An unambiguous test of positivity at lepton colliders

Jiayin Gu (顾嘉荫)

Fudan University

Joint Workshop of the CEPC Physics, Software and New Detector Concept May 25, 2022

[arXiv:2011.03055] JG, Lian-Tao Wang, Cen Zhang



Jiayin Gu (顾嘉荫)

Introduction

Can all EFTs be UV completed?

- Dispersion relations of forward elastic amplitudes suggest that certain operator coefficients can only be positive.
 - Assuming the UV physics is consistent with the fundamental principles of QFT (analyticity, locality, unitarity, Lorentz invariance).
 - [hep-th/0602178] Adams, Arkani-Hamed, Dubovsky, Nicolis, Rattazzi, ... many papers...
 [1902.08977, 2005.03047, ...] Zhang, Zhou et al.,
 [1908.09845, 2004.02885] Remmen, Rodd. ...
- These positivity bounds only exist for certain Dimension-8 (or higher) operators!

$$rac{d^2}{ds^2}\mathcal{A}(ab
ightarrow ab)_{t
ightarrow 0}\geq 0\,.$$

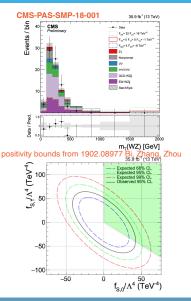


By measuring these dim-8 operator coefficients, we can test whether the underlying new physics is consistent with the fundamental principles of QFT.

Can we do it?

Probing positivity bounds on dimension-8 operators

- The dimension-8 contribution has a large energy enhancement (~ E⁴/Λ⁴)!
- It is difficult for LHC to probe these bounds.
 - Low statistics in the high energy bins.
 - Example: Vector boson scattering.
 - Λ ≤ √s, the EFT expansion breaks down!



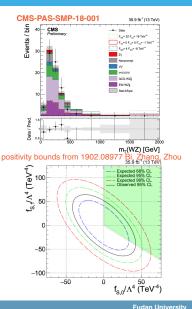
3

Probing positivity bounds on dimension-8 operators

- The dimension-8 contribution has a large energy enhancement (~ E⁴/Λ⁴)!
- It is difficult for LHC to probe these bounds.
 - Low statistics in the high energy bins.
 - Example: Vector boson scattering.
 - Λ ≤ √s, the EFT expansion breaks down!
- Can we separate the dim-8 and dim-6 effects?
 - Precision measurements at several different √s?

(A very high energy lepton collider?)

Or find some special process where dim-8 gives the leading new physics contribution?



Jiayin Gu (顾嘉荫)

The diphoton channel



e⁺e⁻ → γγ (or μ⁺μ⁻ → γγ), SM, non-resonant.
 Tree level SM: the only helicity configuration is A(f⁺f⁻γ⁺γ⁻).

- Leading order contribution: dimension-8 contact interaction.
- $(f^+f^- \rightarrow \bar{e}_L e_L \text{ or } e_R \bar{e}_R)$

$$\mathcal{A}(f^{+}f^{-}\gamma^{+}\gamma^{-})_{\rm SM+d8} = 2e^{2}\frac{\langle 24\rangle^{2}}{\langle 13\rangle\langle 23\rangle} + \frac{a}{v^{4}}[13][23]\langle 24\rangle^{2}.$$

 Operators: Also contributes to ZZ/Zγ final states with opposite helicities.
 [1806.09640] Bellazzini, Riva, see the d8 basis in
 [2005.00008] Shu et al., [2005.00059] Murphy

$$\begin{split} a_L &= -2 \frac{v^4}{\Lambda^4} \left(c_W^2 c_{l^2 B^2 D}^2 - 2 s_W c_W c_{l^2 W B D}^{(2)} + s_W^2 c_{l^2 W^2 D}^{(1)} \right), \\ a_R &= -2 \frac{v^4}{\Lambda^4} \left(c_W^2 c_{e^2 B^2 D}^2 + s_W^2 c_{e^2 W^2 D}^2 \right), \end{split}$$

$$\begin{split} &Q_{l^2B^2D} = i(\bar{l}\gamma^{\mu} \overleftrightarrow{D}^{\nu} l) B_{\mu\rho} B_{\nu}^{\,\rho}, \\ &Q_{l^2WBD}^{(2)} = i(\bar{l}\gamma^{\mu} \tau^{I} \overleftrightarrow{D}^{\nu} l) (B_{\mu\rho} W_{\nu}^{I\rho} + B_{\nu\rho} W_{\mu}^{I\rho}), \\ &Q_{l^2W^2D}^{(1)} = i(\bar{l}\gamma^{\mu} \overleftrightarrow{D}^{\nu} l) W_{\mu\rho}^{I} W_{\nu}^{I\rho}, \\ &Q_{e^2B^2D} = i(\bar{e}\gamma^{\mu} \overleftrightarrow{D}^{\nu} e) B_{\mu\rho} B_{\nu}^{\,\rho}, \\ &Q_{e^{2W^2D}} = i(\bar{e}\gamma^{\mu} \overleftrightarrow{D}^{\nu} e) W_{\mu\rho}^{I} W_{\nu}^{I\rho}. \end{split}$$

Jiayin Gu (顾嘉荫)

Positivity bounds

• The $e^+e^- \rightarrow \gamma\gamma$ amplitude:

$$\mathcal{A}(f^+f^-\gamma^+\gamma^-)_{\rm SM+d8} = 2e^2 \frac{\langle 24\rangle^2}{\langle 13\rangle\langle 23\rangle} + \frac{a}{v^4} [13][23]\langle 24\rangle^2 = 2e^2 \frac{\langle 24\rangle^2}{\langle 13\rangle\langle 23\rangle} \left(1 + \frac{a}{2e^2v^4}tu\right)$$

• The $e\gamma \rightarrow e\gamma$ amplitude:

$$\mathcal{A}(f^+\gamma^+f^-\gamma^-)_{\rm SM+d8} = 2e^2\frac{\langle 34\rangle^2}{\langle 12\rangle\langle 32\rangle}\left(1+\frac{a}{2e^2v^4}su\right) \underset{t\to 0}{=} \mathcal{M}_{\rm SM}\left(1-\frac{a}{2e^2v^4}s^2\right)\,,$$

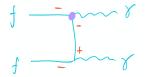
• $\mathcal{M}_{\rm SM} = -2e^2$ is the SM amplitude in the forward limit.

- ► Positivity bound $\frac{d^2}{ds^2} \mathcal{A}(f^+\gamma^+f^-\gamma^-)|_{t\to 0} \ge 0$ implies $a \ge 0$.
- ► The interference term is bounded to be destructive in $e_{\gamma} \rightarrow e_{\gamma}$, and constructive in $e^+e^- \rightarrow \gamma\gamma!$

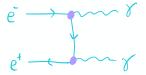
Jiayin Gu (顾嘉荫)

All other contributions are either vanishing or suppressed!

The only tree-level d6 contribution are from dipole operators and have different fermion helicities.



- SM×d6 at tree level: no interference.
- d6²: Dipole operators are very well constrained by g 2 and EDM measurements.



Jiayin Gu (顾嘉荫)

All other contributions are either vanishing or suppressed!

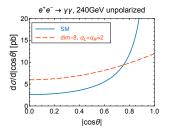
- SM×d6 at 1-loop: are either very-well constrained by other measurements with tree-level contributions, or forbidden by selection rules.
 - O_{3W} is very well constrained by $e^+e^- \rightarrow WW$ measurements.



- Other contributions are constrained by Z-pole measurements or suppressed by the small y_{e} .
- Contribution from the *eett* 4f operator is forbidden by angular momentum selection rules. ((2001.04481) Shu et al.)

$$e^{i}$$
 e^{i} e^{i} e^{i} e^{-i} with opposite helicities)

other d8: They have different helicities and do not interfere with SM.



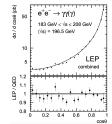
Differential cross section (The production polar angle θ is "folded" since the photon polarizations are not measured.)

$$\begin{split} & \frac{d\sigma(e^+e^- \to \gamma\gamma)}{d|\cos\theta|} \\ &= \frac{(1-P_{e^-})(1+P_{e^+})}{4} \frac{e^4}{4\pi s} \left(\frac{1+c_\theta^2}{1-c_\theta^2} + a_L \frac{s^2(1+c_\theta^2)}{4e^2v^4}\right) \\ &+ \frac{(1+P_{e^-})(1-P_{e^+})}{4} \frac{e^4}{4\pi s} \left(\frac{1+c_\theta^2}{1-c_\theta^2} + a_R \frac{s^2(1+c_\theta^2)}{4e^2v^4}\right) \,, \end{split}$$

- Positivity bounds: $a_L \ge 0$, $a_R \ge 0$.
- Positivity bound directly on the cross section!

$$\sigma(\boldsymbol{e}^{+}\boldsymbol{e}^{-} \to \gamma\gamma) \geq \sigma_{\rm SM}(\boldsymbol{e}^{+}\boldsymbol{e}^{-} \to \gamma\gamma).$$

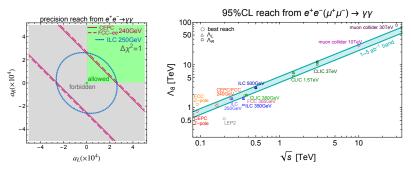
> The LEP measurement was $\sim 1.5\sigma$ below the SM prediction.



Jiayin Gu (顾嘉荫)

An unambiguous test of positivity at lepton colliders

1302.3415



- χ^2 fit to the binned distribution
 - Statistics only, 19 bins in $\cos \theta \subset [0, 0.95]$.
 - Agrees reasonably well with LEP result ($\lesssim 10\%$ in the reach on Λ).
- Is beam polarization useful? Yes and no!
 - One could measure σ_L and σ_R simultaneously.
- High energy still wins!

$$\frac{\Lambda_2}{\Lambda_1} = \left(\frac{E_2}{E_1}\right)^{\frac{3}{4}} \left(\frac{L_2}{L_1}\right)^{\frac{1}{8}} \ .$$

Jiayin Gu (顾嘉荫)

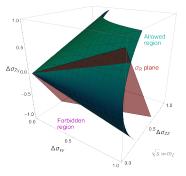
Combined $\gamma\gamma/Z\gamma/ZZ$ analysis at high energy

- $Z\gamma$, ZZ processes are more complicated due to the massive Z.
 - Other helicity states contribute in both SM and BSM (e.g. nTGCs).
 - ▶ In the high energy limit, $A(f^+f^-V^+V^-)$ dominates in SM.
- In the $\sqrt{s} \gg m_Z$ limit,

 $\sigma(e^+e^- \to ZZ) \ge \sigma_{\rm SM}(e^+e^- \to ZZ)$.

- Consider the elastic amplitude of eV → eV,
 - V is an arbitrary mixing state of γ and Z,
 - scan over the mixing angle to obtain the strongest bound (Δσ ≡ σ − σ_{SM}),

 $(\Delta \sigma_{Z\gamma})^2 \le 4 \Delta \sigma_{\gamma\gamma} \Delta \sigma_{ZZ}.$



- σ_R s only occupy a plane in the 3d parameter space.
 - 3 operators with ℓ_L , 2 operators with e_R .

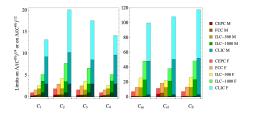
Jiayin Gu (顾嘉荫)

Many operators, many positivity bounds...

$$\begin{split} O_1 &= \partial^a (\bar{e} \gamma^\mu e) \partial_\alpha (\bar{e} \gamma_\mu e) , & C_1 &\ge \gamma, \\ O_1 &= \partial^a (\bar{e} \gamma^\mu e) \partial_\alpha (\bar{e} \gamma_\mu e) , & C_2 &\le 0, \\ O_2 &= \partial^a (\bar{e} \gamma^\mu e) \partial_\alpha (\bar{l} \gamma_\mu l) , & C_5 &\le 0, \\ O_3 &= D^\alpha (\bar{e} l) D_\alpha (\bar{l} e) , & C_3 &\ge 0, \\ O_4 &= \partial^\alpha (\bar{l} \gamma^\mu l) \partial_\alpha (\bar{l} \gamma_\mu l) , & Q_4 &= \partial^\alpha (\bar{l} \gamma^\mu l) \partial_\alpha (\bar{l} \gamma_\mu l) , \\ O_1 &= (\bar{l} \gamma^\mu e) (\bar{l} \gamma_\mu l) , & O_5 &= D^\alpha (\bar{l} \gamma^\mu \tau^I l) D_\alpha (\bar{l} \gamma_\mu \tau^I l) , & 2\sqrt{C_1(C_4 + C_5)} &\ge -(C_2 + C_3). \end{split}$$

 $C_1 < 0$

 Multiple runs with different energies & beam polarizations are very useful! Angular distributions also help.



Jiayin Gu (顾嘉荫)

Conclusion

- ► Measurements of $e^+e^- \rightarrow \gamma\gamma$ (or $\mu^+\mu^- \rightarrow \gamma\gamma$) offer a unique opportunity to directly probe dimension-8 operators and their positivity bounds.
- ▶ We can do it at a lepton collider with $\sqrt{s} \sim 240 \text{ GeV}$ (but higher energy is always better).
 - Build a Higgs factory, get a positivity test for free!
- If there is a deviation from SM, we can measure e⁺e⁻ → γγ at several energies (e.g. Z-pole and 240 GeV) to check whether it comes from d8 operators (~ s²).

Conclusion

- Measurements of e⁺e⁻ → γγ (or μ⁺μ⁻ → γγ) offer a unique opportunity to directly probe dimension-8 operators and their positivity bounds.
- ▶ We can do it at a lepton collider with $\sqrt{s} \sim 240 \text{ GeV}$ (but higher energy is always better).
 - Build a Higgs factory, get a positivity test for free!
- If there is a deviation from SM, we can measure e⁺e⁻ → γγ at several energies (e.g. Z-pole and 240 GeV) to check whether it comes from d8 operators (~ s²).
- Can QFT really break down at the TeV scale?
 - Example from history: Nobody expected classical physics to break down, nobody expected parity to be violated, ...



It's important to do the experiment!

Jiayin Gu (顾嘉荫)

backup slides

Jiayin Gu (顾嘉荫

Fudan University



Cen Zhang (1984-2021)

Jiayin Gu (顾嘉荫)

Dispersion relations

• Consider a forward ($t \rightarrow 0$) elastic amplitude ($s + t + u = 4m^2$)

$$\begin{split} \tilde{\mathcal{A}}_{ab}(s) &= \sum_{n} c_{n} (s-\mu^{2})^{n}, \\ c_{n} &= \frac{1}{2\pi i} \oint_{s=\mu^{2}} ds \frac{\tilde{\mathcal{A}}_{ab}(s)}{(s-\mu^{2})^{n+1}}, \end{split}$$

- Applying the fundamental principles of QFT
 - Analyticity (Cauchy's theorem applies)
 - Locality (poles from tree-level factorization, branch cuts from loops, Froissart Bound)
 - Unitarity (Optical theorem, $\mathrm{Im}\mathcal{A}\sim\sigma_{\mathrm{tot}}$)
 - Lorentz invariance (Crossing symmetry)
 - Dispersion relation tells us that

$$c_n = \int_{4m^2}^{\infty} \frac{ds}{\pi} s \sqrt{1 - \frac{4m^2}{s}} \left(\frac{\sigma_{\text{tot}}^{ab}}{(s - \mu^2)^{n+1}} + (-1)^n \frac{\sigma_{\text{tot}}^{a\bar{b}}}{(s - 4m^2 + \mu^2)^{n+1}} \right) + c_n^{\infty} \,,$$

Jiayin Gu (顾嘉荫)

b in(s) in(s)

Sum rules and positivity bounds

Sum rule:

$$c_n = \int_{4m^2}^{\infty} \frac{ds}{\pi} s \sqrt{1 - \frac{4m^2}{s}} \left(\frac{\sigma_{\text{tot}}^{ab}}{(s - \mu^2)^{n+1}} + (-1)^n \frac{\sigma_{\text{tot}}^{a\bar{b}}}{(s - 4m^2 + \mu^2)^{n+1}} \right) + c_n^{\infty} ,$$

- ► Froissart bound: $\mathcal{A} < \text{const} \cdot s \log^2 s \Rightarrow c_n^\infty = 0 \text{ for } n > 1.$
- For even *n*, the two terms with cross sections are both positive, so $c_n > 0$.
- Consider the limit $m^2 \ll \mu^2 \ll \Lambda^2$ (massless SMEFT).

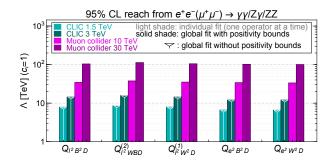
$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \sum_{i} \frac{c_{i}^{(6)}}{\Lambda^{2}} \mathcal{O}_{i}^{(6)} + \sum_{j} \frac{c_{j}^{(8)}}{\Lambda^{4}} \mathcal{O}_{j}^{(8)} + \cdots$$
$$\mathcal{A}(s)|_{t=0} = c_{0} + c_{1} s + c_{2} s^{2} + \cdots$$

- ► $c_{n=1}$ \Leftrightarrow dimension-6 (no positivity bounds, boundary can be nonzero), $c_{n=2}$ \Leftrightarrow dimension-8 (or d6²) (has positivity bounds), ...
- See [2011.00037] Bellazzini, Miró, Rattazzi, Riembau, Riva, [2012.15849] Arkani-Hamed, Huang, Huang for more general positivity bounds for d ≥ 8 and [2010.04723] Remmen, Rodd, [2108.06334] Davighi, Melville, You for positivity bounds at dim-6 (require additional assumptions).

Jiayin Gu (顾嘉荫)

$\int \mathcal{L} dt [\mathrm{ab}^{-1}]$					
unpolarized	91 GeV	161 GeV	240 GeV	365 GeV	
CEPC	8	2.6	5.6		
FCC-ee	150	10	5	1.5	
ILC	250 GeV	350 GeV	500 GeV		
(-0.8, +0.3)	0.9	0.135	1.6		
(+0.8, -0.3)	0.9	0.045	1.6		
$(\pm 0.8, \pm 0.3)$	0.1	0.01	0.4		
CLIC	380 GeV	1.5 TeV	3 TeV		
(-0.8, 0)	0.5	2	4		
(+0.8, 0)	0.5	0.5	1		
muon collider	10 TeV	30 TeV			
unpolarized	10	90			

Jiayin Gu (顾嘉荫)



- Global fit of the $\gamma\gamma/Z\gamma/ZZ$ processes in the high energy limit.
- No beam polarizations ⇒ flat directions.
- Flat directions are lifted once the positivity bounds are imposed!

What if positivity bound is violated?

Statistical fluctuation, systematic error, ...

• Even 5σ can go away in the diphoton channel.

EFT is not valid?

- An *s*-channel light ($m \lesssim \sqrt{s}$) spin-2 particle?
- ► Very well probed by resonance searches $e^+e^- \rightarrow X\gamma/XZ$, $X \rightarrow \gamma\gamma/e^+e^-$. (see *e.g.* ILC 750 GeV study [1607.03829])
- ▶ By measuring $e^+e^- \rightarrow \gamma\gamma$ at several energies (*e.g.* Z-pole and 240 GeV) we can check whether the deviation comes from d8 operators ($\sim s^2$) or something else.

Use helicity amplitudes to classify the sum rules.

elastic 4-point amplitudes $\mathcal{A}(12 \rightarrow 3_{=1}4_{=2})$	spinor form of $\mathcal{A}_4^{[2]}$ (d6 operators)	$\begin{array}{c} \text{spinor form of } \mathcal{A}_4^{[4]} \\ (\text{d8 or } \text{d6}^2) \end{array}$	
$\phi_1\phi_2\phi_1^*\phi_2^*$	s_{ij}	$s_{ij} imes s_{kl}$	
$\psi^- \phi \psi^+ \phi^*$	$\langle 12 \rangle [23]$	$\langle 12 \rangle [23] \times s_{ij}$	
$\psi_1^- \psi_2^- \psi_1^+ \psi_2^+$	$\langle 12 \rangle [34]$	$\langle 12 \rangle [34] \times s_{ij}$	
$V^- \phi V^+ \phi^*$	X	$\langle 12 \rangle^2 [23]^2$	
$V^-\psi^-V^+\psi^+$	X	$(12)^{2}[23][34]$	
$V_1^- V_2^- V_1^+ V_2^+$	×	$\langle 12 \rangle^2 [34]^2 , \ \langle 12 \rangle^2 [34]^2 \frac{t-u}{s}$	

- Tree level dimension-6: only scalar-scalar, scalar-fermion and fermion-fermion amplitudes!
- Forward limit:

$$\tilde{\mathcal{A}}_4^{[2]} \equiv \mathcal{A}_4^{[2]}|_{t \to 0} \propto \boldsymbol{s}, \qquad \quad \tilde{\mathcal{A}}_4^{[4]} \equiv \mathcal{A}_4^{[4]}|_{t \to 0} \propto \boldsymbol{s}^2$$

20

scalar-scalar

$$\begin{split} & \frac{c_H + 3c_T}{\Lambda^2} = \left. \frac{d\mathcal{A}_{\phi^+\phi^-}}{ds} \right|_{s=0} = \left. \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\rm tot}^{\phi^+\phi^-} - \sigma_{\rm tot}^{\phi^+\phi^+} \right) + c_\infty \,, \\ & - \frac{2c_T}{\Lambda^2} = \left. \frac{d\bar{\mathcal{A}}_{\phi^+\phi^0}}{ds} \right|_{s=0} = \left. \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\rm tot}^{\phi^+\phi^0} - \sigma_{\rm tot}^{\phi^+\phi^0} \right) + c_\infty \,, \end{split}$$

$$\begin{array}{c|c} \mathcal{O}_{H} = \frac{1}{2} (\partial_{\mu} |H|^{2})^{2} & \mathcal{O}_{T} = \frac{1}{2} (H^{\dagger} \overrightarrow{D_{\mu}} H)^{2} \\ \mathcal{O}_{H\ell} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overline{\ell}_{L} \gamma^{\mu} \ell_{L} & \\ \mathcal{O}_{H\ell}' = i H^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H \overline{\ell}_{L} \sigma^{a} \gamma^{\mu} \ell_{L} & \mathcal{O}_{He} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overline{e}_{R} \gamma^{\mu} e_{R} \\ \mathcal{O}_{Hq} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overline{q}_{L} \gamma^{\mu} q_{L} & \mathcal{O}_{Hu} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overline{u}_{R} \gamma^{\mu} u_{R} \\ \mathcal{O}_{Hq}' = i H^{\dagger} \sigma^{a} \overrightarrow{D_{\mu}} H \overline{q}_{L} \sigma^{a} \gamma^{\mu} q_{L} & \mathcal{O}_{Hd} = i H^{\dagger} \overrightarrow{D_{\mu}} H \overline{d}_{R} \gamma^{\mu} d_{R} \end{array}$$

scalar-fermion (also the same for leptons)

Fermion-fermion only showing ^{Cege}/_{Λ²} (ē_Rγ_μ e_R) (ē_Rγ^μ e_R), 20 in total for 1 generation

$$-\frac{2c_{ee}}{\Lambda^2} = \left.\frac{d\bar{\mathcal{A}}_{e_R}\overline{e_R}}{ds}\right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\text{tot}}^{e_R}\overline{e_R} - \sigma_{\text{tot}}^{e_R}\right) + c_\infty \,.$$

$$\begin{split} \frac{2(c_{Hq}-c'_{Hq})}{\Lambda^2} &= \left.\frac{d\tilde{\mathcal{A}}_{u_L\,\phi^0}}{ds}\right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\mathrm{tot}}^{u_L\,\phi^0} - \sigma_{\mathrm{tot}}^{u_L\,\phi^{0*}}\right) + c_\infty\,,\\ \frac{2c_{Hu}}{\Lambda^2} &= \left.\frac{d\tilde{\mathcal{A}}_{u_R\,\phi^0}}{ds}\right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\mathrm{tot}}^{u_R\,\phi^0} - \sigma_{\mathrm{tot}}^{u_R\,\phi^{0*}}\right) + c_\infty\,,\\ \frac{2(c_{Hq}+c'_{Hq})}{\Lambda^2} &= \left.\frac{d\tilde{\mathcal{A}}_{d_L\,\phi^0}}{ds}\right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\mathrm{tot}}^{d_L\,\phi^0} - \sigma_{\mathrm{tot}}^{d_R\,\phi^{0*}}\right) + c_\infty\,,\\ \frac{2c_{Hd}}{\Lambda^2} &= \left.\frac{d\tilde{\mathcal{A}}_{d_R\,\phi^0}}{ds}\right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma_{\mathrm{tot}}^{d_R\,\phi^0} - \sigma_{\mathrm{tot}}^{d_R\,\phi^{0*}}\right) + c_\infty\,, \end{split}$$

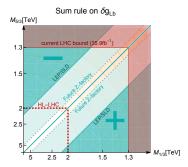
Jiayin Gu (顾嘉荫)

Example: *Zbb* Custodial symmetry

• How the $Zb_L \overline{b}_L$ couplings is related to heavy quarks.

$$\frac{4 \,\delta g_{Lb}}{v^2} = -\frac{2(c_{Hq} + c'_{Hq})}{\Lambda^2} = \left. \frac{d\tilde{\mathcal{A}}_{t_L \phi^-}}{ds} \right|_{s=0} = \int_0^\infty \frac{ds}{\pi s} \left(\sigma^{t_L \phi^- \to F^{-\frac{1}{3}}} - \sigma^{t_L \phi^+ \to F^{\frac{5}{3}}} \right) + c_\infty ,$$

We can impose some symmetry to ensure the cancellation of the two cross section terms. (*Zbb* custodial symmetry, [hep-ph/0605341] Agashe et al.)



Jiayin Gu (顾嘉荫)