

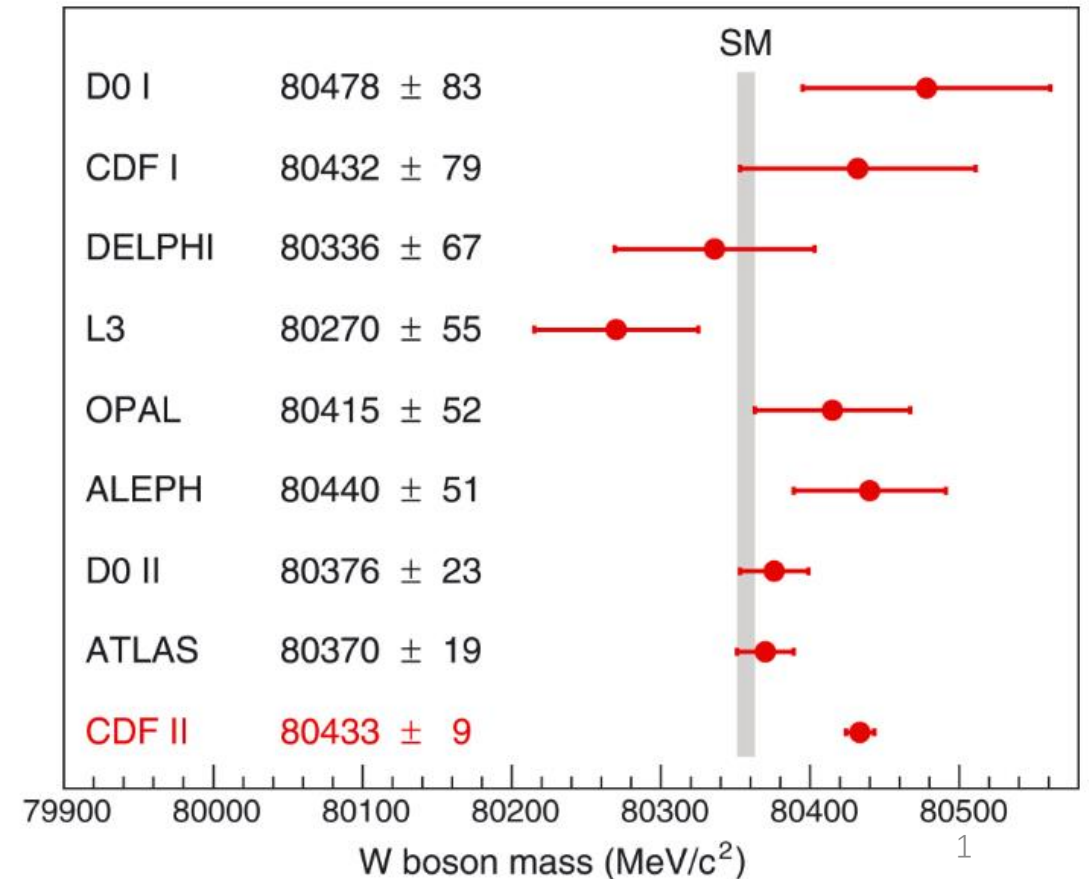
W-Boson Mass, Electroweak Precision Tests and SMEFT

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Based on arXiv: [2204.04805](https://arxiv.org/abs/2204.04805),

with JiJi Fan, Tao Liu and Kun-Feng Lyu

W mass discussion
Tuesday, April 26, 2022



In total six Dim-6 SMEFT operators that are “self-contained”:
restrictions power comes from EWPO (except O_{WB}):

$$O_{WB} \approx 1/3 S$$

$$O_{WB} = gg' H^\dagger \sigma^a H W_{\mu\nu}^a B^{\mu\nu},$$

$$O_{T_1} \approx 1/8 T$$

$$O_T = \frac{1}{2} (H^\dagger \overleftrightarrow{D}_\mu H)^2,$$

$$\mathcal{O}_L^{(3)l} = (iH^\dagger \sigma^a \overleftrightarrow{D}_\mu H) (\bar{L}_L \gamma^\mu \sigma^a L_L),$$

$$\mathcal{O}_{LL}^{(3)l} = (\bar{L}_L \gamma_\mu \sigma^a L_L) (\bar{L}_L \gamma^\mu \sigma^a L_L),$$

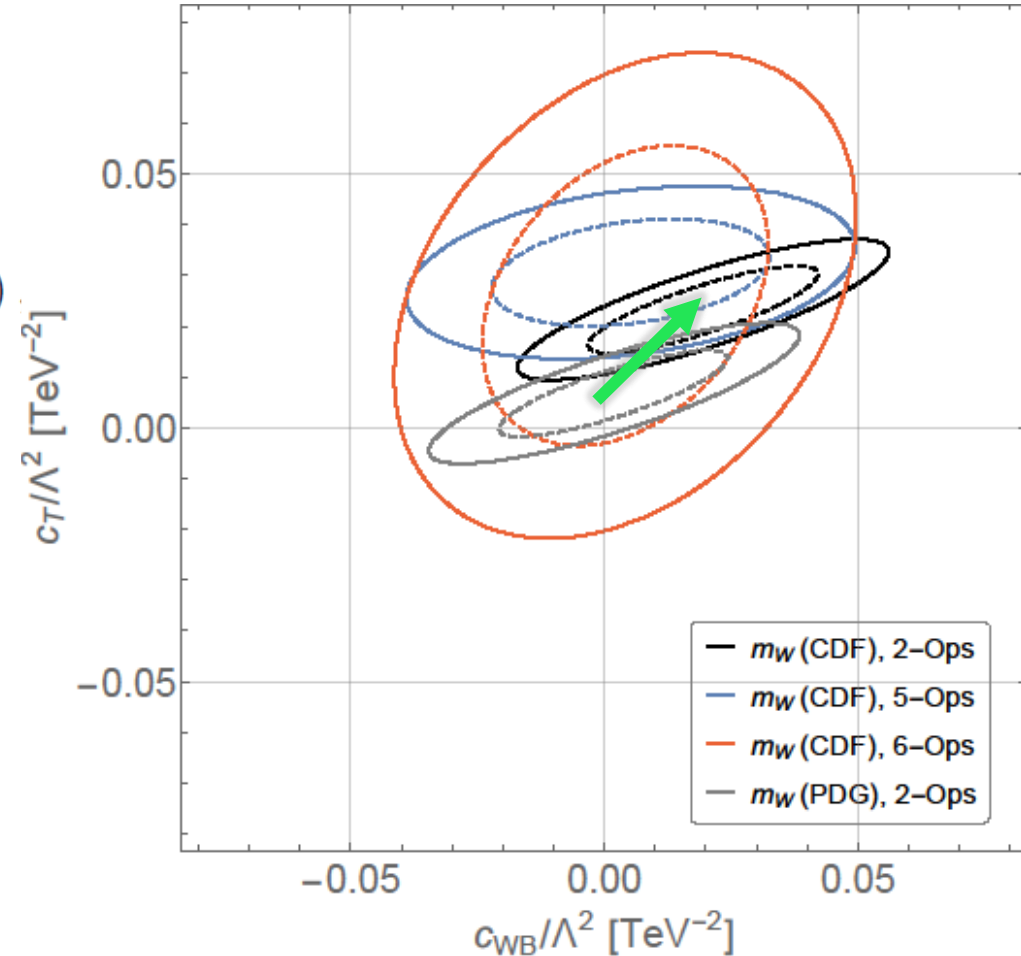
$$\mathcal{O}_L^l = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{L}_L \gamma^\mu L_L),$$

$$\mathcal{O}_R^e = (iH^\dagger \overleftrightarrow{D}_\mu H) (\bar{l}_R \gamma^\mu l_R).$$

Fit with basic EWPO constraints with a
theoretical W mass: 80354 ± 6 MeV:

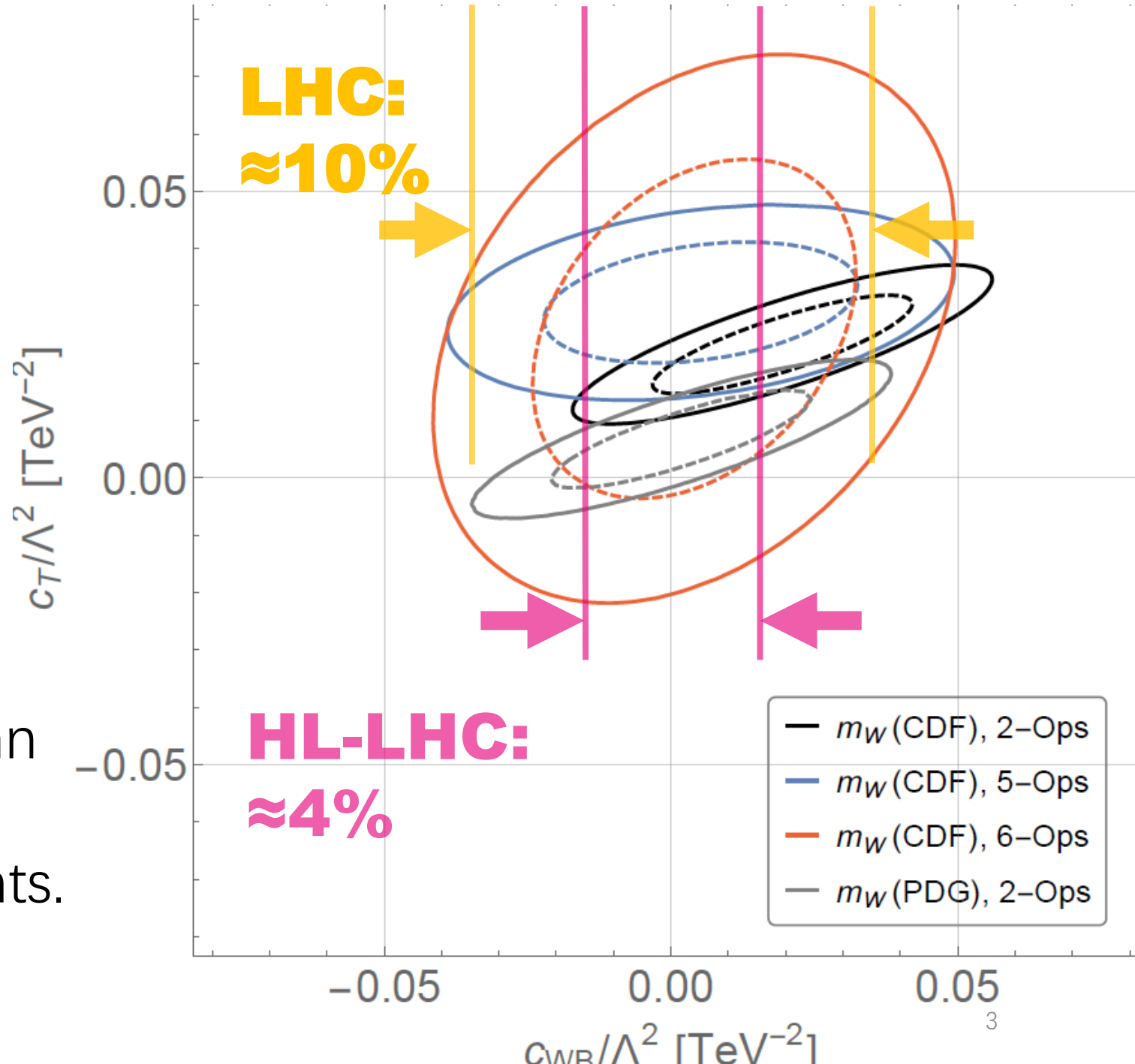
$$R_b = \frac{\Gamma_b}{\Gamma_{\text{had}}}, \quad R_\ell = \frac{\Gamma_{\text{had}}}{\Gamma_\ell}, \quad A_f, \quad A_{FB}^f = \frac{3}{4} A_e A_f \quad (f = b, \ell),$$

$$\sin^2 \theta_{\text{eff}}^{\text{lep}} = \frac{1}{4} \left(1 - \frac{g_V^l}{g_A^l} \right), \quad \Gamma_Z, \quad \sigma_{\text{had}}^0 = \frac{12\pi}{m_Z^2} \frac{\Gamma_e \Gamma_{\text{had}}}{\Gamma_Z^2}, \quad \Gamma_W, \quad \text{BR}_{W \rightarrow \text{had}}$$



Also include the Higgs to $\gamma\gamma$ signal strength: $\mu_{ggh}^{\gamma\gamma}/\mu_{SM}$ to constrain O_{WB}

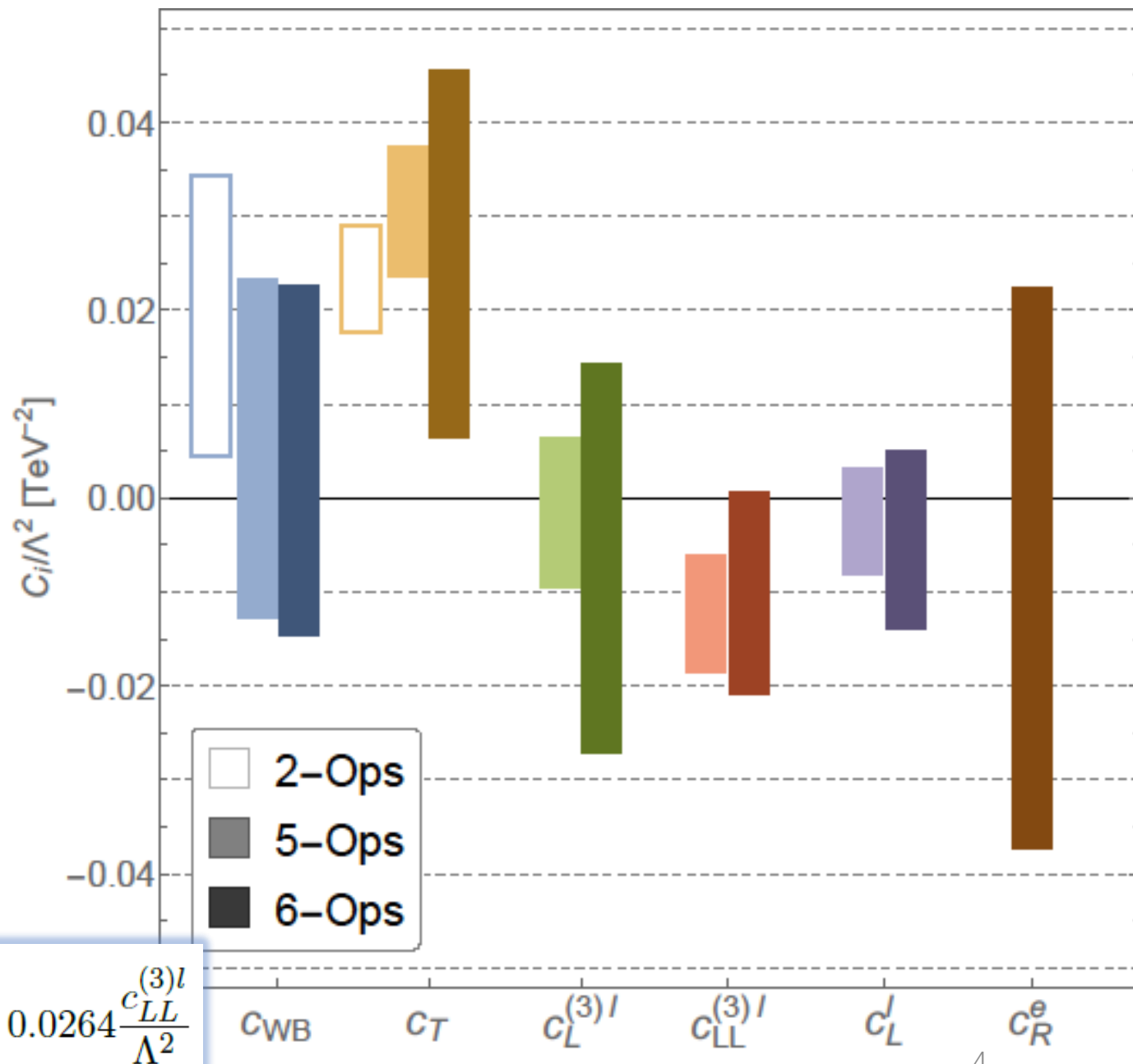
Other Higgs signal strengths, especially $Z\gamma$, ZZ , and WW can further help pinning O_{WB} and O_T , but with weaker constraints.



Three different scenarios are considered:

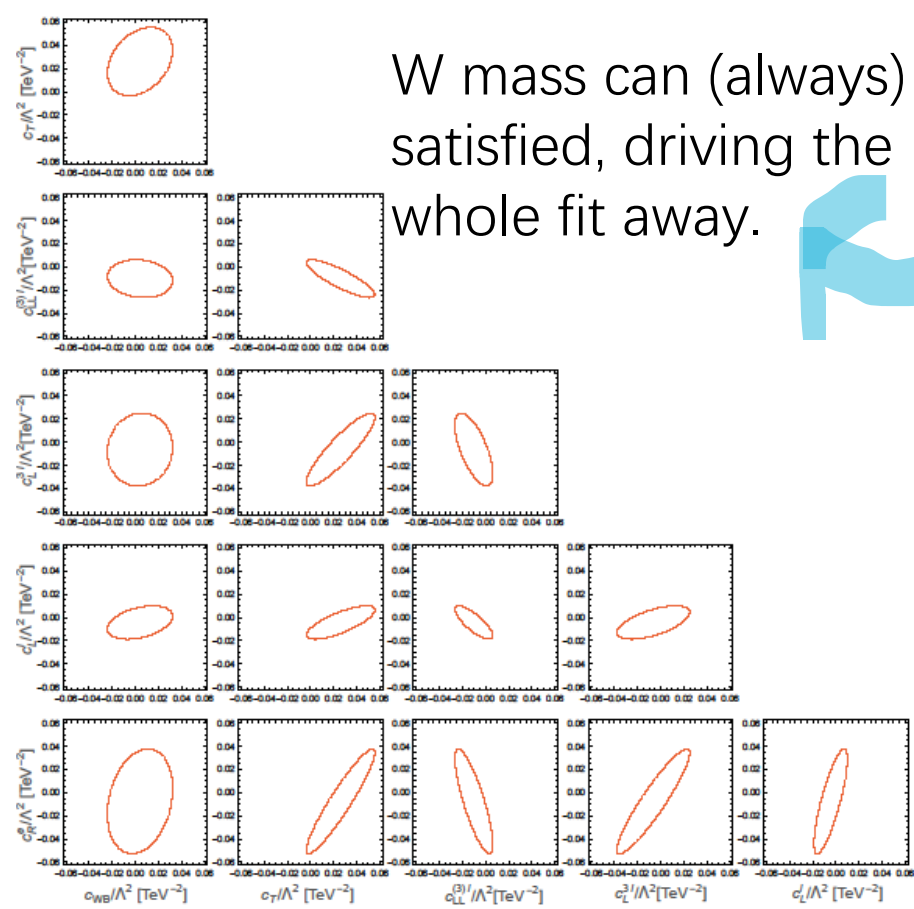
1. Only \mathcal{O}_{WB} and \mathcal{O}_T operators are turned on, corresponding to an S-T fit.
2. Five operators (except \mathcal{O}_R^e) are turned on.
3. All six operators are turned on.

$c_T(\text{TeV}/\Lambda)^2 \gtrsim 0.01$ in all scenarios



$$\frac{\Delta m_W}{m_W} = -0.0111 \frac{c_{WB}}{\Lambda^2} + 0.0433 \frac{c_T}{\Lambda^2} - 0.0264 \frac{c_L^{(3)l}}{\Lambda^2} + 0.0264 \frac{c_{LL}^{(3)l}}{\Lambda^2}$$

W mass can (always) be satisfied, driving the whole fit away.



W width is also larger, coincide with the CDF W mass if $\Gamma_W \propto m_W^3$

The fit quality doesn't improve by including more operators.

Observables	Case (1)	Case (2)	Case (3)	Experimental Measurement
m_W (GeV)	80.4182	80.4335	80.4335	80.4335 ± 0.0094 [21]
A_b	0.934895	0.93481	0.934944	0.923 ± 0.020 [5, 19]
A_ℓ (P_τ)	0.14889	0.14744	0.14736	0.1465 ± 0.0033 [5, 19]
A_ℓ (SLD)	0.14889	0.14744	0.14736	0.1513 ± 0.0021 [5, 19]
R_b	0.21587	0.21588	0.21587	0.21629 ± 0.00066 [5, 19]
R_ℓ	20.7510	20.7592	20.7634	20.767 ± 0.025 [5, 19]
A_{FB}^b	0.10448	0.10340	0.10335	0.0996 ± 0.0016 [5, 19]
A_{FB}^ℓ	0.01657	0.01629	0.01627	0.0171 ± 0.0010 [5, 19]
Γ_Z (GeV)	2.49818	2.49515	2.49537	2.4955 ± 0.0023 [5]
σ_{had}^0 (nb)	41.4915	41.4729	41.4771	41.480 ± 0.033 [22]
Γ_W (GeV)	2.09262	2.09109	2.09261	2.085 ± 0.042 [5]
$\text{BR}_{W \rightarrow \text{had}}$	0.6748	0.6748	0.6749	0.6741 ± 0.0021 [5]
$\sin^2 \theta_{\text{eff}}^{\text{lep}} (10^{-5})$	23127.7	23146.6	23147.7	(23143 ± 25) [6]
$\mu_{\text{ggh}}^{\gamma\gamma} / \mu_{\text{SM}}$	1.11	1.03	1.02	1.02 ± 0.11 [23]
$\chi^2/\text{D.O.F}$	1.38	1.20	1.34	

Implications of New Physics

A hypercharge-free triplet (Σ) with $SU(3) \times SU(2) \times U(1) = (1,3,0)$:

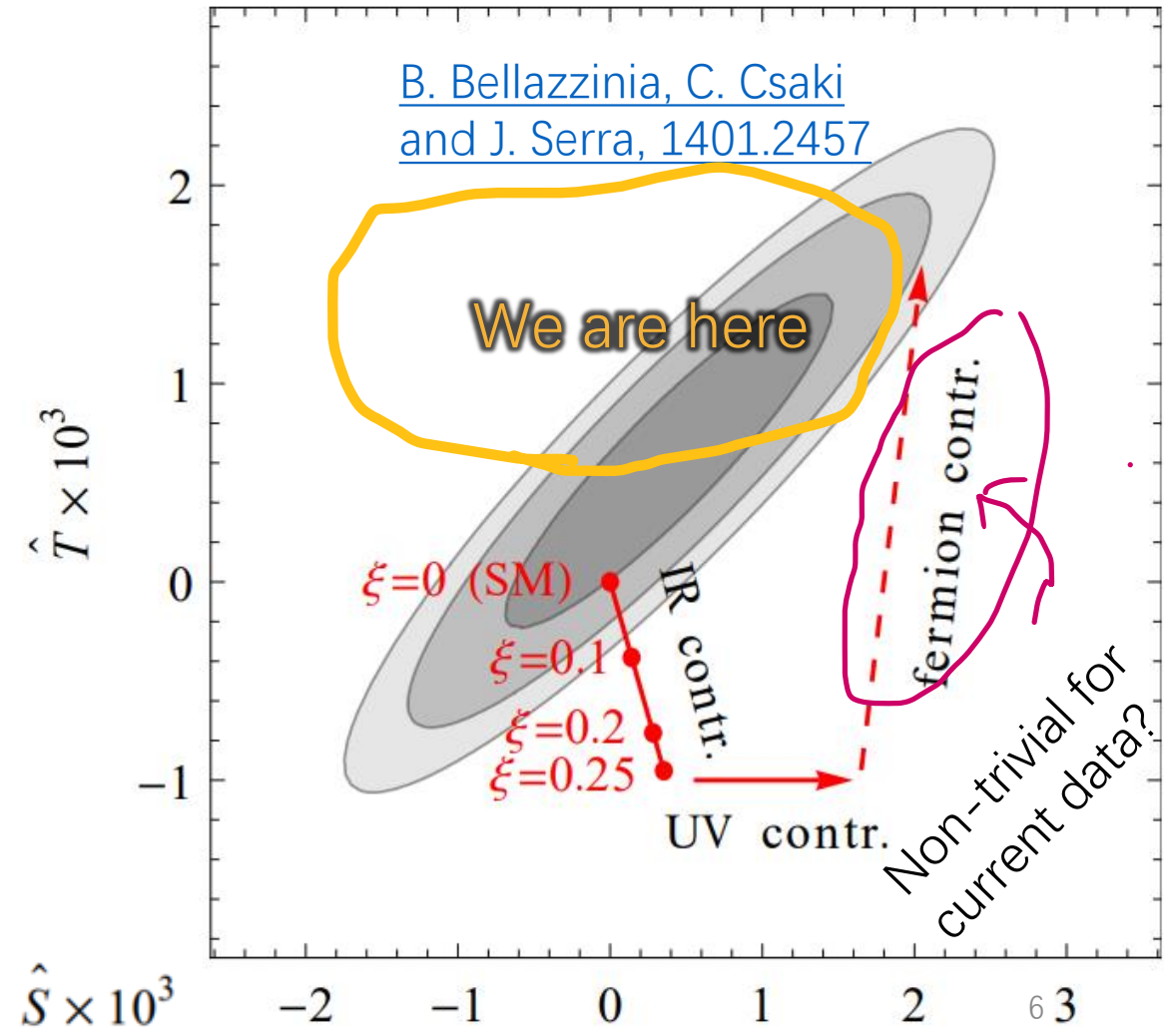
$$\mathcal{L} \supset -\lambda H^\dagger \Sigma H - \frac{\lambda_3}{2} (H^\dagger H) \Sigma \Sigma, \Rightarrow T \simeq \frac{1}{\alpha} \frac{2 \langle \Sigma \rangle^2}{v^2}$$

Found in many references, see e.g:

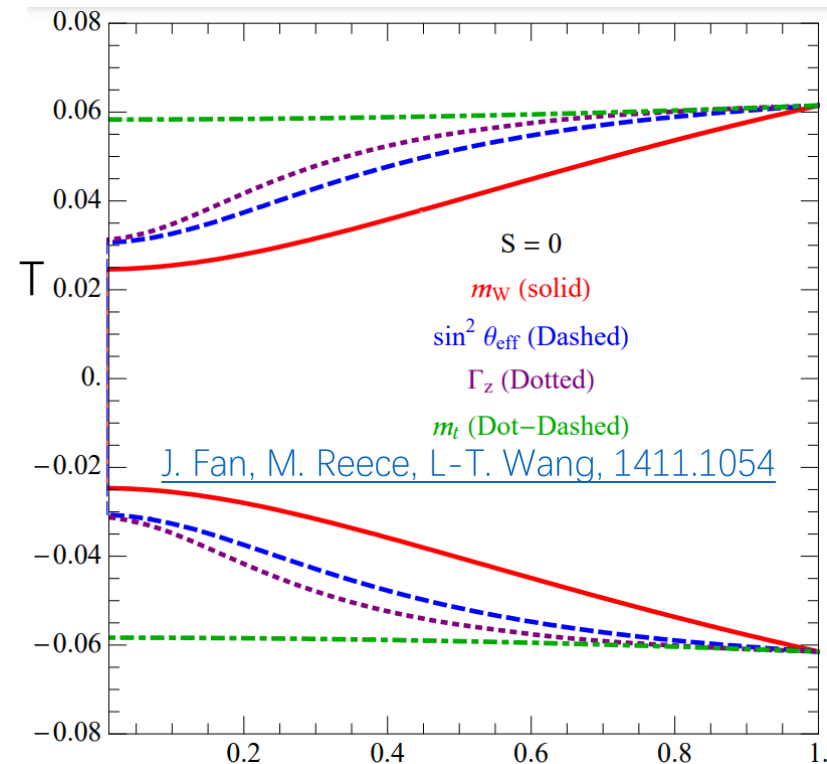
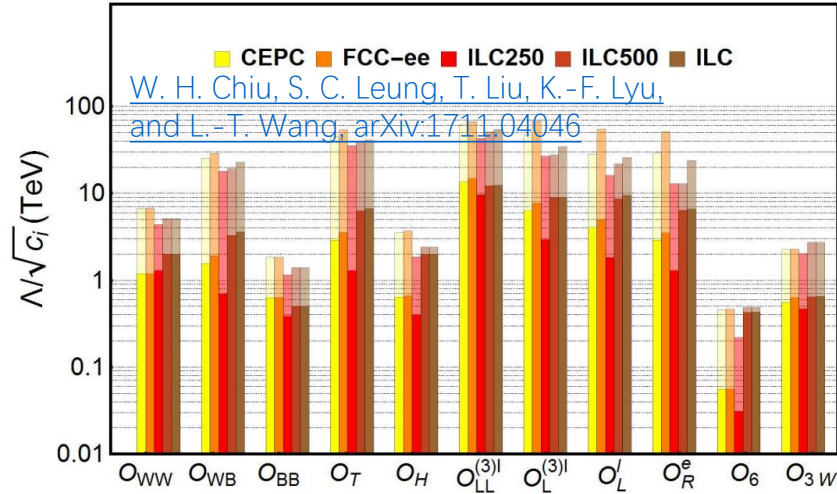
[Z. U. Khandker, D. Li, and W. Skiba, 1201.4383](#)

Mass raised to multi-TeV range with large couplings, not guaranteed at HL-LHC.

Composite Higgs models: not in a good shape?



CEPC Wishlist



Could future ee colliders like CEPC bring us the best experimental precision on bread and butter for EWPO: m_W , m_Z , Γ_Z , m_t , $\sin\theta_w$, etc.?

- YES! Powerful runs at the Z pole, WW threshold(!), Higgs factory mode and tt threshold after upgrades.
- Key numbers from the preliminary CEPC white paper and other ref.: $\delta m_W \approx 0.5-1$ MeV, $\delta m_Z \approx 0.1$ MeV, $\delta m_t \lesssim 100$ MeV, $\delta \sin\theta_w \lesssim 10^{-5}$: experiment is no longer the most limiting factor.
- Possible to bring the current EW precision up by an order of magnitude.

Could the theory interpretation of m_W catch-up with the experiment by the time of CEPC runs? (More discussions in [J. Fan, M. Reece, L-T. Wang, 1411.1054](#) & [A. Freitas, S. Heinemeyer et al. 1906.05379](#))

- “parametric uncertainties” bottle necks: currently from m_t ($0.5 \rightarrow <0.1$ GeV). At CEPC era: $\Delta\alpha_{\text{had}}^{(5)}$ ($4 \times 10^{-4} \rightarrow \sim 5 \times 10^{-5}$) $\rightarrow \delta m_W(\text{th}) \lesssim 1$ MeV.
- “Intrinsic uncertainties”: on m_W itself needs to go beyond two-loops ($4 \rightarrow 1$ MeV). QED radiation & $\sigma(\text{WW} \rightarrow 4f)$ will contribute $\delta m_W(\text{th}) \lesssim 0.6$ MeV.

Could CEPC figure out the nature of new physics?

- O(20) EW (pseudo)observables and similarly many Higgs ones: greatly narrow down the candidate theory space.

Hope for CEPC to DISCOVER the new physics DIRECTLY?