Which Way Beyond the Standard Model?

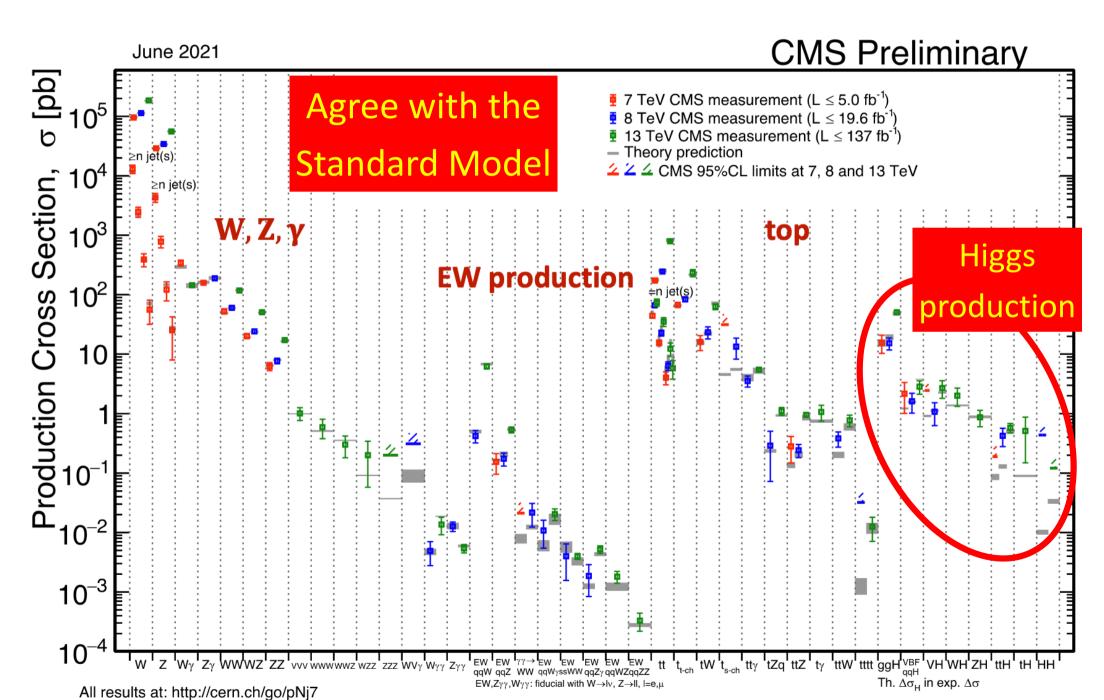


LHC measurements and the Higgs boson
Beyond the Standard Model with Effective Field Theory

 $m_W \& g_{\mu} - 2?$

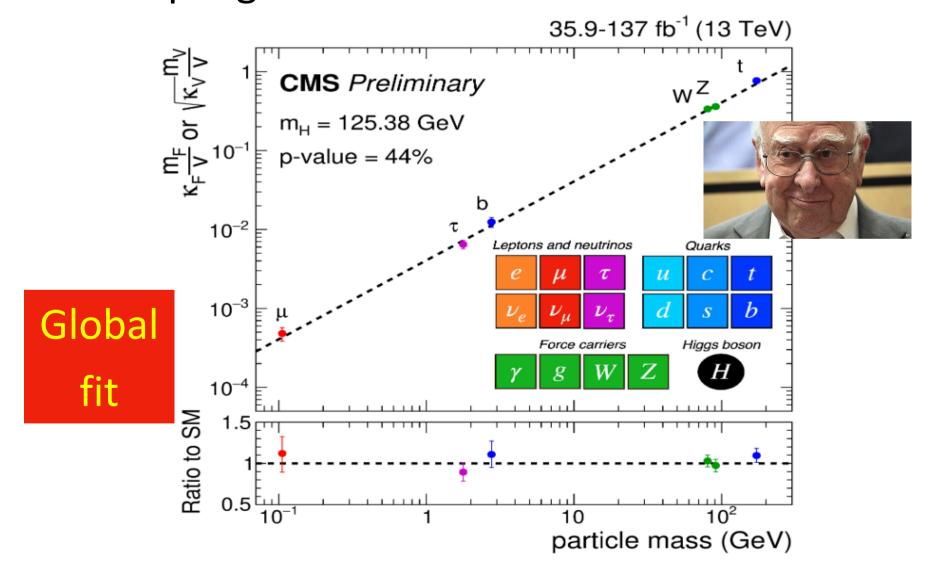


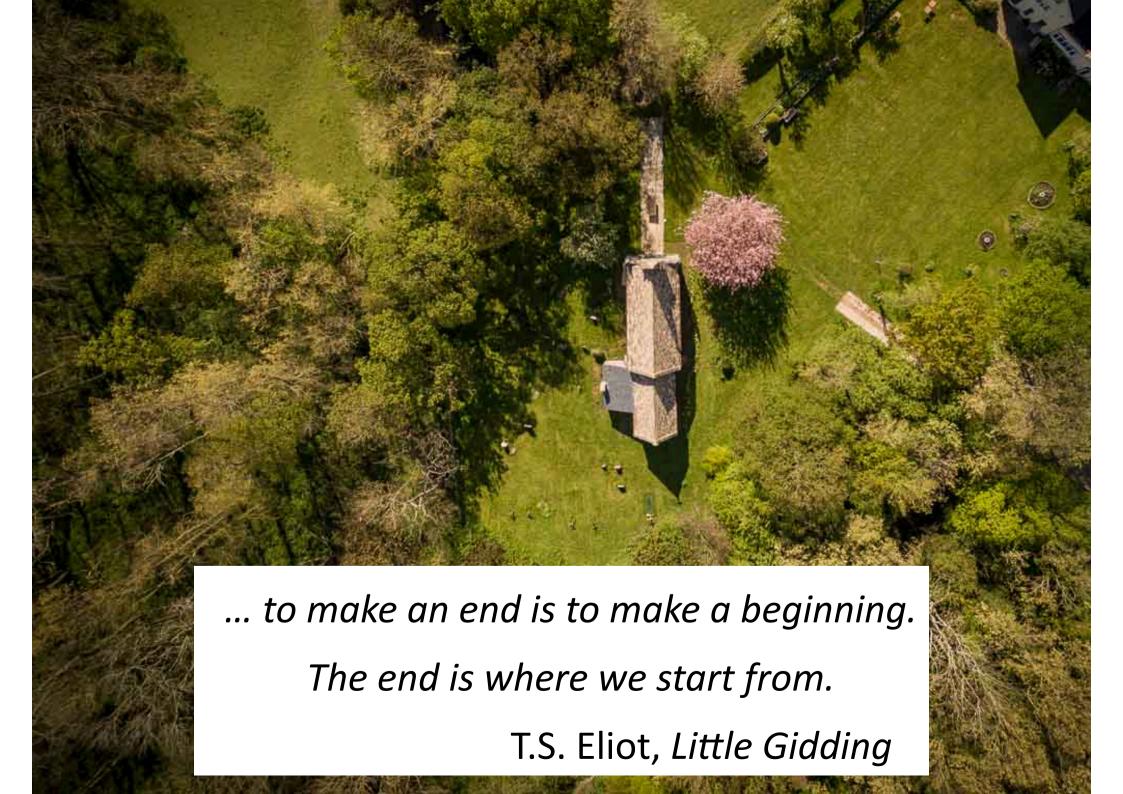
LHC Measurements



It Walks and Quacks like a Higgs

Do couplings scale ~ mass? With scale = v?





Everything about Higgs is Puzzling

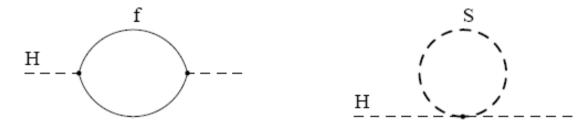
$$\mathcal{L} = yH\psi\overline{\psi} + \mu^2|H|^2 - \lambda|H|^4 - V_0 + \dots$$

- Pattern of Yukawa couplings y:
 - Flavour problem
- Magnitude of mass term μ:
 - Naturalness/hierarchy problem
- Magnitude of quartic coupling λ:
 - Stability of electroweak vacuum
- Cosmological constant term V₀:
 - Dark energy

Higher-dimensional interactions?

Loop Corrections to Higgs Mass²

Consider generic fermion and boson loops:



• Each is quadratically divergent: $\int^{\Lambda} d^4k/k^2$

$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + \dots]$$

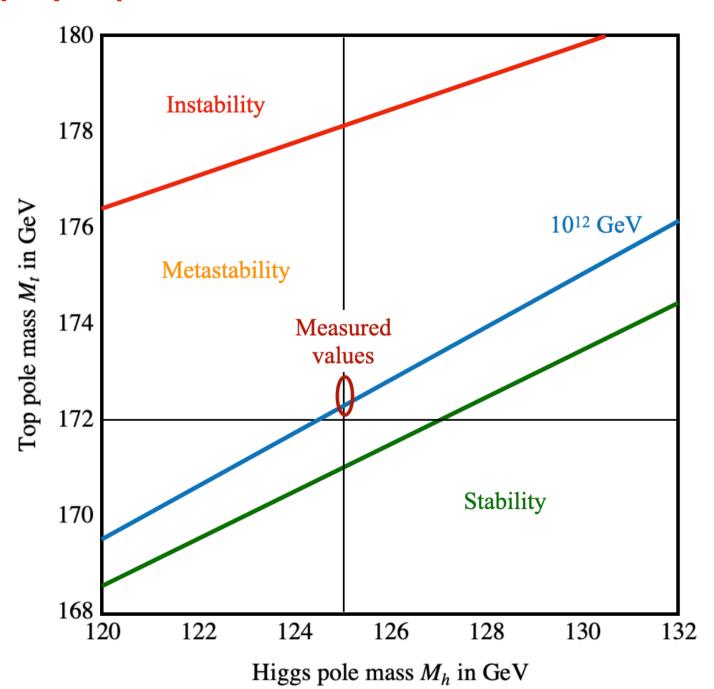
$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

• Leading divergence $\lambda_S = y_f^2 \ge 2$

Supersymmetry!

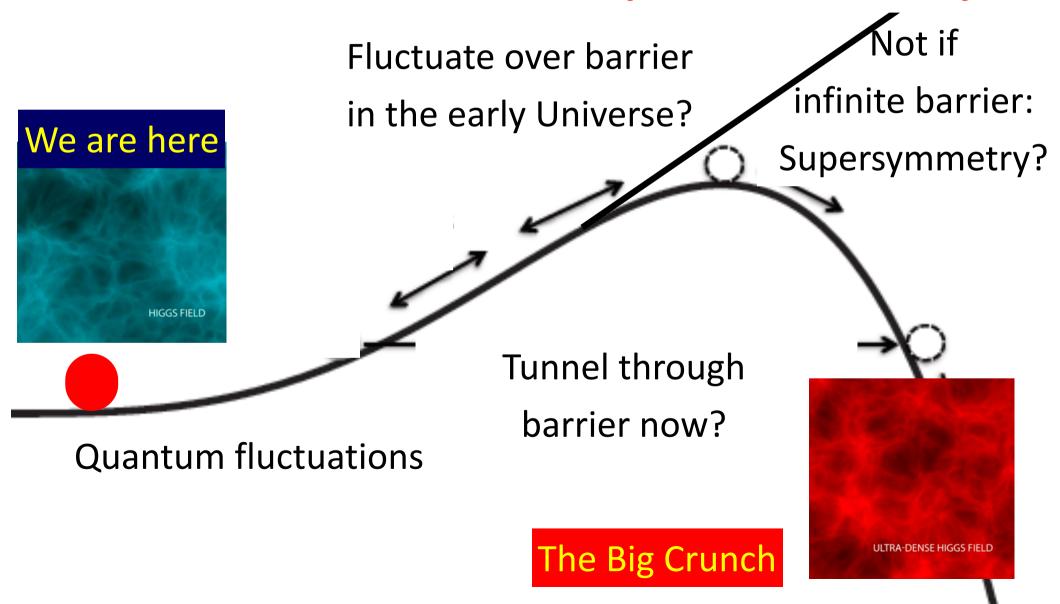
Is "Empty Space" Unstable?

Depends on masses of Higgs boson and top quark



Will the Universe Collapse?

Should it have Collapsed already?



What lies beyond the Standard Model?

Supersymmetry

Stabilize electroweak vacuum

- New motivations from LHC
- Successful prediction for Higgs mass
 - Should be < 130 GeV in simple models</p>
- Successful predictions for couplings
 - Should be within few % of SM values
- Naturalness, GUTs, string, dark matter, $g_{\mu} 2$, ...



"...the direct method may be used...but indirect methods will be needed in order to secure victory...."

"The direct and the indirect lead on to each other in turn. It is like moving in a circle...."

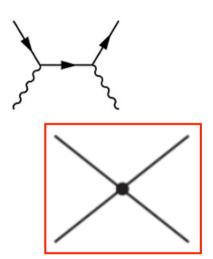
Who can exhaust the possibilities of their combination?"

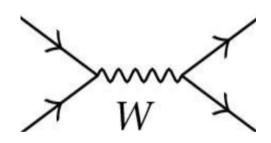
Sun Tzu

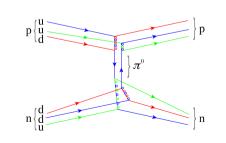
Effective Field Theories (EFTs) a long and glorious History

- 1930's: "Standard Model" of QED had d=4
- Fermi's four-fermion theory of the weak force
- Dimension-6 operators: form = S, P, V, A, T?
 - Due to exchanges of massive particles?
- V-A → massive vector bosons → gauge theory
- Yukawa's meson theory of the strong N-N force
 - Due to exchanges of mesons? → pions









Standard Model Effective Field Theory a more powerful way to analyze the data

- Assume the Standard Model Lagrangian is correct (quantum numbers of particles) but incomplete
- Look for additional interactions between SM particles due to exchanges of heavier particles
- Analyze Higgs data together with electroweak precision data and top data
- Most efficient way to extract largest amount of information from LHC and other experiments
- Model-independent way to look for physics beyond the Standard Model (BSM)

Summary of Analysis Framework

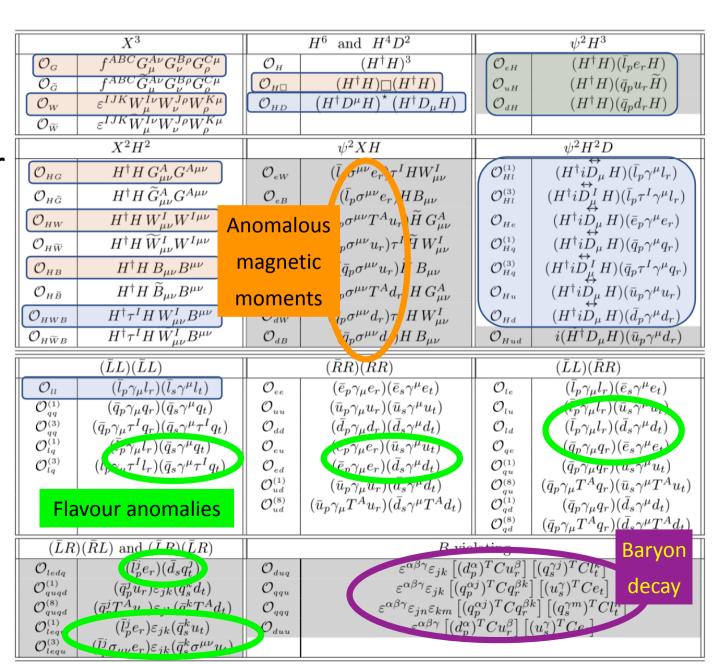
Include all leading dimension-6 operators?

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{i=1}^{2499} \frac{C_i}{\Lambda^2} \mathcal{O}_i$$

- Simplify by assuming flavour $SU(3)^5$ or $SU(2)^2 \times SU(3)^3$ symmetry for fermions
- Work to linear order in operator coefficients, i.e. $\mathcal{O}(1/\Lambda^2)$
- Use G_F , M_Z , α as input parameters

Dimension-6 SMEFT Operators

- Including 2- and 4fermion operators
- Different colours for different data sectors
- Grey cells violate
 SU(3)⁵ symmetry
- Important when including top observables



Global SMEFT Fit

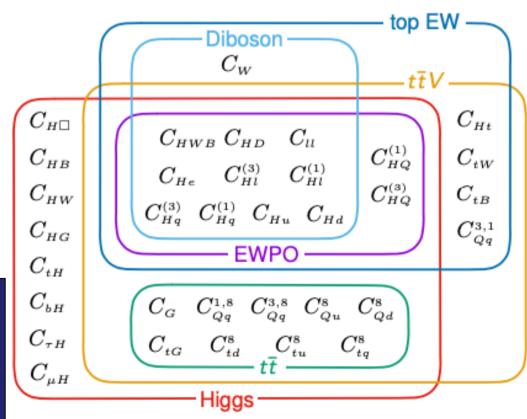
to Top, Higgs, Diboson, Electroweak Data

JE, Madigan, Mimasu, Sanz & You, arXiv:2012.02779

 Global fit to dimension-6 operators using precision electroweak data, W+W- at LEP, top, Higgs and diboson data from LHC Runs 1, 2

- Search for BSM
- Constraints on BSM
 - At tree level
 - At loop level

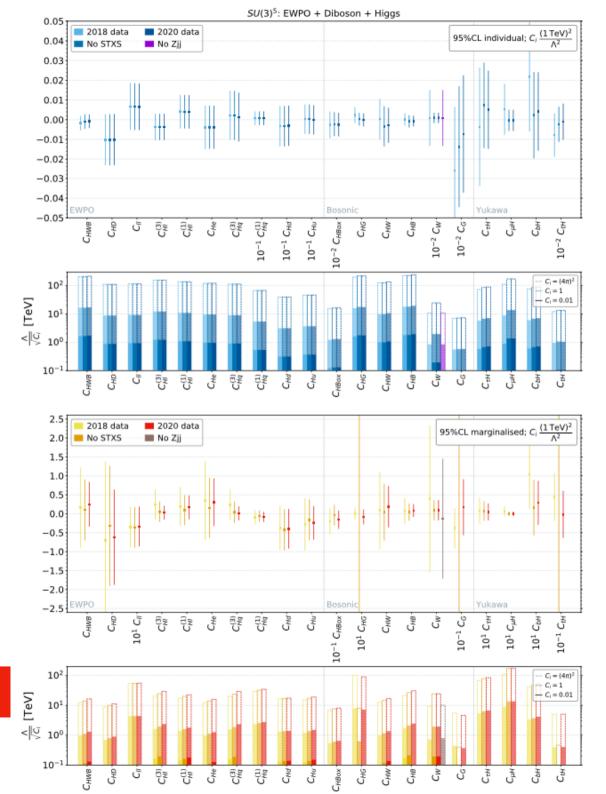
341 measurements included in global analysis



Dimension-6 Constraints with Flavour-Universal SU(3)⁵ Symmetry

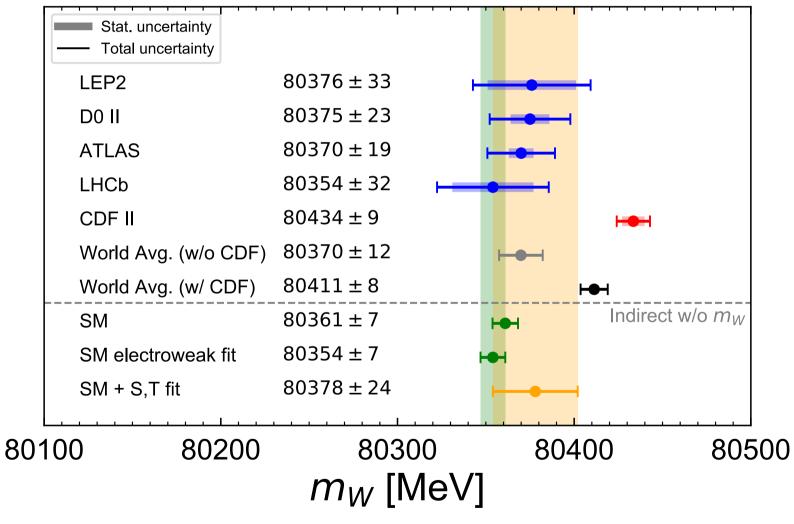
- Individual operator coefficients
- Marginalised over all other operator coefficients

No significant deviations from SM



CDF Measurement of mw

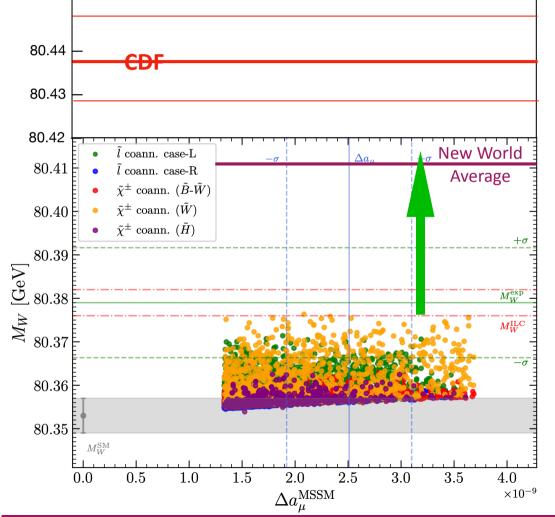
compared with previous measurements



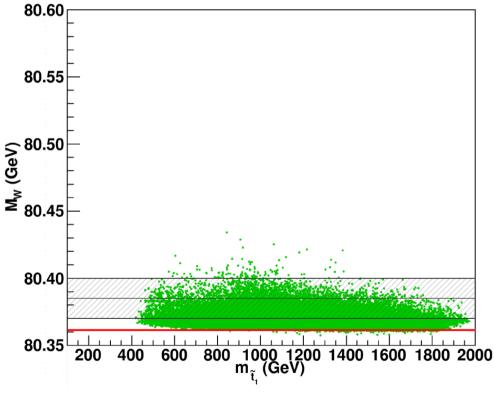
Tension: 7- σ discrepancy with Standard Model?

W Mass in Supersymmetry?

Assuming supersymmetric dark matter: electroweak sparticles reach old world average, but not CDF or new world average



Contribution from stops?



Heinemeyer, Weiglein & Zeune, 2013

SMEFT Operators that can Contribute to W Mass

Relevant SMEFT operators

$$\mathcal{O}_{HWB} \equiv H^{\dagger} \tau^{I} H W_{\mu\nu}^{I} B^{\mu\nu}, \quad \mathcal{O}_{HD} \equiv \left(H^{\dagger} D^{\mu} H \right)^{\star} \left(H^{\dagger} D_{\mu} H \right)$$
$$\mathcal{O}_{\ell\ell} \equiv \left(\bar{\ell}_{p} \gamma_{\mu} \ell_{r} \right) \left(\bar{\ell}_{s} \gamma^{\mu} \ell_{t} \right), \quad \mathcal{O}_{H\ell}^{(3)} \equiv \left(H^{\dagger} i \overset{\leftrightarrow}{D}_{\mu}^{I} H \right) \left(\bar{\ell}_{p} \tau^{I} \gamma^{\mu} \ell_{r} \right)$$

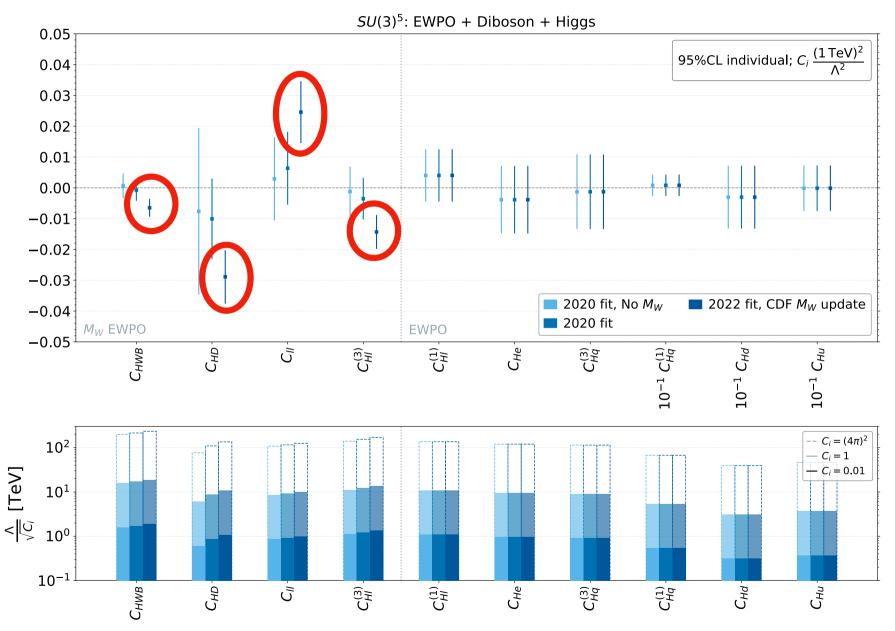
Contributions to W mass

$$\frac{\delta m_W^2}{m_W^2} = -\frac{\sin 2\theta_w}{\cos 2\theta_w} \frac{v^2}{4\Lambda^2} \left(\frac{\cos \theta_w}{\sin \theta_w} C_{HD} + \frac{\sin \theta_w}{\cos \theta_w} \left(4C_{Hl}^{(3)} - 2C_{ll} \right) + 4C_{HWB} \right)$$

Contributions to S and T oblique parameters

$$\frac{v^2}{\Lambda^2}C_{HWB} = \frac{g_1g_2}{16\pi}S$$
 , $\frac{v^2}{\Lambda^2}C_{HD} = -\frac{g_1g_2}{2\pi(g_1^2 + g_2^2)}T$

SMEFT Fit with the Mass of the W Boson



Non-zero coefficients for any of four operators can fit W mass

Bagnaschi, JE, Madigan, Mimasu, Sanz & You, arXiv:2204.05260

Single-Field Extensions of the Standard Model

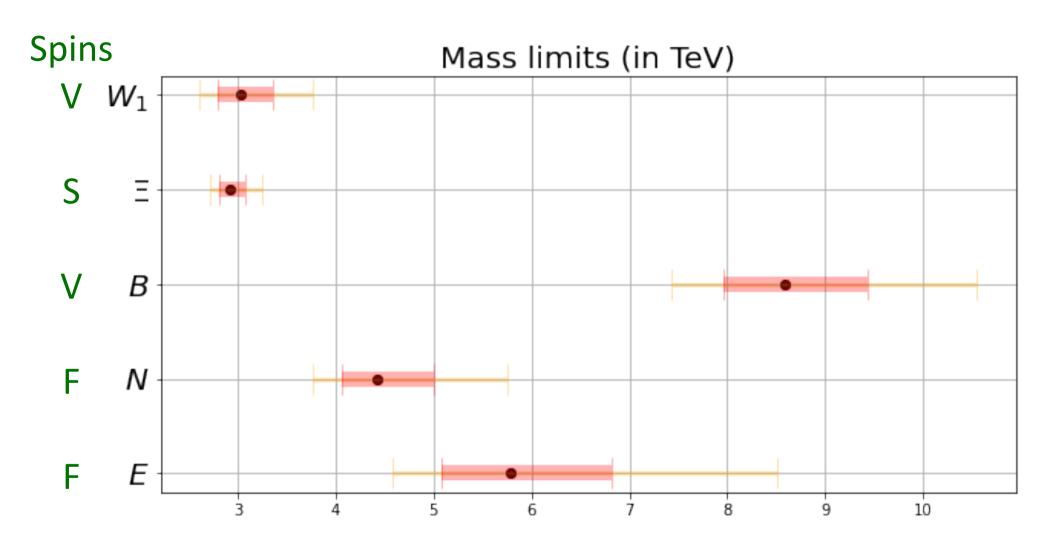
	Name	Spin	SU(3)	SU(2)	U(1)	Name	Spin	SU(3)	SU(2)	U(1)
	S	0	1	1	0	Δ_1	$\frac{1}{2}$	1	2	$-\frac{1}{2}$
	S_1	0	1	1	1	Δ_3	$\frac{1}{2}$	1	2	$-rac{1}{2}$
	Q	0	Spin ze	ero 2	$\frac{1}{2}$	Σ	$\frac{1}{2}$	1	3	0
ackslash	[I]	0	1	3	0	Σ_1	$\frac{1}{2}$	1	3	-1
		9	1	3	1	U	$\frac{1}{2}$	3	1	$\frac{2}{3}$
	\mathcal{B}	1	1	1	0	D	$\frac{1}{2}$	3	1	$-\frac{1}{3}$
	B_1	1	Voctor	1	1	Q_1	$\frac{1}{2}$	3	2	$\frac{1}{6}$
	W	1	Vector -	3	0	Q_5	$\frac{1}{2}$	3	2	$-\frac{5}{6}$
	W_1	1	1	3	1	Q_7	$\frac{1}{2}$	3	2	$\frac{7}{6}$
	N	$\frac{1}{2}$	1	1	0	T_1	$\frac{1}{2}$	3	3	$-\frac{1}{3}$
	\boldsymbol{E}	$rac{1}{2}$	1	1	-1	T_2	$\frac{1}{2}$	3	3	$\frac{2}{3}$
	T	$\frac{1}{2}$	3	1	$\frac{2}{3}$	TB	$\frac{1}{2}$	3	2	$\frac{1}{6}$

Single-Field Models that can Contribute to W Mass

Model	C_{HD}	C_{ll}	$C_{H^{1}}^{(3)}$	$C_{Hl}^{(1)}$	C_{He}	$C_{H\square}$	$C_{ au H}$	C_{tH}	C_{bH}
S_1		X							
Σ	Wrong	sign	*	$\frac{3}{16}$			$\frac{y_{ au}}{4}$		
Σ_1	VVIOLIB	31811	*	$-\frac{3}{16}$			$\frac{y_{ au}}{8}$		
N			$-\frac{1}{4}$	$rac{1}{4}$					
E			$-\frac{1}{4}$	$-\frac{1}{4}$			$rac{y_{ au}}{2}$		
B_1	X					$-\frac{1}{2}$	$-rac{y_{ au}}{2}$	$-\frac{y_t}{2}$	$-\frac{y_b}{2}$
B	-2	Righ	nt sign				$-y_{ au}$	$-y_t$	$-y_b$
Ξ	-2					$\frac{1}{2}$	$y_{ au}$	y_t	y_b
W_1	$-\frac{1}{4}$					$-\frac{1}{8}$	$-\frac{y_{ au}}{8}$	$-\frac{y_t}{8}$	$-\frac{y_b}{8}$
W	X					$-\frac{1}{2}$	$-y_{ au}$	$-y_t$	$-y_b$

Operators contributing to m_W

Models Fitting the Mass of the W Boson



68 and 95% CL ranges of masses assuming unit couplings, mass range proportional to coupling

Models Fitting Mass of the W Boson

	Model	Pull	Best-fit mass	$1-\sigma$ mass	2 - σ mass	$1-\sigma \text{ coupling}^2$	
Spins			(TeV)	range (TeV)	range (TeV)	range	
V	W_1	6.4	3.0	[2.8, 3.6]	[2.6, 3.8]	[0.09, 0.13]	
S	B	\mid 6.4 \mid	8.6	[8.0, 9.4]	[7.4, 10.6]	[0.011, 0.016]	
V	Ξ	6.4	2.9	[2.8, 3.1]	[2.7, 3.2]	[0.011, 0.016]	
F	N	5.1	4.4	[4.1,5.0]	[3.8, 5.8]	[0.040, 0.060]	
F	E	3.5	5.8	[5.1, 6.8]	[4.6, 8.5]	[0.022, 0.039]	

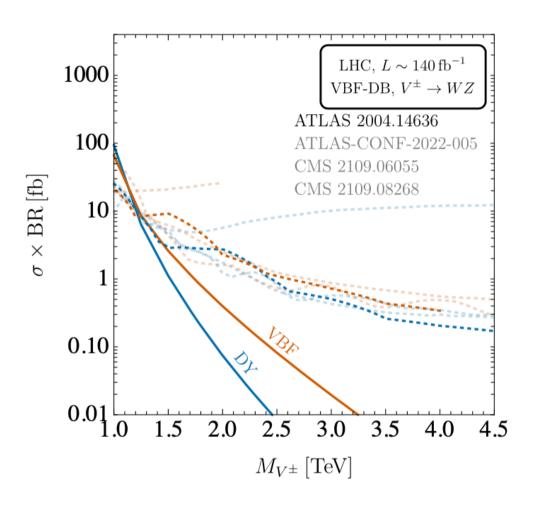
Best-fit, 68 and 95% CL ranges of masses assuming unit couplings

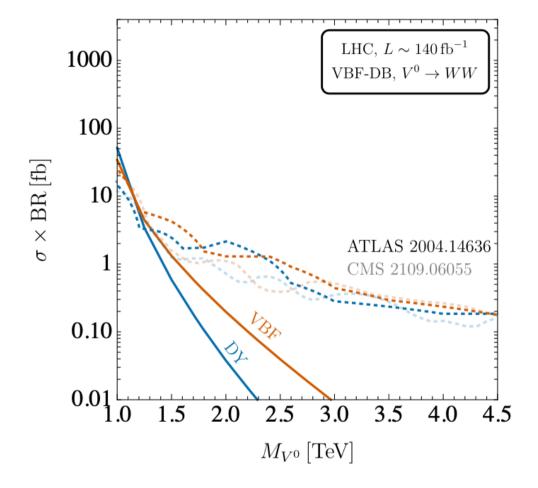
68% CL ranges of couplings for 1 TeV

Searching for Models Fitting the Mass of the W Boson

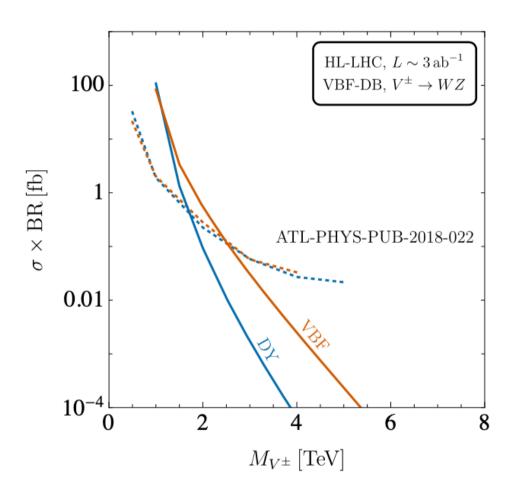
- W: Isotriplet vector boson, mass ~ 3 TeV x coupling, electroweak production, accessible at LHC?
- B: Singlet vector boson, mass ~ 8 TeV x coupling, phenomenology depends on fermion couplings, too heavy for LHC?
- E: Isotriplet scalar boson, mass ~ 3 TeV x coupling, detectable in LHC searches for heavy Higgs bosons?
- N: Isosinglet neutral fermion, mass ~ 4 TeV x coupling, similar to (right-handed) singlet neutrino
- E: Isosinglet charged fermion, mass ~ 6 TeV x coupling, similar to (right-handed) singlet electron

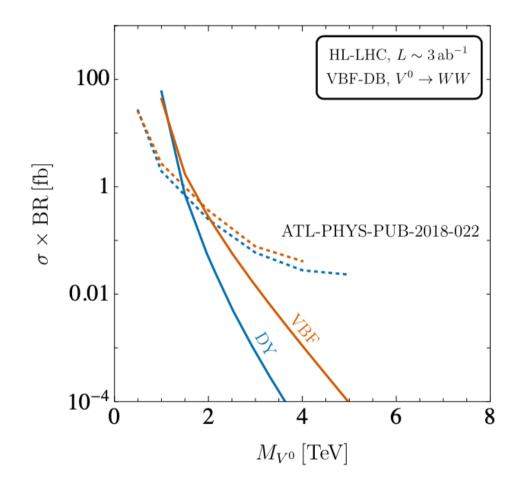
LHC Search for Triplet Vector Boson





HL-LHC Search for Triplet Vector Boson





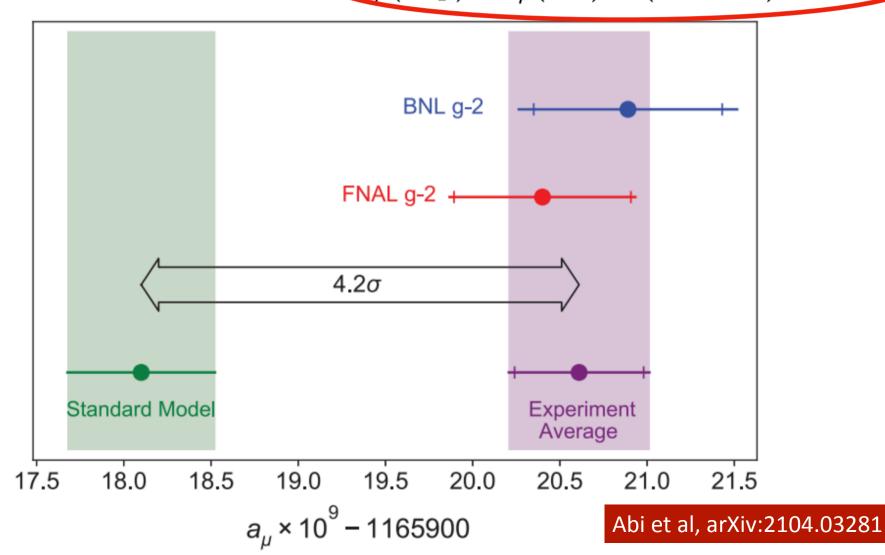


Fermilab Measurement

FNAL result: $a_{\mu}(\text{FNAL}) = 116\,592\,040(54) \times 10^{-11}$ (0.46 ppm)

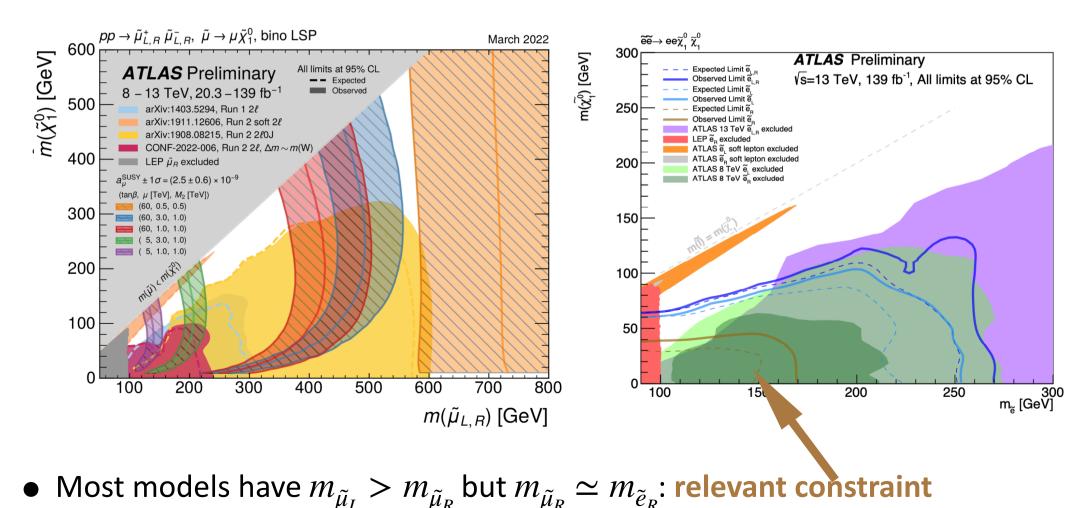
Combined result: $a_{\mu}(\text{Exp}) = 116\,592\,061(41) \times 10^{-11}$ (0.35 ppm)

Difference from Standard Model $a_{\mu}(\mathrm{Exp}) - a_{\mu}(\mathrm{SM}) = (251 \pm 59) \times 10^{-11}$



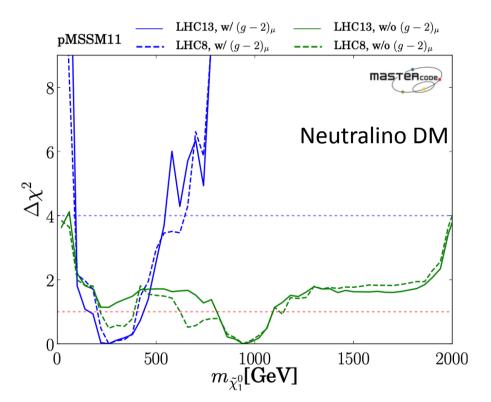
LHC vs Supersymmetry

- LHC favours squarks & gluinos > 2 TeV (but loopholes)
- Does not exclude lighter electroweakly-interacting particles, e.g., sleptons

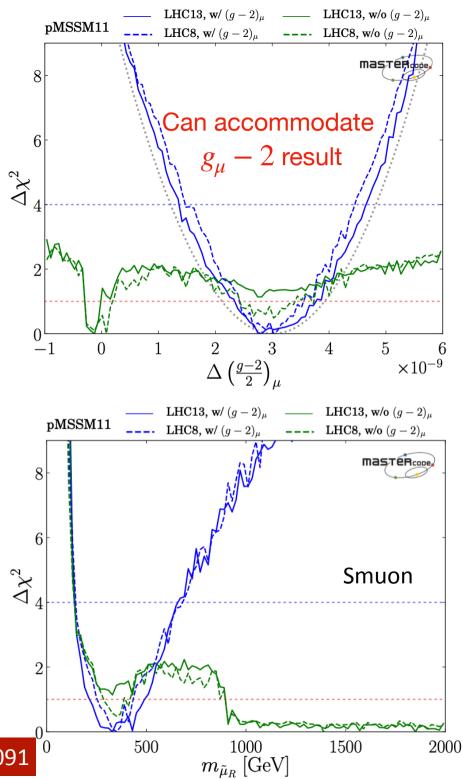


g_{μ} — 2 in Phenomenological Supersymmetry (pMSSM11)

No relation between squark/gluino masses and slepton/neutralino masses

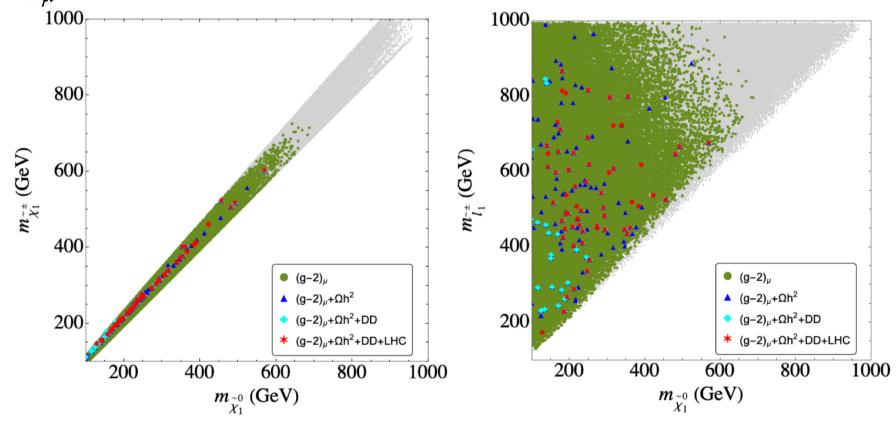


No problem accommodating BNL/FNAL result Neutralino DM, smuon masses $\sim 300/400~{\rm GeV}$ compatible with SUSY dark matter



Supersymmetry

• $g_{\mu}-2$ -friendly scenario with light neutralino, chargino & slepton



 Red star points include all relevant LHC, dark matter density and direct scattering constraints

Chakraborti, Heinemeyer & Saha, arXiv:2104.03287

Summary

