



中国科学院高能物理研究所  
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# Probing Higgs CP properties at the CEPC

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JOINT WORKSHOP OF THE CEPC PHYSICS, SOFTWARE AND NEW DETECTOR CONCEPT IN 2022

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[arXiv:2203.11707](https://arxiv.org/abs/2203.11707)

## Probing Higgs $CP$ properties at the CEPC

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### Abstract

In the Circular Electron Positron Collider (CEPC), a measurement of the Higgs  $CP$  mixing through  $e^+e^- \rightarrow ZH \rightarrow \mu^+\mu^-H(\rightarrow bb/cc/gg)$  process is presented, with  $5.6 \text{ ab}^{-1} e^+e^-$  collision data at the center-of-mass energy of 240 GeV. In this study, the  $CP$ -violating parameter  $\hat{\alpha}_{AZ}$  is constrained between the region of  $-8.27 \times 10^{-2}$  and  $8.09 \times 10^{-2}$  and  $\hat{\alpha}_{ZZ}$  between  $-2.15 \times 10^{-2}$  and  $2.02 \times 10^{-2}$  at 95% confidence level. This study demonstrates the great potential of probing Higgs  $CP$  properties at the CEPC.

Keywords: the Higgs Boson,  $CP$  violation, CEPC

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# Introduction

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Properties of Higgs in Standard Model:  $m_H = 125.10\text{GeV}, J^{PC} = 0^{++}$

Related experiments in LHC:

- The hypothesis of spin-1 or spin-2 Higgs has been excluded by the ATLAS and CMS at >99% CL in  $\sqrt{s} = 7\&8\text{ TeV}, 25\text{ fb}^{-1}$  data. [Eur. Phys. J. C75 \(2015\) 476](#)
- The results of the study on the CP properties of the Higgs boson interactions with gauge bosons by the ATLAS and CMS show no deviations from the SM predictions.

Higgs-gauge vector boson interaction lacks precise measurement in all inclusive Higgs production mode(i.e. ggF dominant).

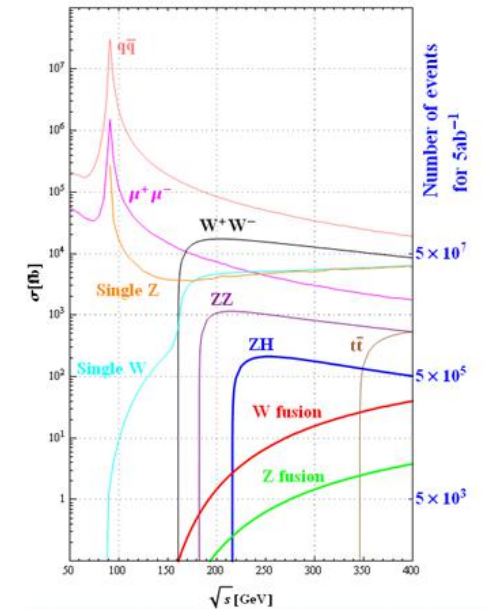
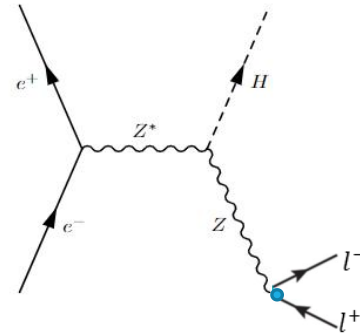
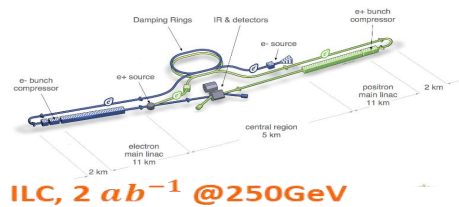
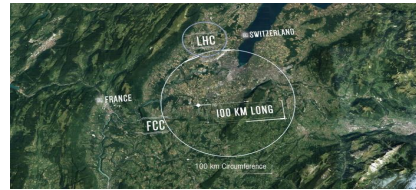
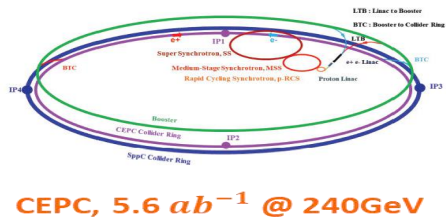
**Any observation of CP violation in Higgs would be New Physics!**

What we want to study is the Higgs CP mixing model aiming to find the CP-odd Higgs.

# Introduction

Future  $e^+e^-$  collider experiment as Higgs factory :

- At a center of mass energy of  $\sqrt{s} \sim 240 \text{ GeV}$  which maximizes the Higgs boson production cross section through  $e^+e^- \rightarrow ZH$  process.
- Cleaner environment and more events produced than (HL)-LHC.
- More precise Higgs-gauge boson coupling study.



Consider a 6-dimension EFT model:  $\mathcal{L}_{eff} = \mathcal{L}_{SM}^{(4)} + \frac{1}{\Lambda^2} \sum_{k=1}^{59} \alpha_k \mathcal{O}_k (\mathcal{L}_{BSM})$

$$\mathcal{L}_{eff} \supset c_{ZZ}^{(1)} H Z_\mu Z^\mu + c_{ZZ}^{(2)} H Z_{\mu\nu} Z^{\mu\nu} + c_{Z\tilde{Z}} H Z_{\mu\nu} \tilde{Z}^{\mu\nu} + c_{AZ} H Z_{\mu\nu} A^{\mu\nu} + c_{A\tilde{Z}}^{HZ\mu\nu} \tilde{A}^{\mu\nu} \\ + H Z_\mu \bar{\ell} \gamma^\mu (c_V + c_{A\gamma_5}) \ell + Z_\mu \bar{\ell} \gamma^\mu (g_V - g_{A\gamma_5}) \ell - g_{em} Q_\ell A_\mu \bar{\ell} \gamma^\mu \ell$$

Where:  $c_{ZZ}^{(1)} = m_Z^2 (\sqrt{2} G_F)^{1/2} (1 + \hat{\alpha}_{ZZ}^{(1)})$ ,  $c_{ZZ}^{(2)} \& = (\sqrt{2} G_F)^{1/2} \hat{\alpha}_{ZZ}$ ,  $c_{Z\tilde{Z}} \& = (\sqrt{2} G_F)^{1/2} \hat{\alpha}_{Z\tilde{Z}}$ ,  
 $c_{AZ} = (\sqrt{2} G_F)^{1/2} \hat{\alpha}_{AZ}$ ,  $c_{A\tilde{Z}} = (\sqrt{2} G_F)^{1/2} \hat{\alpha}_{A\tilde{Z}}$ .

- In this base, the experimental observables  $G_F, m_Z, \alpha_{em}$  could be presented:

$$m_Z = m_{Z0} (1 + \delta_Z), \quad G_F = G_{F0} (1 + \delta_{G_F}), \quad \alpha_{em} = \alpha_{em0} (1 + \delta_A)$$

$$\text{where: } \delta_Z = \hat{\alpha}_{ZZ} + \frac{1}{4} \hat{\alpha}_{\Phi D}, \quad \delta_{G_F} = -\hat{\alpha}_{4l} + 2\hat{\alpha}_{\Phi l}^{(3)}, \quad \delta_A = 2\hat{\alpha}_{AA}.$$

$$m_{Z0} = 91.1876$$

$$G_{F0} = 1.166367e-5$$

$$\alpha_{em0} = 1/127.940$$

The  $H \rightarrow Zll$  matrix element:

$$\mathcal{M}_{HZ\ell\ell}^\mu = \frac{1}{m_H} \bar{u}(p_3, s_3) \left[ \gamma^\mu (H_{1,V} + H_{1,A}\gamma_5) + \frac{q^\mu \not{q}}{m_H^2} (H_{2,V} + H_{2,A}\gamma_5) + \frac{\epsilon^{\mu\nu\sigma\rho} p_\nu q_\sigma}{m_H^2} \gamma_\rho (H_{3,V} + H_{3,A}\gamma_5) \right] v(p_4, s_4)$$

- Where  $\epsilon_{0123} = +1$  and  $q = p_3 + p_4$ .

And the parameters in the function are following:

$$H_{1,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2} r}{r-s} g_V \left( 1 + \hat{\alpha}_1^{\text{eff}} - \frac{\kappa}{r} \hat{\alpha}_{ZZ} - \frac{\kappa}{2r} \frac{Q_\ell g_{em}(r-s)}{sg_V} \hat{\alpha}_{AZ} \right)$$

$$H_{1,A} = \frac{2m_H(\sqrt{2}G_F)^{1/2} r}{r-s} g_A \left( 1 + \hat{\alpha}_2^{\text{eff}} - \frac{\kappa}{r} \hat{\alpha}_{ZZ} \right),$$

$$H_{2,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2}}{r-s} g_V \left[ 2\hat{\alpha}_{ZZ} + \frac{Q_\ell g_{em}(r-s)}{sg_V} \hat{\alpha}_{AZ} \right]$$

$$H_{2,A} = \frac{4m_H(\sqrt{2}G_F)^{1/2}}{r-s} g_A \hat{\alpha}_{ZZ}$$

$$H_{3,V} = -\frac{2m_H(\sqrt{2}G_F)^{1/2}}{r-s} g_V \left[ 2\hat{\alpha}_{ZZ} + \frac{Q_\ell g_{em}(r-s)}{sg_V} \hat{\alpha}_{AZ} \right]$$

$$H_{3,A} = \frac{4m_H(\sqrt{2}G_F)^{1/2}}{r-s} g_A \hat{\alpha}_{ZZ}$$

$$\hat{\alpha}_1^{\text{eff}} \equiv \hat{\alpha}_{ZZ}^{(1)} - \frac{m_H(\sqrt{2}G_F)^{1/2}(r-s)}{2\sqrt{r}} \frac{\hat{\alpha}_{\Phi l}^V}{g_V}$$

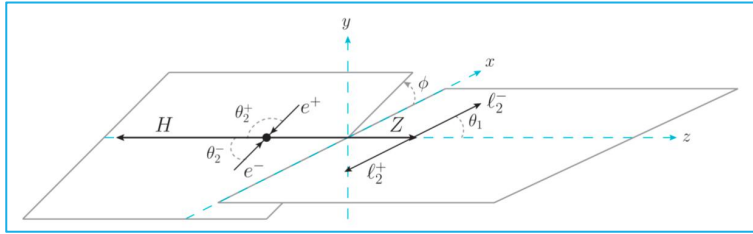
$$\hat{\alpha}_2^{\text{eff}} \equiv \hat{\alpha}_{ZZ}^{(1)} + \frac{m_H(\sqrt{2}G_F)^{1/2}(r-s)}{2\sqrt{r}} \frac{\hat{\alpha}_{\Phi l}^A}{g_A}$$

 : SM term  
Others : EFT contribution

Differential cross section for  $e^+e^- \rightarrow ZH \rightarrow llH$ :

$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = \frac{\mathcal{N}_\sigma(q^2)}{m_H^2} \mathcal{J}(q^2, \theta_1, \theta_2, \phi),$$

$$\mathcal{N}_\sigma(q^2) = \frac{1}{2^{10}(2\pi)^3} \cdot \frac{1}{\sqrt{r}\gamma_Z} \cdot \frac{\sqrt{\lambda(1,s,r)}}{s^2}$$



$$\begin{aligned} \mathcal{J}(q^2, \theta_1, \theta_2, \phi) = & J_1(1 + \cos^2 \theta_1 \cos^2 \theta_2 + \cos^2 \theta_1 + \cos^2 \theta_2) \\ & + J_2 \sin^2 \theta_1 \sin^2 \theta_2 + J_3 \cos \theta_1 \cos \theta_2 \\ & + (J_4 \sin \theta_1 \sin \theta_2 + J_5 \sin 2\theta_1 \sin 2\theta_2) \sin \phi \\ & + (J_6 \sin \theta_1 \sin \theta_2 + J_7 \sin 2\theta_1 \sin 2\theta_2) \cos \phi \\ & + J_8 \sin^2 \theta_1 \sin^2 \theta_2 \sin 2\phi + J_9 \sin^2 \theta_1 \sin^2 \theta_2 \cos 2\phi. \end{aligned}$$

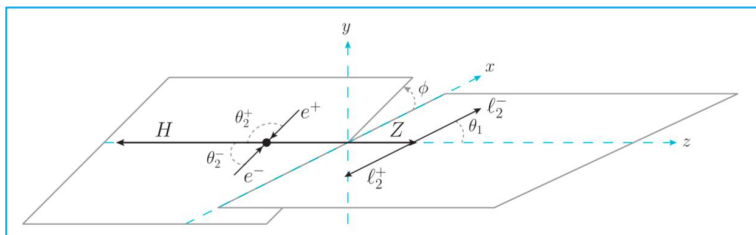
Variables for studying distribution:  $\theta_1, \theta_2, \phi$



Differential cross section for  $e^+ e^- \rightarrow ZH \rightarrow llH$ :

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Variables for studying distribution:  $\theta_1, \theta_2, \phi$

Assumption for simplification:

- $\hat{\alpha}_{A\tilde{Z}}$  and  $\hat{\alpha}_{Z\tilde{Z}}$  contribute to cp-odd. (useful parameters)
- Others are set to 0, so  $H_{2,V/A} = 0$ .

$$J_1 = 2rs(g_A^2 + g_V^2)(|H_{1,V}|^2 + |H_{1,A}|^2),$$

$$J_2 = \kappa(g_A^2 + g_V^2)[\kappa(|H_{1,V}|^2 + |H_{1,A}|^2) + \lambda \text{Re}(H_{1,V}H_{2,V}^* + H_{1,A}H_{2,A}^*)],$$

$$J_3 = 32rs g_A g_V \text{Re}(H_{1,V}H_{1,A}^*),$$

$$J_4 = 4\kappa\sqrt{rs}\lambda g_A g_V \text{Re}(H_{1,V}H_{3,A}^* + H_{1,A}H_{3,V}^*),$$

$$J_5 = \frac{1}{2}\kappa\sqrt{rs}\lambda(g_A^2 + g_V^2) \text{Re}(H_{1,V}H_{3,V}^* + H_{1,A}H_{3,A}^*),$$

$$J_6 = 4\sqrt{rs}g_A g_V [4\kappa \text{Re}(H_{1,V}H_{1,A}^*) + \lambda \text{Re}(H_{1,V}H_{2,A}^* + H_{1,A}H_{2,V}^*)],$$

$$J_7 = \frac{1}{2}\sqrt{rs}(g_A^2 + g_V^2) [2\kappa(|H_{1,V}|^2 + |H_{1,A}|^2) + \lambda \text{Re}(H_{1,V}H_{2,V}^* + H_{1,A}H_{2,A}^*)],$$

$$J_8 = 2rs\sqrt{\lambda}(g_A^2 + g_V^2) \text{Re}(H_{1,V}H_{3,V}^* + H_{1,A}H_{3,A}^*),$$

$$J_9 = 2rs(g_A^2 + g_V^2)(|H_{1,V}|^2 + |H_{1,A}|^2).$$

6 of these 9 functions are independent

|  |                      |
|--|----------------------|
| <del>—</del>   | 0 in assumption      |
| <span style="border: 1px solid blue; padding: 2px;"> </span> | EFT CP-odd term      |
| Others   | CP-even contribution |

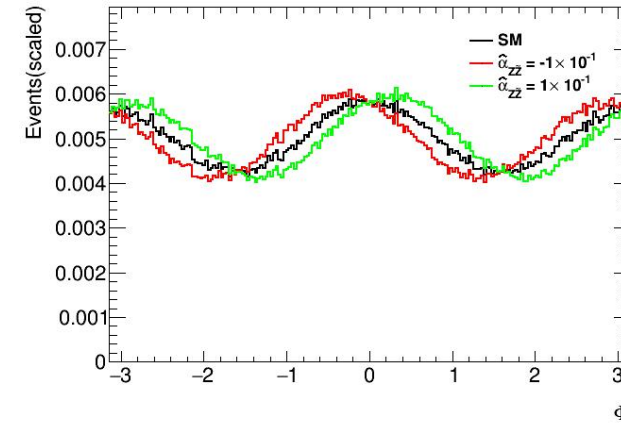
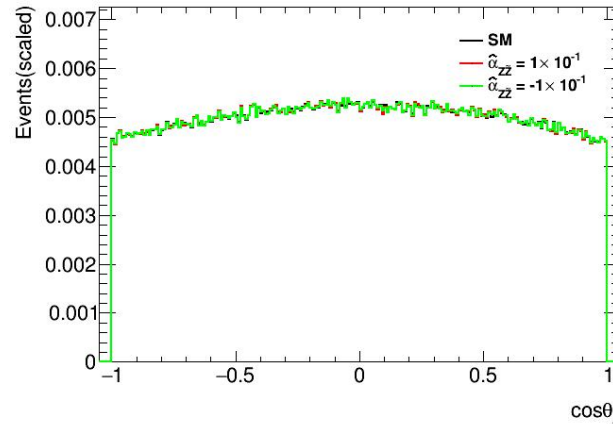
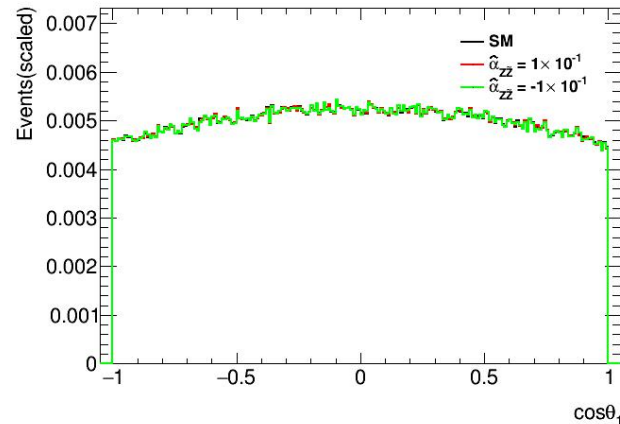
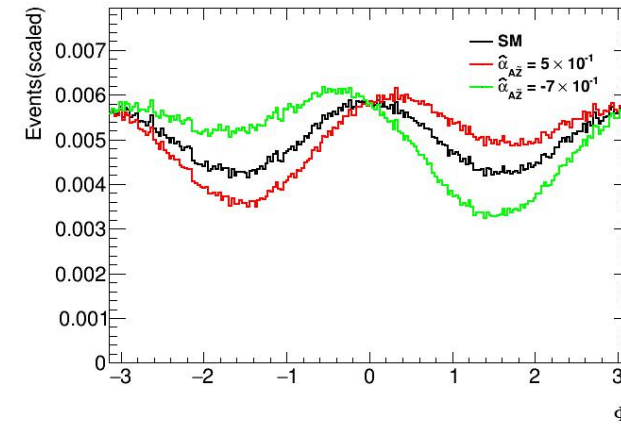
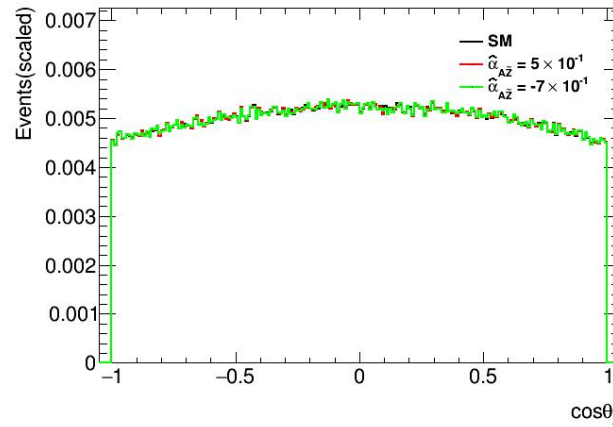
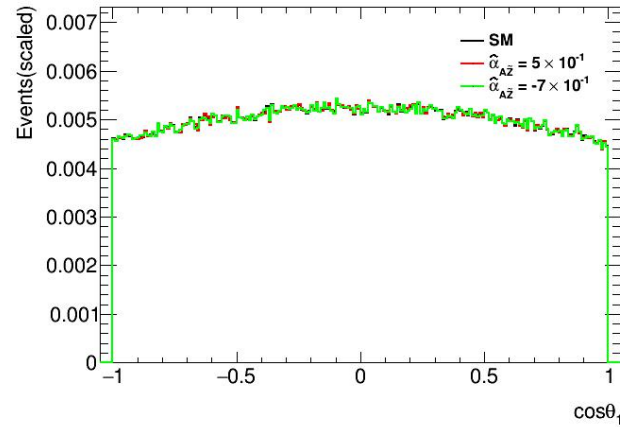


# Optimal variable approach

Differential cross section could be represent as:

$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = N \times \left( J_{\text{even}}(\theta_1, \theta_2, \phi) + \hat{\alpha}_{A\tilde{Z}} \times J_{\text{odd}_1}(\theta_1, \theta_2, \phi) + \hat{\alpha}_{Z\tilde{Z}} \times J_{\text{odd}_2}(\theta_1, \theta_2, \phi) \right)$$

where  $\hat{\alpha}_{A\tilde{Z}}$  and  $\hat{\alpha}_{Z\tilde{Z}}$  are CP-violating parameters.



$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = N \times \left( J_{\text{even}}(\theta_1, \theta_2, \phi) + \hat{\alpha}_{A\bar{Z}} \times J_{\text{odd}_1}(\theta_1, \theta_2, \phi) + \hat{\alpha}_{Z\bar{Z}} \times J_{\text{odd}_2}(\theta_1, \theta_2, \phi) \right)$$

In this formation, we could define **Optimal Variable  $\omega$**  which combines the information from  $\{\theta_1, \theta_2, \phi\}$ :

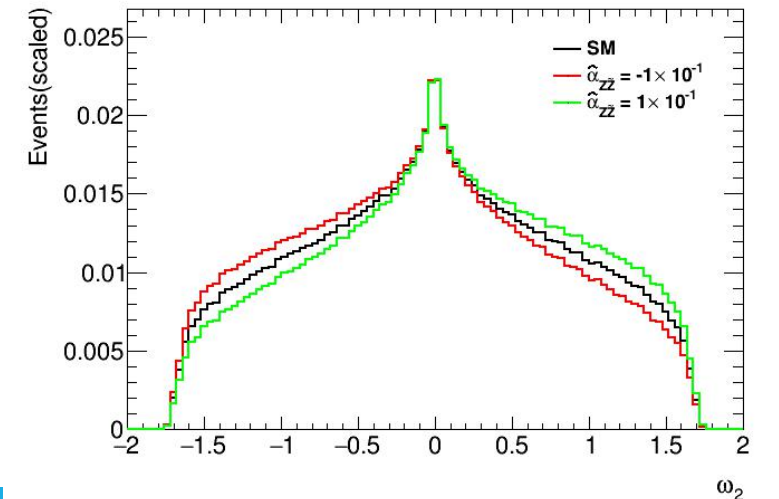
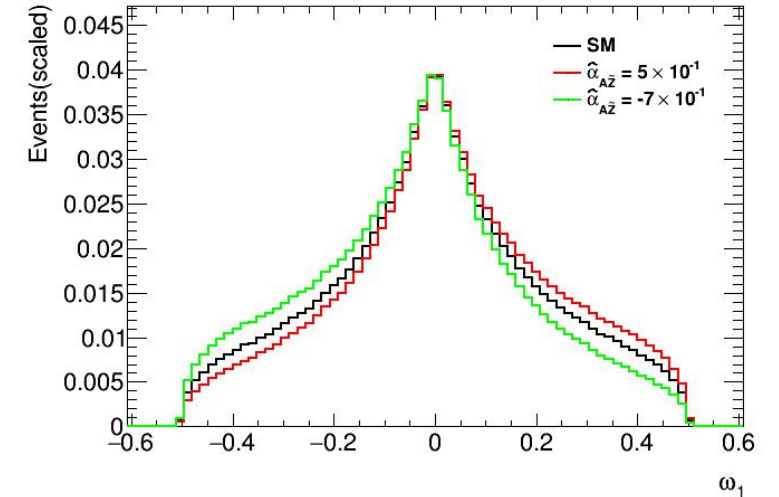
$$\omega_1 = 1000 \times \frac{J_{\text{odd}_1}(\theta_1, \theta_2, \phi)}{J_{\text{even}}(\theta_1, \theta_2, \phi)} \text{ to measure } \hat{\alpha}_{A\bar{Z}}$$

$$\omega_2 = 1000 \times \frac{J_{\text{odd}_2}(\theta_1, \theta_2, \phi)}{J_{\text{even}}(\theta_1, \theta_2, \phi)} \text{ to measure } \hat{\alpha}_{Z\bar{Z}}$$

(The factor of 1000 is included here only for numerical convenience)

Benefits:

- Combine the information from 3-dimension phase space
- Easier to study



# Monte Carlo samples

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## Samples:

- The SM Higgs and background samples: generate with Whizard 1.95 and fast simulated based on the CEPC baseline detector design.
- CP-mixing Higgs samples: generate according to differential cross section for  $e^+e^- \rightarrow ZH \rightarrow llH$ :

$$\frac{d\sigma}{d\cos\theta_1 d\cos\theta_2 d\phi} = \frac{\mathcal{N}_\sigma(q^2)}{m_H^2} \mathcal{J}(q^2, \theta_1, \theta_2, \phi),$$

- $\sqrt{s} = 240\text{GeV}$
- The mass of Higgs boson is set to be 125GeV and the couplings are set to the SM predictions.
- All the generations are normalized to the expected yields in data with an integrated luminosity of  $5.6\text{ab}^{-1}$ .

# Event selection

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## (using the SM Higgs and background samples)

- **Signal:**  $e^+e^- \rightarrow ZH \rightarrow \mu^+\mu^-H(\rightarrow b\bar{b}/c\bar{c}/gg)$  channel
- **Background:** Irreducible background which contains the same final states as that in signal.

Choose selections by the best significance:

- Muon pair selection:

$$|\cos\theta_{\mu^+\mu^-}| < 0.81; \quad \text{Mass}_{\mu\mu} \in (77.5\text{GeV}, 104.5\text{GeV}); \quad M_{recoil_{\mu\mu}} \in (124\text{GeV}, 140\text{GeV}).$$

$$\text{Where } M_{recoil_{\mu\mu}}^2 = (\sqrt{s} - E_{\mu\mu})^2 - p_{\mu\mu}^2 = s - 2E_{\mu\mu}\sqrt{s} + m_{\mu\mu}^2$$

- Jets pair selection:

$$|\cos\theta_{jet}| < 0.96; \quad \text{Mass}_{jj} \in (100\text{GeV}, 150\text{GeV}).$$

# Event selection

## Cut Flow:

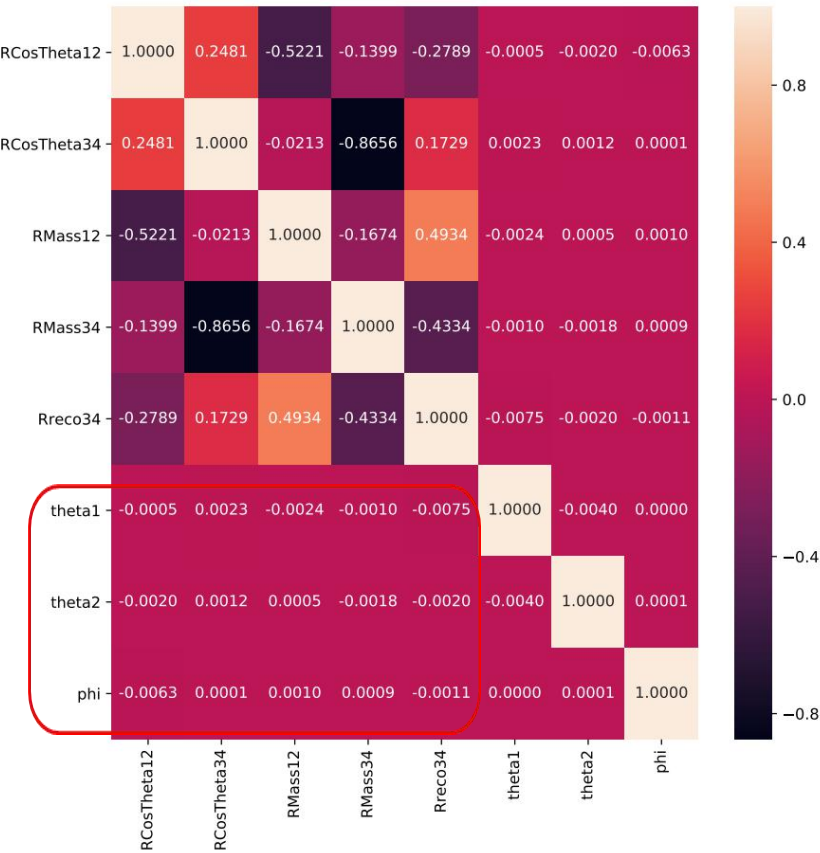
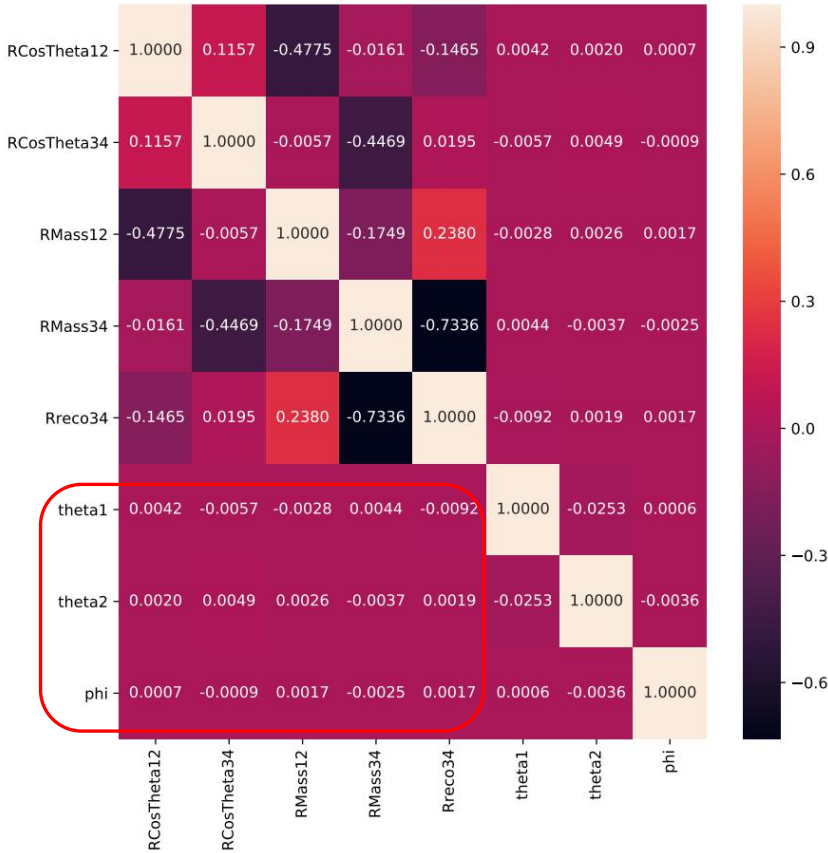
$ZH \rightarrow \mu^+ \mu^- + b\bar{b}/c\bar{c}/gg$  channel

|                     | Signal                                 | Irreducible Background                |
|---------------------|--|---------------------------------------|
| Original            | $2.86 \times 10^6$                     | $1.25 \times 10^6$                    |
| Muon pair selection | $1.84 \times 10^4$ (efficiency:64.33%) | $1.14 \times 10^4$ (efficiency:0.91%) |
| All selection       | $1.33 \times 10^4$ (efficiency:46.50%) | $3.61 \times 10^3$ (efficiency:0.29%) |

# Event selection

## Correlation:

- We can see that  $\theta_1, \theta_2, \phi$  have little correlation with  $\cos\theta_{\mu^+\mu^-}, \text{Mass}_{\mu\mu}, M_{recoil_{\mu\mu}}, \cos\theta_{jet}, \text{Mass}_{jj}$ .



- So we can ignore the impact of event selections to  $\theta_1, \theta_2,$  and  $\phi$ .

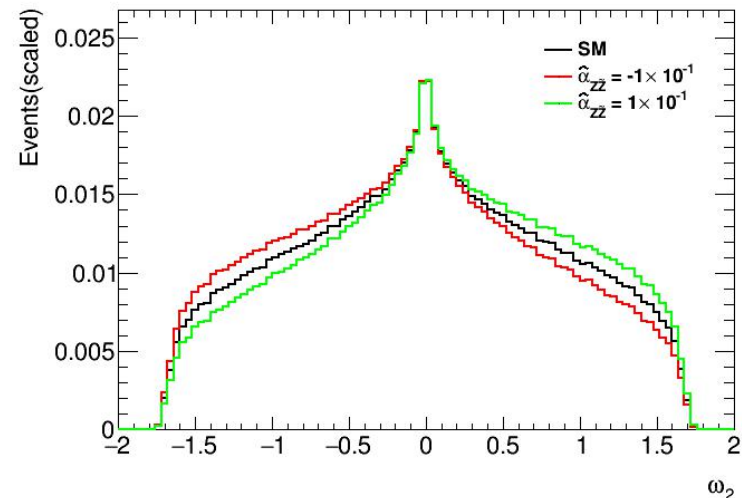
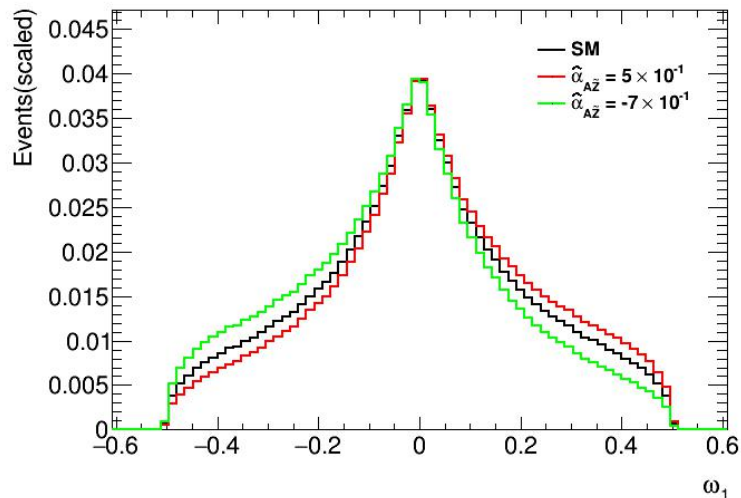
# Fitting strategy and result

Fit strategy: Maximum-likelihood fit

$$f^{\vec{\alpha}}(\omega) = N_{\text{sig}} * f_{\text{sig}}^{\vec{\alpha}}(\omega) + N_{\text{bkg}} * f_{\text{bkg}}^{\vec{\alpha}}(\omega)$$

where  $\vec{\alpha}$  means  $\hat{\alpha}_{A\bar{Z}}$  and  $\hat{\alpha}_{Z\bar{Z}}$ ,  $\omega$  represents  $\omega_1$  and  $\omega_2$ .

- Fit  $\omega$  to get  $f_{\text{sig}}^{\vec{\alpha}}(\omega)$  and  $f_{\text{bkg}}^{\vec{\alpha}}(\omega)$
- Fit  $M_{\text{recoil}_{\mu\mu}}$  to get  $N_{\text{sig}}$  and  $N_{\text{bkg}}$
- Evaluate likelihood function for each  $\vec{\alpha}$  value hypothesis, and construct a  $\Delta NLL$  as a function of  $\vec{\alpha}$ .





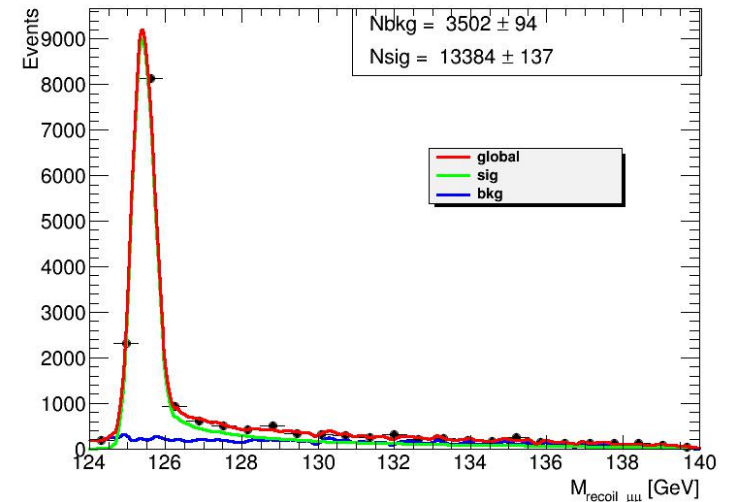
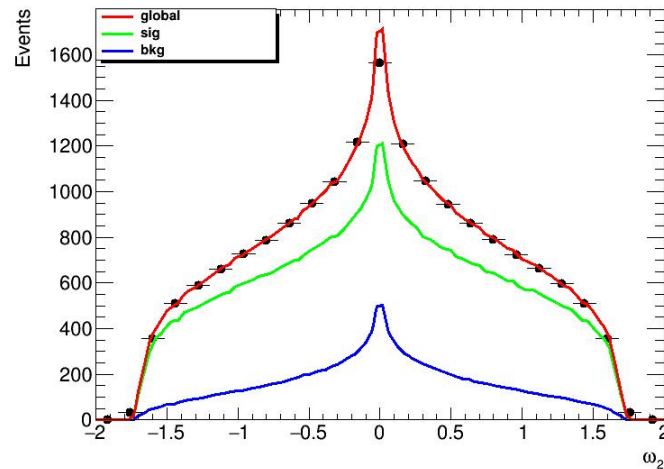
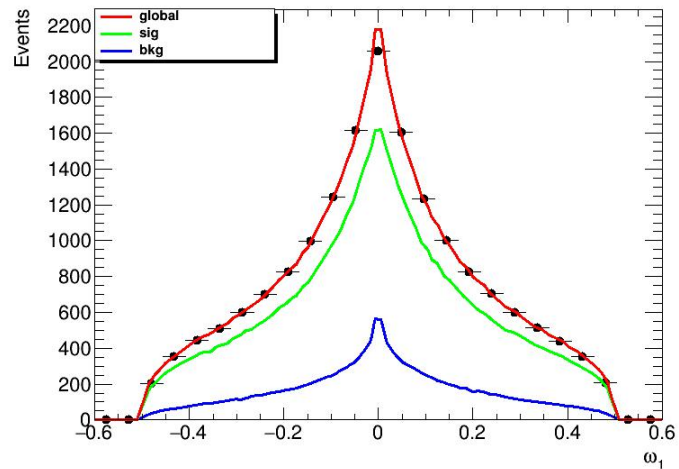
# Fitting strategy and result

## Fit $\omega$ :

- Use histogram pdf to fit **MC signal and background sample**.
- The red curve is global fit, the green curve is signal events, the blue curve is background events.

## Fit $M_{recoil_{\mu\mu}}$ :

- The signal modeled by the Crystal Ball function.
- The background modeled by a second-order polynomial.
- Using **ISR sample** can simulate the small exponential tail (which corresponding to the expected distribution.)



# Individual Fit

Extract maximum-likelihood fit p-value and interval

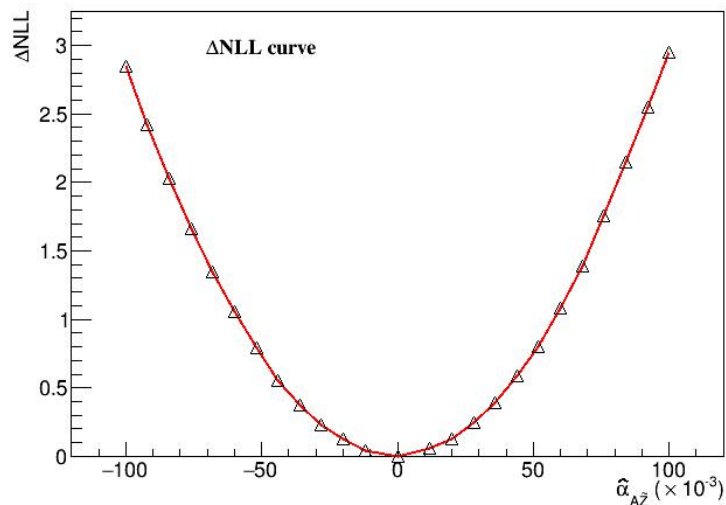
- Fit  $\Delta NLL$  curve with a quadratic function  $\Delta NLL(\vec{\alpha}) = a \cdot (\vec{\alpha} - \vec{\alpha}_0)^2$
- 68%(95%) CL interval corresponds to  $\Delta NLL=0.5(1.96)$ .
- *Set: fit to  $\hat{\alpha}_{A\tilde{Z}}, \hat{\alpha}_{Z\tilde{Z}} = 0$ .*

$$\Delta NLL(\hat{\alpha}_{A\tilde{Z}}|\omega_1) = 2.93 \times 10^{-4}(\hat{\alpha}_{A\tilde{Z}} + 8.68 \times 10^{-1})^2$$

For  $\hat{\alpha}_{A\tilde{Z}}$ :

68% CL:  $[-4.22 \times 10^{-2}, 4.04 \times 10^{-2}]$

95% CL:  $[-8.27 \times 10^{-2}, 8.09 \times 10^{-2}]$



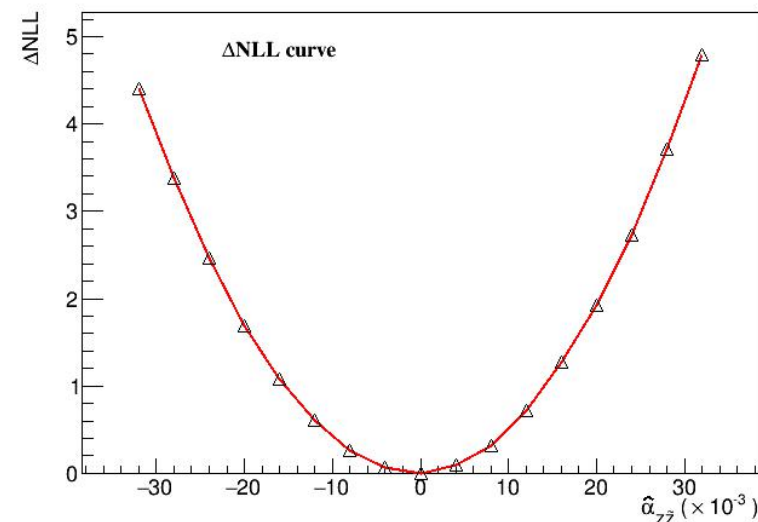
- *Set: fit to  $\hat{\alpha}_{Z\tilde{Z}}, \hat{\alpha}_{A\tilde{Z}} = 0$ .*

$$\Delta NLL(\hat{\alpha}_{Z\tilde{Z}}|\omega_2) = 4.51 \times 10^{-3}(\hat{\alpha}_{Z\tilde{Z}} + 6.36 \times 10^{-1})^2$$

For  $\hat{\alpha}_{Z\tilde{Z}}$ :

68% CL:  $[-1.12 \times 10^{-2}, 9.89 \times 10^{-3}]$

95% CL:  $[-2.15 \times 10^{-2}, 2.02 \times 10^{-2}]$



# Fit to phi

$\phi$  has the most information among the three kinematic variables ( $\theta_1, \theta_2, \phi$ )

straight-forward to fit  $\phi$ .

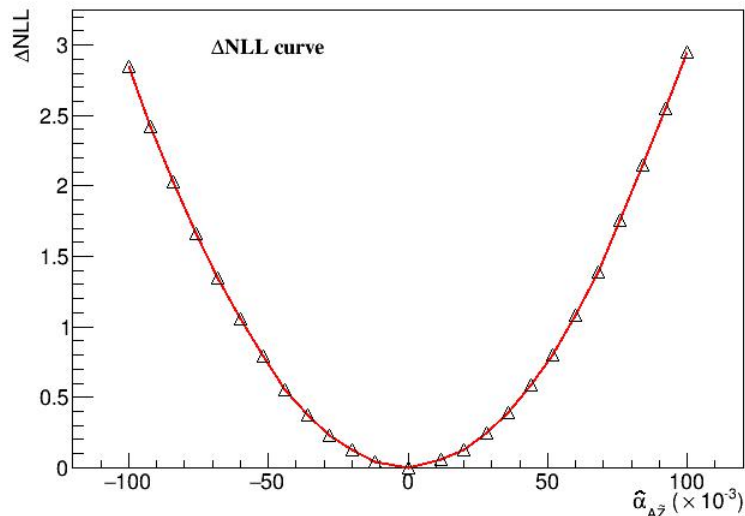
- Set: fit to  $\hat{\alpha}_{A\tilde{Z}}, \hat{\alpha}_{Z\tilde{Z}} = 0$ .

$$\Delta NLL(\hat{\alpha}_{A\tilde{Z}}|\phi) = 2.68 \times 10^{-4}(\hat{\alpha}_{A\tilde{Z}} + 1.05)^2$$

For  $\hat{\alpha}_{A\tilde{Z}}$ :

68% CL:  $[-4.42 \times 10^{-2}, 4.21 \times 10^{-2}]$

95% CL:  $[-8.66 \times 10^{-2}, 8.45 \times 10^{-2}]$



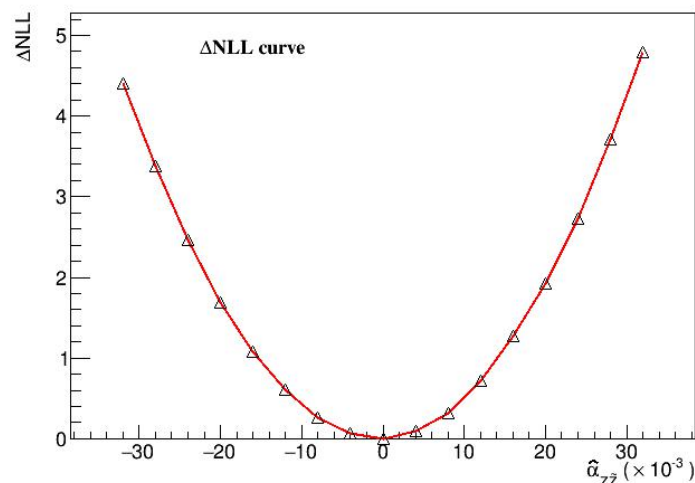
- Set: fit to  $\hat{\alpha}_{Z\tilde{Z}}, \hat{\alpha}_{A\tilde{Z}} = 0$ .

$$\Delta NLL(\hat{\alpha}_{Z\tilde{Z}}|\phi) = 2.98 \times 10^{-3}(\hat{\alpha}_{Z\tilde{Z}} + 5.53 \times 10^{-1})^2$$

For  $\hat{\alpha}_{Z\tilde{Z}}$ :

68% CL:  $[-1.35 \times 10^{-2}, 1.24 \times 10^{-2}]$

95% CL:  $[-2.62 \times 10^{-2}, 2.51 \times 10^{-2}]$



The results of  $\phi$ -fitting is slight worse than those of the  $\omega$ -fitting

- $\theta_1$  and  $\theta_2$  have less information.

# Result compare --> Compared with HL-LHC

In order to compare our study with HL-LHC, some conversion is necessary. (show in backup.)

In HL-LHC: (1sigma)

| Parameter                 | $\tilde{c}_{Z\gamma}$ | $\tilde{c}_{ZZ}$ | Case                |
|---------------------------|-----------------------|------------------|---------------------|
| HL-LHC ( $4\ell$ , incl.) | [-0.22,0.22]          | [-0.33,0.33]     | 1P                  |
|                           | [-0.25,0.25]          | [-0.27,0.27]     | 1P <sub>marg.</sub> |
| HL-LHC ( $4\ell$ , diff.) | [-0.10,0.10]          | [-0.31,0.31]     | 1P                  |
|                           | [-0.13,0.13]          | [-0.22,0.22]     | 1P <sub>marg.</sub> |
| HE-LHC ( $4\ell$ , incl.) | [-0.18,0.18]          | [-0.17,0.17]     | 1P                  |
|                           | [-0.23,0.23]          | [-0.20,0.20]     | 1P <sub>marg.</sub> |
| HE-LHC ( $4\ell$ , diff.) | [-0.05,0.05]          | [-0.13,0.13]     | 1P                  |
|                           | [-0.06,0.06]          | [-0.10,0.10]     | 1P <sub>marg.</sub> |

[arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

In CEPC (fit to  $\omega$ ):

|                     | $\tilde{c}_{Z\gamma}$ | $\tilde{c}_{ZZ}$ |
|---------------------|-----------------------|------------------|
| 68% CL( $1\sigma$ ) | [-0.36, 0.35]         | [-0.08, 0.07]    |
| 95% CL( $2\sigma$ ) | [-0.71, 0.70]         | [-0.16, 0.15]    |

# Summary

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An EFT based Higgs CP-mixing test is performed.

- Set up some basic assumptions to have a simplest CP-mixing model.
- Introduced optimal variable with better performance.
- Used ML-fit in  $\omega$  and  $\phi$  distribution to extract  $\hat{\alpha}_{A\tilde{Z}}$  and  $\hat{\alpha}_{Z\tilde{Z}}$ .
- Result: 95% CL  $\hat{\alpha}_{A\tilde{Z}} \in [ - 8.27 \times 10^{-2}, 8.09 \times 10^{-2} ]$  and  $\hat{\alpha}_{Z\tilde{Z}} \in [ - 2.15 \times 10^{-2}, 2.02 \times 10^{-2} ]$

For future

- Increasing luminosity like  $20ab^{-1}$ .
- More processes such as  $ZH \rightarrow e^+e^-H$ .
- The sensitivities to new physics could be improved by **a factor of around 4**.

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Thank you!

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# Backup



# Result compare --> Compared with HL-LHC

In HL-LHC: [arXiv:1902.00134](https://arxiv.org/abs/1902.00134)

$$\mathcal{L}_{\text{CPV}} = \frac{H}{v} \left[ \tilde{c}_{\gamma\gamma} \frac{e^2}{4} A_{\mu\nu} \tilde{A}^{\mu\nu} + \tilde{c}_{Z\gamma} \frac{e\sqrt{g_1^2 + g_2^2}}{2} Z_{\mu\nu} \tilde{A}^{\mu\nu} + \tilde{c}_{ZZ} \frac{g_1^2 + g_2^2}{4} Z_{\mu\nu} \tilde{Z}^{\mu\nu} + \tilde{c}_{WW} \frac{g_2^2}{2} W_{\mu\nu}^+ \tilde{W}^{\mu\nu} \right]$$

Compare theory model in [P5](#), we can get that the value in red frame are same:

$$(g_1=0.358, g_2=0.648, e=0.313, v = 1/\sqrt{\sqrt{2}G_F^0} = 2M_W/g \approx 246.22\text{GeV})$$

$$(\sqrt{2}G_F)^{1/2} \hat{\alpha}_{ZZ} H Z_{\mu\nu} \tilde{Z}^{\mu\nu} = \frac{H}{v} \tilde{c}_{ZZ} \frac{g_1^2 + g_2^2}{4} Z_{\mu\nu} \tilde{Z}^{\mu\nu} \quad \frac{g_1^2 + g_2^2}{4} = 0.137$$

$$(\sqrt{2}G_F)^{1/2} \hat{\alpha}_{AZ} H Z_{\mu\nu} \tilde{A}^{\mu\nu} = \frac{H}{v} \tilde{c}_{Z\gamma} \frac{e\sqrt{g_1^2 + g_2^2}}{2} Z_{\mu\nu} \tilde{A}^{\mu\nu} \quad \frac{e\sqrt{g_1^2 + g_2^2}}{2} = 0.116$$