

R value measurement at BESIII

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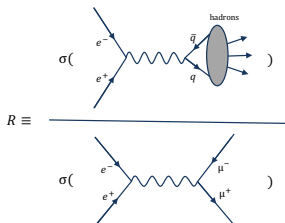
2022 年 8 月 11 日 辽宁师范大学 大连

Definition of R value

The R value is defined as the leading-order production cross section ratio of hadron and muon pairs in the electron-positron annihilation:

$$R \equiv \frac{\sigma^0(e^+e^- \rightarrow \text{hadrons})}{\sigma^0(e^+e^- \rightarrow \mu^+\mu^-)} \equiv \frac{\sigma_{\text{had}}^0}{\sigma_{\mu\mu}^0}$$

That is, according to QCD,



A direct result from the QED theory:

$$\sigma_{\mu\mu}^0(s) = \frac{4\pi\alpha^2}{3s} \frac{\beta_\mu(3 - \beta_\mu^2)}{2}, \quad \text{with } \beta_\mu = \sqrt{1 - 4m_\mu^2/s}$$

Running of QED coupling constant: $\Delta\alpha(s)$

The contributions to $\Delta\alpha(s)$ can be distinguished to three pieces:

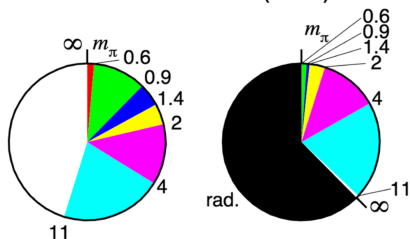
$$\Delta\alpha(s) = 1 - \alpha(0)/\alpha(s) = \Delta\alpha_{\text{lepton}}(s) + \Delta\alpha_{\text{had}}^{(5)}(s) + \Delta\alpha_{\text{top}}(s)$$

- $\Delta\alpha_{\text{lepton}}(s)$ can be calculated analytically using the perturbative theory.
- Since the top quark is heavy, $\Delta\alpha_{\text{top}}(s)$ is small ($10^{-7} \sim 10^{-10}$ for BESIII region).
- $\Delta\alpha_{\text{had}}^{(5)}(s)$ should be calculated by using the R value:

$$\Delta\alpha_{\text{had}}^{(5)}(s) = -\frac{\alpha s}{3\pi} \text{Re} \int_{E_{\text{th}}}^{\infty} ds' \frac{R(s')}{s'(s' - s - i\epsilon)}$$

Fractional contribution to $\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$:

Phys. Rev. D 97, 114025 (2018)
value (error)²



Eur. Phys. J. C 80, 241 (2020)

Source	Contribution ($\times 10^{-4}$)
$\Delta\alpha_{\text{lepton}}(M_Z^2)$	314.979 ± 0.002
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$	276.0 ± 1.0
$\Delta\alpha_{\text{top}}(M_Z^2)$	-0.7180 ± 0.0054

$\Delta\alpha_{\text{had}}^{(5)}(s)$ is sensitive with the R value over all energy region!

Muon anomalous magnetic moment: a_μ

- Magnetic moment of the muon: $\vec{\mu} = g_\mu \frac{e}{2m_\mu} \vec{S}$

- Dirac theory: $g_\mu = 2$ \Rightarrow Quantum Field Theory: $a_\mu = \frac{|g_\mu - 2|}{2} \Rightarrow$ **Muon Anomaly**

Anomalous Magnetic Moment:

- Standard model prediction:

$$a_\mu^{\text{SM}} = a_\mu^{\text{QED}} + a_\mu^{\text{QCD}} + a_\mu^{\text{weak}}$$

Phys. Rep. 887, 1 (2020)

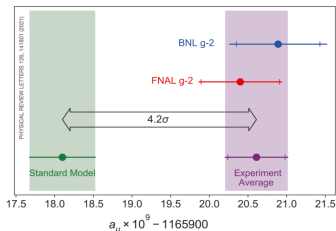
- Direct measurement

(Exp. average BNL & FNAL)

Phys. Rev. Lett. 126, 141801 (2021)

\Rightarrow **Discrepancy of 4.2σ**

- Hadronic contributions dominate uncertainty of a_μ^{SM}
 - Hadronic Light-by-Light Scattering (HLbL) & **Hadronic Vacuum Polarization (HVP)**



The HVP contribution, i.e., $a_\mu^{\text{LO-HVP}}$, is calculated with **R value** by using **dispersion relation**:

$$a_\mu^{\text{LO-HVP}} = \left(\frac{\alpha m_\mu}{3\pi} \right)^2 \int_{4m_\pi^2}^{\infty} ds \frac{R(s)K(s)}{s^2}$$

$E_{\text{beam}}: 1.0 - 2.45 \text{ GeV}$
 $\sigma_E: 5.16 \times 10^{-4}$
 $L: 1.0 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1} @3770$

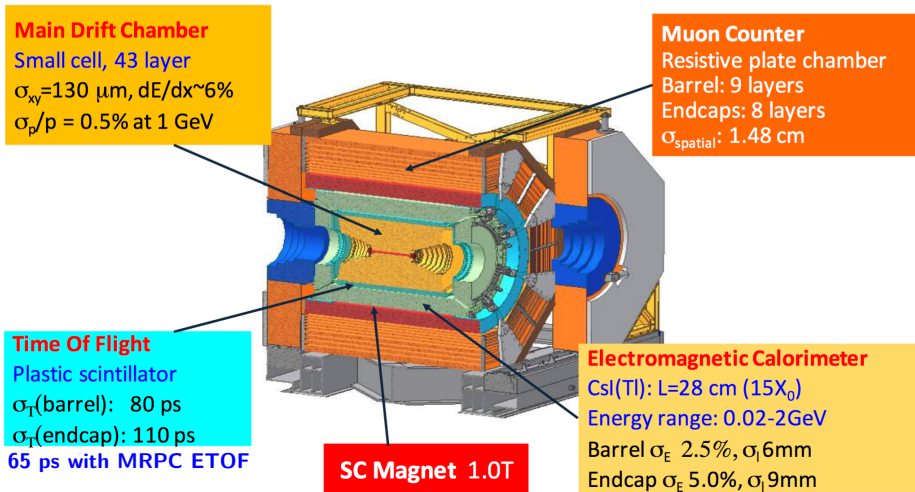
Linac

BES

Storage ring

Quarks	u up	c charm	t top
	d down	s strange	b bottom
	ν_e e- neutrino	ν_μ μ - neutrino	ν_τ τ - neutrino
Leptons	e electron	μ muon	τ tau
	I	II	III
	Three Generations of Matter		

BEPC = Beijing Electron Positron Collider



BESIII = Beijing Spectrometer III

Determination of R value in experiment

Experimentally, the R value is determined by

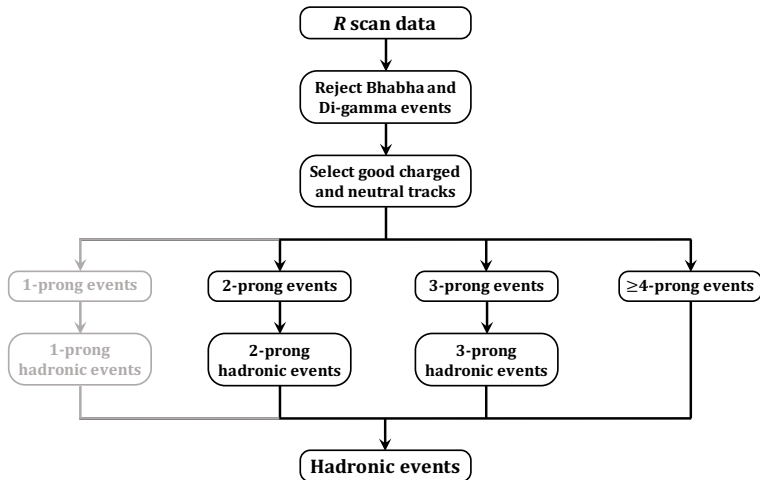
$$R = \frac{N_{\text{had}}^{\text{obs}} - N_{\text{bkg}}}{\sigma_{\mu\mu}^0 \mathcal{L}_{\text{int.}} \varepsilon_{\text{trig}} \varepsilon_{\text{had}} (1 + \delta)}$$

- $N_{\text{had}}^{\text{obs}}$: Numbers of observed hadronic events.
- N_{bkg} : Number of the residual background events.
- $\sigma_{\mu\mu}^0$ (s) = 86.85 nb/s: Leading order QED cross section for $e^+e^- \rightarrow \mu^+\mu^-$.
- $\mathcal{L}_{\text{int.}}$: Integrated luminosity is measured by analyzing Bhabha events.
- $\varepsilon_{\text{trig}}$: Trigger efficiency $\sim 100\%$.
- ε_{had} : Detection efficiency of the hadronic events.
- $(1 + \delta)$: ISR correction factor.

► **Determination of ε_{had} is the most challenging task!**

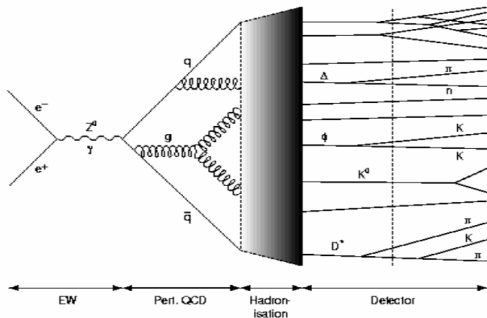
► **Two different signal simulation models are developed and investigated intensively.**

Analysis strategy



Nominal signal simulation model: LUARLW

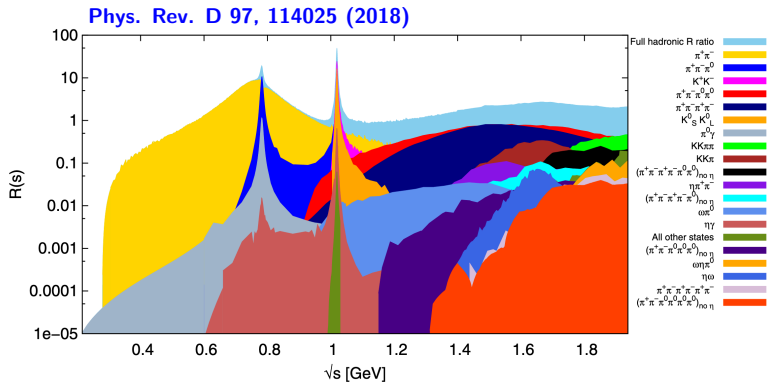
Hadronization procedure in electron-positron annihilation:



Main features of the **LUARLW** model:

- ▶ A self-consistent inclusive generator developed based on **JETSET**.
- ▶ **Initial-state radiation (ISR)** process is implemented with the **Feynman diagram** scheme.
- ▶ Kinematic quantities of initial hadrons are sampled by the **Lund area law**.
- ▶ Phenomenological parameters are tuned based on comparisons between data and MC.

Alternative model: first exclusive attempt in R analysis



The main features of the **HYBRID** model:

- Combination of **THREE** well-established models: **CONEXC**, **PHOKHARA**, and **LUARLW**.
- As much as currently known **experimental knowledges** are implemented.
- Different **ISR** and **VP** correction schemes from the nominal ones are adopted.

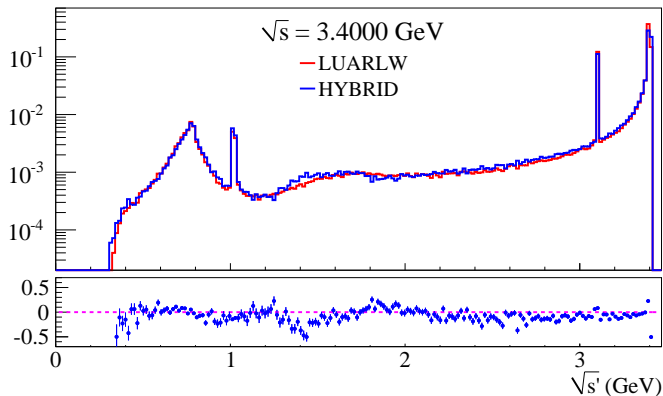
Construction of the HYBRID model

- The **structure function scheme** is used to simulate the ISR process in **CONEXC**.
- **PHOKHARA** is used to simulate **10** exclusive processes with known cross sections and intermediate states, $e^+e^- \rightarrow 2\pi, 3\pi, 4\pi$ etc..
- **CONEXC** simulates **47** exclusive processes with known cross sections according to **PHSP** model, such as $e^+e^- \rightarrow K^+K^-\pi^0, K_S^0K^\pm\pi^\mp, K^+K^-\pi\pi, 5\pi, 6\pi$ and $\gamma_{\text{ISR}}J/\psi$.
- As much as exclusive channels containing intermediate states are implemented in the **CONEXC** with their contributions to the related inclusive channels are excluded.
- **LUARLW** model is partially used to simulate remain unknown processes, in which a set of chosen parameters are tuned after comparing **HYBRID simulations** with data.
- Processes simulated by **PHOKHARA** or **CONEXC** are prohibited in **LUARLW** to avoid excessive generation of some specific processes.
- The residual double-generatings among the three components are **negligible**.

A lot of efforts have gone into engineering the HYBRID generator!

Comparison in truth level

The effective energy ($\sqrt{s'}$) spectra of LUARLW and HYBRID after ISR process



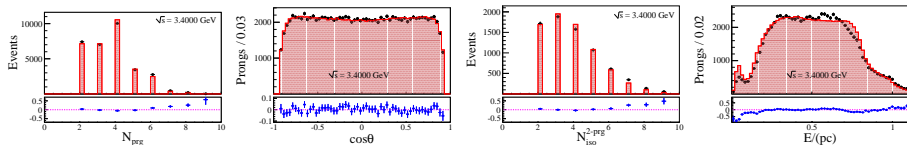
- In LUARLW and HYBRID, the ISR process is simulated in **different** ways.
- The $\sqrt{s'}$ spectrum directly reflect the **fraction** of the ISR-returned processes.
- **These two different simulation schemes result in consistent $\sqrt{s'}$ spectrum!**

Comparison in observable level

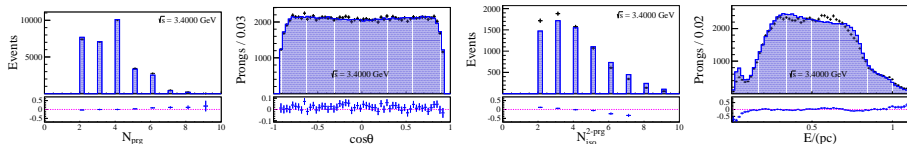
Comparison between MC and data in a few observables:

- N_{prg} : the number of detected the good charged tracks (**prong**).
- $\cos\theta$, E , and p : polar angle, deposited energy in EMC, and measured momentum in MDC.
- $N_{\text{iso}}^{2\text{-prg}}$: the number of isolated photons of two-prong events.

LUARLW



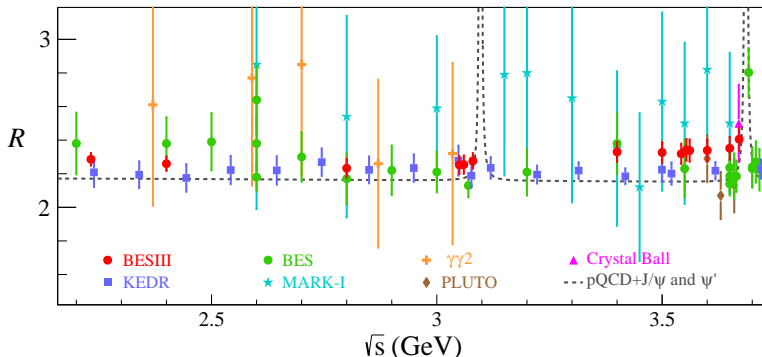
HYBRID



Both the two simulation models give good consistency with data!

Measured R values between 2.2 ~ 3.7 GeV

Comparing BESIII R values with previously published results:

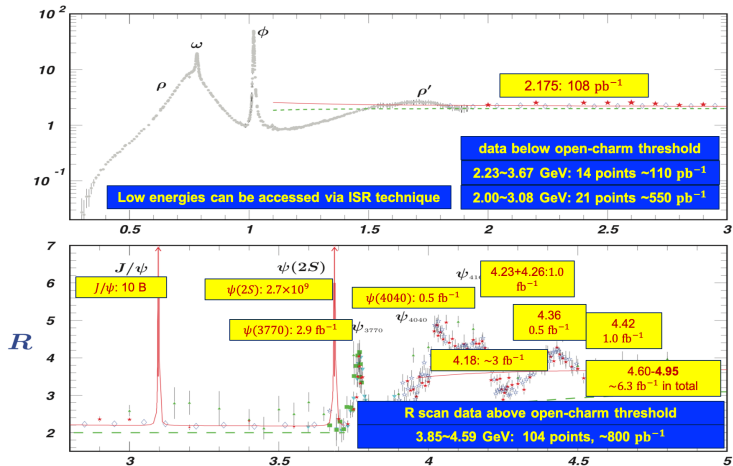


► The accuracy is better than 2.6% below 3.1 GeV and 3.0% above.

► Larger than the pQCD prediction by 2.7σ between 3.4 ~ 3.6 GeV:

- Larger $a_{\mu}^{\text{LO-HVP}}$ which is close to a_{μ} calculated by the lattice QCD
- Contributions from new, long-lived neutral hadrons? [[arXiv:2206.13460](https://arxiv.org/abs/2206.13460)].

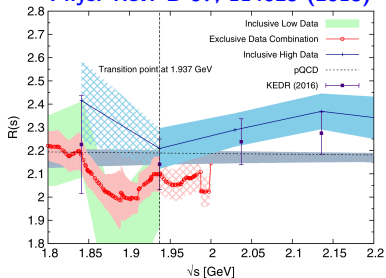
More measurements using the BESIII data



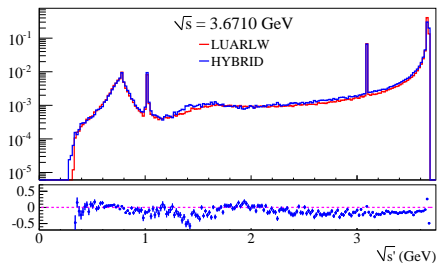
- ▶ BESIII collected data from 2.00 to 4.95 GeV, which can be used for the R measurement.
- ▶ R measurement in the continuum and open-charm regions has significant impacts.

Different methods and different physics?

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The \sqrt{s} spectrum after ISR at 3.67 GeV



- ▶ R measured **inclusively** and **exclusively** at or below 2.0 GeV, and a comparison between them would be interesting.
- ▶ R measured via the **ISR technique** taking advantage of **BESIII $\psi(3770)$ data** and the **HYBRID model**, the R value from $\pi^+\pi^-$ threshold to continuum region can be accessed.
- ▶ Both of these two attempts will contribute to understanding the **discrepancy of muon anomaly** between SM calculation and experiment measurement.

总结

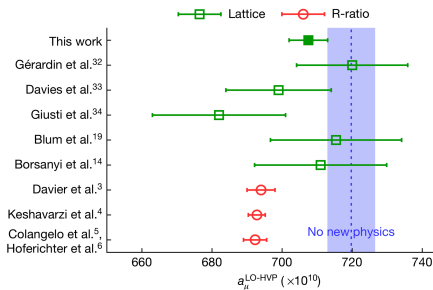
- 实验上不断提高 R 值的精度对检验标准模型，尤其是理解当前与缪子反常磁矩有关的疑难问题具有重要意义。
- 基于大量细致的分析和检查，BESIII 测量得到的连续能区的 R 值具有**目前世界上最好的精度和可靠性**。
- BESIII 上正在开展基于不同方法的 R 值测量工作，包括**单举方法**、**遍举方法**以及**ISR 方法**，这些工作将对粒子物理领域提供高质量的基础实验数据。

Thanks for your attention!

Muon anomalous magnetic moment: a_μ

New calculation of $a_\mu^{\text{LO-HVP}}$ from the lattice QCD approach decreases the discrepancy between a_μ^{SM} and a_μ^{exp} :

Nature (London) 593, 51 (2021)



Source	Contribution ($\times 10^{-11}$)
a_μ^{QED}	116584718.931 ± 0.104
a_μ^{Weak}	153.6 ± 1.0
$a_\mu^{\text{LO-HVP}} (R\text{-ratio})$	6931 ± 40
$a_\mu^{\text{LO-HVP}} (\text{lattice})$	7075 ± 55
$a_\mu^{\text{NLO-HVP}}$	-98.3 ± 0.7
$a_\mu^{\text{NNLO-HVP}}$	12.4 ± 0.1
a_μ^{HLbL}	92 ± 18
a_μ^{SM}	116591954 ± 58
a_μ^{exp}	116592061 ± 41
Δa_μ	$107 \pm 71 (1.5\sigma)$

The R -ratio approach still gives the best prediction to $a_\mu^{\text{LO-HVP}}$.

Additional checks on the R value

- Inclusion of one-prong events: R changes by 0.8% at most.
- Exclusion of two-prong events: A maximum of 2.2% differences of R is observed.
- The LUARLW generator is quantitatively checked in a few exclusive channels, by replacing the corresponding production fractions (f) and inclusive efficiencies (ϵ^{inc})
 - ▶ $\pi^+\pi^-$: $f_{2\pi}$ and $\epsilon_{2\pi}^{\text{inc}}$ replaced by that of HYBRID, ϵ_{had} changes by 2.1% at most.
 - ▶ $\pi^+\pi^-\pi^0$: $f_{3\pi}$ and $\epsilon_{3\pi}^{\text{inc}}$ replaced by that of HYBRID, ϵ_{had} changes by 0.6% at most.
 - ▶ $\pi^+\pi^-\pi^+\pi^-$: $f_{4\pi}$ replaced by that extracted from experimental data and $\epsilon_{4\pi}^{\text{inc}}$ by that of HYBRID, ϵ_{had} differs from the nominal value by 1.1% at most.
 - ▶ $\pi^+\pi^-\pi^0\pi^0$: $f_{4\pi}$ replaced by that extracted from experimental data and $\epsilon_{4\pi}^{\text{inc}}$ by that of HYBRID, the resulted differences in ϵ_{had} is less than 0.6%.
 - ▶ $\gamma_{\text{ISR}}J/\psi$: $f_{J/\psi}$ and $\epsilon_{J/\psi}^{\text{inc}}$ replaced by that of HYBRID, the maximum changement in ϵ_{had} is 0.2% at $\sqrt{s} = 3.4$ GeV.

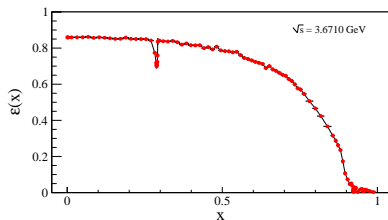
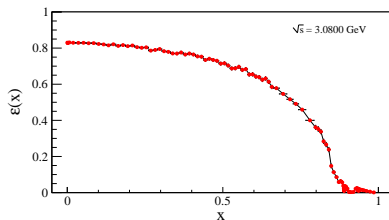
An alternative treatment of ISR process

In previous R measurement works, a different treatment of ISR process is adopted:

$$R = \frac{N_{\text{had}}^{\text{obs}} - N_{\text{bkg}}}{\sigma_{\mu\mu}^0 \mathcal{L}_{\text{int.}} \varepsilon_{\text{trig}} \varepsilon_{\text{had}}(0) (1 + \delta_{\text{obs}})},$$

where the $\varepsilon_{\text{had}}(0)$ stands for the detection efficiency of events without radiating ISR photon.

$$1 + \delta_{\text{obs}} = \frac{\delta_{\text{vert}}}{|1 - \Pi(s)|^2} + \frac{1}{\sigma_{\text{had}}^0(s) \varepsilon_{\text{had}}(0)} \int_0^{x_m} \frac{x^\beta}{x} \left(1 - x + \frac{x^2}{2}\right) \frac{\sigma_{\text{had}}^0(s') \varepsilon_{\text{had}}(x)}{|1 - \Pi(s')|^2} dx.$$



The maximum difference in R value resulted by this treatment is 0.8%.