

High Performance Computing and Lattice QCD

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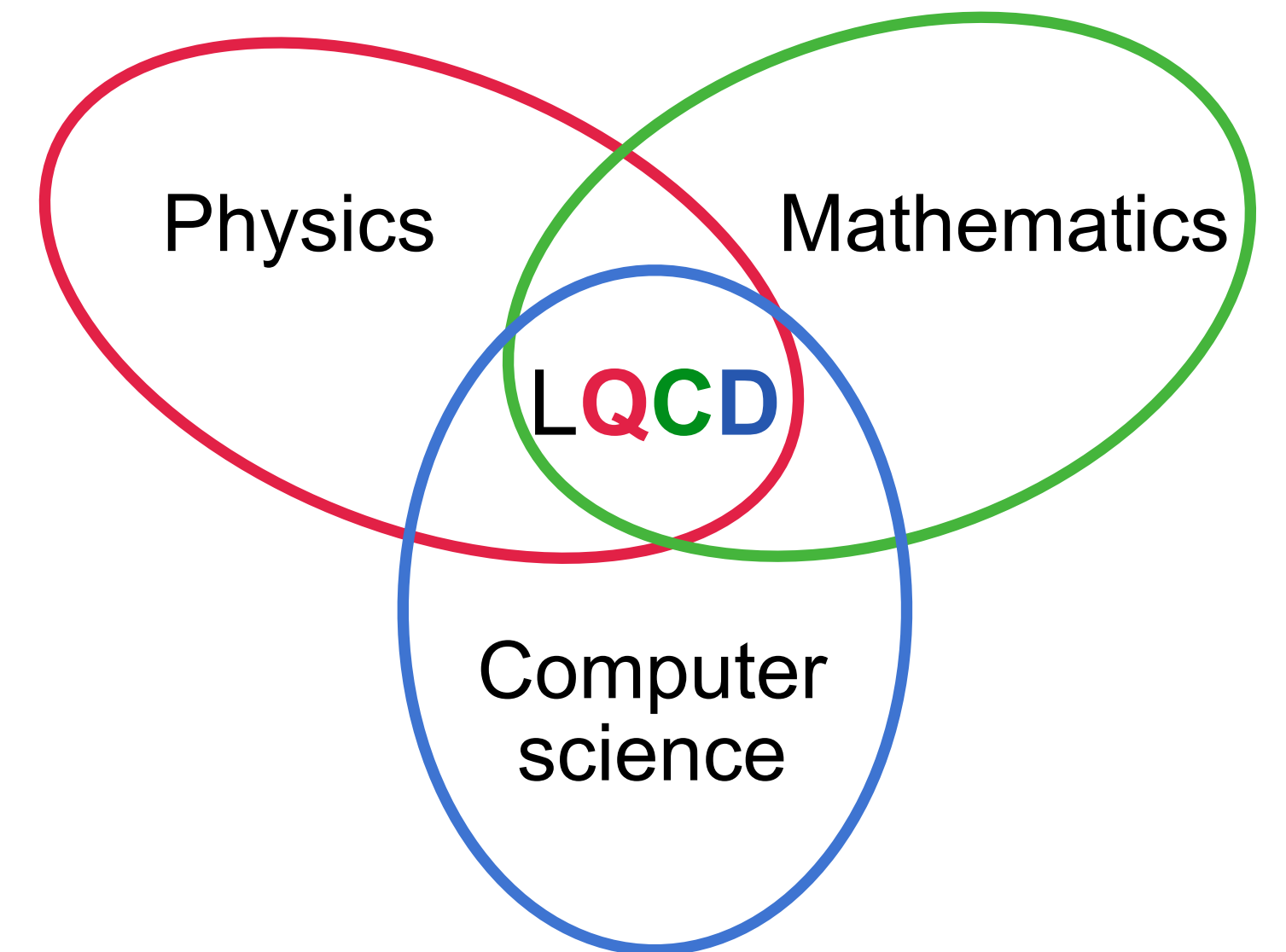
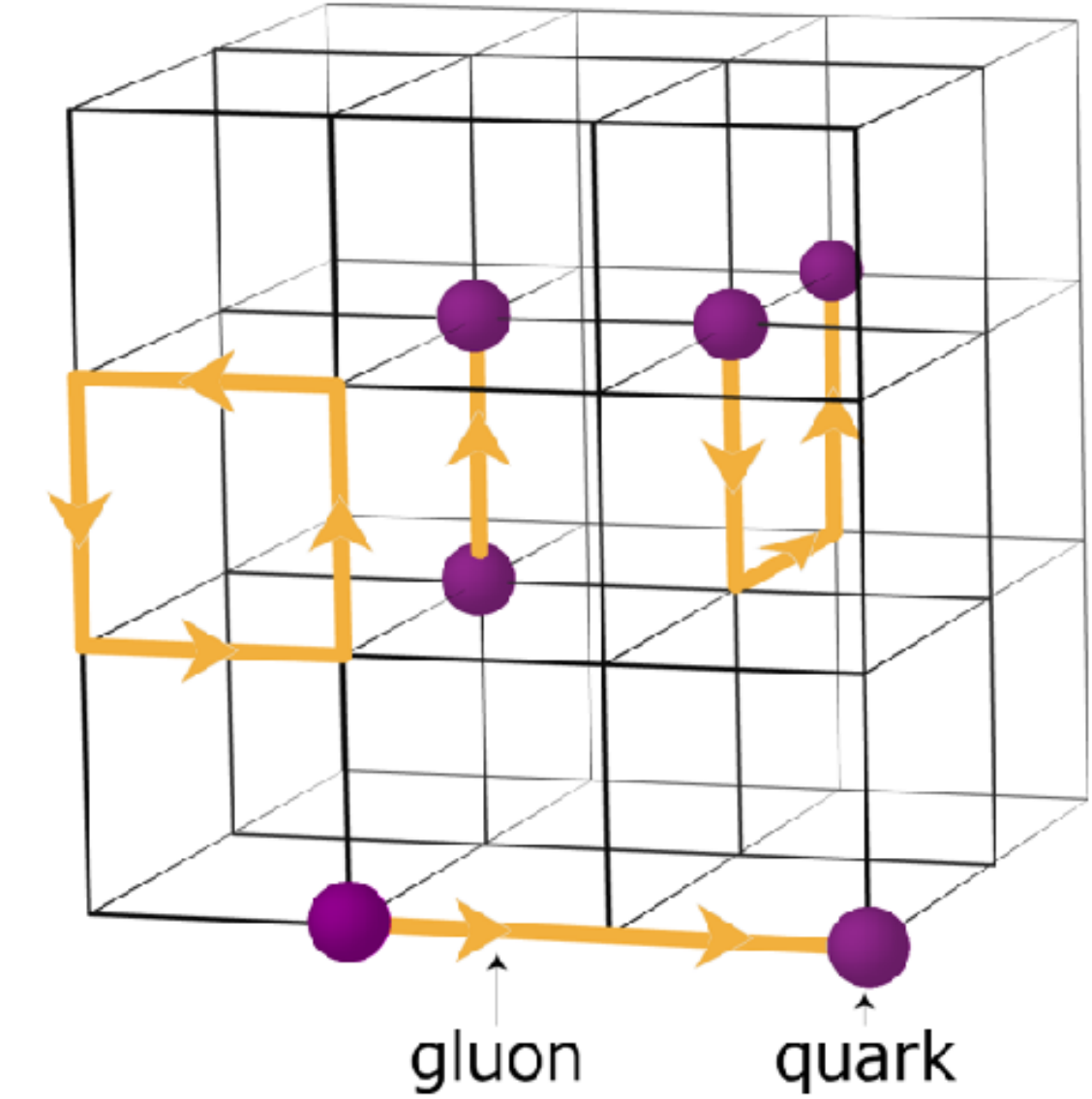
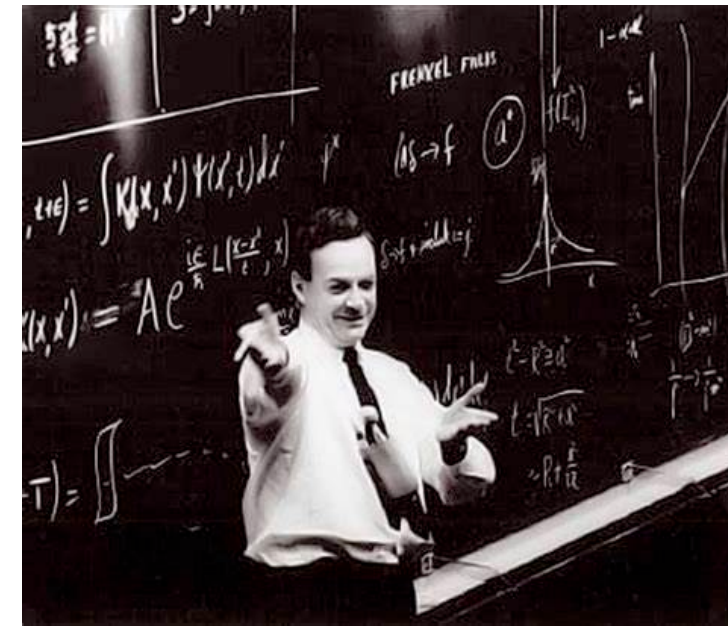
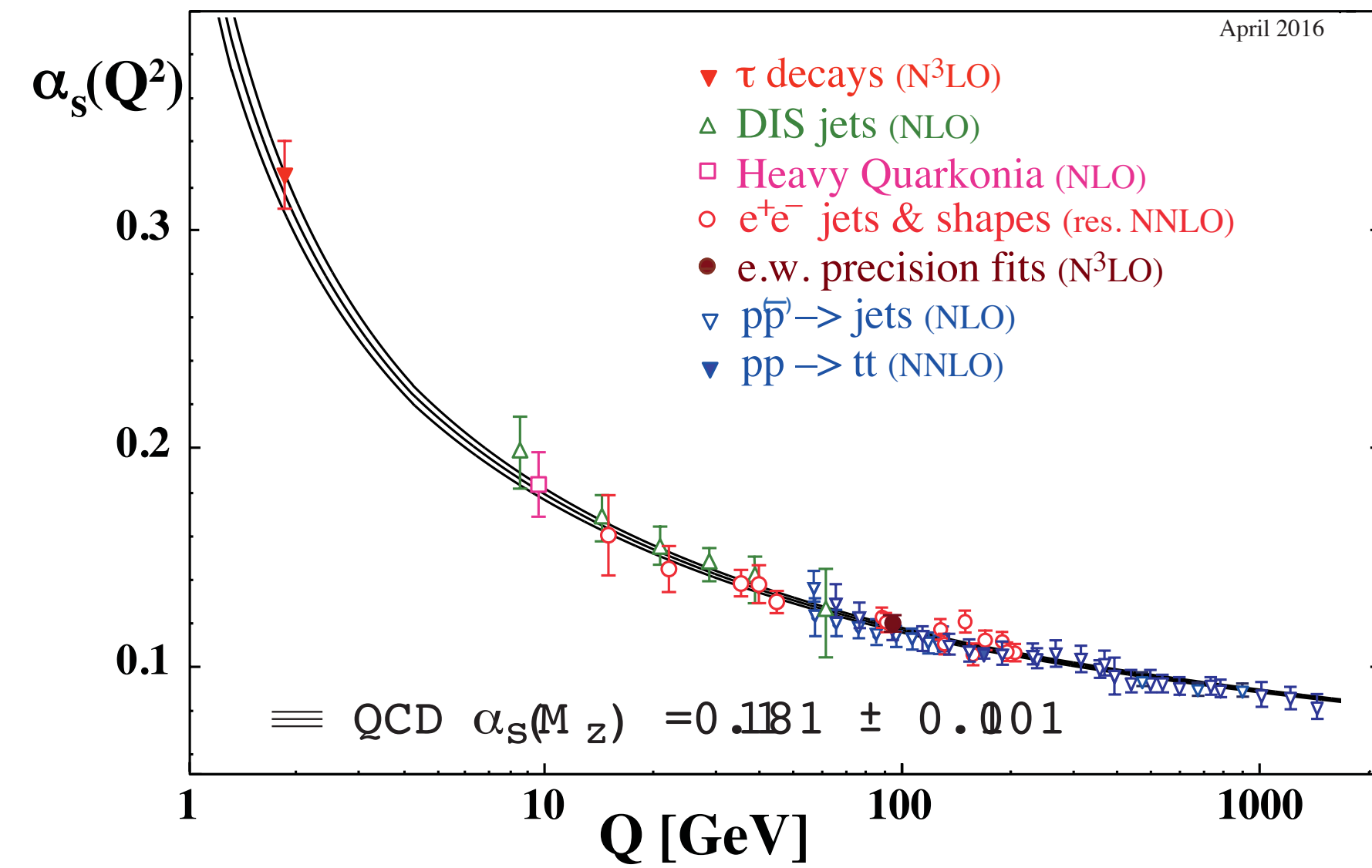
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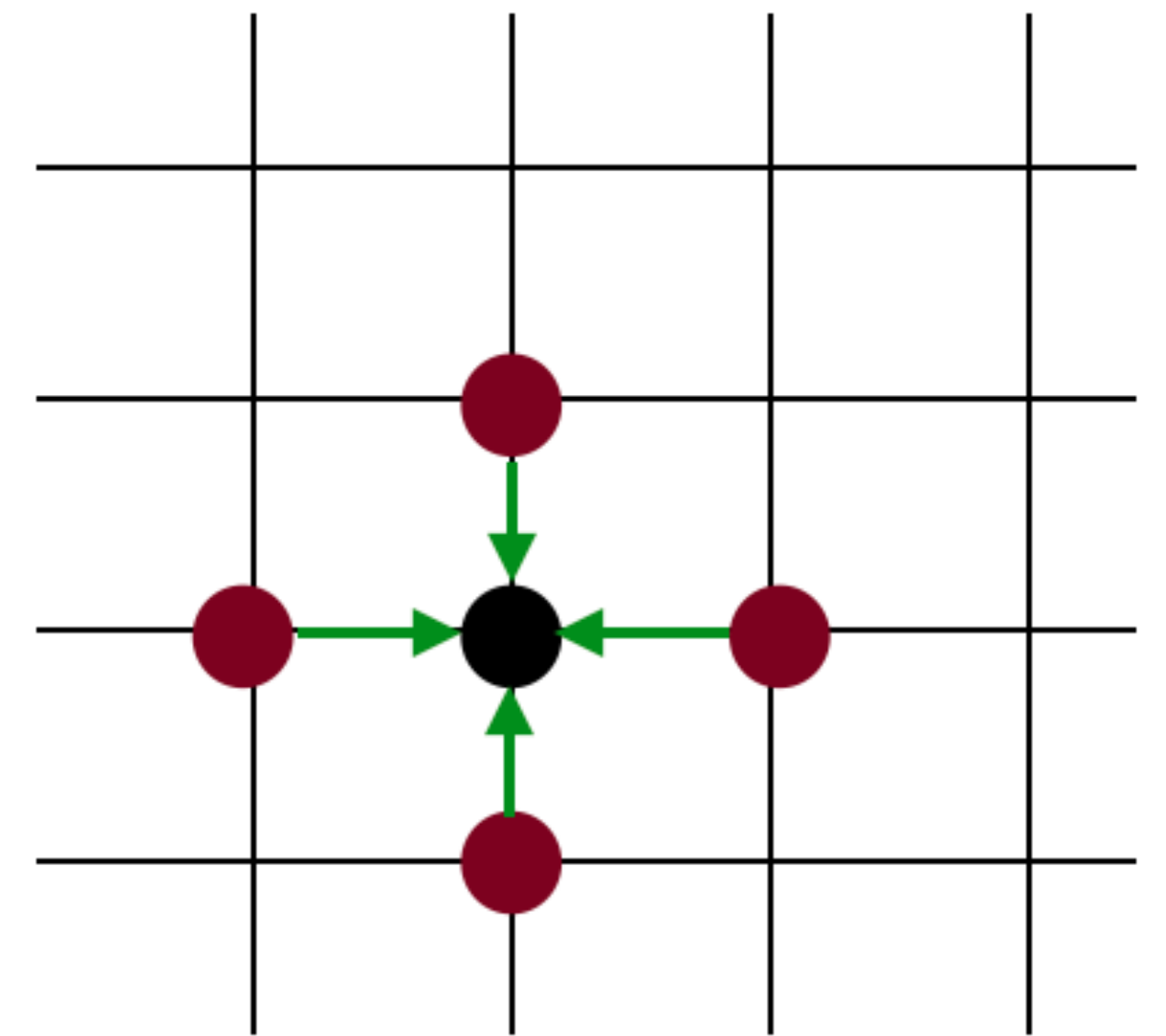
Introduction to LQCD



- Lattice QCD (LQCD) : QCD on a **spacetime lattice**
- Calculate QCD path integral with **Monte Carlo** method

Computational Perspectives of LQCD

- Dirac equation on the lattice is to solve the large sparse linear system $Mx = b$
- $M = m + 4 - \frac{1}{2}D$, D is the Dslash operation
- $$D_{x,y} = \sum_{\mu=1}^4 U_{\mu}(x)(1 - \gamma_{\mu})\delta_{x+\hat{\mu},y} + U_{\mu}(x - \hat{\mu})^{\dagger}(1 + \gamma_{\mu})\delta_{x-\hat{\mu},y}$$
- 4 dimensional 8(9) point stencil operator
- Nearest neighbor communication, very suitable for parallel computing
- LQCD is expensive
 - $N_f = 2 + 1$, $64^3 \times 128$, $m_{\pi} \approx 170 \text{ MeV}$, $\beta = 6.3$
 - 512 V100 GPUs
 - 700 GPU*Hour per gauge configuration
 - $O(1M)$ GPU*Hour for $O(1000)$ gauge configuration
 - $O(10 - 100)$ GB per quark propagator



Computational Perspectives of LQCD

LQCD with HPC

- Decades ago - customized processors
- QCDOC (QCD On a Chip)
- Nowadays - supercomputers / clusters
- TOP 500

QCDOC Asic, 1 Gflop/s

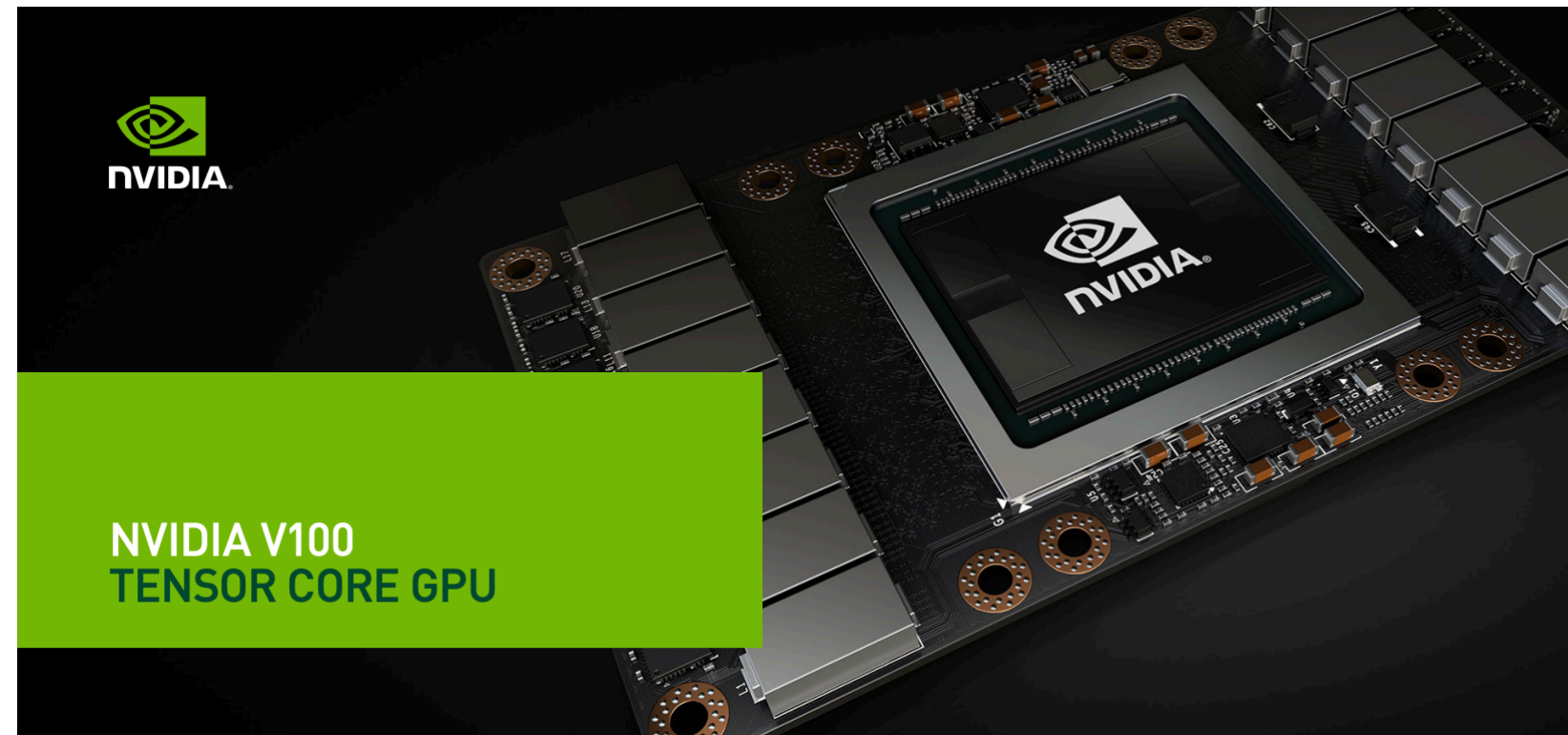


Rank	System	Cores	Rmax (PFlop/s)	Rpeak (PFlop/s)	Power (kW)
1	Frontier - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE DOE/SC/Oak Ridge National Laboratory United States	8,730,112	1,102.00	1,685.65	21,100
2	Supercomputer Fugaku - Supercomputer Fugaku, A64FX 48C 2.2GHz, Tofu interconnect D, Fujitsu RIKEN Center for Computational Science Japan	7,630,848	442.01	537.21	29,899
3	LUMI - HPE Cray EX235a, AMD Optimized 3rd Generation EPYC 64C 2GHz, AMD Instinct MI250X, Slingshot-11, HPE EuroHPC/CSC Finland	1,110,144	151.90	214.35	2,942
4	Summit - IBM Power System AC922, IBM POWER9 22C 3.07GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM DOE/SC/Oak Ridge National Laboratory United States	2,414,592	148.60	200.79	10,096
5	Sierra - IBM Power System AC922, IBM POWER9 22C 3.1GHz, NVIDIA Volta GV100, Dual-rail Mellanox EDR Infiniband, IBM / NVIDIA / Mellanox DOE/NNSA/LLNL United States	1,572,480	94.64	125.71	7,438

- LQCD awarded 1995, 1998, 2006 Goldon Bell Prize and 2018 finalist

Computational Perspectives of LQCD

Computing resources of IHEP LQCD group (after 2018)



Nvidia V100 GPU cards: 280 = 200 (Beijing) + 80 (Dongguan)



x86 CPU: ~ 12000 cores

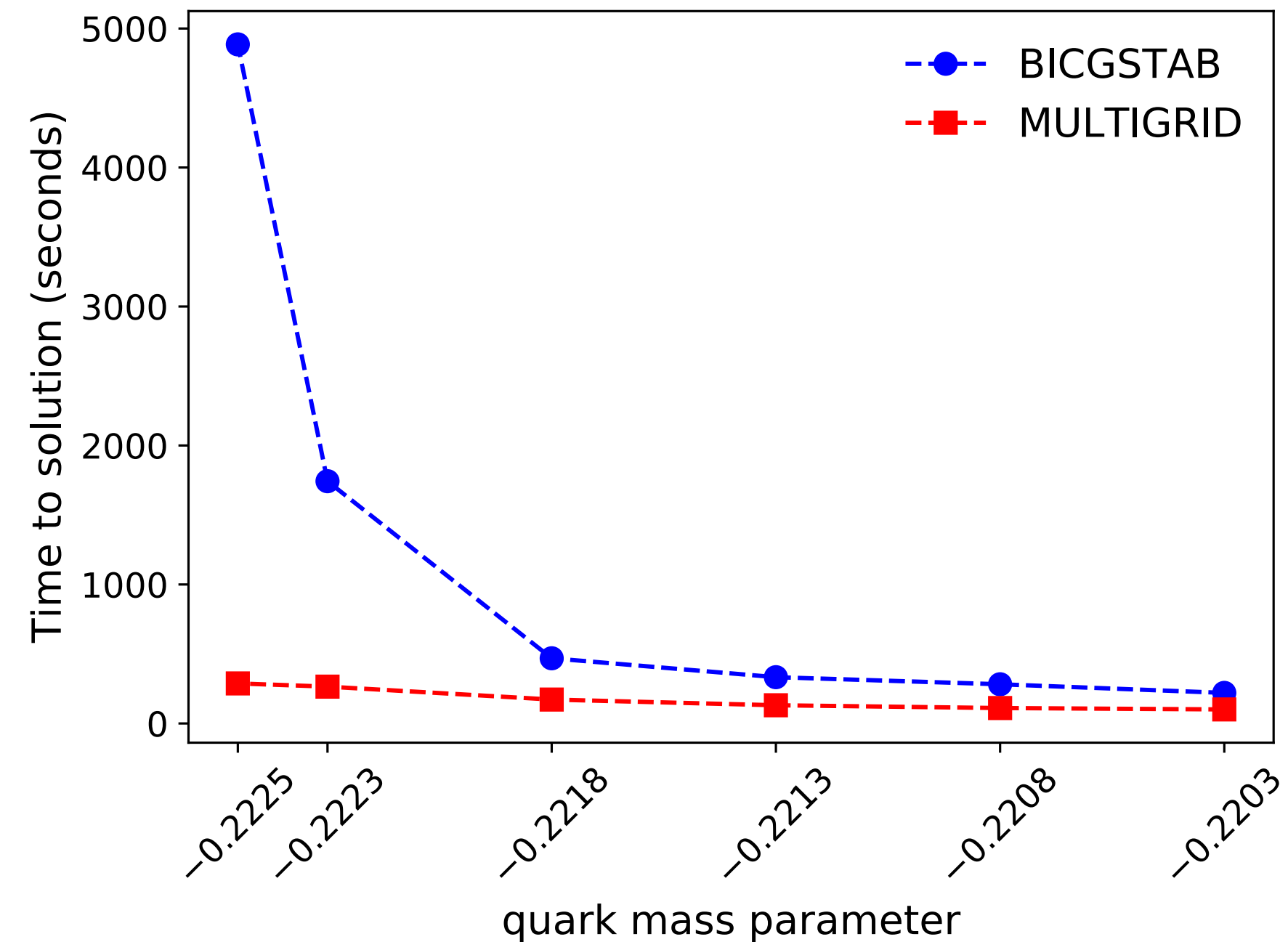
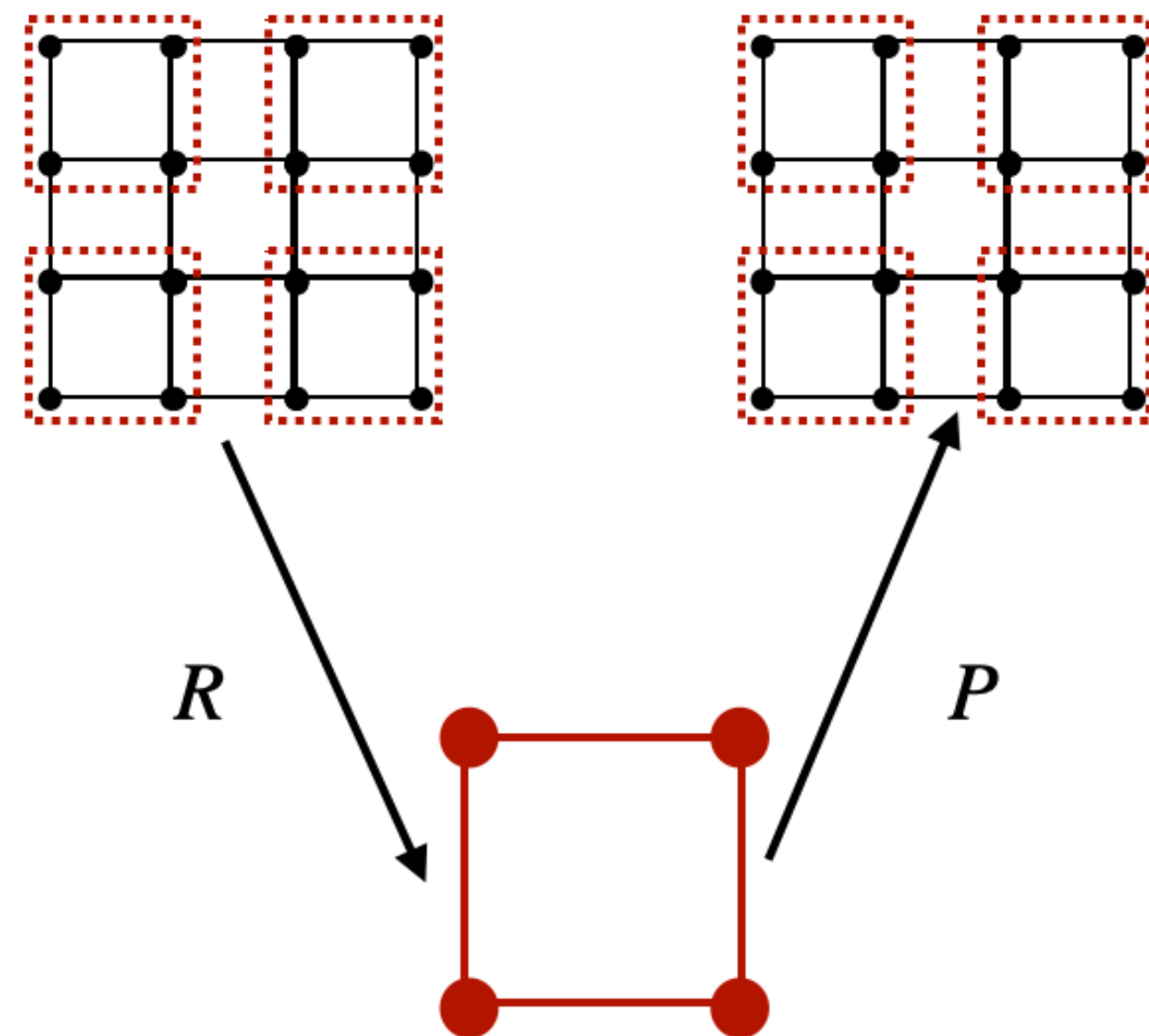


ARM CPU: ~ 10000 cores

Computational Perspectives of LQCD

Multigrid algorithm for LQCD

- Need to large amount of sparse linear system $Mx = b$
- Traditional Krylov Subspace method suffers **critical slowing down** problem
- Explore the **multigrid algorithm**



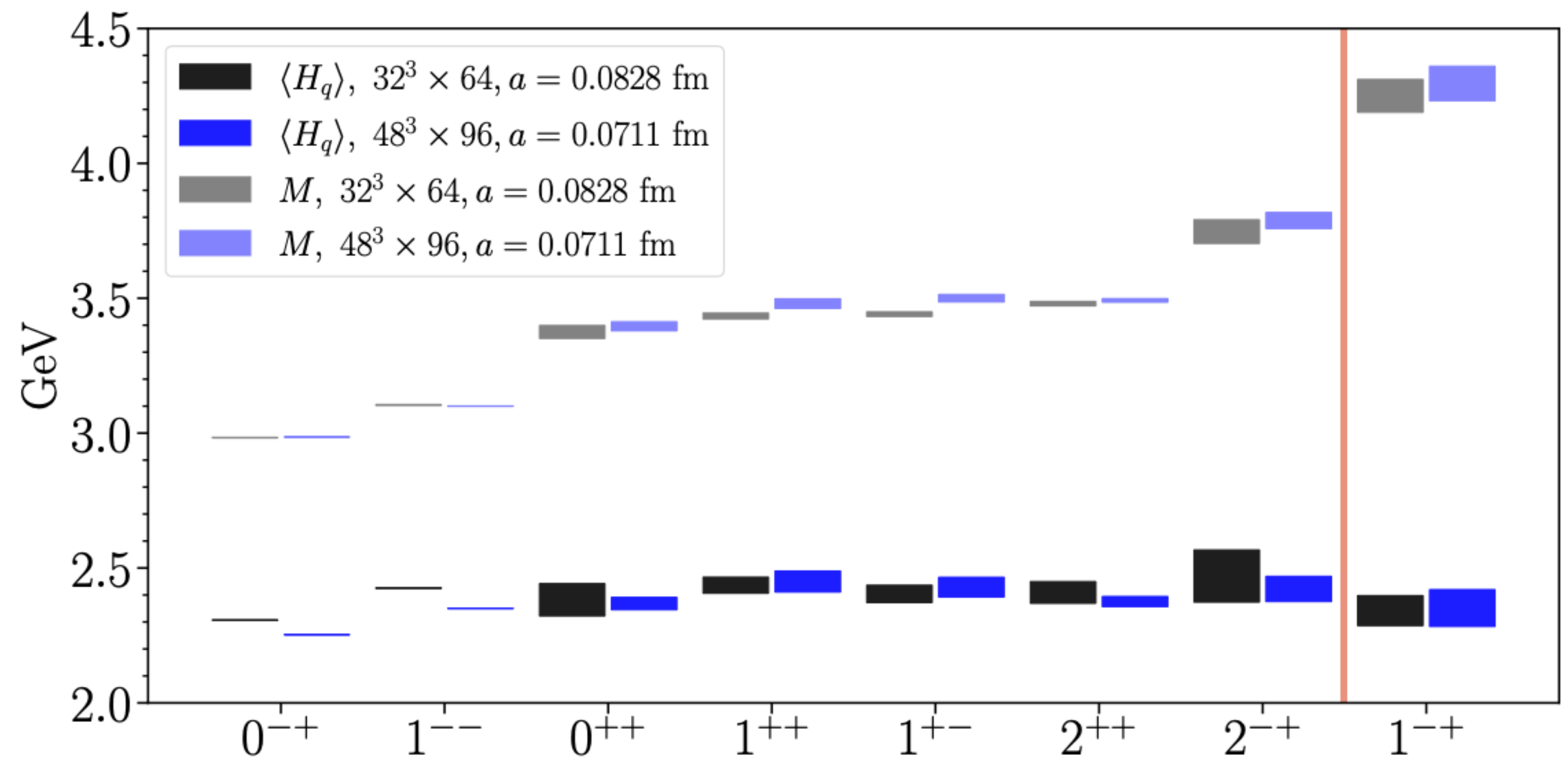
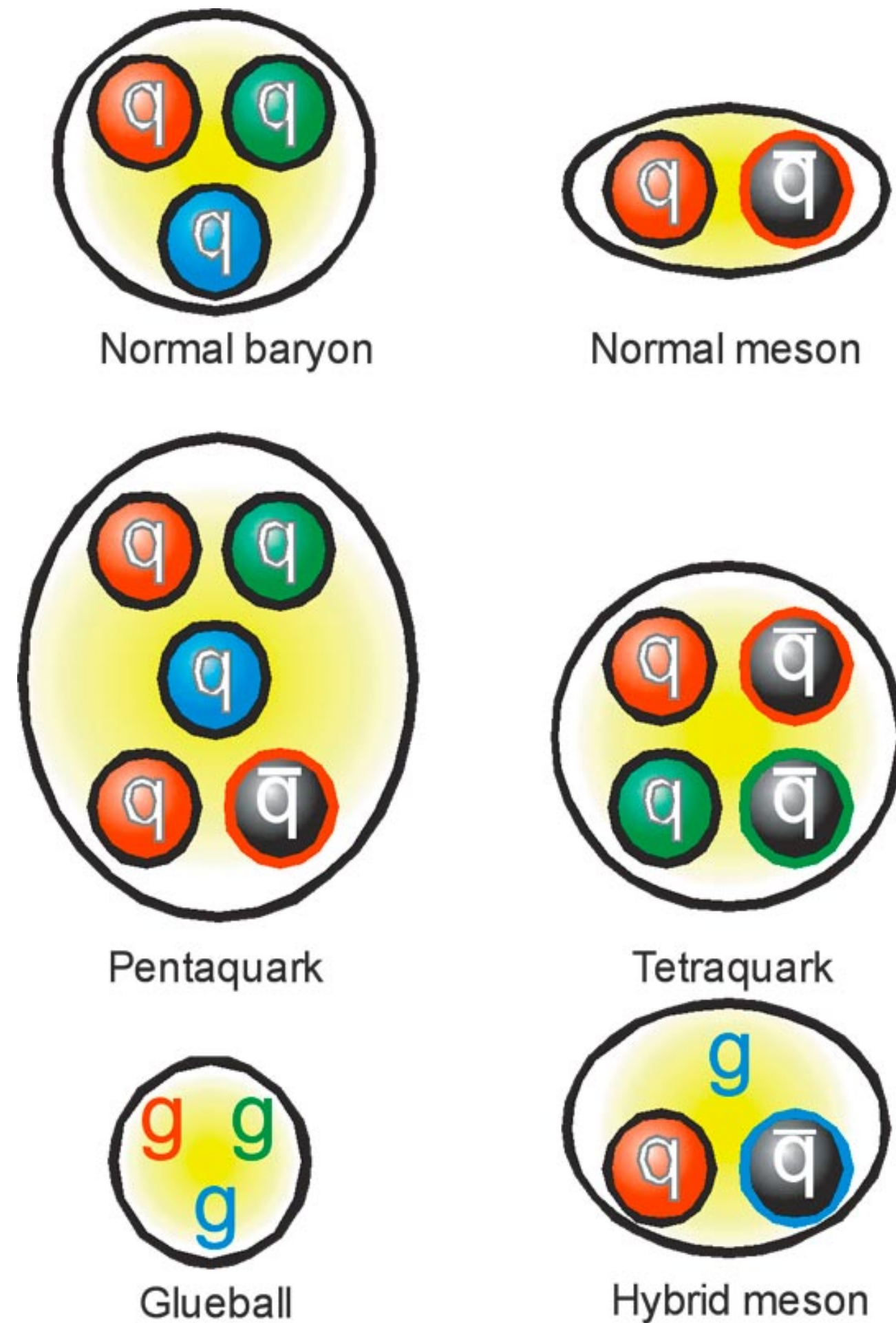
- Supported by China Postdoctoral Science Foundation

Charmonium related LQCD studies

Gluons in charmoniumlike states

[[W.Sun](#), Y.Chen, P.Sun, Y.B.Yang, *Phys.Rev.D* 103 (2021) 9, 094503]

- Mass decomposition of $1S, 1P, 2^{-+}, 1^{-+}$ charmoniumlike states



Charmonium related LQCD studies

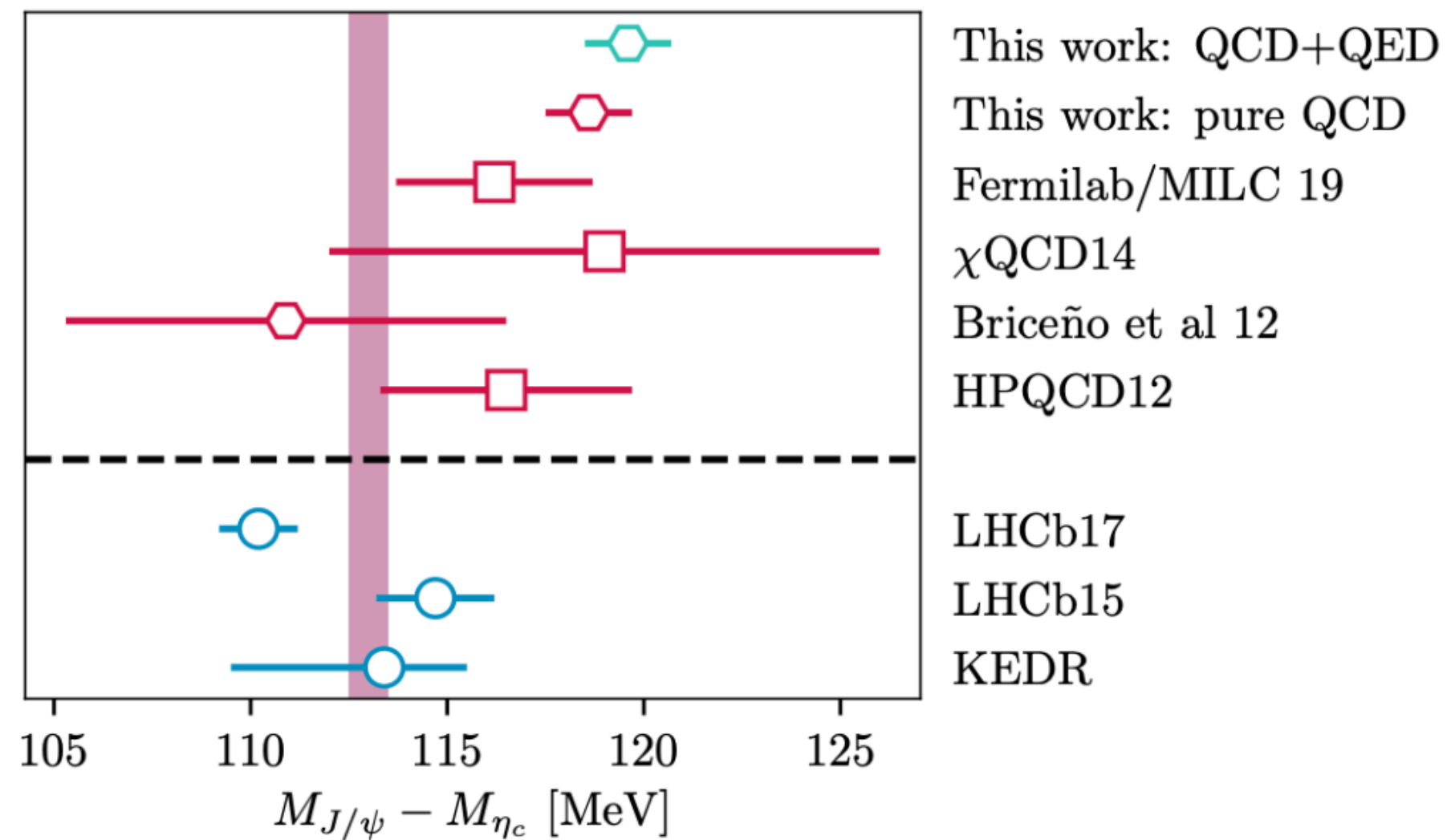
The glueball content of η_c

$$\eta_c(1S) \quad I^G(J^{PC}) = 0^+(0^{-+})$$

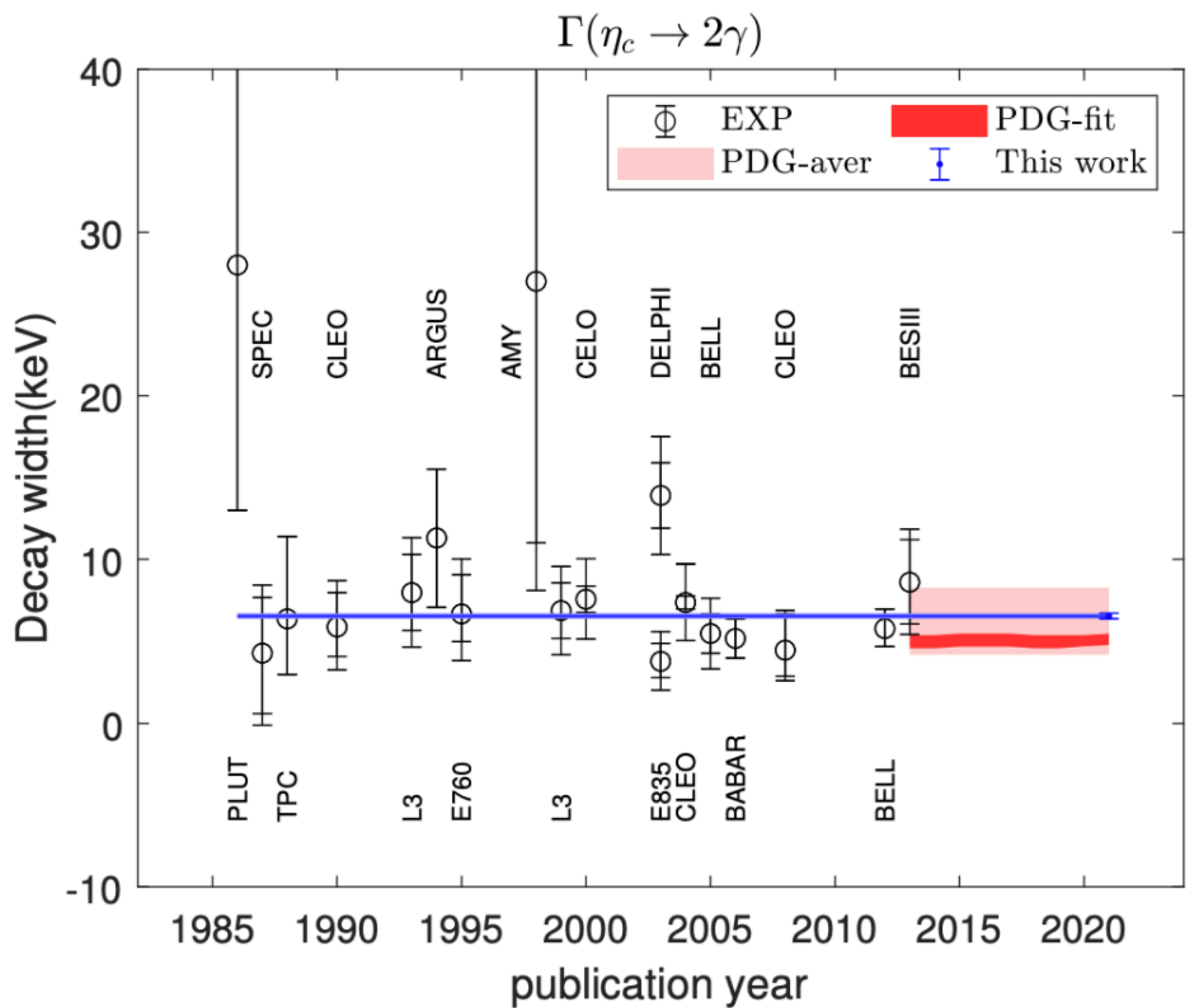
Large decay width compared to other charmonium

$\eta_c(1S)$ MASS 2983.9 ± 0.4 MeV ($S = 1.2$)

$\eta_c(1S)$ WIDTH 32.0 ± 0.7 MeV



D. Hatton et.al, Phys. Rev. D 102, 054511 (2020)



Y. Meng et.al, arXiv:2109.09381

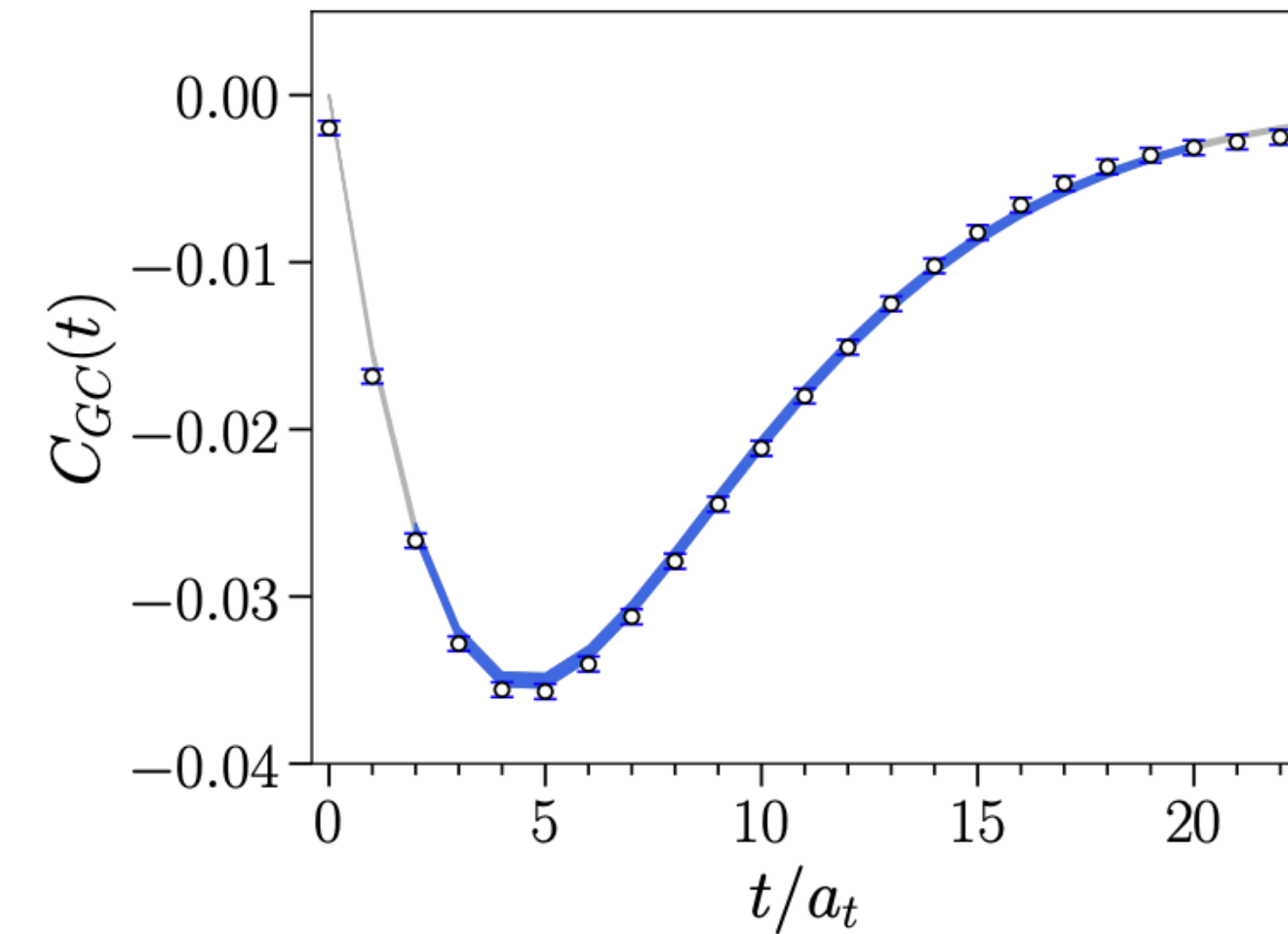
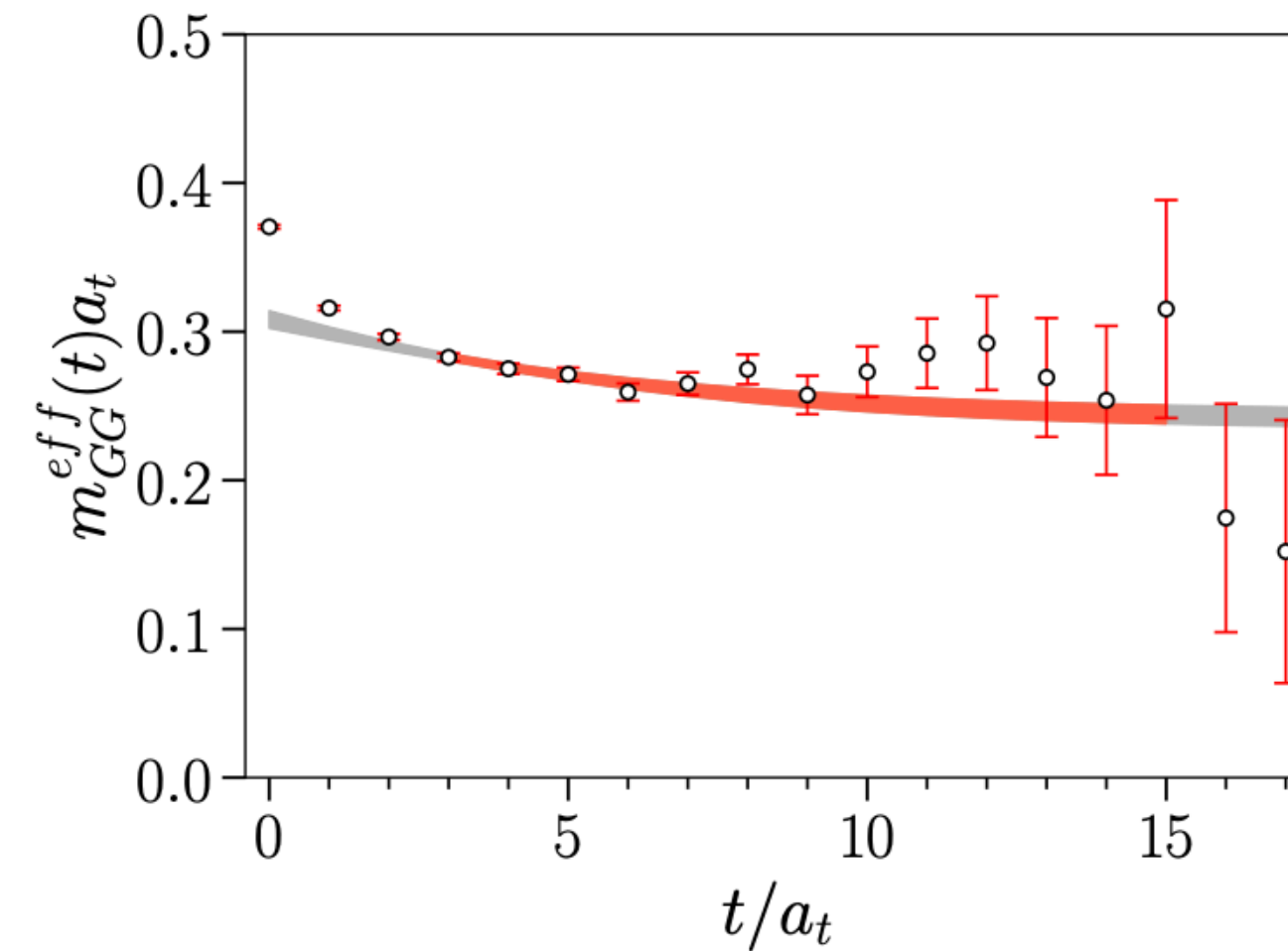
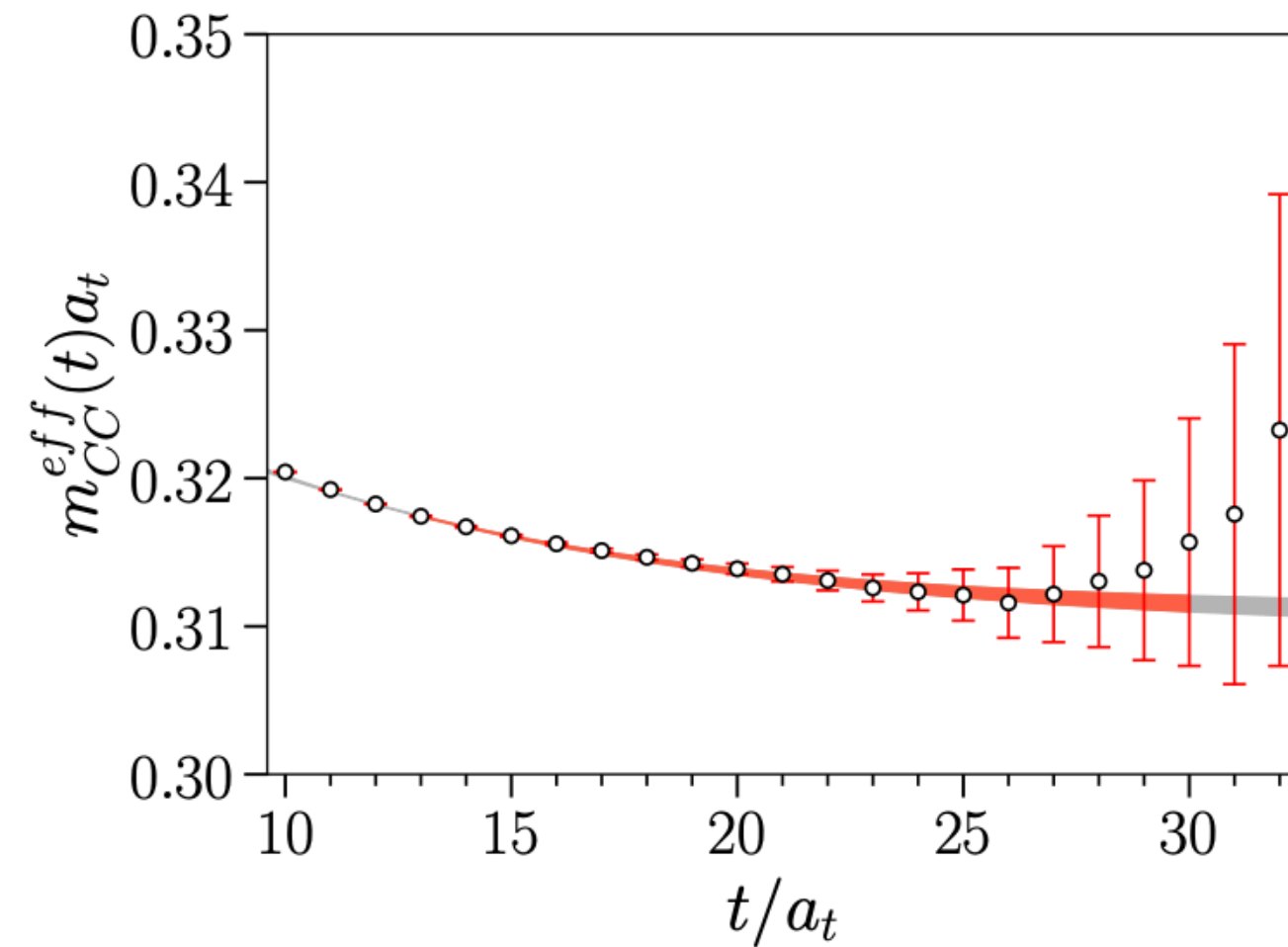
Charmonium hyperfine splitting: 120 MeV (lattice) vs. 113 MeV (exp.)

3.6 σ discrepancy of $\Gamma(\eta_c \rightarrow 2\gamma)$ between exp. and lattice

Charmonium related LQCD studies

The glueball content of η_c

[R.Zhang, **W.Sun**, Y.Chen et al., *Phys.Lett.B* 827 (2022) 136960]



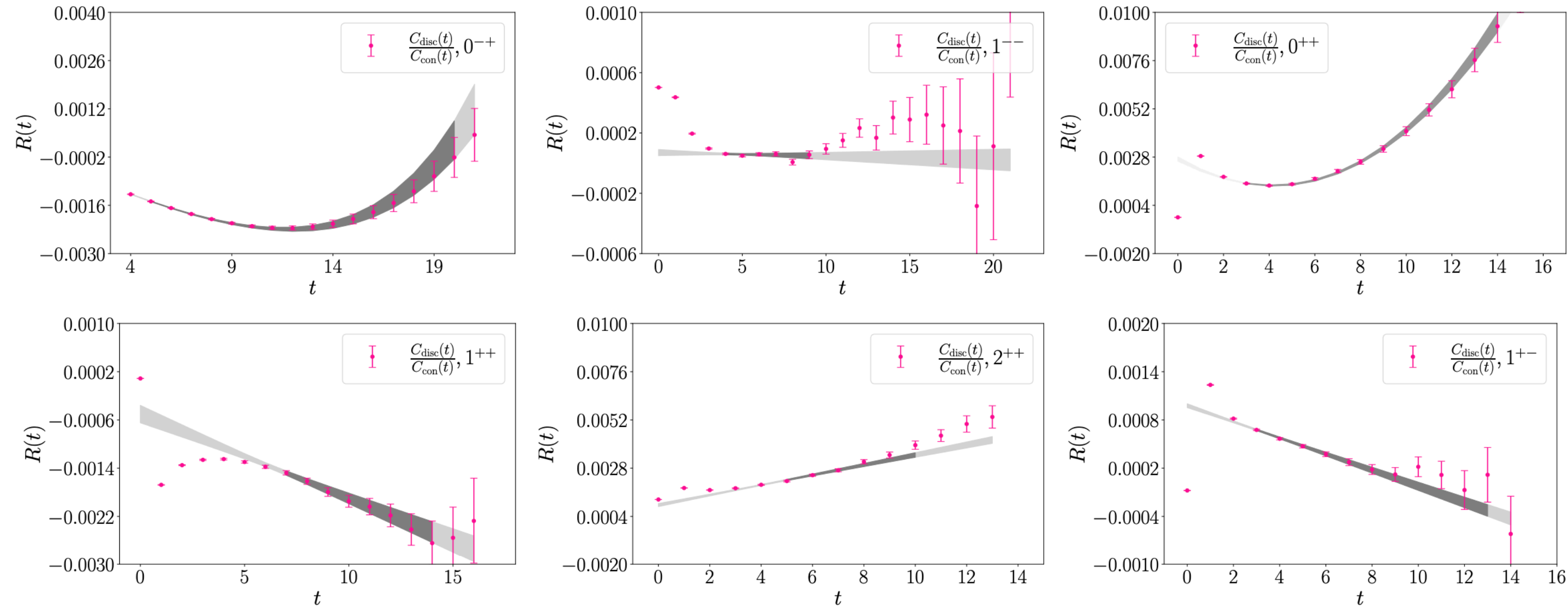
Ensemble	$L^3 \times T$	β	a_s (fm)	ξ	N_{cfg}	$m_{J/\psi}$ (MeV)
I	$16^3 \times 128$	2.8	0.1026	5	~ 7000	2743
II	$16^3 \times 128$	2.8	0.1026	5	~ 6000	3068

- mixing angle $\theta = 4.3(3)^\circ$, mixing energy $x = 49(6)$ MeV
- raise the decay width of $c\bar{c}$ by approximately 7 MeV
- shift the mass of pseudoscalar $c\bar{c}$ state upward by approximately 3.9(9) MeV

Charmonium related LQCD studies

Annihilation diagram contribution to charmonium masses

[R.Zhang, **W.Sun**, F.Chen et al., *Chin.Phys.C* 46 (2022) 043102]



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- No effect for J/ψ , increase η_c by 3-4 MeV
- Increase χ_{c1}, h_c by ~ 1 MeV
- Decrease χ_{c2} by ~ 3 MeV

Summary

- Progress of LQCD is strongly related to the development of HPC system
- LQCD is one of the most computing resource demanding research area in high energy physics
- LQCD is also an important application of high performance supercomputers and clusters
- We show some recent results related to charmoniumlike states from IHEP LQCD group