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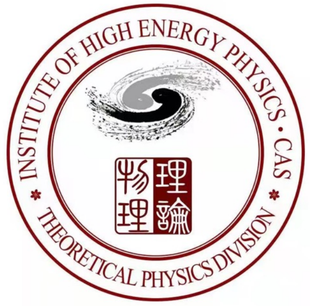

Pulsar Polarization Arrays

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第三届粒子物理前沿研讨会

July 23, 2022

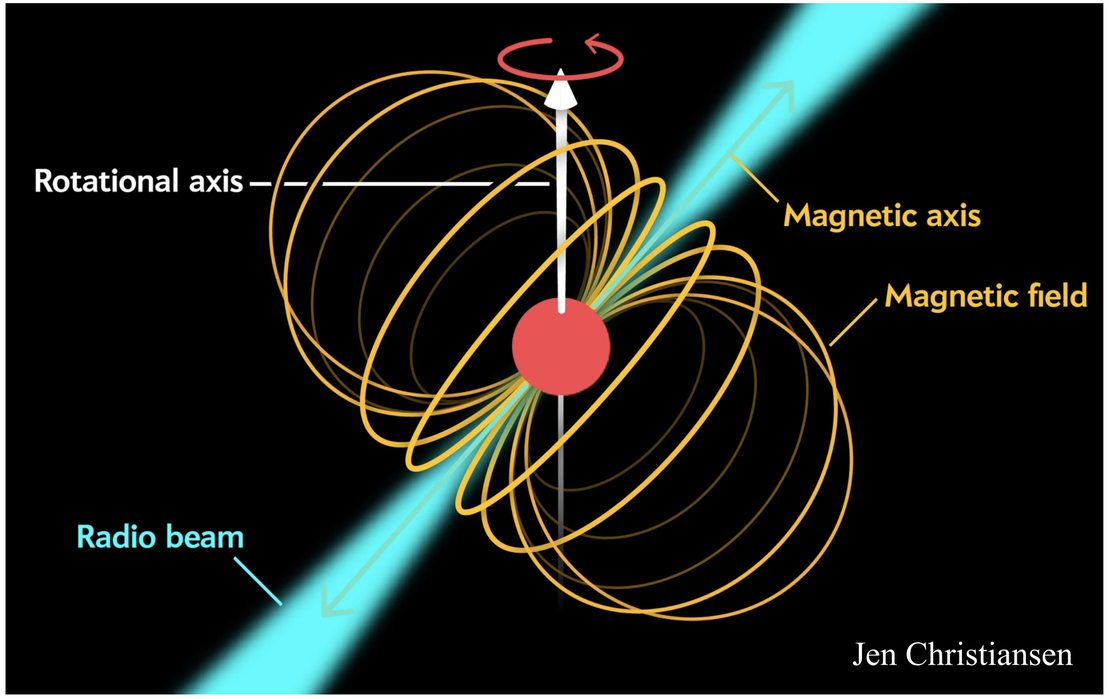
Based on work with Tao Liu, Xuzixiang Lou, arXiv: 2111.10615

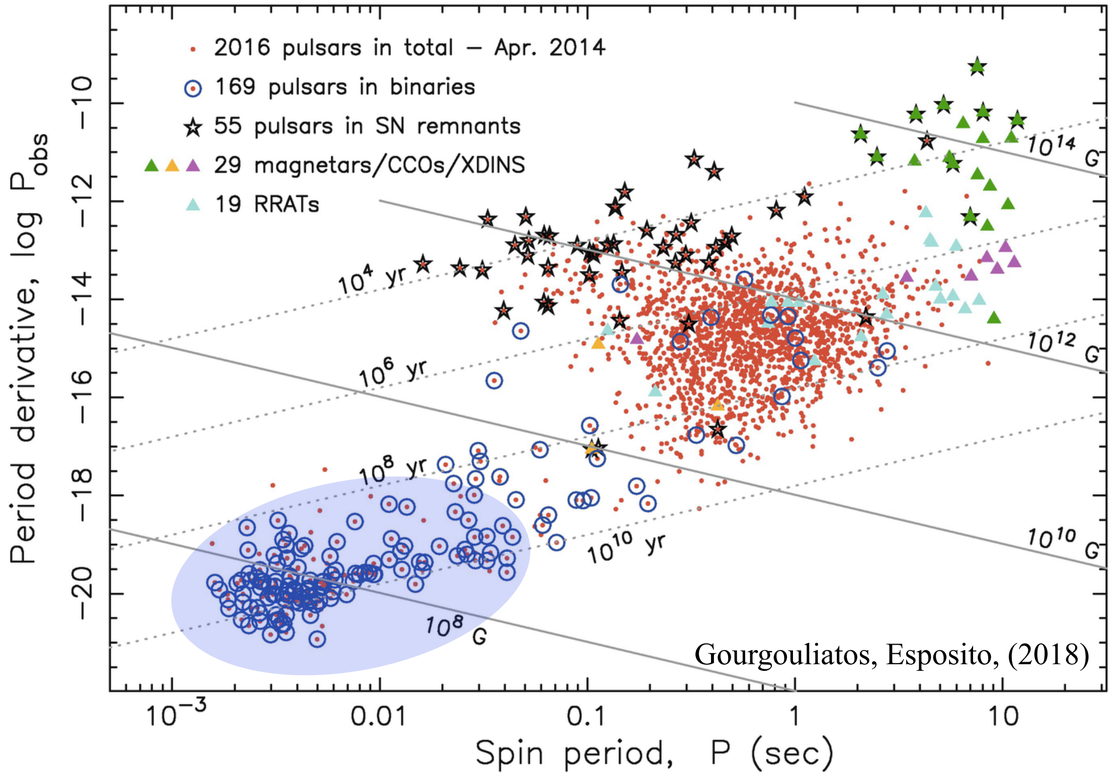
Content

- Pulsar timing arrays (PTAs) and pulsar polarization arrays (PPAs)
- Ultralight axion-like dark matter (ALDM)
- Ultralight ALDM detection by PPAs through cosmic birefringence

Pulsars

- Pulsars emit electromagnetic pulses with extraordinary regularity, with the period ranging from milliseconds to seconds. Up to now about 3000 pulsars observed in our galaxy
- Millisecond pulsars (MSPs) are especially stable due to mass and angular momentum transfer from a companion. Although emission mechanism not fully clarified, they play significant roles as astronomical clocks





Pulsar timing arrays (PTAs)

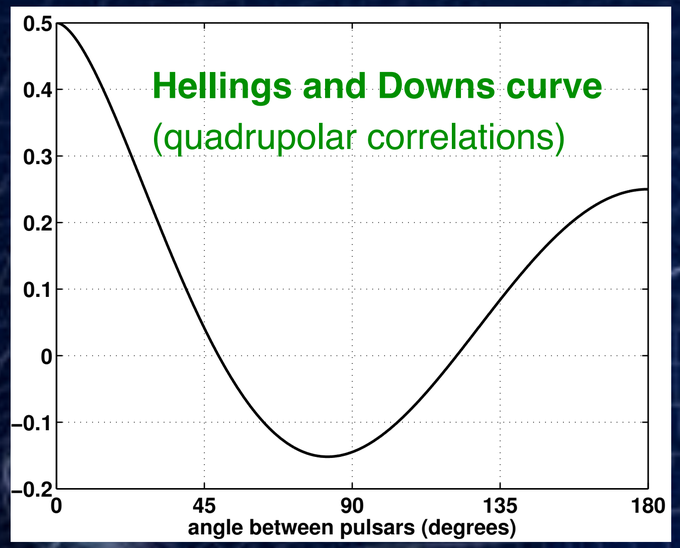
- Global PTA network monitors over 80 MSPs in the timespan of years. FAST/SKA may increase the number to the order of 1000

- Given precise timing model of the expected time of arrival of the pulse, the measured **time difference** can be directly related to **gravitational waves (GWs)**

$$\Delta T(t) = \int_{-\infty}^{\infty} df \frac{1}{2} u^a u^b h_{ab}(f,\hat{n})\, e^{i2\pi f(t+\hat{n}\cdot\vec{r}_2/c)} \frac{1}{i2\pi f} \frac{1}{1+\hat{n}\cdot\hat{u}} \left[1 - e^{-\frac{i2\pi f L}{c}(1+\hat{n}\cdot\hat{u})}\right]$$

metric perturbation — "Earth" — "pulsar"

- PTAs with MSPs in different directions serve as **galactic interferometers** to measure nHZ GWs. Stochastic GW backgrounds (SGWBs) can be identified by the **quadrupolar spatial correlations among pulsars**

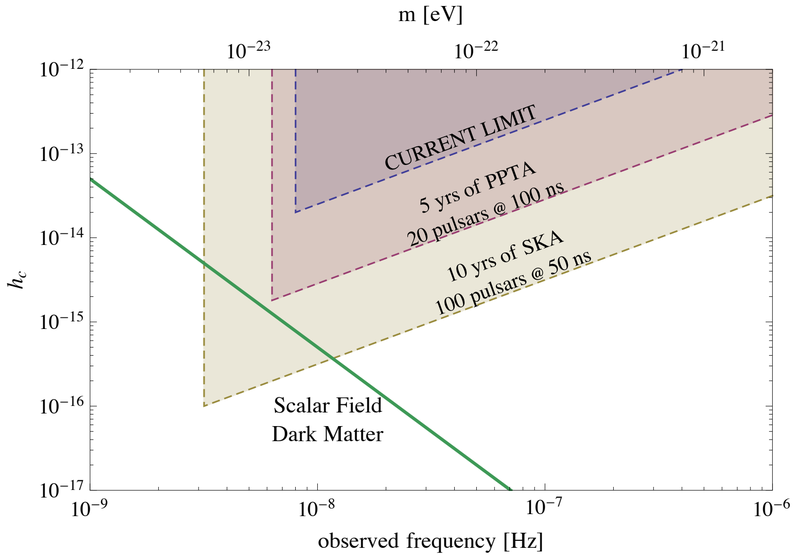


Pulsar timing arrays (PTAs)

Recently, the explorations on the PTA targets extended to dark matter (DM) physics

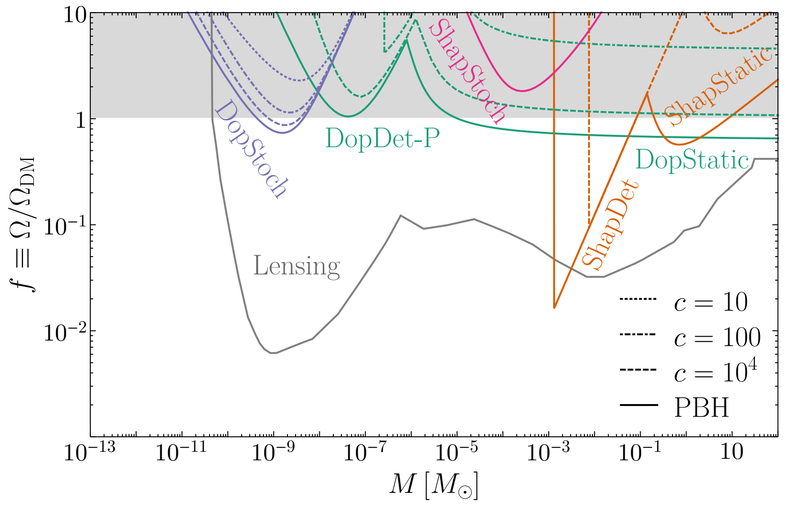
Oscillating gravitational potential induced by ultralight scalar DM

Khmelnitsky and Rubakov, 1309.5888; De Martino et al. 1705.04367; Porayko et al., 1810.03227



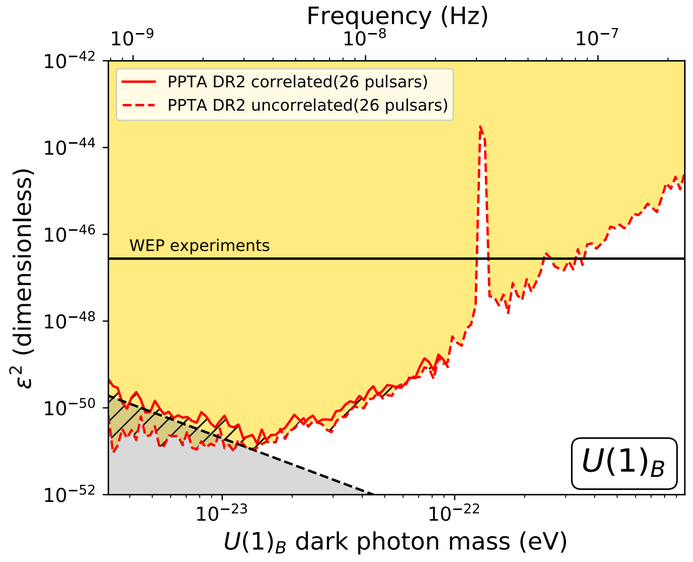
Doppler/Shapiro effects induced by transiting objects associated with DM substructure

Zurek et al., 1901.04490, 2005.03030, 2104.05717



Oscillating fifth force induced by ultralight dark photon DM

Xue et al. [PPTA], 2112.07687

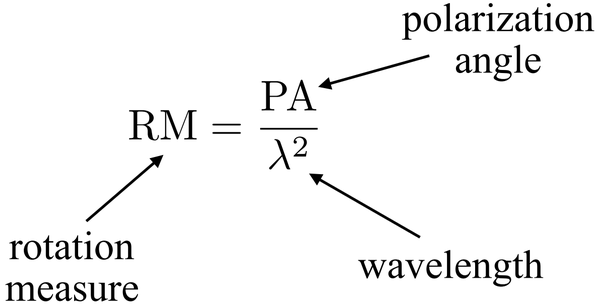


Pulsar polarization arrays (PPAs)

- Pulsar radio emissions typically have strong linear polarization

#	NAME		P0 (s)			DM (cm^-3 pc)			RM (rad m^-2)			DIST (kpc)
1	J0002+6216	cwp+17	0.1153635682680	14	cwp+17	218.6	6	wcp+18	*	0	*	6.357
2	J0006+1834	cnt96	0.69374767047	14	cn95	11.41	55	bkk+16	-20	3	npn+20	0.860
3	J0007+7303	aaa+09c	0.3158731909	3	awd+12	*	0	*	*	0	*	1.400
4	J0011+08	dsm+16	2.55287	0	dsm+16	24.9	0	dsm+16	*	0	*	5.399
5	B0011+47	dth78	1.240699038946	11	hlk+04	30.405	13	bkk+16	-15.56	10	sbg+19	1.776
36	J0026+6320	jml+09	0.31835777079	3	sjm+19	245.06	6	sjm+19	-294	2	npn+20	6.619
37	J0030+0451	lzb+00	0.0048654532114961	19	aab+21a	4.332772	0	aab+21a	1.17	8	sbg+19	0.324
38	J0033+57	hrk+08	0.315	0	hrk+08	75.65	9	mss+20	*	0	*	2.251
39	J0033+61	hrk+08	0.912	0	hrk+08	37.7	3	mss+20	*	0	*	1.654
40	J0034-0534	bhl+94	0.0018771818845850	2	aaa+10b	13.76517	4	aaa+10b	-38	17	hmvd18	1.348
96	B0144+59	stwd85	0.19632137543003	16	ywml10	40.111	3	hlk+04	-9.5	5	npn+20	2.128
97	B0148-06	mlt+78	1.464664549334	7	hlk+04	25.66	3	hlk+04	2	4	hl87	25.000
98	J0152+0948	clm+05	2.74664729014	10	clm+05	22.881	12	bkk+16	1.4	2	sbg+19	2.477
99	B0149-16	mlt+78	0.8327416126878	13	hlk+04	11.92577	4	srb+15	+6.6	50	fdr15	0.920
100	J0154+1833	mgf+19	0.0023645697763006	5	mgf+19	19.7978	1	mgf+19	21.6	1	mgf+19	1.622
366	J0818-3232	bjd+06	2.161258926939	15	bjd+06	131.80	7	bjd+06	25.2	50	hmvd18	0.484
367	B0818-13	vl70	1.2381295438682	8	hlk+04	40.938	3	hlk+04	-1.2	4	hl87	1.900
368	J0820-3826	bkl+13	0.1248366735581	5	psj+19	195.50	3	mss+20	+122	6	jsd+21	4.084
369	J0820-3921	bjd+06	1.07356658405	4	bjd+06	179.4	1	bjd+06	126.9	71	hmvd18	3.576
370	B0818-41	mlt+78	0.5454455601	3	lbs+20	113.4	2	antt94	57.7	5	qmlg95	0.571

ATNF Pulsar Catalogue
(Version: 1.66)



- Polarization profiles are usually obtained as a by-product of PTAs due to the crucial role played by polarization calibration for precise timing

arXiv > astro-ph > arXiv:2111.10615

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[Submitted on 20 Nov 2021]

Pulsar Polarization Arrays

Tao Liu, Xuzixiang Lou, Jing Ren

Pulsar timing arrays (PTAs) consisting of widely distributed and well-timed millisecond pulsars can serve as a galactic interferometer to measure gravitational waves. With the same data acquired for PTAs, we propose to develop pulsar polarization arrays (PPAs), to explore astrophysics and fundamental physics. As in the case of PTAs, PPAs are best suited to reveal temporal and spatial correlations at large scales that are hard to mimic by local noise. To demonstrate the physical potential of PPAs, we consider detection of ultralight axion-like dark matter (ALDM), through cosmic birefringence induced by its Chern-Simon coupling. Because of its tiny mass, the ultralight ALDM can be generated as a Bose-Einstein condensate, characterized by a strong wavy nature. Incorporating both temporal and spatial correlations of the signal, we show that PPAs have a potential to probe the Chern-Simon coupling up to $\sim 10^{-14} - 10^{-17}\mathrm{GeV}^{-1}$, with a mass range $\sim 10^{-27} - 10^{-21}\mathrm{eV}$.

Measured polarization angle:

$$\mathrm{PA} = \mathrm{PA}_{\mathrm{source}} + \mathrm{PA}_{\mathrm{instru}} + \mathrm{PA}_{\mathrm{propa}}$$

- **Source**: change of pulsar orientation/ magnetosphere; stochastic variation of single pulse profile (jitter noise)
- **Instrument**: related to PA calibration; radiometer noise
- **Propagation**: Faraday rotation caused by interstellar magnetic field/Earth's ionosphere; new physics effects??

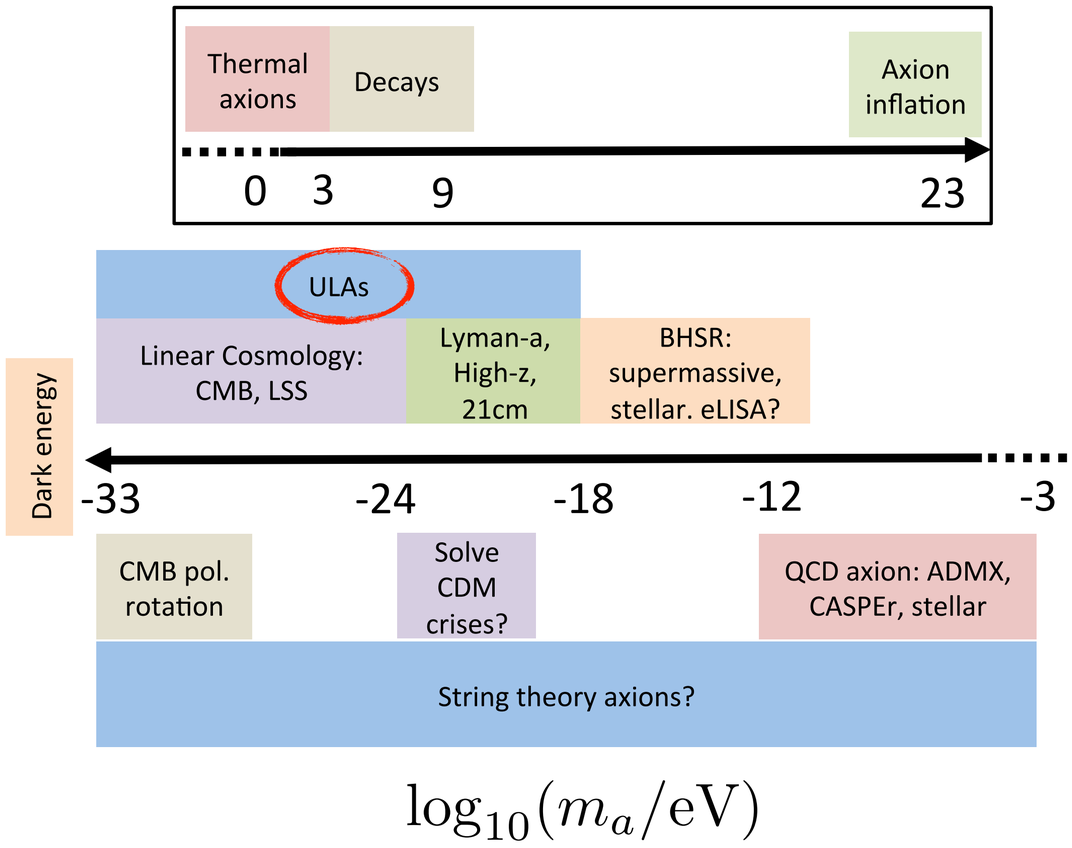
Axion and axion-like particles (ALPs)

- **QCD axion** well motivated to solve the strong CP problem and also serve as an DM candidate; **ALPs** introduced in many BSM scenarios, e.g. string axions.

- **Ultralight ALPs** (m_a<10^{-18}eV) can be generated as a Bose-Einstein condensate from misalignment; behave effectively as a **classical scalar field**

- **Ultralight ALPs may serve as DM or DE during cosmic evolution**. Here we focus on ALDM (e.g. fuzzy DM at m_a~10^{-22}eV, subdominant at m_a<10^{-24}eV)

ALPs landscapes



D. Marsh, Phys. Rept. 643, 1-79 (2016)

Physical properties of ALDM

- **Local ALDM field** made up by a large number of ALP classical fields with uncorrelated random phases Foster, Rodd, Safdi, PRD 97, no.12, 123006 (2018)

density velocity element

$$a(\mathbf{x},t)=\frac{\sqrt{\rho(\mathbf{x})}}{m_a}\sum_d \alpha_d\sqrt{f_{\mathbf{x}}(\mathbf{v}_d)(\Delta v)^3}\cos[\omega_a(t-\mathbf{v}_d\cdot\mathbf{x})+\phi_d]$$

  - **Non-relativistic limit**: $\omega_a \approx m_a$; velocity distribution $f_{\mathbf{x}}(\mathbf{v})$ peaked around $|\mathbf{v}|\sim v_0\sim 10^{-3}c$ (CDM velocity in our galaxy)
  - **Random nature**: random amplitude α_d and phase ϕ_d (follow the Rayleigh and uniform distributions)

- **ALPs effective action**: gravitational interaction, coupling to SM particles…

$$S=\int d^4x\sqrt{-g}\left[\frac{1}{2}\nabla^\mu a\nabla_\mu a-\frac{1}{2}m_a^2a^2+\frac{g_{a\gamma}}{2}aF_{\mu\nu}\tilde{F}^{\mu\nu}+\frac{g_{af}}{2m_f}\nabla_\mu a(\bar{f}\gamma^\mu\gamma_5 f)+\ldots\right]$$

Chern-Simons coupling

ALDM induced cosmic birefringence

When photons propagate in ALDM field *a*, the Chern-Simons coupling *g* corrects the dispersion relations of their two circular polarization modes in opposite way, yielding polarization angle (PA) rotation of linearly polarized photons

$$\omega_{\pm} \simeq k \pm g\left(\frac{\partial a}{\partial t} + \nabla a \cdot \frac{\mathbf{k}}{k}\right) \xrightarrow[\text{relativistic}]{\text{non}-} k \pm g\frac{\partial a}{\partial t}$$

$$\Delta\theta_{p,n} \approx \frac{g}{m_a}\sum_d \alpha_d \Big\{ \underbrace{\sqrt{\rho_p f_p}\cos[m_a(t_n - L_p - \mathbf{v}_d\cdot\mathbf{x}_p) + \phi_d]}_{\text{“Pulsar”}} - \underbrace{\sqrt{\rho_e f_e}\cos\left(m_a t_n + \phi_d\right)}_{\text{“Earth”}} \Big\} (\Delta v)^{\frac{3}{2}} \,.$$

- relies only on field profiles at two endpoints of photon traveling
- quasi-monochromatic oscillation around the frequency $\omega_a \approx m_a$
- no radio frequency dependence (FR increases with wavelength)

A variety of astrophysical light sources proposed before to constrain *g*

[Carroll et al., PRD, 1990; Antonucci, ARAA, 1993; Ivanov et al., JCAP, 2019; Fujita et al., PRL, 2019; Liu et al., PRD, 2020; Caputo et al., PRD, 2019; Chigusa et al., PLB, 2020; Chen et al., PRL, 2020 …]

Yet, spatial correlations of the signal among individual sources not properly considered

ALDM induced signal for PPAs

PA rotation signal on PPAs with many pulsars Liu, Lou, **JR**, 2021, [arXiv: 2111.10615]

- Construct a **signal vector s** from the time series of PA rotation for each pulsar in PPA

$$\mathbf{s} \equiv (\Delta\theta_{1,1}, ..., \Delta\theta_{1,N_1}, ..., \Delta\theta_{\mathcal{N},1}, ..., \Delta\theta_{\mathcal{N},N_{\mathcal{N}}})^T$$

- Signal **s** follows a **multivariable Gaussian distribution** with zero mean and the covariance matrix

$$\Sigma^{(s)}_{p,n;q,m} \approx \frac{g^2}{m_a^2}\left\{\rho_e \cos(m_a\Delta t) + \sqrt{\rho_p\rho_q}\cos[m_a(\Delta t - \Delta L)]\frac{\sin y_{pq}}{y_{pq}} + ...\right\}$$

$y_{pq} = \Delta x / l_c$

$l_c = 1/(m_a v_0)$

(coherence length)

Comparison	SGWB	ALDM (PTAs and PPAs)
Earth-term correlation	quadrupolar correlation	monopolar correlation (universal)
pulsar-term correlation	pulsar-terms suppressed in $L \gg 1/\omega$ limit; **spatial correlations rapidly degrade**	**spatial correlations degrade slower** ($L \gg l_c \gg 1/m_a$); encode DM density dep.; enhanced at galactic center

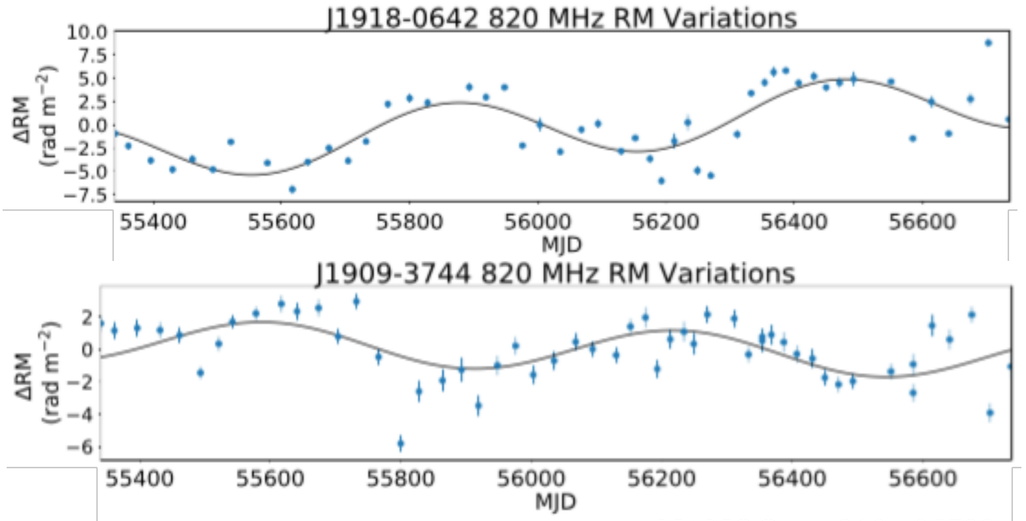
Pulsar correlations

Considering **background n** dominated by white noise, **data d = s + n** follows a **multivariate Gaussian distribution** with zero mean and **covariance matrix** $\mathbf{\Sigma} = \mathbf{\Sigma}^{(s)} + \mathbf{B}$

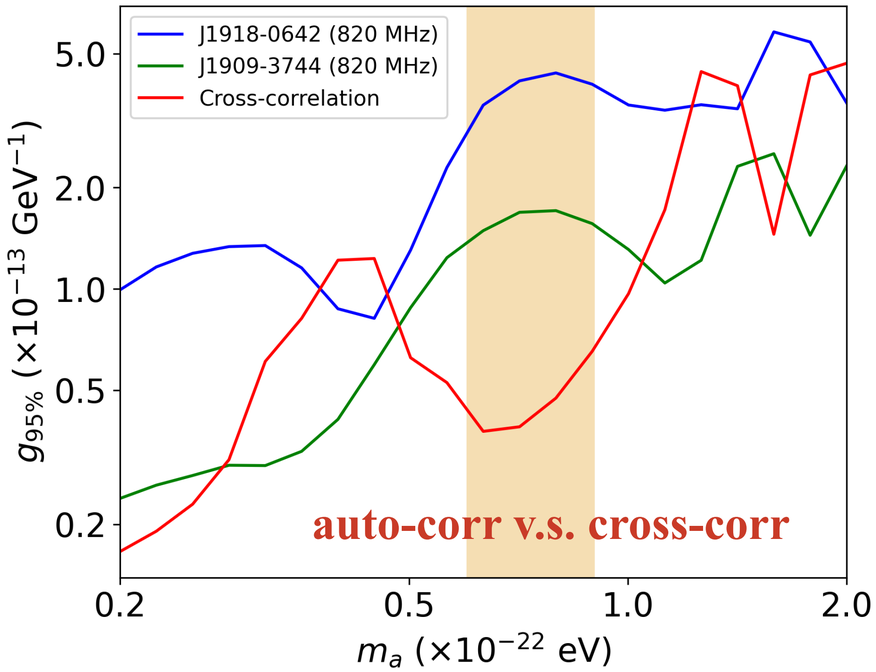
- Likelihood function: $\mathcal{L}(\theta|\mathbf{d}) = \det[2\pi\mathbf{\Sigma}]^{-1/2} \exp\left[-\frac{1}{2}\mathbf{d}^T \cdot \mathbf{\Sigma}^{-1} \cdot \mathbf{d}\right]$
- Exclusion TS on the coupling *g*: $q(g, m_a) \equiv 2[\ln \mathcal{L}(\hat{g}, m_a|\mathbf{d}) - \ln \mathcal{L}(g, m_a|\mathbf{d})]$ ($\hat{g}$ maximizes likelihood)

Both **auto-correlation** of individual pulsars and **cross-correlation** among different pulsars contribute. **Cross-correlation** highly valuable to distinguish spatial correlated and uncorrelated contributions

Detected oscillating PA rotation with period ~1yr



NANOGrav, 2104.05723.



Pulsar correlations

Asimov form of exclusion TS for projection: averaging different data realizations under the background only assumption

$$\langle q \rangle = \mathrm{Tr}\left[\mathbf{B}(\mathbf{\Sigma}^{-1} - \mathbf{B}^{-1})\right] + \ln\det\mathbf{\Sigma}/\ln\det\mathbf{B} + \ldots$$

$$\langle q \rangle \approx \frac{1}{2}\sum_{p,q}\frac{1}{\lambda_p\lambda_q}\mathrm{Tr}\left(\mathbf{\Sigma}^{(s)}_{pq}\mathbf{\Sigma}^{(s)}_{qp}\right)$$ (small signal limit; λ noise variance)

Auto-correlation

$$\mathrm{Tr}\left(\mathbf{\Sigma}^{(s)}_{pp}\mathbf{\Sigma}^{(s)}_{pp}\right) \sim \frac{g^4}{m_a^4}N_p^2\left[\rho_e + \rho_p - 2\sqrt{\rho_e\rho_p}\cos(m_a L_p)\right.$$

# of data points for p-th pulsar

$$\left.\frac{\sin y_{ep}}{y_{ep}}\right]^2. \quad y_{ep} = L_p/l_c$$

- N_p enhancement reflects temporal correlation, insensitive to distribution of sampled points
- Earth-pulsar correlation (3rd) suppressed if $L_\mathrm{p} \gg l_\mathrm{c}$

Cross-correlation

$$\mathrm{Tr}\left(\mathbf{\Sigma}^{(s)}_{pq}\mathbf{\Sigma}^{(s)}_{pq}\right) \sim \frac{g^4}{m_a^4}N_pN_q\left[\rho_e^2 + \rho_p\rho_q\frac{\sin^2 y_{pq}}{y_{pq}^2}\right.$$

$$\left.+2\rho_e\sqrt{\rho_p\rho_q}\cos(m_a\Delta L)\frac{\sin y_{pq}}{y_{pq}} + f(y_{ep}, y_{eq})\right].$$

- Earth-terms cross-correlations (1st) universal
- Pulsar-terms cross-correlations (2nd) dominate for pulsars around galactic center

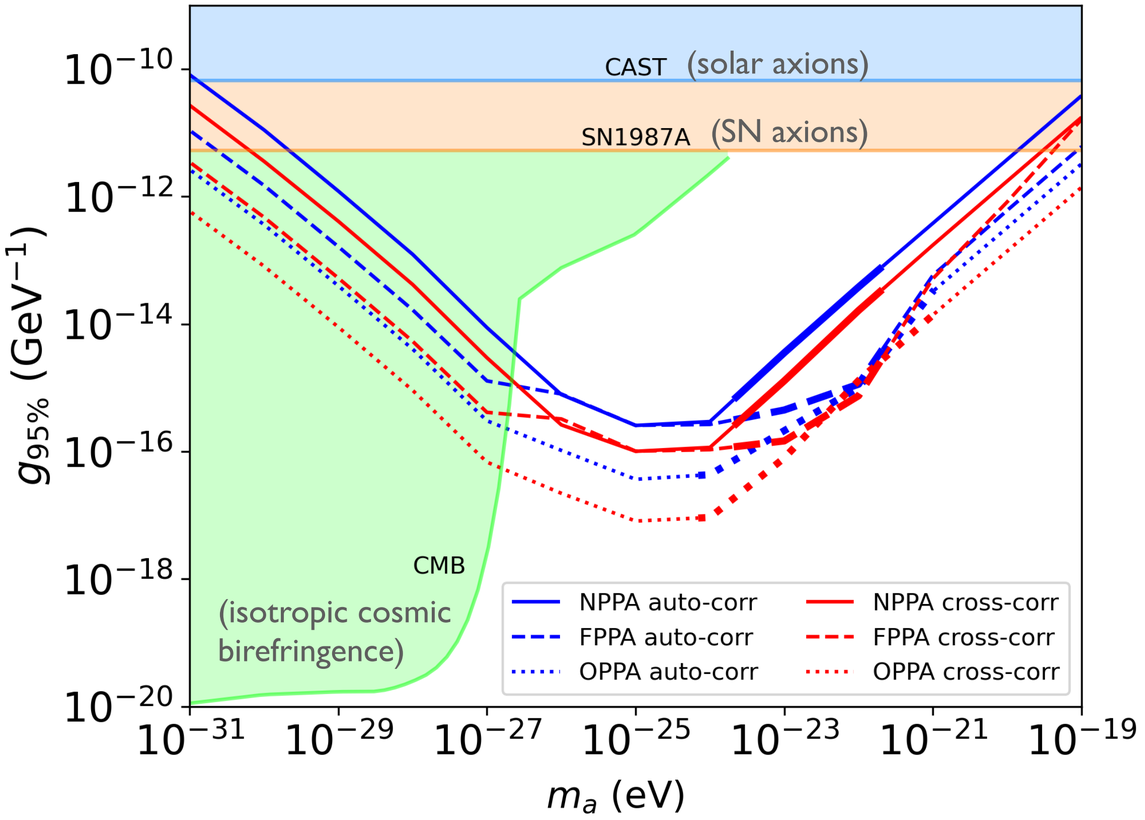
PPA projected sensitivity to ALDM

- Three PPA scenarios (different stage of PTAs)

  NPPA: 100 MSPs around 1kpc (*current PTAs*)
  FPPA: 100 MSPs in galactic bulge (*FAST/SKA era*)
  OPPA: 1000 MSPs following ATNF (*FAST/SKA era*)

- Galactic ALDM density profile: soliton formed by quantum pressure ($r < l_c$, $\rho_c \propto m_a^2$) + NFW ($r > l_c$); CMB constraints on relic abundance imposed

- Pulsar distance uncertainty (~20%) marginalized in constraints estimate



- **Cross-correlation limits** are typically **stronger** than auto-correlation ones
- As m_a decreases, the limit decreases (fuzzy DM), stay flat and increases
- Projected PPA limits form a great complementarity with the existing bounds

Summary and Outlook

- We propose **development of PPAs** with the same data acquired for PTAs. PPAs can be used to **detect ultralight ALDM induced cosmic birefringence with special temporal and spatial correlations**. Projected limits on its Chern-Simons coupling form a great complementarity with existing bounds

- Real data analysis with PPTA polarization data

  Liu, Luu, **JR**, Shu, Xue, Zhao 2022, ongoing…

- Cross-correlation of oscillating signals induced by ALDM on both PPAs and PTAs

  Liu, **JR**, Xu, 2022, ongoing…

- More physical targets for PPAs as a new tool for exploring fundamental physics?

- Synergize PPAs with other observations to further distinguish different scenarios?

Thank You!