



# Probing EWSB in the early Universe with GWs and colliders

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Joint Workshop of the CEPC Physics, Software and New Detector Concept in 2022

**2022/05/25**

# Contents

- **Motivation**

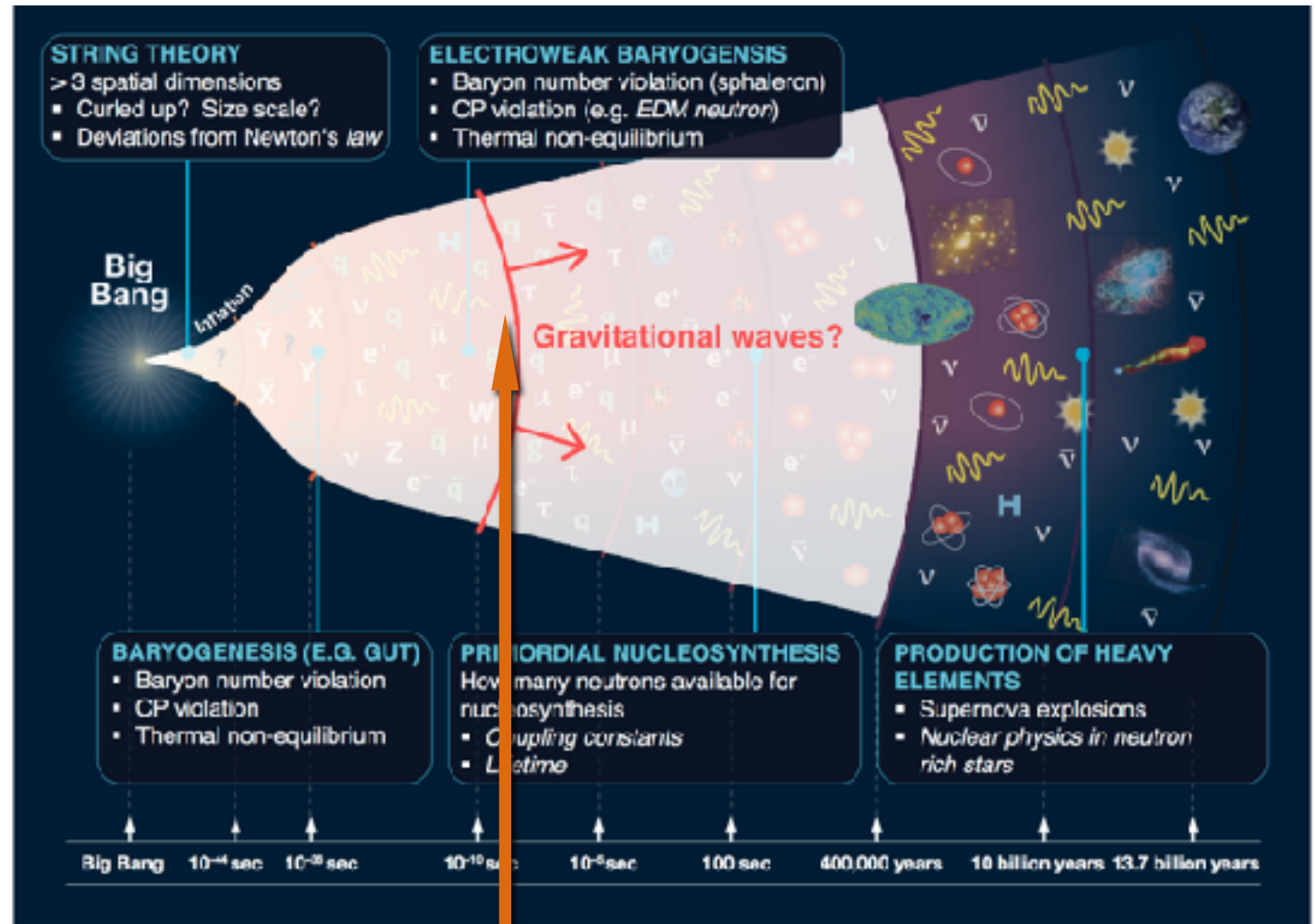
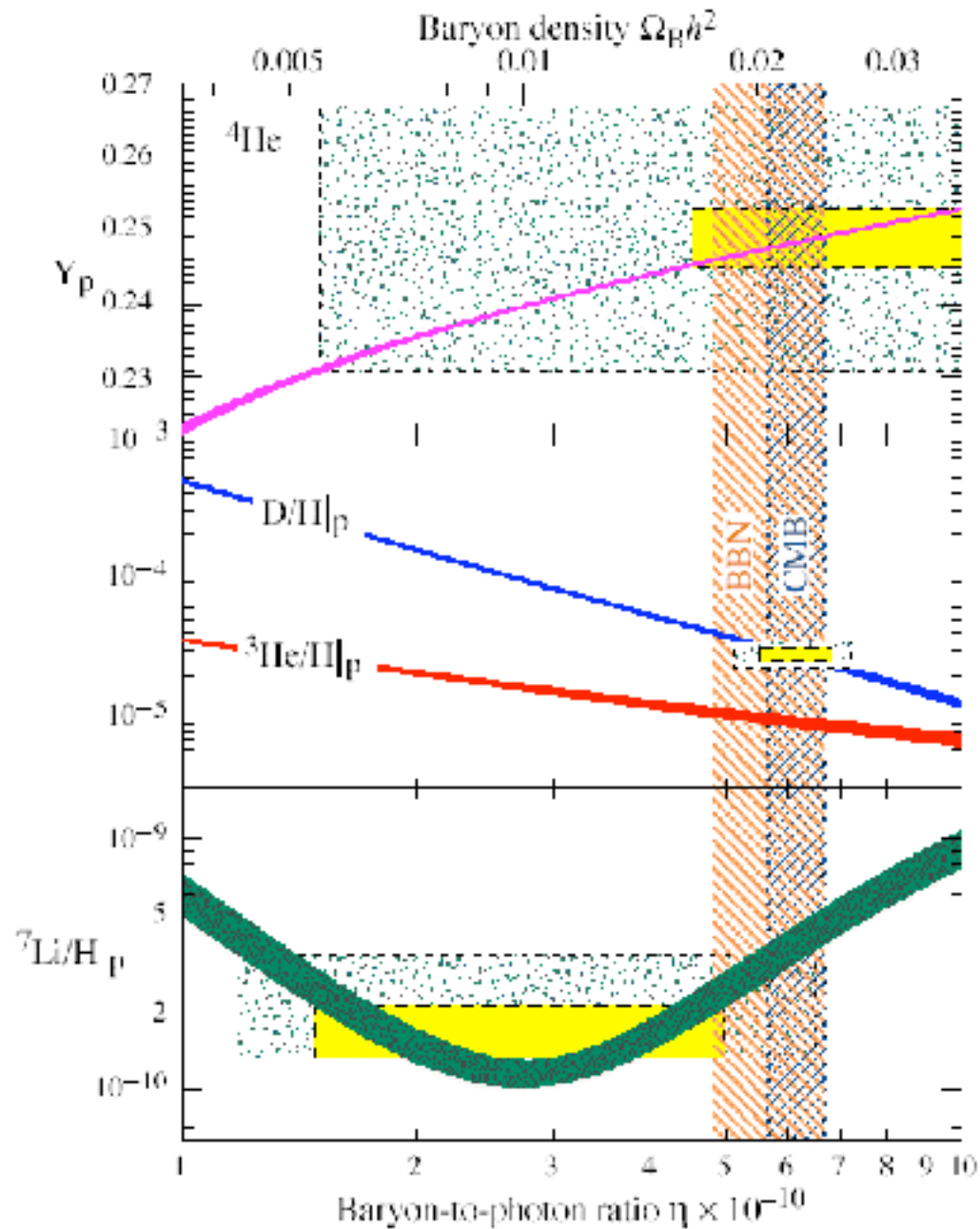
- **One-step FOPT**

- **Two-step FOPT**

- **Summary**

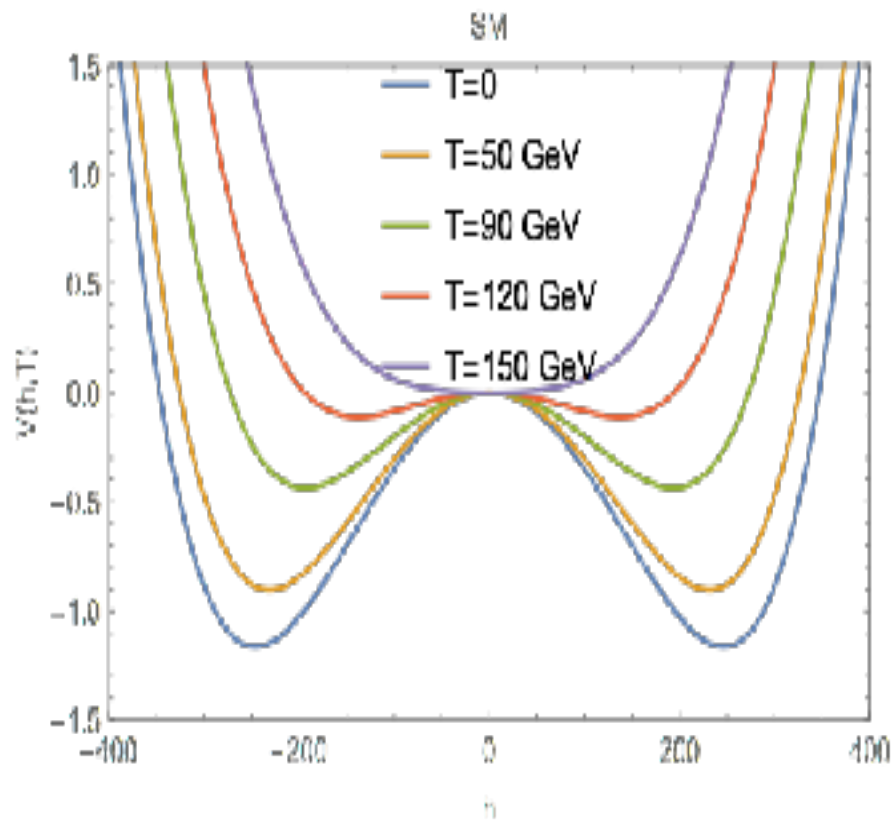


# ► SFOEWPT&BAU&GW

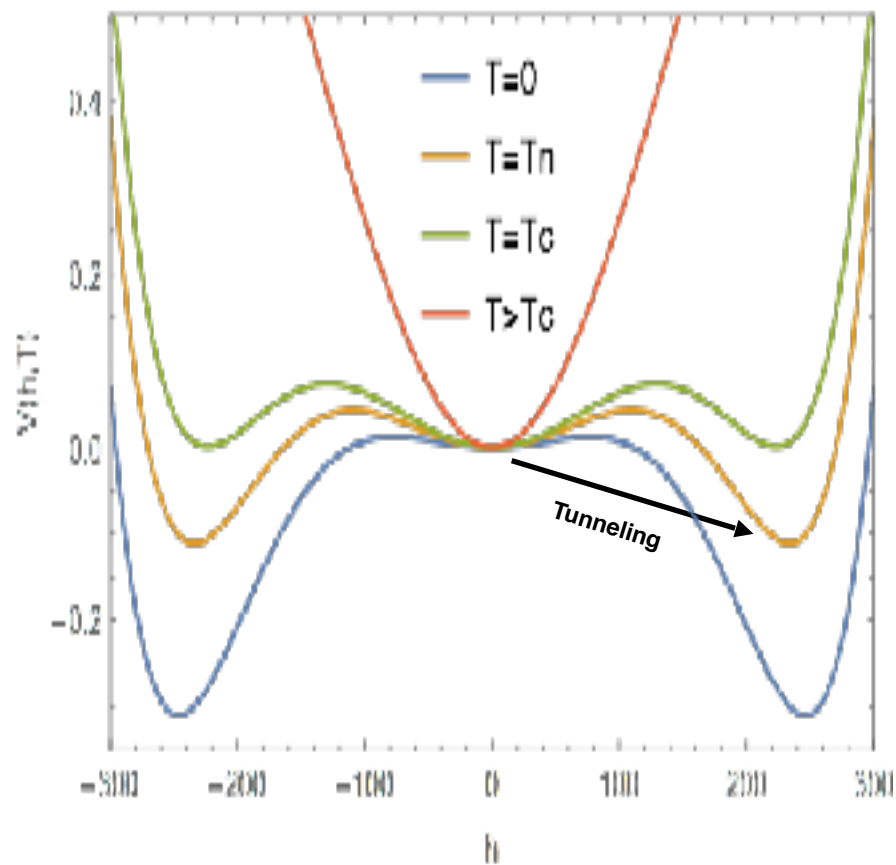
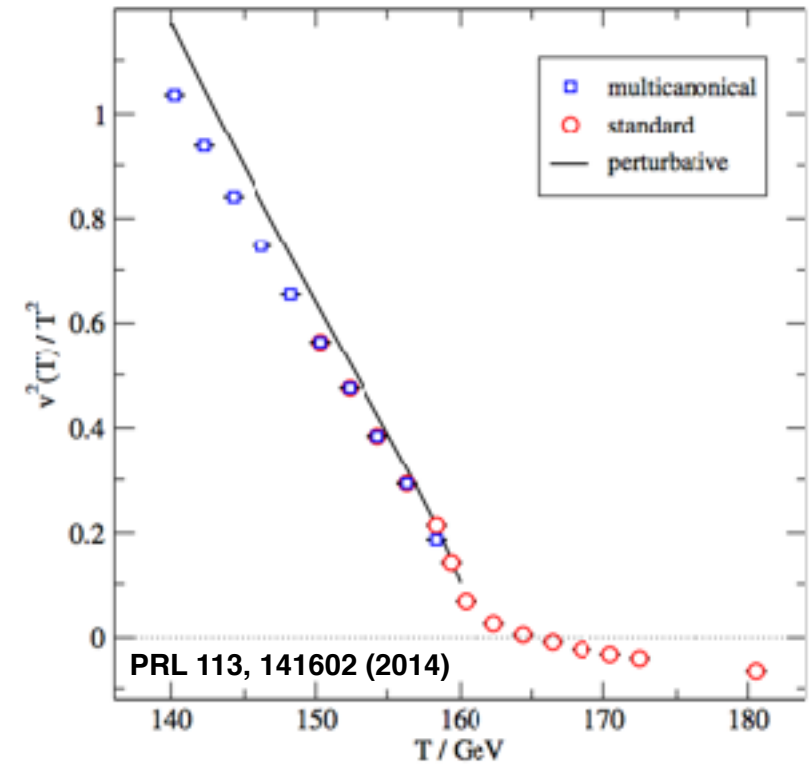


**EWBG + SGWB**

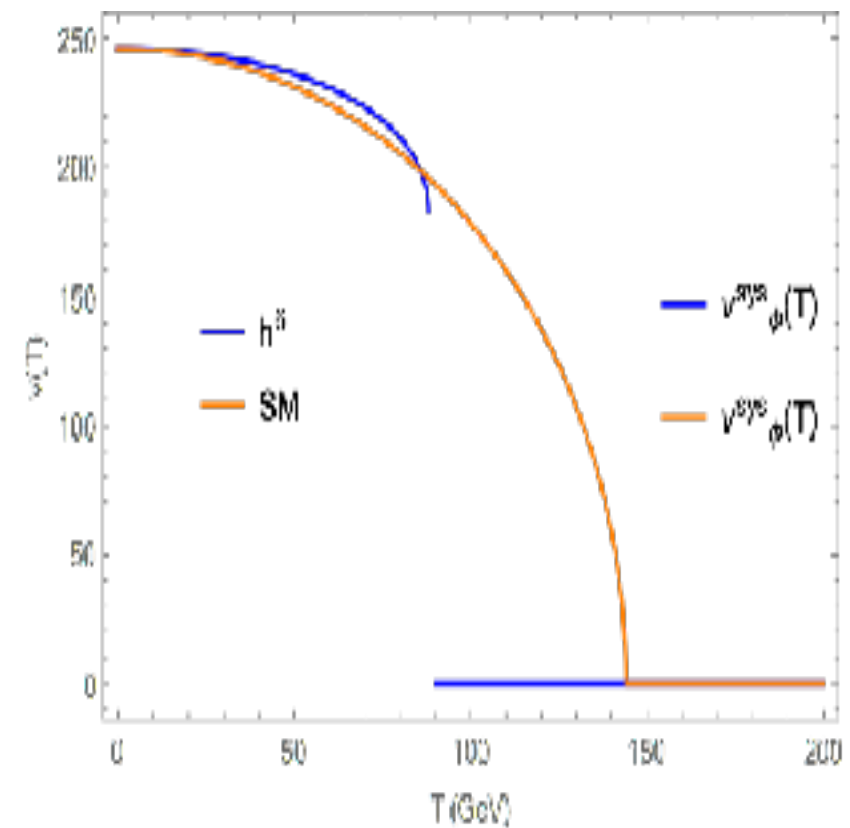
# FOEWPT & Higgs physics



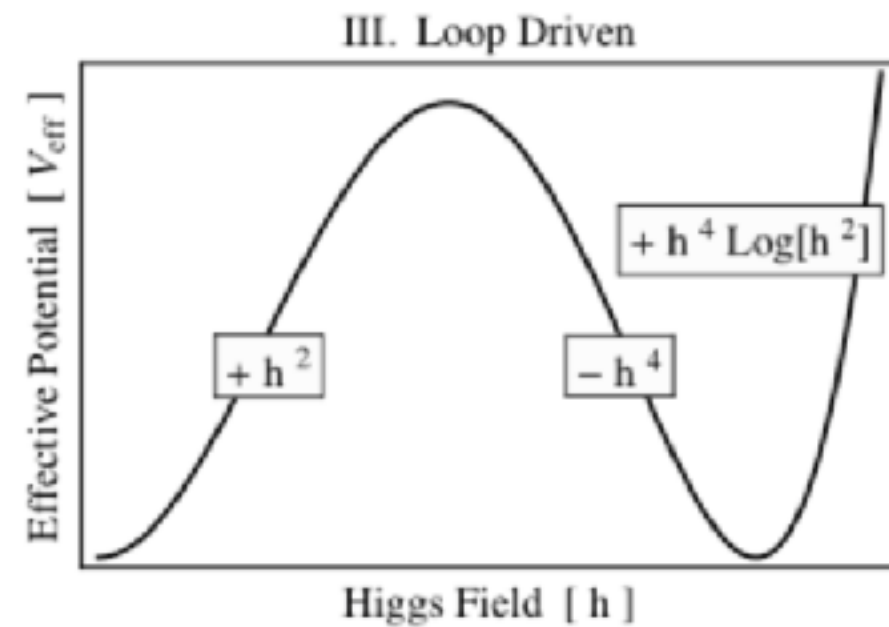
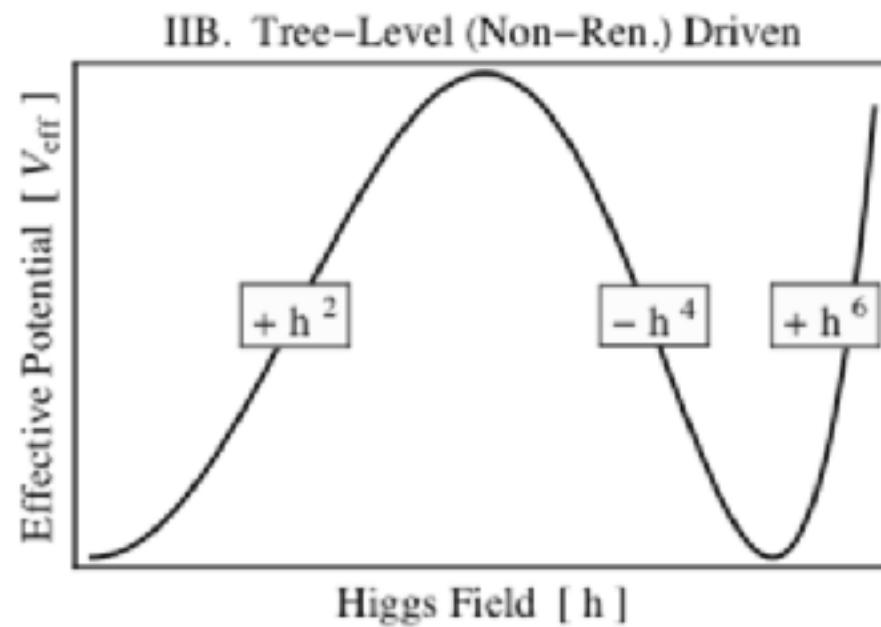
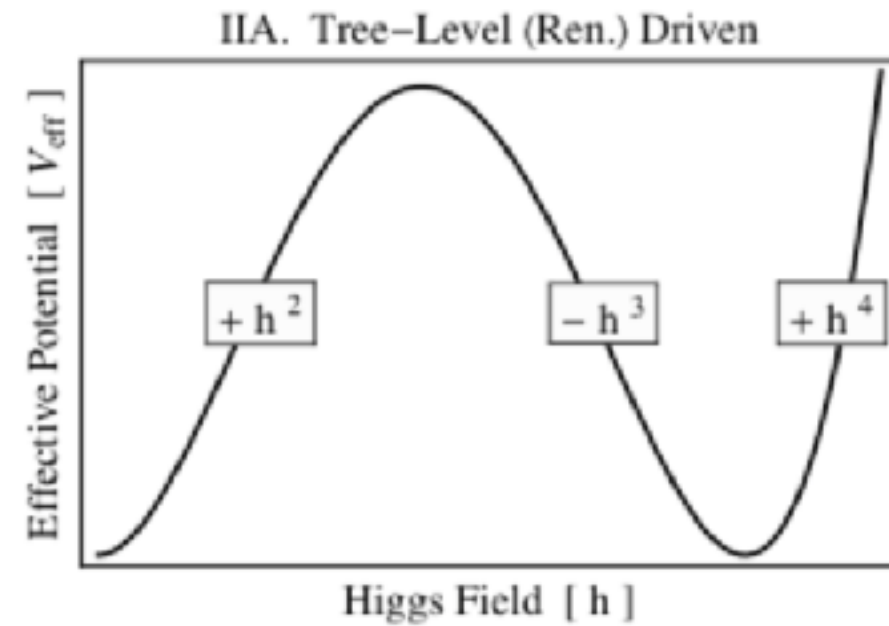
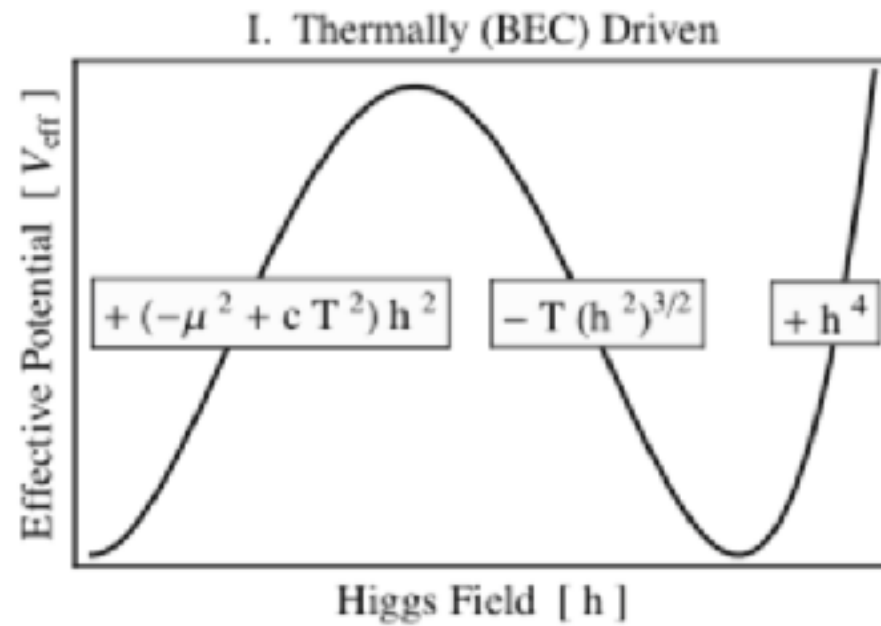
Higgs announcement seminar on 4 July 2012



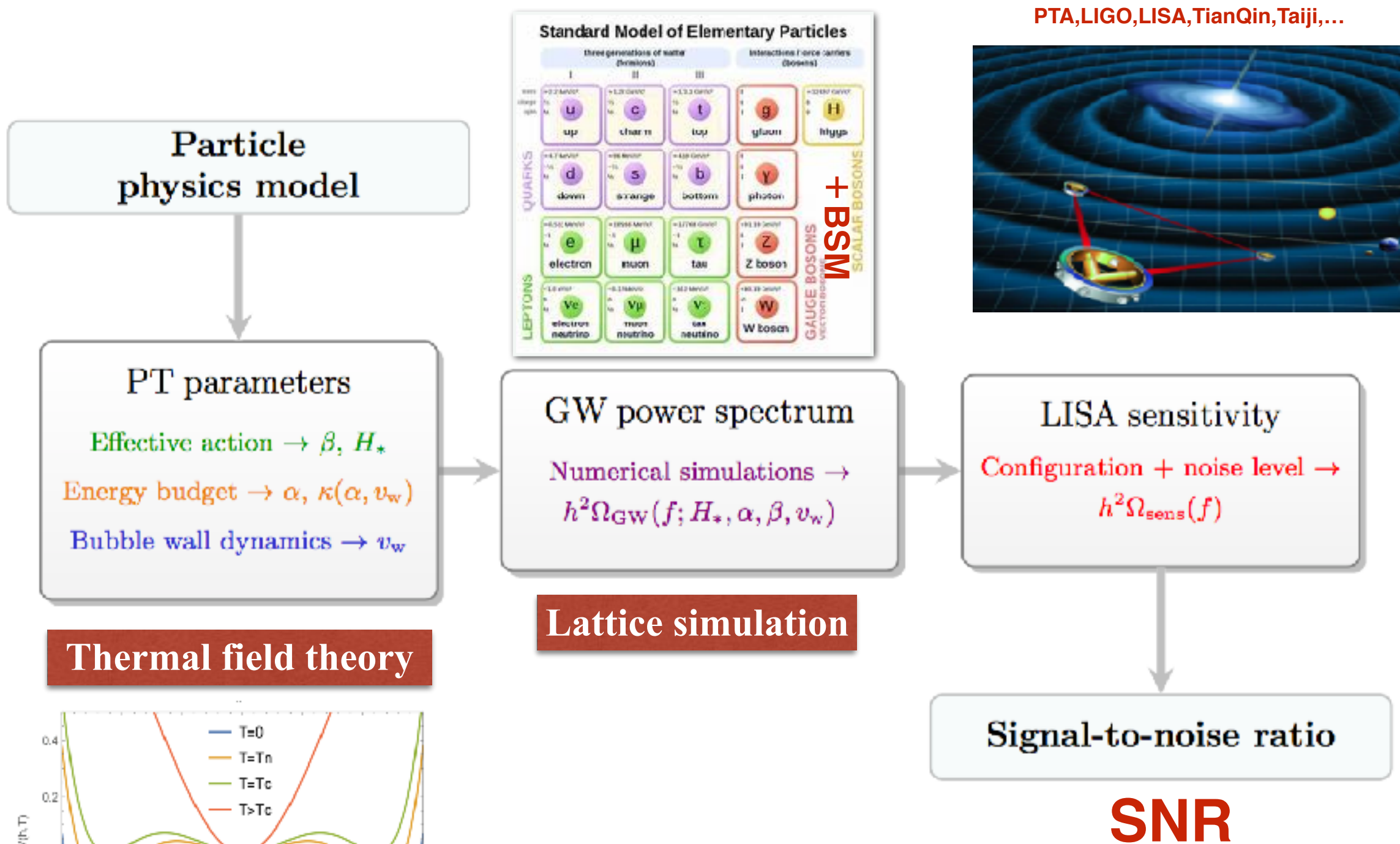
Grojean, Servant, Wells  
05, Huang, Jokelar, Li,  
Wagner 15, Cao,  
Huang, Xie, & Zhang  
17, Zhou, Bian, Guo 19



# Model classes for one-step FOPT



Chung, Long, Wang, Phys.Rev.D 87 (2013) 2, 023509





# ► One-step FOPT

PHYSICAL REVIEW LETTERS 126, 251102 (2021)

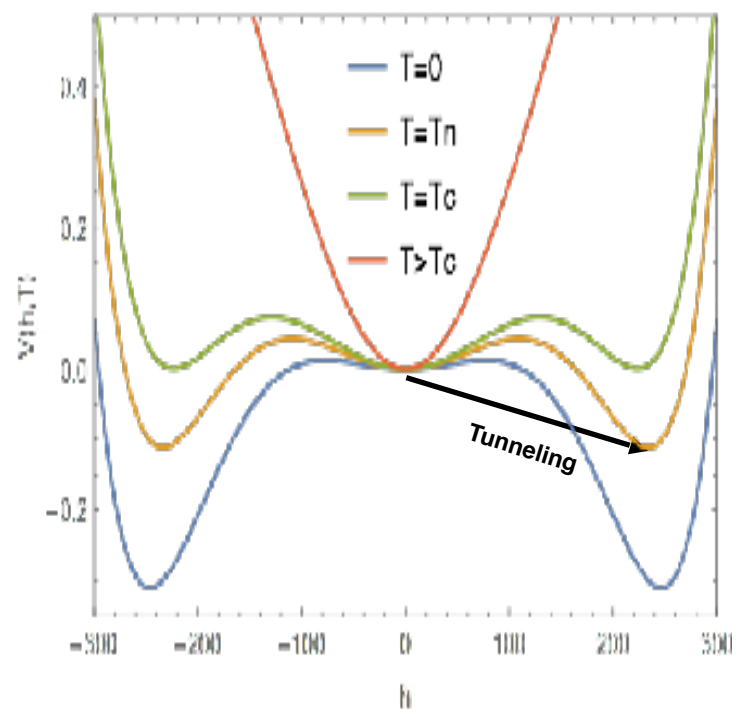
## Magnetic Field and Gravitational Waves from the First-Order Phase Transition

Yuefeng Di, Jialong Wang, Ruiyu Zhou, and Ligong Bian<sup>✉</sup>  
*Department of Physics, Chongqing University, Chongqing 401331, China*

Rong-Gen Cai<sup>†</sup>  
*CAS Key Laboratory of Theoretical Physics, Institute of Theoretical Physics, Chinese Academy of Sciences,  
P.O. Box 2735, Beijing 100190, China,  
School of Physical Sciences, University of Chinese Academy of Sciences, No. 19A Yuquan Road, Beijing 100049, China,  
and School of Fundamental Physics and Mathematical Sciences, Hangzhou Institute for Advanced Study,  
University of Chinese Academy of Sciences, Hangzhou 310024, China*

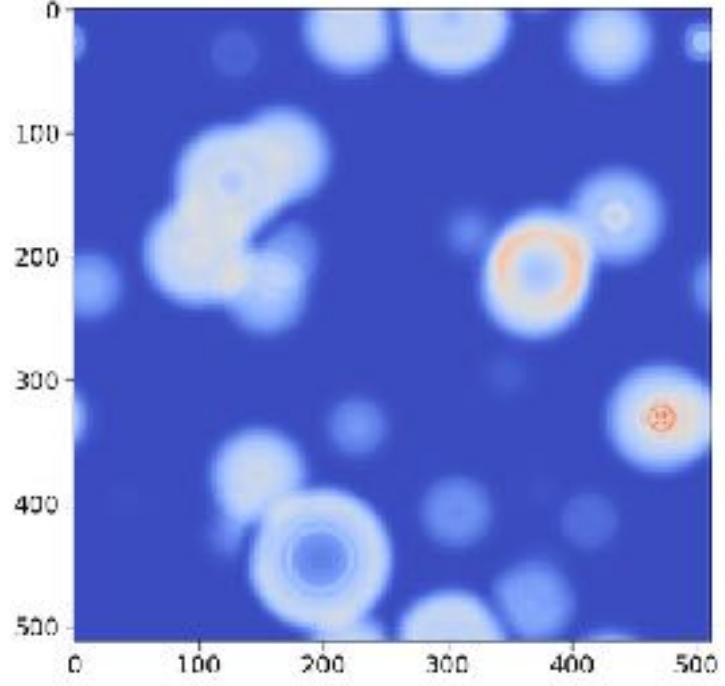
Jing Liu<sup>‡</sup>  
*School of Fundamental Physics and Mathematical Sciences, Hangzhou Institute for Advanced Study,  
University of Chinese Academy of Sciences, Hangzhou 310024, China  
and School of Physical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China*

### Finite-T Veff

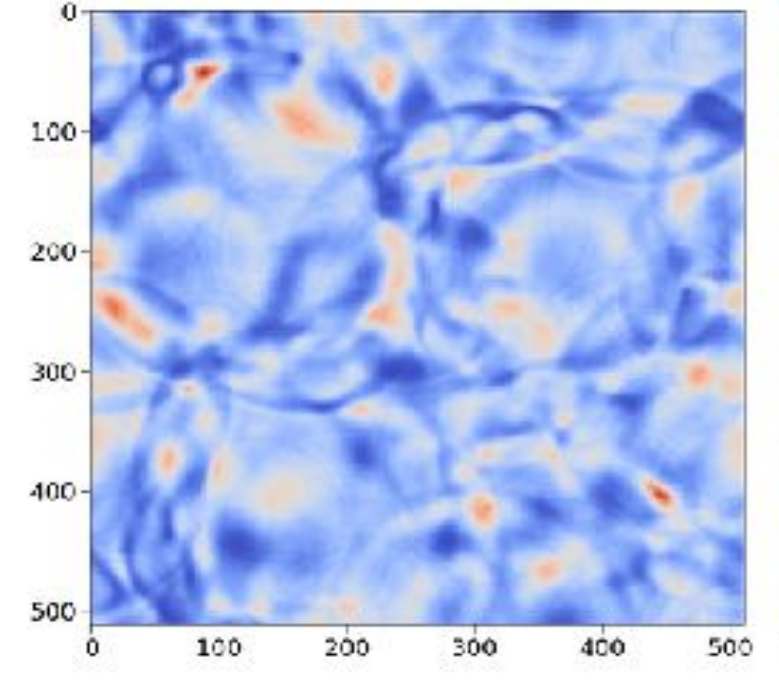


Finite-T calculation

### Nucleation



### Expansion&Percolation



Lattice Simulation

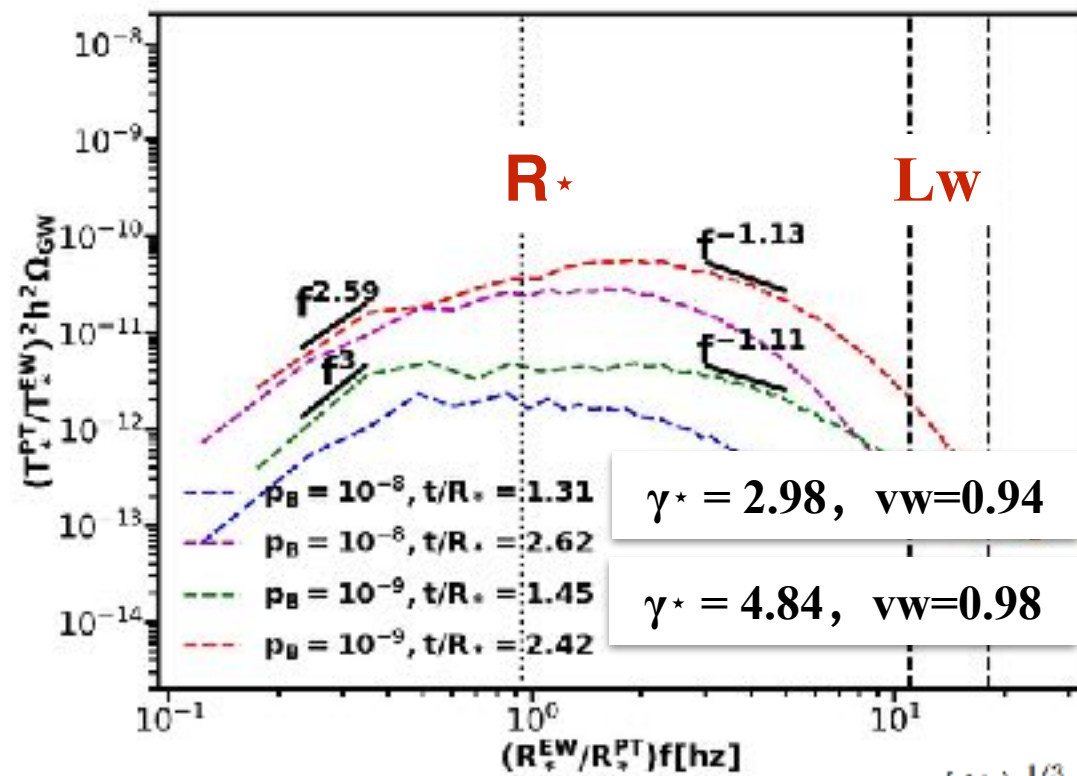
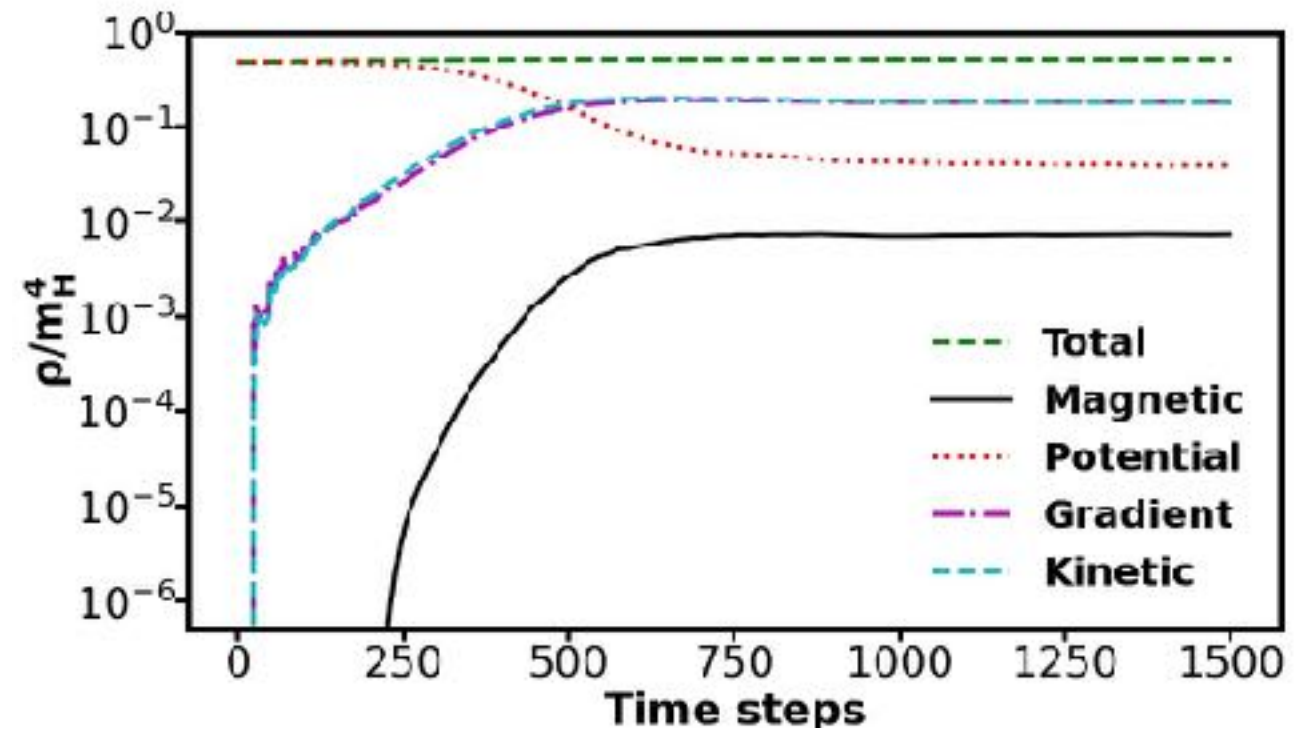
# GW from Bubble collisions

$$\ddot{h}_{ij} - \nabla^2 h_{ij} = 16\pi G T_{ij}^{TT}$$

$$T_{\mu\nu} = \partial_\mu \Phi^\dagger \partial_\nu \Phi - g_{\mu\nu} \frac{1}{2} \text{Re}[(\partial_i \Phi^\dagger \partial^i \Phi)^2]$$

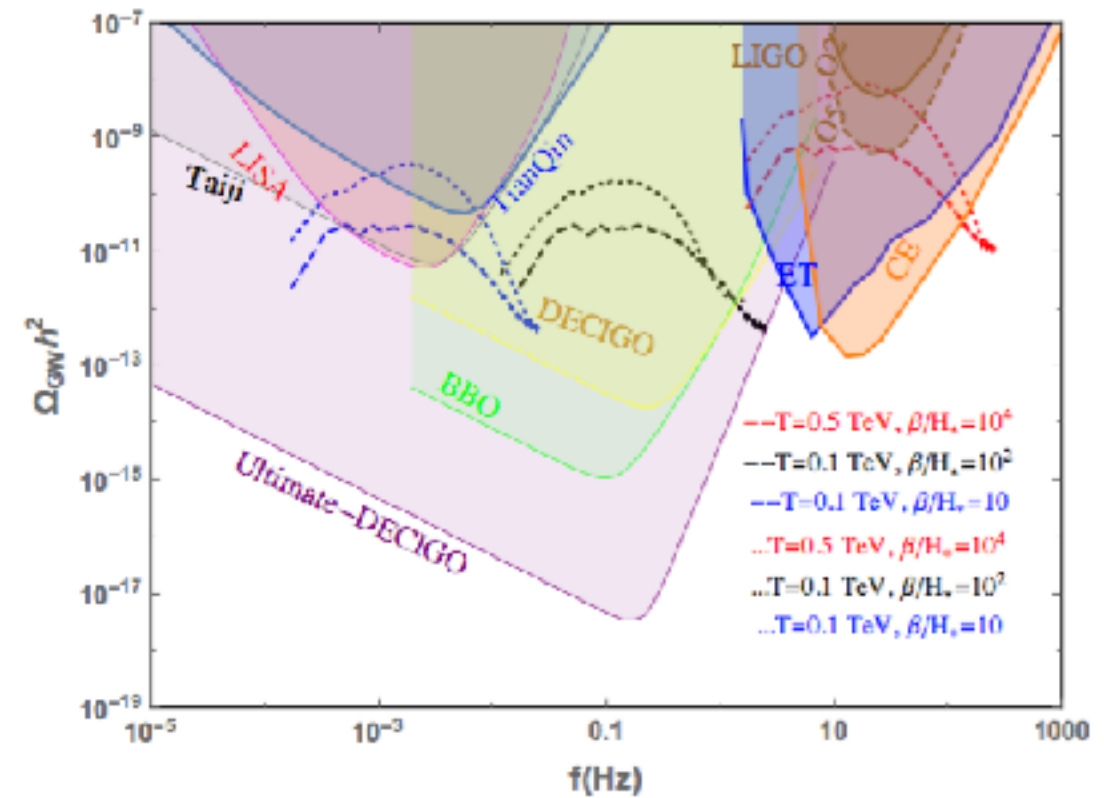
$$\langle \dot{h}_{ij}^{TT}(\mathbf{k}, t) \dot{h}_{ij}^{TT}(\mathbf{k}', t) \rangle = P_h(\mathbf{k}, t) (2\pi)^3 \delta(\mathbf{k} + \mathbf{k}')$$

$$\frac{d\Omega_{\text{gw}}}{d\ln(k)} = \frac{1}{32\pi G \rho_c} \frac{k^3}{2\pi^2} P_h(\mathbf{k}, t)$$



$$\gamma^* = R_* / (2Rc)$$

$$R_* = \left( \frac{\nu}{N_b} \right)^{1/3}$$



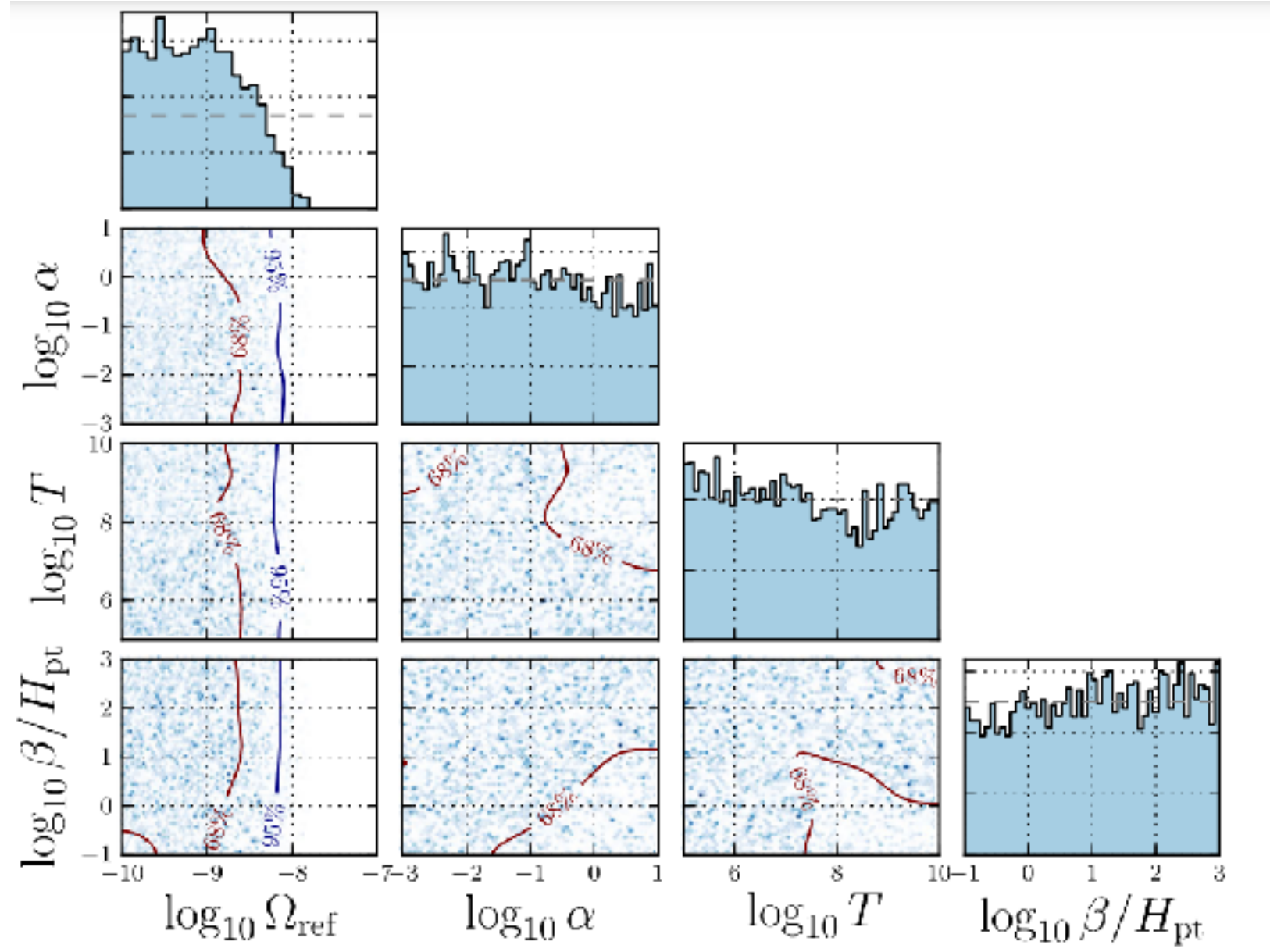


# ► LIGO-Virgo search for FOPT

## High-scale PT

Romero, Martinovic, Callister, Guo, et al., Phys.Rev.Lett. 126 (2021) 15, 151301

LIGO-Virgo O3



# ▶ PPTA search for FOPT

- PPTA DR2 dataset constrain low-scale phase transition, dark sector and QCD scale FOPT

PHYSICAL REVIEW LETTERS **127**, 251303 (2021)

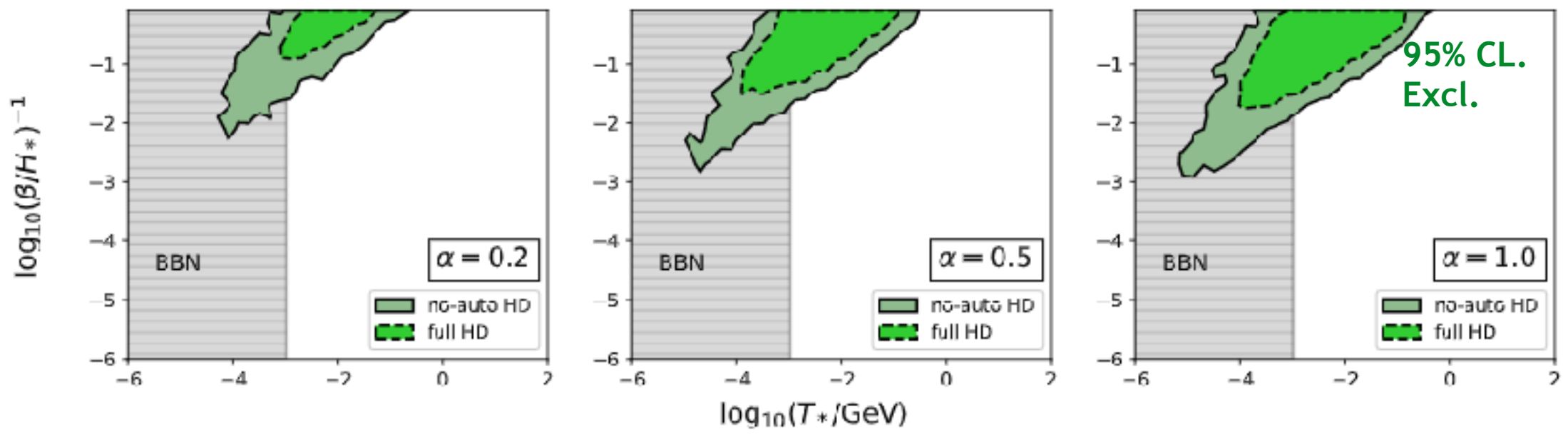
Editors' Suggestion    Featured In Physics

## Constraining Cosmological Phase Transitions with the Parkes Pulsar Timing Array

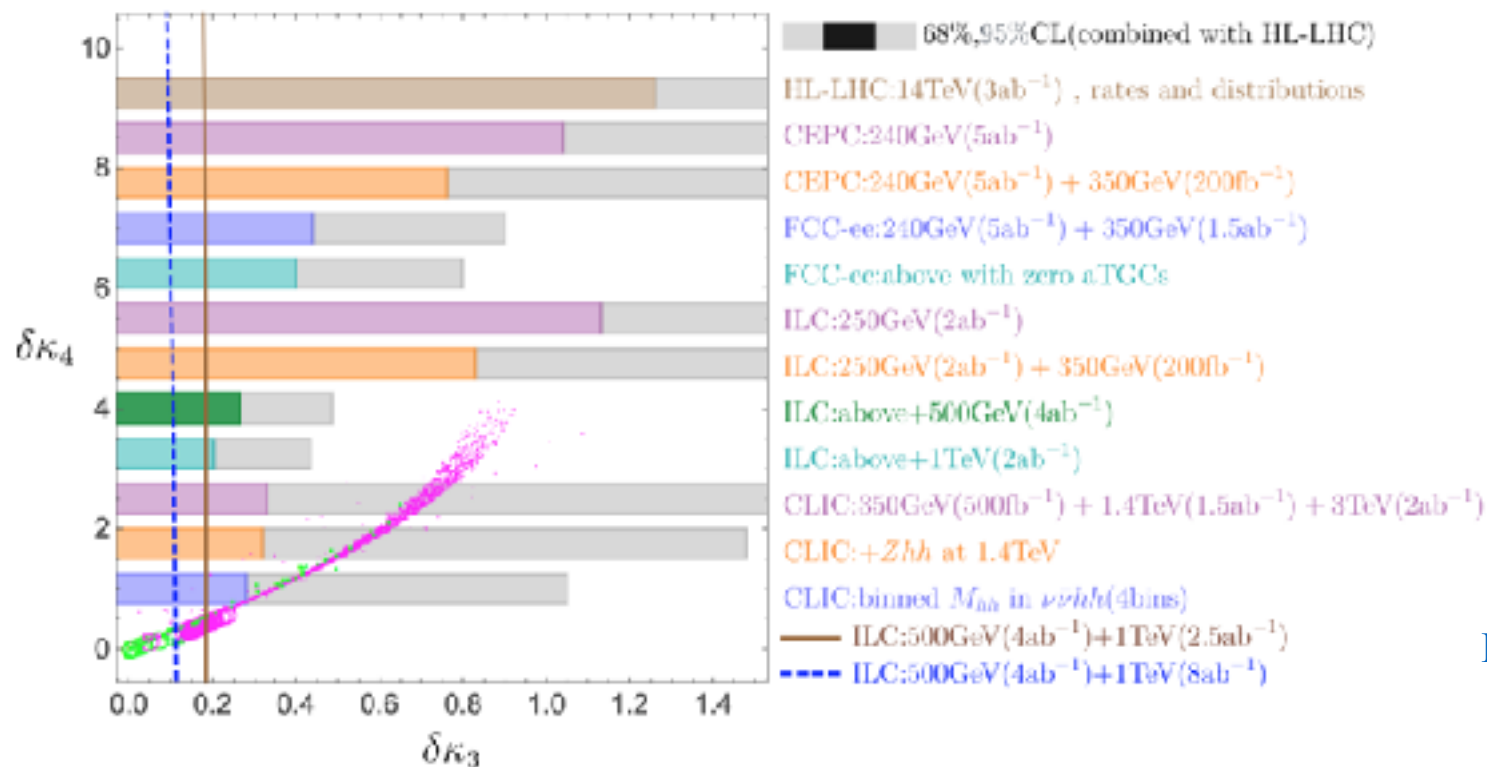
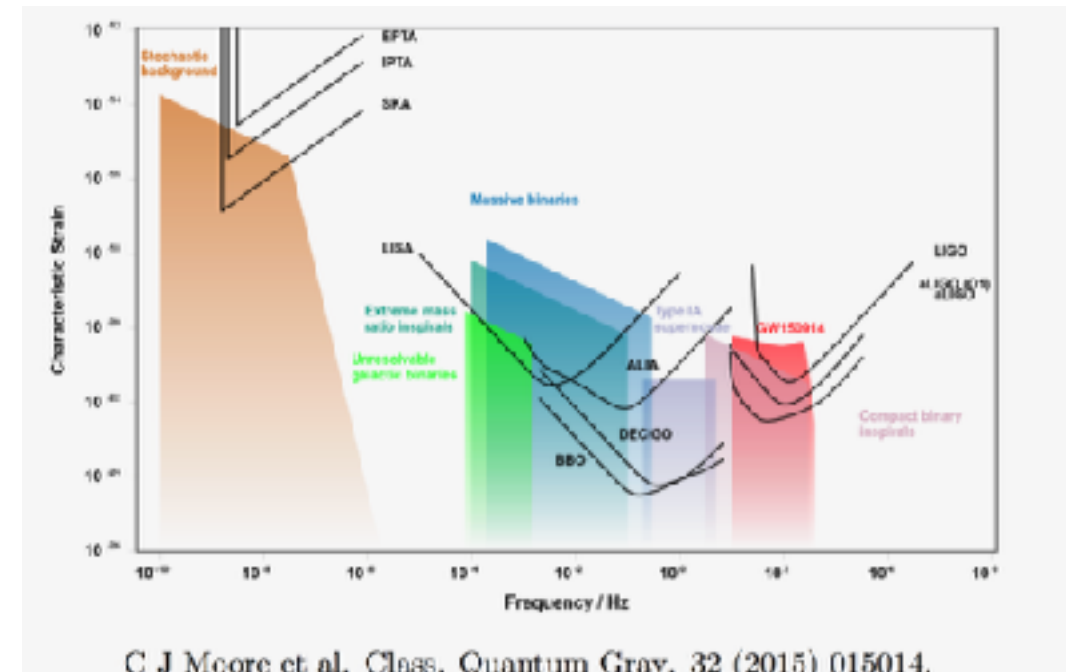
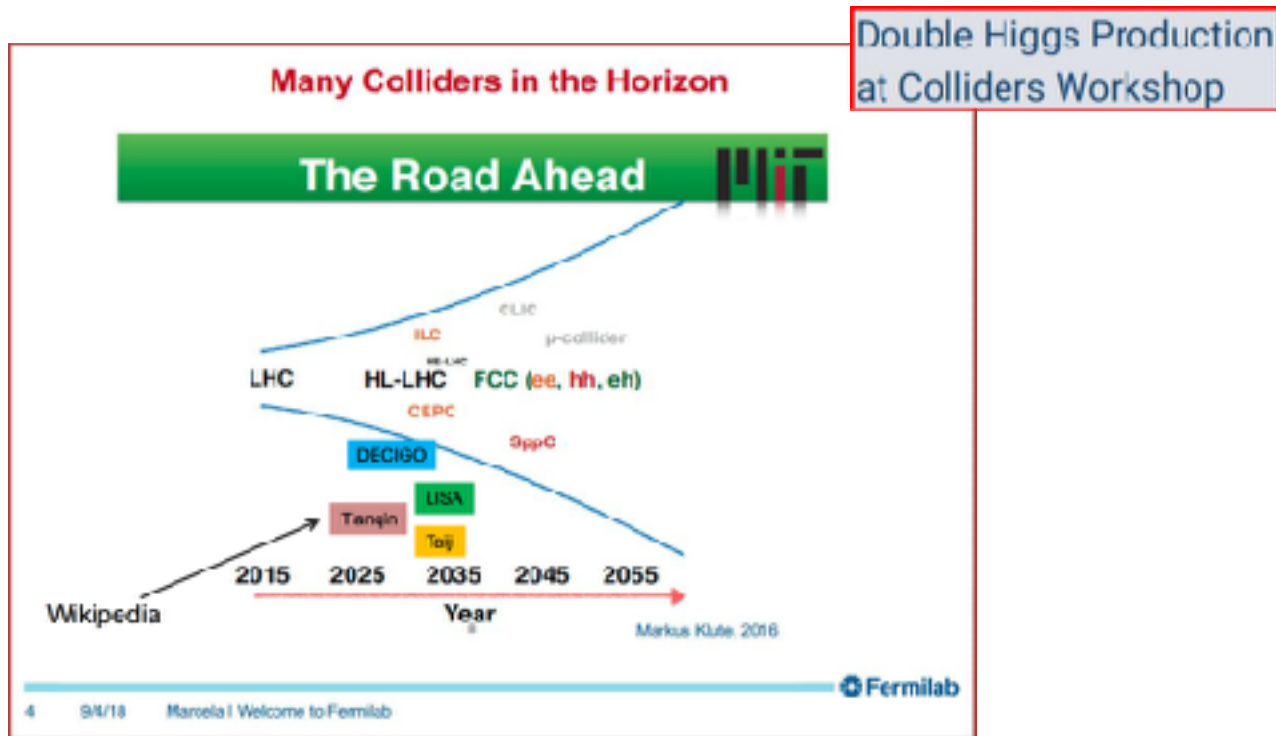
Xiao Xue<sup>1,2,3</sup>, Ligong Bian<sup>4,5,8</sup>, Jing Shu<sup>1,2,6,7,8,†</sup>, Qiang Yuan<sup>9,10,7,‡</sup>, Xingjiang Zhu<sup>11,12,13,§</sup>, N. D. Ramesh Bhat<sup>14</sup>,  
 Shi Dai<sup>15</sup>, Yi Feng<sup>16</sup>, Boris Goncharov<sup>11,12</sup>, George Hobbs<sup>17</sup>, Eric Howard<sup>17,18</sup>, Richard N. Manchester<sup>17</sup>,  
 Christopher J. Russell<sup>19</sup>, Daniel J. Reardon<sup>12,20</sup>, Ryan M. Shannon<sup>12,20</sup>, Renée Spiewak<sup>21,20</sup>,  
 Nithyanandan Thyagarajan<sup>22</sup> and Jingbo Wang<sup>23</sup>

TABLE I: Description of hypotheses tested in this work and the Bayes factors between them.

Hypothesis	Pulsar noise	Common red process	HD process FOPT spectrum	Bayes Factors	Parameter Estimation (median and 1- $\sigma$ interval)	
					$T_*/\text{MeV}, \alpha \times 10^3, \beta/H_*$	$A_{\text{comred}}, \gamma_{\text{comred}}$
H0:Pulsar Noise	yes	no	no			
H1:Common Red	yes	yes	no	$10^{3.5}$ (against H0)		$-14.45^{+0.62}_{-0.64}, 3.31^{+1.36}_{-1.53}$
H2:FOPT	yes	no	yes (full HD)	$10^{1.8}$ (against H0)	$7.4^{+11.9}_{-4.7}, 271^{+165}_{-92}, 9.9^{+11.4}_{-5.4}$	
H3:FOPT1	yes	yes	yes (full HD)	1.04 (against H1)	$9.6^{+232.2}_{-9.2}, 3.8^{+27.5}_{-3.4}, 854^{+9622}_{-782}$	$-14.51^{+0.64}_{-0.68}, 3.36^{+1.39}_{-1.54}$
H4:FOPT2	yes	yes	yes (no-auto HD)	0.96 (against H1)	$10.9^{+290.5}_{-10.6}, 3.2^{+19.9}_{-2.8}, 1053^{+11256}_{-962}$	$-14.45^{+0.62}_{-0.64}, 3.27^{+1.37}_{-1.54}$



# PTGW and collider search



$$\Delta\mathcal{L} = -\frac{1}{2} \frac{m_h^2}{v} (1 + \delta\kappa_3) h^3 - \frac{1}{8} \frac{m_h^2}{v^2} (1 + \delta\kappa_4) h^4$$

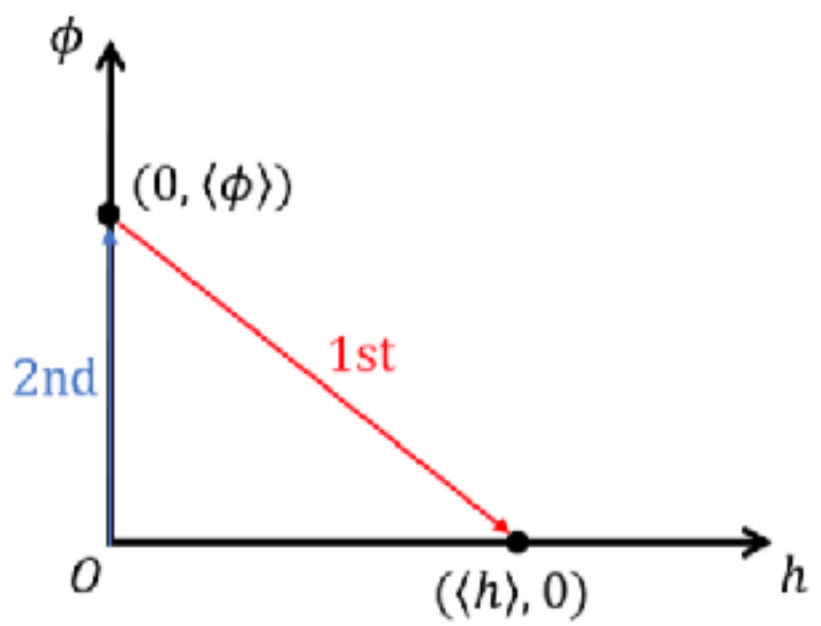
**SNR > 10 for two-step and one-step SFOEWPT**

Bian, Guo, Wu, Zhou, *Phys.Rev.D* 101 (2020) 3, 035011



# Two-step FOPT

## Type-a

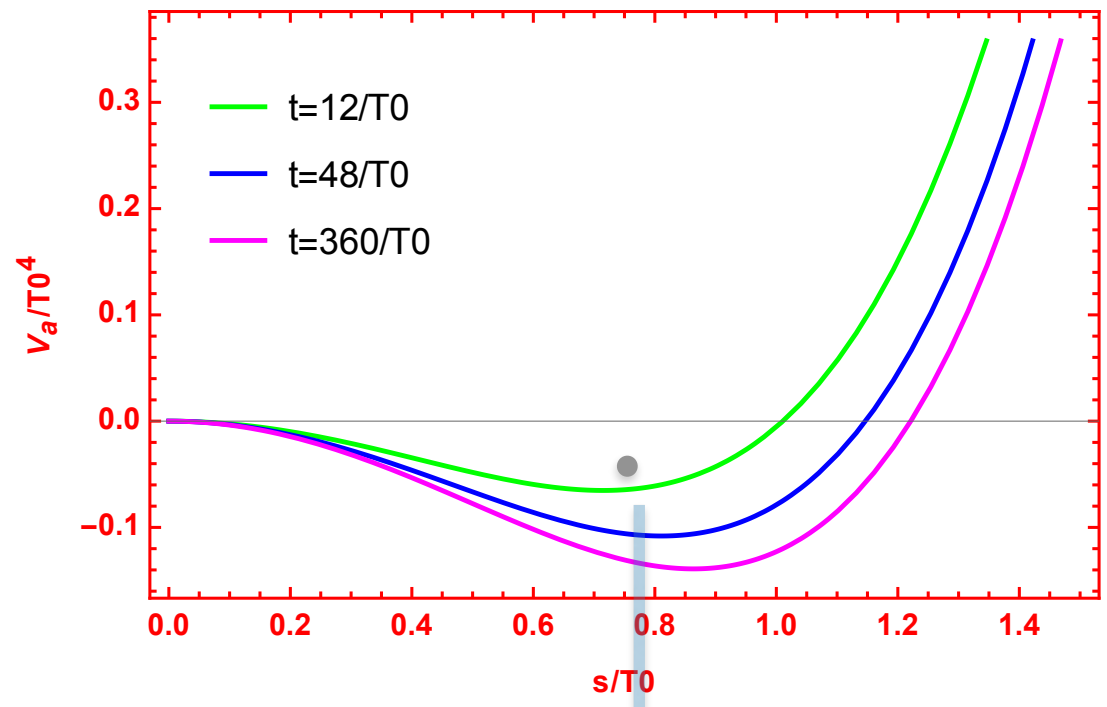


$$V_a(\phi, h, T) = \frac{1}{2}(\mu_\phi^2 + c_\phi T^2)\phi^2 + \frac{1}{2}\lambda_{h\phi}h^2\phi^2 + \frac{1}{4}\lambda_\phi\phi^4$$

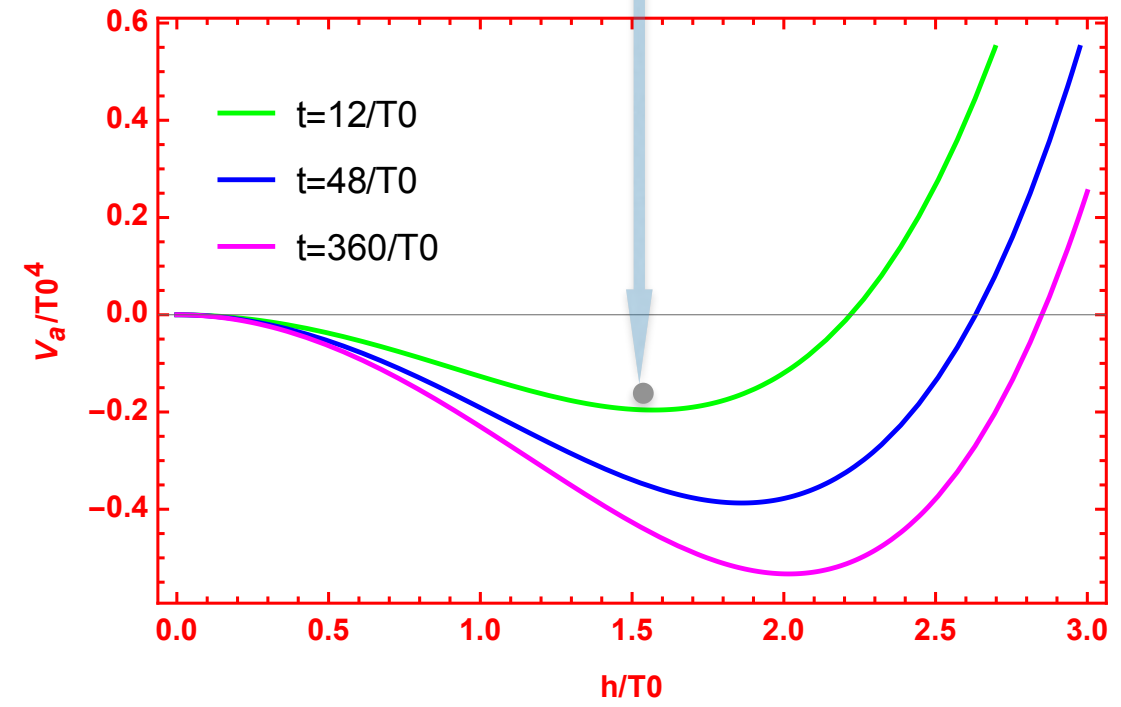
$$+ \frac{1}{2}(-\mu_h^2 + c_h T^2)h^2 + \frac{1}{4}\lambda_h h^4$$

$$c_\phi = \lambda_\phi/4 + \lambda_{h\phi}/3$$

$$c_h = (2m_W^2 + m_Z^2 + 2m_t^2)/(4v^2) + \lambda_h/2 + \lambda_{h\phi}/12$$



1st



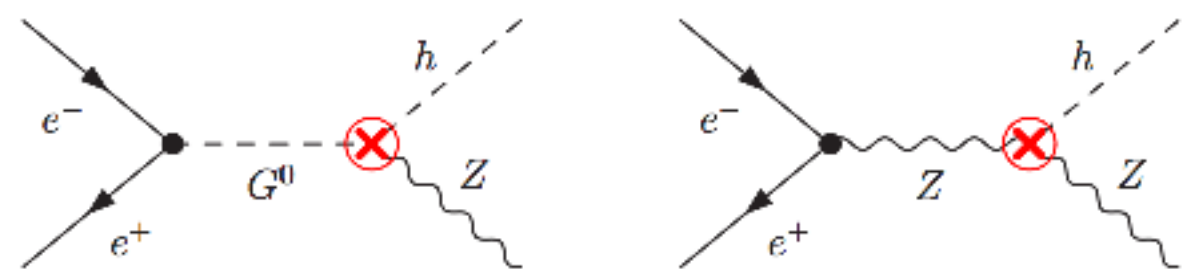
Motivated for DM&EWBG, see:1804.06813,1702.06124,1609.07143, 1605.08663, 1605.08663,etc

# ► Collider search for FOPT

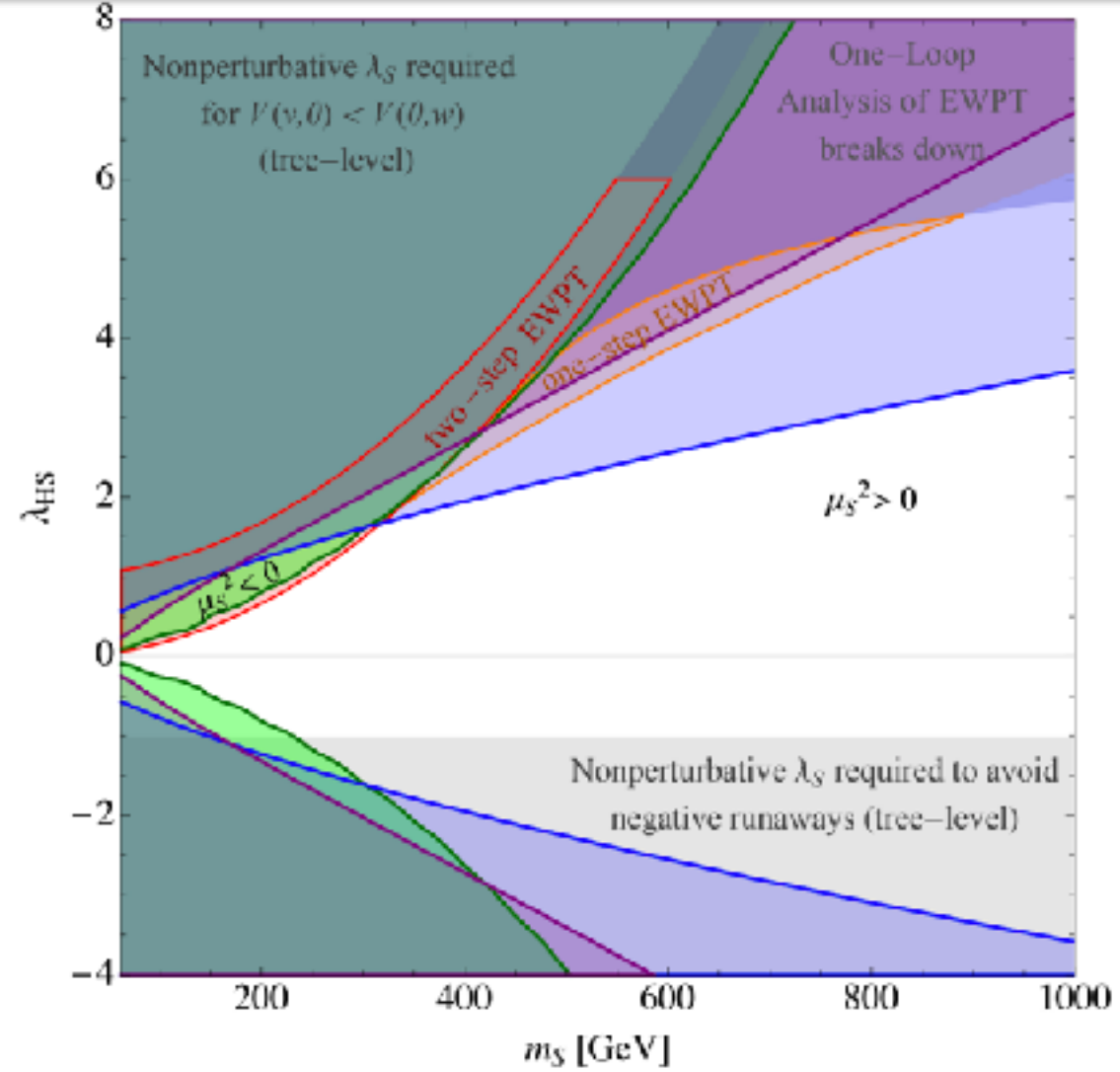
## ◎ Zh@ILC/CEPC

$$V_0 = -\mu^2|H|^2 + \lambda|H|^4 + \frac{1}{2}\mu_S^2 S^2 + \lambda_{HS}|H|^2 S^2 + \frac{1}{4}\lambda_S S^4$$

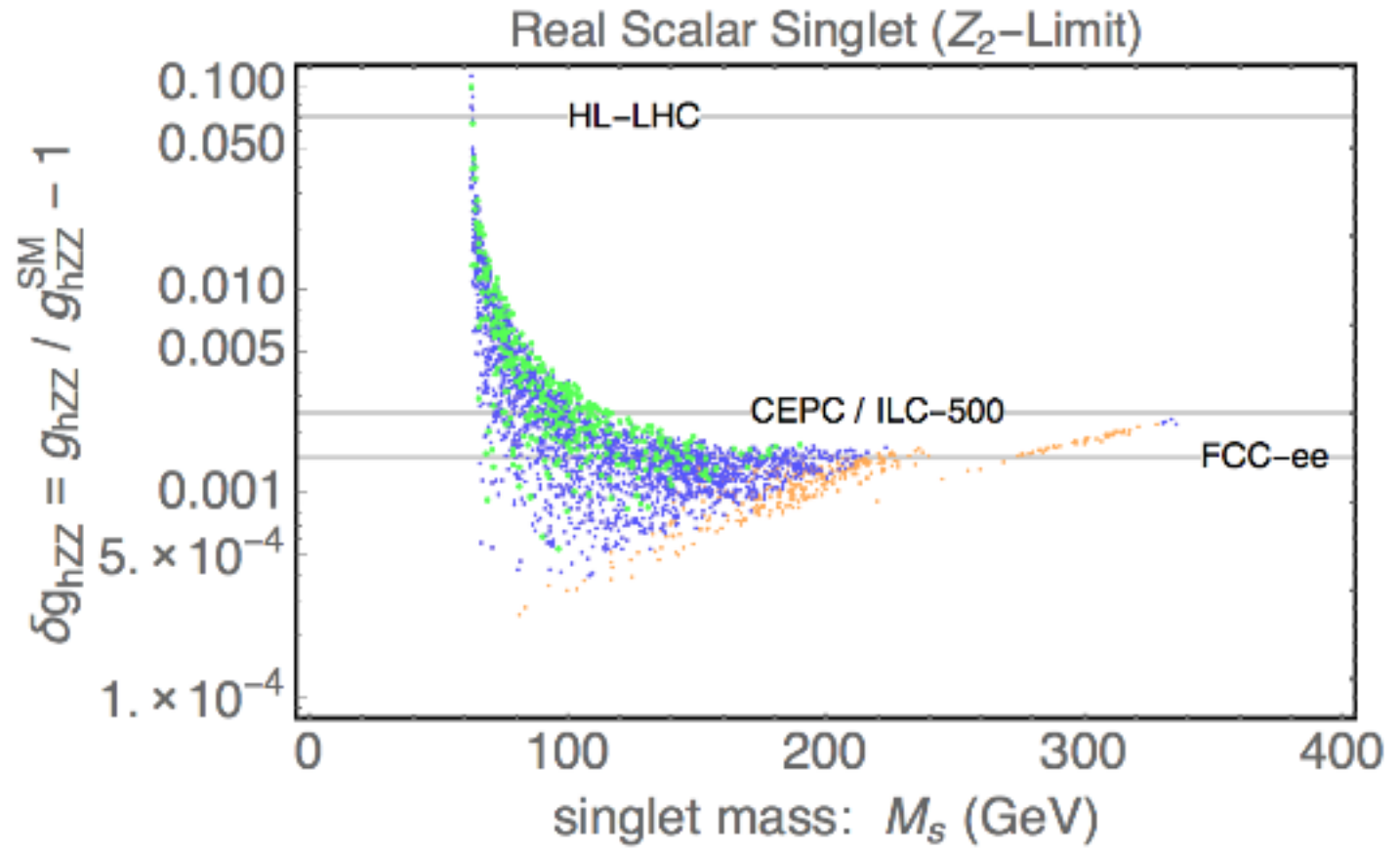
$$V_{\text{eff}}(h, T) = V_0(h) + V_0^{\text{CW}}(h) + V_T(h, T) + V_r(h, T)$$



Craig, Englert, and McCullough, 1305.5251



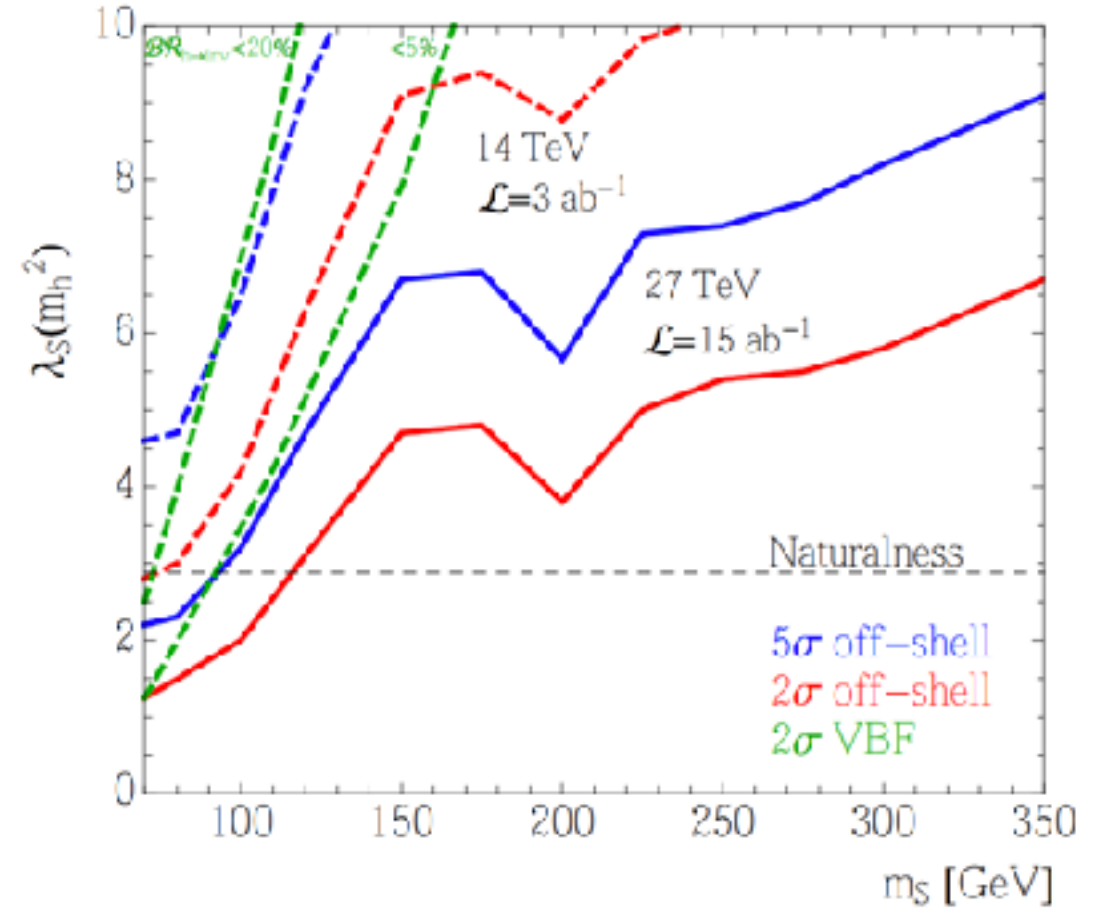
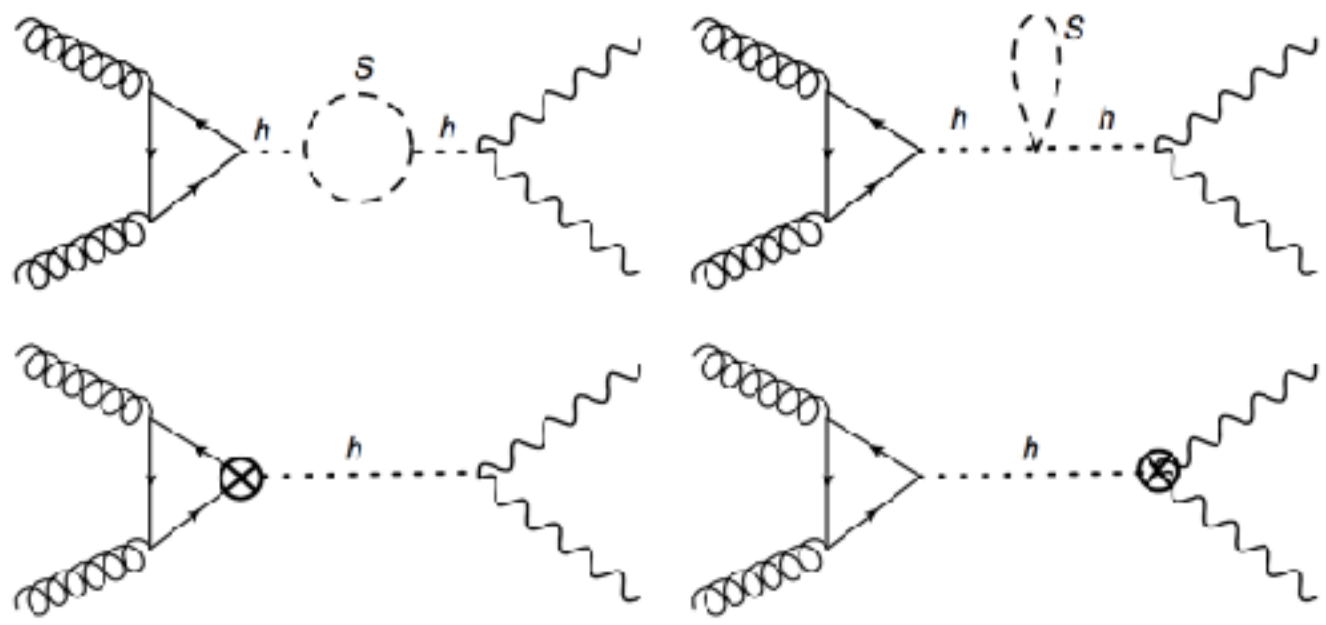
Curtin, Meade, Yu, 1409.0005



Huang, Long, and Wang, 1608.06619

# ► Collider search for FOPT

## ● Off-shell Higgs@LHC



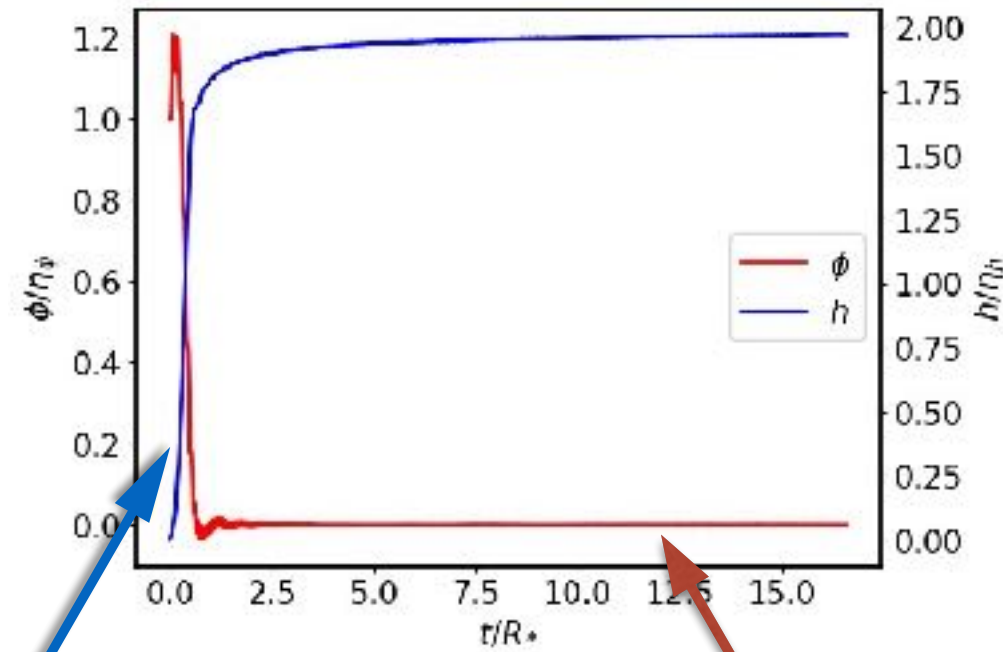
Goncalves, Han, and Mukhopadhyay, 1710.02149

See also: Lee, Park, and Qian, 1812.02679

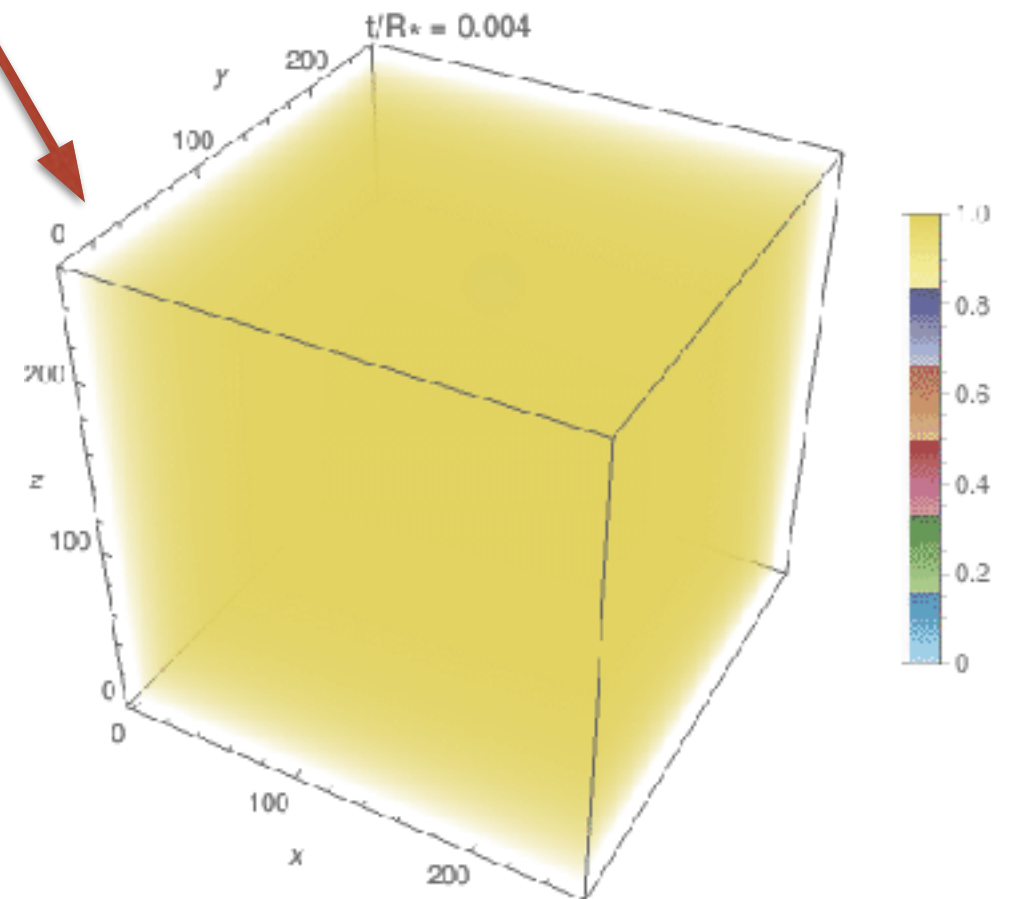
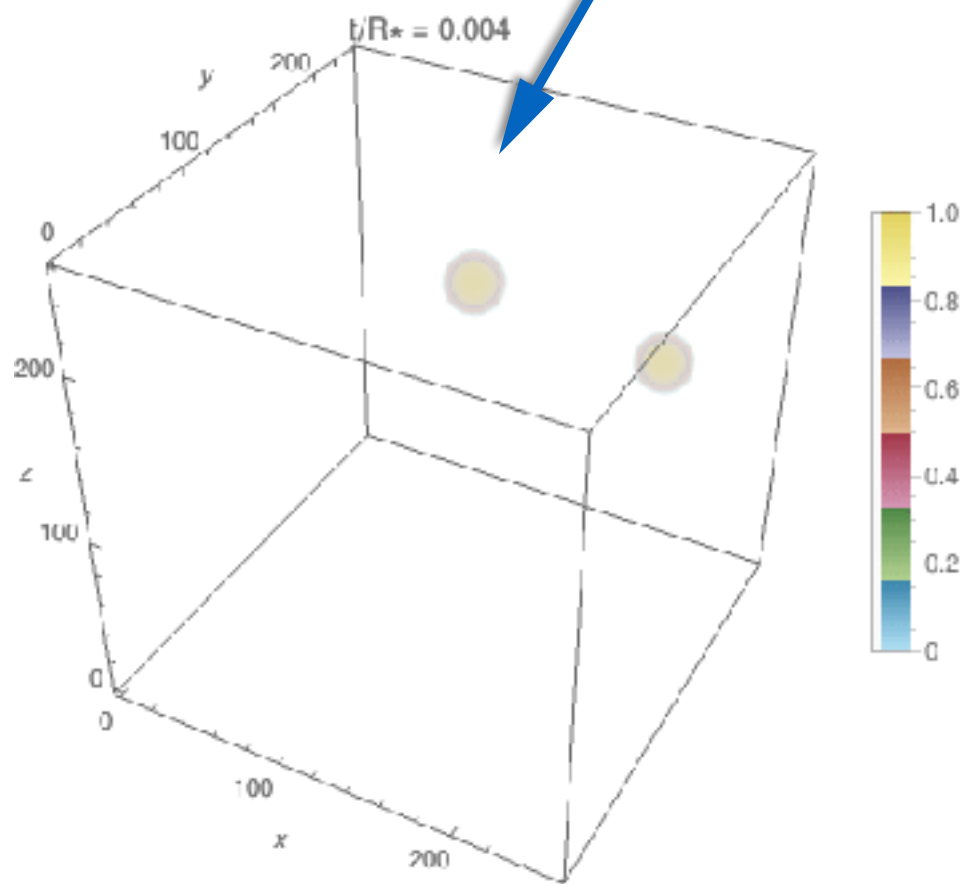


# Two-step PT with the second-step being FOPT

Type-a

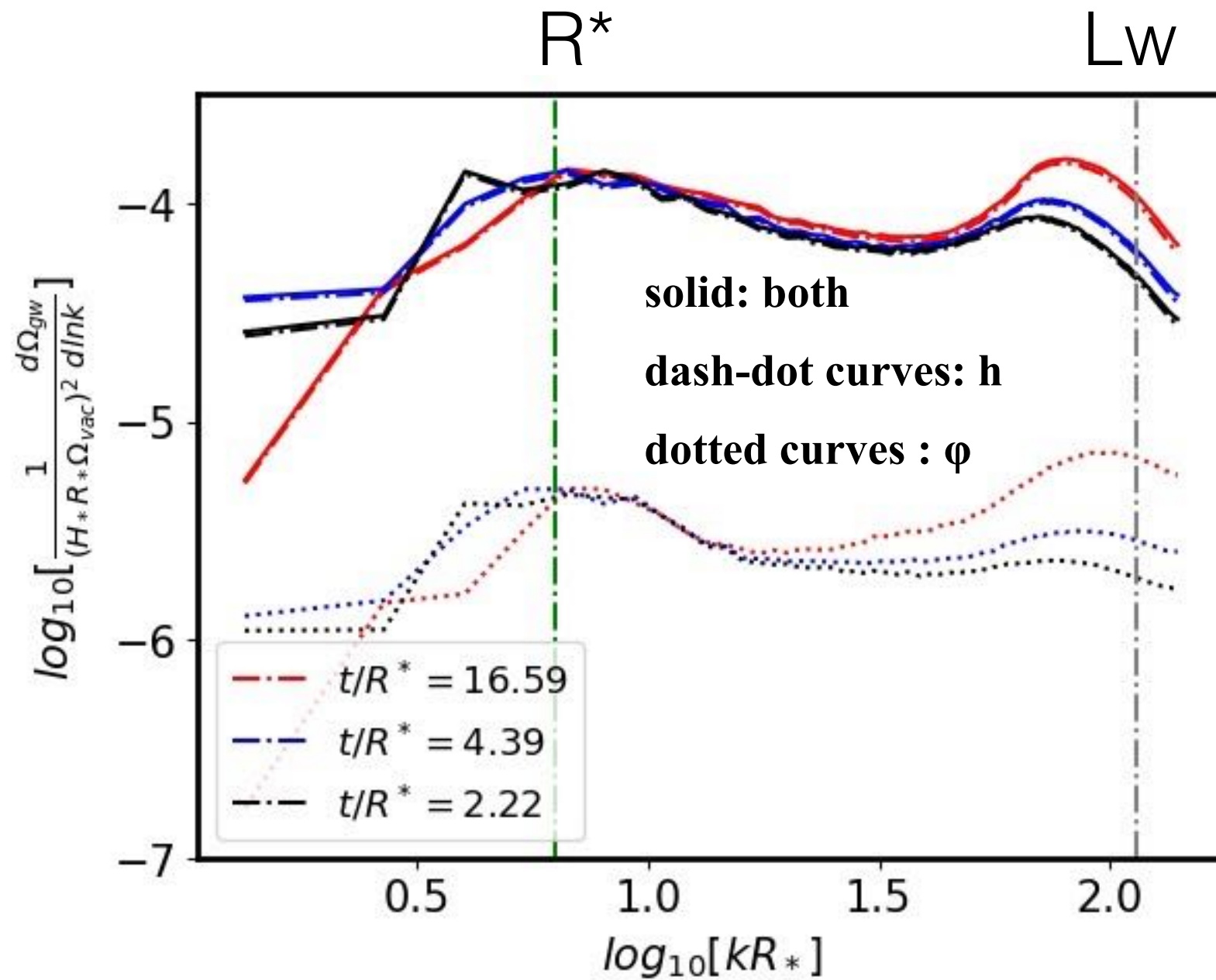


$$h(t=0, r) = \eta_h/2 \left[ 1 - \tanh\left(\frac{r-R_0}{L_w}\right) \right]$$
$$\phi(t=0, r) = \eta_\phi/2 \left[ 1 + \tanh\left(\frac{r-R_0}{L_w}\right) \right]$$



# Two-step PT with the second-step being FOPT

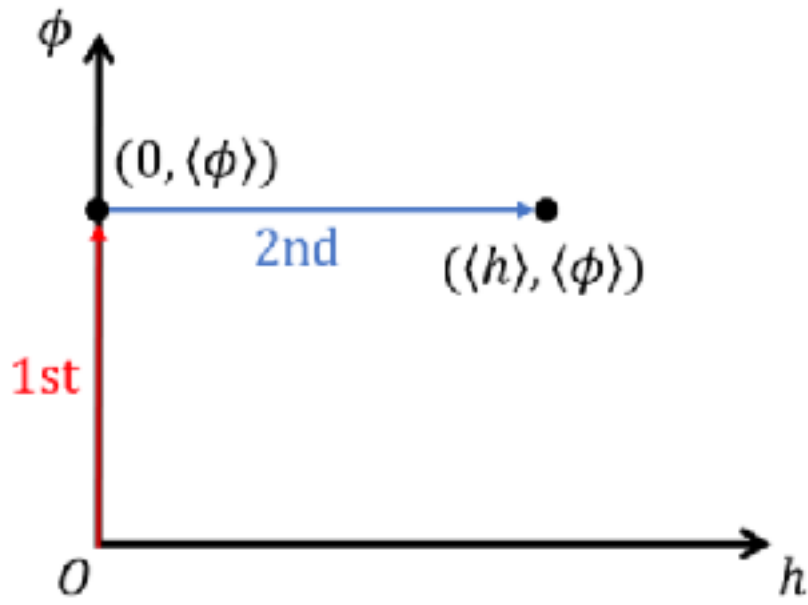
Type-a



# Two-step PT with first-step being FOPT

**Type-b**

Without Global U(1)



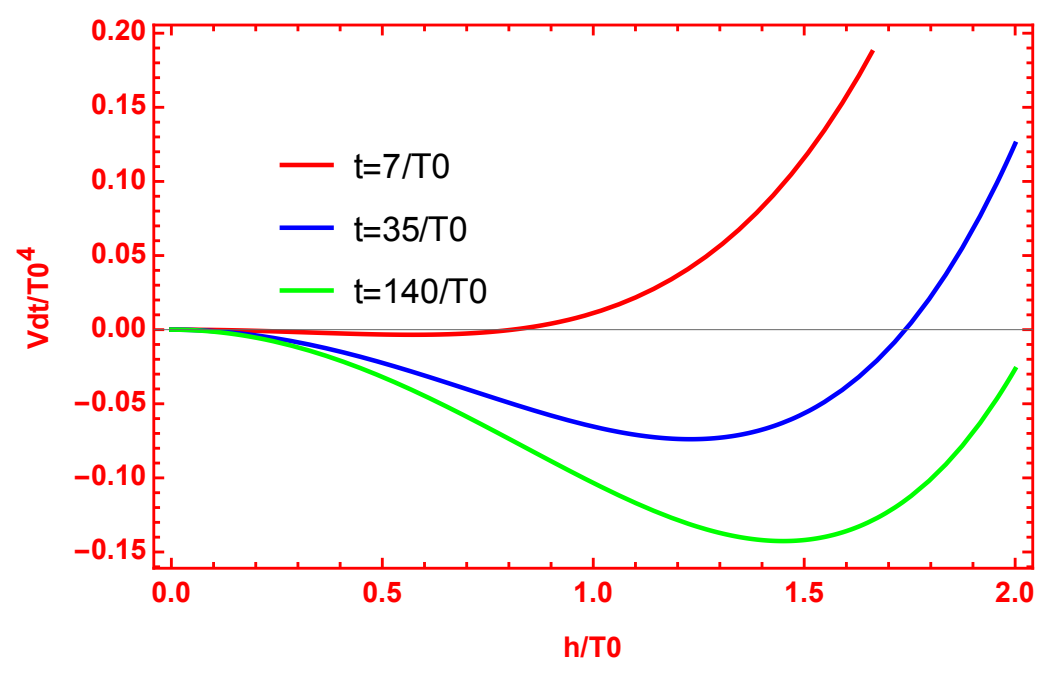
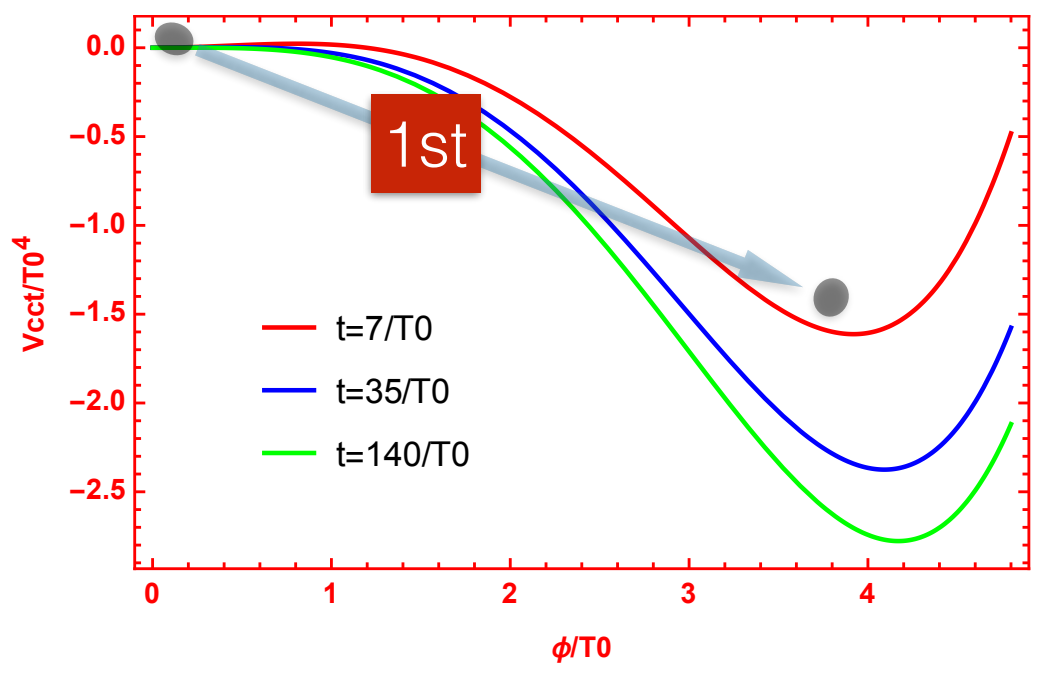
$$V_{cct}(\phi, T) = a\phi^4 (\log[|\phi|^2/v_\phi^2] - 1/4) + bT^2|\phi|^2$$

$$V_{dt}(\phi, h, T) = \frac{1}{2}c'_h T^2 h^2 + \frac{1}{4}\lambda_h h^4 - \frac{\lambda_p}{4} h^2 \phi^2$$

$$c'_h = (2m_W^2 + m_Z^2 + 2m_t^2)/(4v^2) + \lambda_h/2 + \lambda_p/24$$

$$\langle h \rangle = \sqrt{(\lambda_p \eta^2 - 2c'_h T^2)/(2\lambda_h)}$$

Classical conformal + Dimensional transmutation

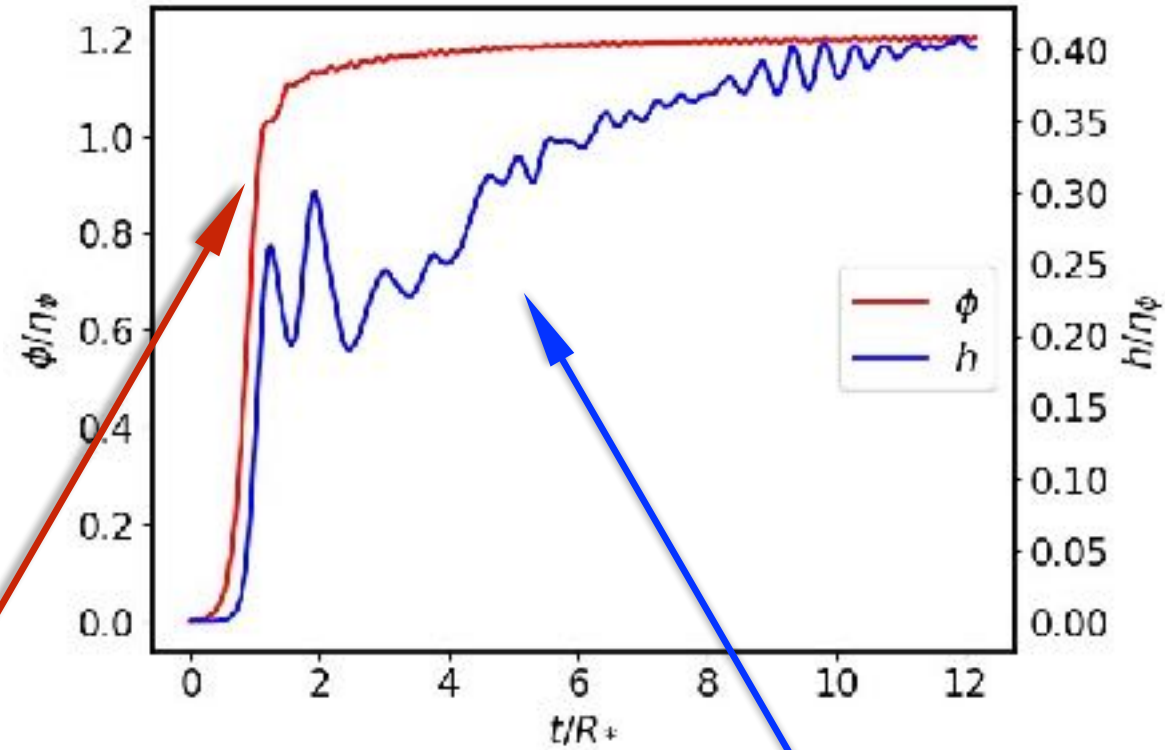




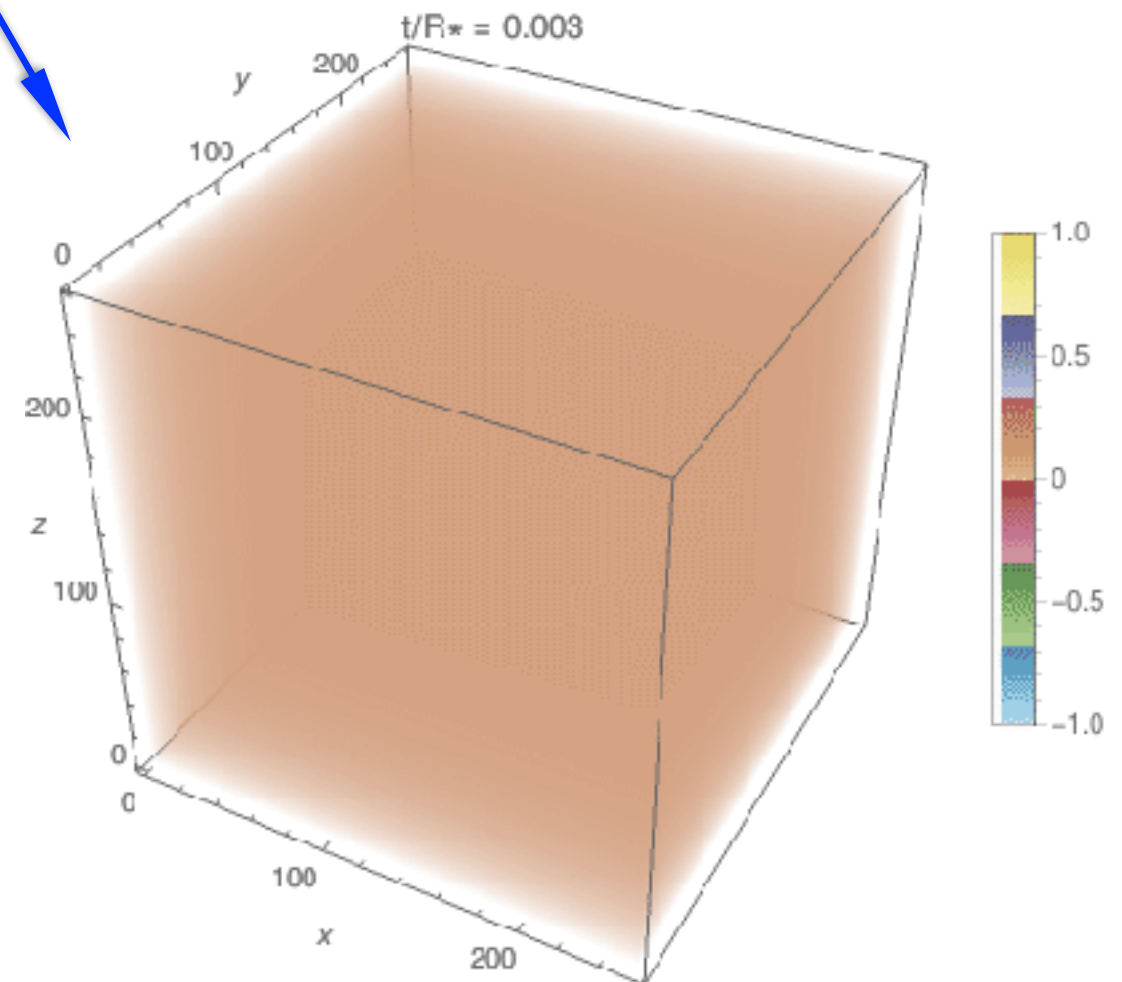
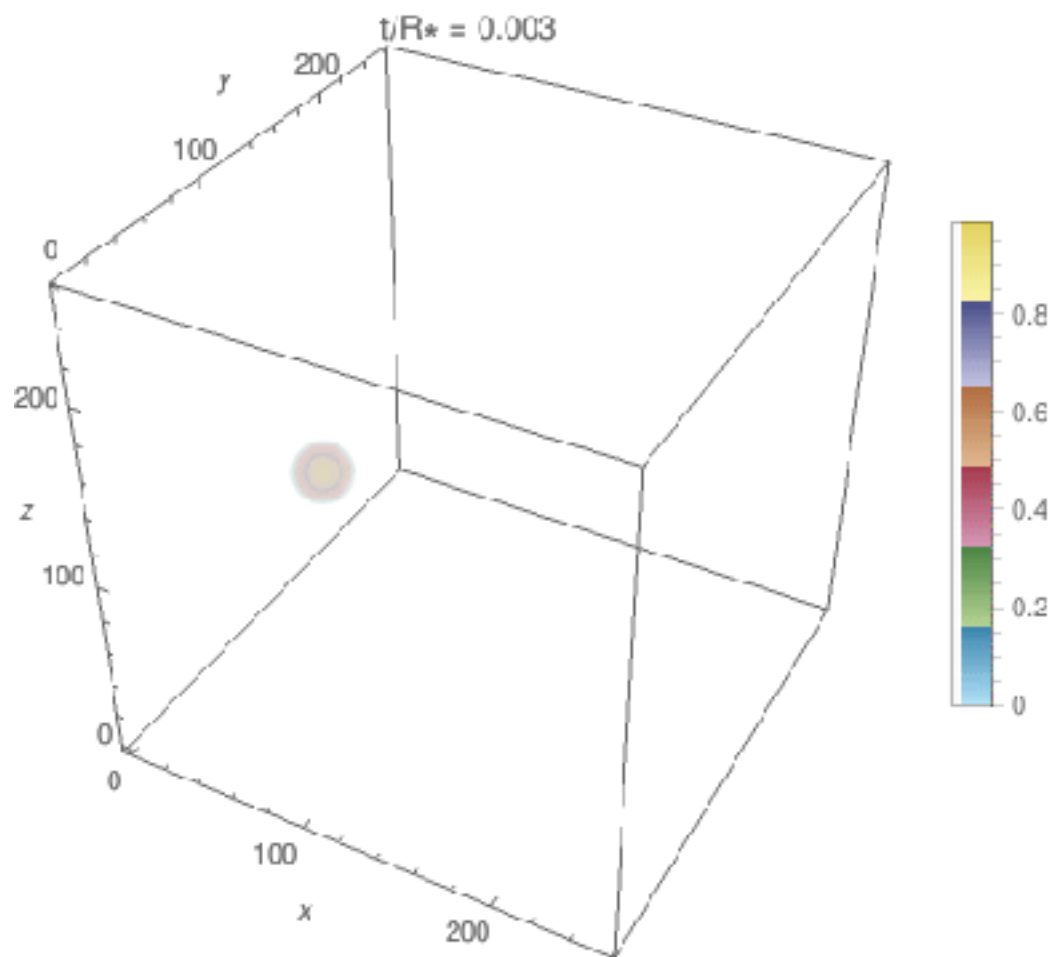
# Two-step PT with first-step being FOPT

**Type-b**

Without Global U(1)



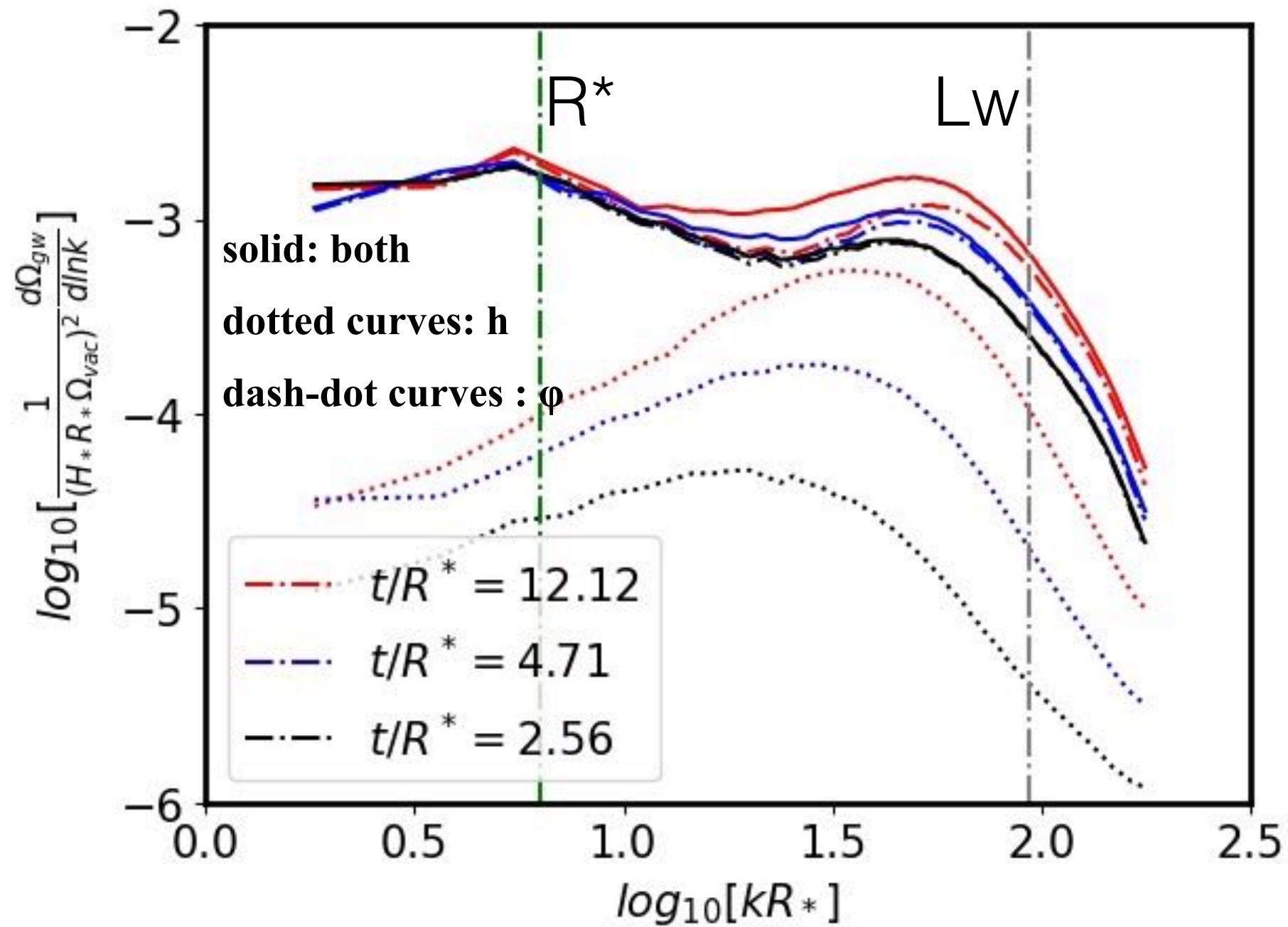
$$\phi(t=0, r) = \eta_\phi/2 \left[ 1 - \tanh\left(\frac{r-R_0}{L_w}\right) \right]$$
$$\langle h \rangle = \sqrt{(\lambda_p \eta^2 - 2c'_h T^2)/(2\lambda_h)}$$



# Two-step PT with first-step being FOPT

Type-b

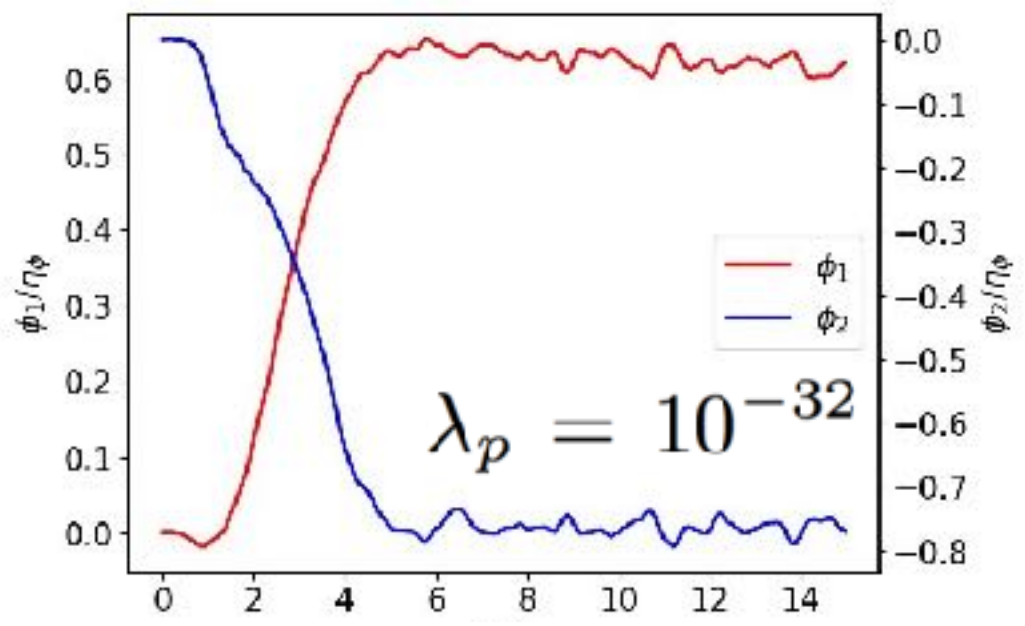
Without Global U(1)



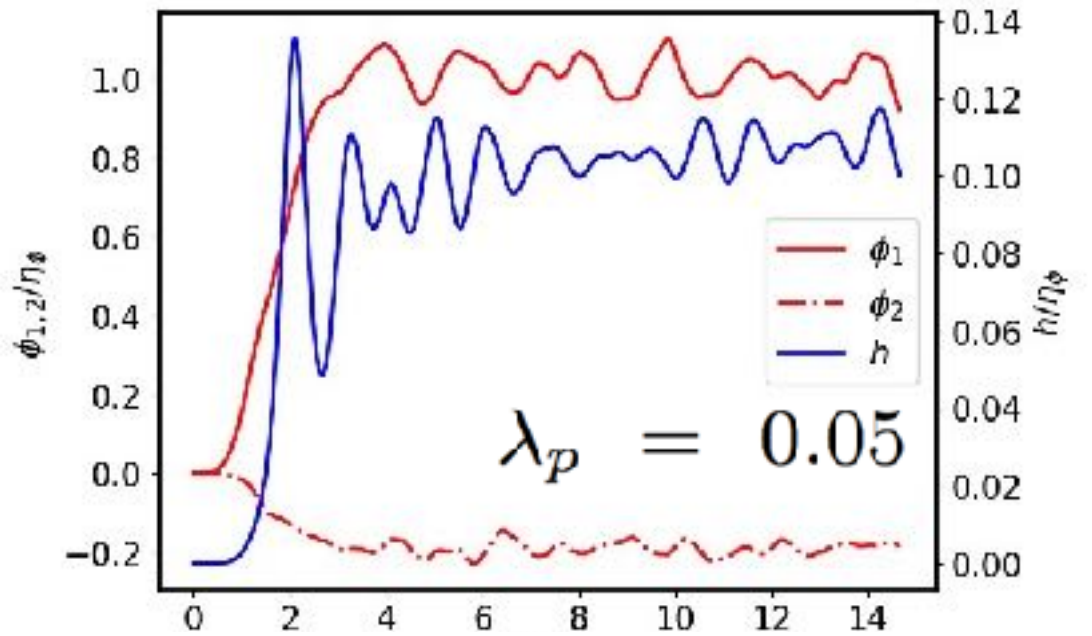
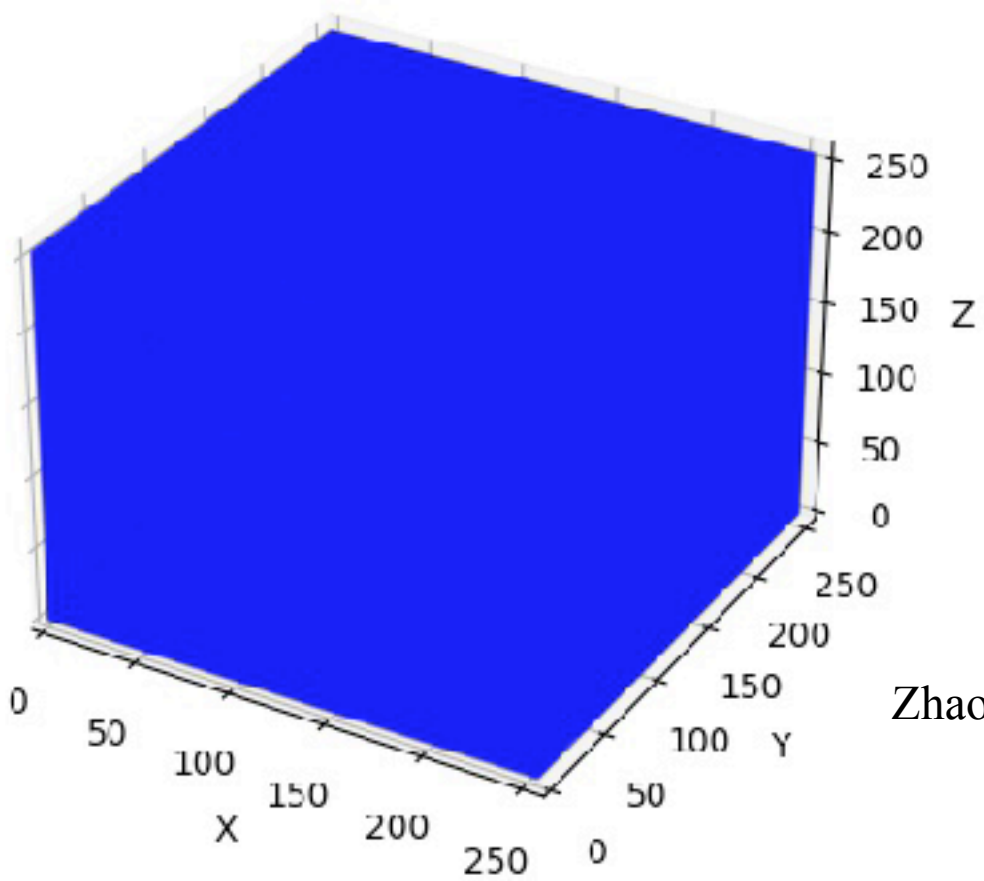
# Two-step FOPT with global U(1)

**Type-b**

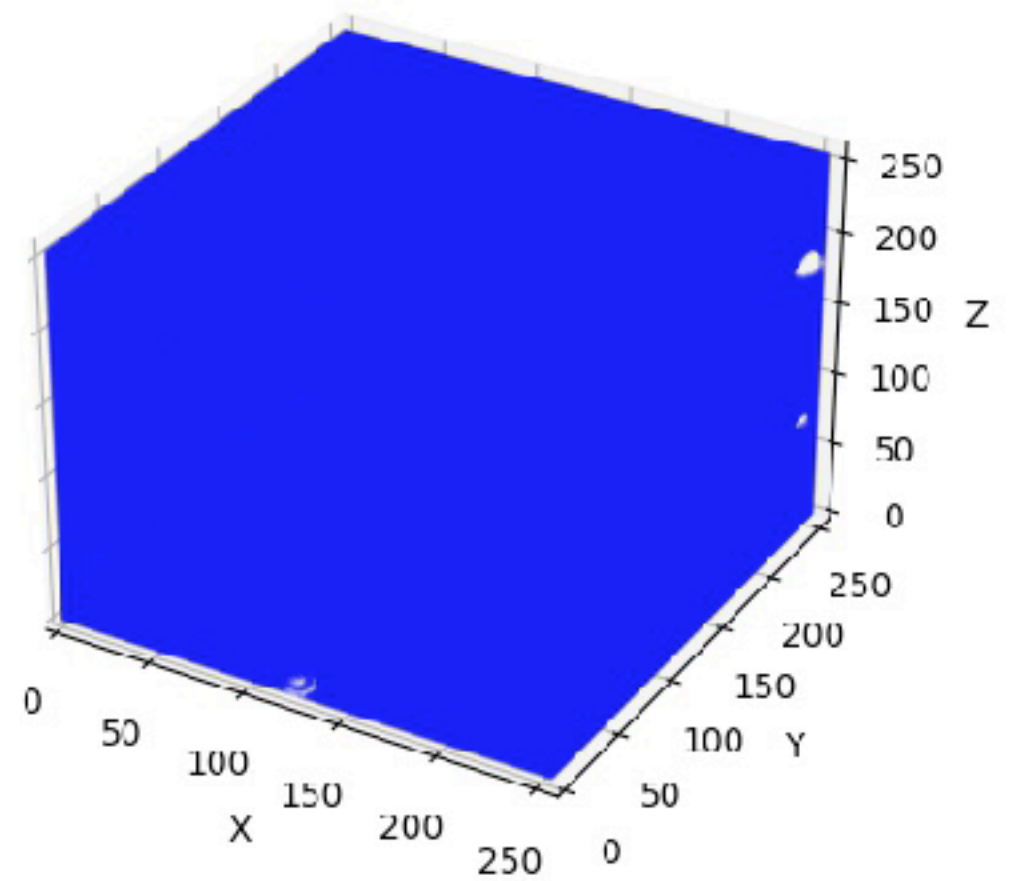
With Global U(1) Motivated for strong CP and axion DM



$t/R^* = 0.43$



$t/R^* = 0.45$



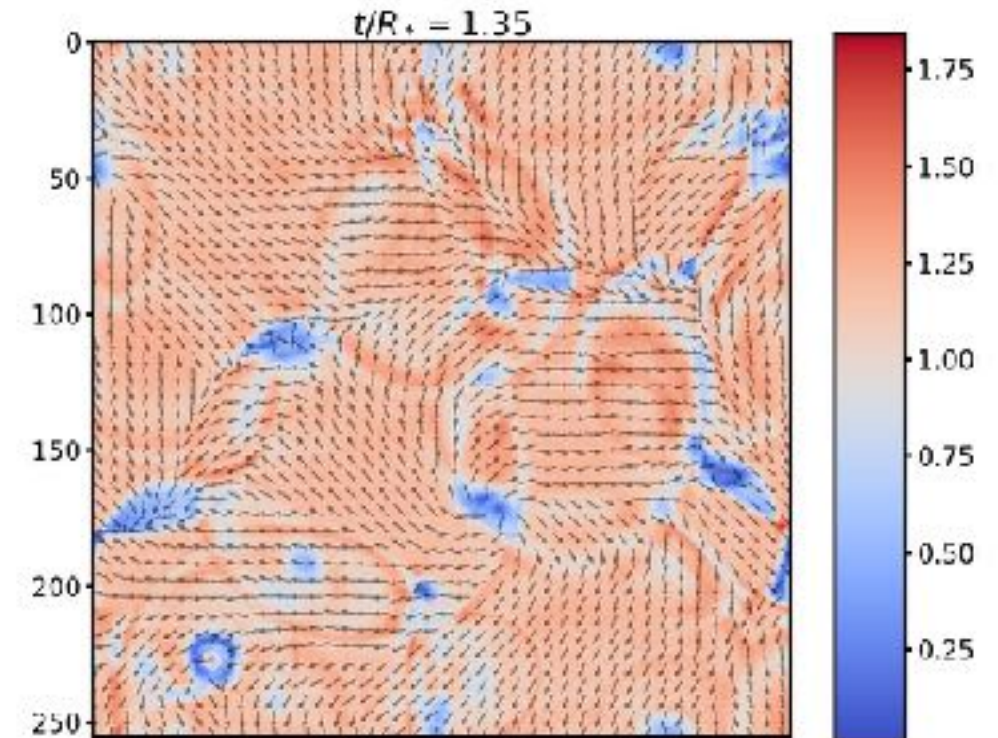
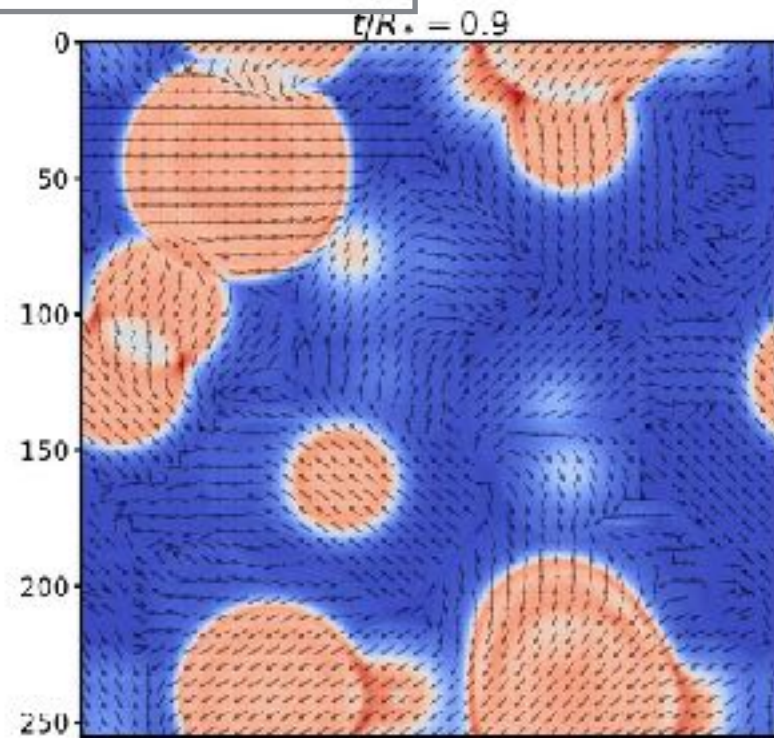
Zhao, Di, [Bian](#), Cai, 2204.04427



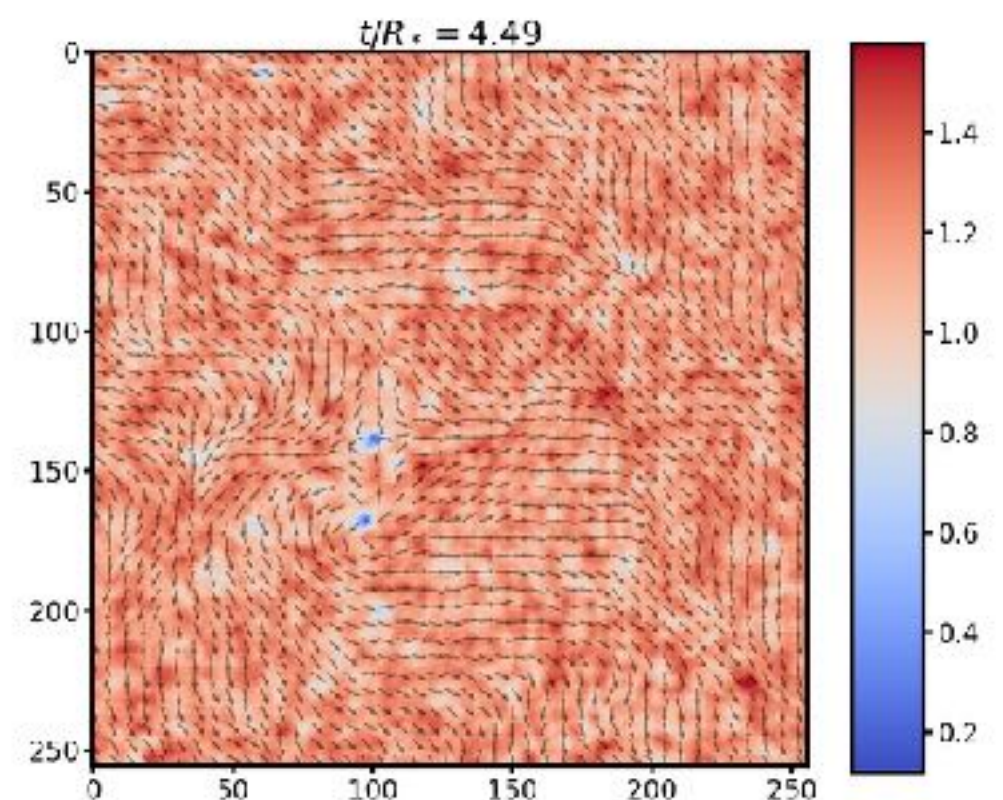
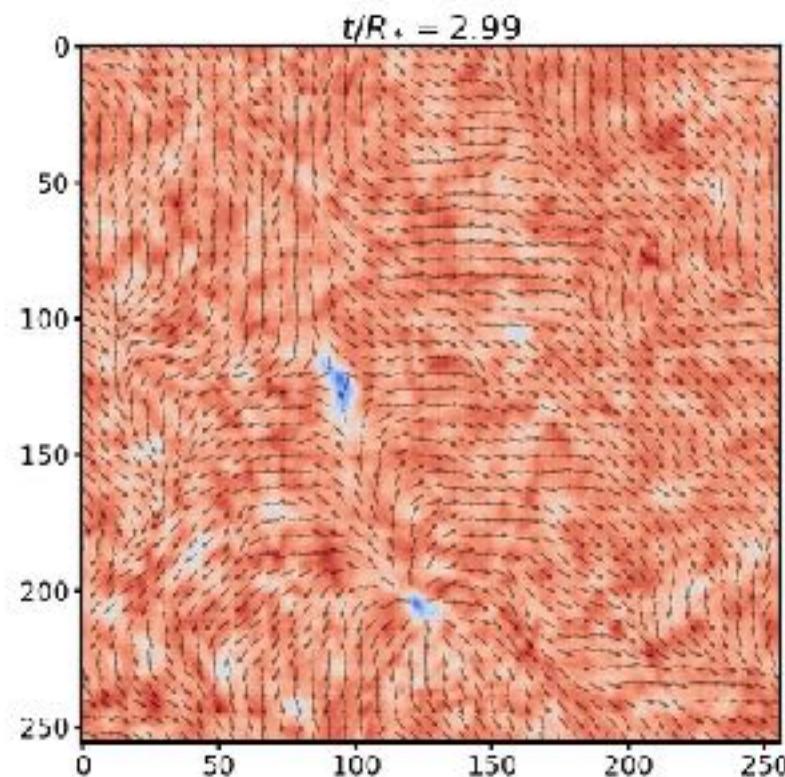
# ► Bubbles and vortex&anti-vortex

Type-b

With Global U(1)



Arrows: phase distribution

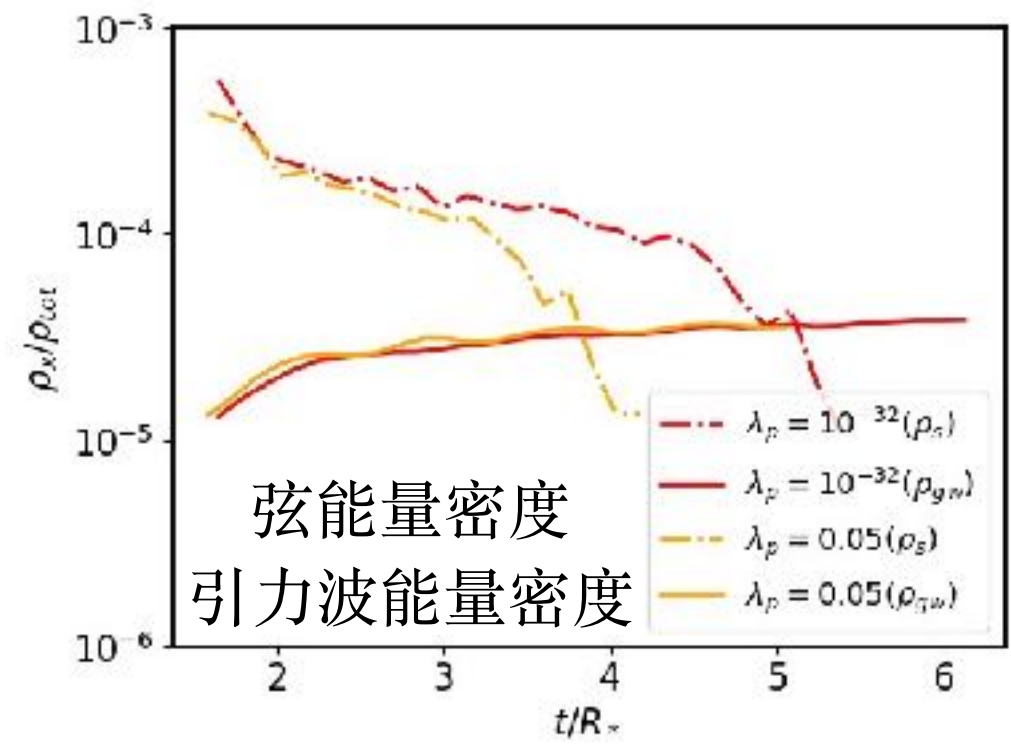
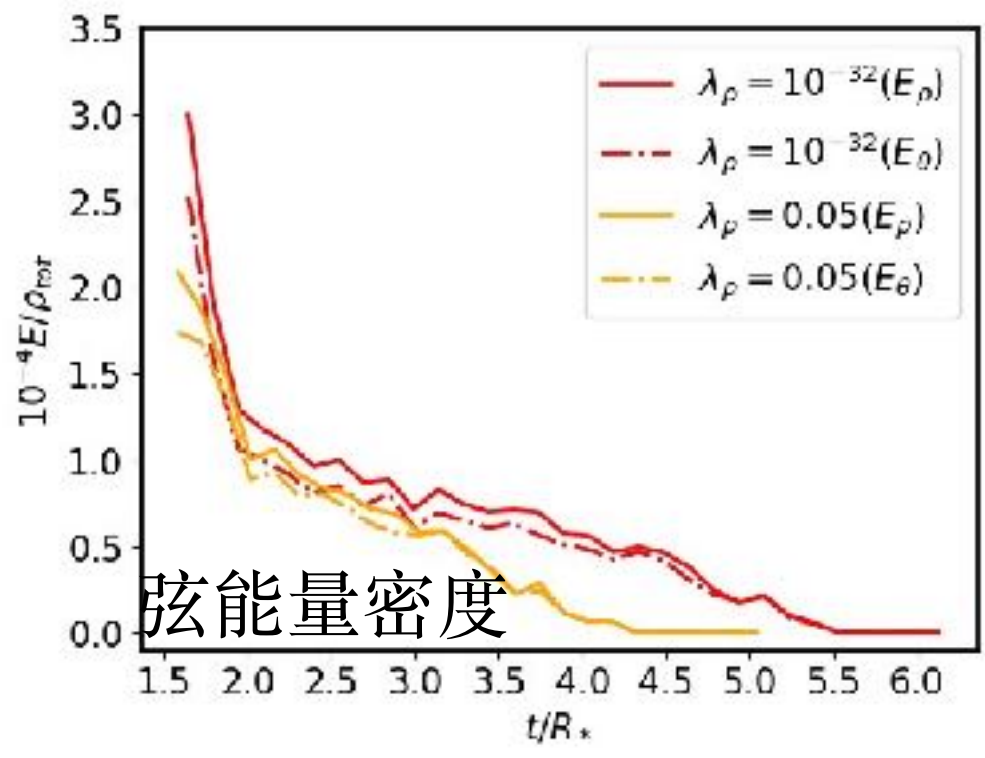
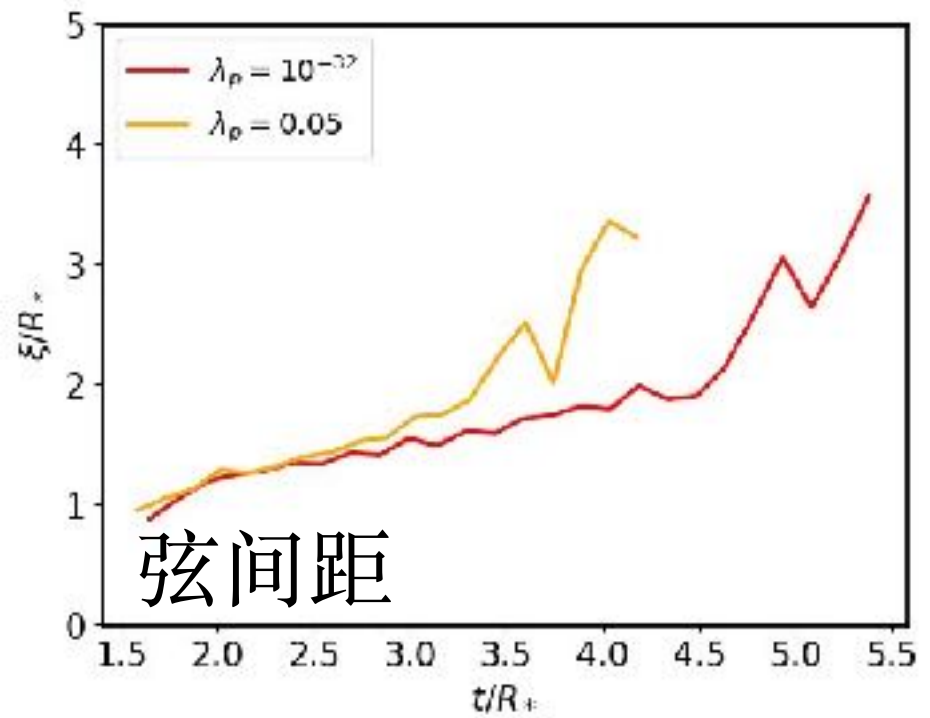
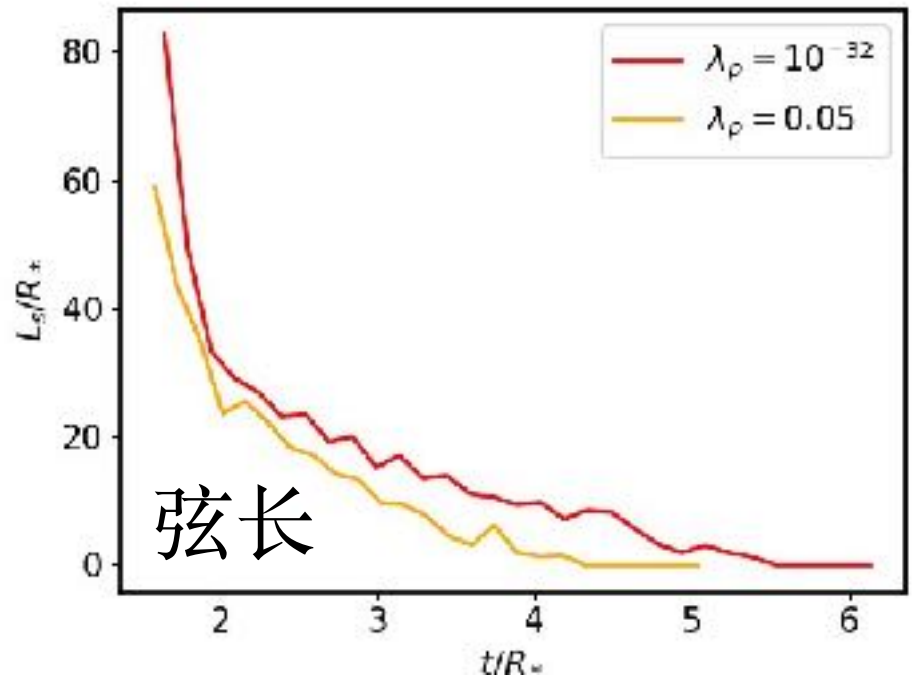




# Global string from FOPT

**Type-b**

With Global U(1)



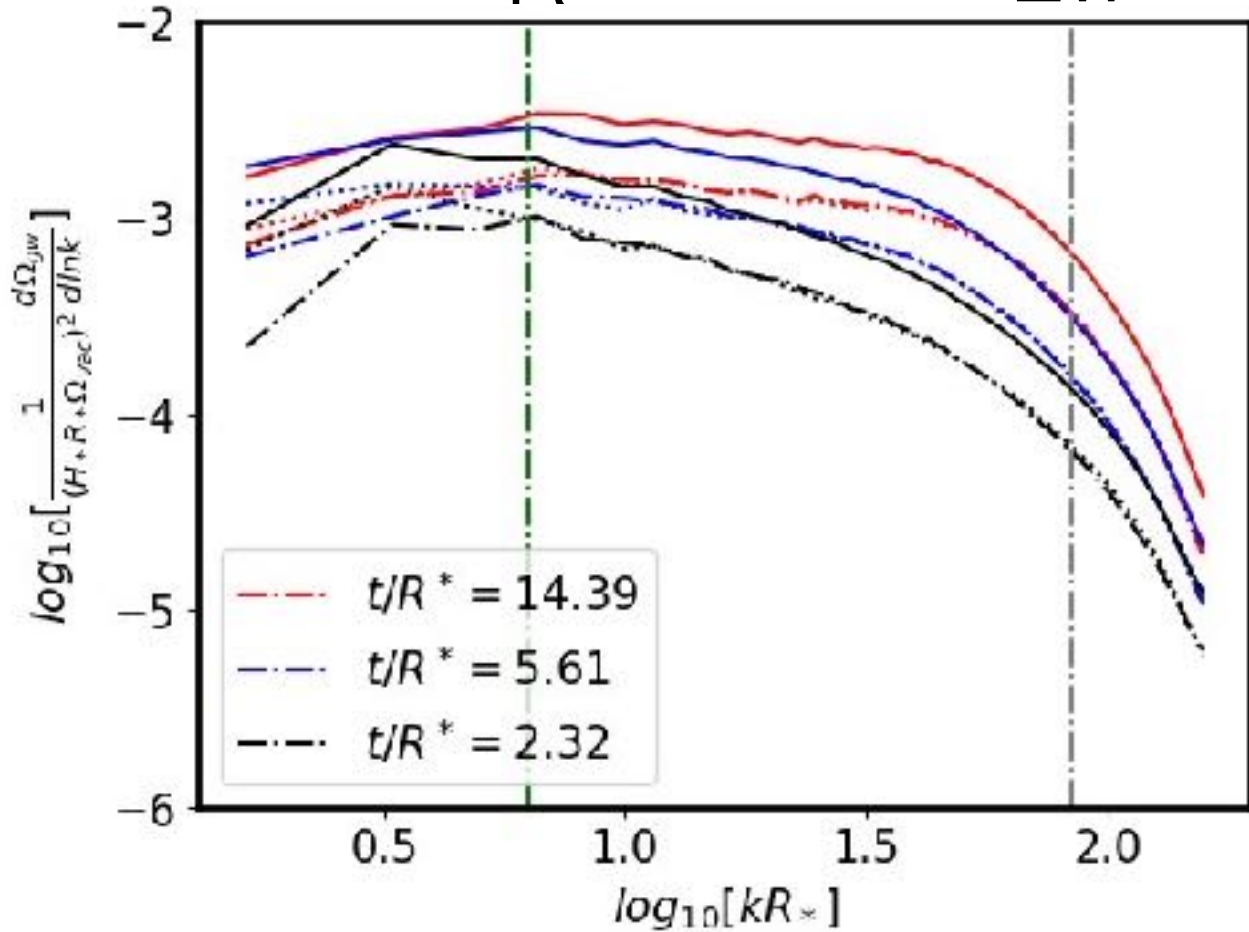
# Global string from FOPT

**Type-b**

With Global U(1)

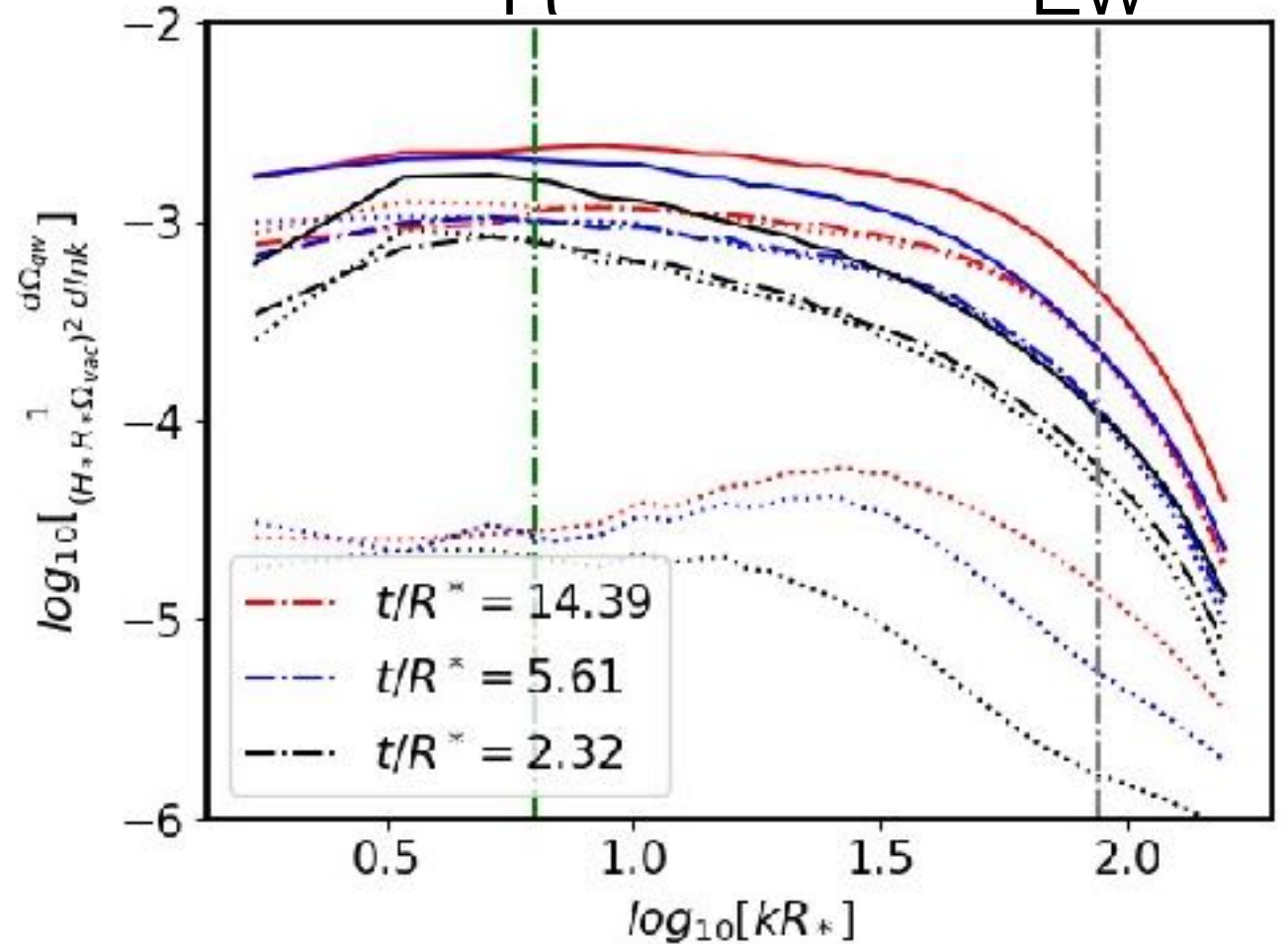
$$\lambda_p = 10^{-32}$$

$R^*$   $LW$



$$\lambda_p = 0.05$$

$R^*$   $LW$



solid: all    dotted curves: h    dash-dot curves :  $\phi_1$     dash curves :  $\phi_2$



1. EWSB and GW from FOPT
  - **Probing the Higgs Potential shape and EWPT patterns with GW production and Colliders complementarily**
2. BAU and GW from FOPT
  - **Sphaleron process, bubble velocity**
3. DM and GW from FOPT
  - **DM and high/low-scale PT, DM out-of-equilibrium & FOPT, PBH DM&FOPT**
4. Topological defects from FOPT
  - **Magnetic monopoles, cosmic strings, domain walls**

Thanks!