

第八届中国LHC物理研讨会

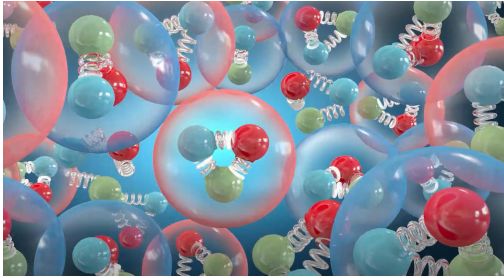
Theory Overview of Heavy Ion Physics

Yifeng Sun

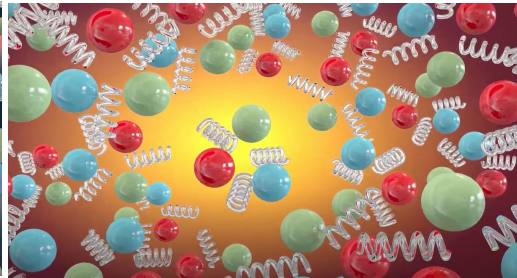
Shanghai Jiao Tong University

2022年11月26日

Why relativistic heavy ion collisions

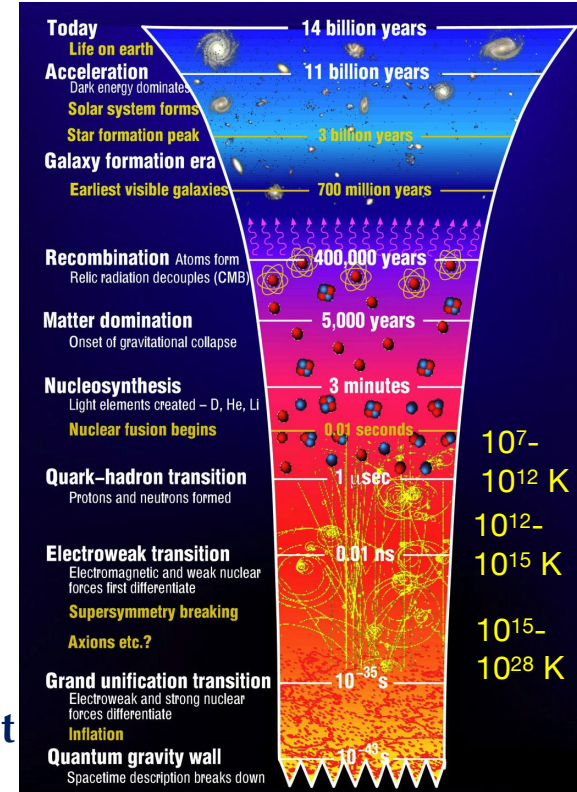


Confined

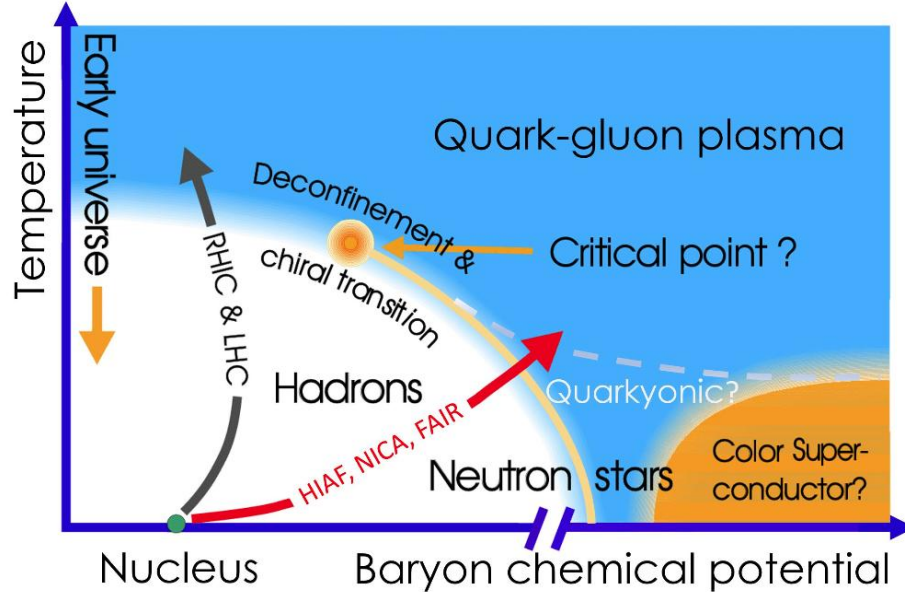


Deconfined

- ❑ Quark confinement vs asymptotic freedom
- ❑ Quark-Gluon Plasma:
 - ✓ phase diagram
 - ✓ chiral symmetry restoration, quark confinement
 - ✓ Topological phase transition

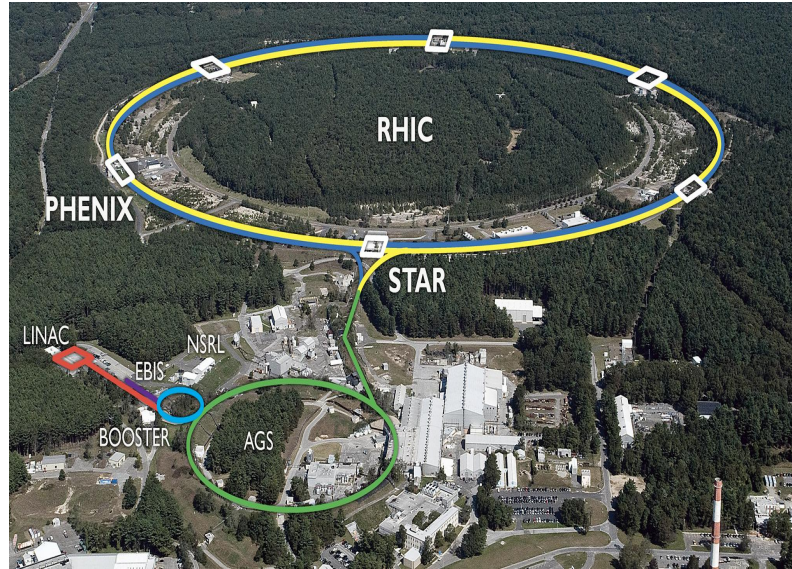


Why relativistic heavy ion collisions



- ❑ Smooth Crossover at high T and low μ_B
- ❑ Is there a **first order phase transition** at low T and high μ_B ?
- ❑ Is there a **critical point**?
- ❑ **Neutron star** can also probe it

Currently Operating facilities



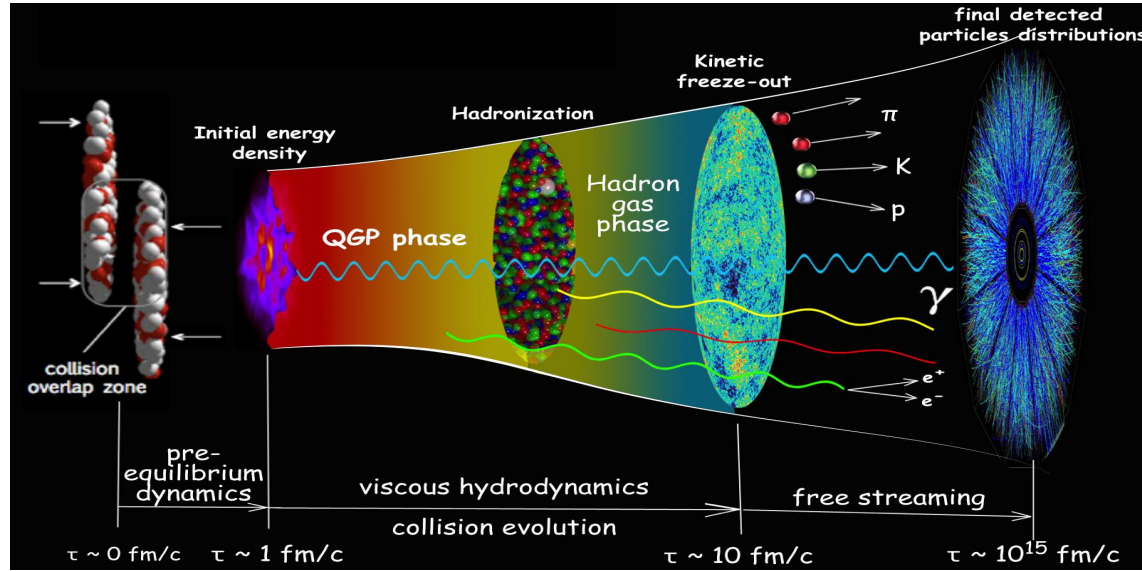
RHIC@BNL, 2000-



LHC@CERN, 2010-

3-200GeV@RHIC, 2.76-5.02TeV@LHC

Little Bangs



- ❑ Initial non-equilibrium+Hydrodynamics+hadronization+hadron gas
- ❑ Design probes and observables to probe these stages

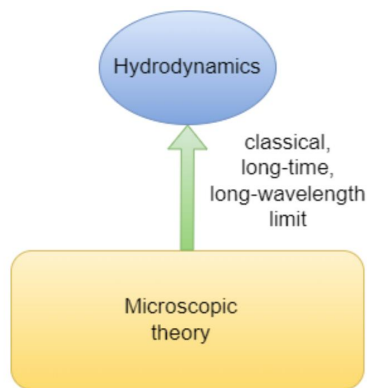
Outline

- ❑ QGP evolution
- ❑ QGP transport coefficient
- ❑ Hadronization
- ❑ QCD phase diagram
- ❑ Spin phenomena

Outline

- ❑ QGP evolution
- ❑ QGP transport coefficient
- ❑ Hadronization
- ❑ QCD phase diagram
- ❑ Spin phenomena

1. Success of visco-hydrodynamics in HICs



- ❑ Low p_T dynamics
- ❑ Long wavelength limit

$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_n)]$$

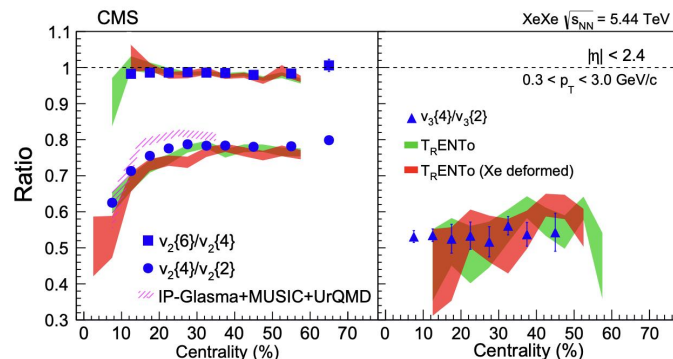
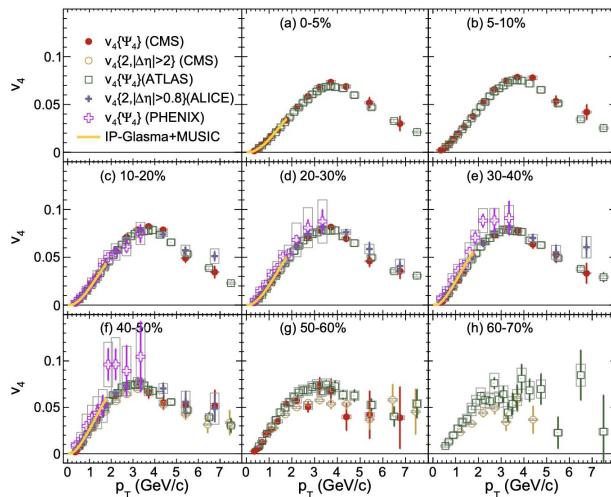
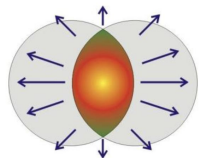
$$\partial_\mu T^{\mu\nu} = 0$$

4 equations
10 unknowns

- Symmetric energy-momentum tensor

$$T^{\mu\nu} = \epsilon u^\mu u^\nu + \Delta^{\mu\nu}(p(\epsilon) + \Pi) + \pi^{\mu\nu}$$

- Local energy density: ϵ
- Flow vector: $T^{\mu\nu} u_\nu = -\epsilon u^\mu$
- Local 3-metric: $\Delta^{\mu\nu} = g^{\mu\nu} + u^\mu u^\nu$ with $g^{\mu\nu} = \text{diag}(-1, 1, 1, 1)$
- Equation of state: $p = p(\epsilon)$
- Bulk pressure: Π
- Shear tensor: $\pi^{\mu\nu} = \pi^{\nu\mu}$, $u_\mu \pi^{\mu\nu} = 0 = \pi_\mu^\mu$
- A symmetric rank-2 tensor has 10 d.o.f. $\Rightarrow \epsilon, \Pi, u^i, \pi^{ij}$



1. Bayesian analysis

- Energy-momentum conservation laws

$$0 = D\epsilon + (\epsilon + p + \Pi)\nabla_\alpha U^\alpha + \pi_\mu^\alpha \sigma_\alpha^\mu$$

$$0 = (\epsilon + p + \Pi)Du_\alpha + c_s^2 \nabla_\alpha \epsilon + \nabla_\alpha \Pi + \Delta_\alpha^\beta \nabla_\mu \pi_\beta^\mu + \pi_\alpha^\mu Du_\mu$$

- Relaxation equations

$$\tau_\Pi D\Pi + \Pi = -\zeta \nabla_\alpha U^\alpha - \delta_{\Pi\Pi} \Pi \nabla_\alpha U^\alpha - \lambda_{\Pi\pi} \pi^{\mu\nu} \sigma_{\mu\nu}$$

$$\tau_\pi \Delta_{\alpha\beta}^{\mu\nu} D\pi^{\alpha\beta} + \pi^{\mu\nu} = -\eta \sigma^{\mu\nu} - \delta_{\pi\pi} \pi^{\mu\nu} \nabla_\alpha U^\alpha - \tau_{\pi\pi} \pi_\alpha^{(\mu} \sigma^{\nu)\alpha} - \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu}$$

Observables

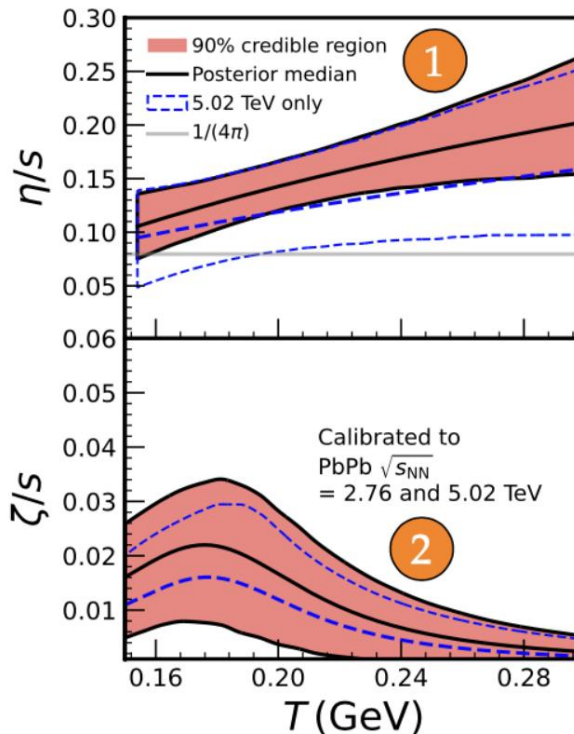
[2] Jyvaskyla (2022)

2.76 TeV

- | | |
|------------------------|--------------------------------------|
| • N_{ch} | • $\text{PID}^1 \langle p_T \rangle$ |
| • $\text{NSC}(3,2),$ | • v_2 to v_4 |
| $\text{NSC}(4,2)$ | • $\chi_{4,22}$ to |
| • $\text{NSC}(2,3,4),$ | $\chi_{6,mk}$ |
| $\text{NSC}(2,3,5)$ | • $\rho_{4,22}$ to |
| | $\rho_{6,mk}$ |

5.02 TeV

- | | |
|------------------------|------------------------------------|
| • PID^2 mult. | • $\text{PID} \langle p_T \rangle$ |
| and N_{ch} | • v_2 to v_7 |
| • $\text{NSC}(3,2)$ | • $\chi_{4,22}$ to |
| to | $\chi_{6,mk}$ |
| $\text{NSC}(4,3)$ | • $\rho_{4,22}$ to |
| | $\rho_{6,mk}$ |



❑ $2.7 \cdot 10^3$ CPU-years for 8 parameters

❑ T dependence of QGP transport coefficient

1. Causality violations in visco-Hydro

Bemfica et al., PRL 2021

- Energy-momentum conservation laws

$$0 = D\epsilon + (\epsilon + p + \Pi)\nabla_\alpha U^\alpha + \pi_\alpha^\mu \sigma_\mu^\alpha$$

$$0 = (\epsilon + p + \Pi)Du_\alpha + c_s^2 \nabla_\alpha \epsilon + \nabla_\alpha \Pi + \Delta_\alpha^\beta \nabla_\mu \pi_\beta^\mu + \pi_\alpha^\mu Du_\mu$$

- Relaxation equations

$$\tau_\Pi D\Pi + \Pi = -\zeta \nabla_\alpha U^\alpha - \delta_{\Pi\Pi} \Pi \nabla_\alpha U^\alpha - \lambda_{\Pi\pi} \pi^{\mu\nu} \sigma_{\mu\nu}$$

$$\tau_\pi \Delta_{\alpha\beta}^{\mu\nu} D\pi^{\alpha\beta} + \pi^{\mu\nu} = -\eta \sigma^{\mu\nu} - \delta_{\pi\pi} \pi^{\mu\nu} \nabla_\alpha U^\alpha - \tau_{\pi\pi} \pi_\alpha^{\mu} \sigma^{\mu\alpha} - \lambda_{\pi\Pi} \Pi \sigma^{\mu\nu}$$

$$(\epsilon + p + \Pi - |\Lambda_1|) - \frac{1}{2\tau_\pi} (2\eta + \lambda_{\pi\Pi} \Pi) - \frac{\tau_{\pi\pi}}{2\tau_\pi} \Lambda_3 \geq 0, \quad (5a)$$

$$(2\eta + \lambda_{\pi\Pi} \Pi) - \tau_{\pi\pi} |\Lambda_1| > 0, \quad (5b)$$

$$\tau_{\pi\pi} \leq 6\delta_{\pi\pi}, \quad (5c)$$

$$\frac{\lambda_{\Pi\pi}}{\tau_\Pi} + c_s^2 - \frac{\tau_{\pi\pi}}{12\tau_\pi} \geq 0, \quad (5d)$$

$$\frac{1}{3\tau_\pi} [4\eta + 2\lambda_{\pi\Pi} \Pi + (3\delta_{\pi\pi} + \tau_{\pi\pi}) \Lambda_3]$$

$$+ \frac{\zeta + \delta_{\Pi\Pi} \Pi + \lambda_{\Pi\pi} \Lambda_3}{\tau_\Pi} + |\Lambda_1| + \Lambda_3 c_s^2$$

$$+ \frac{\frac{12\delta_{\pi\pi} - \tau_{\pi\pi}}{12\tau_\pi} (\frac{\lambda_{\Pi\pi}}{\tau_\Pi} + c_s^2 - \frac{\tau_{\pi\pi}}{12\tau_\pi}) (\Lambda_3 + |\Lambda_1|)^2}{\epsilon + p + \Pi - |\Lambda_1| - \frac{1}{2\tau_\pi} (2\eta + \lambda_{\pi\Pi} \Pi) - \frac{\tau_{\pi\pi}}{2\tau_\pi} \Lambda_3}$$

$$\leq (\epsilon + p + \Pi)(1 - c_s^2), \quad (5e)$$

$$\frac{1}{6\tau_\pi} [2\eta + \lambda_{\pi\Pi} \Pi + (\tau_{\pi\pi} - 6\delta_{\pi\pi}) |\Lambda_1|]$$

$$+ \frac{\zeta + \delta_{\Pi\Pi} \Pi - \lambda_{\Pi\pi} |\Lambda_1|}{\tau_\Pi} + (\epsilon + p + \Pi - |\Lambda_1|) c_s^2 \geq 0, \quad (5f)$$

$$1 \geq \frac{\frac{12\delta_{\pi\pi} - \tau_{\pi\pi}}{12\tau_\pi} (\frac{\lambda_{\Pi\pi}}{\tau_\Pi} + c_s^2 - \frac{\tau_{\pi\pi}}{12\tau_\pi}) (\Lambda_3 + |\Lambda_1|)^2}{[\frac{1}{2\tau_\pi} (2\eta + \lambda_{\pi\Pi} \Pi) - \frac{\tau_{\pi\pi}}{2\tau_\pi} |\Lambda_1|]^2}, \quad (5g)$$

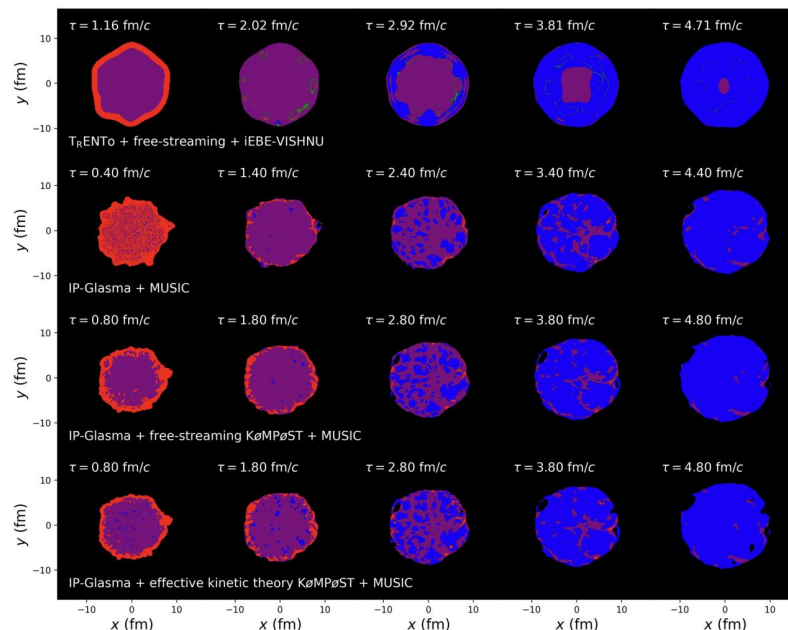
$$\frac{1}{3\tau_\pi} [4\eta + 2\lambda_{\pi\Pi} \Pi - (3\delta_{\pi\pi} + \tau_{\pi\pi}) |\Lambda_1|]$$

$$+ \frac{\zeta + \delta_{\Pi\Pi} \Pi - \lambda_{\Pi\pi} |\Lambda_1|}{\tau_\Pi} + (\epsilon + p + \Pi - |\Lambda_1|) c_s^2$$

$$\geq \frac{(\epsilon + p + \Pi + \Lambda_3)(\epsilon + p + \Pi + \Lambda_3)}{3(\epsilon + p + \Pi - |\Lambda_1|)}$$

$$\times \left\{ 1 + \frac{2[\frac{1}{2\tau_\pi} (2\eta + \lambda_{\pi\Pi} \Pi) + \frac{\tau_{\pi\pi}}{2\tau_\pi} \Lambda_3]}{\epsilon + p + \Pi - |\Lambda_1|} \right\}, \quad (5h)$$

Plumberg et al., PRC 2022



❑ Causality means $v_s^2 < c^2$ (red point means acausal)

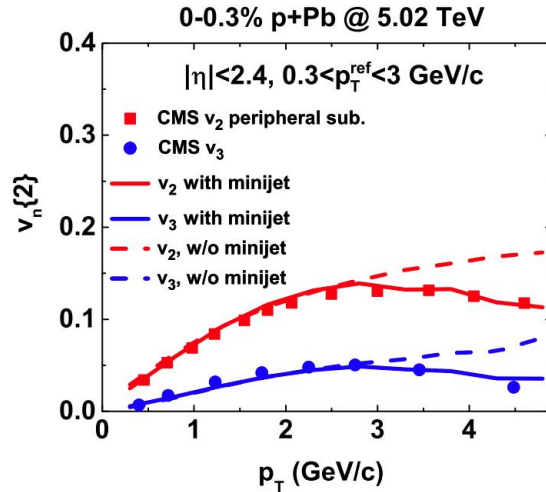
❑ Large violation of causality even in PbPb central collisions

1. Transport theory

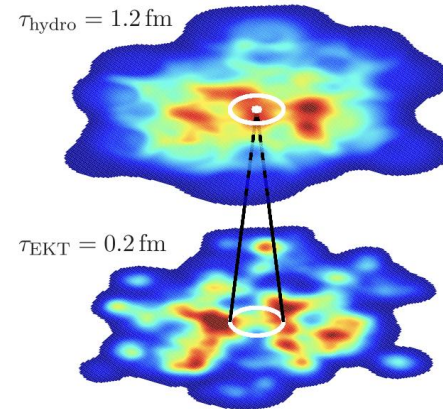
$$p_\mu \partial^\mu f(x, p) + m^* \partial^\mu m^* \partial_{p^\mu} f(x, p) = \mathcal{C}[f]$$

Kurkela et al., PRL 2019

$$\begin{aligned} \partial_\tau f_{\mathbf{x}, \mathbf{p}} + \frac{\mathbf{p}}{|\mathbf{p}|} \cdot \nabla_{\mathbf{x}} f_{\mathbf{x}, \mathbf{p}} - \frac{p^z}{\tau} \partial_{p^z} f_{\mathbf{x}, \mathbf{p}} \\ = -\mathcal{C}_{2 \leftrightarrow 2}[f_{\mathbf{x}, \mathbf{p}}] - \mathcal{C}_{1 \leftrightarrow 2}[f_{\mathbf{x}, \mathbf{p}}]. \end{aligned}$$



Sun et al., EPJC 2020



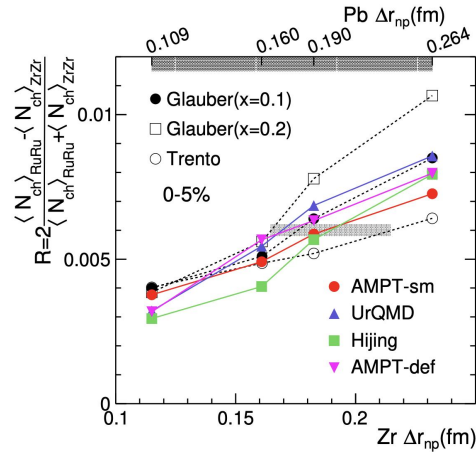
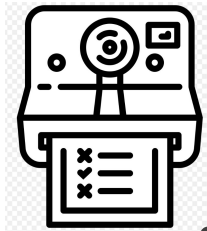
- ❑ Causality **guaranteed**
- ❑ Used also in pre-thermal equilibrium stage
- ❑ **No consistent formulation and no precise prediction**

1. Public available code and applications in nuclear structure

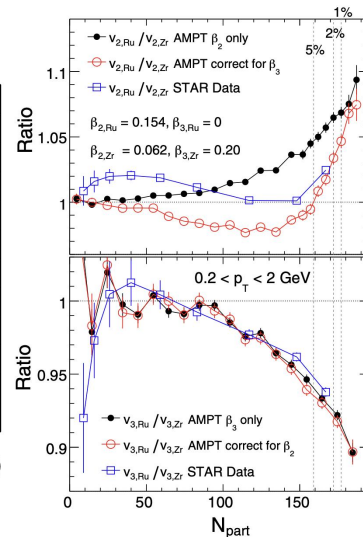
□ Hydro: MUSIC, SONIC, ECHO-QGP, CLVISC, vHLLE, VISHNU

□ Transport: UrQMD, AMPT, SMASH, PHSD, Hijing

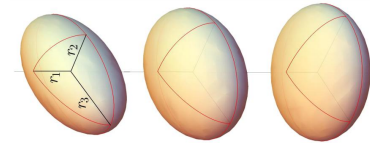
A snapshot of
nucleon distri.



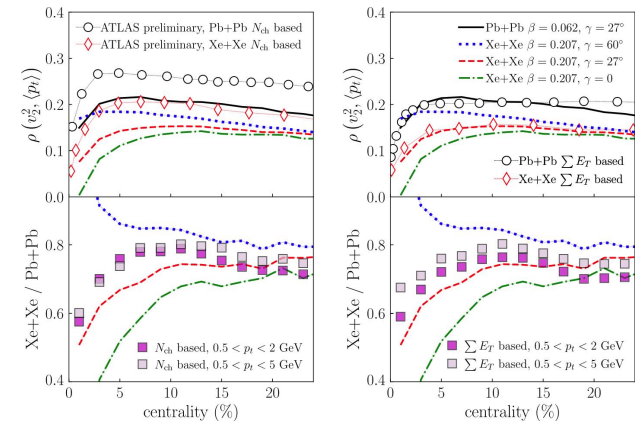
Li et al., PRL 2020



Zhang et al., PRL 2022



Bally et al., PRL 2022



$$\rho(r, \theta, \phi) = \frac{\rho_0}{1 + e^{[r - R(\theta, \phi)]/a}},$$

$$R(\theta, \phi) = R_0(1 + \beta_2 Y_2^0 + \beta_3 Y_3^0 + \beta_4 Y_4^0),$$

$$R(\theta, \varphi) = R_0 \{1 + \beta [\cos \gamma Y_{20}(\theta, \varphi) + \sin \gamma Y_{22}(\theta, \varphi)]\}$$

Outline

- ❑ QGP evolution

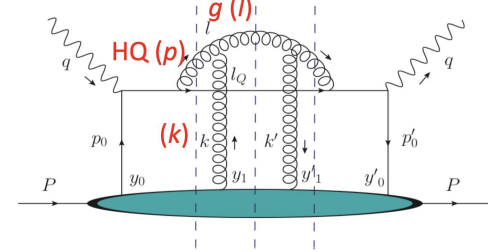
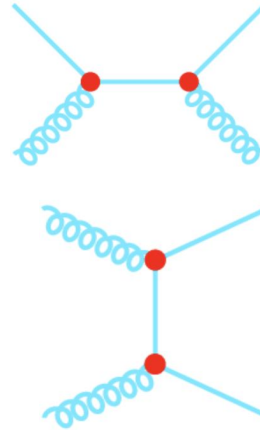
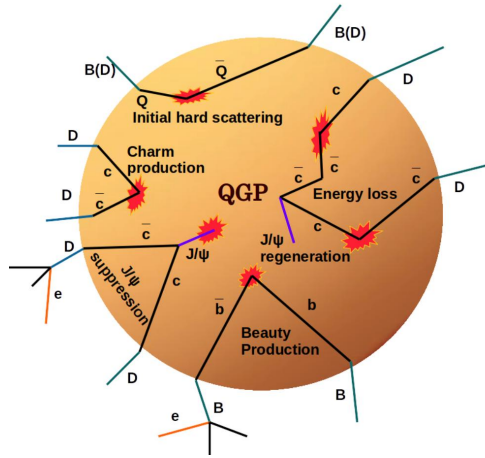
- ❑ QGP transport coefficient

- ❑ Hadronization

- ❑ QCD phase diagram

- ❑ Spin phenomena

2. Heavy quarks and jets and their diffusions



□ Heavy quarks and jets as a probe of QGP

- ✓ clear production (hard scattering)
- ✓ long thermalization time ($\sim \text{fm}/c$)

□ Two dominate processes

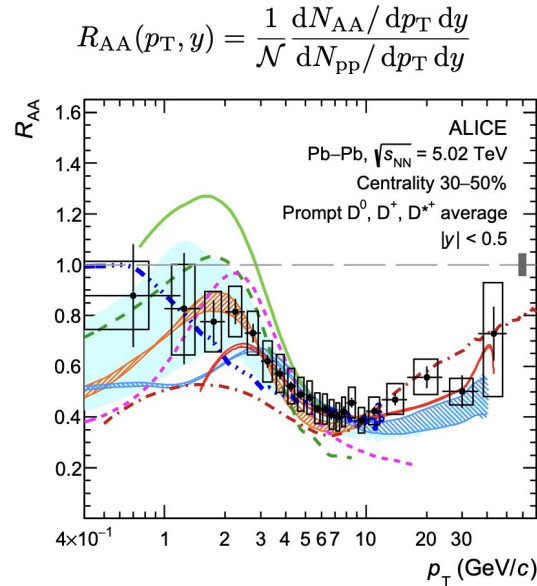
- ✓ elastic parton scattering
- ✓ inelastic gluon emission

2. Transport coefficients

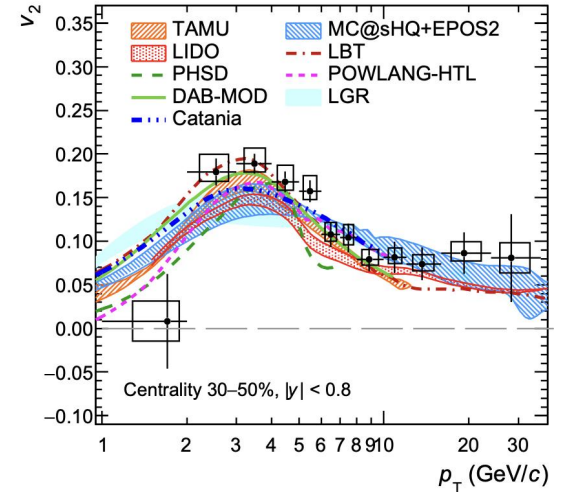
$$p_1 \cdot \partial f_1(x_1, p_1) = E_1(C_{el} + C_{inel})$$

$$D_s = \frac{d(\Delta \vec{x})^2}{dt}$$

$$\hat{q} = \frac{d(\Delta \vec{p}_T)^2}{dt}$$



$$\frac{2\pi}{N} \frac{dN}{d\phi} = 1 + \sum_{n=1}^{\infty} 2v_n \cos[n(\phi - \Psi_n)]$$



ALICE Coll., JHEP 2022

❑ Two transport coefficients (coordinate and momentum)

❑ R_{AA} and V_n probe the interaction strength

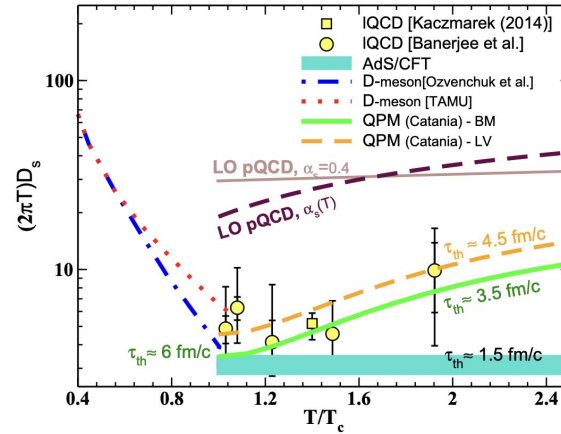
✓ Smaller R_{AA} and larger V_n mean larger interaction strength (larger \hat{q} or smaller D_s)

2. Transport coefficients by far

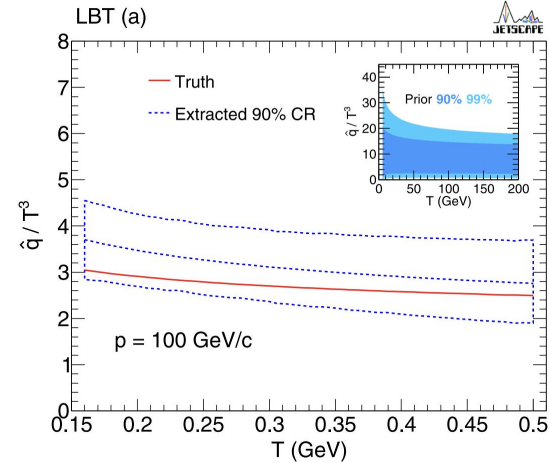
Scardina et al., PRC 2017

$$D_s = \frac{d(\Delta \vec{x})^2}{dt}$$

$$\hat{q} = \frac{d(\Delta \vec{p}_T)^2}{dt}$$



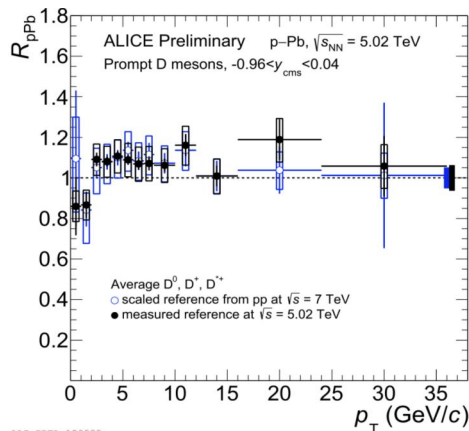
Cao et al., PRC 2021



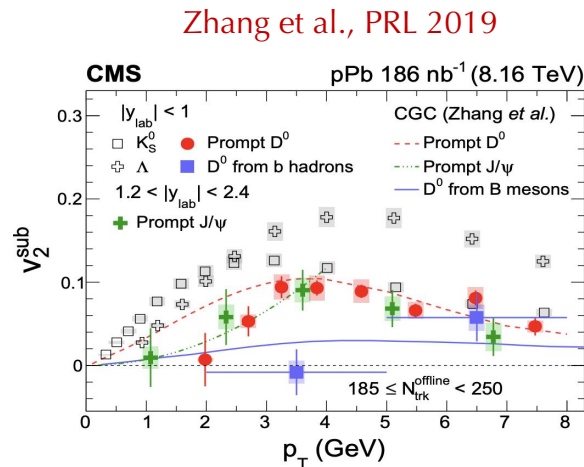
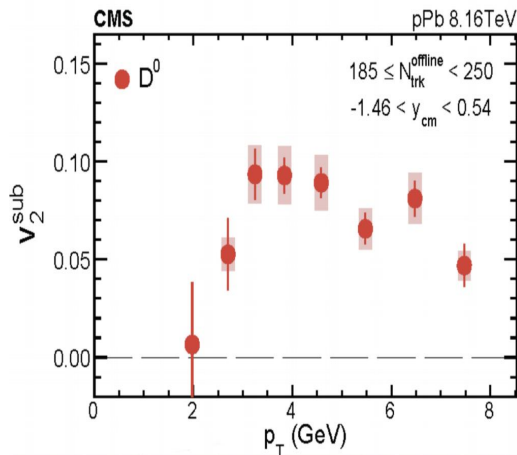
□ qualitative determination of D_s and \hat{q}

See talk by Xing Wenjing
See talk by Mao Yaxian

2. Challenges by small system collisions



ALICE-PREL-150535



Zhang et al., PRL 2019

- ❑ Sizeable v_2 and small R_{pA} suppression. Not explained by QGP interaction
- ❑ The initial states effect by CGC (dense gluon field) can explain R_{pA} and v_2
- ❑ PHENIX sees the R_{pA} suppression of $\psi(2S)$
 - ✓ May be both CGC and QGP? R_{pA} and v_n vs centrality

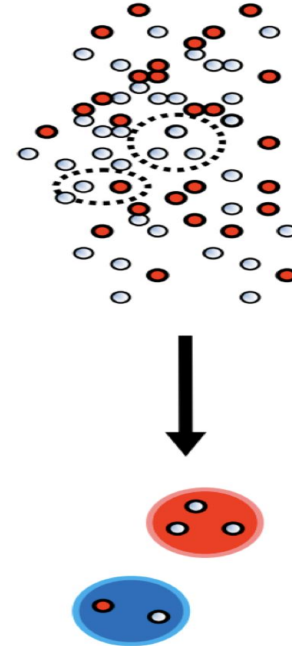
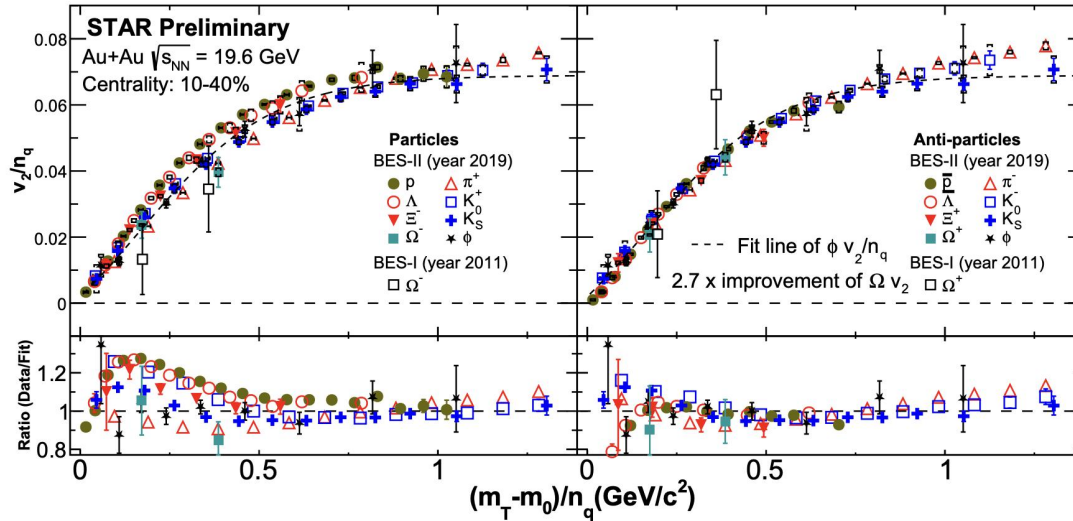
See talk by Wang Jianqiao
See talk by Fu Baochi
See talk by Lu Zhiyong

Outline

- ❑ QGP evolution
- ❑ QGP transport coefficient
- ❑ Hadronization
- ❑ QCD phase diagram
- ❑ Spin phenomena

3. Hadronization of light quark hadron

- ❑ The spectra and v_2 can be described well by statistical mechanics in low p_T and Fragmentation in high p_T
- ❑ NCQ scaling suggests coalescence

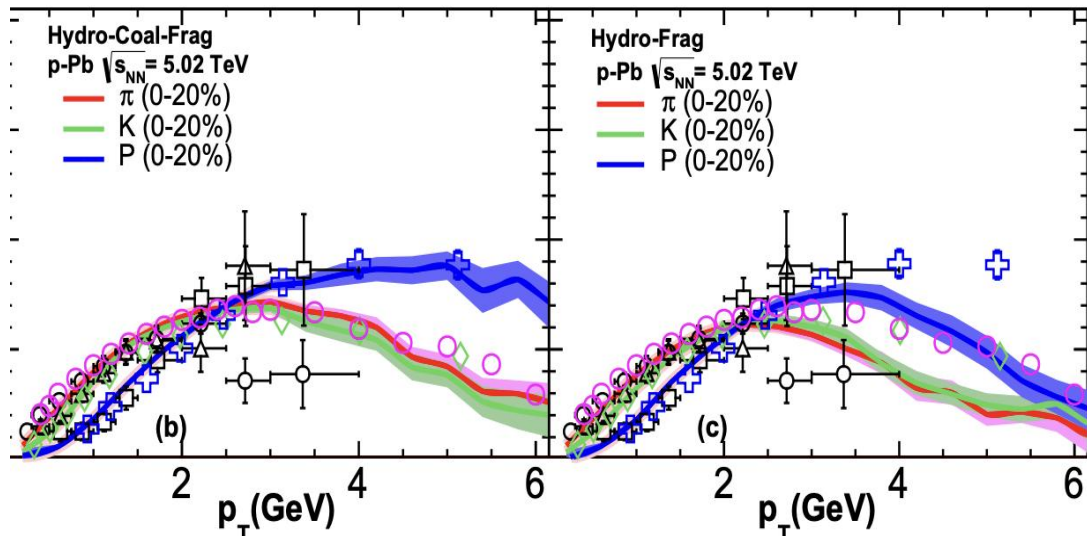
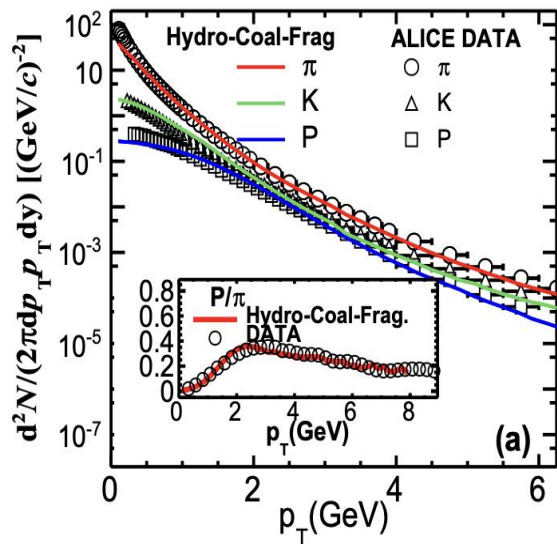


3. Hadronization of light quark hadron

Intermediate p_T data needs coalescence

$$\begin{aligned}\frac{dN_M}{d^3\mathbf{P}_M} &= g_M \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 f_q(\mathbf{x}_1, \mathbf{p}_1) f_q(\mathbf{x}_2, \mathbf{p}_2) \\ &\quad \times W_M(\mathbf{y}, \mathbf{k}) \delta^{(3)}(\mathbf{P}_M - \mathbf{p}_1 - \mathbf{p}_2), \\ \frac{dN_B}{d^3\mathbf{P}_B} &= g_B \int d^3\mathbf{x}_1 d^3\mathbf{p}_1 d^3\mathbf{x}_2 d^3\mathbf{p}_2 d^3\mathbf{x}_3 d^3\mathbf{p}_3 f_{q_1}(\mathbf{x}_1, \mathbf{p}_1) \\ &\quad \times f_{q_2}(\mathbf{x}_2, \mathbf{p}_2) f_{q_3}(\mathbf{x}_3, \mathbf{p}_3) W_B(\mathbf{y}_1, \mathbf{k}_1; \mathbf{y}_2, \mathbf{k}_2) \\ &\quad \times \delta^{(3)}(\mathbf{P}_B - \mathbf{p}_1 - \mathbf{p}_2 - \mathbf{p}_3).\end{aligned}\quad (1)$$

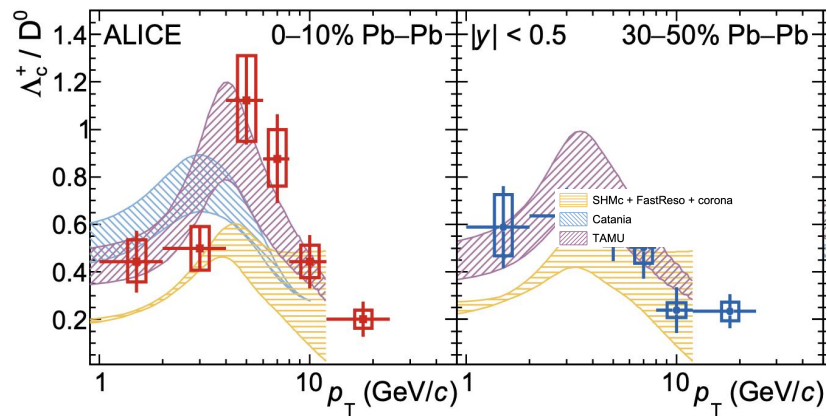
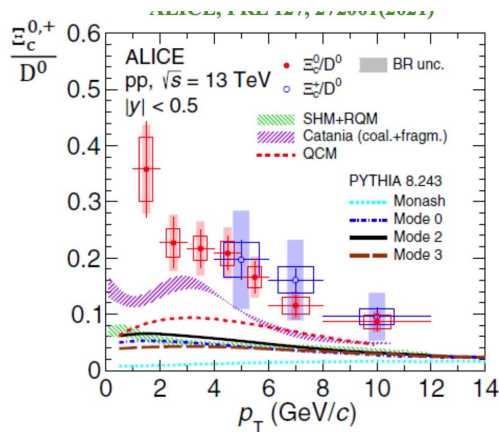
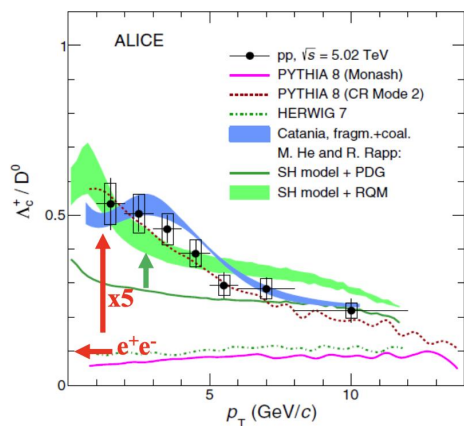
Zhao et al., PRL 2020



3. Hadronization of heavy quark hadron

Fragmentation+coalescence in HF hadrons

- ✓ What is the **formal and consistent** formulation of coalescence
- ✓ Need to understand why coalescence **is a sharp process**



ALICE Coll., PRL 2021

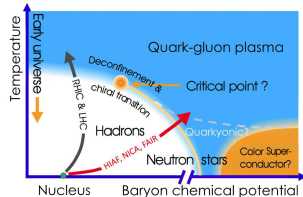
See talk by Zhu Jianhui
See talk by Cheng Tiantian

ALICE Coll., arxiv 2112.08156

Outline

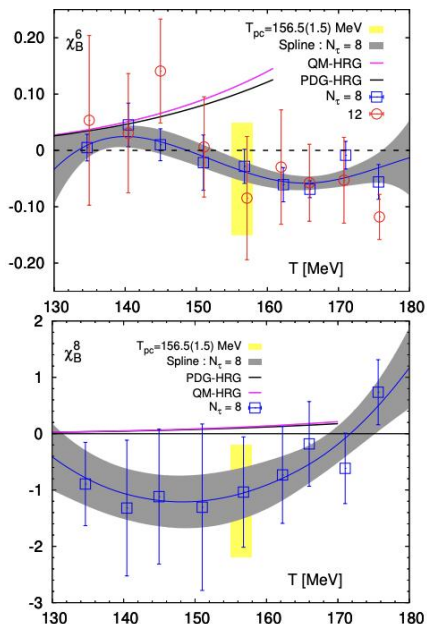
- ❑ QGP evolution
- ❑ QGP transport coefficient
- ❑ Hadronization
- ❑ QCD phase diagram
- ❑ Spin phenomena

4. Efforts at finite μ_B

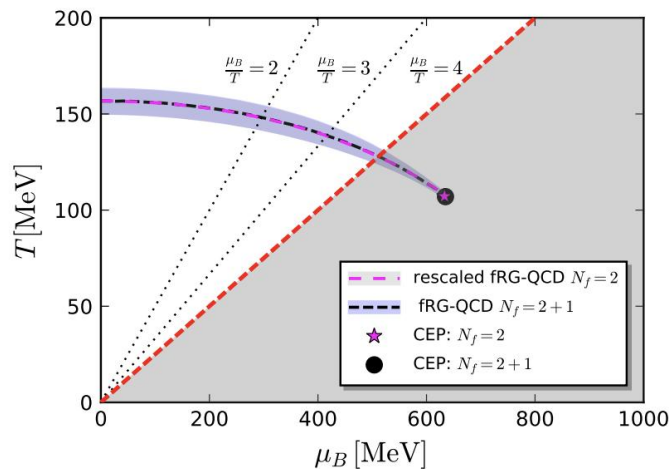


$$\chi_n^X(T, \vec{\mu}) = \frac{1}{VT^3} \frac{\partial^n \ln Z(T, \vec{\mu})}{\partial \hat{\mu}_X^n}$$

HotQCD Coll., PRD 2020



Fu et al., PRD 2021



$$\Gamma_k = \int_x \left\{ Z_{q,k} \bar{q} \left[\gamma_\mu \partial_\mu - \gamma_0 (\mu + ig A_0) \right] q + \frac{1}{2} Z_{\phi,k} (\partial_\mu \phi)^2 + h_k \bar{q} (\tau^0 \sigma + \boldsymbol{\tau} \cdot \boldsymbol{\pi}) q + V_k(\rho, A_0) - c\sigma \right\}, \quad (1)$$

- ❑ LQCD calculation of higher moments
- ❑ QCD assisted effective theory with fRG can reproduce well LQCD result
- ❑ Still problems At $\mu_B/T > 4$

4. Dynamical phase transition theory-Hydro

$$\begin{aligned} D\phi_Q &= -\Gamma_Q (\phi_Q - \bar{\phi}_0) \\ \partial_\mu T^{\mu\nu} &= 0 \end{aligned}$$

$$\begin{aligned} \phi_Q(x) &\sim \int_{\Delta x} \left\langle \delta \frac{s}{n}(t, x + \frac{1}{2}\Delta x) \delta \frac{s}{n}(t, x - \frac{1}{2}\Delta x) \right\rangle e^{iQ \cdot \Delta x} \\ T^{\mu\nu} &= e u^\mu u^\nu - p_{(+)} \Delta^{\mu\nu} + \pi^{\mu\nu} \\ p_{(+)}(e, n) &= p(e, n) + \Delta p(e, n, \phi(e, n)) \\ \Delta p &= [-(e+p)\Delta\beta + n\Delta\alpha + \Delta s] / \beta_{(+)} \\ \Delta s(e, n, \phi) &\equiv \int dQ \Delta s_Q \\ &= \int dQ \frac{Q^2}{(2\pi)^2} \left[\log \frac{\phi_Q}{\bar{\phi}_Q(e, n)} - \frac{\phi_Q}{\bar{\phi}_Q(e, n)} + 1 \right] \\ \Delta\beta &= \int dQ \frac{Q^2}{(2\pi)^2} \frac{\phi_Q - \bar{\phi}_Q}{(\bar{\phi}_Q)^2} \left(\frac{\partial \bar{\phi}_Q}{\partial e} \right)_n, \\ \Delta\alpha &= - \int dQ \frac{Q^2}{(2\pi)^2} \frac{\phi_Q - \bar{\phi}_Q}{(\bar{\phi}_Q)^2} \left(\frac{\partial \bar{\phi}_Q}{\partial n} \right)_e \end{aligned}$$

Stephanov et al., JHEP 2018

$$\partial_t n_B(\mathbf{x}, t) = \Gamma \nabla^2 (\mathcal{F}'[n_B]) + \nabla \cdot \mathbf{J}(\mathbf{x}, t)$$

$$\begin{aligned} \mathbf{J}(\mathbf{x}, t) &= \sqrt{2T\Gamma} \boldsymbol{\zeta}(\mathbf{x}, t) \\ \langle \zeta_i(\mathbf{x}, t) \zeta_j(\mathbf{x}', t') \rangle &= \delta(\mathbf{x} - \mathbf{x}') \delta(t - t') \delta_{ij} \\ \mathcal{F}[n_B] &= T \int d^3x \left(\frac{m^2}{2n_c^2} (\Delta n_B)^2 + \frac{K}{2n_c^2} (\nabla n_B)^2 \right. \\ &\quad \left. + \frac{\lambda_3}{3n_c^3} (\Delta n_B)^3 + \frac{\lambda_4}{4n_c^4} (\Delta n_B)^4 + \frac{\lambda_6}{6n_c^6} (\Delta n_B)^6 \right) \end{aligned}$$

Nahrgang et al., PRD 2019

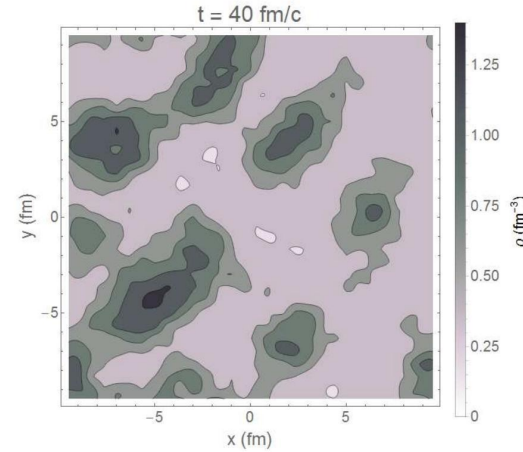
❑ Deterministic method (Hydro+) vs Stochastic method

❑ How to apply first order phase transition?

4. Dynamical phase transition theory-Transport

$$\begin{aligned} & \partial_{X^0} f_a(X, \mathbf{p}) + \frac{p^{i\pm}}{E_{\mathbf{p}^\pm}} \partial_{X^i} f_a(X, \mathbf{p}) \\ & - \partial_{X^i} V_a^S(X) \frac{M_a}{E_{\mathbf{p}^\pm}} \partial_{p_i} f_a(X, \mathbf{p}) \mp \partial_{X^i} V_0^V(X) \partial_{p_i} f_a(X, \mathbf{p}) \\ & \mp \partial_{X^i} V_j^V(X) \frac{p^{j\pm}}{E_{\mathbf{p}^\pm}} \partial_{p_i} f_a(X, \mathbf{p}) = \mathcal{C}[f_a], \end{aligned} \quad (4)$$

$$\begin{aligned} \mathcal{L}_{NJL}^S = & \bar{q}(i \not{\partial} - m_0)q + \frac{G_S}{2} \sum_{a=0}^8 \left[(\bar{q} \lambda^a q)^2 + (\bar{q} i \gamma_5 \lambda^a q)^2 \right] \\ & - K \left[\det_f \left(\bar{q} (1 + \gamma_5) q \right) + \det_f \left(\bar{q} (1 - \gamma_5) q \right) \right], \end{aligned} \quad (1)$$



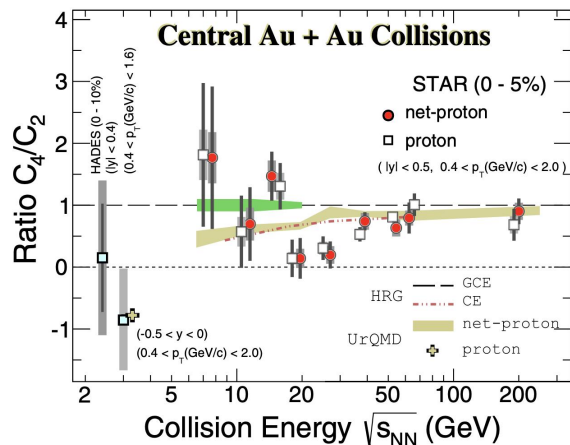
Li et al., PRC 2017

❑ Dynamical generation of first order phase transition

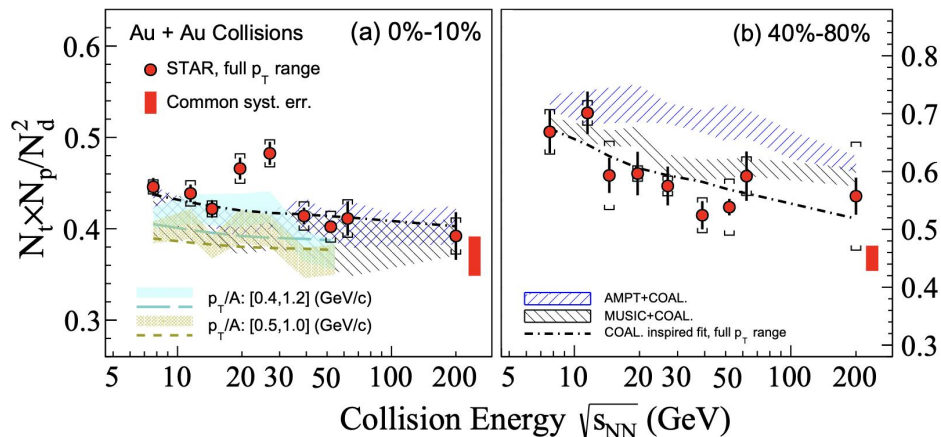
❑ More reliable effective theory? How to include second order phase transition?

4. Comparison with experiments

STAR Coll, PRL 2022



STAR Coll, arXiv 2209.08058



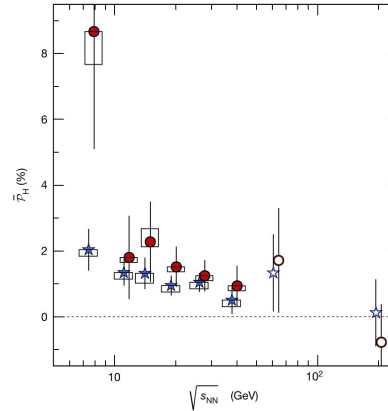
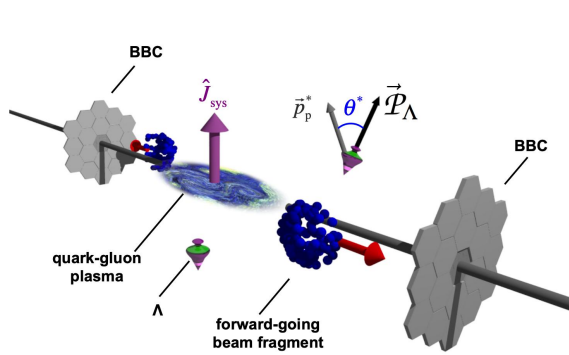
❑ Nonmonotonic variation

✓ need theoretical input

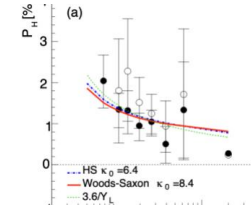
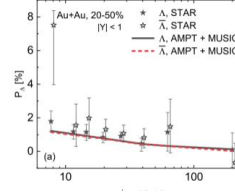
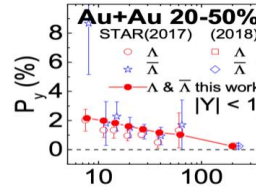
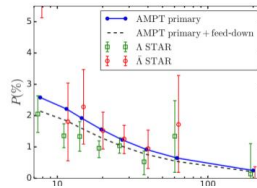
Outline

- ❑ QGP evolution
- ❑ QGP transport coefficient
- ❑ Hadronization
- ❑ QCD phase diagram
- ❑ Spin phenomena

5. Spin phenomena in HICs

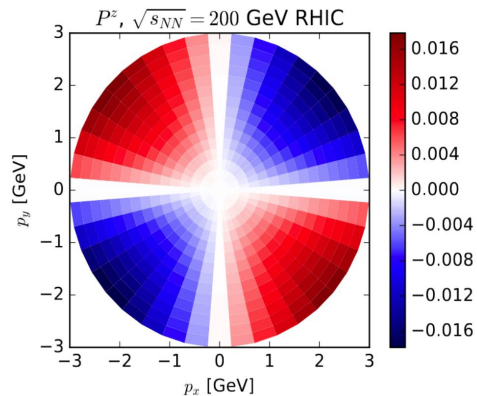


STAR Coll, Nature 2017

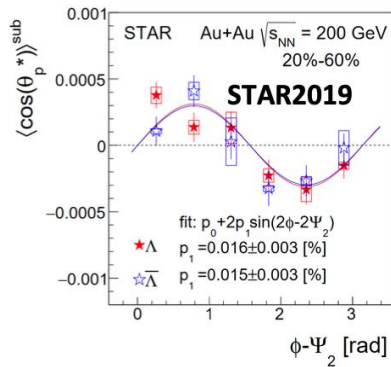


- Highly rotating QGP with rotation speed 10^{22} s^{-1}
- Good agreement between experiments and theories using statistical method on global spin polarization

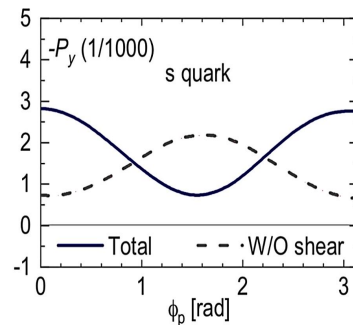
5. Angular dependence of longitudinal spin polarization



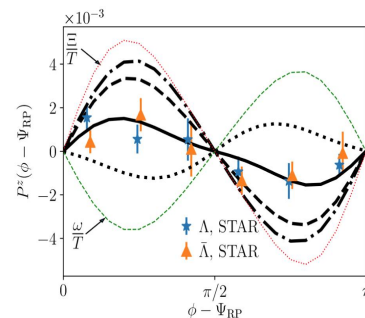
Becattini et al., PRL 2018



STAR Coll., PRL 2019



Fu et al., PRL 2021



Becattini et al., PRL 2021

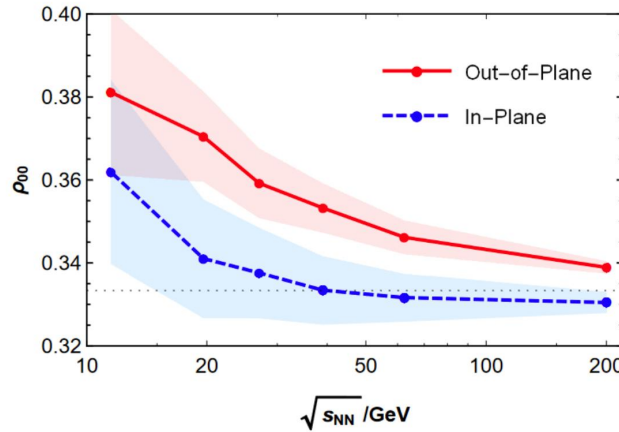
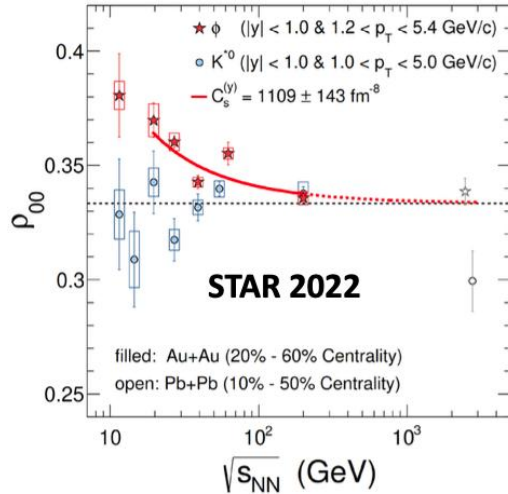
$$\varpi_{\rho\sigma} = \frac{1}{2}(\partial_\sigma\beta_\rho - \partial_\rho\beta_\sigma), \quad \xi_{\rho\sigma} = \frac{1}{2}(\partial_\sigma\beta_\rho + \partial_\rho\beta_\sigma)$$

- ❑ Thermal vorticity can not reproduce experimental data
- ❑ Thermal shear can but a non-global thermal equilibrium effect
- ✓ need spin transport theory

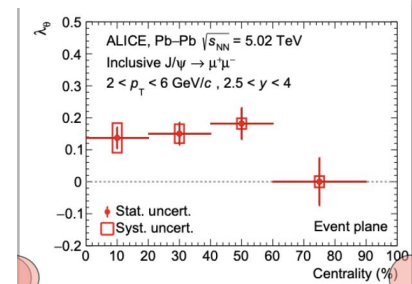
5. Vector meson spin alignment

$$\frac{dN}{d(\cos\theta^*)} = N_0 \times [(1 - \rho_{00}) + (3\rho_{00} - 1) \cos^2\theta^*]$$

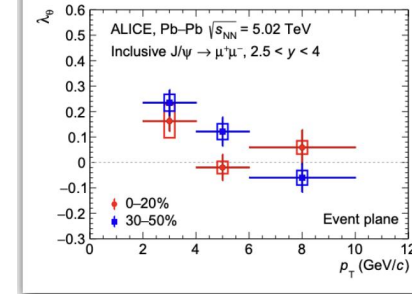
$$W(\theta) \propto \frac{1}{3 + \lambda_\theta} (1 + \lambda_\theta \cos^2\theta) \quad \lambda_\theta \propto (3\rho_{00} - 1)/(1 - \rho_{00})$$



Sheng et al., arXiv 2205.15689



ALICE Coll., arXiv 2204.10171



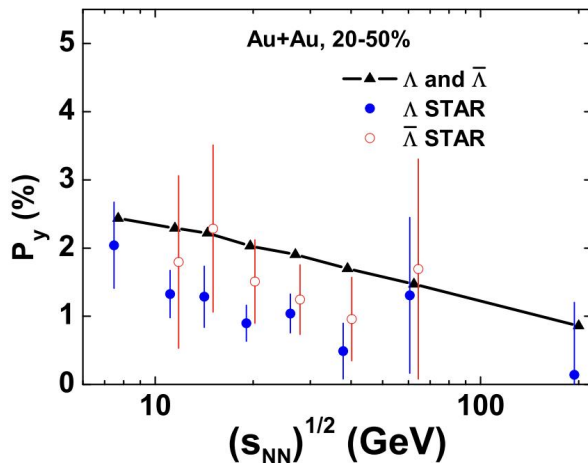
❑ Vector meson spin alignment can not be described by vorticity

❑ ϕ field may explain it

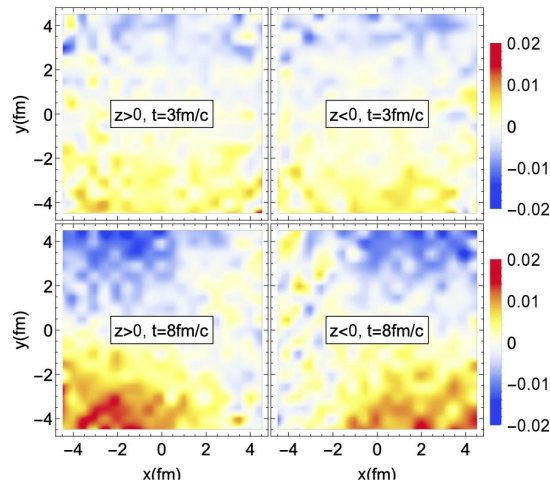
- ✓ need to calculate ϕ field theoretically
- ✓ need to understand charm meson spin

See talk by Bai Xiaozhi

5. Transport theory



Sun et al., PRC 2017



Liu et al., PRL 2020

❑ Chiral kinetic theory can describe well global and local spin polarization

- ✓ fully dynamic
- ✓ need to develop to include finite mass

Summary

❑ There are many materials that I do not cover

- ✓ anomalous phenomena, exotic particles in HICs, UPC, HQ diffusion in

Glamsa, quarkonia production, neutron star.....

See talk by Wu Wenya
See talk by Li Tianqi

❑ Much achievements and more problems

- ✓ hydro valid range, small systems, $\mu_B/T > 4$, pseudogauge dependence with spin, other spin puzzle

Thank you for your attentions!