

$\Lambda_b \rightarrow p$ transition form factors in perturbative QCD

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Introduction

- 研究对象： $\Lambda_b \rightarrow p$
- 研究方法：PQCD
- 研究发现：
 - ① twist-4 Λ_b 重子 LCDAs 和 twist-4 和 twist-5 质子 LCDAs 起主要作用
 - ② b 夸克质量不够重，更高阶的贡献起着至关重要的作用

Theoretical framework

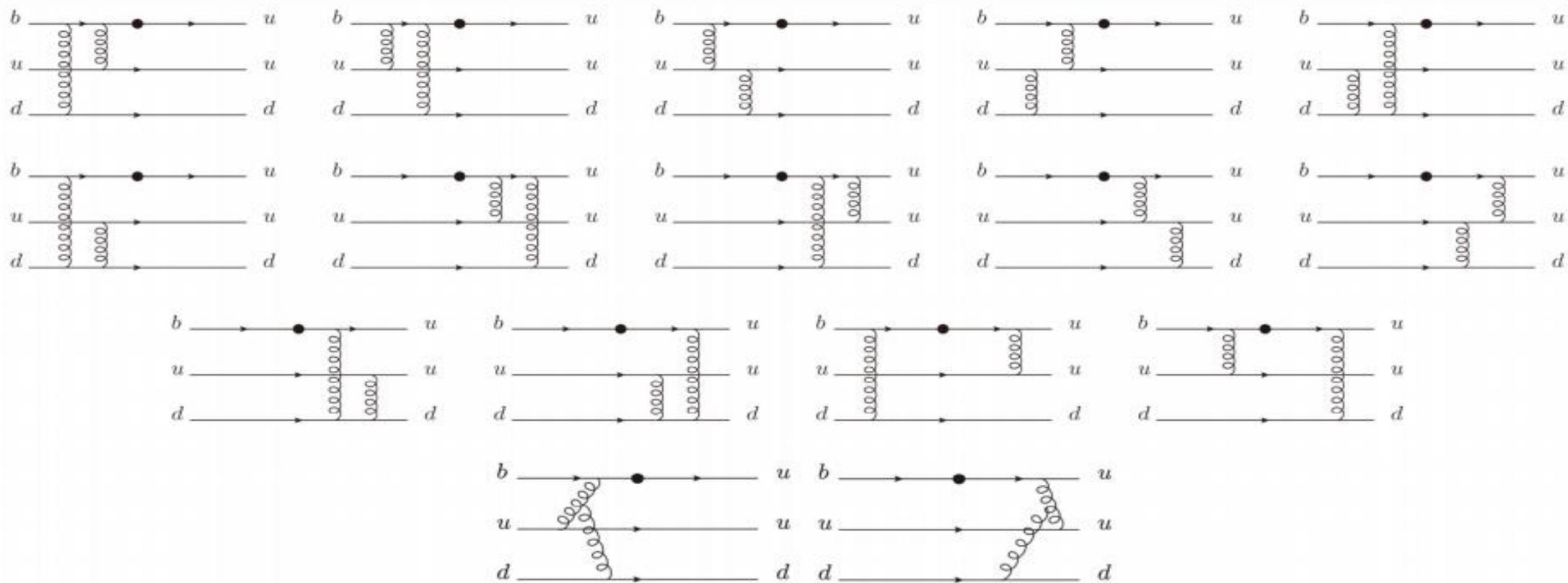


Figure 1: Feynman diagrams for the $\Lambda_b \rightarrow p$ transition form factors, where the black dots denote the weak interaction vertices. These diagrams are labelled by D_1, D_2, \dots and D_{16} in sequence in the text.

Theoretical framework

- Twist-3 LCDAs

$$V_1(x_i) = 120x_1x_2x_3[\phi_3^0 + \phi_3^+(1 - 3x_3)], \quad (18)$$

$$A_1(x_i) = 120x_1x_2x_3(x_2 - x_1)\phi_3^-, \quad (19)$$

$$T_1(x_i) = 120x_1x_2x_3[\phi_3^0 + \frac{1}{2}(\phi_3^- - \phi_3^+)(1 - 3x_3)]. \quad (20)$$

Theoretical framework

- Twist-4 LCDAs

$$V_2(x_i) = 24x_1x_2[\phi_4^0 + \phi_4^+(1 - 5x_3)], \quad (21)$$

$$V_3(x_i) = 12x_3[\psi_4^0(1 - x_3) + \psi_4^-(x_1^2 + x_2^2 - x_3(1 - x_3)) + \psi_4^+(1 - x_3 - 10x_1x_2)], \quad (22)$$

$$A_2(x_i) = 24x_1x_2(x_2 - x_1)\phi_4^-, \quad (23)$$

$$A_3(x_i) = 12x_3(x_2 - x_1)[(\psi_4^0 + \psi_4^+) + \psi_4^-(1 - 2x_3)], \quad (24)$$

$$T_2(x_i) = 24x_1x_2[\xi_4^0 + \xi_4^+(1 - 5x_3)], \quad (25)$$

$$\begin{aligned} T_3(x_i) = & 6x_3[(\xi_4^0 + \phi_4^0 + \psi_4^0)(1 - x_3) + (\xi_4^- + \phi_4^- - \psi_4^-)(x_1^2 + x_2^2 - x_3(1 - x_3)) \\ & + (\xi_4^+ + \phi_4^+ + \psi_4^+)(1 - x_3 - 10x_1x_2)], \end{aligned} \quad (26)$$

$$\begin{aligned} T_7(x_i) = & 6x_3[(-\xi_4^0 + \phi_4^0 + \psi_4^0)(1 - x_3) + (-\xi_4^- + \phi_4^- - \psi_4^-)(x_1^2 + x_2^2 - x_3(1 - x_3)) \\ & + (-\xi_4^+ + \phi_4^+ + \psi_4^+)(1 - x_3 - 10x_1x_2)], \end{aligned} \quad (27)$$

$$S_1(x_i) = 6x_3(x_2 - x_1)[(\xi_4^0 + \phi_4^0 + \psi_4^0 + \xi_4^+ + \phi_4^+ + \psi_4^+) + (\xi_4^- + \phi_4^- - \psi_4^-)(1 - 2x_3)], \quad (28)$$

$$P_1(x_i) = 6x_3(x_2 - x_1)[(\xi_4^0 - \phi_4^0 - \psi_4^0 + \xi_4^+ - \phi_4^+ - \psi_4^+) + (\xi_4^- - \phi_4^- + \psi_4^-)(1 - 2x_3)]. \quad (29)$$

Theoretical framework

- Twist-5 LCDAs

$$V_4(x_i) = 3[\psi_5^0(1 - x_3) + \psi_5^-(2x_1x_2 - x_3(1 - x_3)) + \psi_5^+(1 - x_3 - 2(x_1^2 + x_2^2))], \quad (30)$$

$$V_5(x_i) = 6x_3[\phi_5^0 + \phi_5^+(1 - 2x_3)], \quad (31)$$

$$A_4(x_i) = 3(x_2 - x_1)[- \psi_5^0 + \psi_5^- x_3 + \psi_5^+(1 - 2x_3)], \quad (32)$$

$$A_5(x_i) = 6x_3(x_2 - x_1)\phi_5^-, \quad (33)$$

$$\begin{aligned} T_4(x_i) = & \frac{3}{2}[(\xi_5^0 + \psi_5^0 + \phi_5^0)(1 - x_3) + (\xi_5^- + \phi_5^- - \psi_5^-)(2x_1x_2 - x_3(1 - x_3)) \\ & + (\xi_5^+ + \phi_5^+ + \psi_5^+)(1 - x_3 - 2(x_1^2 + x_2^2))], \end{aligned} \quad (34)$$

$$T_5(x_i) = 6x_3[\xi_5^0 + \xi_5^+(1 - 2x_3)], \quad (35)$$

$$\begin{aligned} T_8(x_i) = & \frac{3}{2}[(\psi_5^0 + \phi_5^0 - \xi_5^0)(1 - x_3) + (\phi_5^- - \phi_5^- - \xi_5^-)(2x_1x_2 - x_3(1 - x_3)) \\ & + (\phi_5^+ + \phi_5^+ - \xi_5^+)(\mu)(1 - x_3 - 2(x_1^2 + x_2^2))], \end{aligned} \quad (36)$$

$$S_2(x_i) = \frac{3}{2}(x_2 - x_1)[-(\psi_5^0 + \phi_5^0 + \xi_5^0) + (\xi_5^- + \phi_5^- - \psi_5^0)x_3 + (\xi_5^+ + \phi_5^+ + \psi_5^0)(1 - 2x_3)], \quad (37)$$

$$P_2(x_i) = \frac{3}{2}(x_2 - x_1)[(\psi_5^0 + \phi_5^0 - \xi_5^0) + (\xi_5^- - \phi_5^- + \psi_5^0)x_3 + (\xi_5^+ - \phi_5^+ - \psi_5^0)(1 - 2x_3)]. \quad (38)$$

- Twist-6 LCDAs

$$V_6(x_i) = 2[\phi_6^0 + \phi_6^+(1 - 3x_3)], \quad (39)$$

$$A_6(x_i) = 2(x_2 - x_1)\phi_6^-, \quad (40)$$

$$T_6(x_i) = 2[\phi_6^0 + \frac{1}{2}(\phi_6^- - \phi_6^+)(1 - 3x_3)], \quad (41)$$

Numerical results

Table 1: Twist classification of the proton LCDAs in Eq. (16).

	twist-3	twist-4	twist-5	twist-6
Vector	V_1	V_2, V_3	V_4, V_5	V_6
Pseudo-Vector	A_1	A_2, A_3	A_4, A_5	A_6
Tensor	T_1	T_2, T_3, T_7	T_4, T_5, T_8	T_6
Scalar		S_1	S_2	
Pseudoscalar		P_1	P_2	

Table 2: Parameters in the proton LCDAs in units of 10^{-2} GeV² [73]. The accuracy of those parameters without uncertainties is of order of 50%.

	ϕ_i^0	ϕ_i^-	ϕ_i^+	ψ_i^0	ψ_i^-	ψ_i^+	ξ_i^0	ξ_i^-	ξ_i^+
twist-3 ($i = 3$)	0.53 ± 0.05	2.11	0.57						
twist-4 ($i = 4$)	-1.08 ± 0.47	3.22	2.12	1.61 ± 0.47	-6.13	0.99	0.85 ± 0.31	2.79	0.56
twist-5 ($i = 5$)	-1.08 ± 0.47	-2.01	1.42	1.61 ± 0.047	-0.98	-0.99	0.85 ± 0.31	-0.95	0.46
twist-6 ($i = 6$)	0.53 ± 0.05	3.09	-0.25						

Numerical results

Table 3: Form factors in units of 10^{-3} from the leading-twist Λ_b baryon LCDA in Eq. (15) and the proton LCDAs of various twists.

	Twist-3	Twist-4	Twist-5	Twist-6	Total
f_1	1.9	6.3	1.0	-0.015	9.2
f_2	0.12	-0.45	-0.63	~ 0	-0.96
f_3	-0.015	0.84	0.66	~ 0	1.5
g_1	2.5	8.4	0.71	-0.008	11.6
g_2	0.12	-0.30	-0.66	~ 0	-0.84
g_3	-0.027	0.90	0.64	~ 0	1.5

Summary

- ◆ twist-4 Λ_b 重子LCDAs 和 twist-5 (twist-4) 质子LCDAs 主导了对形状因子 $f_{1,2,3}$ 和 $g_{1,2}$ (形状因子 g_3) 的贡献，而 twist-6 质子LCDAs 的贡献确实受到了抑制。
- ◆ 来自高 twist LCDAs 的端点贡献可以在 PQCD 形式中得到适当地处理。

谢谢！