

Type II Seesaw leptogenesis

韩成成

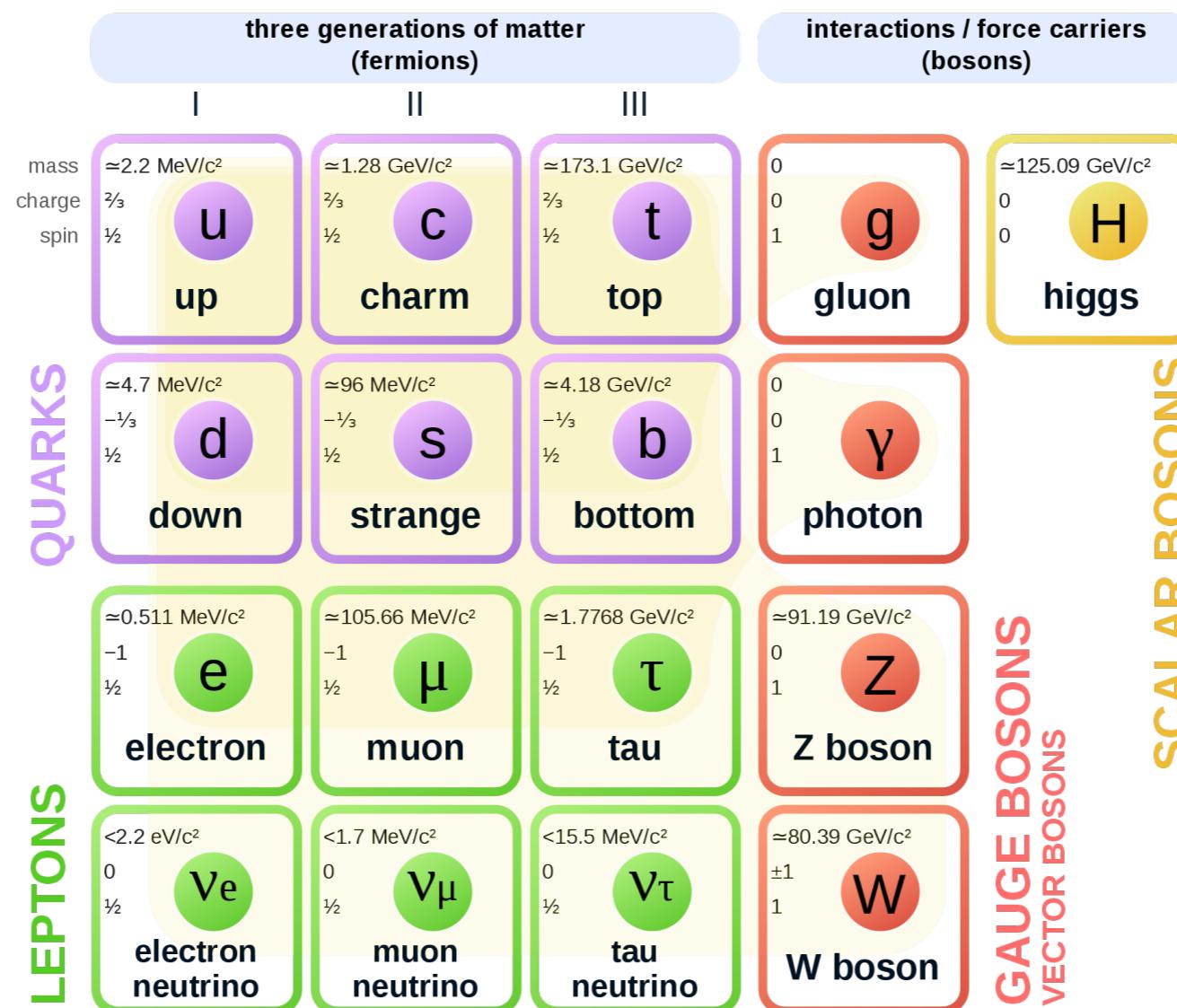
中山大学

With Neil D. Barrie and Hitoshi Murayama(村山齐)
arXiv:2106.03381(Phys. Rev. Lett. 128, 141801) and
arXiv:2204.08202(JHEP 05 (2022) 160)

第十九届重味物理和CP破坏研讨会
2022.12.10

Standard model

Standard Model of Elementary Particles



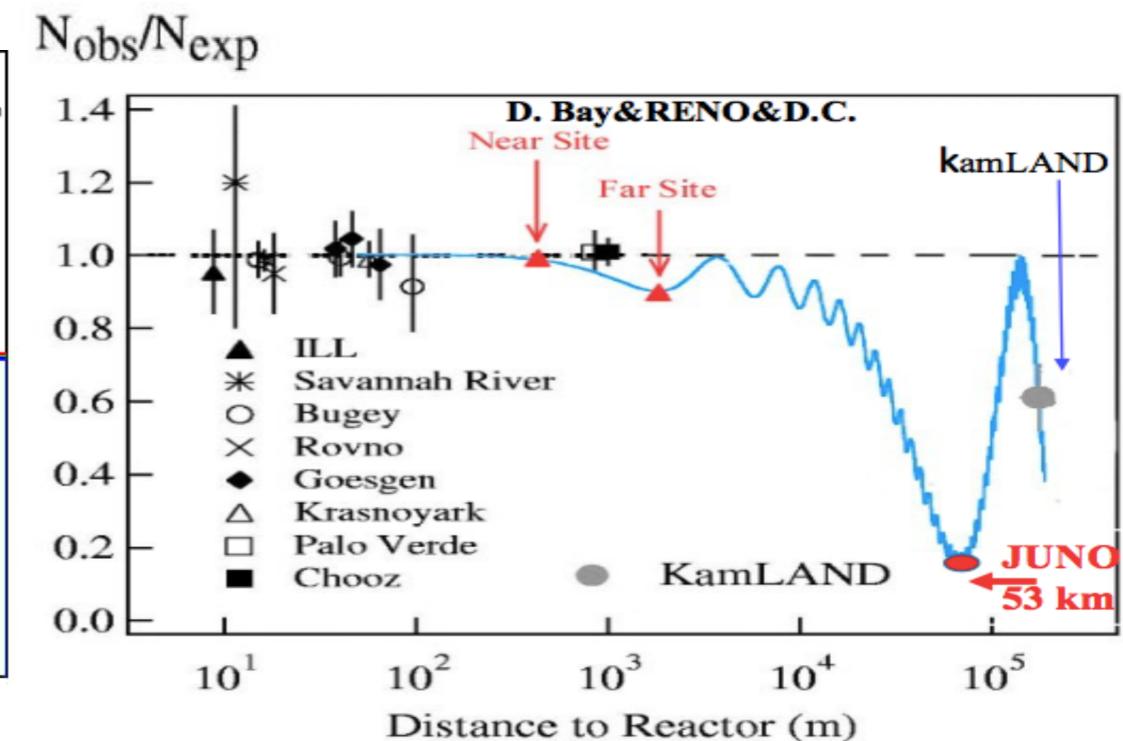
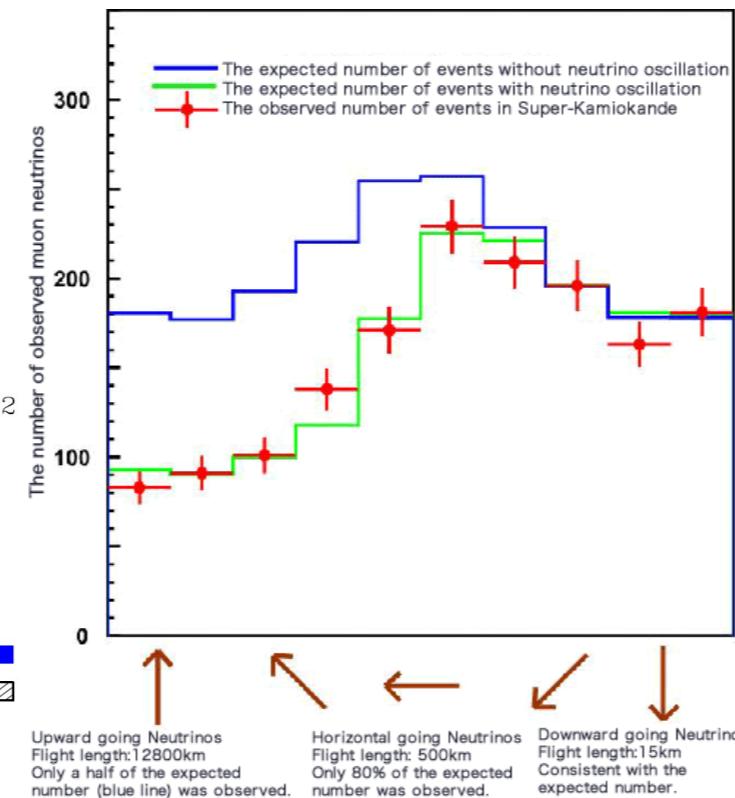
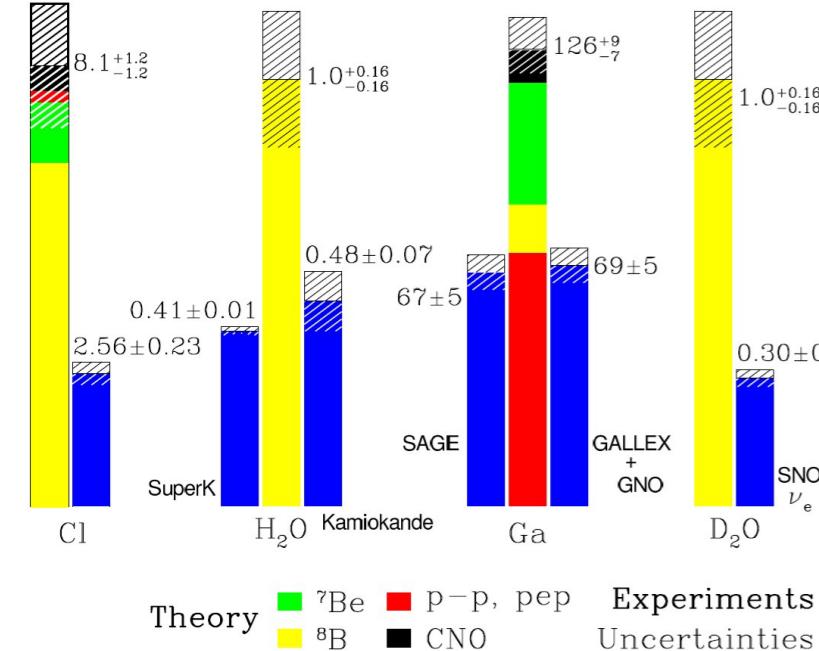
Very successful describing low energy scale physics

Observation requiring new physics

- Neutrino masses
 - Baryon asymmetry of our universe
 - Inflation
- today's talk
- Dark matter
 - Others(muon g-2? W mass?)

Neutrino masses

Neutrino oscillation requiring massive neutrinos



Solar Neutrino oscillations

$$\theta_{12}$$

$$\Delta m_{21}^2 \simeq 7.42 \times 10^{-5} \text{ eV}^2$$

Atmospheric Neutrino Oscillations

$$\theta_{23}$$

$$|\Delta m_{13}^2| \approx |\Delta m_{23}^2| \simeq 2.5 \times 10^{-3} \text{ eV}^2$$

Reactor Neutrino Oscillations

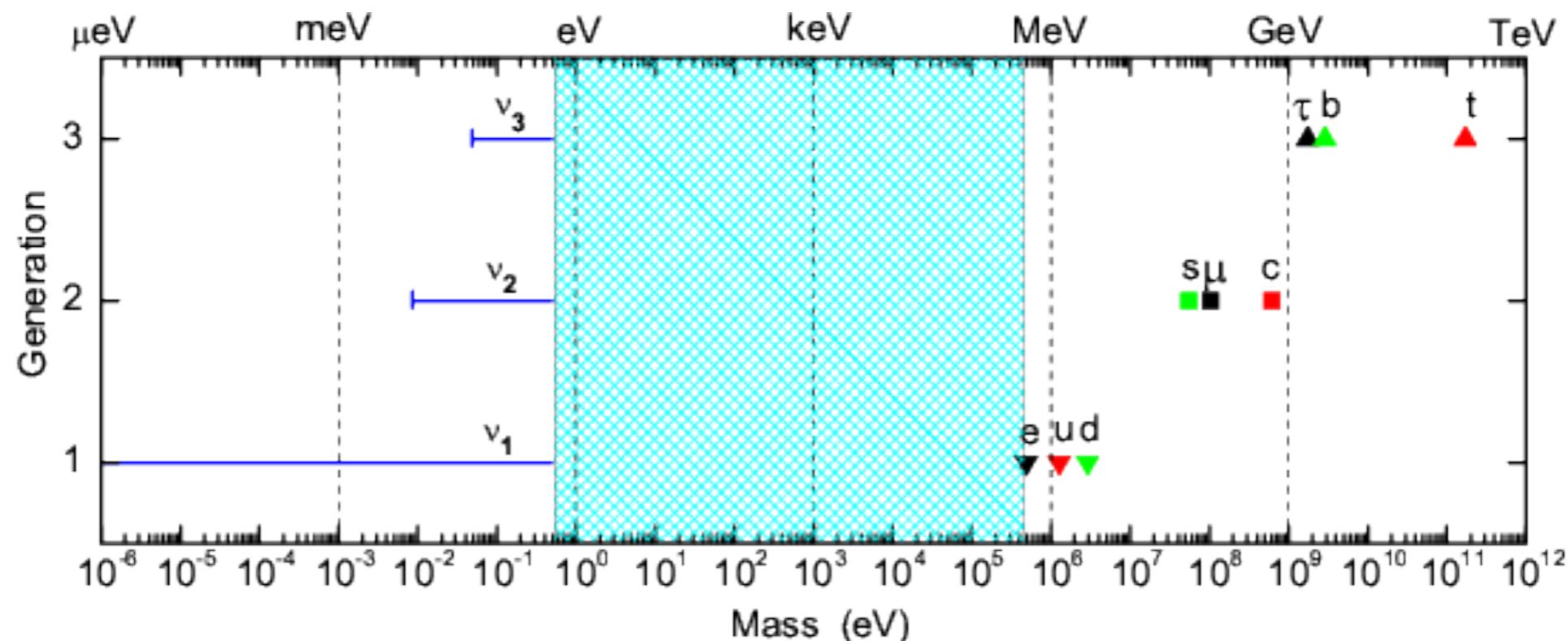
$$\theta_{13}$$

At least a neutrino mass larger or similar to 0.05 eV

May provide new source of CP violation

Neutrino masses vs other fermion masses

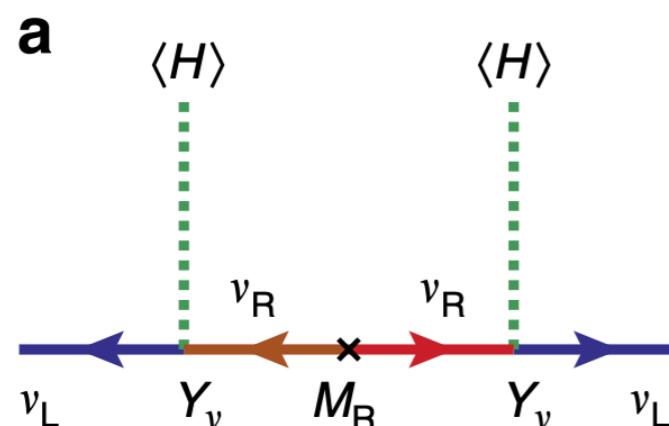
A large hierarchy comparing with other fermion masses



Origin of neutrino masses

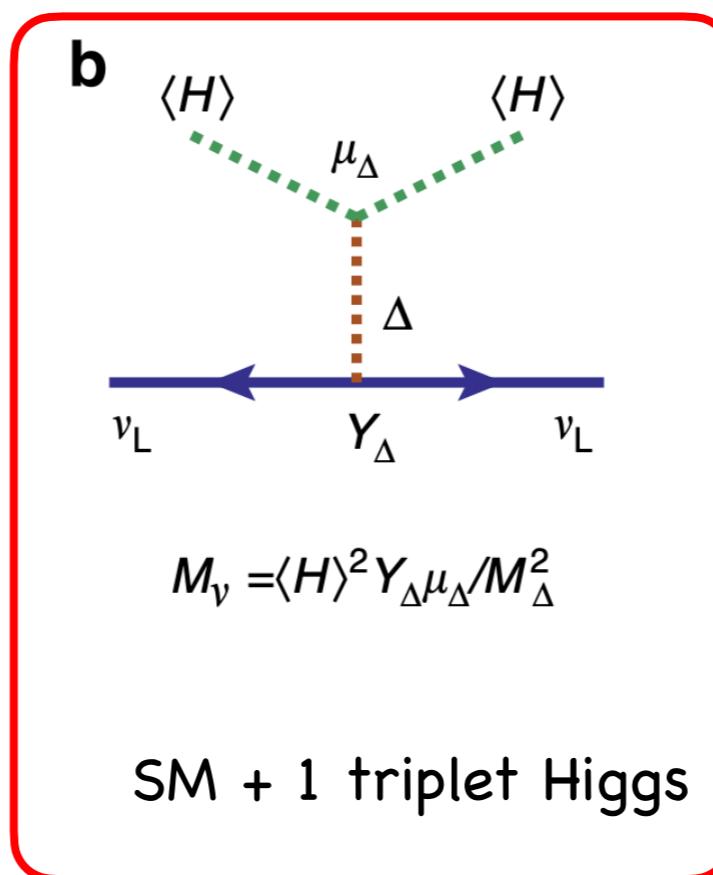
Three types of seesaw model(tree level)

Tommy Ohlsson, Shun Zhou, Nature Commun. 5 (2014) 5153



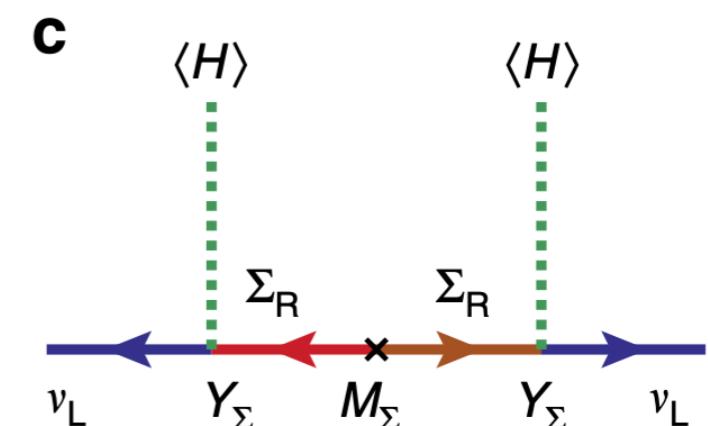
$$M_\nu = -\langle H \rangle^2 Y_\nu M_R^{-1} Y_\nu^\top$$

SM + 3 singlets fermions



$$M_\nu = \langle H \rangle^2 Y_\Delta \mu_\Delta / M_\Delta^2$$

SM + 1 triplet Higgs



$$M_\nu = -\langle H \rangle^2 Y_\Sigma M_\Sigma^{-1} Y_\Sigma^\top$$

SM + 3 triplet fermions

Providing a minimal framework

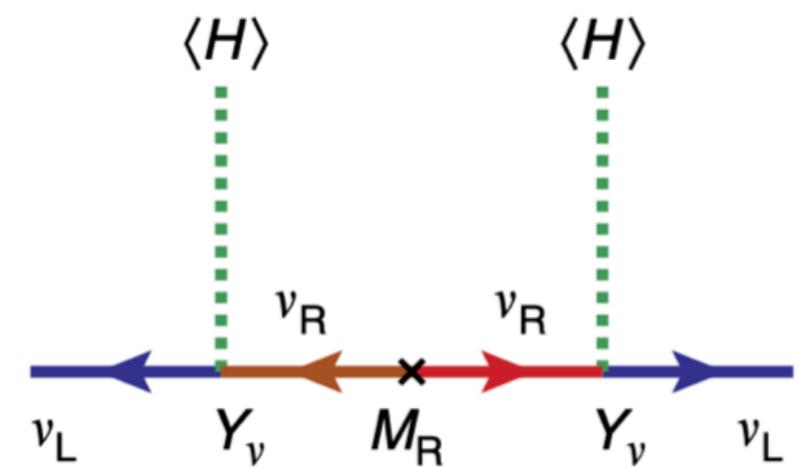
Origin of neutrino masses: type I seesaw

加入三个单态中性右手中微子 $N(1, 1, 0)$

$$\mathcal{L} = \mathcal{L}_{SM} + y_\nu \tilde{H} \bar{L} N - M_R \bar{N}^c N$$

$$M = \begin{pmatrix} 0 & m_D \\ m_D^T & M_R \end{pmatrix}$$

$$m_\nu \sim \frac{m_D^2}{M_R} = \frac{1}{2} \frac{y_\nu^2 \langle H \rangle^2}{M_R}$$



$$M_\nu = -\langle H \rangle^2 Y_\nu M_R^{-1} Y_\nu^\top$$

中微子质量被压低!

Origin of neutrino masses: type II seesaw

引入一个希格斯三重态跟中微子直接耦合

$$H(2, 1/2), \Delta(3, 1), L(2, -1/2)$$

$$H = \begin{pmatrix} h^+ \\ h \end{pmatrix}, \quad \Delta = \begin{pmatrix} \Delta^+/\sqrt{2} & \Delta^{++} \\ \Delta^0 & -\Delta^+/\sqrt{2} \end{pmatrix}$$

$$\mathcal{L}_{Yukawa} = \mathcal{L}_{Yukawa}^{\text{SM}} - \boxed{\frac{1}{2} y_{ij} \bar{L}_i^c \Delta L_j} + h.c.$$



$$\frac{1}{2} y_{ij} \Delta^0 \bar{\nu}^c \nu + h.c.$$

- Giving neutrino mass matrix with vev of Delta
- at the same time Delta get a lepton number -2

Origin of neutrino masses: type II seesaw

$H(2, 1/2), \Delta(3, 1), L(2, -1/2)$

$$\begin{aligned} V(H, \Delta) = & -m_H^2 H^\dagger H + \lambda_H (H^\dagger H)^2 + m_\Delta^2 \text{Tr}(\Delta^\dagger \Delta) + \lambda_1 (H^\dagger H) \text{Tr}(\Delta^\dagger \Delta) \\ & + \lambda_2 (\text{Tr}(\Delta^\dagger \Delta))^2 + \lambda_3 \text{Tr}(\Delta^\dagger \Delta)^2 + \lambda_4 H^\dagger \Delta \Delta^\dagger H \\ & + [\mu (H^T i\sigma^2 \Delta^\dagger H) + h.c.] + \dots \end{aligned}$$

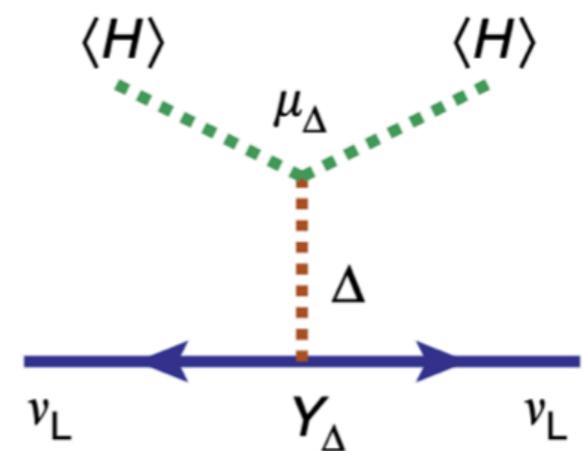
U(1)L breaking term

$$\langle \Delta^0 \rangle \simeq \frac{\mu v_{\text{EW}}^2}{2m_\Delta^2}$$

电弱精确测量限制

$$\mathcal{O}(1) \text{ GeV} > |\langle \Delta^0 \rangle| \gtrsim 0.05 \text{ eV}$$

中微子质量要求

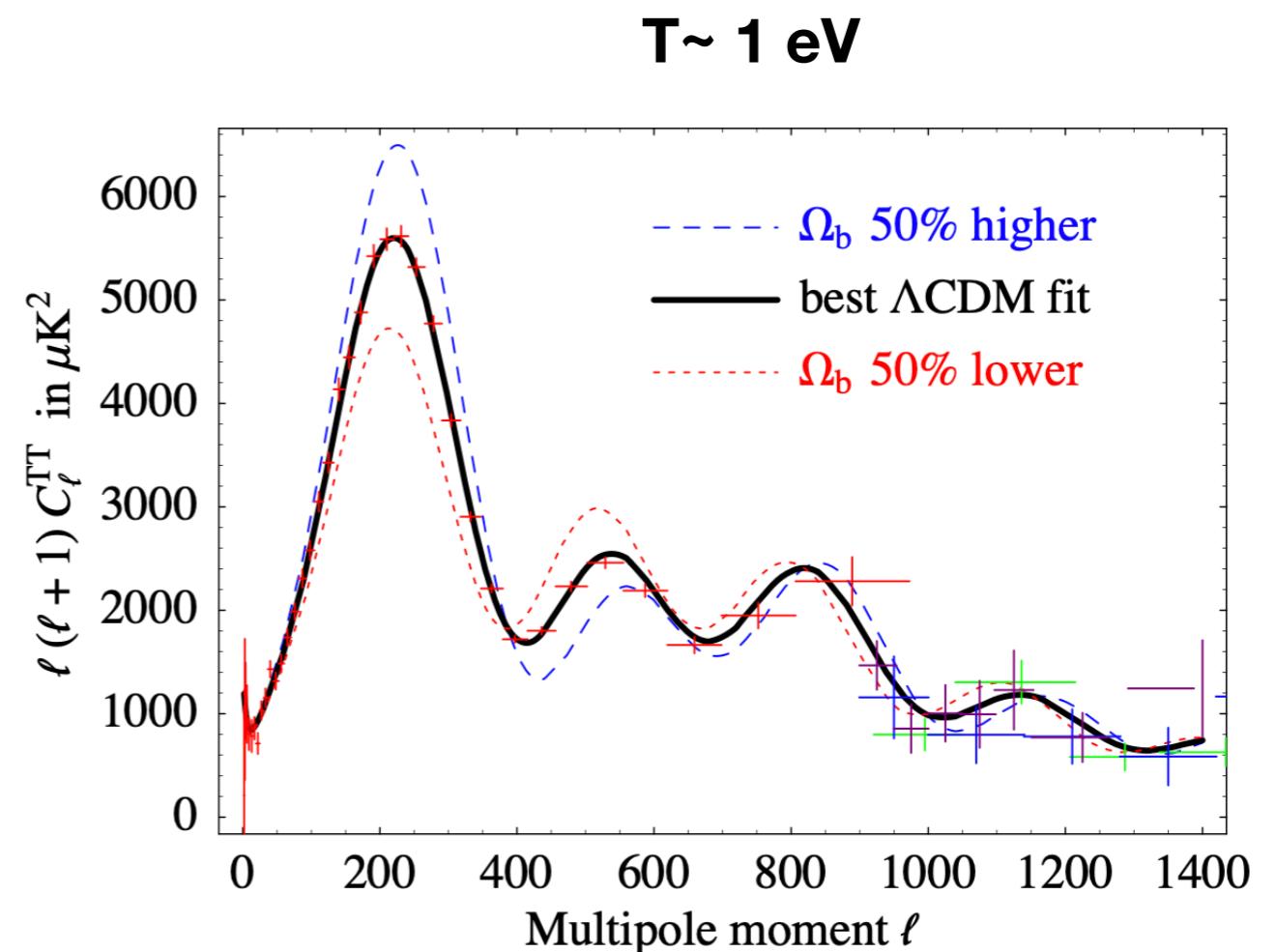
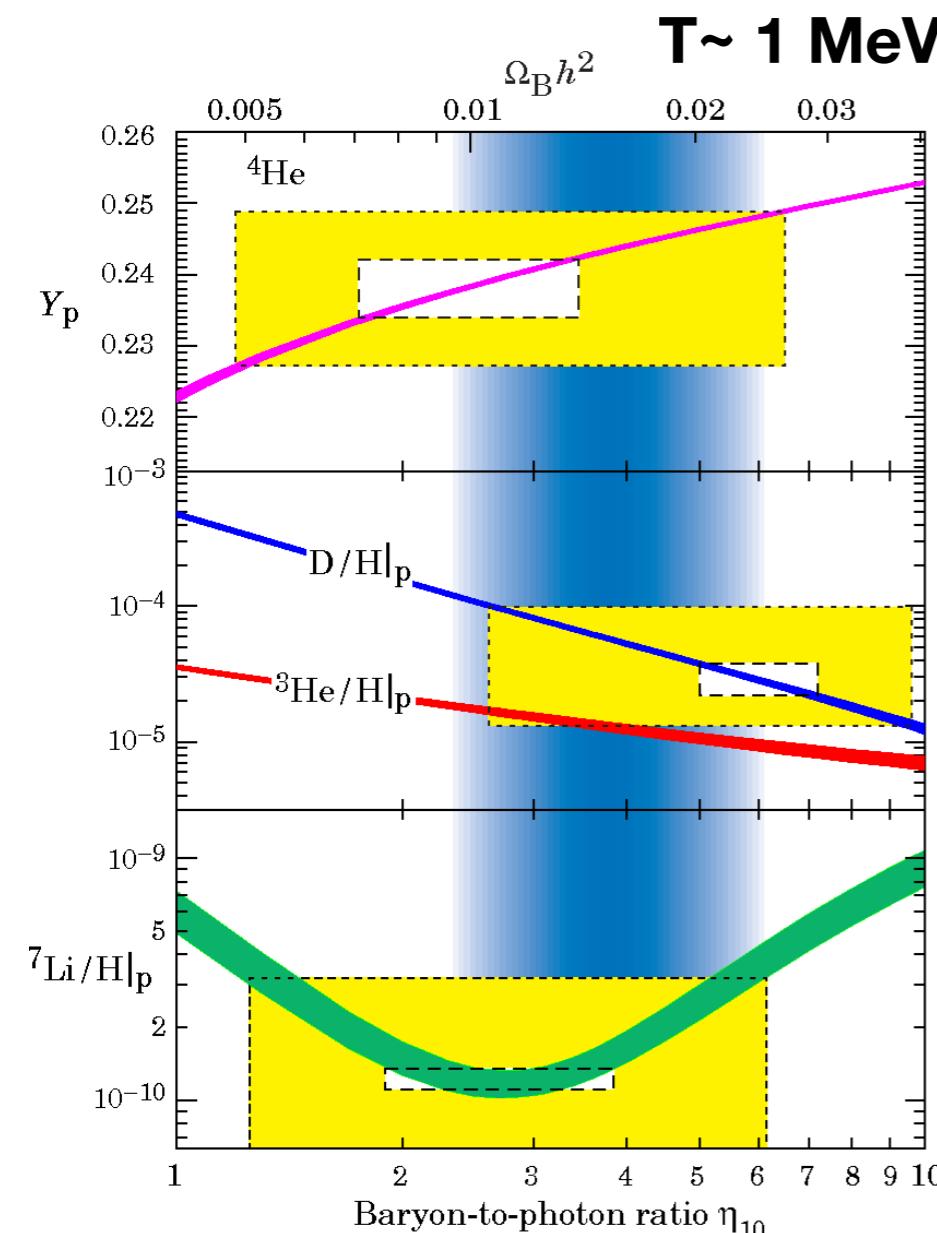


$$M_\nu = \langle H \rangle^2 Y_\Delta \mu_\Delta / M_\Delta^2$$

Neutrino masses connecting another
important problem: leptogenesis

Baryon asymmetry of our universe

Baryon asymmetry of our universe



BBN

$$\eta = \frac{n_b - n_{\bar{b}}}{n_\gamma} \sim 10^{-10}$$

How to generate baryon asymmetry?

Assuming no baryon asymmetry in the beginning
(if any, diluted by inflation)

Sakharov conditions

1. B number violation
2. C and CP violation
3. Out of thermal equilibrium

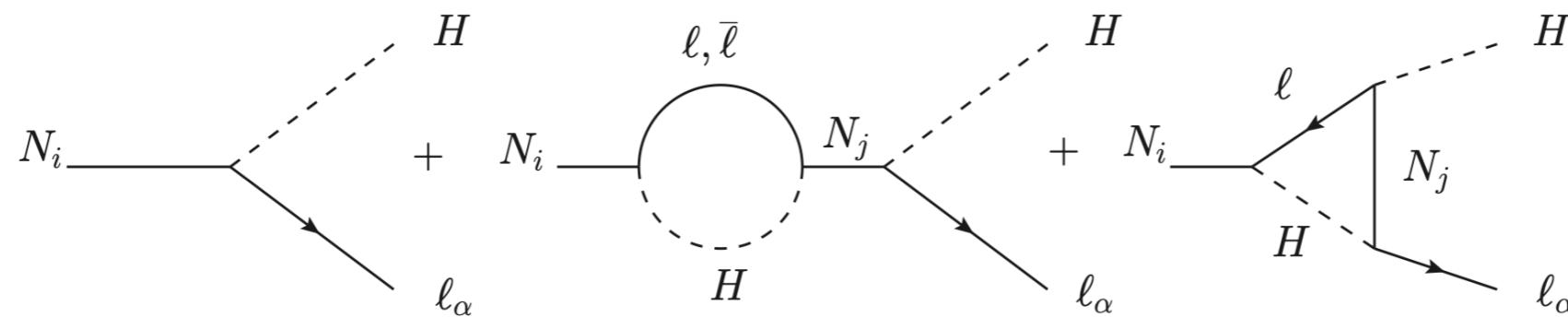
SM has (1) (2) but not enough CP violation, (3) does not

CP violation in neutrino sector  Baryogenesis via leptogenesis

Baryogenesis via leptogenesis from Type I seesaw

Baryogenesis Without Grand Unification (4000 citations),
Fukugita and Yanagida, 1986'

$$\mathcal{L}_I = \mathcal{L}_{SM} + i\overline{N_{R_i}}\partial N_{R_i} - \left(\frac{1}{2}M_i\overline{N_{R_i}^c}N_{R_i} + \epsilon_{ab}Y_{\alpha i}\overline{N_{R_i}}\ell_\alpha^a H^b + h.c. \right)$$



$$\epsilon_{i\alpha} = \frac{\gamma(N_i \rightarrow \ell_\alpha H) - \gamma(N_i \rightarrow \overline{\ell}_\alpha H^*)}{\sum_\alpha \gamma(N_i \rightarrow \ell_\alpha H) + \gamma(N_i \rightarrow \overline{\ell}_\alpha H^*)}$$

$$n_B = \frac{28}{79}(\mathcal{B} - \mathcal{L})_i$$

Generally N mass $> 10^8$ GeV, difficult to probe

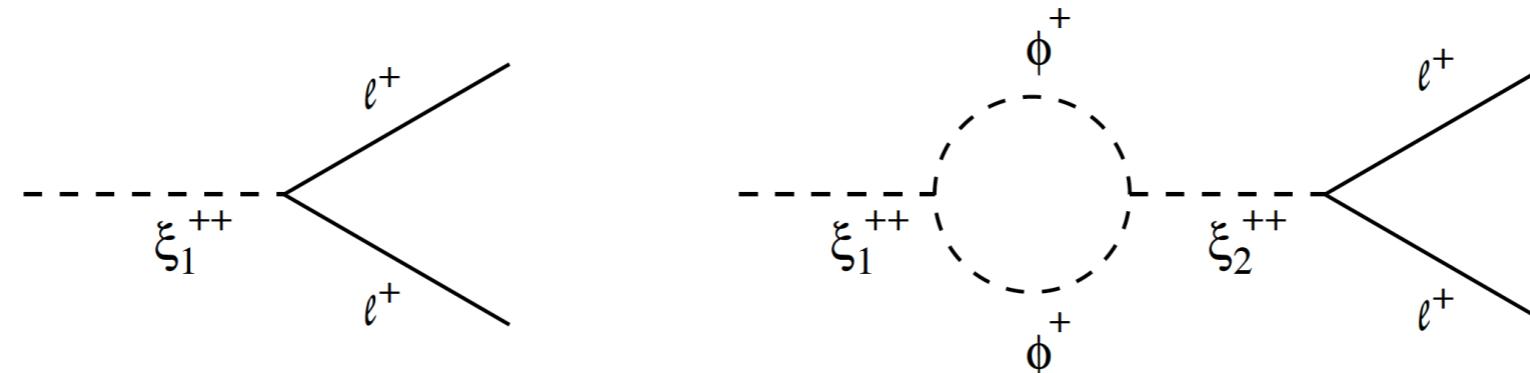
How about type II seesaw leptogenesis?

Leptogenesis from type II seesaw?

Type II seesaw

Neutrino Masses and Leptogenesis with Heavy Higgs Triplets (**533 citations**),
E. Ma, U. Sarkar, Phys.Rev.Lett. 80 (1998) 5716-5719

$M \sim 10^{13}$ GeV



$$\delta_i = 2 [B(\psi_i^- \rightarrow ll) - B(\psi_i^+ \rightarrow l^c l^c)]$$

$$\delta_i = \frac{Im \left[\mu_1 \mu_2^* \sum_{k,l} y_{1kl} y_{2kl}^* \right]}{8\pi^2 (M_1^2 - M_2^2)} \left[\frac{M_i}{\Gamma_i} \right]$$

At least two triplet Higgs are needed to generate the baryon asymmetry
But one triplet Higgs is enough to give neutrino masses

Leptogenesis from type II seesaw?



Physics Reports

Volume 466, Issues 4–5, September 2008, Pages 105-177



Leptogenesis (1,016 citations)

Sacha Davidson ^a  , Enrico Nardi ^{b, c}  , Yosef Nir ^{d, 1}  

To calculate ϵ_T , one should use the Lagrangian terms given in eqn (2.15). While a single triplet is enough to produce three light massive neutrinos, there is a problem in leptogenesis if indeed this is the only source of neutrino masses: The asymmetry is generated only at higher loops and in unacceptably small.

It is still possible to produce the required lepton asymmetry from a single triplet scalar decays if there are additional sources for the neutrino masses, such as type I, type III, or type II contributions from

**One triplet Higgs can not generate leptogenesis!
but it is enough to give neutrino masses!**

Leptogenesis from type II seesaw

PHYSICAL REVIEW LETTERS 128, 141801 (2022)

Affleck-Dine Leptogenesis from Higgs Inflation

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We find that the triplet Higgs of the type-II seesaw mechanism can simultaneously generate the neutrino masses and observed baryon asymmetry while playing a role in inflation. We survey the allowed parameter space and determine that this is possible for triplet masses as low as a TeV, with a preference for a small vacuum expectation value for the triplet $v_\Delta < 10$ keV. This requires that the triplet Higgs must decay dominantly into the leptonic channel. Additionally, this model will be probed at the future 100 TeV collider, upcoming lepton flavor violation experiments such as Mu3e, and neutrinoless double beta decay experiments. Thus, this simple framework provides a unified solution to the three major unknowns of modern physics— inflation, the neutrino masses, and the observed baryon asymmetry—while simultaneously providing unique phenomenological predictions that will be probed terrestrially at upcoming experiments.

Affleck-Dine mechanism

Assuming phi is a complex scalar with B/L charge

$$V(\phi) = \frac{1}{2}m^2|\phi|^2 + [c_{n,m}\phi^n(\phi^*)^m + h.c] \quad m \neq n$$

↓

(B violation)

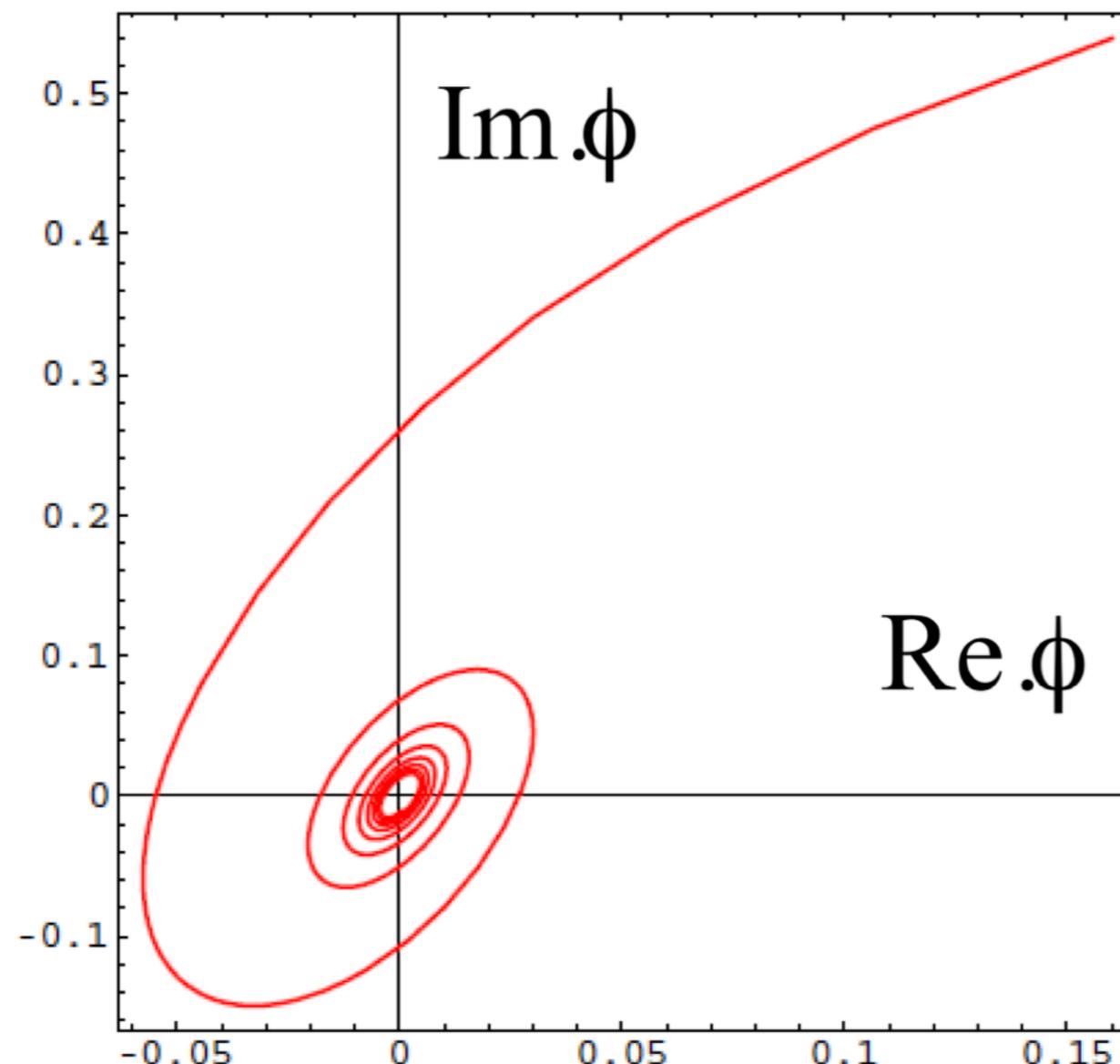
$$j_B^\mu = i(\phi^*\partial^\mu\phi - \phi\partial^\mu\phi^*)$$

ϕ is spatially constant

$$n_B = i(\phi^*\dot{\phi} - \phi\dot{\phi}^*) = \rho_\phi^2\dot{\theta} \quad \phi = \frac{1}{\sqrt{2}}\rho_\phi e^{i\theta}$$

A motion of theta will generate baryon number

Affleck-Dine mechanism



CP is spontaneously broken by $\langle \phi \rangle$

Affleck-Dine mechanism

Three conditions for Affleck-Dine mechanism

Type II seesaw

- Scalar particle with initial displaced vacuum ?
- Scalar particle taking B/L charge ✓
- Small B/L violation term in the potential ✓

Combing the idea of inflation with A-D mechanism

Three conditions for Affleck-Dine mechanism

If the scalar plays the role of inflation

Type II seesaw

● Scalar particle with initial displaced vacuum



● Scalar particle taking B/L charge



● Small B/L violation term in the potential



SM+Type II seesaw

To be consistent with inflation, we need add non-minimal couplings

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2}M_P^2 R - \boxed{f(H, \Delta)R} - g^{\mu\nu}(D_\mu H)^\dagger(D_\nu H) \\ - g^{\mu\nu}(D_\mu \Delta)^\dagger(D_\nu \Delta) - V(H, \Delta) + \mathcal{L}_{\text{Yukawa}}$$

$$h \equiv \frac{1}{\sqrt{2}}\rho_H e^{i\eta} \quad \Delta^0 \equiv \frac{1}{\sqrt{2}}\rho_\Delta e^{i\theta}$$

$$F(H, \Delta) = \xi_H |h|^2 + \xi_\Delta |\Delta^0|^2 = \frac{1}{2}\xi_H \rho_H^2 + \frac{1}{2}\xi_\Delta \rho_\Delta^2$$

SM+Type II seesaw

During inflation(Oleg Lebedev and Hyun Min Lee, arXiv:1105.2284)

$$\frac{\rho_H}{\rho_\Delta} \equiv \tan \alpha = \sqrt{\frac{2\lambda_\Delta \xi_H - \lambda_{H\Delta} \xi_\Delta}{2\lambda_H \xi_\Delta - \lambda_{H\Delta} \xi_H}}$$

$$\rho_H = \varphi \sin \alpha, \quad \rho_\Delta = \varphi \cos \alpha$$

$$\xi \equiv \xi_H \sin^2 \alpha + \xi_\Delta \cos^2 \alpha$$

Similar to SUSY case, but mixing with a general angle

SM+Type II seesaw

Finally the model can be simplified as

$$\begin{aligned}\frac{\mathcal{L}}{\sqrt{-g}} = & -\frac{M_p^2}{2}R - \frac{\xi}{2}\varphi^2 R - \frac{1}{2}g^{\mu\nu}\partial_\mu\varphi\partial_\nu\varphi \\ & -\frac{1}{2}\varphi^2\cos^2\alpha g^{\mu\nu}\partial_\mu\theta\partial_\nu\theta - V(\varphi, \theta)\end{aligned}$$

$$V(\varphi, \theta) = \frac{1}{2}m^2\varphi^2 + \frac{\lambda}{4}\varphi^4 + 2\varphi^3\left(\tilde{\mu} + \frac{\tilde{\lambda}_5}{M_p}\varphi^2\right)\cos\theta$$

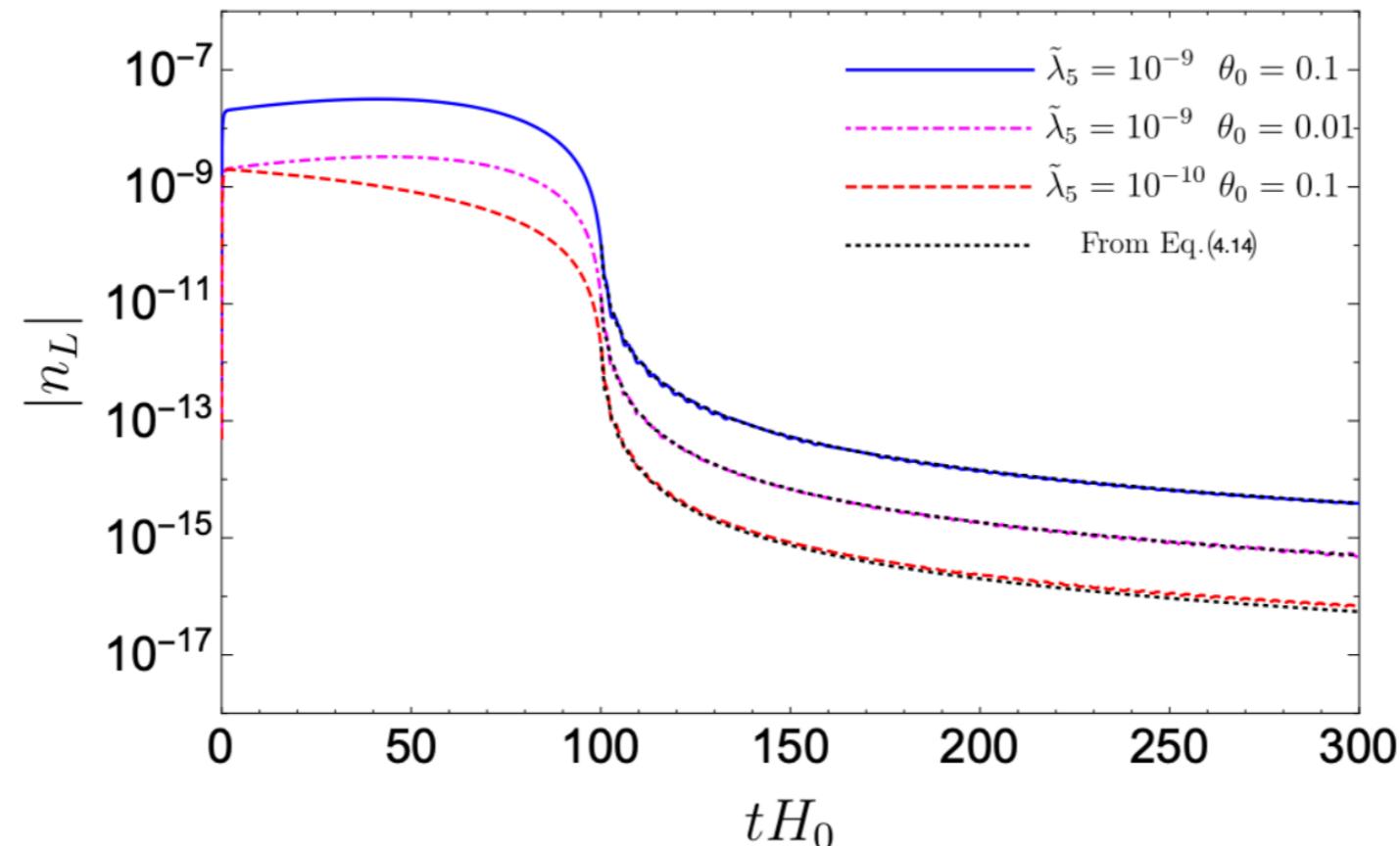
We need keep the theta term, because

$$n_L = Q_L\varphi^2\dot{\theta}\cos^2\alpha$$

Lepton number generation

$$\xi = 300, \lambda = 4.5 \cdot 10^{-5}$$

$$\chi_0 = 6.0M_p, \dot{\chi}_0 = 0, \text{ and } \theta_0 = 0$$



- 暴胀开始轻子数为0
- 轻子数在暴胀过程中产生
- 暴胀结束后轻子数守恒

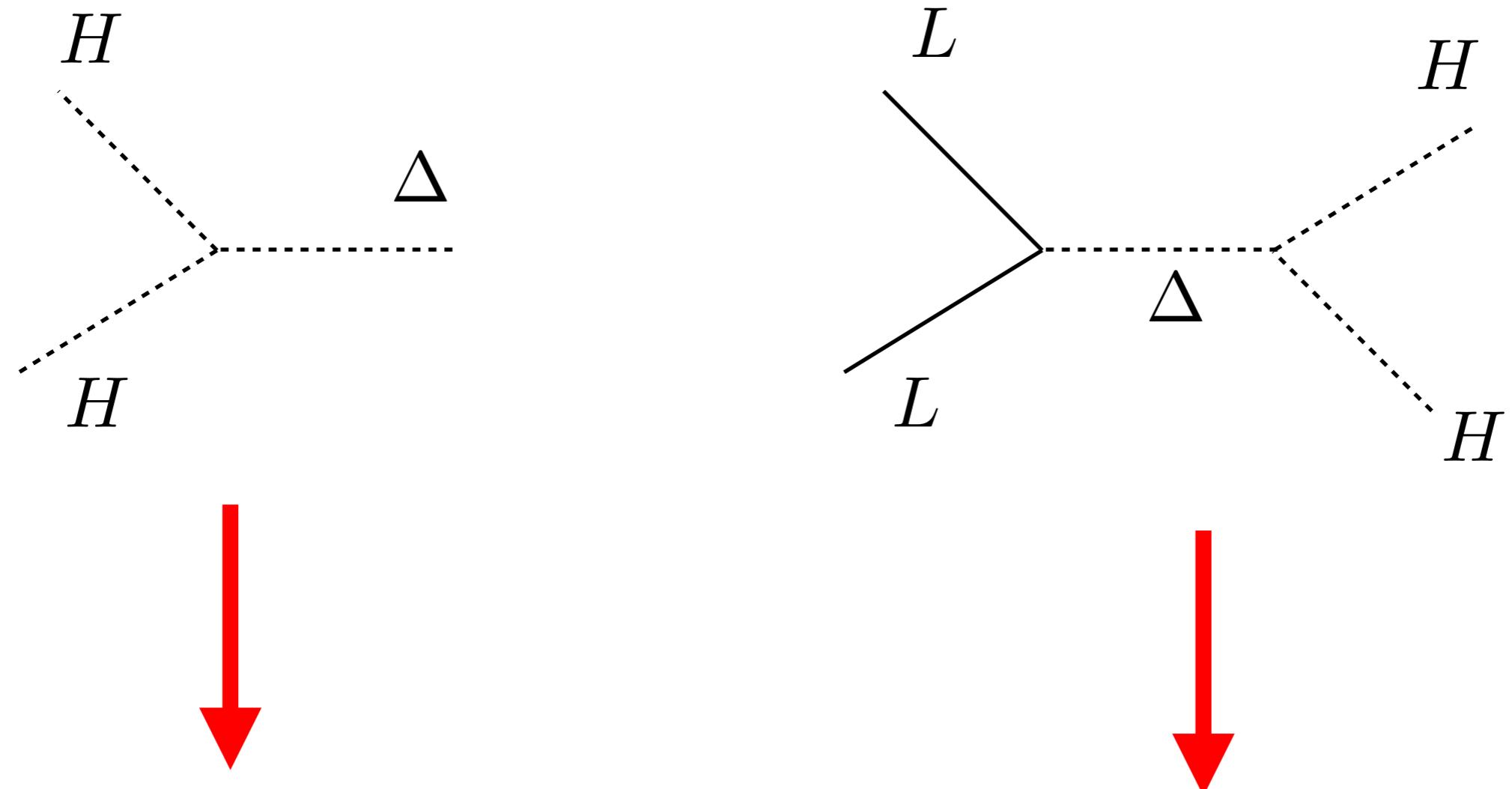
SM+Type II seesaw

$$T_{\text{reh}} \approx 2.2 \cdot 10^{14} \text{ GeV}$$

$$\eta_B = \frac{n_B}{s} \Big|_{\text{reh}} = \eta_B^{\text{obs}} \left(\frac{|n_{L\text{end}}|/M_p^3}{1.3 \cdot 10^{-16}} \right) \left(\frac{g_*}{112.75} \right)^{-\frac{1}{4}}$$

$$\tilde{\lambda}_5 = 7 \cdot 10^{-15} \text{ for } \theta_0 = 0.1$$

Wash out process

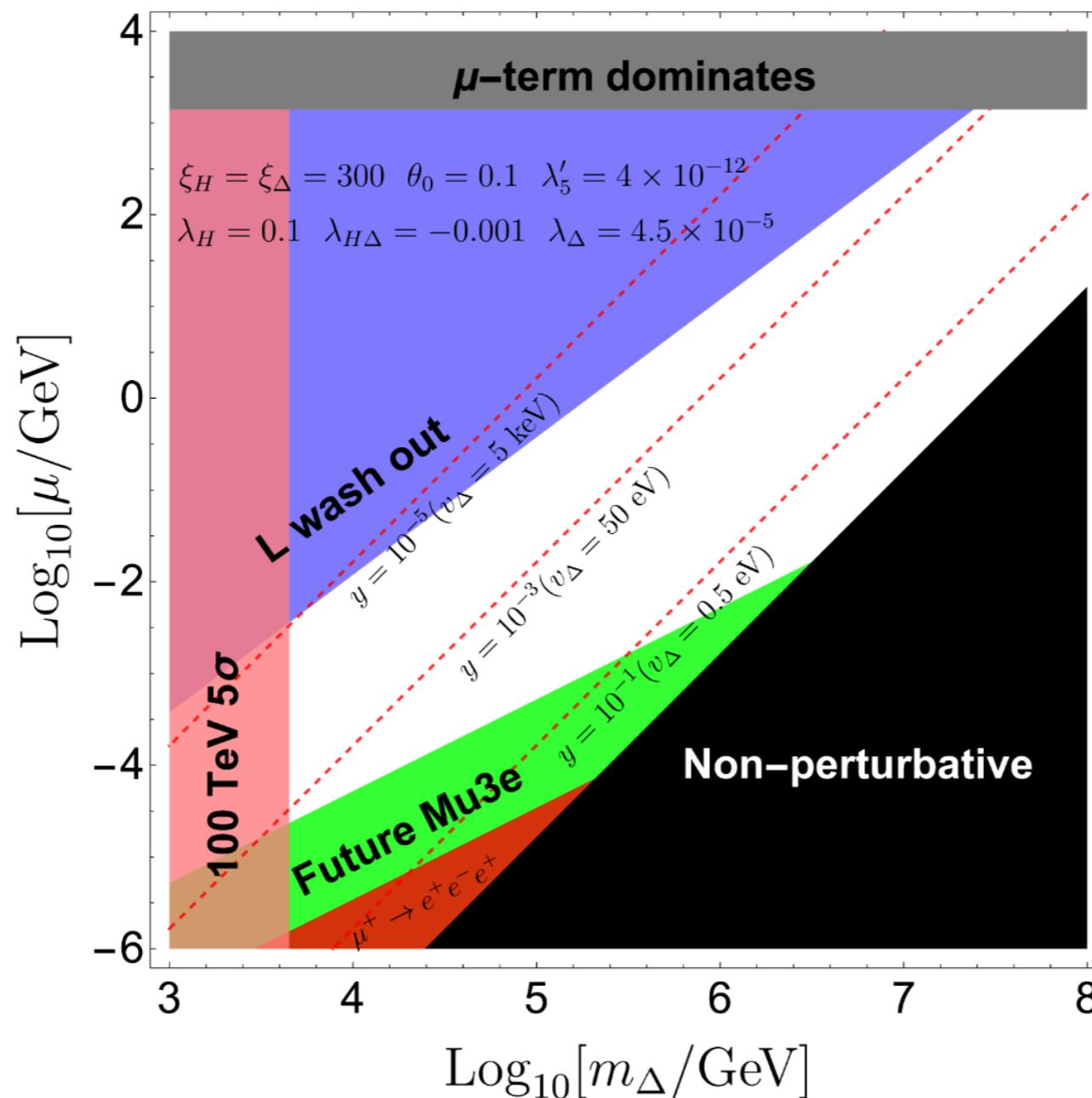


$$\frac{\mu^2}{8\pi m_\Delta} < H(m) = \frac{m_\Delta^2}{M_P}$$

$$m_\Delta < 10^{12} \text{ GeV}$$

A small mu term is preferred

SM+Type II seesaw

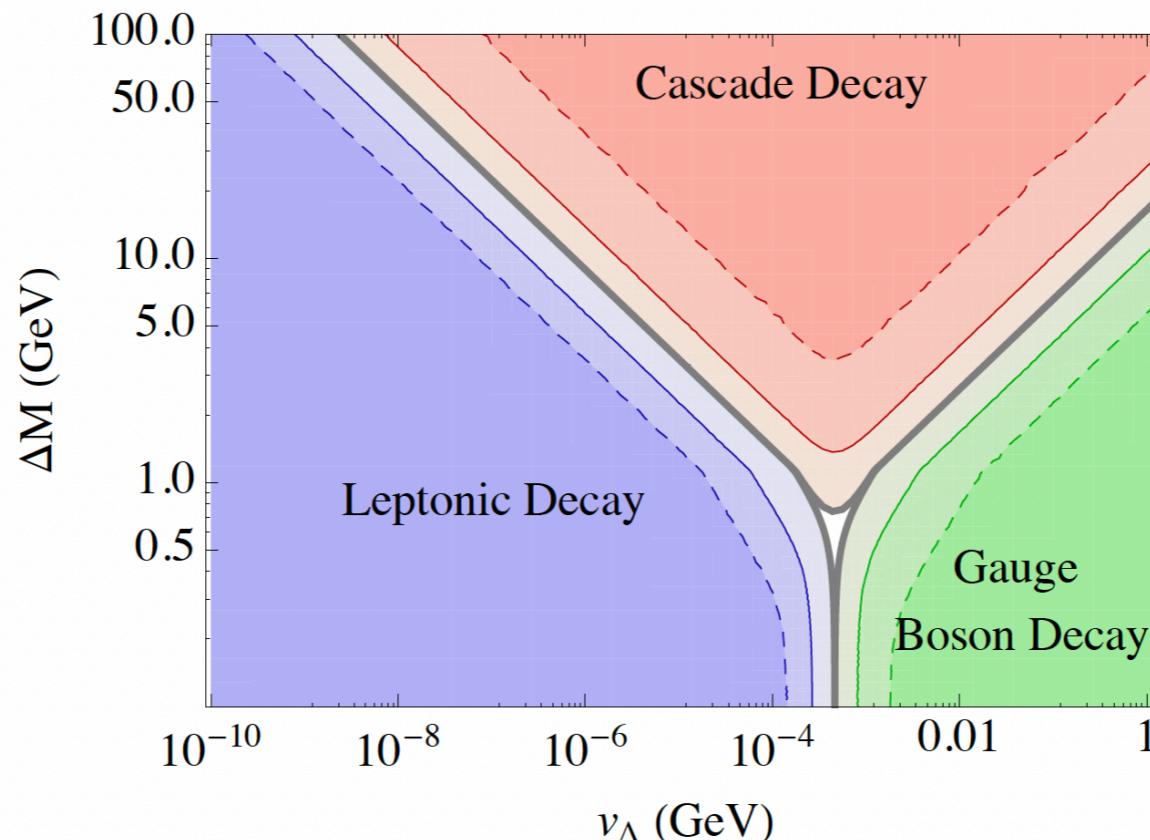


- Triplet Higgs could be as light as TeV
- Vacuum value $< 10 \text{ keV}$, traditional type II seesaw $< 1 \text{ GeV}$

Phenomenology implications I: collider physics

Decay of the doubly-charged Higgs

$$\Delta M = m_{\Delta^{++}} - m_{\Delta^+}$$

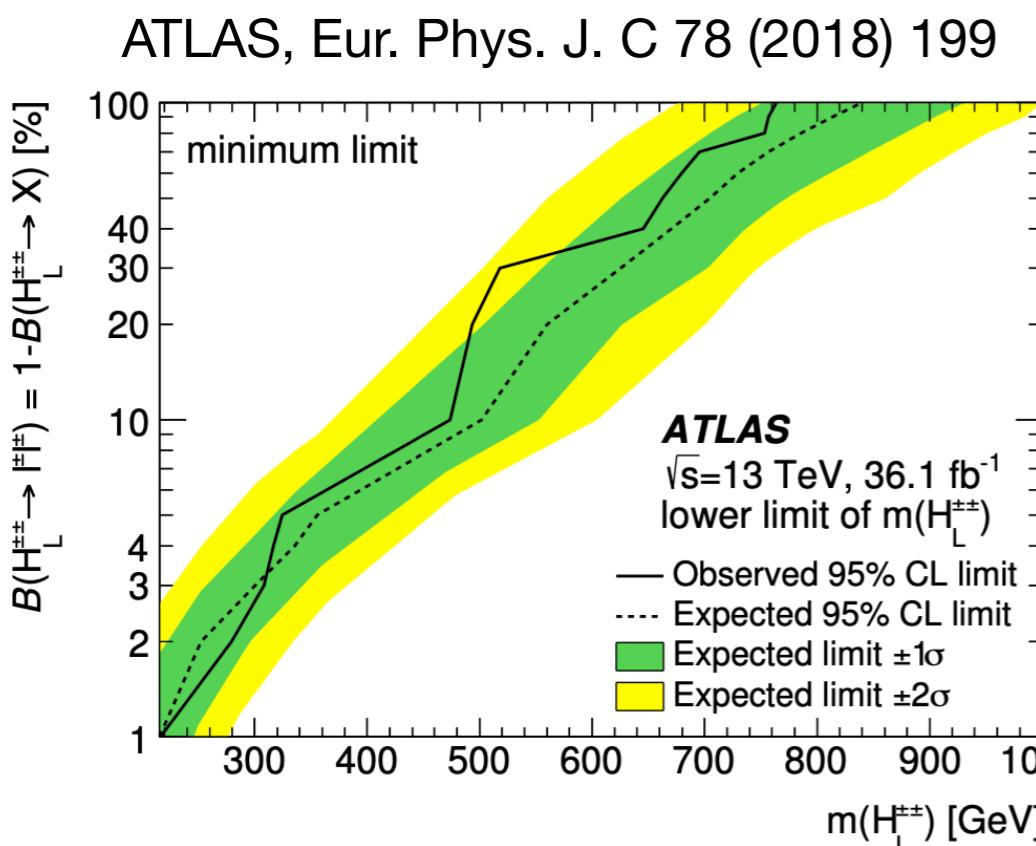


For $\nu > 1 \text{ MeV}$, mainly decay gauge bosons

For $\nu < 0.1 \text{ MeV}$, mainly decay leptons

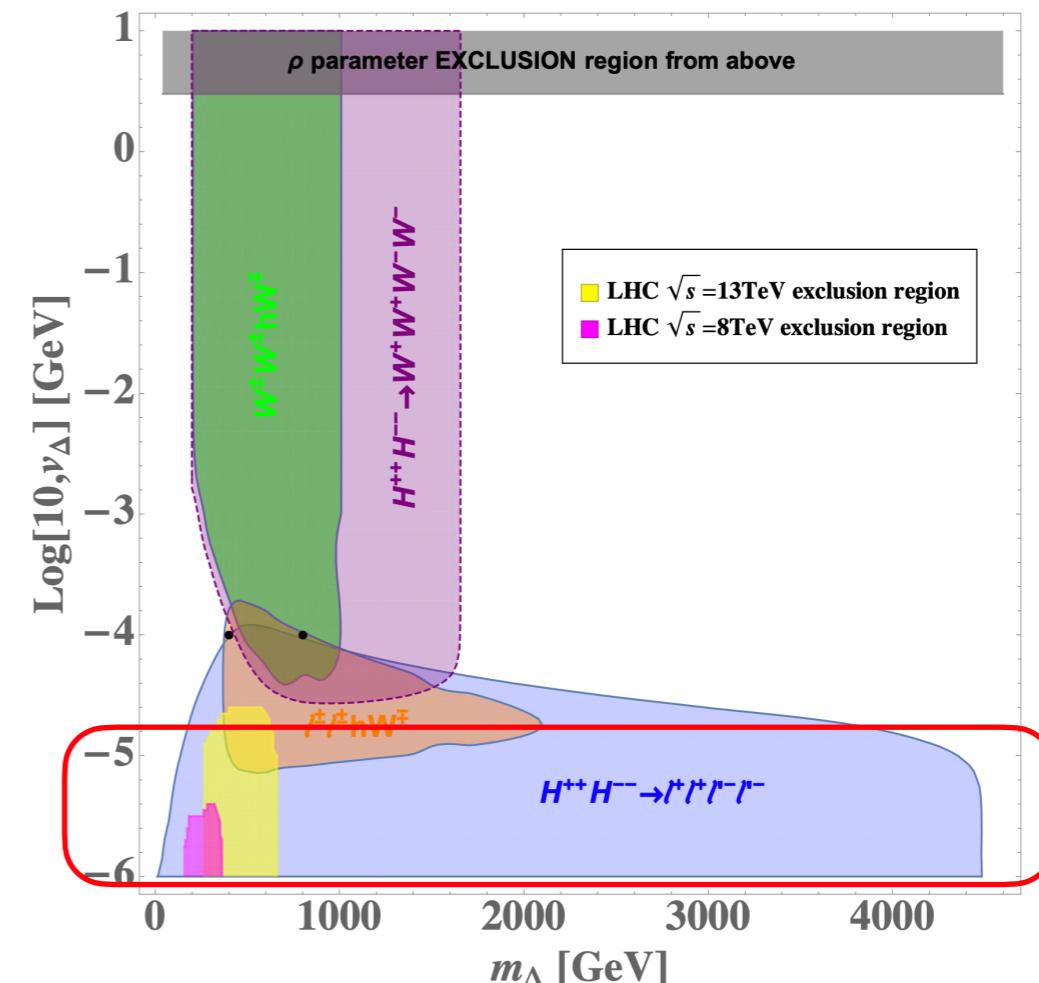
Phenomenology implications I: collider physics

Current limit from LHC



Future reach

Y. Du, A. Dunbrack, M. J. Ramsey-Musolf, J. Yu, JHEP01(2019)101



5 sigma discover region @100 TeV collider

Smoking gun: observing doubly-charged Higgs from leptonic channel

Summary

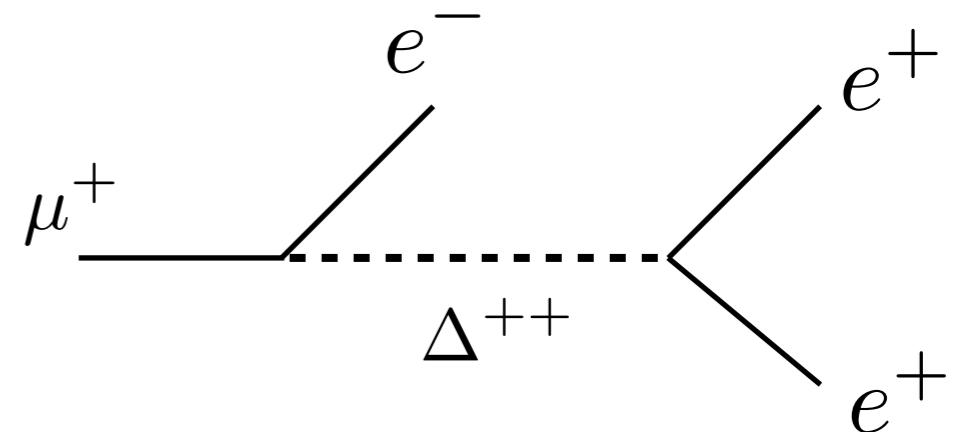
- One simple extension of SM, three problems can be solved: inflation, baryogenesis and neutrino masses
- Unique signatures at collider, LFV violation, neutrino experiments and astronomy observations

Thanks

Back up

Phenomenology implications II: flavor physics

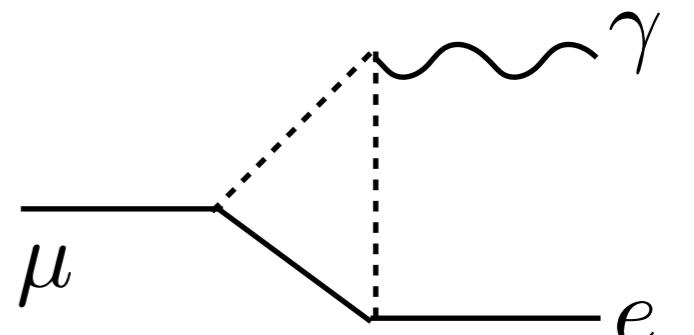
$$\mathcal{B}(\mu^+ \rightarrow e^+ e^- e^+) = \frac{|y_{\mu e} y_{ee}^\dagger|^2}{16 G_F^2 m_{\Delta^{++}}^4}$$



$$\mathcal{B}(\mu^+ \rightarrow e^+ e^- e^+) \leq 1.0 \times 10^{-12}$$

$$\mathcal{B}(\mu \rightarrow e\gamma) \simeq \frac{\alpha}{3072\pi} \frac{|(y^\dagger y)_{e\mu}|^2}{G_F^2} \left(\frac{1}{m_{\Delta^+}^2} + \frac{8}{m_{\Delta^{++}}^2} \right)^2$$

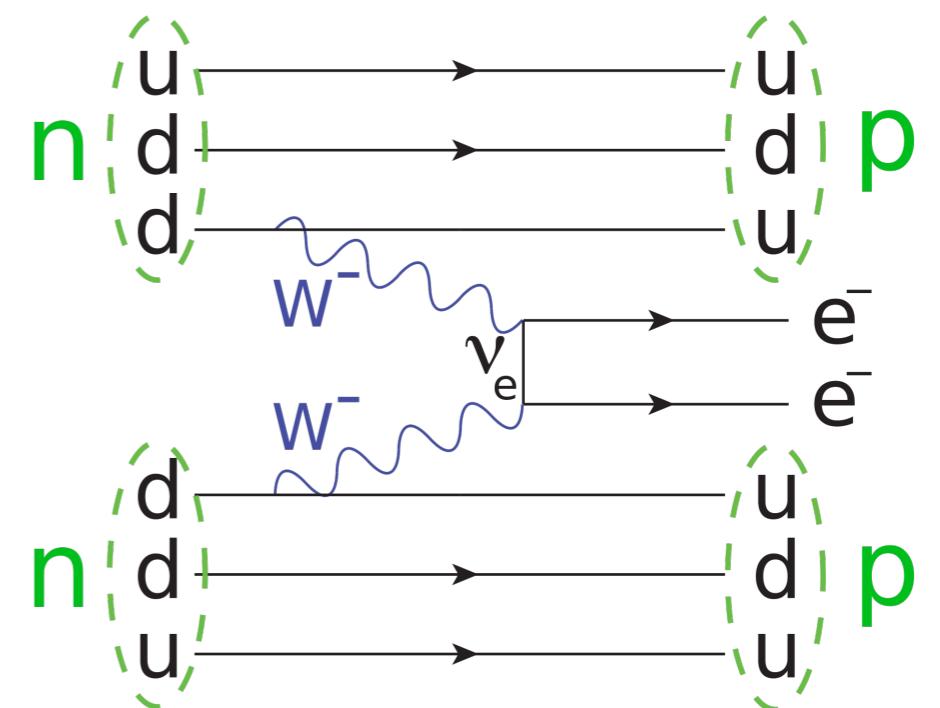
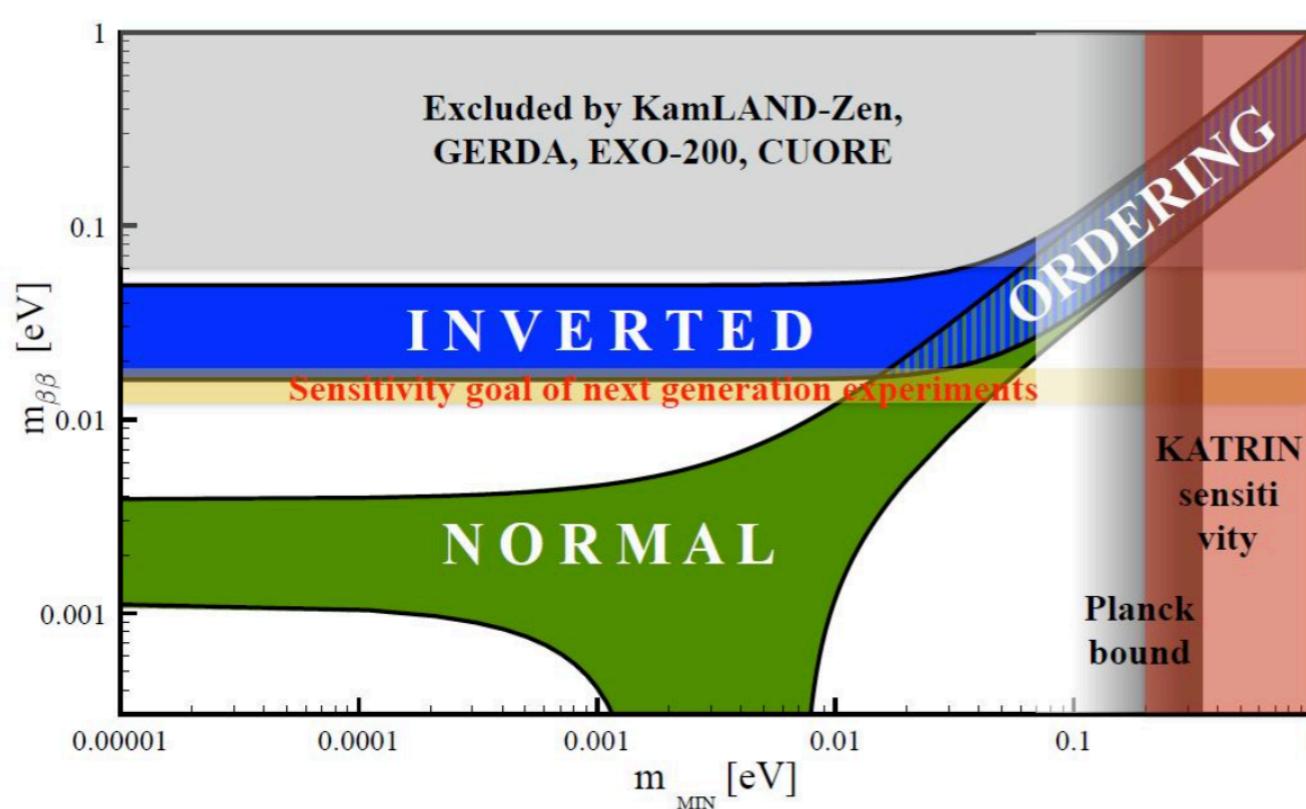
$$\mathcal{B}(\mu \rightarrow e\gamma) < 4.2 \times 10^{-13}$$



Phenomenology implications III: neutrino physics

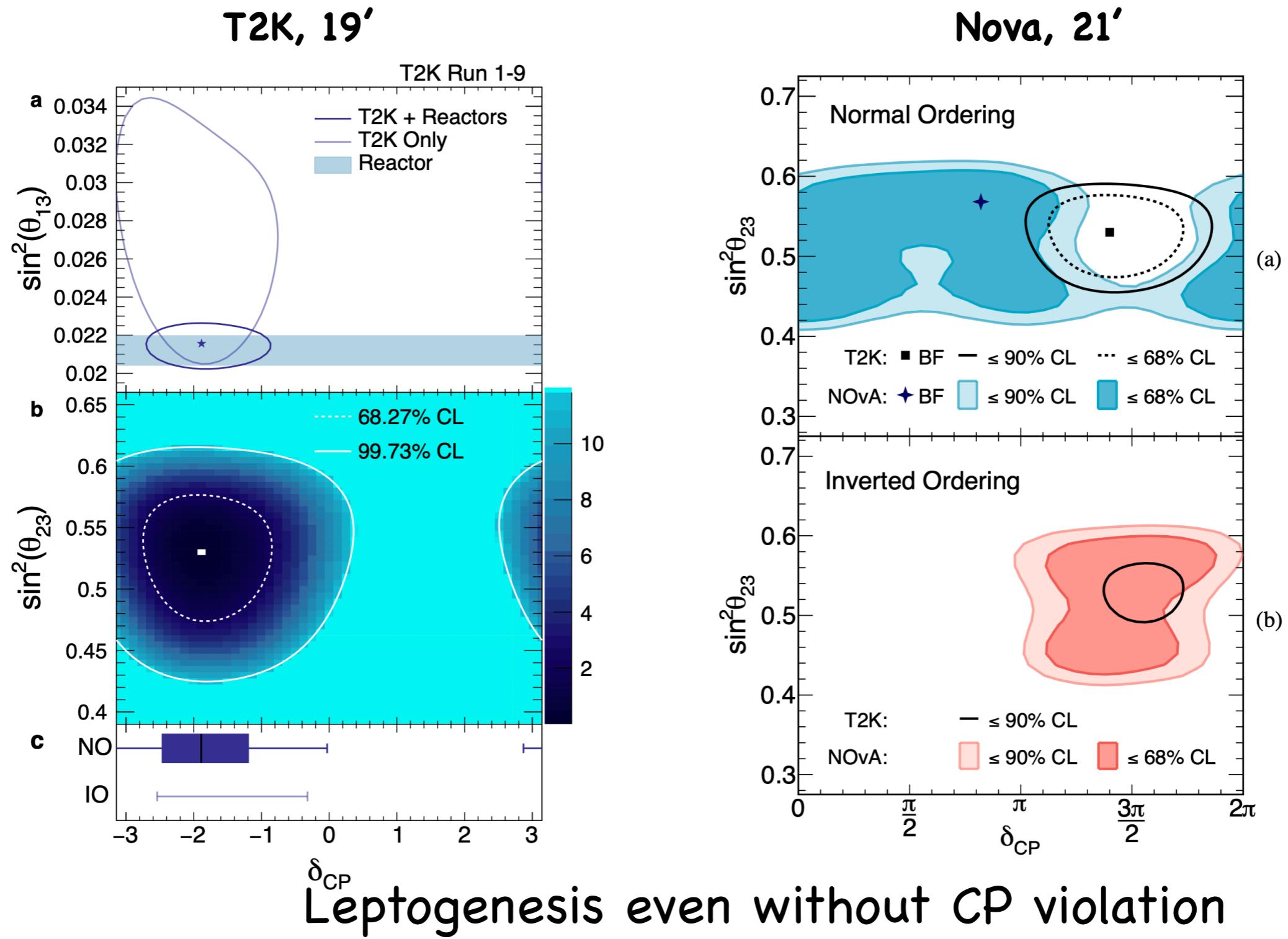
- Neutrino must be majorana type

Neutrinoless double beta decay



Phenomenology implications III: neutrino physics

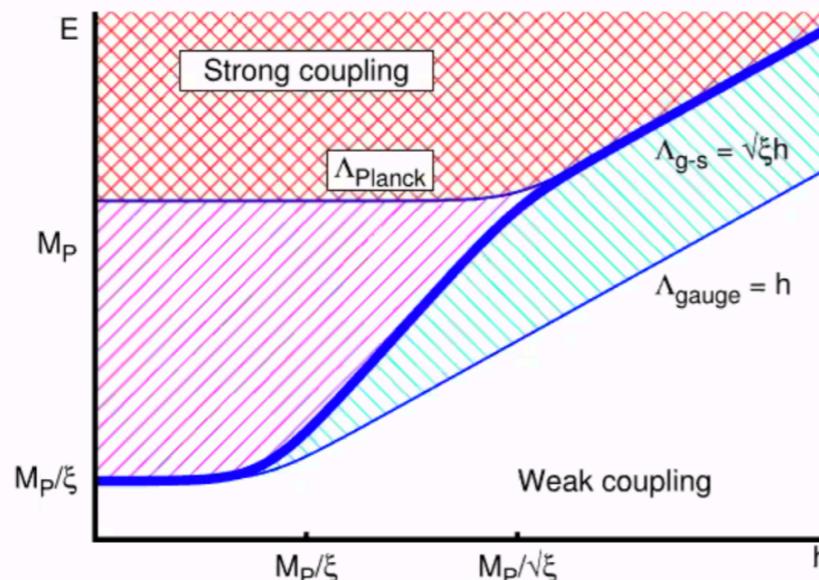
- CP violation in neutrino sector



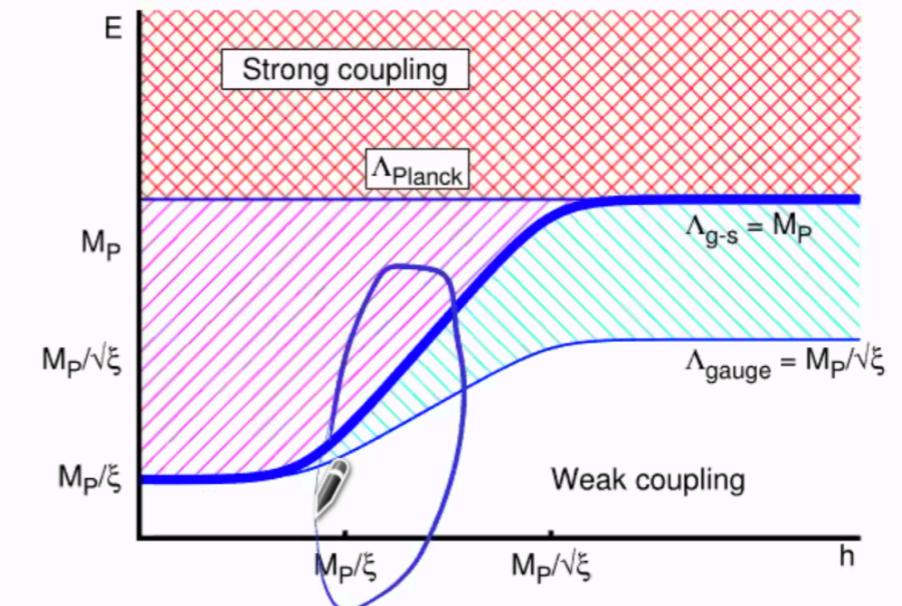
Unitary problem for Higgs inflation

Cut-off grows with the field background

Jordan frame



Einstein frame



Relation between cut-offs in different frames:

$$\Lambda_{\text{Jordan}} = \Lambda_{\text{Einstein}} \Omega$$

Relevant scales at inflation

$$\text{Hubble scale } H \sim \lambda^{1/2} \frac{M_P}{\xi}$$

Energy density at inflation

$$V^{1/4} \sim \lambda^{1/4} \frac{M_P}{\sqrt{\xi}}$$

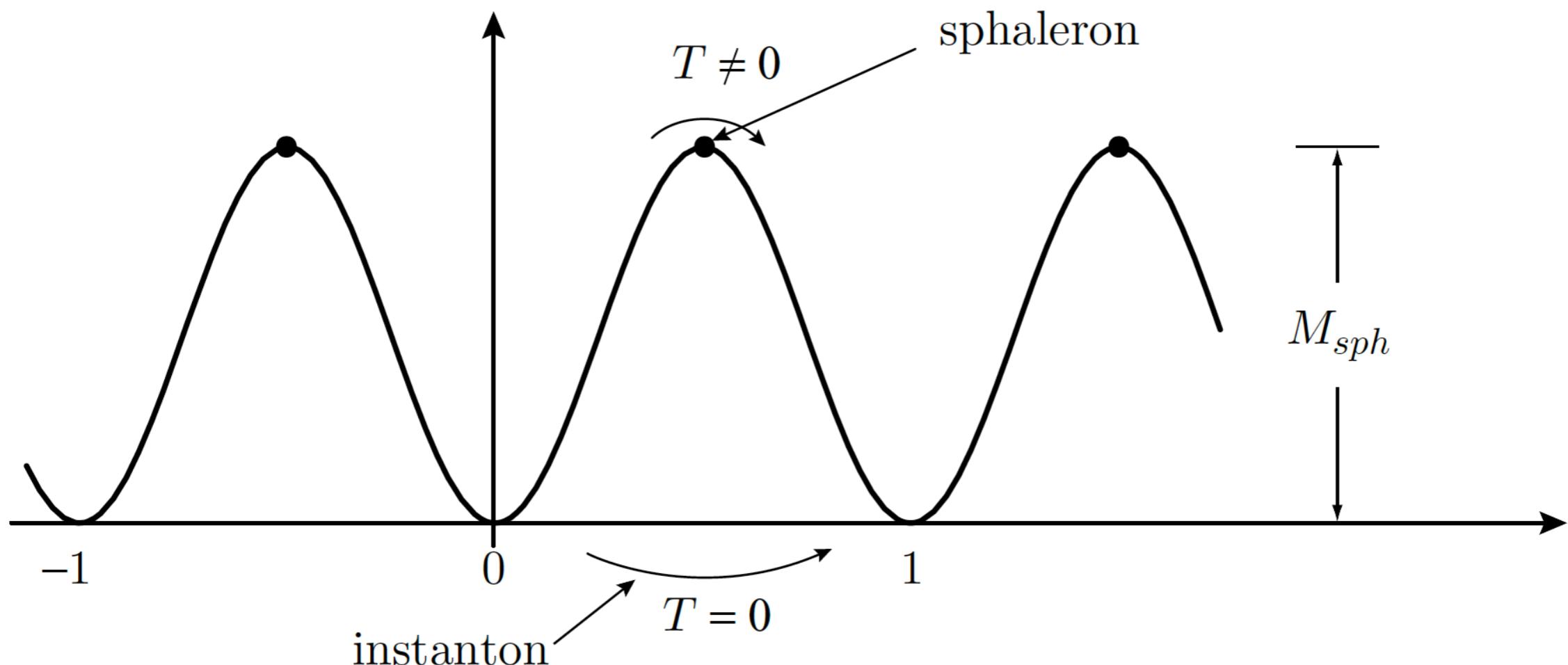
Reheating temperature $M_P/\xi < T_{\text{reheating}} < M_P/\sqrt{\xi}$

Problems during reheating

Instanton, sphaleron process

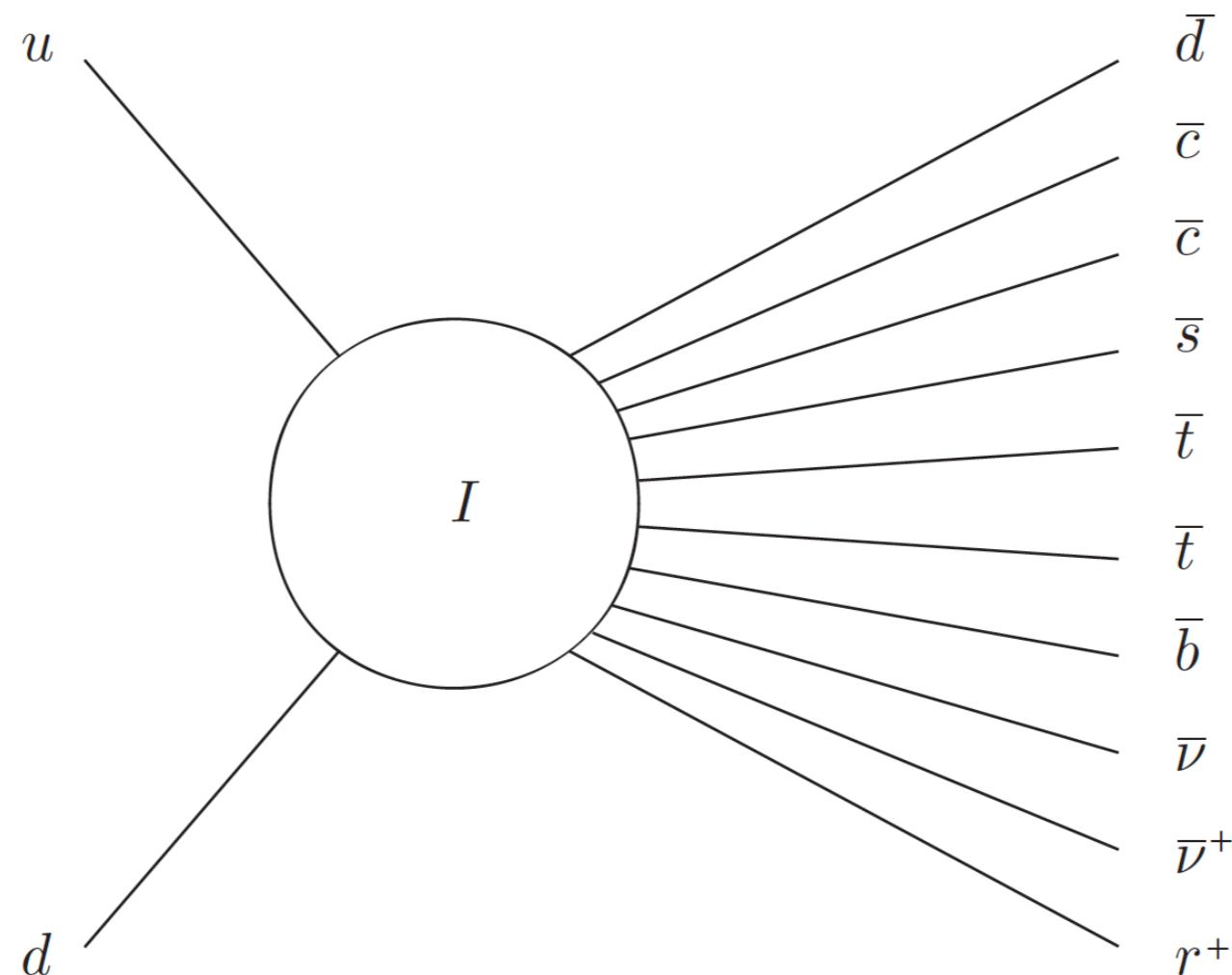
Effective for $T > 100$ GeV

$$\exp\left(-\frac{M_{sph}(T)}{T}\right) \sim \exp\left(-2\pi \frac{M_W(T)}{\alpha_w T}\right)$$



$$\Gamma \propto \exp\left(-\frac{4\pi}{\alpha}\right)$$

Instanton, sphaleron



Baryon asymmetry via leptogenesis

1. the sphaleron interactions themselves:

$$\sum_i (3\mu_{q_i} + \mu_{\ell_i}) = 0$$

2. a similar relation for QCD sphalerons:

$$\sum_i (2\mu_{q_i} - \mu_{u_i} - \mu_{d_i}) = 0.$$

3. vanishing of the total hypercharge of the universe:

$$\sum_i (\mu_{q_i} - 2\mu_{\bar{u}_i} + \mu_{\bar{d}_i} - \mu_{\ell_i} + \mu_{\bar{e}_i}) + \frac{2}{N}\mu_H = 0$$

4. the quark and lepton Yukawa couplings give relations:

$$\mu_{q_i} - \mu_\phi - \mu_{d_j} = 0, \quad \mu_{q_i} - \mu_\phi - \mu_{u_j} = 0, \quad \mu_{\ell_i} - \mu_\phi - \mu_{e_j} = 0.$$

$$B = \frac{8N+4}{22N+13}(\mathcal{B} - \mathcal{L})_i$$