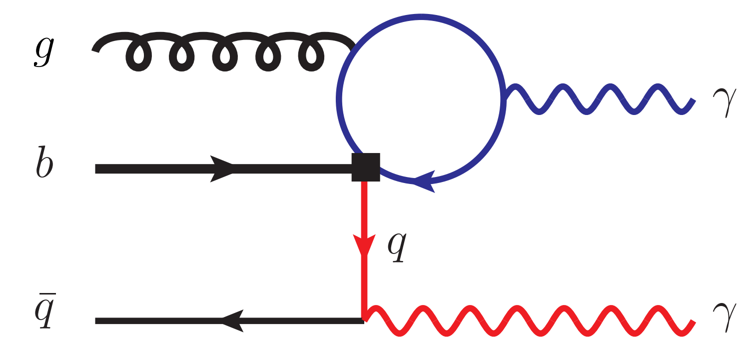

Deciphering the Long-distance Penguin contribution to $B \to \gamma\gamma$ decays

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QQ, Y.-L. Shen, C. Wang, Y.-M. Wang, 2207.02691

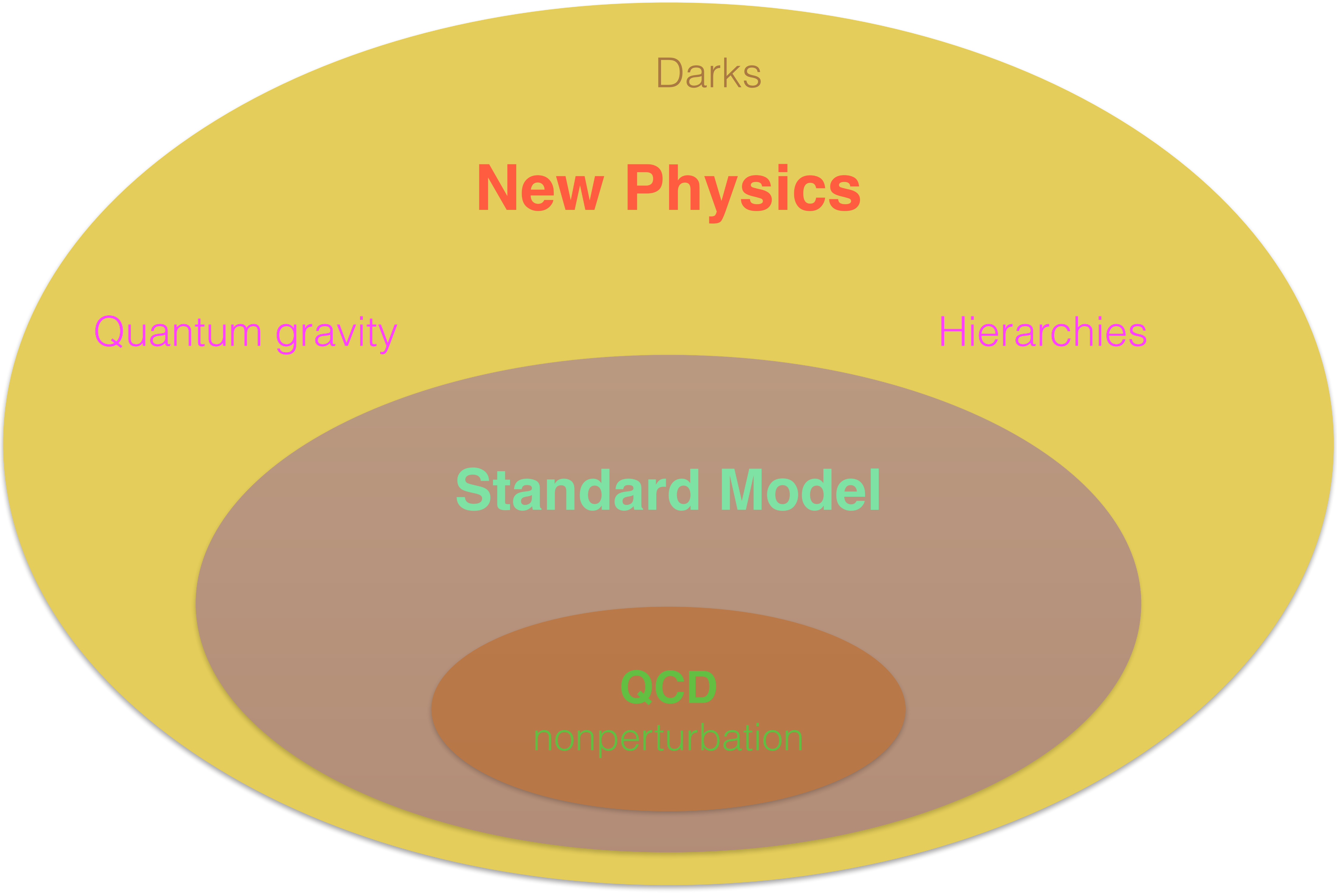
The 4th Workshop of Heavy Flavor Physics and QCD
Changsha, 27-30 July 2022

Contents

- Why $\bar{B} \to \gamma\gamma$?
- History of (1) $\bar{B} \to \gamma\gamma$ and (2) the long-distance penguin contribution
- Factorization of the long-distance penguin contribution

  —— a novel B-meson distribution amplitude
- Numerics
- Summary and Prospects

B decays are important!



Why $\bar{B} \to \gamma\gamma$?

- Sensitive to dynamics beyond the SM (FCNC), e.g. CP violation
- Extraction of the CKM angle γ
- Clean environment to address the intricate strong interaction mechanism of the heavy-meson systems

—— structure of the B meson

Belle II Physics Book

Process	Observable	Theory	Sys. limit (Discovery) [ab^{-1}]	vs LHCb	vs Belle	Anomaly	NP
$B \to X_s l^+ l^-$	R_{X_s}	⋆⋆⋆	>50	⋆⋆⋆	⋆⋆⋆	⋆⋆	⋆⋆⋆
$B \to K^{(*)} e^+ e^-$	$R(K^{(*)})$	⋆⋆⋆	>50	⋆⋆	⋆⋆⋆	⋆⋆⋆	⋆⋆⋆
$B \to X_s \gamma$	$Br.$	⋆⋆	1-5	⋆⋆⋆	⋆	⋆	⋆⋆
$B_{d,(s)} \to \gamma\gamma$	$Br., A_{\rm CP}$	⋆⋆	> 50(5)	⋆⋆	⋆⋆	-	⋆⋆
$B \to K^* e^+ e^-$	P_5'	⋆⋆	>50	⋆⋆⋆	⋆⋆	⋆⋆⋆	⋆⋆⋆
$B \to K \tau l$	$Br.$	⋆⋆⋆	>50	⋆⋆	⋆⋆⋆	⋆⋆	⋆⋆⋆

Why $\bar{B} \to \gamma\gamma$?

- Sensitive to dynamics beyond the SM (FCNC), e.g. CP violation
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—— structure of the B meson

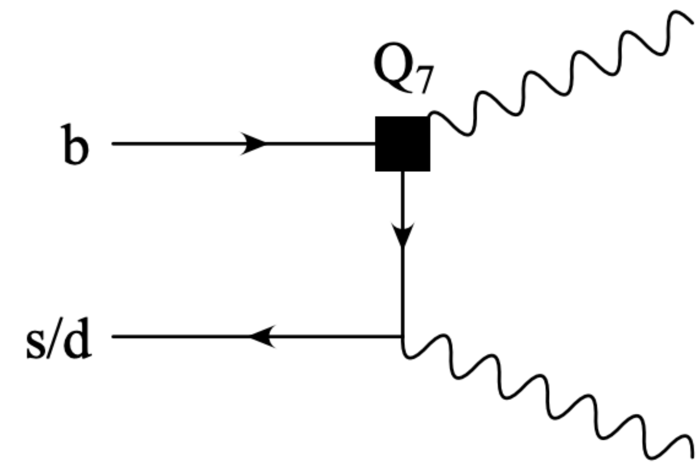
Belle II Physics Book

Observables	Belle $0.71\,\mathrm{ab}^{-1}$ $(0.12\,\mathrm{ab}^{-1})$	Belle II $5\,\mathrm{ab}^{-1}$	Belle II $50\,\mathrm{ab}^{-1}$
$\mathrm{Br}(B_d \to \gamma\gamma)$	$< 740\%$	30%	9.6%
$A_{CP}(B_d \to \gamma\gamma)$	–	78%	25%
$\mathrm{Br}(B_s \to \gamma\gamma)$	$< 250\%$	23%	–

$$\mathcal{BR}(B_d \to \gamma\gamma) = \left(1.352^{+1.242}_{-0.745}\right) \times 10^{-8}\,, \qquad \mathcal{BR}(B_s \to \gamma\gamma) = \left(2.964^{+1.800}_{-1.614}\right) \times 10^{-7}$$

[Y.-L. Shen, Y.-M. Wang, Y.-B. Wei, 2009.02723]

History of $\bar{B} \to \gamma\gamma$



- LO + NLO

$$\bar{A}(\bar{B}_q \to \gamma\gamma) = -\frac{4\,G_F}{\sqrt{2}}\frac{\alpha_{\rm em}}{4\pi}\,\epsilon^{*\alpha}(p)\,\epsilon^{*\beta}(q) \times \sum_{p=u,c} V_{pb}V_{pq}^{*} \sum_{i=1}^{8} C_i\,T^{(p)}_{i,\alpha\beta},$$

$$T^{(p)}_{i,\alpha\beta} = i\,m^3_{B_q}\left[\left(g^{\perp}_{\alpha\beta} - i\,\varepsilon^{\perp}_{\alpha\beta}\right)F^{(p)}_{i,L} - \left(g^{\perp}_{\alpha\beta} + i\,\varepsilon^{\perp}_{\alpha\beta}\right)F^{(p)}_{i,R}\right],$$

Two polarizations

Leading power

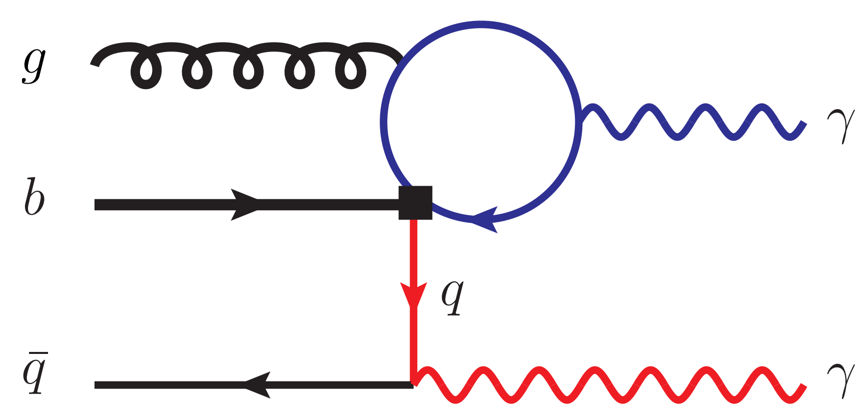
$$F_L^{\rm LP} \propto m_b \int_0^\infty \frac{d\omega}{\omega}\,\phi_B^+(\omega,\mu) \propto \frac{m_b}{\lambda_b}$$

[Bosch, Buchalla, hep-ph/0208202; Descotes-Genon, Sacharajda, hep-ph/0212162]

- NLL corrections + Systematic power corrections

both ~ $\mathcal{O}(10\%)$ [Y.-L. Shen, Y.-M. Wang, Y.-B. Wei, 2009.02723]

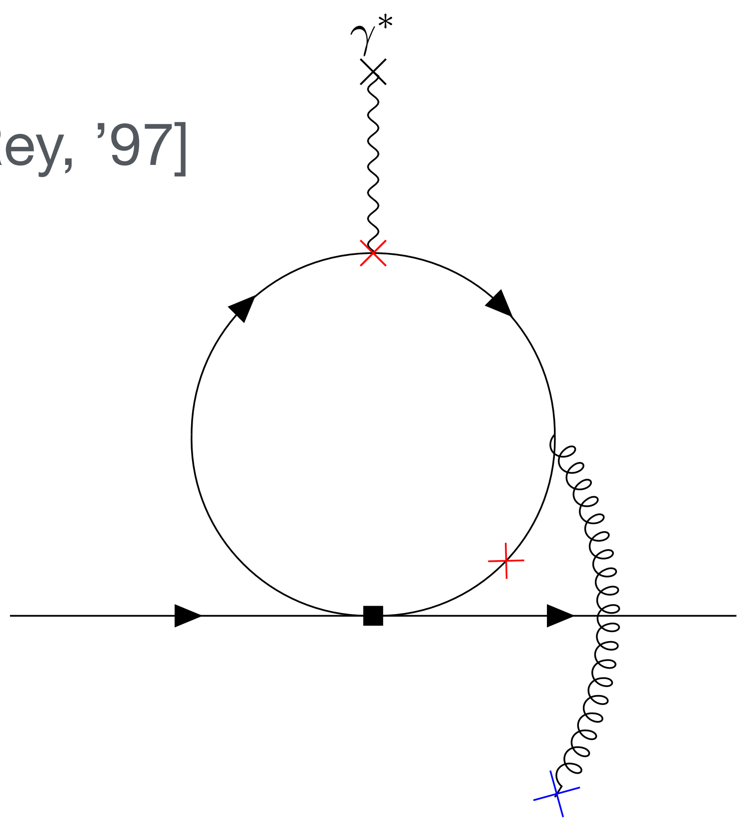
- One important but tough piece missing —— **long-distance penguin contribution**



History of Long-distance penguin contribution

In inclusive $b \to s$ decays

- Realized in $\bar{B} \to X_s \gamma$
  [Voloshin, '96; Ligeti, Randall, Wise, '97; Buchalla, Isidori, Rey, '97]
- Factorization in $\bar{B} \to X_s \gamma$
  [Benzke, Lee, Neubert, Paz, 1003.5012]
- Factorization in $\bar{B} \to X_s \ell \ell$
  [Benzke, Hurth, Turczyk, 1705.10366]

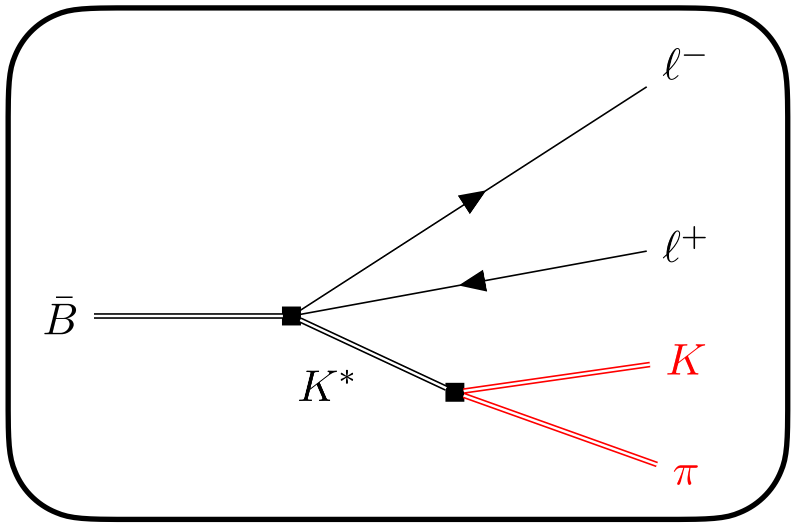


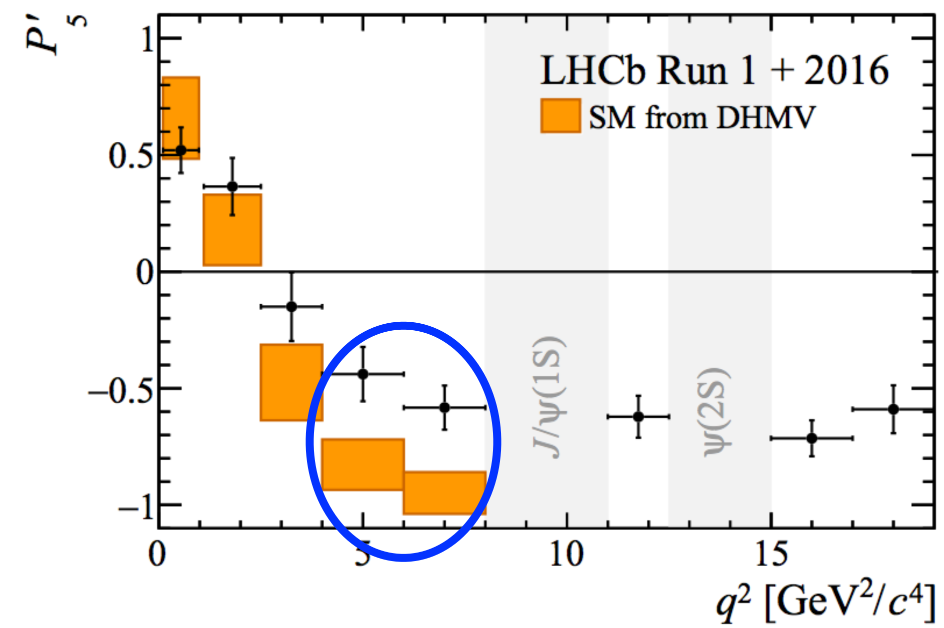
Soft gluon from charm-loop

In exclusive $b \to s$ decays

- Initiated in $B \to K^* \gamma$
  [Khodjamirian, Ruckl, Stoll, Wyler, '97]
- Developed in $B \to K^* \ell \ell$
  [Khodjamirian, Mannel, Pivorarov, Wang, 1006.4945]

History of Long-distance penguin contribution





P'_5: an angular-distribution observable

[LHCb, 2003.04831]

Charm-loop effect in $B \to K^{(*)}\ell^+\ell^-$ and $B \to K^*\gamma$

A. Khodjamirian (Siegen U.), Th. Mannel (Siegen U.), A.A. Pivovarov (Siegen U.), Y.-M. Wang (Siegen U.)

Jun, 2010

35 pages

Published in: *JHEP* 09 (2010) 089

e-Print: 1006.4945 [hep-ph]

pdf cite 414 citations

Factorization

Factorization

$$\mathcal{H}_{\text{eff}} = \frac{4\,G_F}{\sqrt{2}} \sum_{p=u,c} V_{pb} V_{pq}^* \Big[C_1(\nu)\, P_1^p(\nu) + C_2(\nu)\, P_2^p(\nu) + \sum_{i=3}^{8} C_i(\nu)\, P_i(\nu)$$
$$+ \sum_{i=3}^{6} C_i(\nu)\, P_i^Q(\nu) \Big] + \text{h.c.}\,,$$

$$P_1^p = (\bar{q}_L \gamma_\mu T^a p_L)\,(\bar{p}_L \gamma^\mu T^a b_L)\,, \qquad P_2^p = (\bar{q}_L \gamma_\mu p_L)\,(\bar{p}_L \gamma^\mu b_L)\,,$$

$$P_3 = (\bar{q}_L \gamma_\mu b_L) \sum_{q'} (\bar{q}' \gamma^\mu q')\,, \qquad P_4 = (\bar{q}_L \gamma_\mu T^a b_L) \sum_{q'} (\bar{q}' \gamma^\mu T^a q')\,,$$

$$P_5 = (\bar{q}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} b_L) \sum_{q'} (\bar{q}' \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} q')\,,$$

$$P_6 = (\bar{q}_L \gamma_{\mu_1} \gamma_{\mu_2} \gamma_{\mu_3} T^a b_L) \sum_{q'} (\bar{q}' \gamma^{\mu_1} \gamma^{\mu_2} \gamma^{\mu_3} T^a q')\,,$$

Factorization

Integrate out the hard and hard-collinear d.o.f.

$$M = H * J * S \qquad (m_b \gg m_c \sim \mathcal{O}(\sqrt{\Lambda m_b}) \gg \Lambda)$$

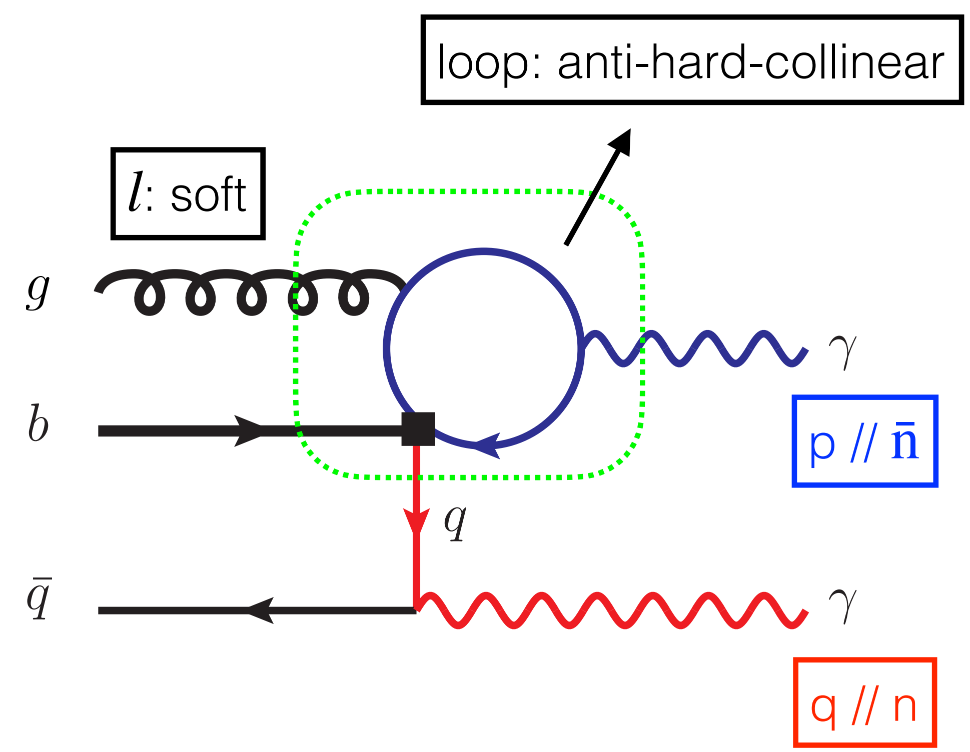
First-step match:

$$M \ni \left(C_2 - \frac{C_1}{2N_c}\right) Q_p \left[F\left(\frac{m_p^2 - i0^+}{(p-l)^2}\right) - 1\right] \frac{p^\alpha}{(p-l)^2} \left[\bar{q}(\tilde{q})\, \gamma_\beta P_L G_{\mu\alpha}\, \tilde{F}^{\mu\beta} b(v)\right]$$

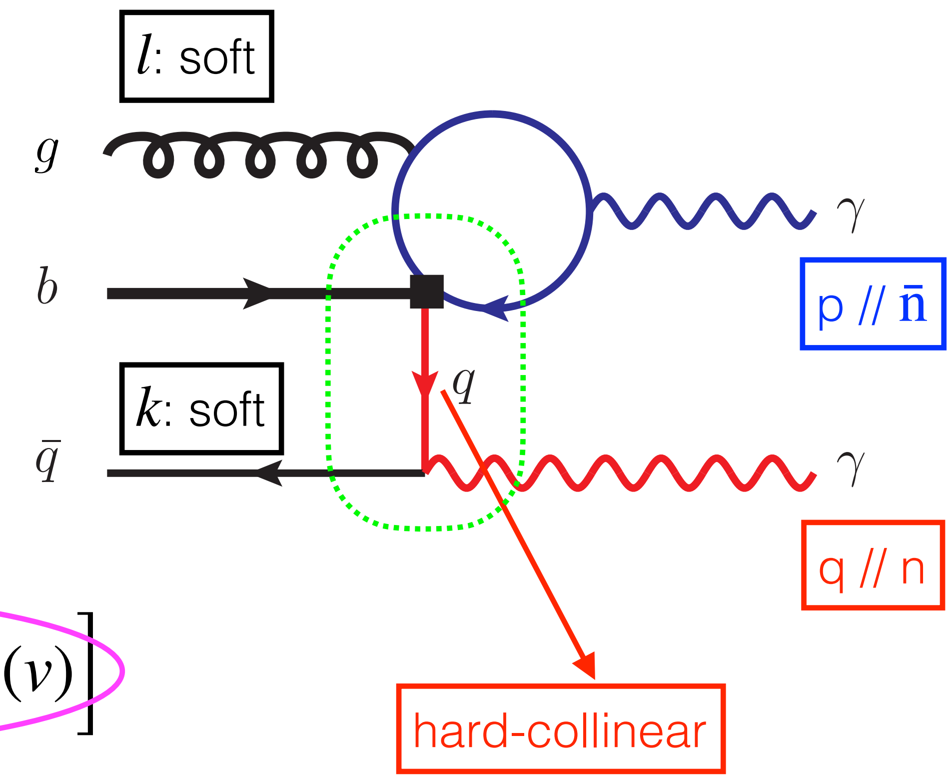
$$F(x) = 4\,x\, \arctan^2\left(\frac{1}{\sqrt{4\,x-1}}\right)$$

$$(p-l)^2 = -2p\cdot l = -m_b \bar{n}\cdot l$$

➡ Non-local operator!



Factorization



Second-step match:

$$\langle \gamma(p)\,\gamma(q)\,|\,\bar{q}\,\gamma_\beta\,P_L\,G_{\mu\alpha}\,\tilde{F}^{\mu\beta}\,b\,|\,g(l)\,b(v)\,\bar{q}(k)\rangle$$

$$\Rightarrow \frac{i\,g_{\rm em}\,e_q}{(q-k)^2}\,\epsilon^{\mu\beta\lambda\tau}\,p_\lambda\,\epsilon^*_\tau(p)\,\epsilon^*_\rho(q) \times \left[\bar{q}(k)\,\gamma^\rho_\perp\,\not{q}\,\gamma_\beta\,P_L\,G_{\mu\alpha}(\ell)\,b(v)\right]$$

$$(q-k)^2 = -\,2q\cdot k = -\,m_b\,n\cdot k$$

- The hard-kernel (jet functions) depends on 2 different light-cone components of the gluon and light quark momenta.
- It becomes evident to introduce the 3-particle B-meson distribution amplitude with 2 light-cone directions.

$$H \star J \star \bar{J} \star \Phi_G$$

Factorization

The explicit factorization formula:

$$\sum_{i=1}^{8} C_i\, F_{i,L}^{(p),\,\mathrm{soft\,4q}} = -\frac{Q_q\, f_{B_q}}{m_{B_q}} \int_0^\infty \frac{d\omega_1}{\omega_1} \int_0^\infty \frac{d\omega_2}{\omega_2} \left(C_2 - \frac{C_1}{2N_c}\right) Q_p \left[F(-\frac{m_p^2}{m_b \omega_2}) - 1\right] \times \Phi_G(\omega_1, \omega_2, \mu)$$

The light quark momentum component $\omega_1 = n \cdot k$;
The soft gluon momentum component $\omega_2 = \bar{n} \cdot l$.

The novel B-meson DA:

$$\langle 0 \,|\, \bar{q}_s(\tau_1 n)(g_s G_{\mu\nu})(\tau_2 \bar{n})\, \bar{n}^\nu \;\; \not{n} \gamma_\perp^\mu \gamma_5\, h_v(0) \,|\, \bar{B}_v \rangle$$
$$= 2 \tilde{f}_B(\mu)\, m_B \int_0^\infty d\omega_1 \int_0^\infty d\omega_2 \exp\left[-i(\omega_1 \tau_1 + \omega_2 \tau_2)\right]\, \Phi_G(\omega_1, \omega_2, \mu)$$

- The quark and gluon fields are localized on 2 distinct light-cone directions.

It might opens an exciting new research subfield aiming at the multidimensional tomography of the composite bottom-meson systems.

Factorization

The normalization conditions of Φ_G:

Matching the conventional 3-particle B meson DAs as τ_1 or $\tau_2 \to 0$.

$$\langle 0 | \bar{q}(z_1)(g_s G_{\mu\nu})(z_2)\, \bar{n}^\nu \;\not{n}\gamma_\perp^\mu \gamma_5\, h_v(0) | \bar{B}_v \rangle = = 2\tilde{f}_B(\mu)\Phi_4(z_1, z_2, \mu)$$

Twist 4

$$\langle 0 | \bar{q}(z_1)(g_s G_{\mu\nu})(z_2)\, n^\nu \;\not{\bar{n}}\gamma_\perp^\mu \gamma_5\, h_v(0) | \bar{B}_v \rangle = = 2\tilde{f}_B(\mu)\Phi_5(z_1, z_2, \mu)$$

Twist 5

[Braun, Ji, Manashov, 1703.02446]

$$\int_0^\infty d\omega_1\, \Phi_G(\omega_1, \omega_2, \mu) = \int_0^\infty d\omega_1\, \Phi_4(\omega_1, \omega_2, \mu)\,,$$

$$\int_0^\infty d\omega_2\, \Phi_G(\omega_1, \omega_2, \mu) = \int_0^\infty d\omega_2\, \Phi_5(\omega_1, \omega_2, \mu)\,,$$

$$\int_0^\infty d\omega_1 \int_0^\infty d\omega_2\, \Phi_G(\omega_1, \omega_2, \mu) = \frac{\lambda_E^2 + \lambda_H^2}{3}\,,$$

The asymptotic behaviors of Φ_G:

$$\Phi_G(\omega_1, \omega_2, \mu) \sim \omega_1\, \omega_2^2 \;\text{ at }\; \omega_1,\, \omega_2 \to 0$$

Factorization

The explicit factorization formula:

$$\sum_{i=1}^{8} C_i F_{i,L}^{(p),\,\mathrm{soft\,4q}} = -\frac{Q_q f_{B_q}}{m_{B_q}} \int_0^\infty \frac{d\omega_1}{\omega_1} \int_0^\infty \frac{d\omega_2}{\omega_2} \left(C_2 - \frac{C_1}{2N_c}\right) Q_p \left[F(-\frac{m_p^2}{m_b\omega_2}) - 1\right] \times \Phi_G(\omega_1,\omega_2,\mu)$$

$$\Phi_G(\omega_1,\omega_2,\mu) \sim \omega_1\,\omega_2^2 \text{ at } \omega_1,\,\omega_2 \to 0$$

➡ The convolution integral converges.

$$\int_0^\infty d\omega_1\, \Phi_G(\omega_1,\omega_2,\mu) = \int_0^\infty d\omega_1\, \Phi_4(\omega_1,\omega_2,\mu)\,,$$

$$\int_0^\infty d\omega_2\, \Phi_G(\omega_1,\omega_2,\mu) = \int_0^\infty d\omega_2\, \Phi_5(\omega_1,\omega_2,\mu)\,,$$

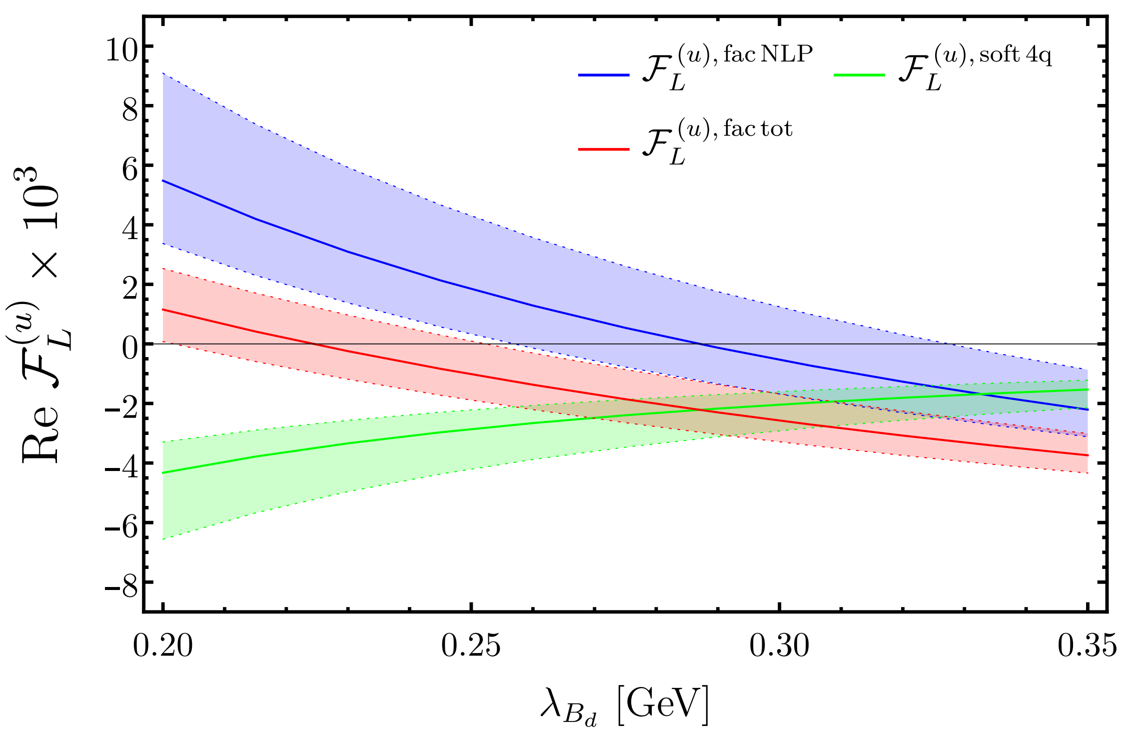
$$\int_0^\infty d\omega_1 \int_0^\infty d\omega_2\, \Phi_G(\omega_1,\omega_2,\mu) = \frac{\lambda_E^2+\lambda_H^2}{3}\,,$$

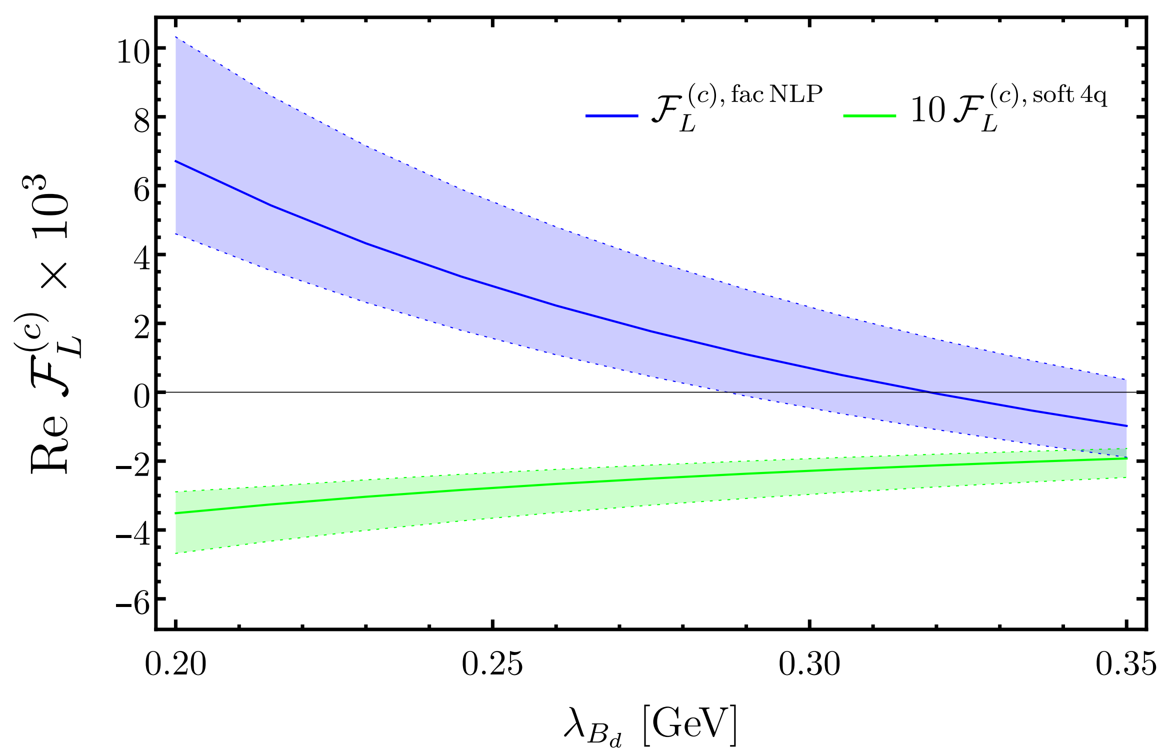
➡ The power counting: $F_L^{\mathrm{soft}\,,4q}/F_L^{\mathrm{LP}} \sim \lambda_B/m_b$

Numerics

The Φ_G parametrization:

$$\Phi_G(\omega_1,\omega_2,\mu_0) = \frac{\lambda_E^2+\lambda_H^2}{6}\,\frac{\omega_1\omega_2^2}{\omega_0^5}\,\exp\left(-\frac{\omega_1+\omega_2}{\omega_0}\right)\frac{\Gamma(\beta+2)}{\Gamma(\alpha+2)}\;U\left(\beta-\alpha, 4-\alpha, \frac{\omega_1+\omega_2}{\omega_0}\right)$$





- The up-loop contribution dominates; the charm-loop is 1-order smaller.
- The new power correction accidentally cancels the previous ones.

→ Clean channel to determine λ_B and to probe new physics.

Numerics

The B_d results:

	Central Value	Total Error	λ_{B_d}	$\{\widehat{\sigma}^{(1)}_{B_d}, \widehat{\sigma}^{(2)}_{B_d}\}$	μ	ν	μ_h	$\bar{\Lambda}$	m_c^{PS}
$10^8 \times \mathcal{BR}$	1.929 [1.900]	$^{+1.096}_{-1.012}$	$^{+0.680}_{-0.439}$	$^{+0.736}_{-0.779}$	$^{+0.083}_{-0.299}$	$^{+0.278}_{-0.287}$	$^{+0.246}_{-0.066}$	$^{+0.212}_{-0.200}$	$^{+0.043}_{-0.043}$
$f_\parallel$	0.408 [0.407]	$^{+0.044}_{-0.046}$	$^{+0.015}_{-0.015}$	$^{+0.016}_{-0.033}$	$^{+0.002}_{-0.009}$	$^{+0.037}_{-0.026}$	$^{+0.007}_{-0.002}$	$^{+0.005}_{-0.006}$	$^{+0.002}_{-0.002}$
$f_\perp$	0.592 [0.593]	$^{+0.046}_{-0.044}$	$^{+0.015}_{-0.015}$	$^{+0.033}_{-0.016}$	$^{+0.009}_{-0.002}$	$^{+0.026}_{-0.037}$	$^{+0.002}_{-0.007}$	$^{+0.006}_{-0.005}$	$^{+0.002}_{-0.002}$
$\mathcal{A}_{CP}^{dir,\parallel}$	0.126 [0.129]	$^{+0.043}_{-0.027}$	$^{+0.007}_{-0.004}$	$^{+0.017}_{-0.010}$	$^{+0.013}_{-0.008}$	$^{+0.027}_{-0.018}$	$^{+0.024}_{-0.012}$	$^{+0.007}_{-0.007}$	$^{+0.004}_{-0.004}$
$\mathcal{A}_{CP}^{mix,\parallel}$	-0.197 [-0.154]	$^{+0.053}_{-0.084}$	$^{+0.019}_{-0.036}$	$^{+0.001}_{-0.002}$	$^{+0.021}_{-0.047}$	$^{+0.026}_{-0.040}$	$^{+0.015}_{-0.029}$	$^{+0.011}_{-0.013}$	$^{+0.008}_{-0.009}$
$\mathcal{A}_{\Delta\Gamma}^{\parallel}$	-0.972 [-0.980]	$^{+0.024}_{-0.013}$	$^{+0.009}_{-0.004}$	$^{+0.003}_{-0.002}$	$^{+0.013}_{-0.005}$	$^{+0.013}_{-0.007}$	$^{+0.010}_{-0.004}$	$^{+0.004}_{-0.003}$	$^{+0.002}_{-0.002}$
$\mathcal{A}_{CP}^{dir,\perp}$	0.330 [0.326]	$^{+0.078}_{-0.053}$	$^{+0.015}_{-0.012}$	$^{+0.060}_{-0.035}$	$^{+0.035}_{-0.014}$	$^{+0.012}_{-0.024}$	$^{+0.014}_{-0.010}$	$^{+0.018}_{-0.016}$	$^{+0.018}_{-0.017}$
$\mathcal{A}_{CP}^{mix,\perp}$	0.136 [0.101]	$^{+0.087}_{-0.066}$	$^{+0.043}_{-0.028}$	$^{+0.015}_{-0.035}$	$^{+0.025}_{-0.014}$	$^{+0.060}_{-0.038}$	$^{+0.026}_{-0.012}$	$^{+0.003}_{-0.003}$	$^{+0.009}_{-0.008}$
$\mathcal{A}_{\Delta\Gamma}^{\perp}$	0.934 [0.940]	$^{+0.017}_{-0.030}$	$^{+0.000}_{-0.003}$	$^{+0.009}_{-0.019}$	$^{+0.007}_{-0.017}$	$^{+0.001}_{-0.002}$	$^{+0.005}_{-0.009}$	$^{+0.006}_{-0.007}$	$^{+0.007}_{-0.008}$

Summary and prospects

- We have factorized the long-distance penguin contribution to $\bar{B} \to \gamma\gamma$ decay, for the first time in an exclusive decay.
- A novel B-meson DA is defined, with quark and gluon fields localized on two different light-cone directions. It will open a new subfield about the inner structure of the B meson.
- The new contribution cancels the known factorizable power corrections, making $\bar{B} \to \gamma\gamma$ a clean channel to determine λ_B and to probe the non-standard four-fermion interactions.
- The developed formalism has a broad field of applications to the entire spectrum of the exclusive FCNC B-meson decays, including flagship modes, e.g. $B \to K^* \gamma$, $B \to K^* \mu\mu$.

Thank you!

Backup

	B_d	B_s
$\mathcal{A}^{\rm LP,NLL}\,[10^{-4}]$	$3.4 + 1.9\,i$	$-20 - 0.37\,i$
$\mathcal{A}^{\rm fac,NLP}\,[10^{-4}]$	$-0.15 - 0.53\,i$	$0.92 + 2.6\,i$
$\mathcal{A}_R^{\rm fac,NLP}\,[10^{-4}]$	$0.25 - 0.36\,i$	$-1.6 + 2.6\,i$
$\mathcal{A}^{\rm had,\gamma}\,[10^{-4}]$	$-0.30 - 0.17\,i$	$1.4 - 0.0021\,i$
$\mathcal{A}^{\rm soft,\,4q}\,[10^{-4}]$	$(-0.0079 + 0.078\,i)$	$-0.11 + 0.016\,i$
$(F_u^{\rm LP,NLL}, F_c^{\rm LP,NLL})$	$(-0.056 - 0.0092i,\ -0.048 - 0.0019i)$	$(-0.057 - 0.0094i,\ -0.049 - 0.0020i)$
$(F_u^{\rm had,\gamma}, F_c^{\rm had,\gamma})$	$(0.0051 + 0.00092i,\ 0.0043 + 0.00019i)$	$(0.0094 + 0.0016i,\ 0.0034 + 0.00016i)$
$(F_u^{\rm soft,4q}, F_c^{\rm soft,4q})$	$(-0.0024,\ -0.00025)$	$(-0.0021,\ -0.00025)$
$(F_u^{\rm HC}, F_c^{\rm HC})$	$(0.0055,\ 0.0055)$	$(0.0067,\ 0.0067)$
$(F_u^{\rm m_q}, F_c^{\rm m_q})$	$(0.000049,\ 0.000049)$	$(0.00078,\ 0.00078)$ [0.00079]
$(F_u^{\rm A_2}, F_c^{\rm A_2})$	$(-0.0010,\ -0.0010)$	$(-0.0011,\ -0.0011)$
$(F_u^{\rm HT}, F_c^{\rm HT})$	$(0.0046,\ 0.0046)$ [0.0047]	$(0.0048,\ 0.0048)$ [0.0050]
$(F_u^{\rm Q_b}, F_c^{\rm Q_b})$	$(-0.0036,\ -0.0036)$	$(-0.0043,\ -0.0043)$
$(F_u^{\rm WA}, F_c^{\rm WA})$	$(-0.0049 + 0.000092i,\ -0.0037 + 0.0056i)$	$(-0.0059 + 0.00011i,\ -0.0045 + 0.0065i)$
$(F_u^{\rm fac,NLP}, F_c^{\rm fac,NLP})$	$(0.00054 + 0.000092i,\ 0.0018 + 0.0056i)$	$(0.00098 + 0.00011i,\ 0.0023 + 0.0065i)$
	$[(0.00063 + 0.000092i,\ 0.0019 + 0.0056i)]$	$(0.0011 + 0.00011i,\ 0.0024 + 0.0065i)$
$(F_{R,u}^{\rm fac,NLP}, F_{R,c}^{\rm fac,NLP})$	$(-0.0046 + 0.000092i,\ -0.0033 + 0.0056i)$	$(-0.0054 + 0.00011i,\ -0.0041 + 0.0065i)$

$$A = V_{uq}^* V_{ub}\, F_u + V_{cq}^* V_{cb}\, F_c \;(q = d, s)$$