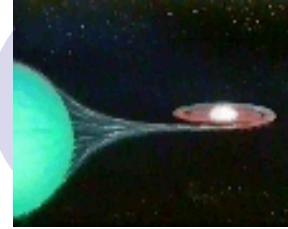


KHz QPOs & millisecond X-ray pulsars in LMXBs



Chengmin Zhang 张承民 (NAOC-CAS)
Dehua Wang 王德华 (Guizhou Norm-U)

Collaborators:

Y.J. Lei, L. Chen, JL.Qu, L.M. Song, H.Yin

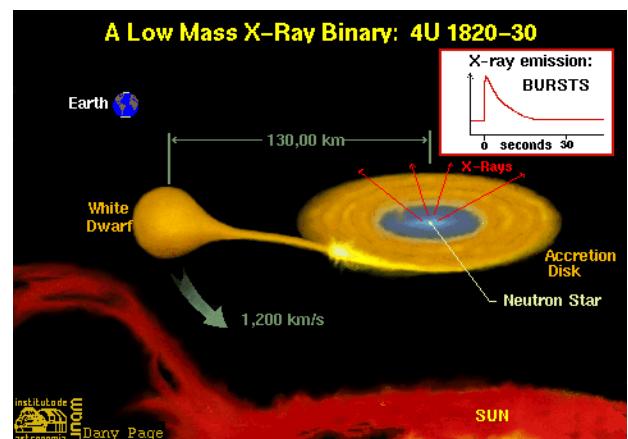
Introduction & Background



Background: oscillations of X-ray in millisecond pulsar near neutron star-LMXB show: QPO, spin, strong gravitation-GR, magnetic field, accretion flow, emission, link of MSP-AMXP, etc.

RXTE (1996-2012, ----) , NICER, ASTROSAT, HXMT, eXTP

1. kHz QPOs of NS-LMXBs
2. Spins of NS-LMXBs
3. Spin and kHz QPO relations
4. Summary

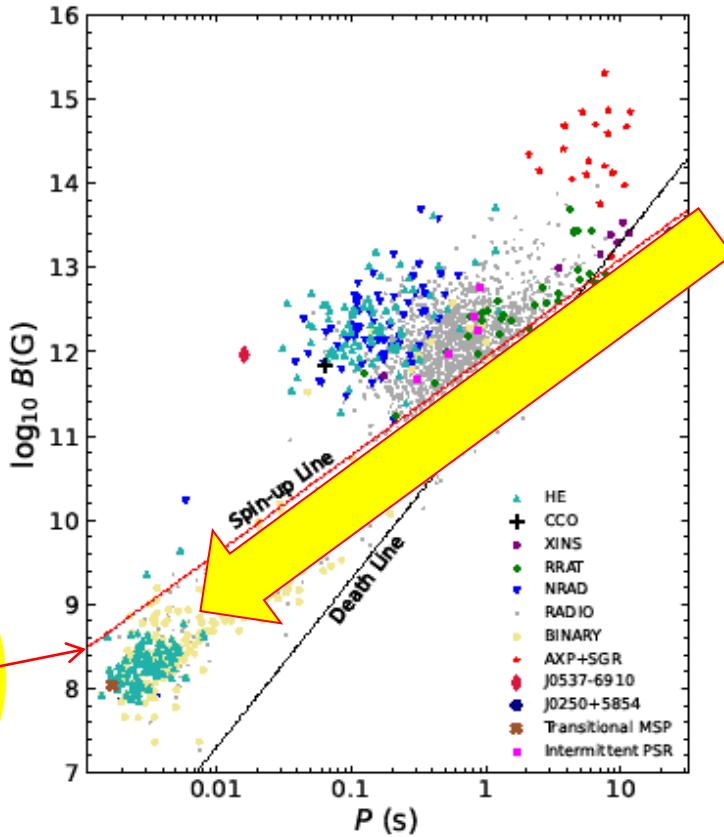


Relation between LMXBs and Radio millisecond pulsars (MSPs)

Pulsar B-P
diagram

LMXBs
MSPs

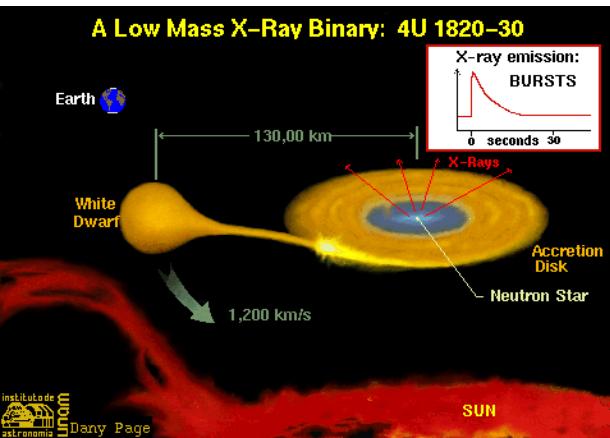
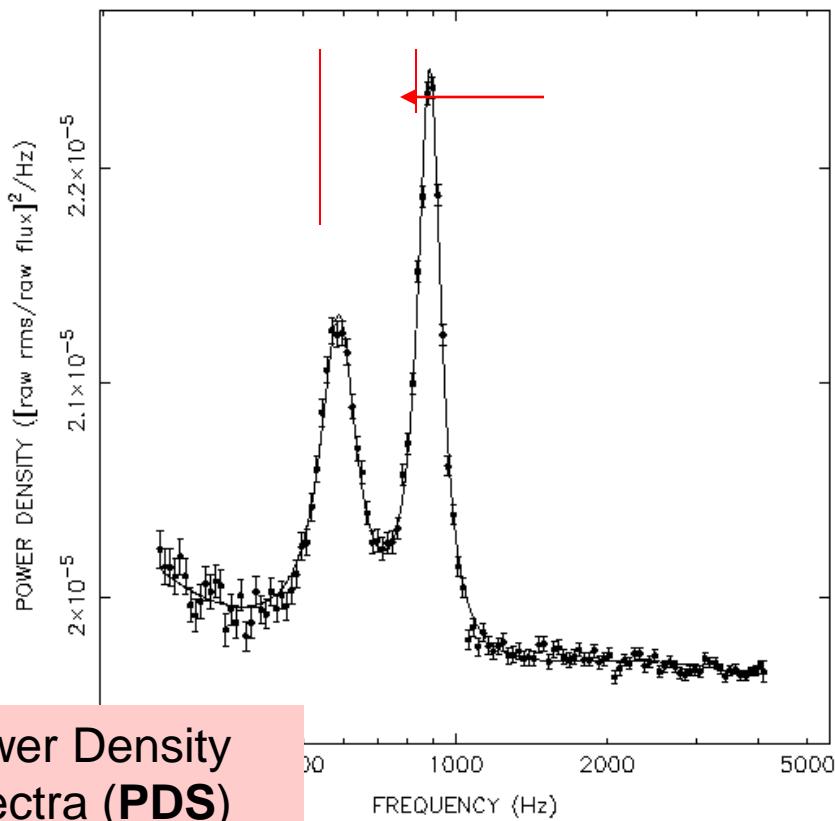
Accretion
Spin-up



1. kHz QPOs in NS-LMXBs

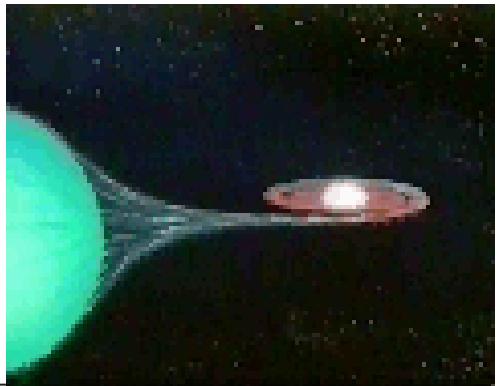
Mendez & Belloni 2021; van der Klis 2006

Twin kHz QPO difference ~300 Hz



Typically: Twin KHz QPO
Upper $\nu_2 \sim 1000$ (Hz)
Lower $\nu_1 \sim 700$ (Hz)
~>300 pairs of kHz QPOs

Quasi-Periodic Oscillations (QPOs)



KiloHertz QPOs:

Time scale is orbital time scale at inner accretion disk.

Other band QPOs:

HBO, NBO, Noise

Not understood well !

kHz QPOs in two types of Sources of NS/LMXBs

Atoll --- Z

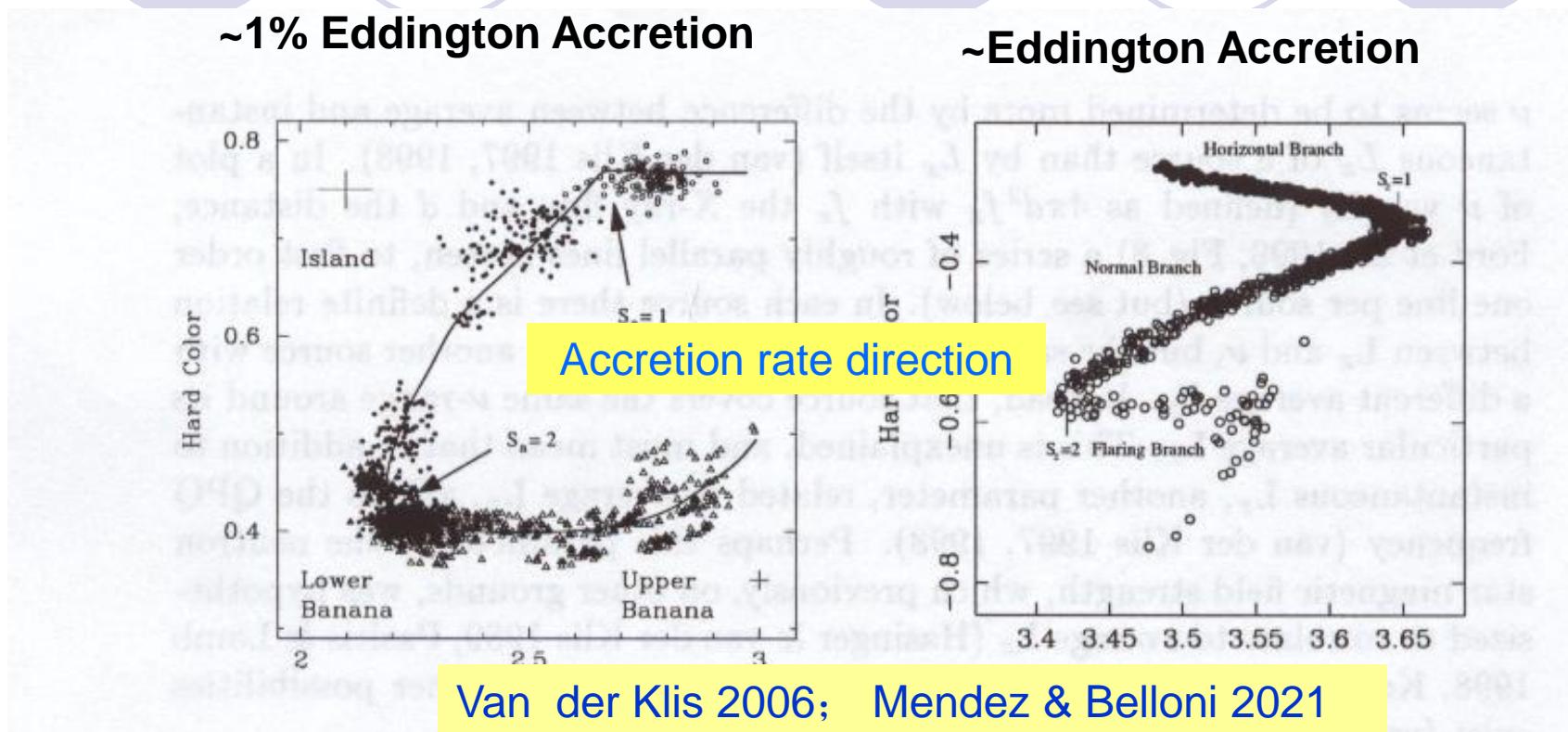


Figure 7: Left: X-ray color-color diagram of the atoll source 4U 1608–52. (Méndez et al. 1999) Right: X-ray hardness vs. intensity diagram of the Z source GX 340+0. (after Jonker et al. 1999c) Values of curve-length parameters S_z and S_a and conventional branch names are indicated. Mass accretion rate is inferred to increase in the sense of increasing S_a and S_z . X-ray color is the log of a count rate ratio ($3.5\text{--}6.4/2.0\text{--}3.5$ and $9.7\text{--}16.0/6.4\text{--}9.7$ keV for soft and hard color respectively); intensity is in the $2\text{--}16$ keV band. kHz QPO detections are indicated with filled symbols.

2. Spin frequency

Accreting X-ray millisecond pulsar

--- SAX J1808.4-3658 (AXMPs); 401 Hz (2.49 ms)

Prutruno & Watt 2021; Wijnands et al 2003

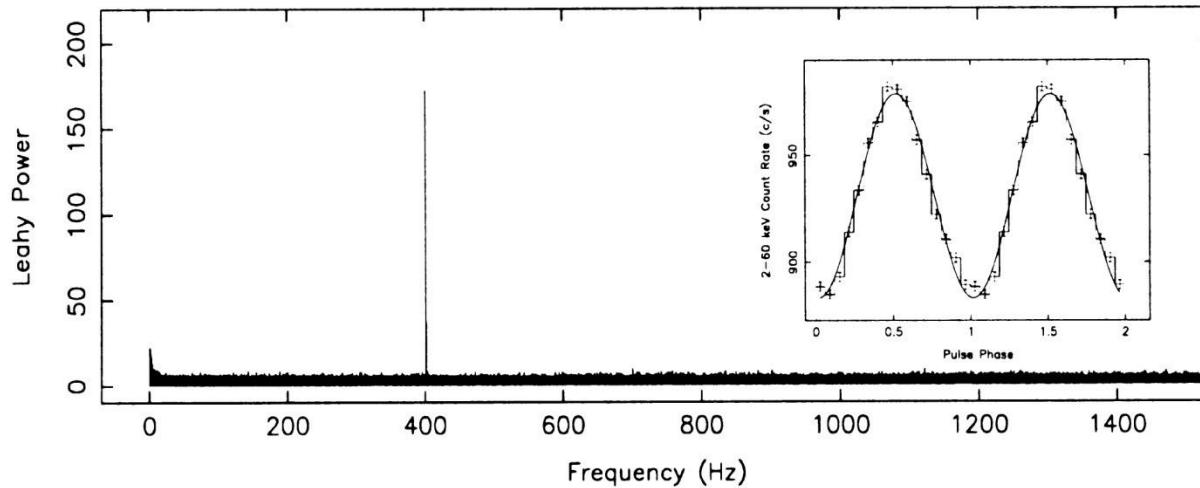
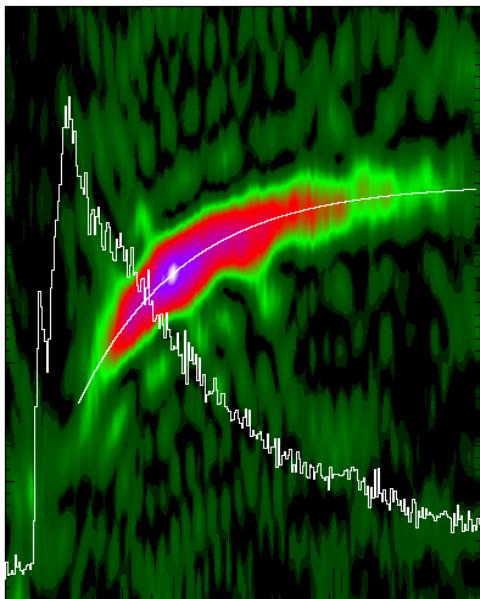
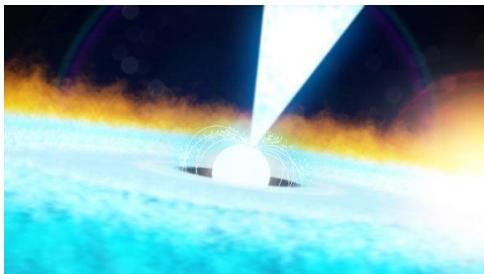


Figure 1: The discovery power spectrum and pulse profile (inset) of the first accreting millisecond X-ray pulsar. Note the low harmonic content evident both from the absence of harmonics in the power spectrum and the near-sinusoidal pulse profile. (after Wijnands & van der Klis 1998b)

2. Spin frequency – Type-I X-ray Burst



Samples

4U1728-34, (363 Hz)
SaxJ1808.4-3658 (401 Hz)

Spin+ burst 40 sources

Galloway & Keek 2021

Summary: Spin and kHz QPOs of LMXBs 1996—2022

1. kHz QPOs (~>300 pairs)

127 - 1329 Hz (4U 0614), Max? :

2. Spin frequency - Burst oscillation (40 samples);

95 - 619 Hz ;

Max=619 Hz (?) Radio MSP 716 Hz

3. HBO, ~ 15-70 Hz, NBO, ~ 5 Hz

3. kHz QPO difference and spin relation

SAXJ 1808.4-3658, Twin kHz QPOs :
700 Hz, 500 Hz; Burst--spin: 401 Hz;
Wijnands et al 2003

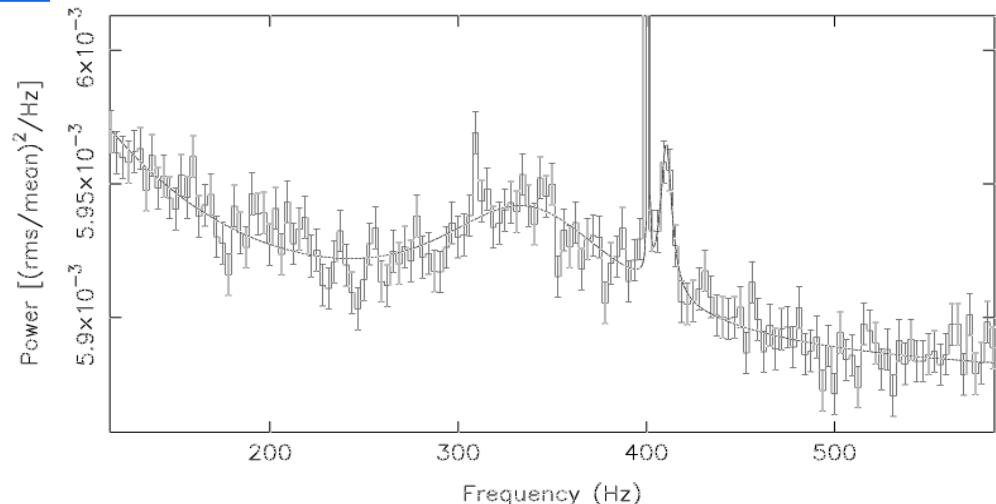
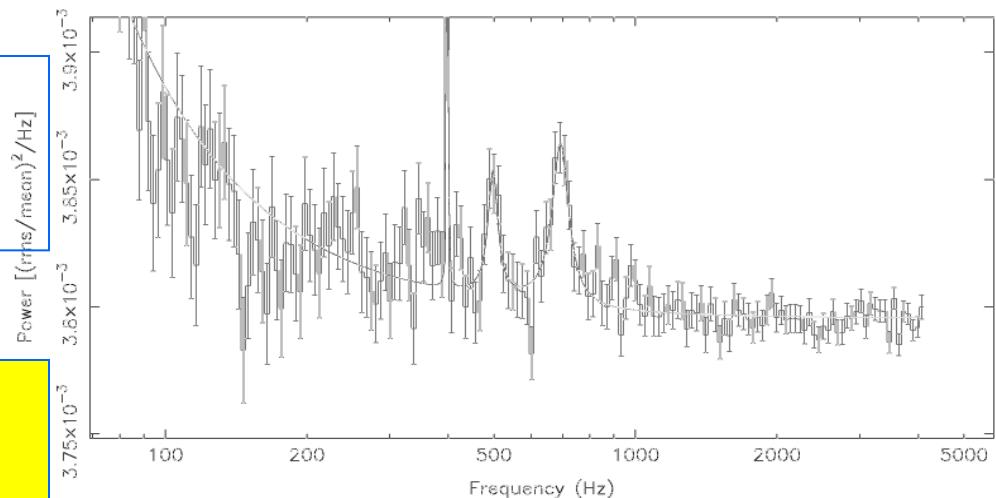
Burst frequency = spin frequency

XTE 1807-294, twin kHz QPOs, 191 Hz

Zhang F et al 2007

Slow rotator; separation/spin ~ 1
Fast rotator; separation/spin ~ 0.5

Linares & van der Klis 2007



difference of twin kHz QPOs = const?

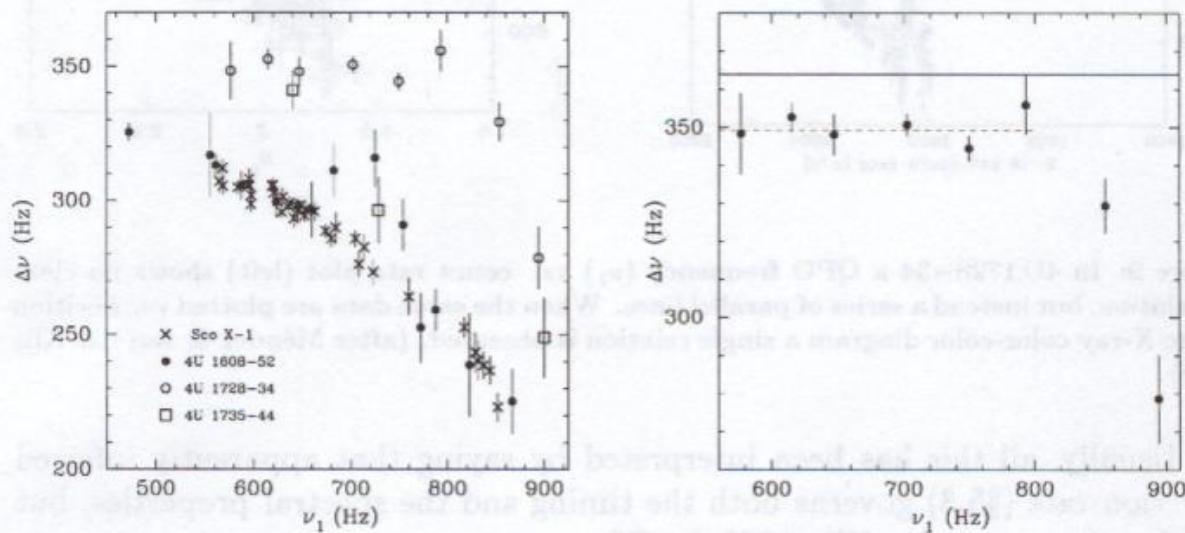


Figure 10: Left: the variations in kHz QPO peak separation as a function of the lower kHz frequency. Right: the data on 4U 1728–34. The burst oscillation frequency is indicated by a horizontal drawn line (Méndez & van der Klis 1999).

Separation = 173 – 359 Hz for all sources

TWELVE sources with twin kHz QPO & spin frequencies

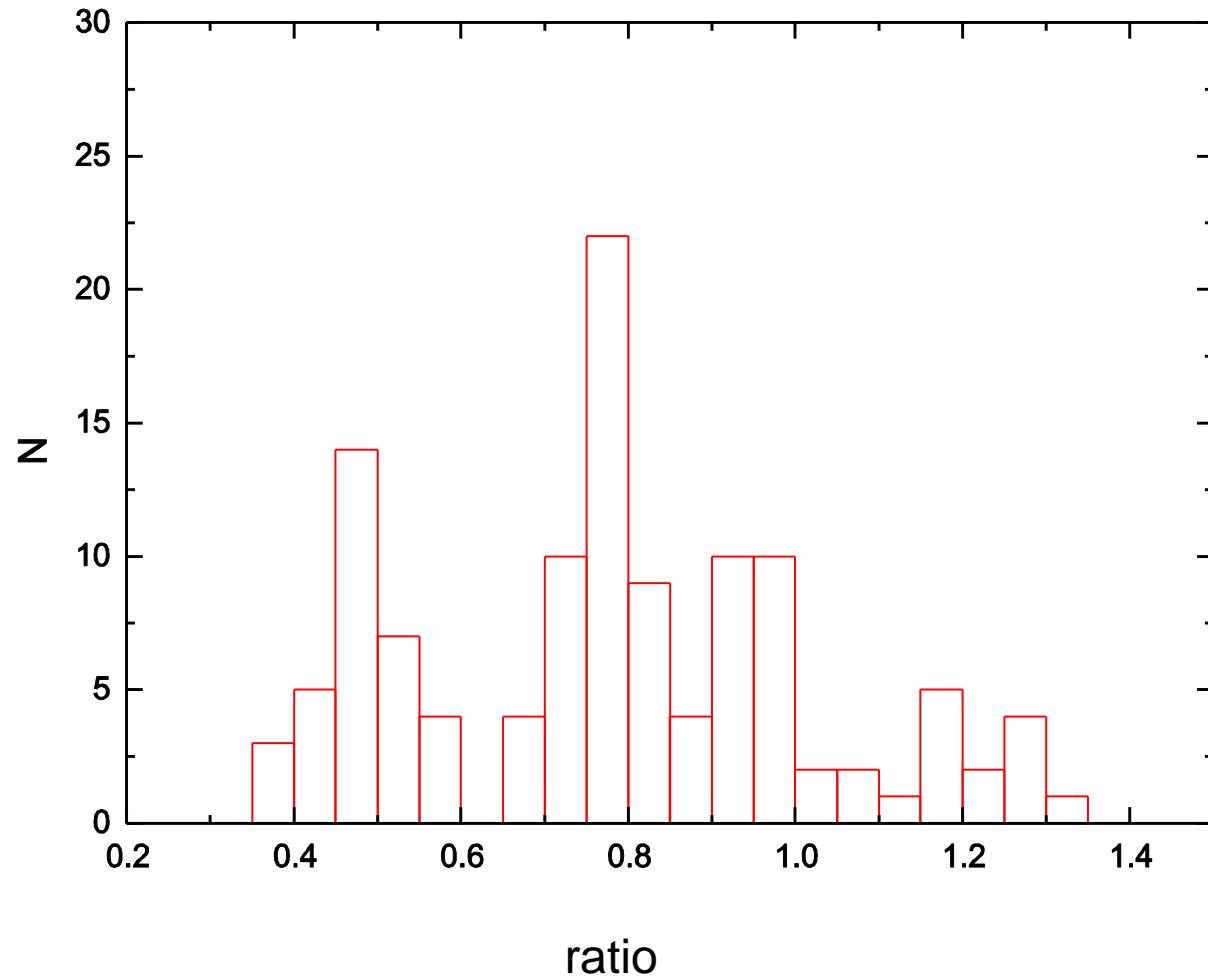
Millisecond pulsars

	sep	spin	ratio
• XTE J1807-294	79-247	191	0.94-1.29
• SAX J1808.4-3658	195	401	0.49

Atoll sources

• 4U 1608-52	224-327	619	0.36-0.53
• 4U 1636-53	217-329	581	0.37-0.57
• 4U 1702-43	333	330	1.01
• 4U 1728-34	271-359	363	0.75-0.99
• KS 1731-260	266	524	0.51
• 4U 1915-05	290-353	270	1.07-1.31
• IGR J17191	330	294	1.12
• SAX J1750.8-29	317	601	0.53
• 4U 0614+09	238-382	415	0.57-0.92
• Aql X-1	278-280	550	0.51-0.51

Ratio of kHz QPO difference to Spin for 12 sources



Twin kHz QPO relation

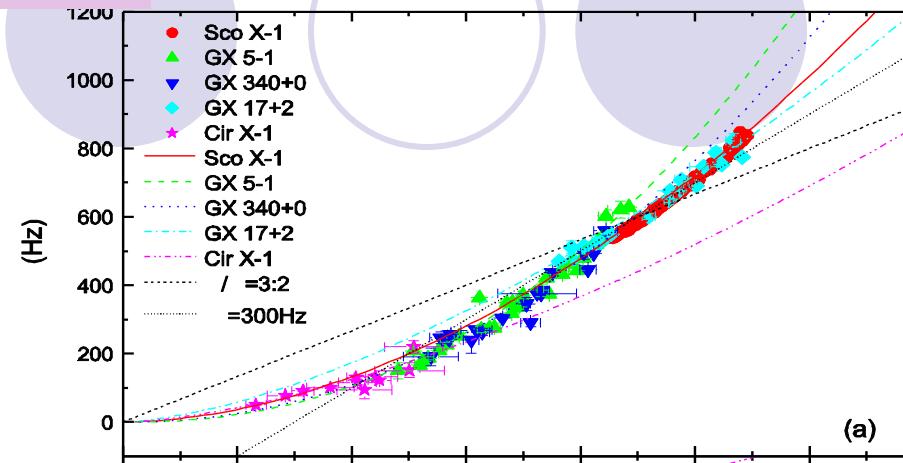
1. separation is constant ? (beat)
2. Linear relation: $v_2 = A v_1 + B$?
3. Ratio is a constant : 3:2 ?

Non-linear relation

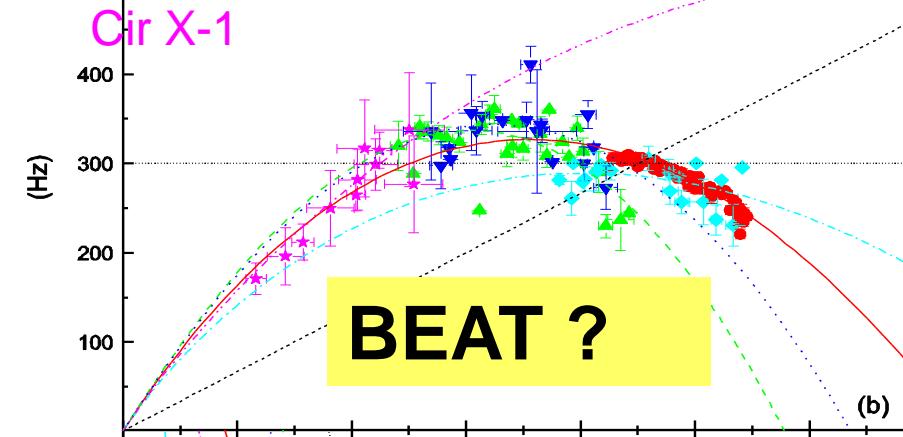
$$v_1 = \sim 700. \text{ (Hz)} (v_2 / 1000 \text{Hz})^b$$

$b \sim 1.6$ Atoll Source, e.g. 4U1728

$b \sim 1.8$ Z Source, e.g. Sco X-1



(a)



(b)

difference
(Hz)

Ratio
 l

BEAT ?

Ratio const ?

Models of kHz QPO: upper frequency = Keplerian Flow

1. Beat model, Miller & Lamb
2. Relativistic precession Model, Stella & Vrtrie
3. Alfvén wave model: Zhang, Li XD & zhang,

Beat Model for KHz QPO

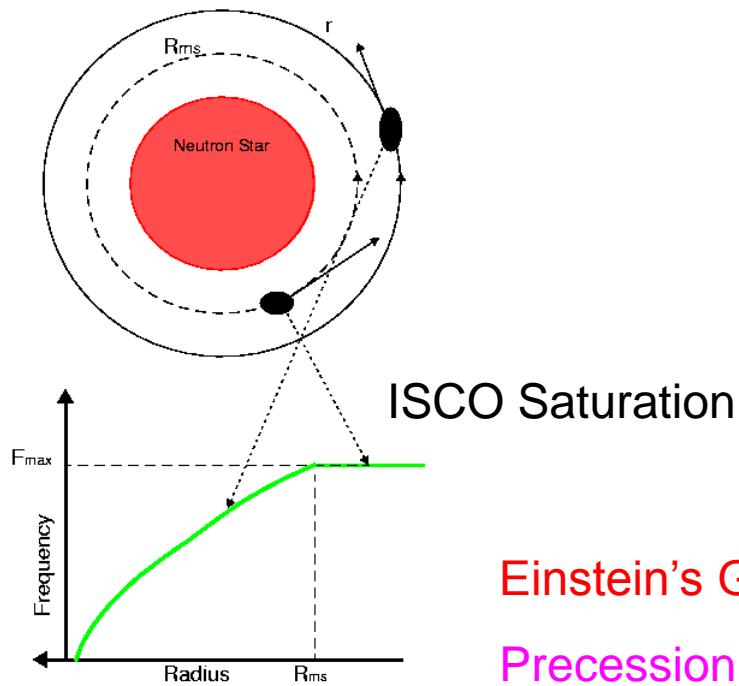
$$v_2 = v_{\text{kepler}}$$

$$v_1 = v_{\text{kepler}} - v_{\text{spin}}$$

$$\Delta v = v_2 - v_1 = v_{\text{spin}}$$

...Constant

Relativistic precession model by Stella & Vietri 1999



Einstein's General Relativity: Perihelion precession

Precession Model for KHz QPO,

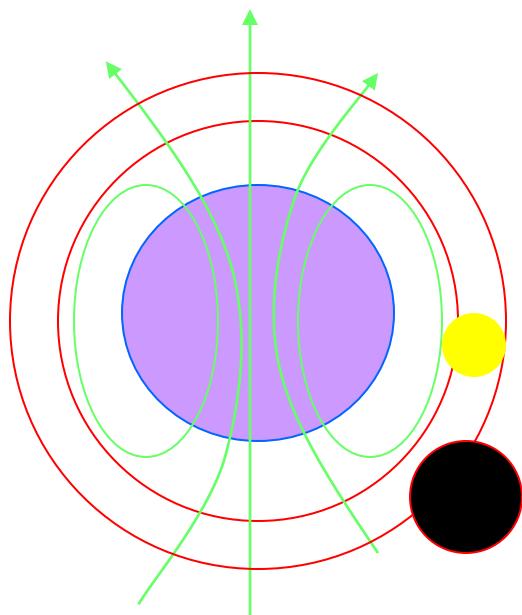
$$v_2 = v_{\text{kepler}}$$

$$v_1 = v_{\text{precession}} = v_2 [1 - (1 - 3R_s/r)^{1/2}]$$

$$\Delta v = v_2 - v_1 \text{ is not constant}$$

Alfven wave oscillation MODEL , Zhang 2004; Li & Zhang 2005;

Keplerian Orbital frequency, MHD Alfven wave Oscillation in the orbit



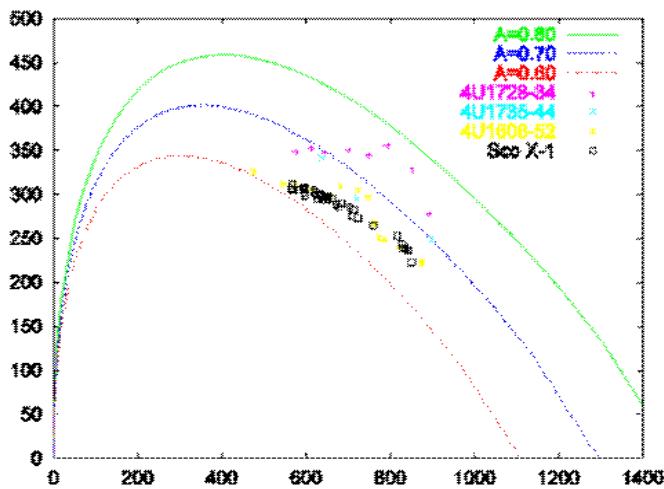
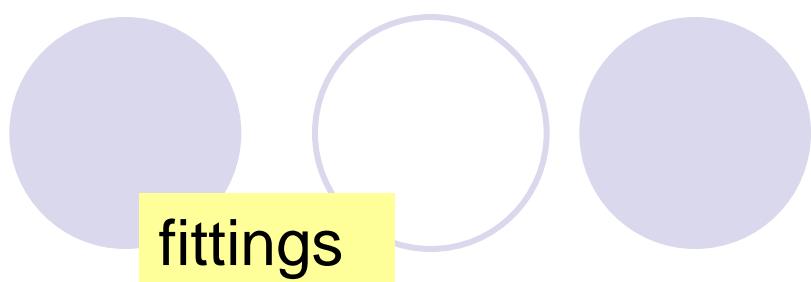
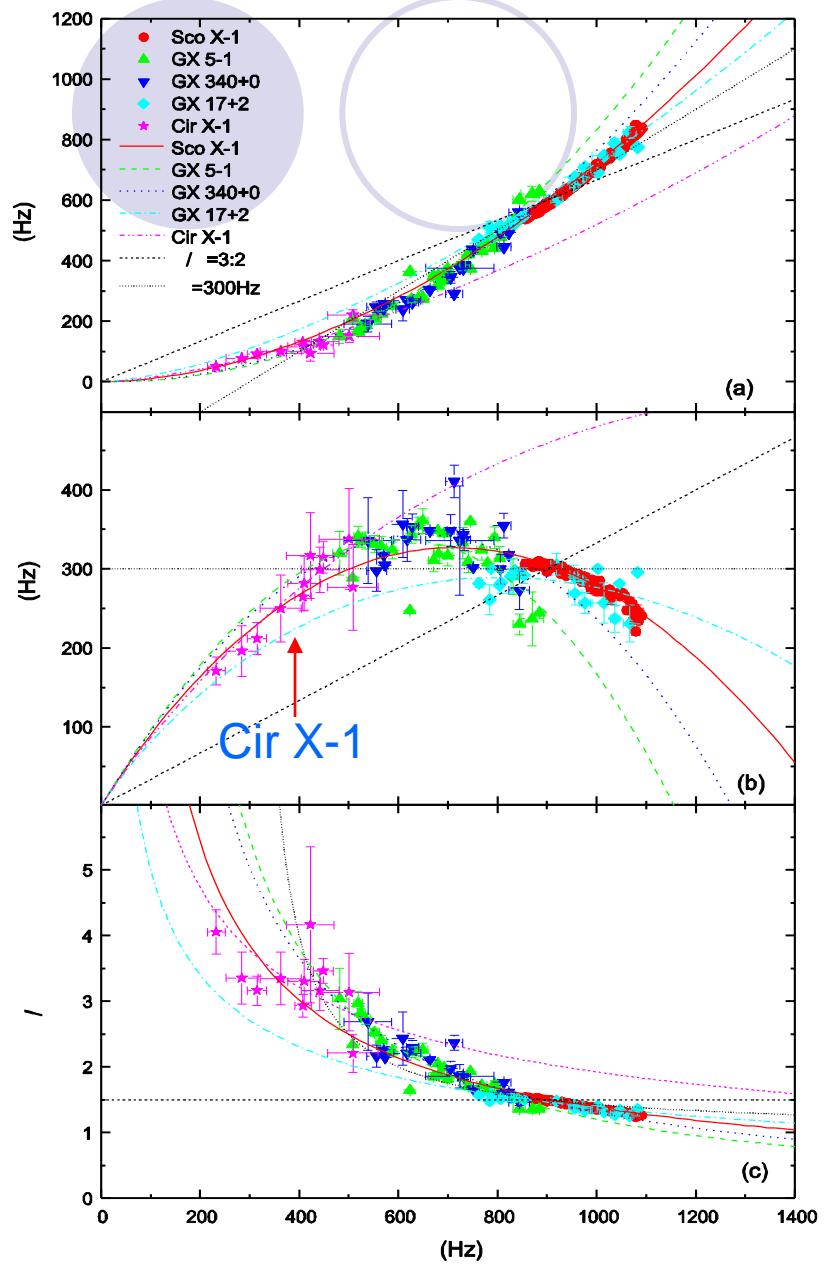
$$v_2 = 1850 \text{ (Hz)} A X^{3/2}$$

$$v_1 = v_2 X (1 - (1-X)^{1/2})^{1/2}$$

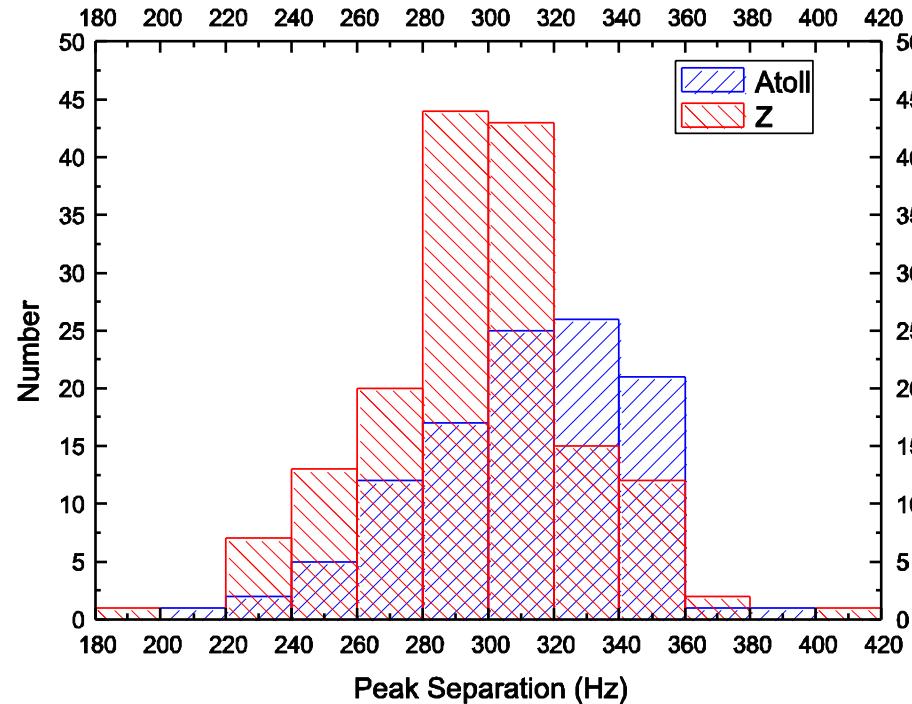
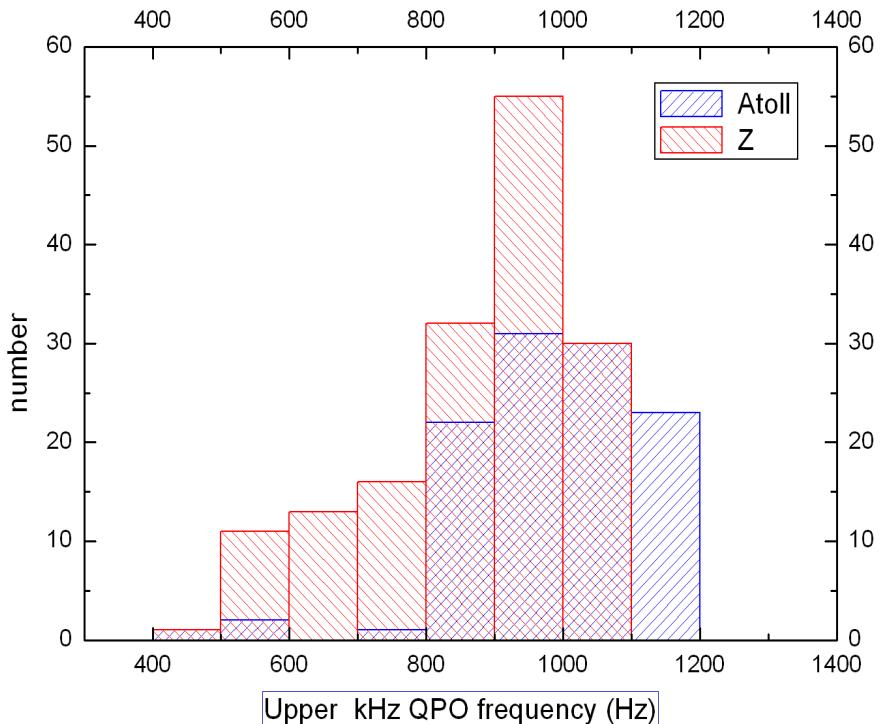
$$A = m^{1/2} / R_6^{3/2}; \quad X = R/r,$$

m : NS mass in solar mass

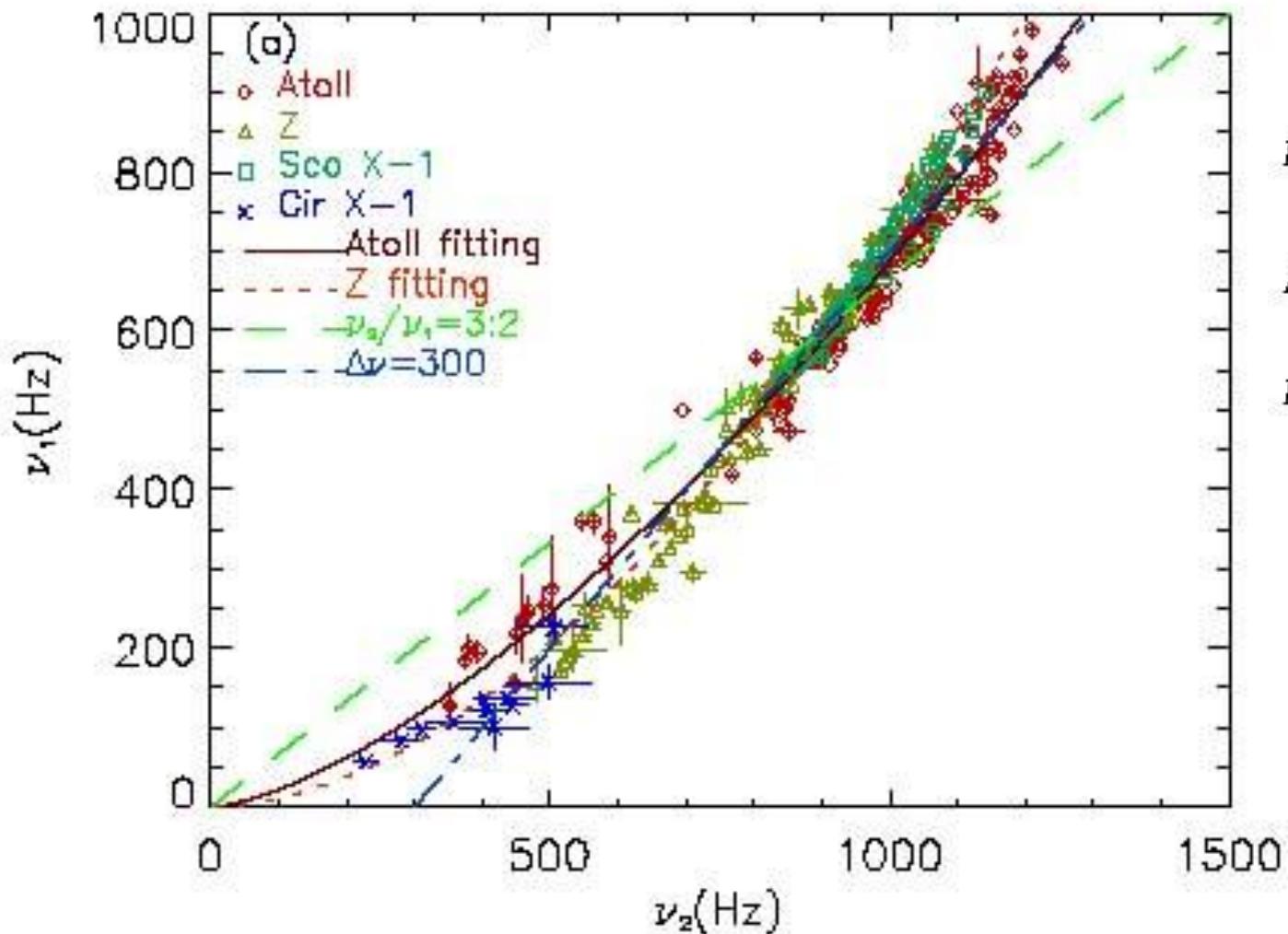
R_6 is NS radius in 10^6 cm



Twin kHz QPO distribution



模型检验



$$\nu_1 = a\left(\frac{\nu_2}{1000}\right)^b \text{Hz}$$

$$\Delta\nu = 300 \text{Hz}$$

$$\nu_2/\nu_1 = 3 : 2$$

拟合结果：指数模型明显优于图另两种模型

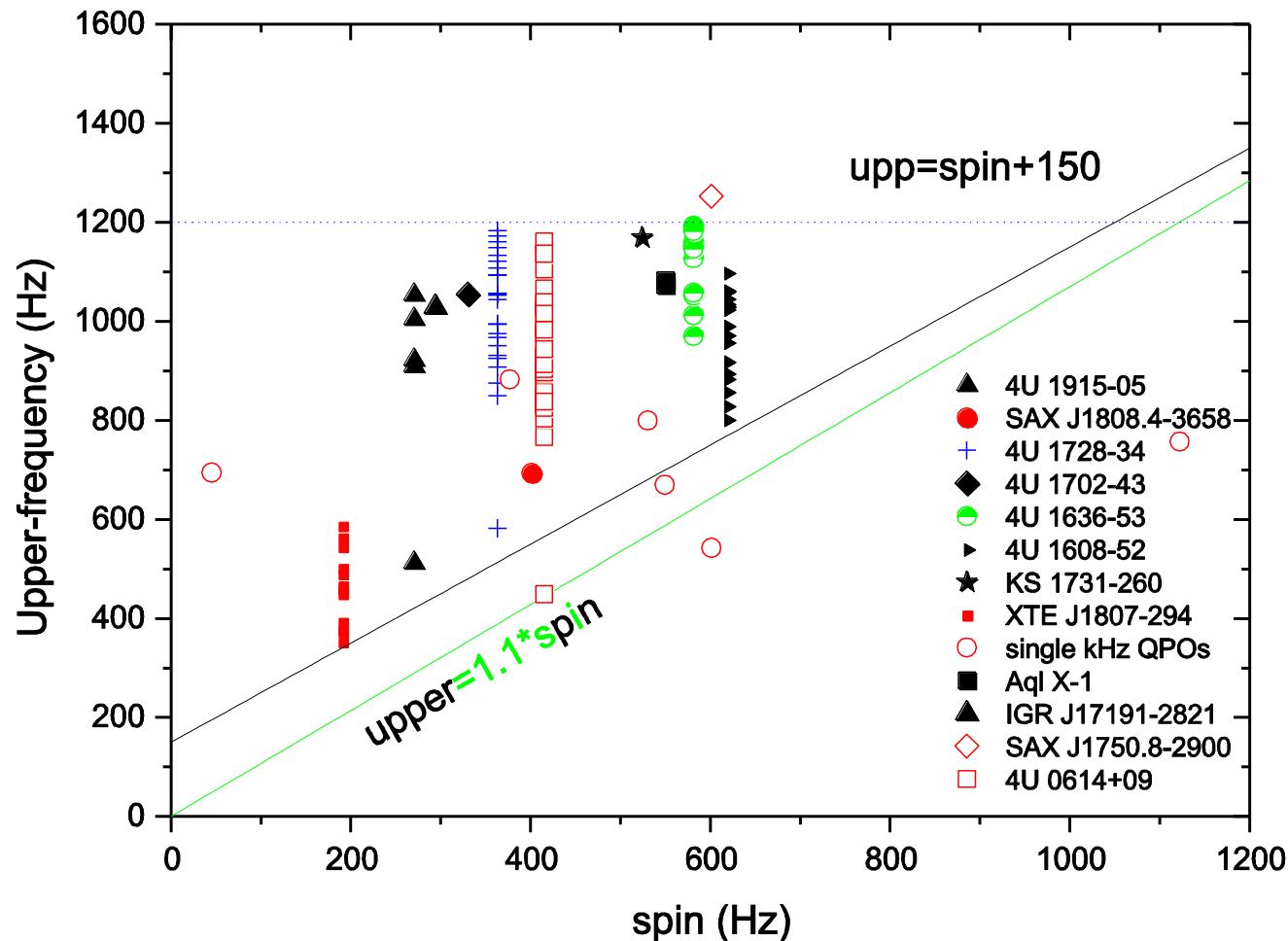
Atoll—— $\chi^2 / d.o.f. = 1.92$ —— $\chi^2 / d.o.f. = 1.86$

4. Summary

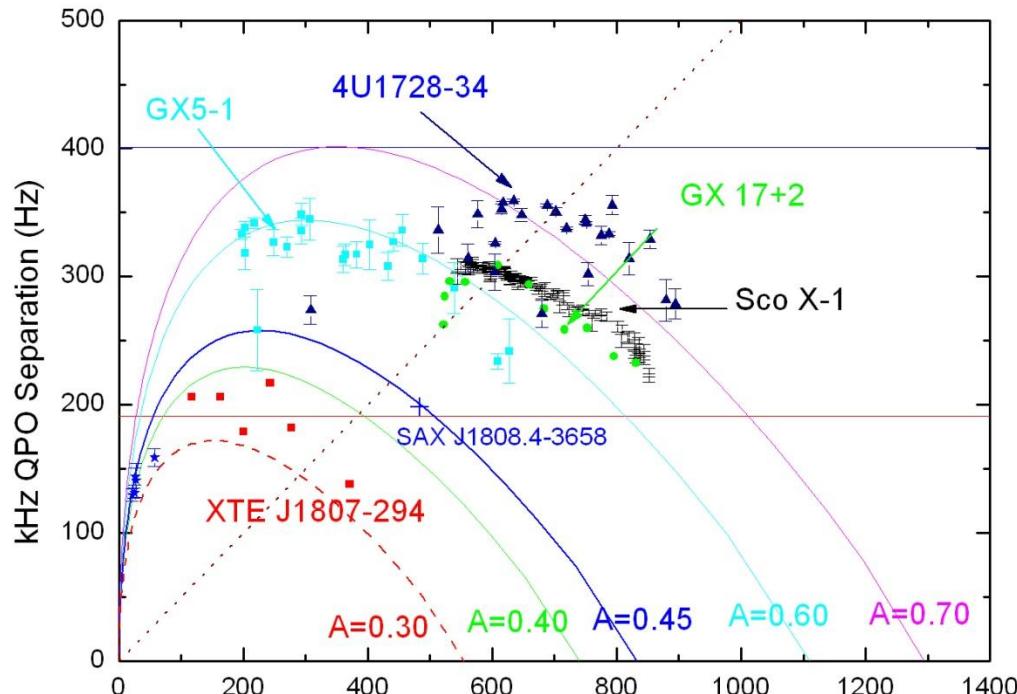
- Spin - kHz QPO relation
 - (a) slow/fast rotator 0.5 - 1.0 ; NO
 - (b) kHz QPO – Spin ; NO direct - No Beat
 - (c) NS twin kHz QPO ratio = 3:2 ? NO
 - (c) Av. kHz QPO – spin relation ? Indirect ?
- twin kHz QPOs – nonlinear relation, Yes
- kHz QPOs Model ? Not yet understood well
- Questions:
 - Radio MSP spin origin ? AMXP? Not same, Wang et al 2021
 - Maximum spin >1000 Hz ? Sub-MSP ? Not yet
 - Minimum magnetic field of MSP = 10^7 Gauss ?

Thanks

Lower of twin kHz QPO frequency > 1.1 spin frequency



AMXP: special cases of 1.5 shift SAXJ1808.4-365; XTE J1807-294



SAXJ1808.4-365: Wijnands et al 2003; XTE1807-294, F. Zhang et al 2006