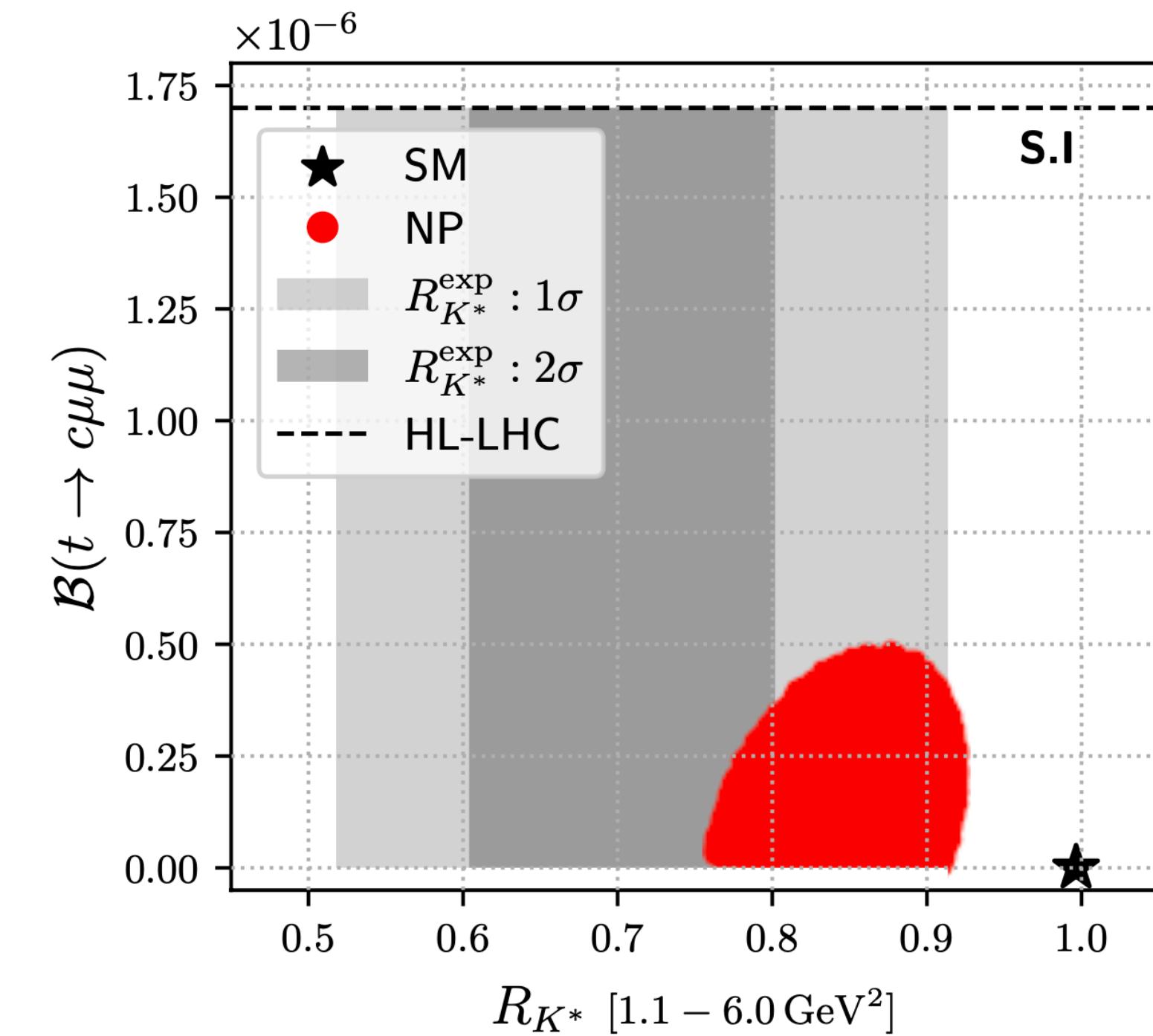
★ $m_{Z'} < m_t$: $t \rightarrow c\mu^+\mu^-$ can serve as a sensitive probe of the Z' boson

★ $m_{Z'} > m_t$: $pp \rightarrow tZ'$ reaches the sensitivity of the HL-LHC (3000 fb^{-1})

► Sensitivity is $\Lambda_{tc\mu\mu} = 1.5 \text{ TeV}$ from an EFT analysis

► $1.4 < \Lambda_{tc\mu\mu} < 4.8 \text{ TeV}$ obtained from the $b \rightarrow s\ell^+\ell^-$ global fit

► Correlation for $m_{Z'} = 1 \text{ TeV}$



Summary: Z' scenarios with top-FCNC couplings

Conclusions

- ▶ A phenomenological Z' scenario is considered, in which a Z' couples only to $t\bar{c}$ and $\mu^+\mu^-$ with left-handed chirality
- ▶ The Z' effects on the $b \rightarrow s\mu^+\mu^-$ automatically induce $C_9^{\text{NP}} = -C_{10}^{\text{NP}}$, which is favored by the global fit
- ▶ The Z' scenario can address the $b \rightarrow s\mu^+\mu^-$ anomalies, which satisfying other flavour and collider constraints
- ▶ For $m_{Z'} < m_t$: resonance searches in $t \rightarrow c\mu^+\mu^-$ can serve as a sensitive probe of the Z' boson
- ▶ For $m_{Z'} > m_t$: $pp \rightarrow tZ'$ reaches the sensitivity of the HL-LHC (3000 fb^{-1})

Issues

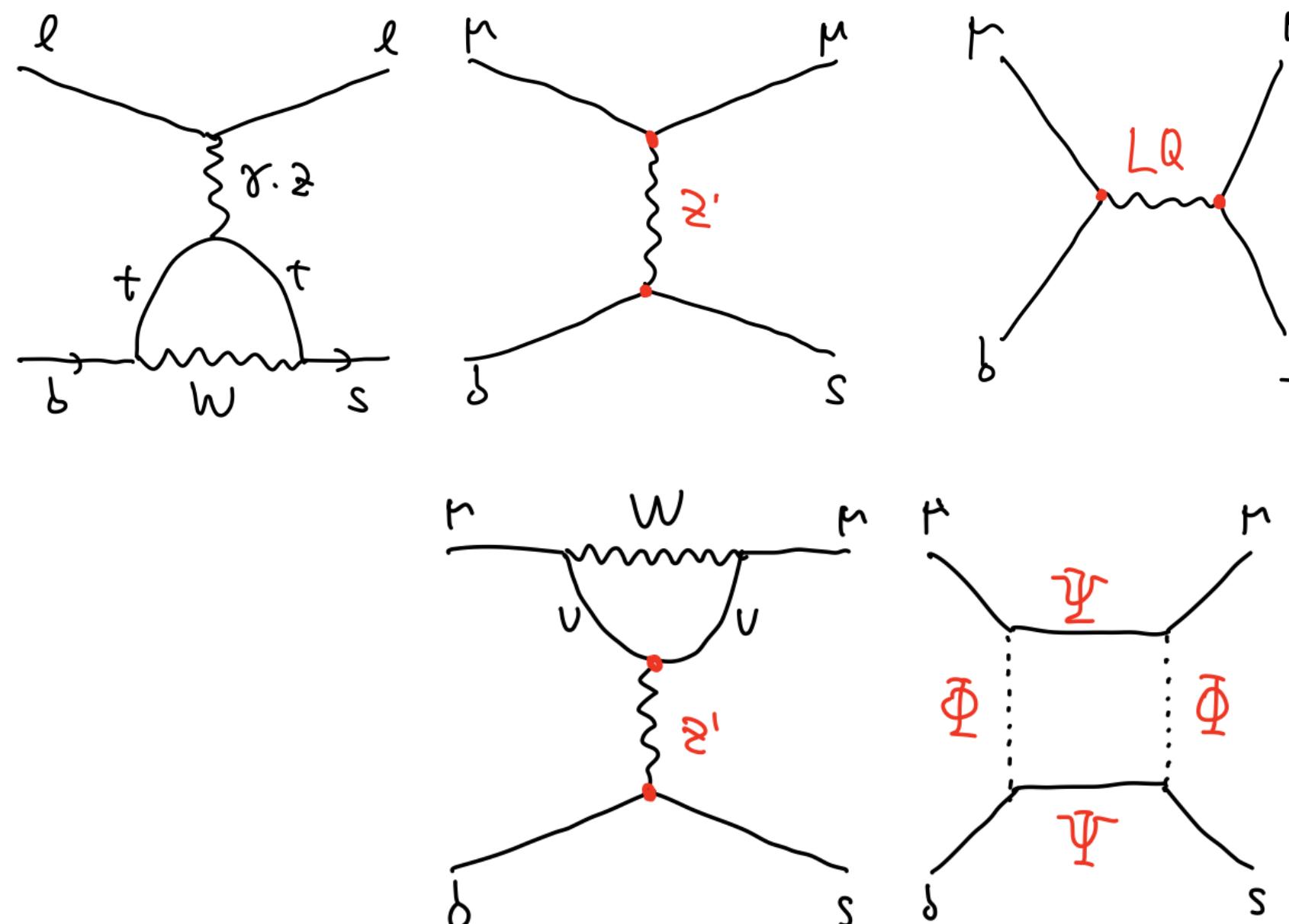
- ▶ NOT UV complete
- ▶ SU(2) invariance
 - ▶ same coupling for $\bar{b}sZ'$ (considered in our work). For $b \rightarrow s\mu^+\mu^-$, effects from $\bar{b}sZ'$ is dominated)
 - ▶ SU(2) is constructed in the interaction eigenstate. However, the rotation matrices from the interaction to the mass eigenstate are different for b_L and t_L . Therefore, the couplings of $\bar{b}sZ'$ and $\bar{t}cZ'$ could be different and should depend on the flavour structure of the UV theory.
 - ▶ In the case of a light Z' (e.g., $m_{Z'} < \mu_{\text{EW}}$), the $\bar{t}cZ'$ could be an effective interaction and SU(2) can be broken

Future works

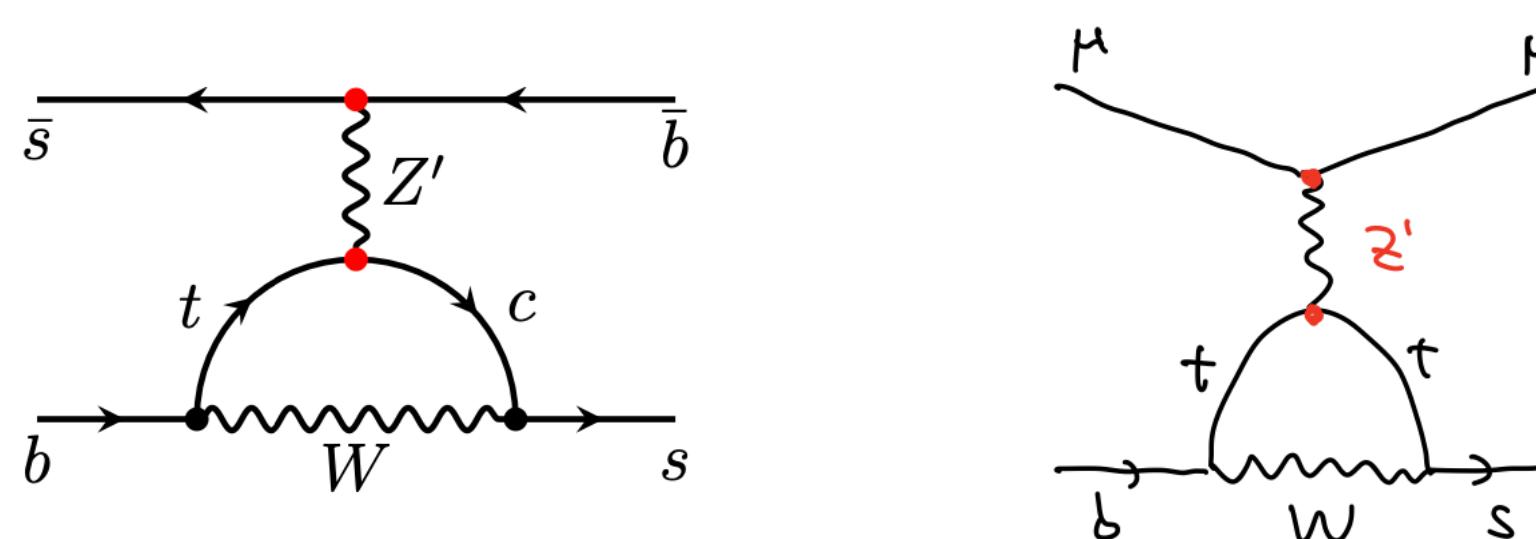
- ▶ UV complete model | (ultra) light Z' | e^+e^-Z' | detailed collider simulation

Flavour anomalies: theoretical interpretation

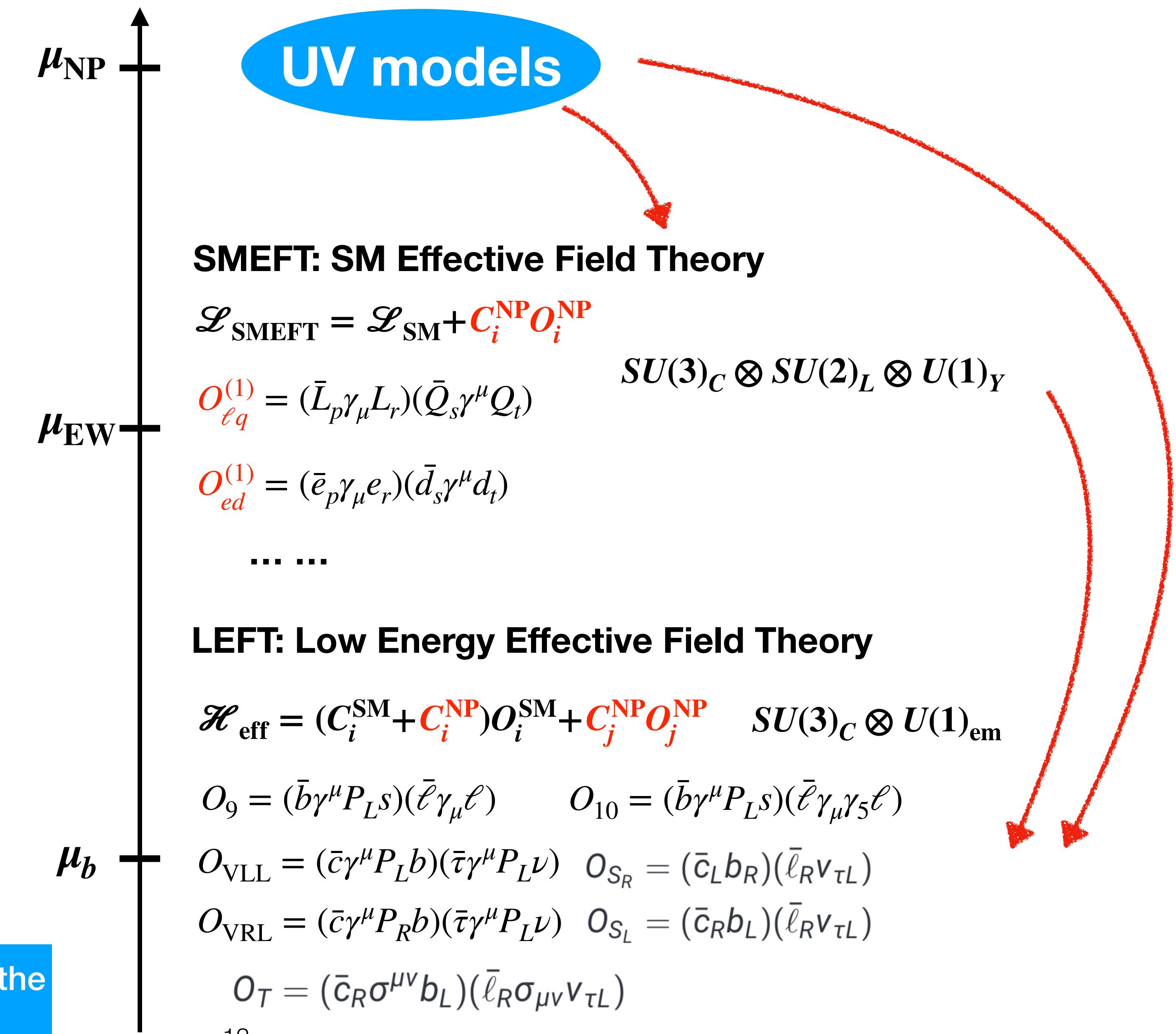
► $b \rightarrow s\ell^+\ell^-$ anomalies



► New possibility ?



Explain $b \rightarrow s\ell^+\ell^-$ by the NP without FCNC ?



Top-philic Z' model

J. F. Kamenik, Y. Soreq, J. Zupan, PRD97 (3) (2018) 035002
 P. J. Fox, I. Low, Y. Zhang, JHEP 03 (2018) 074

- ▶ Gauge group: $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y \otimes U(1)'$
- ▶ New fermions: vector-like top partner $U'_{L,R} \sim (3,1,2/3,q_t)$
- ▶ Lagrangian: quark sector

$$\begin{aligned}\mathcal{L}_{\text{int}} = & (\lambda_H \bar{Q}_{3L} \tilde{H} u_{3R} + \lambda_\Phi \bar{U}'_L u_{3R} \Phi + \mu \bar{U}'_L U'_R + \text{h.c.}) \\ & + q_t g_t (\bar{U}'_L \gamma^\mu U'_L + \bar{U}'_R \gamma^\mu U'_R) Z'_\mu,\end{aligned}$$

Comments

- ▶ interaction eigenstates
- ▶ Assuming only 3rd-gen SM quarks mix with the top partner
- ▶ Vector-like top partner + Z'

Rotation from the interaction to the mass eigenstate

$$\begin{pmatrix} t_L \\ T_L \end{pmatrix} = \begin{pmatrix} \cos \theta_L & -\sin \theta_L \\ \sin \theta_L & \cos \theta_L \end{pmatrix} \begin{pmatrix} u_{3L} \\ U'_L \end{pmatrix}$$

$$\begin{pmatrix} t_R \\ T_R \end{pmatrix} = \begin{pmatrix} \cos \theta_R & -\sin \theta_R \\ \sin \theta_R & \cos \theta_R \end{pmatrix} \begin{pmatrix} u_{3R} \\ U'_R \end{pmatrix}$$

mass

interaction

$$\tan \theta_L = \frac{m_t}{m_T} \tan \theta_R$$

Interactions

$$\mathcal{L}_\gamma = \frac{2}{3} e \bar{t} \not{A} t + \frac{2}{3} e \bar{T} \not{A} T, \quad (7)$$

$$\mathcal{L}_W = \frac{g}{\sqrt{2}} V_{td_i} (c_L \bar{t} \not{W} P_L d_i + s_L \bar{T} \not{W} P_L d_i) + \text{h.c.}, \quad (8)$$

$$\begin{aligned}\mathcal{L}_Z = & \frac{g}{c_W} (\bar{t}_L, \bar{T}_L) \begin{pmatrix} \frac{1}{2} c_L^2 - \frac{2}{3} s_W^2 & \frac{1}{2} s_L c_L \\ \frac{1}{2} s_L c_L & \frac{1}{2} s_L^2 - \frac{2}{3} s_W^2 \end{pmatrix} \not{Z} \begin{pmatrix} t_L \\ T_L \end{pmatrix} \\ & + \frac{g}{c_W} (\bar{t}_R, \bar{T}_R) \left(-\frac{2}{3} s_W^2 \right) \not{Z} \begin{pmatrix} t_R \\ T_R \end{pmatrix},\end{aligned} \quad (9)$$

$$\begin{aligned}\mathcal{L}_{Z'} = & q_t g_t (\bar{t}_L, \bar{T}_L) \begin{pmatrix} s_L^2 & -s_L c_L \\ -s_L c_L & c_L^2 \end{pmatrix} \not{Z}' \begin{pmatrix} t_L \\ T_L \end{pmatrix} \\ & + (L \rightarrow R),\end{aligned} \quad (10)$$

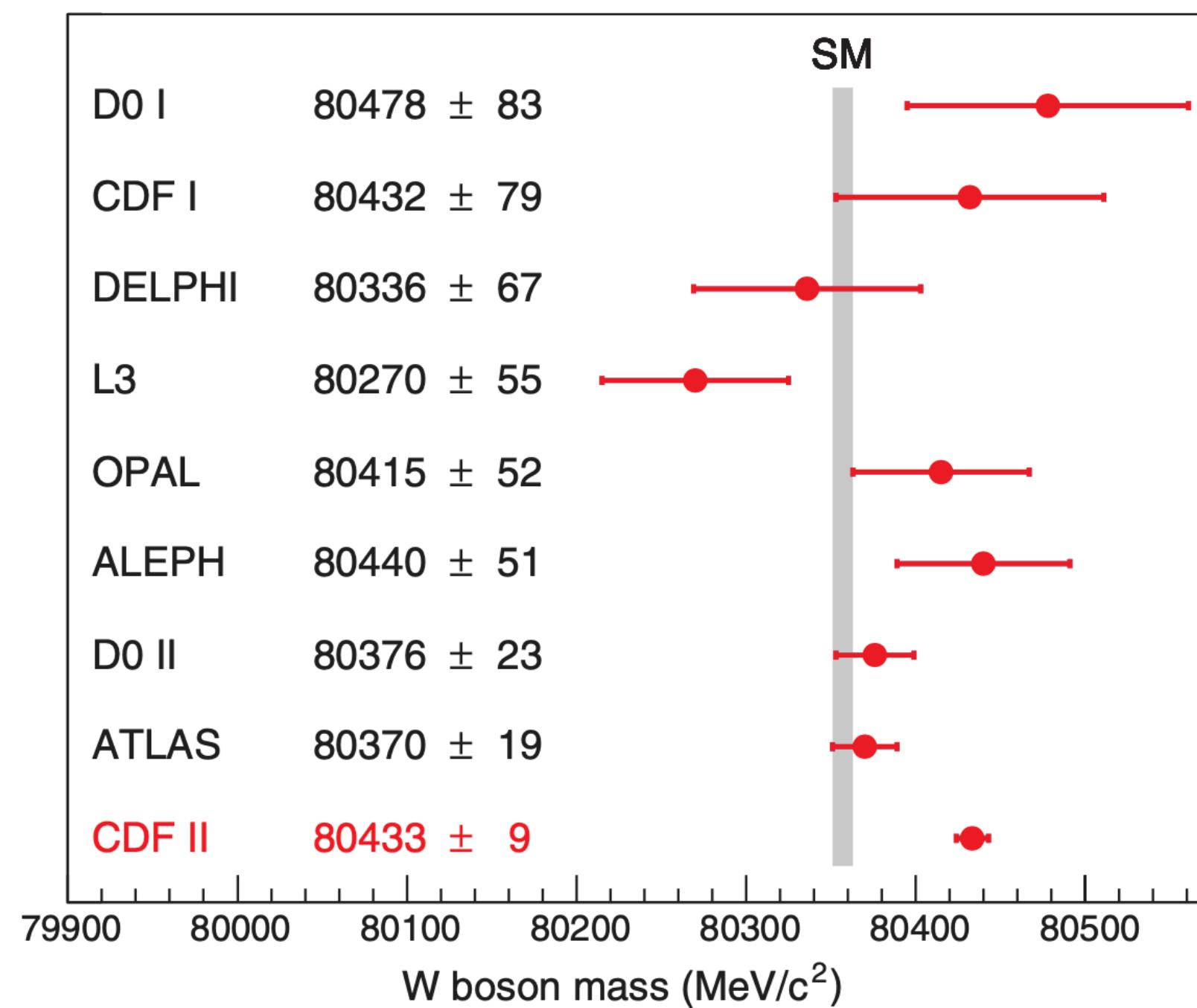
Lagrangian: lepton section

$$\mathcal{L}_\mu = \bar{\mu} \not{Z}' (g_\mu^L P_L + g_\mu^R P_R) \mu$$

NP parameters

$$(\cos \theta_L, m_T, g_\mu^L, g_\mu^R, g_t, q_t, m_{Z'})$$

W-boson mass shift and oblique parameters



CDF: $80433 \pm 9 \text{ GeV}$

EW fit: $80357 \pm 6 \text{ GeV}$

About 7σ deviation !!!

PDG: $80387 \pm 12 \text{ GeV}$

LHCb: $80354 \pm 31 \text{ GeV}$ LHCb, JHEP01(2022)036

Global EW fit

- Most NP effects on the EW sector can be parameterized by S, T, U , e.g.,

$$\Delta m_W^2 = \frac{\alpha c_W^2 m_Z^2}{c_W^2 - s_W^2} \left[-\frac{S}{2} + c_W^2 T + \frac{c_W^2 - s_W^2}{4s_W^2} U \right]$$

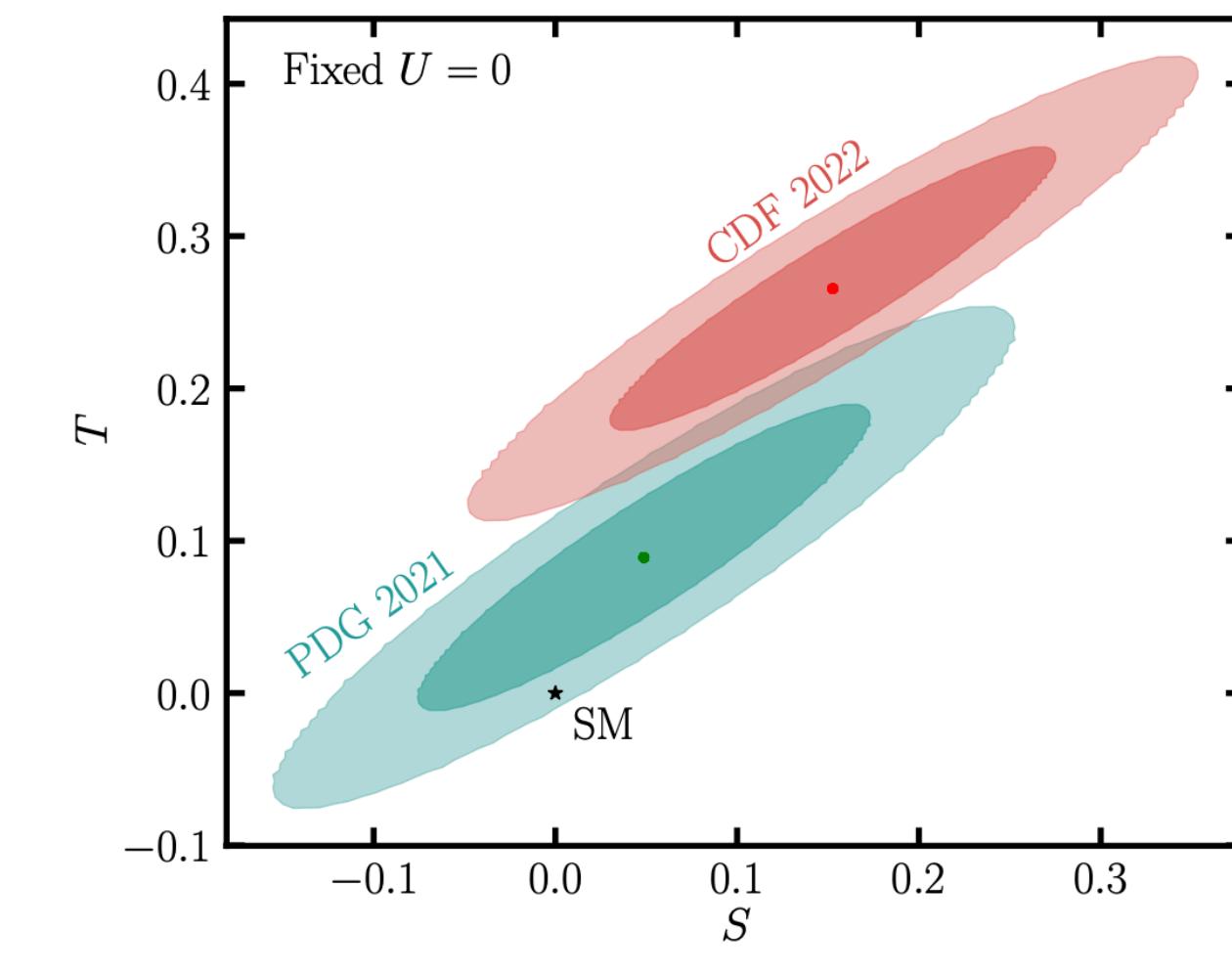
- S, T, U are related to the vacuum polarization of gauge bosons

$$S = \frac{4s_W^2 c_W^2}{\alpha_e} \left[\frac{\Pi_{ZZ}(m_Z^2) - \Pi_{ZZ}(0)}{m_Z^2} - \frac{c_W^2 - s_W^2}{s_W c_W} \Pi'_{Z\gamma}(0) - \Pi'_{\gamma\gamma}(0) \right],$$

$$T = \frac{1}{\alpha_e} \left[\frac{\Pi_{WW}(0)}{m_W^2} - \frac{\Pi_{ZZ}(0)}{m_Z^2} \right],$$

$$U = \frac{4s_W^2}{\alpha_e} \left[\frac{\Pi_{WW}(m_W^2) - \Pi_{WW}(0)}{m_W^2} - \frac{c_W}{s_W} \Pi'_{Z\gamma}(0) - \Pi'_{\gamma\gamma}(0) \right] - S,$$

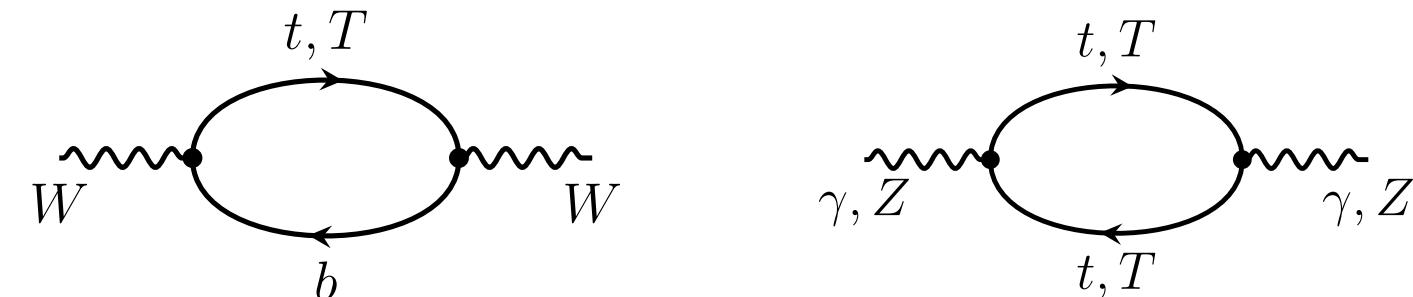
- A global EW fit is needed to explaination of the CDF m_W shift



W-boson mass shift and oblique parameters

Explanation in top-philic Z' scenario

- NP contributions to vacuum polarizations



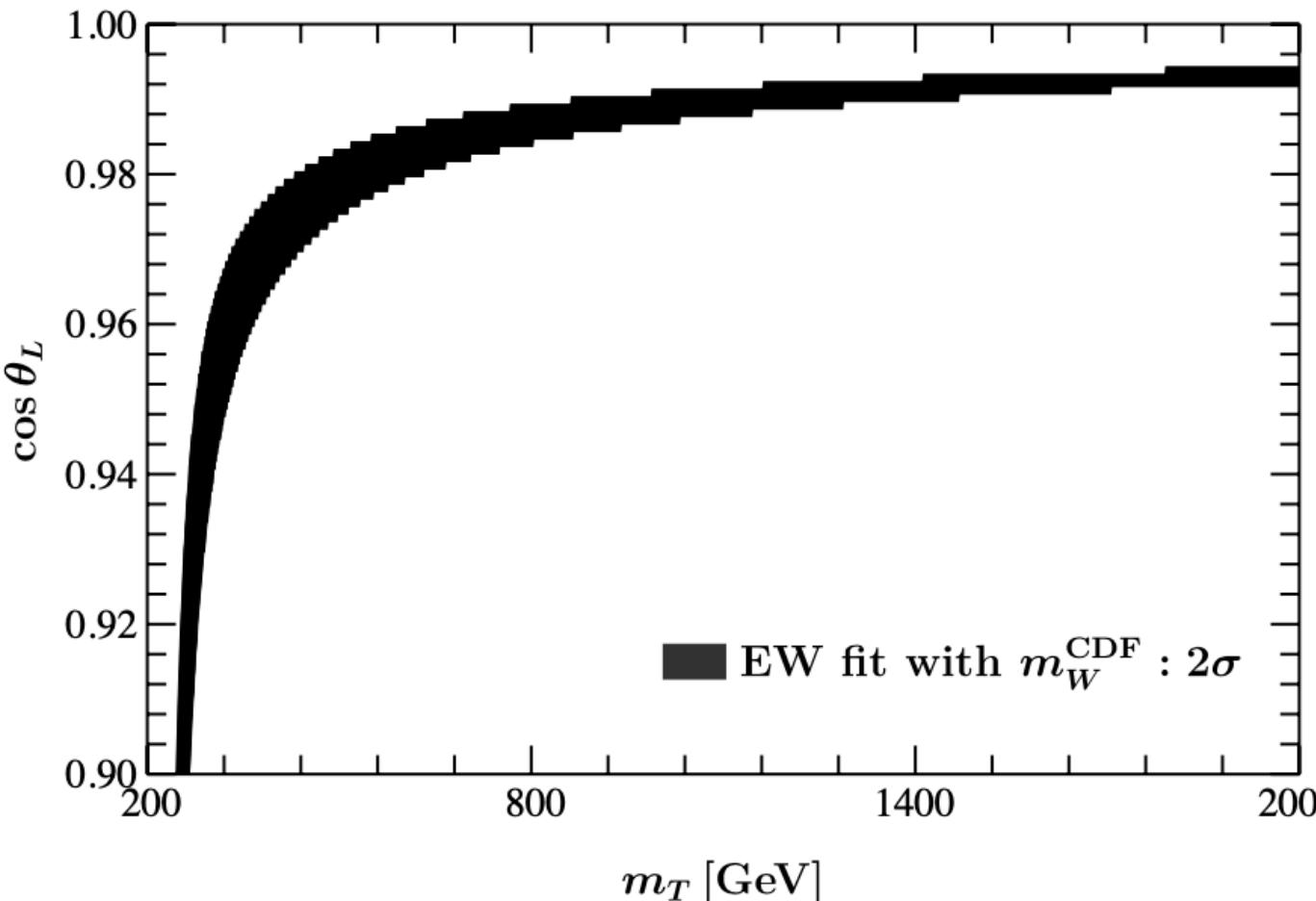
- S, T, U are affected

$$S_T = \frac{s_L^2}{12\pi} \left[K_1(y_t, y_T) + 3c_L^2 K_2(y_t, y_T) \right],$$

$$T_T = \frac{3s_L^2}{16\pi s_W^2} \left[x_T - x_t - c_L^2 \left(x_T + x_t + \frac{2x_t x_T}{x_T - x_t} \ln \frac{x_t}{x_T} \right) \right]$$

$$U_T = \frac{s_L^2}{12\pi} \left[K_3(x_t, y_t) - K_3(x_T, y_T) \right] - S,$$

- Allowed parameter space



- ★ m_W^{CDF} can be explained by the top-parter effects
- ★ small θ_L is allowed

Global EW fit

- Most NP effects on the EW sector can be parameterized by S, T, U , e.g.,

$$\Delta m_W^2 = \frac{\alpha c_W^2 m_Z^2}{c_W^2 - s_W^2} \left[-\frac{S}{2} + c_W^2 T + \frac{c_W^2 - s_W^2}{4s_W^2} U \right]$$

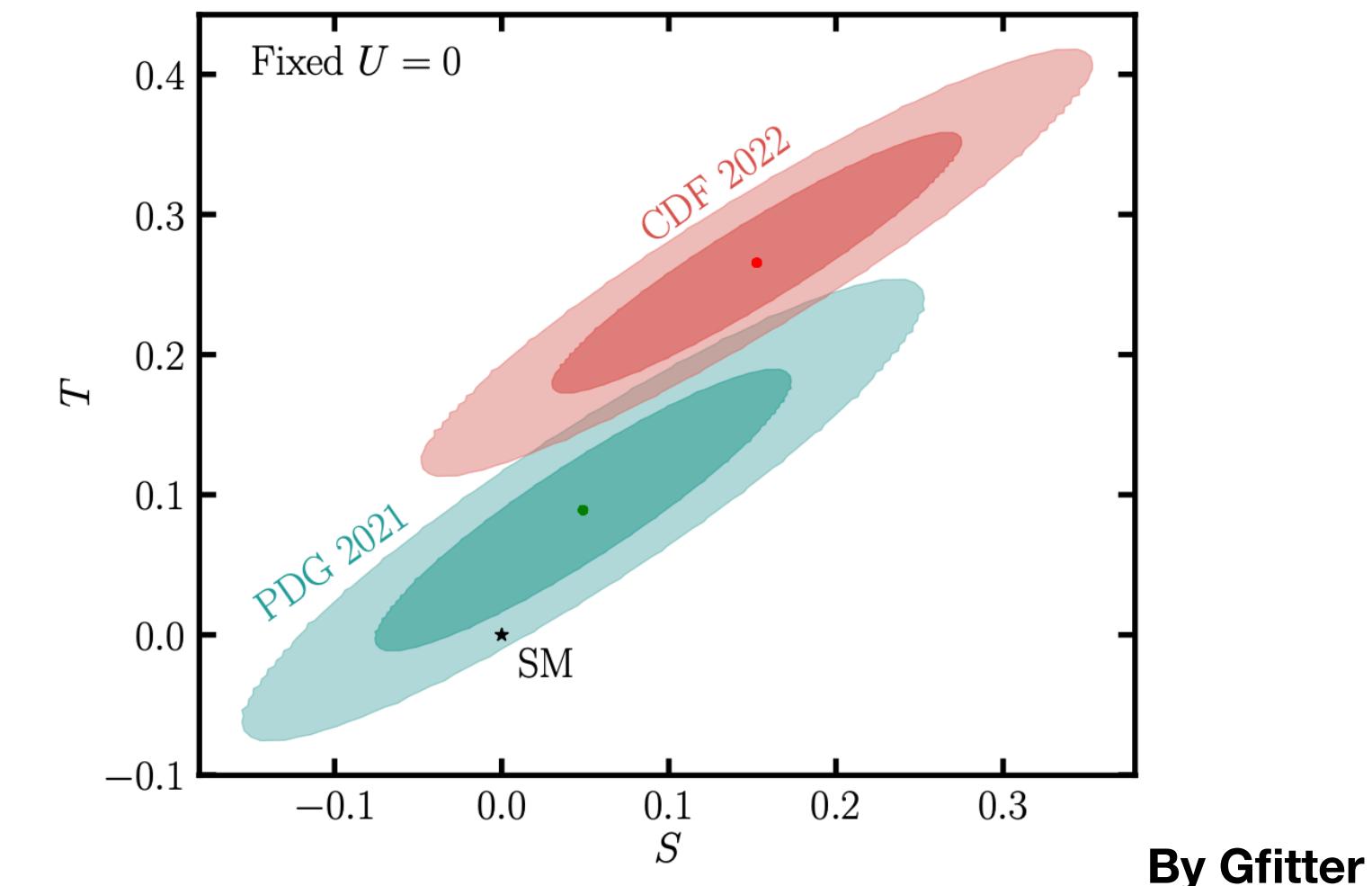
- S, T, U are related to the vacuum polarization of gauge bosons

$$S = \frac{4s_W^2 c_W^2}{\alpha_e} \left[\frac{\Pi_{ZZ}(m_Z^2) - \Pi_{ZZ}(0)}{m_Z^2} - \frac{c_W^2 - s_W^2}{s_W c_W} \Pi'_{Z\gamma}(0) - \Pi'_{\gamma\gamma}(0) \right],$$

$$T = \frac{1}{\alpha_e} \left[\frac{\Pi_{WW}(0)}{m_W^2} - \frac{\Pi_{ZZ}(0)}{m_Z^2} \right],$$

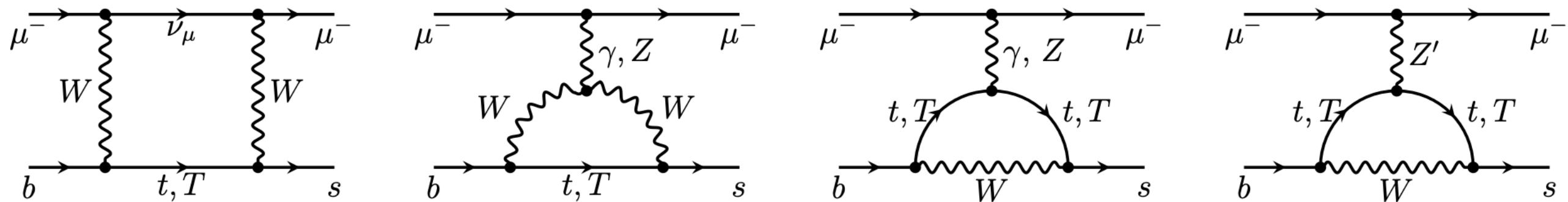
$$U = \frac{4s_W^2}{\alpha_e} \left[\frac{\Pi_{WW}(m_W^2) - \Pi_{WW}(0)}{m_W^2} - \frac{c_W}{s_W} \Pi'_{Z\gamma}(0) - \Pi'_{\gamma\gamma}(0) \right] - S,$$

- A global EW fit is needed to explanation of the CDF m_W shift



$b \rightarrow s\ell^+\ell^-$ anomalies

► NP contributions



► Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} \supset -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha}{4\pi} (\mathcal{C}_9^\mu \mathcal{O}_9^\mu + \mathcal{C}_{10}^\mu \mathcal{O}_{10}^\mu) + \text{h.c.},$$

► Wilson coefficients

$$\mathcal{C}_9^{\text{NP}} = s_L^2 I_1 + s_L^2 \left(1 - \frac{1}{4s_W^2}\right) (I_2 + c_L^2 I_3) + \Delta \mathcal{C}_+^{Z'}$$

$$\mathcal{C}_{10}^{\text{NP}} = \frac{s_L^2}{4s_W^2} (I_2 + c_L^2 I_3) + \Delta \mathcal{C}_-^{Z'},$$

$$\Delta \mathcal{C}_\pm^{Z'} = \frac{(g_L \pm g_R) q_t g_t}{e^2} \frac{m_W^2}{m_{Z'}^2} c_L^2 s_R^2 \left(I_4 - \frac{c_L^2}{c_R^2} I_5\right)$$

★ The W -box, γ - and Z - penguin diagrams are highly suppressed (proportional to $\sin^2 \theta_L$)

★ The Z' penguins do not suffer from this suppression and may affect the $b \rightarrow s\ell^+\ell^-$ processes

► NP parameters

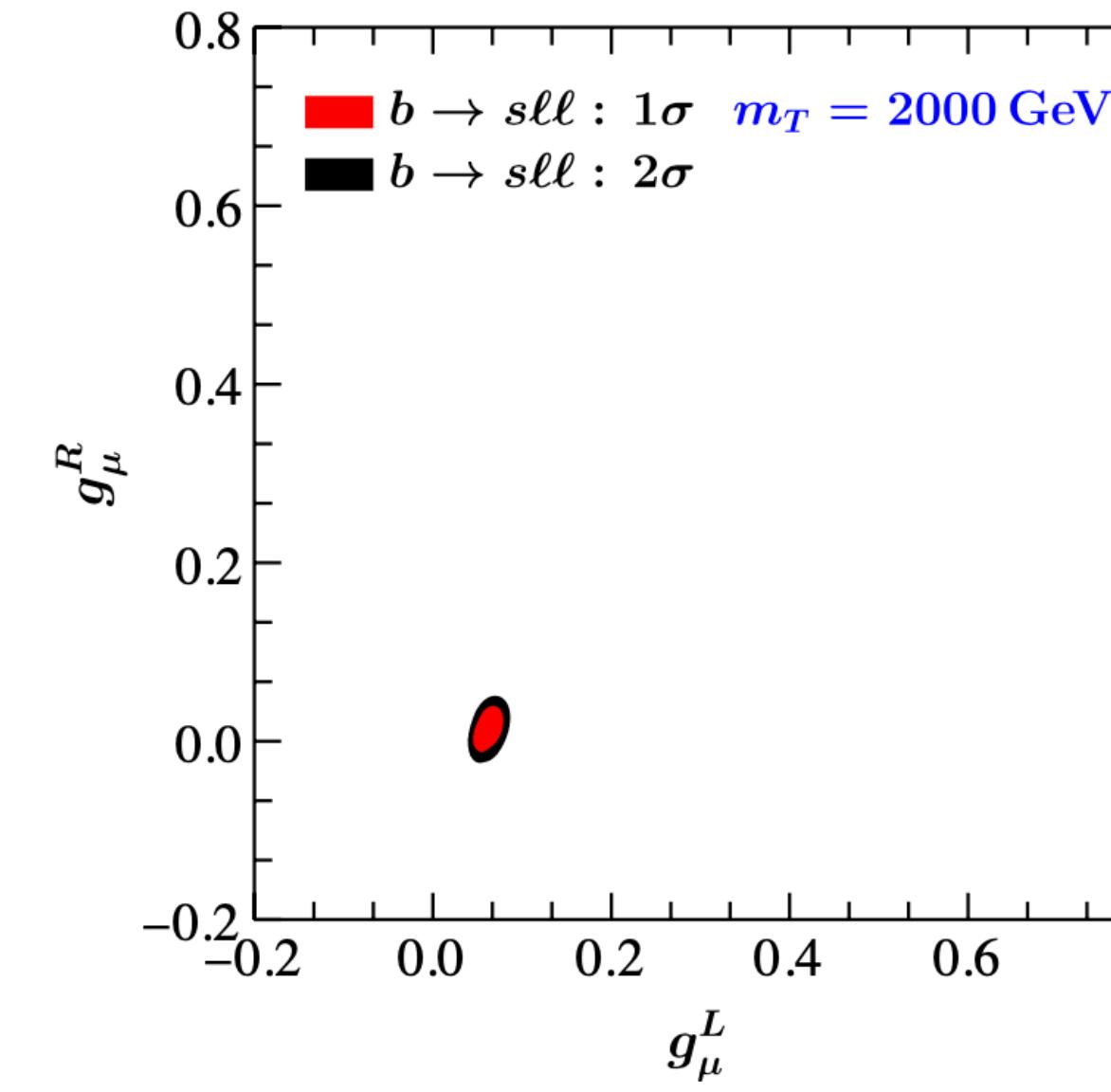
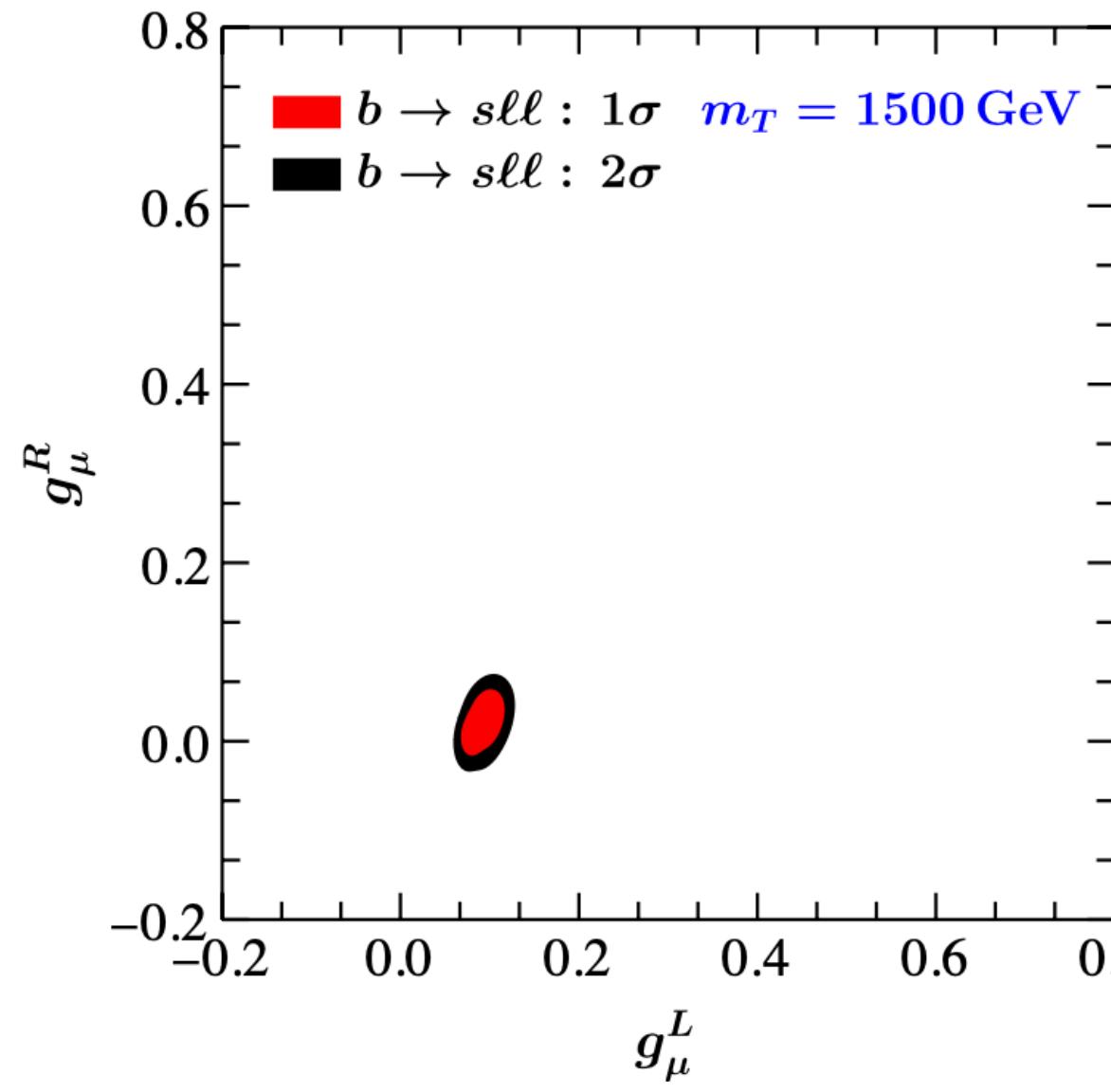
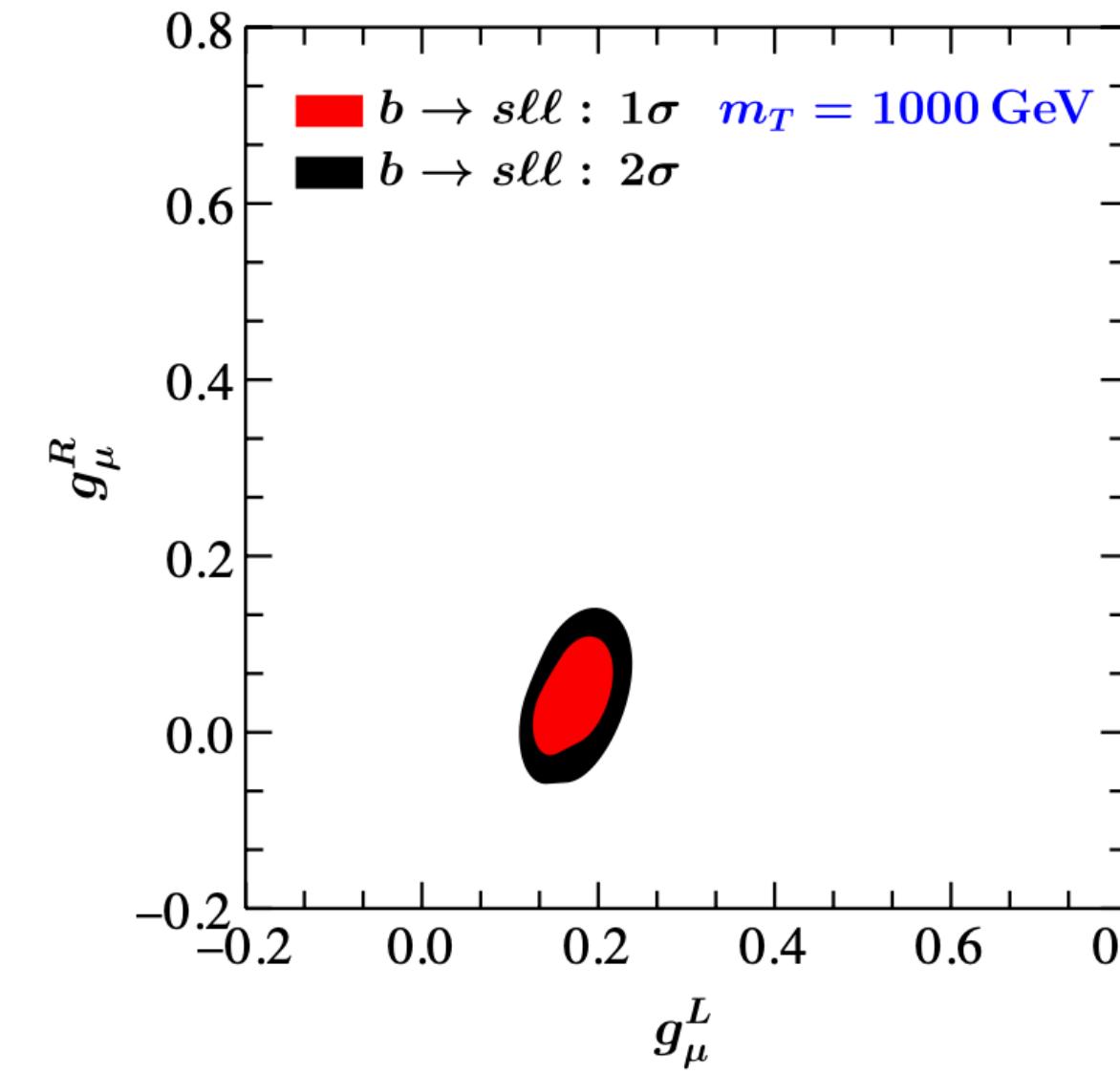
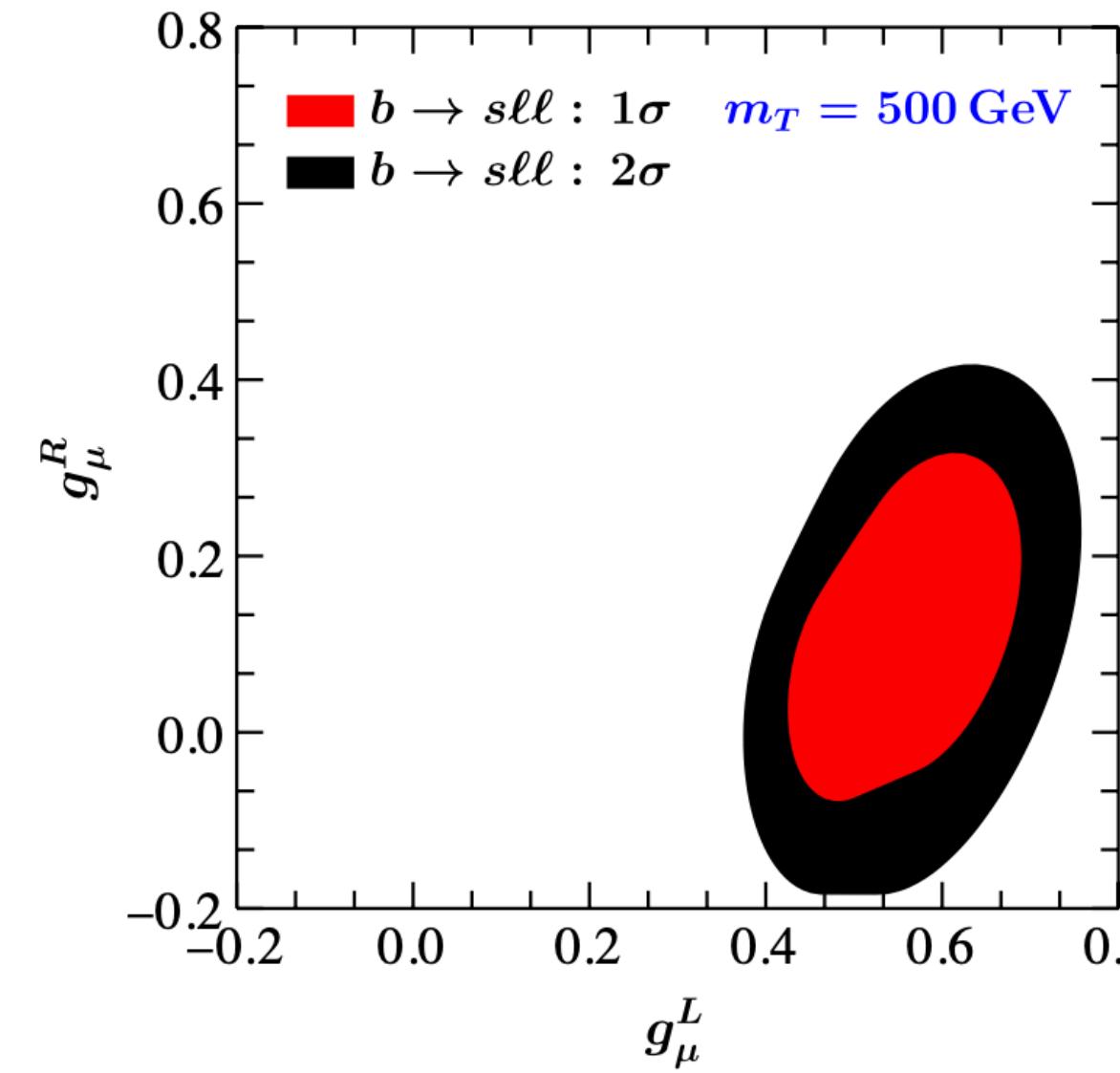
$$\left(\cos \theta_L, m_T, \frac{q_t g_t g_\mu^{L,R}}{m_{Z'}^2} \right)$$

Without loss of generality

$$q_t = 1, g_t = 1, m_{Z'} = 200 \text{ GeV}$$

$$(\cos \theta_L, m_T, g_\mu^L, g_\mu^R)$$

$b \rightarrow s\ell^+\ell^-$ anomalies and the CDF m_W shift



- ▶ $b \rightarrow s\ell^+\ell^-$ ($\cos \theta_L, m_T, g_\mu^L, g_\mu^R$)
- ▶ m_W shift ($\cos \theta_L, m_T$)

★ m_W^{CDF} and $b \rightarrow s\ell^+\ell^-$ anomalies simultaneously explained at 2σ level
 ★ the couplings are safely in the perturbative region

Constraints on (g_μ^L, g_μ^R) from the $b \rightarrow s\ell^+\ell^-$ processes, in the 2σ allowed regions of $(\cos \theta_L, m_T)$ obtained from the global EW fit

Summary

Conclusions

- ▶ Oblique parameters S , T , U and Wilson coefficients C_9 and C_{10} calculated in a topophilic Z' model
- ▶ It is found that the model can simultaneously explain the CDF m_W measurement and the $b \rightarrow s\ell^+\ell^-$ anomalies

Issues

- ▶ Lepton sector is NOT UV complete
- ▶ Top partner mixing with 1st and 2nd generation is also possible
- ▶ Z' contributions to the global EW fit is not included
- ▶ Naturalness from the top partner not discussed

G.C. Branco et al, arXiv:2103.13409

J. Berger, J. Hubisz and M. Perelstein, arXiv: 1205.0013

Future works

- ▶ UV complete model | Z' contributions to EW fit | mixing with 1st and 2nd gen | Nautralness
- ▶ detailed collider simulation

谢谢